

Flavour in the Era of the LHC, CERN, MAY 15-17 2006

Discussion on the SUSY Les Houches Accord 2 project

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(RPV), CPV, (FLV), NMSSM, THEORY ERRORS,
CROSS SECTIONS, GENERAL BSM RESONANCES, ...

Outline

- SLHA1 – brief overview
- SLHA2:

– SUSY CONVENTIONS – HOW TO GENERALISE?

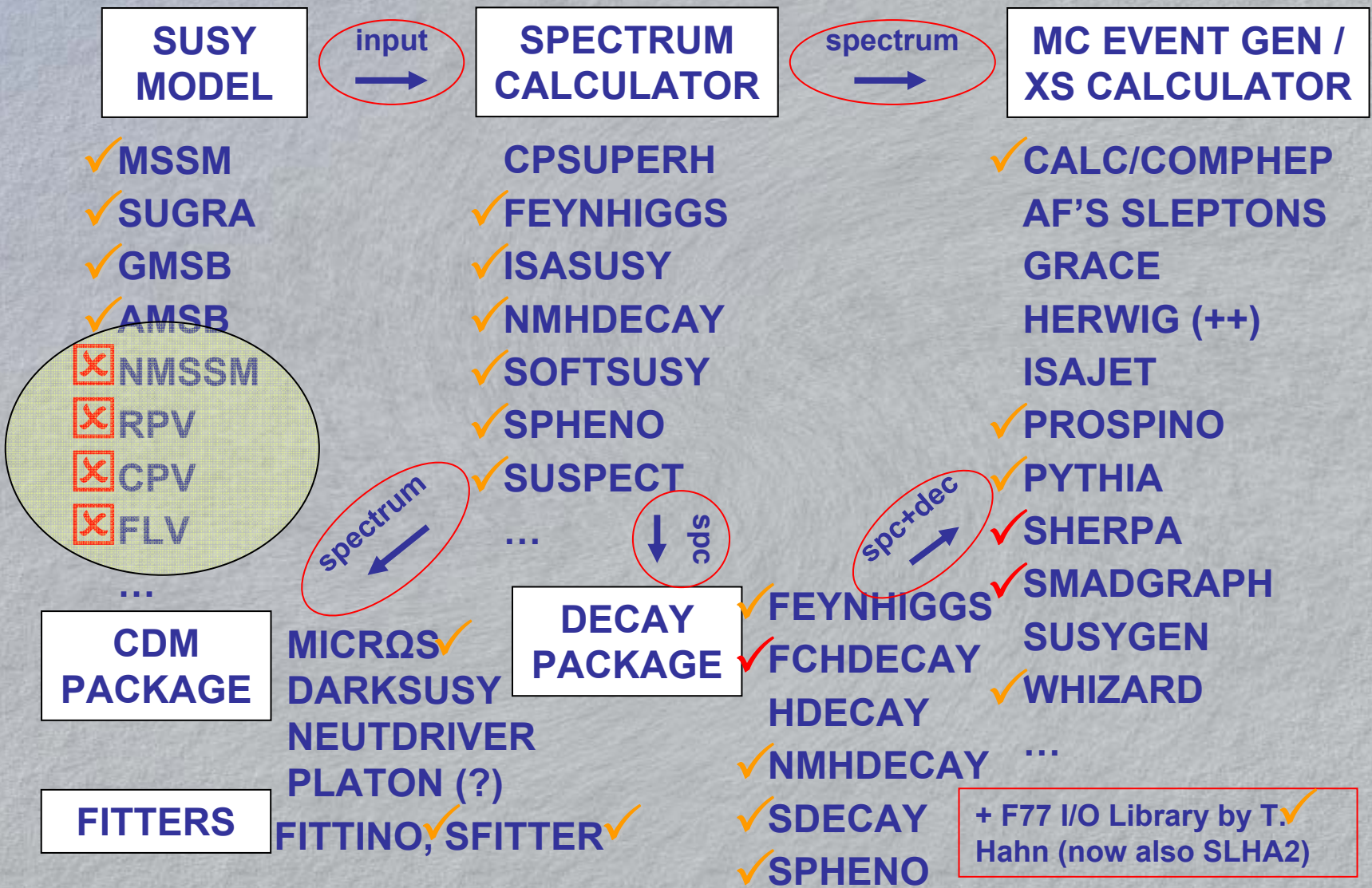
- Model definition
- MSSM w/ **Flavour Violation**
- MSSM w/ **R-parity Violation**
- MSSM w/ **CP Violation (?)**
- NMSSM (?)

– CROSS SECTIONS AND THEORY ERRORS

– OTHER EXTENSIONS

- Well-defined mixing Matrices
- General BSM Resonances - QNUMBERS

SUSY Les Houches Accord v1



Example SLHA Spectrum

```

Block SPINFO # Program information
  1 SOFTSUSY # spectrum calculator
  2 1.9.1 # version number
Block MODSEL # Select model
  1 1 # sugra
Block SMINPUTS # Standard Model inputs
  1 1.27934000e+02 # alpha_em^(-1) (MZ) SM MSbar
  2 1.16637000e-05 # G_Fermi
  3 1.17200000e-01 # alpha_s(MZ)MSbar
  4 9.11876000e+01 # MZ (pole)
  5 4.25000000e+00 # Mb (mb)
  6 1.74300000e+02 # Mtop (pole)
  7 1.77700000e+00 # Mtau (pole)
Block MINPAR # SUSY breaking input parameters
  3 1.00000000e+01 # tanb
  4 1.00000000e+00 # sign(mu)
  1 1.00000000e+02 # m0
  2 2.50000000e+02 # m12
  5 -1.00000000e+02 # A0
# Low energy data in SOFTSUSY: MIXING=-1 TOLERANCE=1.000
# mgut=2.45916471e+16 GeV
Block MASS # Mass spectrum
#PDG code mass particle
  24 8.04191121e+01 # MW
  25 1.10762378e+02 # h0
  35 4.00599584e+02 # H0
  36 4.00231463e+02 # A0
  37 4.08513284e+02 # H+
1000001 5.72700955e+02 # ~d_L
1000002 5.67251814e+02 # ~u_L
1000003 5.72700955e+02 # ~s_L
1000004 5.67251814e+02 # ~c_L
1000005 5.15211952e+02 # ~b_1
1000006 3.95920984e+02 # ~t_1
1000011 2.04276615e+02 # ~e_L
1000012 1.88657729e+02 # ~nu_e_L
1000013 2.04276615e+02 # ~mu_L
1000014 1.88657729e+02 # ~numu_L
1000015 1.36227147e+02 # ~stau_1
1000016 1.87773326e+02 # ~nu_tau_L
1000021 6.07604198e+02 # ~g
1000022 9.72852615e+01 # ~neutralino(1)
1000023 1.80961862e+02 # ~neutralino(2)
1000024 1.80378828e+02 # ~chargino(1)
1000025 -3.64435115e+02 # ~neutralino(3)

Block nmix # neutralino mixing matrix
  1 1 9.86066377e-01 # N_{1,1}
  1 2 -5.46292061e-02 # N_{1,2}
  1 3 1.47649927e-01 # N_{1,3}
  1 4 -5.37424305e-02 # N_{1,4}
  2 1 1.02062420e-01 # N_{2,1}
  2 2 9.42721210e-01 # N_{2,2}
  2 3 -2.74985600e-01 # N_{2,3}
  2 4 1.58880154e-01 # N_{2,4}
  3 1 -6.04575099e-02 # N_{3,1}
  3 2 8.97030908e-02 # N_{3,2}
  3 3 6.95501068e-01 # N_{3,3}
  3 4 7.10335491e-01 # N_{3,4}
  4 1 -1.16624405e-01 # N_{4,1}
  4 2 3.16616055e-01 # N_{4,2}
  4 3 6.47194471e-01 # N_{4,3}
  4 4 -6.83587843e-01 # N_{4,4}
Block Umix # chargino U mixing matrix
  1 1 9.15531658e-01 # U_{1,1}
  1 2 -4.02245924e-01 # U_{1,2}
  2 1 4.02245924e-01 # U_{2,1}
  2 2 9.15531658e-01 # U_{2,2}
Block Vmix # chargino V mixing matrix
  1 1 9.72345994e-01 # V_{1,1}
  1 2 -2.33545003e-01 # V_{1,2}
  2 1 2.33545003e-01 # V_{2,1}
  2 2 9.72345994e-01 # V_{2,2}
Block gauge Q= 4.64231969e+02
  1 3.60968173e-01 # g'(Q)MSSM DRbar
  2 6.46474399e-01 # g(Q)MSSM DRbar
  3 1.09626470e+00 # g3(Q)MSSM DRbar
Block yu Q= 4.64231969e+02
  3 3 8.89731484e-01 # Yt(Q)MSSM DRbar
Block yd Q= 4.64231969e+02
  3 3 1.39732269e-01 # Yb(Q)MSSM DRbar
Block ye Q= 4.64231969e+02
  3 3 1.00914051e-01 # Ytau(Q)MSSM DRbar
Block hmix Q= 4.64231969e+02 # Higgs mixing parameters
  1 3.58339654e+02 # mu(Q)MSSM DRbar
  2 9.75145219e+00 # tan beta(Q)MSSM DRbar
  3 2.44923803e+02 # higgs vev(Q)MSSM DRbar
  4 1.67100152e+05 # mA^2(Q)MSSM DRbar
Block msoft Q=4.64231969e+02 # MSSM DRbar SUSY breaking
  1 1.01439997e+02 # M_1(Q)
  2 1.91579315e+02 # M_2(Q)
  3 5.86586195e+02 # M_3(Q)
  21 3.23914077e+04 # mH1^2(Q)

```

How to Generalise? MSSM

2. Superpotential (at scale Q (normally M_{GUT}) in DRbar)

RPV
CPV
FLV

$$W = \epsilon_{ab} \left[(Y_E)_{ij} H_1^a L_i^b \bar{E}_j + (Y_D)_{ij} H_1^a Q_i^b \bar{D}_j + (Y_U)_{ij} H_2^b Q_i^a \bar{U}_j \right. \\ \left. + \frac{1}{2} \lambda_{ijk} L_i^a L_j^b E_k + \lambda'_{ijk} L_i^a Q_j^b D_k - \epsilon_i L_i^a H_2^b - \mu H_1^a H_2^b \right] + \frac{1}{2} \lambda''_{ijk} U_i D_j D_k$$

3. SUSY Breaking Terms (at scale Q in DRbar)

$$V_3 = \epsilon_{ab} \sum_{ij} \left[(T_E)_{ij} H_1^a \tilde{L}_{iL}^b \tilde{e}_{jR}^* + (T_D)_{ij} H_1^a \tilde{Q}_{iL}^b \tilde{d}_{jR}^* - (T_U)_{ij} H_2^b \tilde{Q}_{iL}^a \tilde{u}_{jR}^* \right. \\ \left. + \frac{1}{2} (T_\lambda)_{ijk} \tilde{L}_{iL}^a \tilde{L}_{jL}^b \tilde{e}_{kR}^* + (T_\lambda')_{ijk} \tilde{L}_i^a \tilde{Q}_j^b \tilde{d}_{kR}^* \right] + \frac{1}{2} (T_{\lambda''})_{ijk} \tilde{u}_{iR}^* \tilde{d}_{jR}^* \tilde{d}_{kR}^* + h.c.$$

$$V_2 = m_{H_1}^2 H_{1a}^* H_1^a + m_{H_2}^2 H_{2a}^* H_2^a + \tilde{Q}_{iLa}^* (m_{\tilde{Q}}^2)_{ij} \tilde{Q}_{jL}^a + \tilde{L}_{iLa}^* (m_{\tilde{L}}^2)_{ij} \tilde{L}_{jL}^a + \\ \tilde{u}_{iR} (m_{\tilde{u}}^2)_{ij} \tilde{u}_{jR}^* + \tilde{d}_{iR} (m_{\tilde{d}}^2)_{ij} \tilde{d}_{jR}^* + \tilde{e}_{iR} (m_{\tilde{e}}^2)_{ij} \tilde{e}_{jR}^* - \epsilon_{ab} (m_{\tilde{H}}^2 H_1^a H_2^b + D_i L_i^a H_2^b$$

$$\mathcal{L}_G = \frac{1}{2} \left(M_1 \tilde{b}\tilde{b} + M_2 \tilde{w}^A \tilde{w}^A + M_3 \tilde{g}^X \tilde{g}^X \right) + h.c. . \quad + m_{LH} L_i^a H_1^b + h.c. .$$

How to Generalise? Model Definition

- Additions to global switches in block **MODSEL**:

3) Choice of particle content

0: MSSM (default)

1: NMSSM



Q: Is one model sufficient for NMSSM, nMSSM, MNMSSM, ...

4) R-parity violation

0: R-parity conserved (default)

1: R-parity violated

In principle the models are qualitatively different, but still ... same particle content?

5) CP violation

0: CP conserved (default)

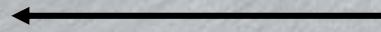
1: CP violated but only by CKM phase

2: CP violated, general phases allowed

6) Flavour violation

0: No (SUSY) flavour violation (default)

1: Flavour violated



Q: Is this adequate?

NB: For SLHA2 we are keeping RPV, CPV, and FLV ~ separate

How to Generalise? FLV

- **SUPER-CKM BASIS:**

- defined as basis in which quark Yukawas, in DRbar, are diagonal
- NB: lepton mixing not treated yet (though see RPV).

- **INPUT**

- **VCKMIN**: V_{CKM} in PDG parametrisation (SM MSbar at M_Z).
- **SMINPUTS**: Include $m_{u,d,s}(2\text{GeV})^{MSbar}$ and $m_c(m_c)^{MSbar}$
- NB: no explicit proposal yet for input of non-diagonal soft SUSY-breaking trilinear and bilinear terms, e.g. **MSQ₂IN**, **MSU₂IN**, **MSD₂IN**?

- **LAGRANGIAN PARAMETERS** (all DRbar at scale **Q**) :

- Yukawas: Super-CKM basis → always diagonal (but same blocks as SLHA1)
- **VCKM** and bilinear SUSY-breaking **MSQ₂**, **MSU₂**, **MSD₂** matrices
- Matrices are symmetric: Give **only** $i < j$ entries of M_{ij} ? ← see next:
(Jaume)
- Or entire matrix $i \leq j$? ($i=j$ already in EXTPAR → inconsistencies?)
- Hermiticity → $MSQ_2(i,j)=MSQ_2(j,i)^*$ → keep these matrices real?

How to Generalise? FLV

- **EW SCALE MIXING:**

- **USQMIX:** 6x6 up-squark mixing in super-CKM basis
- **DSQMIX:** 6x6 down-squark mixing in super-CKM basis

- Problem: which quark is which? Enumeration of mass eigenstates.

- **(from Jaume):** *“Particle codes: we have taken the following convention: squarks ordered in growing mass, the PDG codes for squarks are used.”*

FCHDECAY
fchdecay.googlepages.com

Down squarks: PDG code	Up squarks: PDG Code
1000001 d_1	1000002 u_1
1000003 d_2	1000004 u_2
1000005 d_3	1000006 u_3
2000001 d_4	2000002 u_4
2000003 d_5	2000004 u_5
2000005 d_6	2000006 u_6

Main Issue: PDG (no-mixing limit):	
1000001 d_L	1000002 u_L
1000003 s_L	1000004 c_L
1000005 b_1	1000006 t_1
2000001 d_R	2000002 u_R
2000003 s_R	2000004 c_R
2000005 b_2	2000006 t_2

How to Generalise? RPV

- **INPUT**

- New input blocks for all **RPV superpotential parameters, soft-breaking parameters, and sneutrino vevs** (prefix “**RV**” and suffix “**IN**”)

- **LAGRANGIAN PARAMETERS** (DRbar at scale **Q**) :

- New output blocks for **all RPV parameters** (prefix “**RV**”)

- **POLE MASSES**

- “new” sneutrinos:
- **1000017, 1000018, 1000019**

- **EW SCALE MIXING:**

- **RVNMIX**: 7x7 neutralino/neutrino
- **RVHMIX**: 5x5 CP-even H/sneutrino
- **RVAMIX**: 5x5 CP-odd H/sneutrino
- **RVLMIX**: 8x8 Charged H/slepton
- **RVUMIX, RVVMIX**: 5x5 chargino/lepton

Input block	Output block	data
RVLAMBDAIN	RVLAMBDA	$i j k \lambda_{ijk}$
RVLAMBDA PIN	RVLAMBDA P	$i j k \lambda'_{ijk}$
RVLAMBDA P PIN	RVLAMBDA P P	$i j k \lambda''_{ijk}$
RVKAPPAIN	RVKAPPA	$i \kappa_i$
RVAIN	RVA	$i j k A_{ijk}$
RVAPIN	RVAP	$i j k A'_{ijk}$
RVAPPIN	RVAPP	$i j k A''_{ijk}$
RVDIN	RVD	$i D_i$
RVSNEVIN	RVSNEV	$i v_i$
RVMLH1SQIN	RVMLH1SQ	$i m_{L_i H_1}^2$

example... →

How to Generalise? RPV

- Mixing Example: Charged colour-singlet fermions

Flavour basis

e^+	= e^+ flavour eigenstate
μ^+	= μ^+ -"-
τ^+	= τ^+ -"-
$-i \sim w^+$	= charged wino
$\sim h^+$	= charged higgsino (up-type)

Mass basis (PDG numbers), strictly mass-ordered:

-11 (e^+)	= lightest state (regardless of composition!)
-13 (μ^+)	= 2 nd lightest
-15 (τ^+)	= 3 rd lightest
1000027 (χ_1^+)	= ...
1000037 (χ_2^+)	= heaviest charged colour-singlet fermion

NB: currently using U,V mixing etc for each sector separately and not "Super-MNS" for leptons/Higgses. Need to discuss?

How to Generalise? CPV

- **SIMPLEST WAY**
 - Add prefix “**IM**” to already existing SLHA1 blocks
 - E.g. in input: **IMEXTPAR**; in output: **IMNMIX** etc ...
 - Not completely general, but useful starting point
- **MORE GENERAL**
 - Add prefix “**IM**” to new SLHA2 blocks (supersede SLHA1 if present)
- **EW SCALE MIXING:**
 - **CVHMIX**: 4x4 neutral Higgs (CP-even & CP-odd) mixing
 - **IMCVHMIX**: imaginary parts
 - Charged Higgs mixing (2x2) not yet agreed upon

How to Generalise? NMSSM

Cf. NMHDecay,
Ellwanger, Gunion, Hugonie

2. Superpotential (at scale Q (normally M_{GUT}) in DRbar) **NMSSM**

$$W = W_{\text{MSSM}} + \lambda \epsilon_{ab} S H_1^a H_2^b + \frac{\kappa}{3} S^3 \quad (\text{usually with } \mu_{\text{MSSM}}=0)$$

3. SUSY Breaking Terms (at scale Q in DRbar) **EXTPAR:**

$$V_3 = V_{3,\text{MSSM}} + (\epsilon_{ab} \lambda A_\lambda S H_1^a H_2^b + h.c.) + \frac{\kappa}{3} A_\kappa S^3,$$

$$V_2 = V_{2,\text{MSSM}} + m_S^2 S^2$$

- 61) lambda
- 62) kappa
- 63) A_lambda
- 64) A_kappa
- 65) mu_eff=lambda<S>

4. Physical Spectrum

- 3 H^0 (PDG: 25,35,45), 2 A^0 (PDG: 36, 46), 5 χ^0 (PDG: 1000045)
- Mixing: **NMHMIX** **NMAMIX** **NMNMIX**

See also MicrOMEGAs & CalcHEP
+ Interface to PYTHIA

Cross Sections & Theory Errors

NB: Not included in current LH status report

- **Theory Errors**
 - Introduce (unphysical) input variables corresponding to variations within theoretical uncertainty -> **range of spectra**.
(Similar in spirit to error PDF's)
 - Calculation of observables from spectrum →
+/- errors on computed variables
- **Cross Sections used by fit programs** **Fittino, Sfitter**
 - Templated in SPheno. Collecting experiences now.

These (and more?) to be included in journal writeup

Including (possibility for) well-defined mixing matrices

- In **SLHA1**, exact definition of mixing matrices was “left up to RGE program” (since the only thing we could agree on was not to agree ...)
 - **Read the individual manual**
 - DRbar at some scale m ? ($m^2_{\text{SUSY}} = m_{t1}m_{t2}$, $m = (m_h + m_H)/2$, ...)
 - On-shell ?
 - Etc ...
 - **Not a huge problem**
 - DRbar Lagrangian parameters also given
 - → can always construct desired mixing structure
- **Still**, would be nice to have possibility for exact definition
 - Include option for giving DRbar mixing matrices at scale Q :

e.g. BLOCK NMIX Q=...

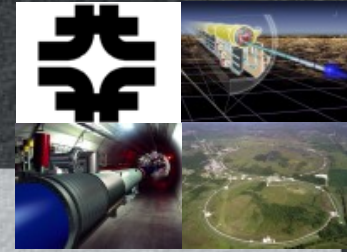
or

BLOCK DRNMIX Q=...

BLOCK NMIXDR Q=...

MC4BSM Workshop

Monte Carlo Tools for Beyond-the-Standard-Model Physics. March 20-21 2006. Fermilab



- **MC4BSM:** first workshop to focus explicitly on tools for non-SUSY BSM:

- Survey what is available: communication + feedback
- Identify promising models and start to fill up the gaps
- Streamlining the process of going from models to events

- **One question that came up:**

- Successive resonance decays of general new physics resonances?
- Can be done with SLHA decay tables, just add basic information about particle
- **→ Proposal for SLHA2. BLOCK QNUMBERS (or PARTICLE?)**

```
BLOCK QNUMBERS 1234567 # new_guy PDG=1234567
  1 0 # 3 times electric charge
  2 2 # number of spin states (2S+1)
  3 1 # colour rep (1: singlet, 3: triplet, 8: octet)
  4 0 # Particle/Antiparticle distinction (0=own anti)
BLOCK MASS # Mass Spectrum
1234567 3.1415926535E+02 # new_guy
DECAY 1234567 1.000000E+00 # new_guy width
1.0000E-00 2 22 22 # Br(new_guy -> gamma gamma)
```

- (→ Already used to interface CalcHEP, NMHDecay, and PYTHIA, for the NMSSM)

Outlook

- ‘Conceptual Design Report’ for SLHA2 in Les Houches BSM Proceedings, hep-ph/0602198 concerns core SLHA2 conventions.
- More extensive writeup to follow in 2006. To discuss:
 - Flavour in the Era of the LHC, CERN, May 15-17, 2006 (flavour)
 - Tools 2006, Annecy, Jun 26-28, 2006
 - MC4LHC, CERN, Jul 17-26, 2006
 - MC4BSM, Gainesville, FL, Winter 06/07
- See also Les Houches BSM tools repository:
<http://www.ippp.dur.ac.uk/montecarlo/BSM>

Work 1

$$W_{MSSM} = \sum_{ab}^2 \mathcal{L} \left((Y_E)_{ij} H_1^a L_i^b \bar{E}_j + (Y_D)_{ij} H_1^a Q_i^b \bar{D}_j + (Y_U)_{ij} H_2^b Q_i^a \bar{U}_j + h.c. \right)$$

$$V_3 = \sum_{ij}^2 \mathcal{L} \left((T_E)_{ij} H_1^a L_i^b \bar{e}_j + (T_D)_{ij} H_1^a Q_i^b \bar{d}_j + (T_U)_{ij} H_2^b Q_i^a \bar{u}_j + h.c. \right)$$

$$V_2 = m_{H_1}^2 H_1^a H_1^a + m_{H_2}^2 H_2^a H_2^a + Q_{iL}^a (m_{Q_{iL}}^2)_{ij} Q_{jL}^a + L_{iL}^a (m_{L_{iL}}^2)_{ij} L_{jL}^a +$$

$$U_{iR} (m_{U_{iR}}^2)_{ij} U_{jR}^a + D_{iR} (m_{D_{iR}}^2)_{ij} D_{jR}^a + E_{iR} (m_{E_{iR}}^2)_{ij} E_{jR}^a + (m_{3ab}^2 H_1^a H_2^b + h.c.) :$$

$$L_G = \frac{1}{2} \left(M_1 \bar{\nu} \nu + M_2 w^A w^A + M_3 g^X g^X + h.c. \right)$$

Work 2

$$W = \int_{ab}^{\mathcal{L}} (Y_E)_{ij} H_1^a L_i^b \dot{E}_j + (Y_D)_{ij} H_1^a Q_i^b \dot{D}_j + (Y_U)_{ij} H_2^b Q_i^a \dot{U}_j \\ + \frac{1}{2} (T_{,ijk}) L_i^a L_j^b E_k + (T_{,0ijk}) L_i^a Q_j^b D_k + (T_{,i2j}) L_i^a H_2^b + (T_{,1H_2}) H_1^a H_2^b + \frac{1}{2} (T_{,ijk}) U_i D_j D_k$$

$$V_3 = \int_{ab}^{\mathcal{L}} (T_E)_{ij} H_1^a L_i^b e_{jR}^{\alpha} + (T_D)_{ij} H_1^a Q_i^b d_{jR}^{\alpha} + (T_U)_{ij} H_2^b Q_i^a u_{jR}^{\alpha} \\ + \frac{1}{2} (T_{,ijk}) L_i^a L_j^b e_{kR}^{\alpha} + (T_{,0ijk}) L_i^a Q_j^b d_{kR}^{\alpha} + \frac{1}{2} (T_{,ijk}) u_{iR}^{\alpha} d_{jR}^{\alpha} d_{kR}^{\alpha} + \text{h.c.}$$

$$V_2 = m_{H_1}^2 H_{1a}^{\alpha} H_1^a + m_{H_2}^2 H_{2a}^{\alpha} H_2^a + Q_{iLa}^{\alpha} (m_Q^2)_{ij} Q_{jL}^a + L_{iLa}^{\alpha} (m_L^2)_{ij} L_{jL}^a + \\ u_{iR}^{\alpha} (m_u^2)_{ij} u_{jR}^{\alpha} + d_{iR}^{\alpha} (m_d^2)_{ij} d_{jR}^{\alpha} + e_{iR}^{\alpha} (m_e^2)_{ij} e_{jR}^{\alpha} + \int_{ab}^{\mathcal{L}} (m_3^2 H_1^a H_2^b + D_i L_i^a H_2^b$$

$$L_G = \frac{1}{2} (M_1 \dot{\phi}^{\alpha} + M_2 \dot{w}^A w^A + M_3 \dot{g}^X g^X + \text{h.c.}) + m_{LH} L_i^a H_1^b + \text{h.c.} :$$

Work 3

$$W = W_{MSSM} + \frac{1}{2} g_{ab}^2 S H_1^a H_2^b + \frac{1}{3} S^3$$

$$V_3 = V_{3;MSSM} + (g_{ab}^2 A, S H_1^a H_2^b + h:c:) + \frac{1}{3} A \cdot S^3;$$

$$V_2 = V_{2;MSSM} + m_S^2 S^2$$

Conclusions

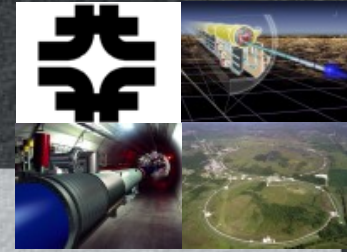
Tough conditions call for good tools! We will be ready for NMSSM, CPV, RPV, FLV, ...



Then all we need is a signal ...

MC4BSM Workshop

Monte Carlo Tools for Beyond-the-Standard-Model Physics. March 20-21 2006. Fermilab



- Many new models of New Physics emerged over last few years:
 - e.g. Extra Dimensions, new technicolor-like models, Higgsless, Little Higgs, gauge and/or matter extensions to MSSM, ...
 - Many of these imply qualitatively new phenomenological signatures
 - The rest imply a possible experimental confusion with existing models
- MSSM has been useful benchmark scenario to test experimental and phenomenological strategies for a long time
 - Now increasing focus on non-MSSM signatures + how we could get confused
 - Many advanced tools exist to study all aspects of MSSM phenomenology in detail (dark matter, electroweak precision, cross sections, decay widths, NLO, spin correlations, event generators, ...) + most use SUSY Les Houches Accord (now being extended to CPV, RPV, FLV, NMSSM)
 - **For non-MSSM BSM much fewer / less sophisticated tools**

The SLHA1 Conventions

1. Experimental boundary conditions

- “SM” gauge couplings and Yukawas (measured)
- → “MSSM” couplings and Yukawas (not the same, since different field content → different quantum corrections)

2. Superpotential (at scale Q (normally M_{GUT}) in DRbar)

$$^1 W_{MSSM} = \epsilon_{ab} [(Y_E)_{ij} H_1^a L_i^b \bar{E}_j + (Y_D)_{ij} H_1^a Q_i^b \bar{D}_j + (Y_U)_{ij} H_2^b Q_i^a \bar{U}_j - \mu H_1^a H_2^b]$$

3. SUSY Breaking Terms (at scale Q in DRbar)

$$\begin{aligned}
 \mathbf{A} \quad V_3 &= \epsilon_{ab} \sum_{ij} [(T_E)_{ij} H_1^a \tilde{L}_{iL}^b \tilde{e}_{jR}^* + (T_D)_{ij} H_1^a \tilde{Q}_{iL}^b \tilde{d}_{jR}^* + (T_U)_{ij} H_2^b \tilde{Q}_{iL}^a \tilde{u}_{jR}^*] + h.c. , \\
 \mathbf{m}_0 \quad V_2 &= m_{H_1}^2 H_{1a}^* H_1^a + m_{H_2}^2 H_{2a}^* H_2^a + \tilde{Q}_{iLa}^* (m_{\tilde{Q}}^2)_{ij} \tilde{Q}_{jL}^a + \tilde{L}_{iLa}^* (m_{\tilde{L}}^2)_{ij} \tilde{L}_{jL}^a + \\
 \mathbf{m}_A \quad &\tilde{u}_{iR} (m_{\tilde{u}}^2)_{ij} \tilde{u}_{jR}^* + \tilde{d}_{iR} (m_{\tilde{d}}^2)_{ij} \tilde{d}_{jR}^* + \tilde{e}_{iR} (m_{\tilde{e}}^2)_{ij} \tilde{e}_{jR}^* - (m_3^2 \epsilon_{ab} H_1^a H_2^b + h.c.) . \\
 \mathbf{M} \quad \frac{1}{2} \mathcal{L}_G &= \frac{1}{2} (M_1 \tilde{b}\tilde{b} + M_2 \tilde{w}^A \tilde{w}^A + M_3 \tilde{g}^X \tilde{g}^X) + h.c. .
 \end{aligned}$$