

Looking for Wtb anomalous couplings in top pair decays

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Summary

- 1 Introduction
- 2 Top decays and W helicity
- 3 Top pair decays and $t\bar{t}$ spin correlations
- 4 Top pair decays and CP violation

Introduction

Reminder

- The Higgs boson may exist or not (most people hope it)
- Supersymmetry may exist or not (some people hope it)
- New fermions may exist or not (fewer people hope it)
- The top quark **definitely exists** (we are happy for it)
and we must study its properties at LHC

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Top quark properties

- Mass  Possibly new physics influence
Measured at Tevatron
But no standard theory for masses
- Couplings  Sensitive to new physics corrections
Predicted in the SM
May be measured / bounded
- Spin  Testable in top production and decay

Probing top couplings

- Wtb vertex 
 [top decays $t \rightarrow W^+b$ [many authors]
 single top LHC [Boos et al., EPJC '99]
- $Ztt, \gamma tt$ 
 [$t\bar{t}Z, t\bar{t}\gamma$ at LHC [Baur et al., PRD '05,'06]
 $t\bar{t}$ at ILC
- g_{tt} 
 [$t\bar{t}$ at LHC [Cheung, PRD '96]
 $t\bar{t}g$ at ILC [Rizzo, PRD '94]
- $Ztq, \gamma tq, gtq$  FCN production and decay [many authors]

General Wtb vertex

$$\begin{aligned} \mathcal{L} = & -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu (V_L P_L + V_R P_R) t W_\mu^- \\ & -\frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) t W_\mu^- + \text{h.c.} \end{aligned}$$

(Additional terms p^μ , etc. rewritten with Gordon identities)

V_R, g_L, g_R zero at tree level

$V_L \simeq 1$, normalised to unity

V_R, g_L, g_R expected to be (very) small

Top decays and W helicity

Equivalent descriptions of $t \rightarrow W^+ b \rightarrow \ell^+ \nu b$

- ℓ angular distribution \leftrightarrow angular asymmetries
in W rest frame, determined by W^+ helicity fractions
- ℓ energy distribution \leftrightarrow energy asymmetries
in t rest frame, determined by W^+ helicity fractions and W boost

ℓ angular distribution in W rest frame

Assume t , W on shell

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_\ell^*} = \frac{3}{8} (1 + \cos \theta_\ell^*)^2 F_R + \frac{3}{8} (1 - \cos \theta_\ell^*)^2 F_L + \frac{3}{4} \sin^2 \theta_\ell^* F_0$$

θ_ℓ^* angle between $\left[\begin{array}{l} \ell \text{ momentum in } W \text{ rest frame} \\ W \text{ momentum in } t \text{ rest frame} \end{array} \right.$

$\theta_\ell^* = \pi - \theta_{\ell b}$ $\theta_{\ell b}$ angle between ℓ and b in W rest frame

$$\Gamma(t \rightarrow W^+ b) = \Gamma_R + \Gamma_L + \Gamma_0 \quad F_i = \Gamma_i / \Gamma$$

$F_i \rightarrow$ determine ℓ distribution

W helicity fractions

$(x_W = M_W/m_t, \quad x_b = m_b/m_t, \quad |\vec{q}| = W \text{ momentum})$

$$\begin{aligned}
 \Gamma_0 &= \frac{g^2 |\vec{q}|}{32\pi} \left\{ \frac{m_t^2}{M_W^2} \left[|V_L|^2 + |V_R|^2 \right] \left(1 - x_W^2 - 2x_b^2 - x_W^2 x_b^2 + x_b^4 \right) - 4x_b \operatorname{Re} V_L V_R^* \right. \\
 &\quad + \left[|g_L|^2 + |g_R|^2 \right] \left(1 - x_W^2 + x_b^2 \right) - 4x_b \operatorname{Re} g_L g_R^* \\
 &\quad \left. - 2 \frac{m_t}{M_W} \operatorname{Re} [V_L g_R^* + V_R g_L^*] \left(1 - x_W^2 - x_b^2 \right) + 2 \frac{m_t}{M_W} x_b \operatorname{Re} [V_L g_L^* + V_R g_R^*] \left(1 + x_W^2 - x_b^2 \right) \right\} \\
 \Gamma_{R,L} &= \frac{g^2 |\vec{q}|}{32\pi} \left\{ \left[|V_L|^2 + |V_R|^2 \right] \left(1 - x_W^2 + x_b^2 \right) - 4x_b \operatorname{Re} V_L V_R^* \right. \\
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 &\quad \pm \frac{g^2}{64\pi} \frac{m_t^3}{M_W^2} \left\{ -x_W^2 \left[|V_L|^2 - |V_R|^2 \right] + \left[|g_L|^2 - |g_R|^2 \right] \left(1 - x_b^2 \right) \right. \\
 &\quad \left. + 2x_W \operatorname{Re} [V_L g_R^* - V_R g_L^*] + 2x_W x_b \operatorname{Re} [V_L g_L^* - V_R g_R^*] \right\} \\
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 \end{aligned}$$

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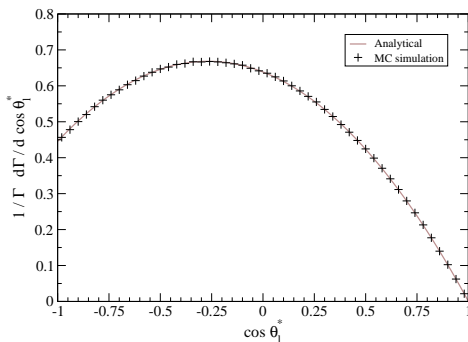
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 \end{aligned}$$

Influence of finite width corrections

But ... is this a good approximation? **Yes!**



Finite width corrections **do not** affect angular distribution

Equivalent parameter sets

Helicity fractions

$$F_i = \Gamma_i / \Gamma$$

$$F_R + F_L + F_0 = 1$$

$$\rho_{R,L} = F_{R,L} / F_0$$

Helicity ratios

$$\rho_{R,L} \equiv \Gamma_{R,L} / \Gamma_0$$

independent quantities

$$F_0 = (1 + \rho_R + \rho_L)^{-1}$$

$$F_{R,L} = \rho_{R,L} (1 + \rho_R + \rho_L)^{-1}$$

They can be obtained from a fit to ℓ distribution

They are sensitive to anomalous couplings

Which one is better? See experimental precision

ℓ angular asymmetries in W rest frame

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta_\ell^*} = \frac{3}{8}(1 + \cos\theta_\ell^*)^2 F_R + \frac{3}{8}(1 - \cos\theta_\ell^*)^2 F_L + \frac{3}{4}\sin^2\theta_\ell^* F_0$$

Take $t \in [-1, 1]$ fixed and define asymmetries

$$A_t = \frac{N(\cos\theta_\ell^* > t) - N(\cos\theta_\ell^* < t)}{N(\cos\theta_\ell^* > t) + N(\cos\theta_\ell^* < t)}$$

$t = 0$	\rightarrow	$A_{\text{FB}} = \frac{3}{4}(F_R - F_L)$	}	Determine F_i without fits
$t = -(2^{2/3} - 1)$	\rightarrow	$A_+ = 3\beta[F_0 + (1 + \beta)F_R]$		
$t = (2^{2/3} - 1)$	\rightarrow	$A_- = -3\beta[F_0 + (1 + \beta)F_L]$ $(\beta \equiv 2^{1/3} - 1)$		

Asymmetries depend on anomalous couplings ...

▶ See

Better or worse? See experimental precision

ℓ energy in t rest frame

Related to $\cos \theta_\ell^*$ by boost

$$E_\ell = \frac{1}{2}(E_W + |\vec{q}| \cos \theta_\ell^*) \quad E_W, |\vec{q}| \text{ constants}$$

$$\frac{1}{\Gamma} \frac{d\Gamma}{dE_\ell} = \frac{1}{(E_{\max} - E_{\min})^3} \left[3(E_\ell - E_{\min})^2 F_R + 3(E_{\max} - E_\ell)^2 F_L \right. \\ \left. + 6(E_{\max} - E_\ell)(E_\ell - E_{\min}) F_0 \right]$$

with $E_{\max} = (E_W + |\vec{q}|)/2$, $E_{\min} = (E_W - |\vec{q}|)/2$

Descriptions equivalent but larger errors for E_ℓ

Top pair decays and $t\bar{t}$ spin correlations

Top decay: distributions in t rest frame

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_X} = \frac{1}{2} (1 + \alpha_X \cos \theta_X) \quad X = \ell, \nu, b, W^+, q, \bar{q}'$$

θ_X angle between X momentum and **top spin**

SM tree level (no anomalous couplings)


$$\alpha_{\ell^+} = \alpha_{\bar{q}'} = 1 \quad \alpha_{\nu} = \alpha_q = -0.31 \quad \alpha_{W^+} = -\alpha_b = 0.41$$



Information on **anomalous couplings** and t **polarisation**

Antitop: $\alpha_{\bar{X}} = -\alpha_X$ if CP conserved

Top quarks produced (almost) unpolarised in $gg, q\bar{q} \rightarrow t\bar{t}$

 compare distribution of $\begin{cases} X \text{ from } t \text{ decay} \\ \bar{X}' \text{ from } \bar{t} \text{ decay} \end{cases}$

Double distribution in helicity basis:

$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_X d \cos \theta_{\bar{X}'}} = \frac{1}{4} (1 + C \alpha_X \alpha_{\bar{X}'} \cos \theta_X \cos \theta_{\bar{X}'})$$

$$C \equiv \frac{\sigma(t_R \bar{t}_R) + \sigma(t_L \bar{t}_L) - \sigma(t_R \bar{t}_L) - \sigma(t_L \bar{t}_R)}{\sigma(t_R \bar{t}_R) + \sigma(t_L \bar{t}_L) + \sigma(t_R \bar{t}_L) + \sigma(t_L \bar{t}_R)}$$

$$\simeq 0.31 \quad (\text{SM tree-level})$$

$$\text{CP: } \sigma(t_R \bar{t}_R) = \sigma(t_L \bar{t}_L) \quad \text{P: } \sigma(t_R \bar{t}_L) = \sigma(t_L \bar{t}_R)$$

Opening angle distribution:

$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \varphi_{X\bar{X}'}} = \frac{1}{2} (1 + D \alpha_X \alpha_{\bar{X}'} \cos \varphi_{X\bar{X}'})$$

$\varphi_{X\bar{X}'}$ angle between $\left[\begin{array}{l} \mathbf{X} \text{ momentum in } t \text{ rest frame} \\ \mathbf{\bar{X}'} \text{ momentum in } \bar{t} \text{ rest frame} \end{array} \right.$

$D \simeq 0.217$ (SM tree-level)

Define asymmetries

$$\begin{aligned}
 A_{X\bar{X}'} &\equiv \frac{N(\cos \theta_X \cos \theta_{\bar{X}'} > 0) - N(\cos \theta_X \cos \theta_{\bar{X}'} < 0)}{N(\cos \theta_X \cos \theta_{\bar{X}'} > 0) + N(\cos \theta_X \cos \theta_{\bar{X}'} < 0)} \\
 &= \frac{1}{4} C \alpha_X \alpha_{\bar{X}'} \\
 \tilde{A}_{X\bar{X}'} &\equiv \frac{N(\cos \varphi_{X\bar{X}'} > 0) - N(\cos \varphi_{X\bar{X}'} < 0)}{N(\cos \varphi_{X\bar{X}'} > 0) + N(\cos \varphi_{X\bar{X}'} < 0)} \\
 &= \frac{1}{2} D \alpha_X \alpha_{\bar{X}'}
 \end{aligned}$$

Sensitive to new physics:

○ in **production** (C, D)

[Bernreuther et al., PRD '98]

[Cheung, PRD '97]

○ in **decay** ($\alpha_X, \alpha_{\bar{X}'}$)

▶ See

Measurement of spin correlation parameters

Spin asymmetries less sensitive to anomalous couplings

▶ See

Use expected precisions
to constrain uncertainty

[Hubaut et al., EPJC '05]

[JAAS & Coimbra group, in prep.]

$$A_{\ell\ell'} \rightarrow C = 0.310 \pm 0.024 \text{ (exp)} \begin{matrix} +2 \times 10^{-5} \\ -0.0003 \end{matrix} (\delta g_R) \begin{matrix} +2 \times 10^{-5} \\ -4 \times 10^{-6} \end{matrix} (\delta g_L) \begin{matrix} +0 \\ -0.0062 \end{matrix} (\delta V_R)$$

$$A_{\ell j} \rightarrow C = 0.310 \pm 0.045 \text{ (exp)} \begin{matrix} +0.0005 \\ -0.0007 \end{matrix} (\delta g_R) \begin{matrix} +0.0002 \\ -0.0009 \end{matrix} (\delta g_L) \begin{matrix} +0.0001 \\ -0.0095 \end{matrix} (\delta V_R)$$

$$\tilde{A}_{\ell\ell'} \rightarrow D = 0.217 \pm 0.011 \text{ (exp)} \begin{matrix} +4 \times 10^{-6} \\ -0.0002 \end{matrix} (\delta g_R) \begin{matrix} +1 \times 10^{-5} \\ -2 \times 10^{-6} \end{matrix} (\delta g_L) \begin{matrix} +0 \\ -0.0042 \end{matrix} (\delta V_R)$$

$$\tilde{A}_{\ell j} \rightarrow D = 0.217 \pm 0.024 \text{ (exp)} \begin{matrix} +8 \times 10^{-5} \\ -0.0003 \end{matrix} (\delta g_R) \begin{matrix} +0.0001 \\ -0.0006 \end{matrix} (\delta g_L) \begin{matrix} +7 \times 10^{-5} \\ -0.0066 \end{matrix} (\delta V_R)$$

Top pair decays and CP violation

Until now we have assumed real V_R, g_L, g_R

... but this may not be the full story ...

Helicity fractions depend on phases through interference terms

More important for g_R  larger phase effects

▶ See

$g_R = \pm 0.055$ gives 3σ effect, $g_R = \pm 0.055i$ gives $\simeq 0.3\sigma$

Spin correlation asymmetries do not help

▶ See

Can CP violating asymmetries help? Perhaps ...

CP violation in top decays

CP-violating asymmetry

[Bernreuther et al., PLB '93]

$$T_2 = (\vec{p}_b - \vec{p}_{\bar{b}}) \cdot (\vec{p}_{\ell^+} \times \vec{p}_{\ell^-})$$

(for dilepton channel only)

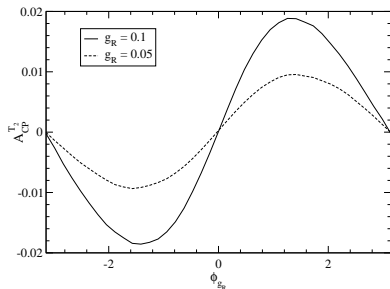
$$\text{👉 } A_{CP}^{T_2} = \frac{N(T_2 > 0) - N(T_2 < 0)}{N(T_2 > 0) + N(T_2 < 0)}$$

Momenta measured $\left[\begin{array}{ll} \text{in } t, \bar{t} \text{ rest frames} & \text{(larger } A) \\ \text{in laboratory frame} & \text{(smaller } A) \end{array} \right.$

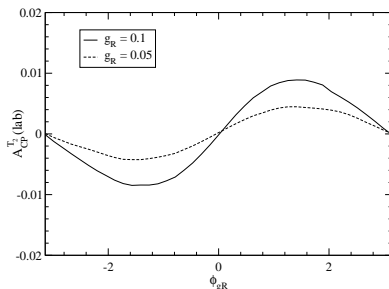
Sensitive to g_R but not to V_R and g_L

CP violation in top decays

t, \bar{t} rest frames



laboratory



Measurable?

Other asymmetries, e.g. based on products

$$T_1 = \hat{e} \cdot (\vec{p}_{\ell^+} - \vec{p}_{\ell^-}) (\vec{p}_{\ell^+} \times \vec{p}_{\ell^-}) \cdot \hat{e}$$

$$T_3 = (\vec{p}_t - \vec{p}_{\bar{t}}) \cdot (\vec{p}_{\ell^+} \times \vec{p}_{\ell^-})$$

$$\Delta_1 = E_{\ell^+} - E_{\ell^-}$$

$$\Delta_2 = \vec{p}_{\bar{t}} \cdot \vec{p}_{\ell^+} - \vec{p}_t \cdot \vec{p}_{\ell^-}$$

$$\Delta_3 = \cos \theta_{\ell^+} - \cos \theta_{\ell^-}$$

Insensitive to CP-violating g_R, g_L, V_R



Test CP violation in production

[Schmidt, Peskin, PRL '92]

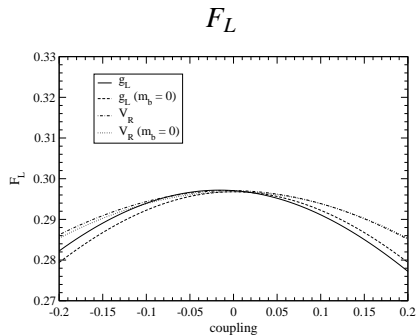
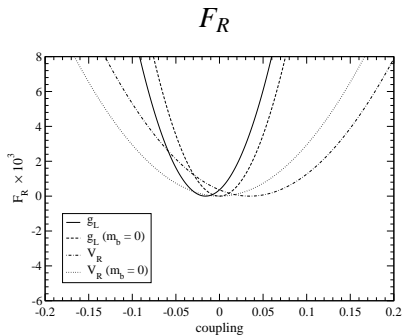
[Bernreuther et al., PLB '93]

[Khater, Osland, NPB '03]

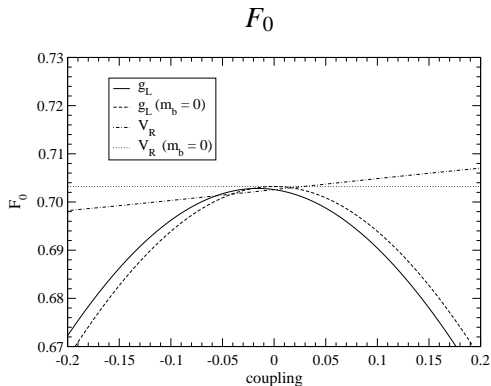
Summary

- Many ways to study Wtb vertex, some better than others
 - 👉 João's talk
- Constraining the Wtb vertex as far as possible can help disentangle new physics in production
(spin correlations, CP violation)
- There are lots of work still to do ...

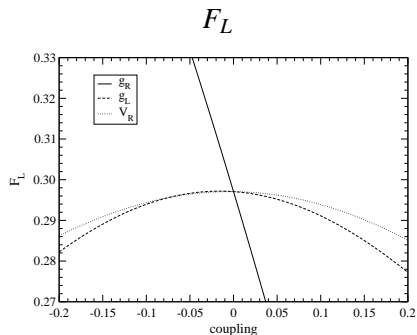
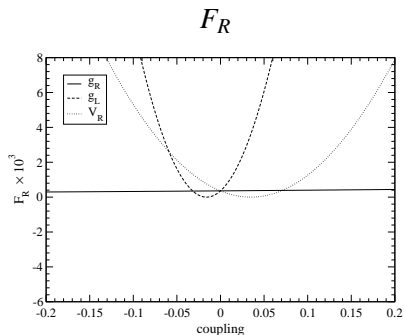
Effect of m_b in helicity fractions


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Effect of m_b in helicity fractions

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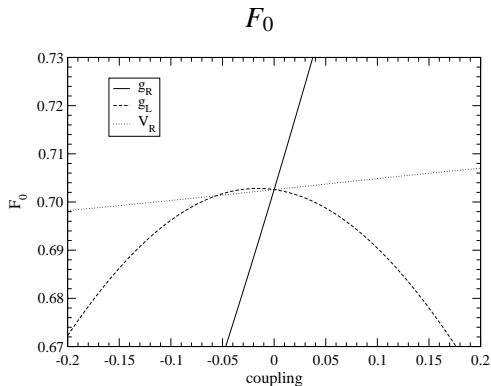
Dependence of F_i on anomalous couplings



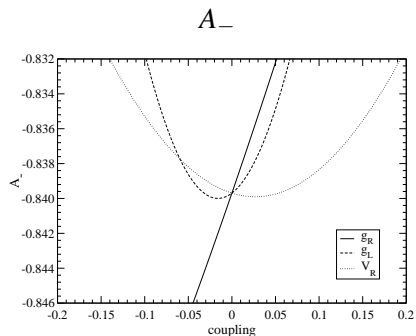
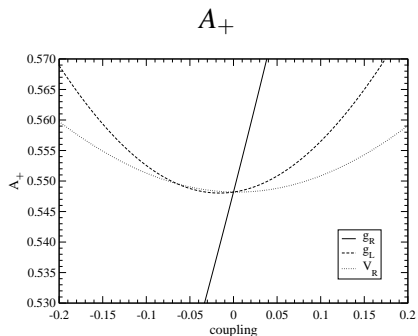
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Dependence of F_i on anomalous couplings

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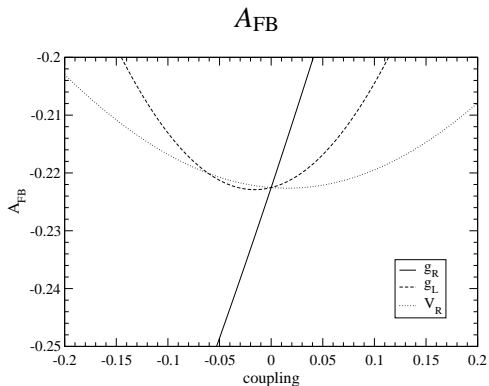
Dependence of asymmetries on anomalous couplings



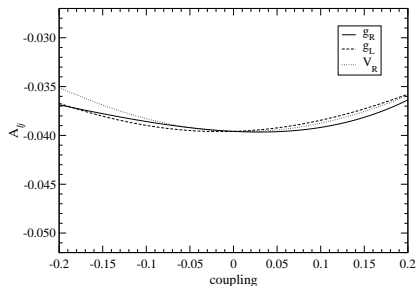
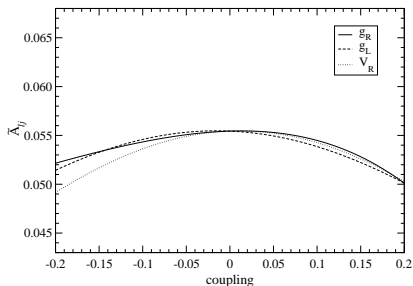
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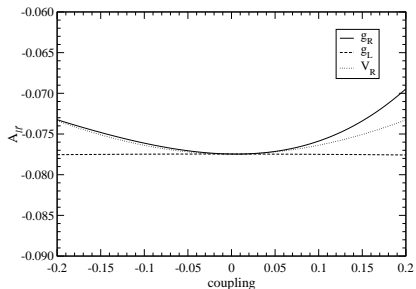
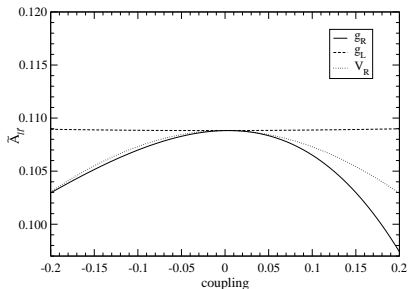
Dependence of asymmetries on anomalous couplings

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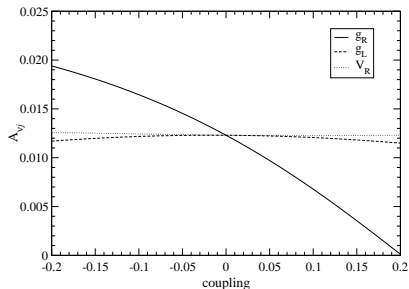
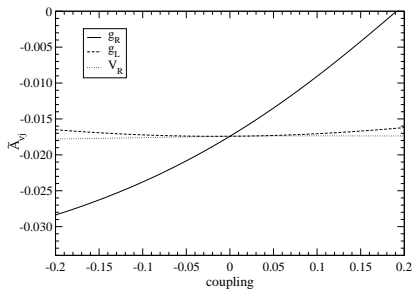
Dependence of spin asymmetries on anomalous couplings

 A_{lj}

 \tilde{A}_{lj}

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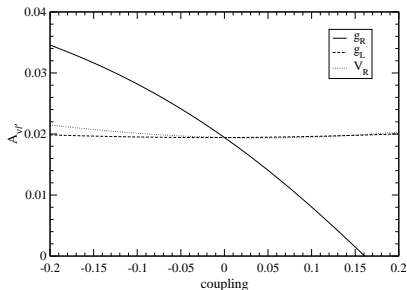
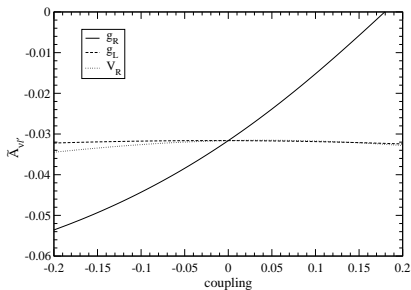
Dependence of spin asymmetries on anomalous couplings

 $A_{\ell\ell'}$

 $\tilde{A}_{\ell\ell'}$

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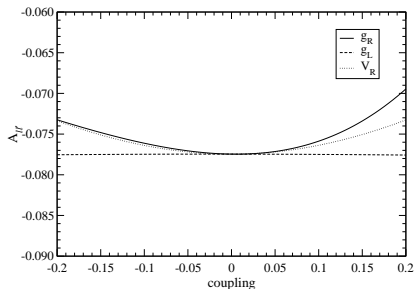
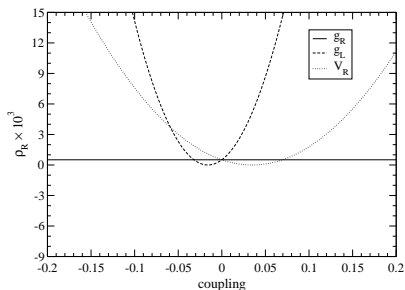
Dependence of spin asymmetries on anomalous couplings

 $A_{\nu j}$

 $\tilde{A}_{\nu j}$

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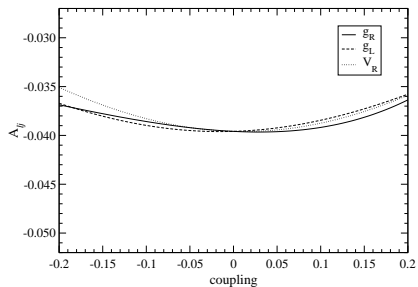
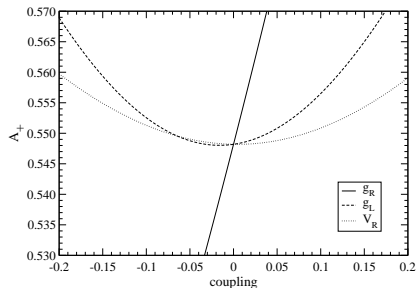
Dependence of spin asymmetries on anomalous couplings

 $A_{\nu\ell'}$

 $\tilde{A}_{\nu\ell'}$

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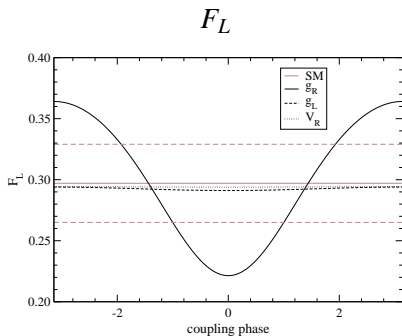
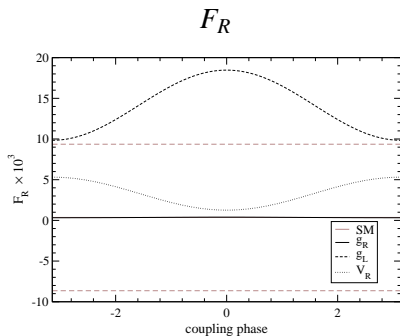
Spin asymmetries: comparison

 $A_{\ell\ell'}$

 ρ_R

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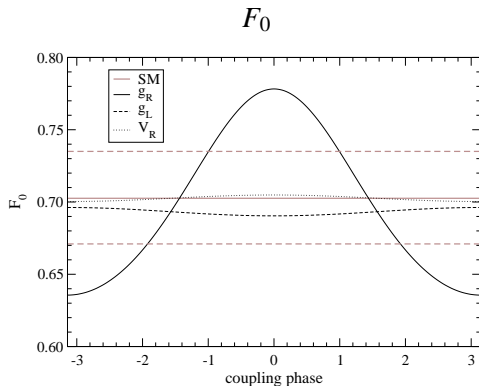
Spin asymmetries: comparison

 A_{lj}

 A_+

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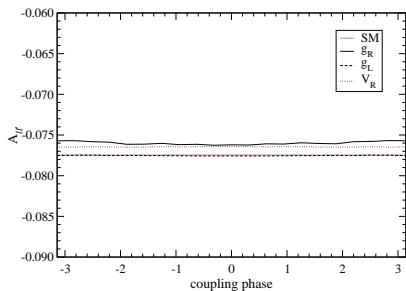
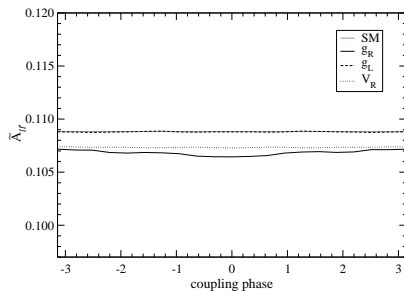
Effect of phases in helicity fractions


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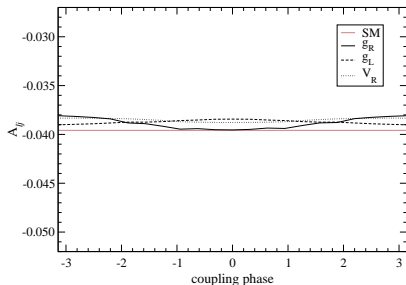
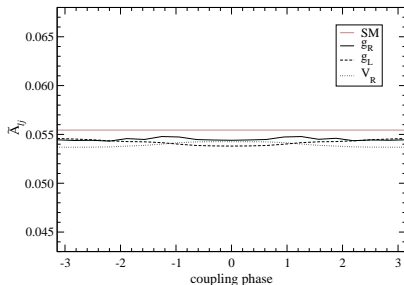
Effect of phases in helicity fractions

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Effect of phases in spin asymmetries

 $A_{\ell\ell'}$

 $\tilde{A}_{\ell\ell'}$

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Effect of phases in spin asymmetries

 A_{lj}

 \tilde{A}_{lj}

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