



Tests of lepton universality with τ decays

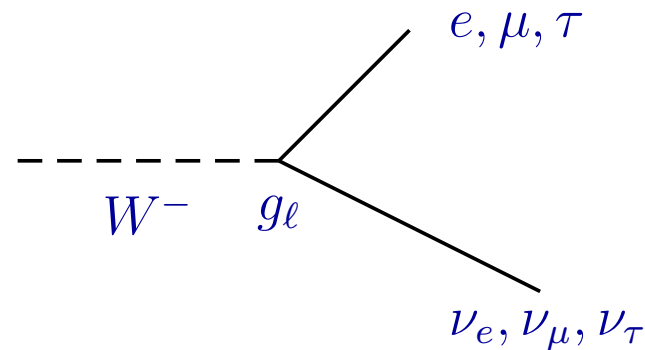
Olga Igonkina

University of Oregon

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- Motivation
- Measurement of τ mass by Belle
- Measurement of τ lifetime by *BABAR*
- Search for CPT violation
- Test of lepton universality

Lepton universality $g_e = g_\mu = g_\tau$



$$\Gamma(\ell_i \rightarrow \ell_f \nu \nu) = \frac{g_i^2 g_f^2}{192\pi^3} \frac{m_i^5}{32M_W^4} C_{if}^{rad}$$

$$C_{if}^{rad} = F\left(\frac{m_f^2}{m_i^2}\right) r_{EW} r_\gamma,$$
$$C_{\mu e}^{rad} = 0.9956, C_{\tau e}^{rad} = 0.9960 \text{ and } C_{\tau \mu}^{rad} = 0.9687.$$

Lepton universality from τ decays



Leptonic decays $\tau \rightarrow \ell \nu \nu$

$$\left(\frac{g_e}{g_\mu}\right)^2 = \frac{\mathcal{B}(\tau \rightarrow e \nu \nu) C_{\tau\mu}^{\text{rad}}}{\mathcal{B}(\tau \rightarrow \mu \nu \nu) C_{\tau e}^{\text{rad}}}$$

$$\left(\frac{g_\mu}{g_\tau}\right)^2 = \frac{C_{\tau e}^{\text{rad}}}{C_{\mu e}^{\text{rad}}} \frac{\tau_\tau}{\tau_\mu} \left(\frac{m_\tau}{m_\mu}\right)^5 \frac{1}{\mathcal{B}(\tau \rightarrow e \nu \nu)}$$

Semileptonic decays $\tau \rightarrow h \nu$

$$\left(\frac{g_\mu}{g_\tau}\right)^2 = \frac{1}{2} \left(\frac{m_\tau}{m_\mu}\right)^2 \frac{H_\pi + H_K}{\mathcal{B}(\tau \rightarrow \pi \nu) + \mathcal{B}(\tau \rightarrow K \nu)},$$

$$H_h = \left(\frac{\tau_\tau}{\tau_h}\right) \left(\frac{m_\tau^2 - m_h^2}{m_h^2 - m_\mu^2}\right)^2 \mathcal{B}(h \rightarrow \mu \nu) (1 + \mathcal{O}_h^{\text{rad}})$$

Experimental ingredients in the calculations



- $m_{\tau}^{Belle} = (1776.71 \pm 0.25_{stat} \pm 0.62_{sys})$ MeV - preliminary measurement by Belle (hep-ex/0511038)
Averaged with PDG is $m_{\tau} = (1776.95 \pm 0.26)$ MeV
- $\tau_{\tau}^{Babar} = (289.40 \pm 0.91_{stat} \pm 0.90_{sys})$ fs - preliminary measurement by BABAR (NPPS144(2005)105);
Averaged with PDG is $\tau_{\tau} = (290.1 \pm 0.83)$ fs.
- leptonic and semileptonic τ decays - PDG-2002 values (LEP and CLEO measurements) - no updates from B -factories and none is expected soon (may be except $\tau \rightarrow K\nu$).
 - $\mathcal{B}(\tau \rightarrow e\nu\nu) \quad (17.84 \pm 0.06)\%$
 - $\mathcal{B}(\tau \rightarrow \mu\nu\nu) \quad (17.36 \pm 0.06)\%$
 - $\mathcal{B}(\tau \rightarrow h\nu) \quad (11.75 \pm 0.11)\%$

hep-ex/0511038, Belle Preliminary, $\mathcal{L} = 253 \text{ fb}^{-1}$

Pseudomass technique :

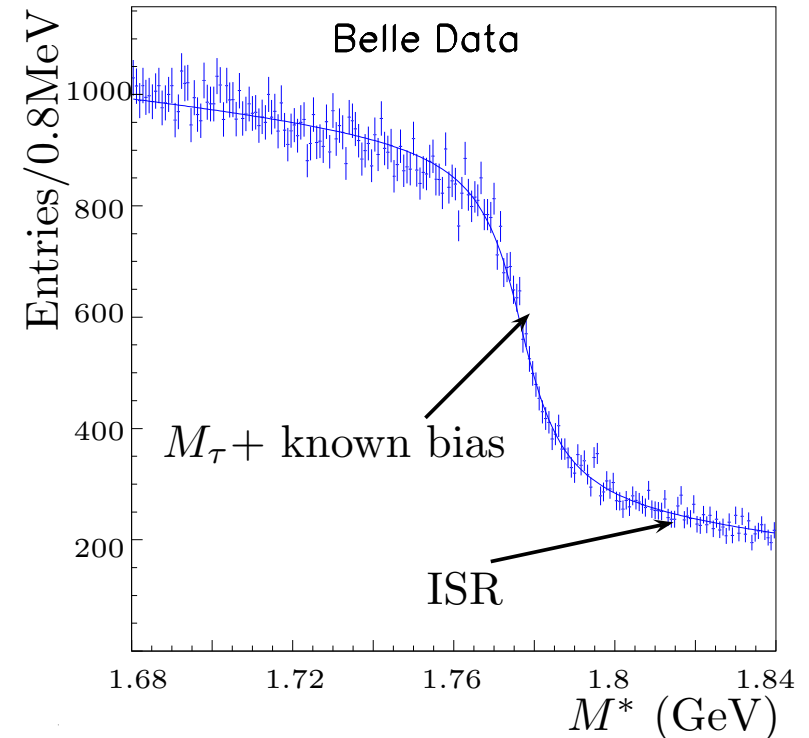
$$M^* = \sqrt{M_{3\pi}^2 + 2(E_{beam} - E_{3\pi})(E_{3\pi} - p_{3\pi})}$$

$$M_\nu = 0, M^* < M_\tau,$$

applied to $\tau \rightarrow 3\pi\nu$,

check with $\tau \rightarrow 3\pi\pi^0\nu$

Systematics	uncertainty(MeV)
Track momenta	0.39
Fit, MC stat	0.41
E_{beam}	0.25
PID, backgrounds	negligible
Total	0.62



$$M_\tau = (1776.71 \pm 0.25_{stat} \pm 0.62_{sys}) \text{ MeV}$$

PDG: $M_\tau = 1776.99^{+0.29}_{-0.26} \text{ MeV}$

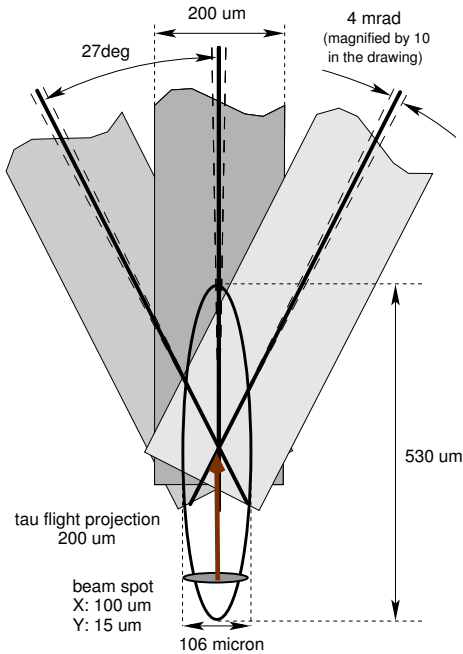
can be improved with \mathcal{L}



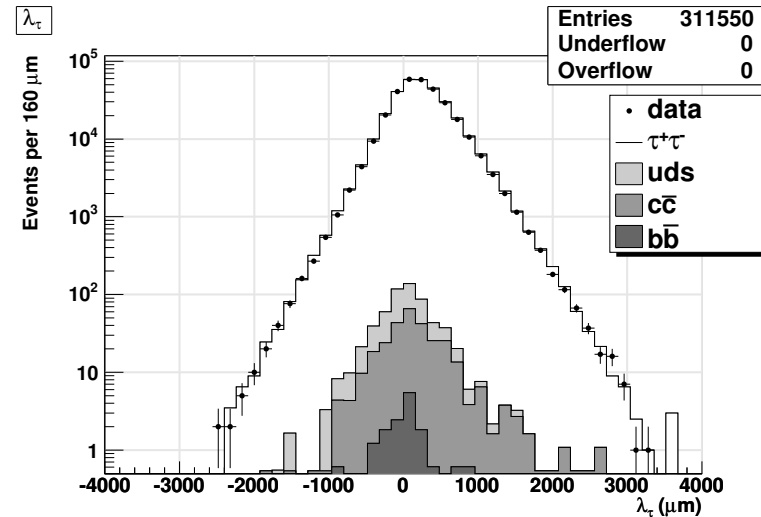
τ Lifetime Measurement



3-prong tau decay
in plane transverse to the beams



NPPS144(2005)105, *BABAR* Preliminary, $\mathcal{L} = 80 \text{ fb}^{-1}$



calculate $\lambda_\tau = \frac{\lambda_T}{\sin \Theta_{3pr}}$ and then
fit $\lambda_\tau(\phi)$ to minimize systematics

$$\tau_\tau = (289.40 \pm 0.91_{stat} \pm 0.90_{sys}) \text{fs}$$

PDG: $\tau_\tau = (290.6 \pm 1.1) \text{fs}$

Can be improved with \mathcal{L}

Systematics

Systematics		$\Delta\tau_\tau$ (%)
Measurement bias	0.336 ±	0.220
Background	-0.428 ±	0.142
Alignment	±	0.111
Beam spot position	±	0.043
Beam spot size	±	0.044
Beam momenta	±	0.043
τ mass	±	0.006
τ momentum	±	0.100
Total	-0.092 ±	0.310

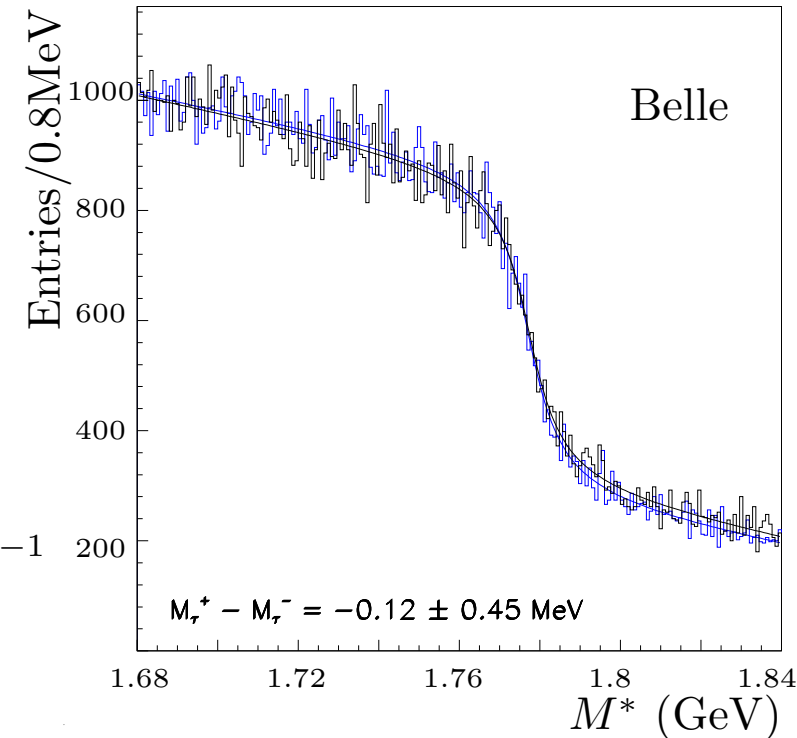
- $M_{\tau^+} - M_{\tau^-} = -0.12 \pm 0.45_{stat} \pm 0.15_{sys}$

$$\frac{|M_{\tau^+} - M_{\tau^-}|}{M_{\tau}} < 5.0 \cdot 10^{-4} \text{ at } 90\% \text{ CL}$$

hep-ex/0511038, Belle Preliminary, $\mathcal{L} = 253 \text{ fb}^{-1}$

- $\frac{\tau_{\tau^-} - \tau_{\tau^+}}{\tau_{\tau^-} + \tau_{\tau^+}} = (0.12 \pm 0.32_{stat} \pm X_{sys})\%$

NPPS144(2005)105, BABAR Preliminary, $\mathcal{L} = 80 \text{ fb}^{-1}$



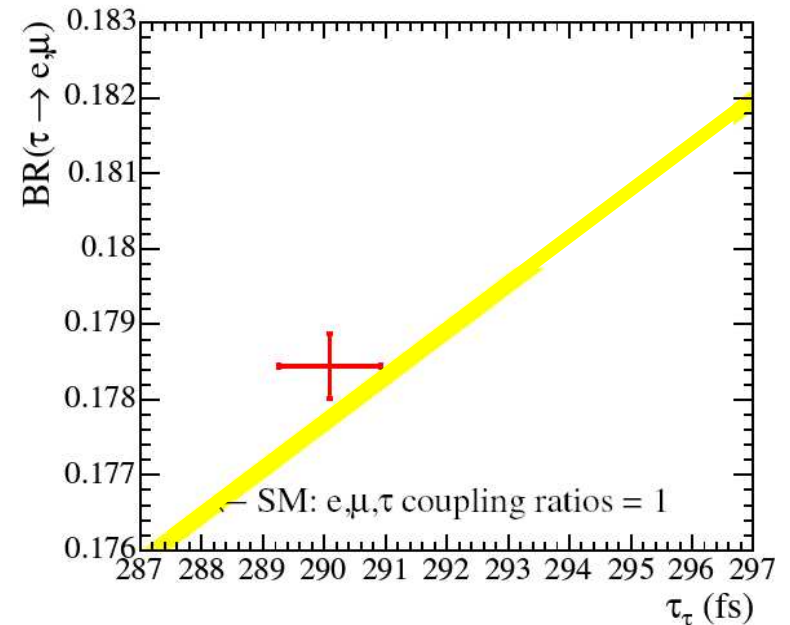
the measurements are statistically limited,
as many systematic uncertainties are canceled

Results from leptonic τ decays



Extract lepton charged current coupling constants from τ leptonic decays.

Combing old τ leptonic decays and new τ_τ, m_τ averaged with PDG04:



$$\frac{g_e}{g_\mu} = 0.9997 \pm 0.0024$$

$$\frac{g_\mu}{g_\tau} = 0.9981 \pm 0.0022$$

courtesy of A.Lusiani

Perfect agreement with SM

Main systematics for g_e/g_μ is $\delta\mathcal{B}(\tau \rightarrow \ell\nu\nu)$.

For g_μ/g_τ the main uncertainties are :

$Br(\tau \rightarrow e\nu\nu)$ ($1.7 \cdot 10^{-3}$), τ_τ ($1.4 \cdot 10^{-3}$)

Results from semileptonic τ decays



Combining old τ semileptonic decays and new τ_τ, m_τ averaged with PDG04:

$$\frac{g_\mu}{g_\tau} = 0.9937 \pm 0.0049$$

Good agreement with SM

Main systematics are from:

$Br(\tau \rightarrow h\nu)$:	$4.5 \cdot 10^{-3}$
τ_τ	:	$1.4 \cdot 10^{-3}$
O_π	:	$0.7 \cdot 10^{-3}$

Average value from $\tau \rightarrow \ell\nu\nu$ and $\tau \rightarrow h\nu$:

$$\frac{g_\mu}{g_\tau} = 0.9976 \pm 0.0021$$



- No deviation from lepton universality is found in τ decays.
 $g_e/g_\mu = 0.9997 \pm 0.0024$, $g_\mu/g_\tau = 0.9976 \pm 0.0021$
- While quite precise, the numbers did not improve significantly for a long time, main uncertainties are on 1-prong τ decays branching fractions . Hard to expect B -factories to improve these tests significantly.
- In future (new experiments?), g_e/g_μ could become better, however, systematics in muon identification are not easy to avoid. For g_μ/g_τ , τ_τ needs to be improved (not mentioning 1-prong branching fractions).