

Weizmann Institute

# Degeneracies in Hubble constant measurements using gravitational lensing

New Physics from Galaxy Clustering II

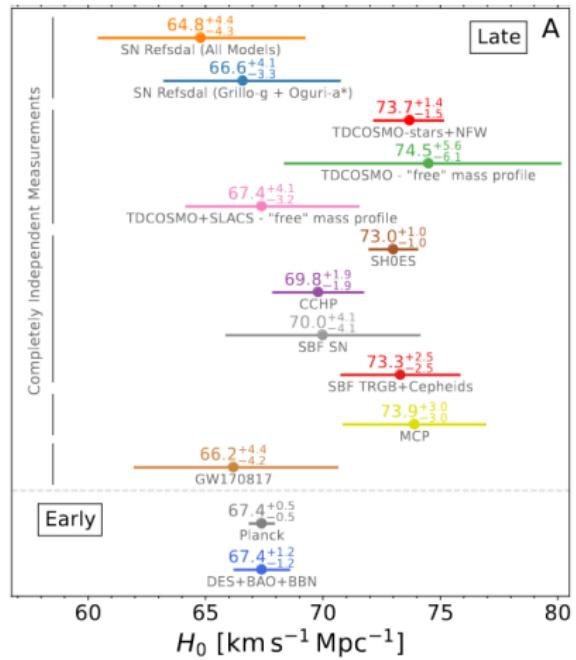
Teodori Luca

November, 2023

# The $H_0$ tension



Worman Institute of Science



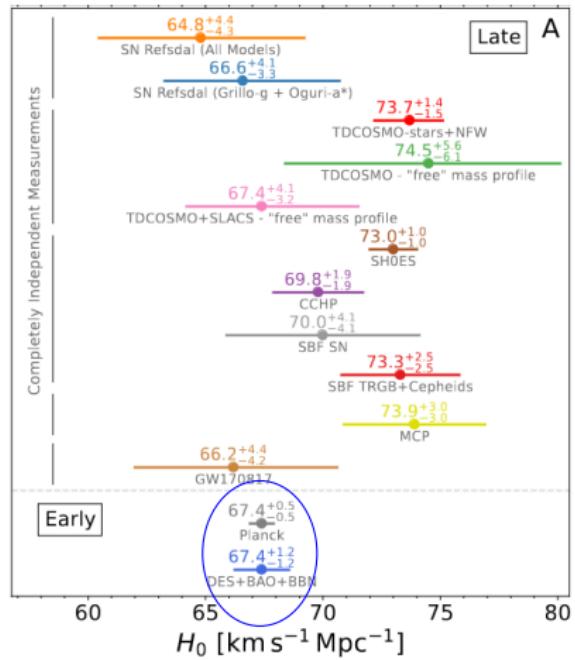
- CMB and LSS (early);
- Distance ladder (late);
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credit: P.L. Kelly et al 2023

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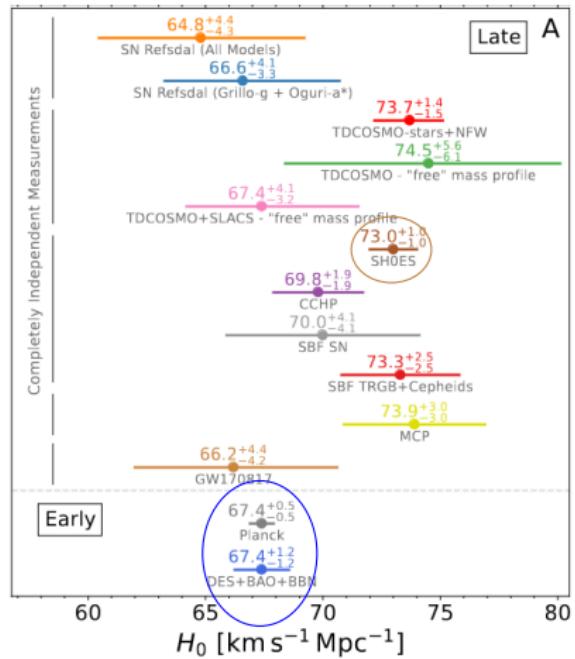
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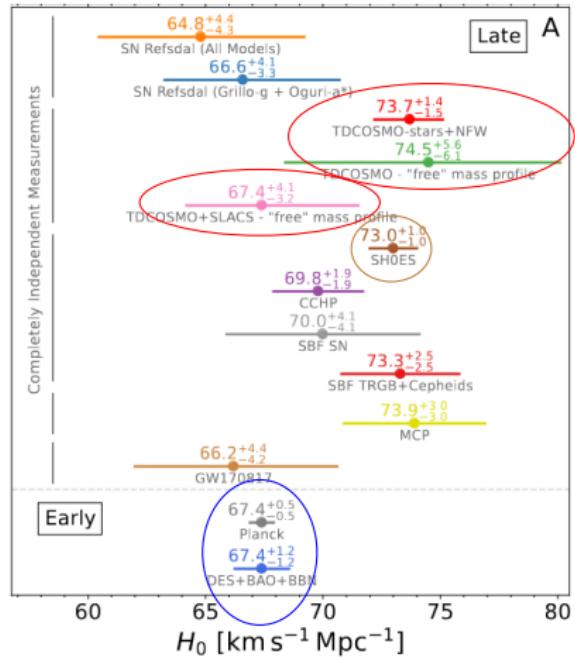
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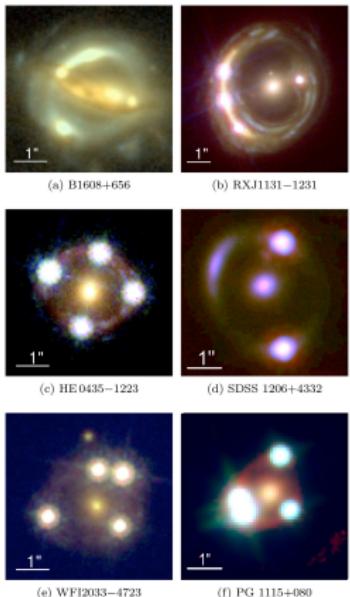
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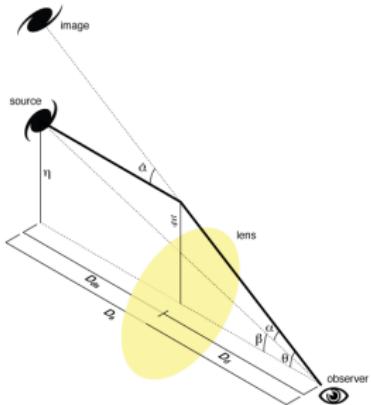
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# Strong Gravitational Lensing in Elliptical Galaxies

How to measure  $H_0$



credit: Wikipedia

- $\hat{\alpha} = 2 \int \nabla_{\perp} \Phi d\lambda \implies \vec{\beta} = \vec{\theta} - \frac{D_{LS}}{D_S} \hat{\alpha}(\vec{\theta})$

- Convergence  $\kappa \sim \int dz \rho$ .

- Lens model + time delay measurement

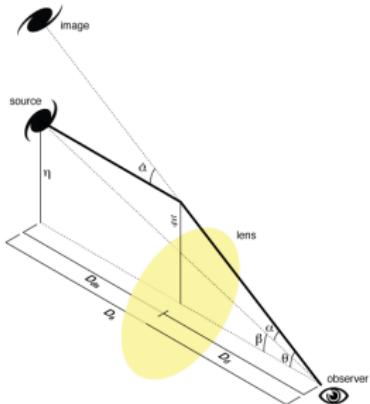
$$\Delta t_{ij} \propto \frac{1}{H_0}.$$

- Degeneracies: source position and mass of galaxy unknown

$$\vec{\beta} \rightarrow \lambda \vec{\beta}, \kappa \rightarrow \lambda \kappa + (1 - \lambda) \implies H_0 \rightarrow \lambda H_0$$

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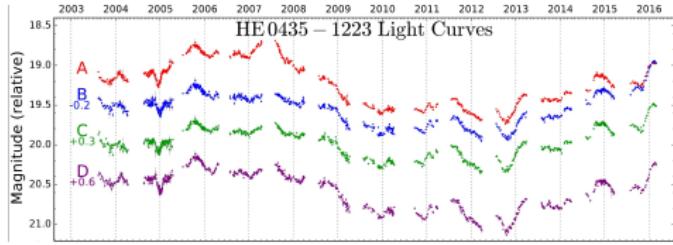
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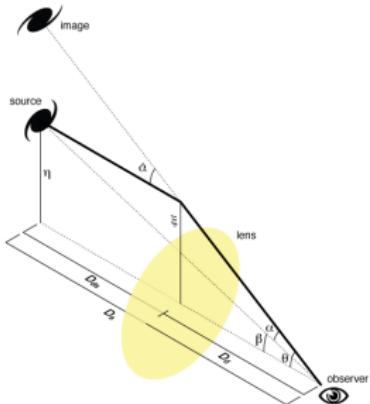
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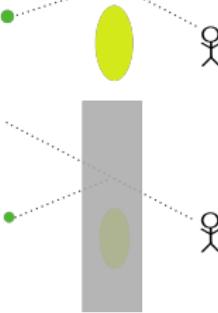
from V. Bonvin et al (2016)

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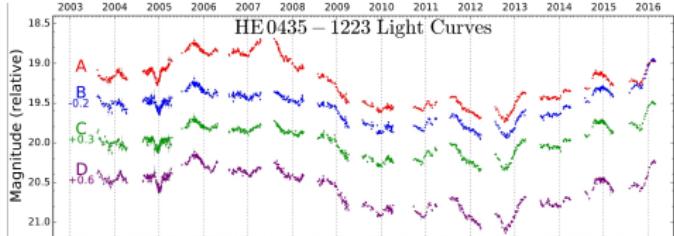
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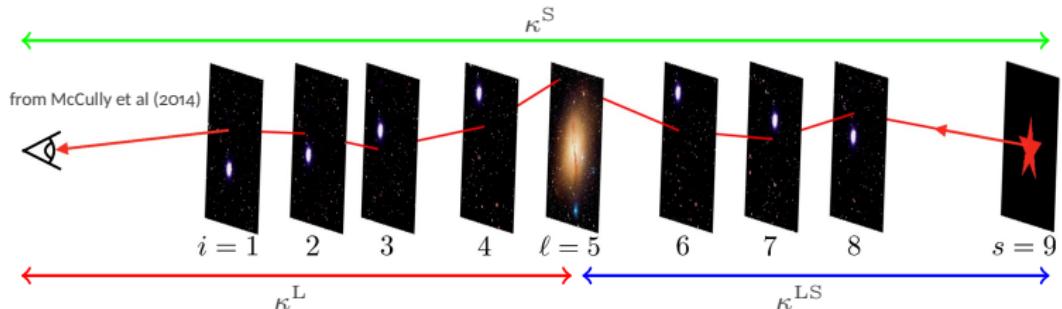
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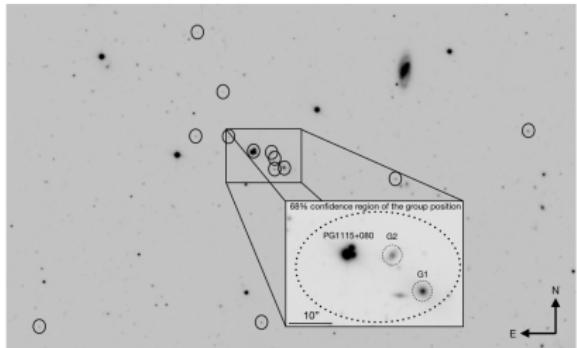
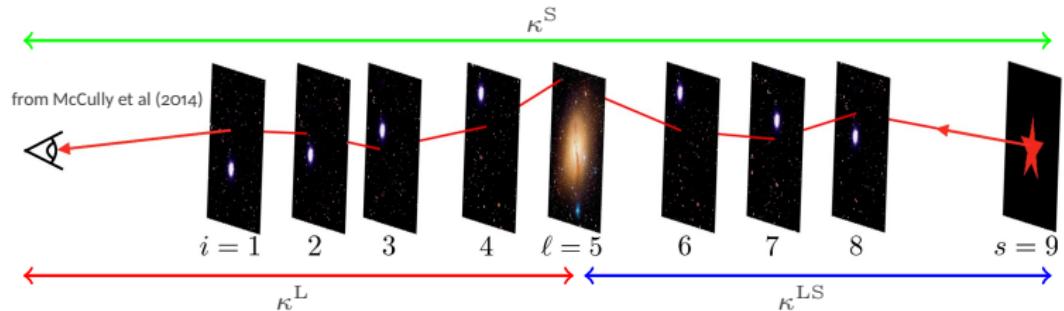
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# Examples of mass sheets



- LSS on the line of sight;
- Host dark matter halo from group/cluster;
- Stellar and galaxy kinematics  $\implies$  proxy for real mass.

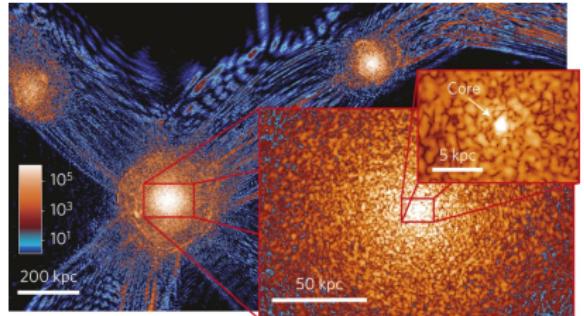
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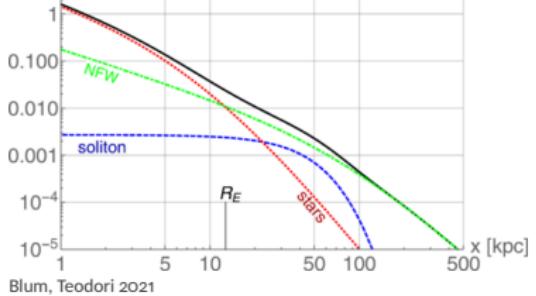
credit: Shajib et al 2019

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# Internal Mass sheet degeneracy: ULDM example



credit: Shajib et al 2019  
 $\rho$  [ $M_\odot \text{ pc}^{-3}$ ]



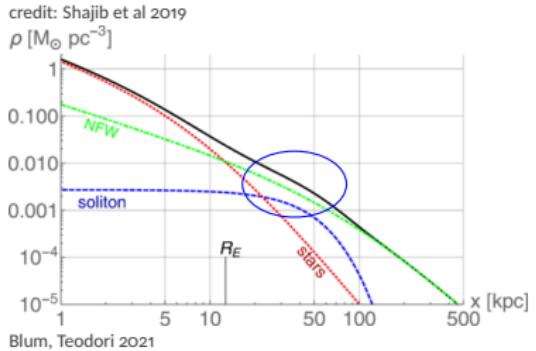
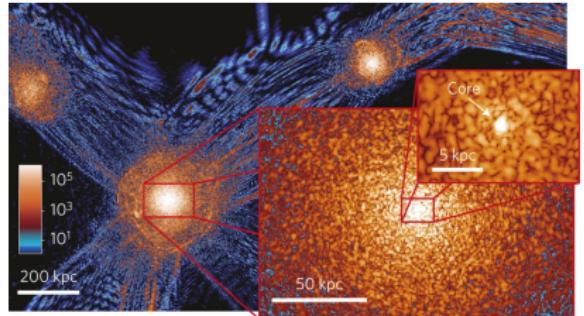
Blum, Teodori 2021

- Possible mass sheets also from internal DM halo
- Possible cores from non-trivial DM models, e.g. Ultralight dark matter, cores

$$\lambda_{\text{deBroglie}} = \frac{1}{mv} \sim 20 \text{ kpc} \frac{1 \times 10^{-24} \text{ eV}}{m}$$

- Kinematics measurements fundamental to constrain MSD, reminding that exact MSD  $\neq$  approximate MSD
- Sensitivity to galaxy features which are hard to probe otherwise.

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# Conclusions

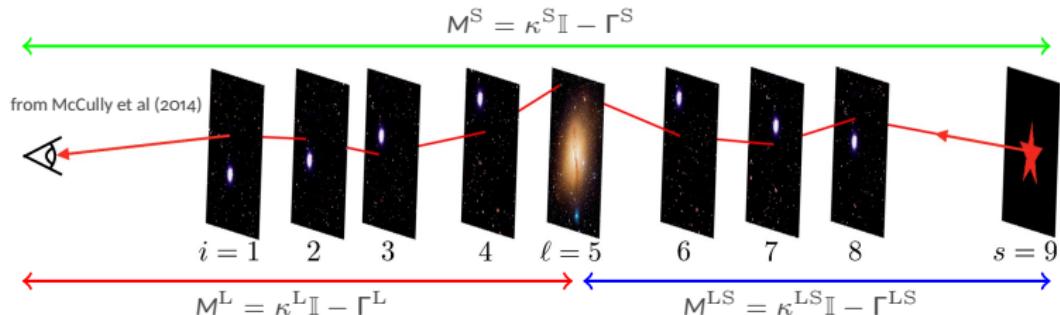
Can we measure  $H_0$  with Gravitational Lensing?



- Challenge: modeling degeneracies; important to point out all the shortcomings to lensing collaborations, in order to achieve an *accurate*  $H_0$  measurement.
- Promising! New data arriving, including precise stellar kinematics, new lensed systems (among which, “clean” multiple source systems) etc.
- **With an  $H_0$  prior, we can measure galactic features which are difficult to spot otherwise, and a better characterization of the weak lensing field**

# The multilens equation

## The tidal approximation



Lens equation in tidal approximation

$$\vec{\beta} = (\mathbb{I} - M^S) \vec{\theta} - (\mathbb{I} - M^{LS}) \vec{\alpha} ((\mathbb{I} - M^L) \vec{\theta})$$

Choose

Degeneracy ("revised" MSD)

$$1 - M^R \longmapsto \lambda_R (1 - M^R),$$

$$\vec{\beta} \longmapsto \lambda_S \vec{\beta},$$

$$\vec{\alpha}(\vec{\theta}) \longmapsto \lambda_S \lambda_{LS}^{-1} \vec{\alpha}(\lambda_L^{-1} \vec{\theta}),$$

$$\Psi(\vec{\theta}) \longmapsto \lambda_S \lambda_{LS}^{-1} \lambda_L \Psi(\lambda_L^{-1} \vec{\theta}).$$

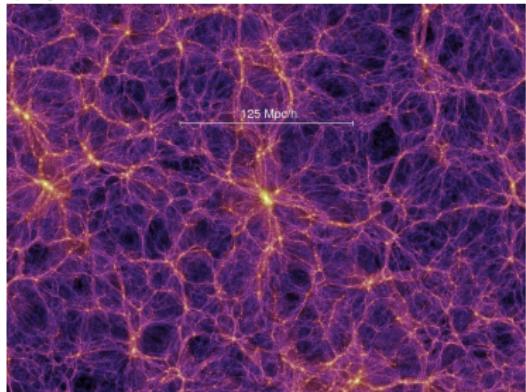
$$\lambda_S = \frac{1}{1 - \kappa^S}, \quad \lambda_{LS} = \frac{1}{1 - \kappa^{LS}}, \quad \lambda_L = \frac{1}{1 - \kappa^L},$$

external convergence removed from the modeling

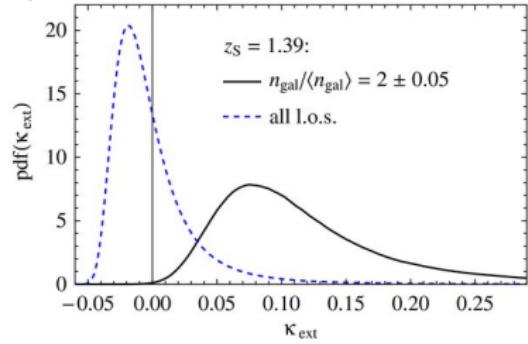
# Interpreting the Mass Sheet Degeneracy



Springer et al 2005



Suyu et al 2010



- Change  $\lambda_S$ : changing one's mind about the true  $\kappa^S$

- 

$$\begin{aligned}\kappa^R &\longmapsto \lambda_R \kappa^R + (1 - \lambda_R) \\ \Gamma^R &\longmapsto \lambda_R \Gamma^R\end{aligned}$$

- Time delays do change!

$$\Delta\tau \rightarrow \lambda_S \lambda_{LS}^{-1} \lambda_L \Delta\tau$$

$$H_0 \rightarrow \lambda_S \lambda_{LS}^{-1} \lambda_L H_0$$

- Estimate  $\kappa^S$  via ray-tracing through Millennium Simulation and characterization of the lens field
- Degeneracy is limited by priors on weak lensing quantities and constraints on mass of lens galaxy (stellar kinematics)

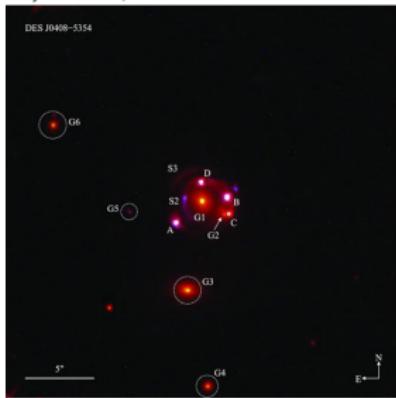
# Multi-source systems and MSD



Cluster MACS J149.5+2223, Credit: NASA



Shajib et al 2019



- New lens equation (ignoring lens-lens coupling)

$$\vec{\beta}_i = (\mathbb{I} - M_i^S)\vec{\theta} - (\mathbb{I} - M_i^{LS})C_i\vec{\alpha}_1((\mathbb{I} - M^L)\vec{\theta})$$

$$C_i := \frac{D_{S1} D_{LSi}}{D_{LS1} D_{Si}}, \quad \left( \hat{\alpha} \frac{D_{LS}}{D_S} =: \vec{\alpha} \right)$$

- MSD untouched! But I cannot rescale away all external convergences  $\implies$  differential external convergences
- Observable:

$$C_i \frac{\left| \vec{\alpha}_1^{\text{model}}(\vec{\theta}) \right|}{\left| \vec{\alpha}_2^{\text{model}}(\vec{\theta}) \right|} \approx \left( 1 + \delta\kappa_{12}^S - \delta\kappa_{12}^{LS} \right)$$