



# Dark Forces vs LSS 1

## Model and Perturbative Structure

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In collaboration with E. Castorina, M. Costa, D. Redigolo, E. Salvioni

Based on 2204.08484 and 2309.11496

# Introduction

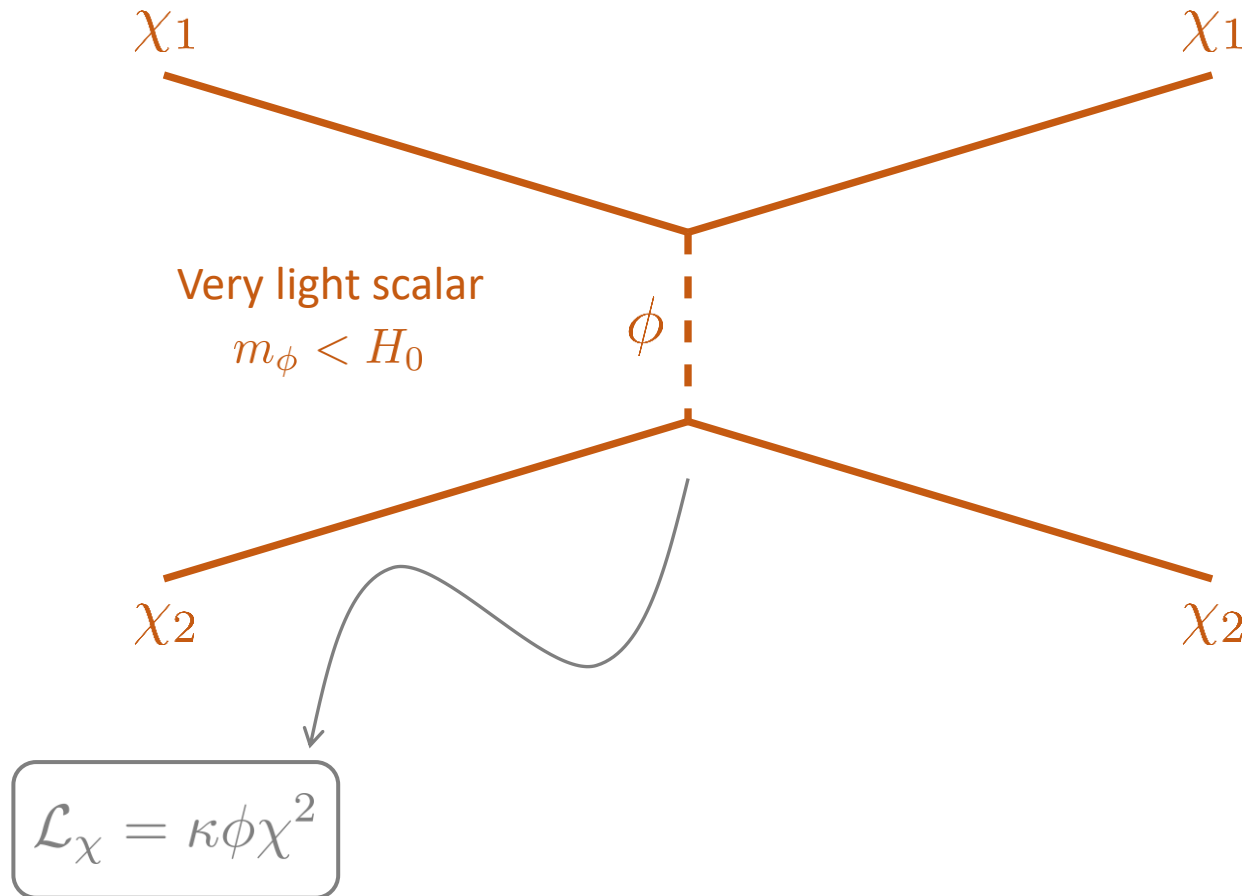
Already all the information we have about Dark Matter ( existence, abundance...) comes from astrophysical and cosmological observations.

Can we get additional information on DM dynamics from cosmology?

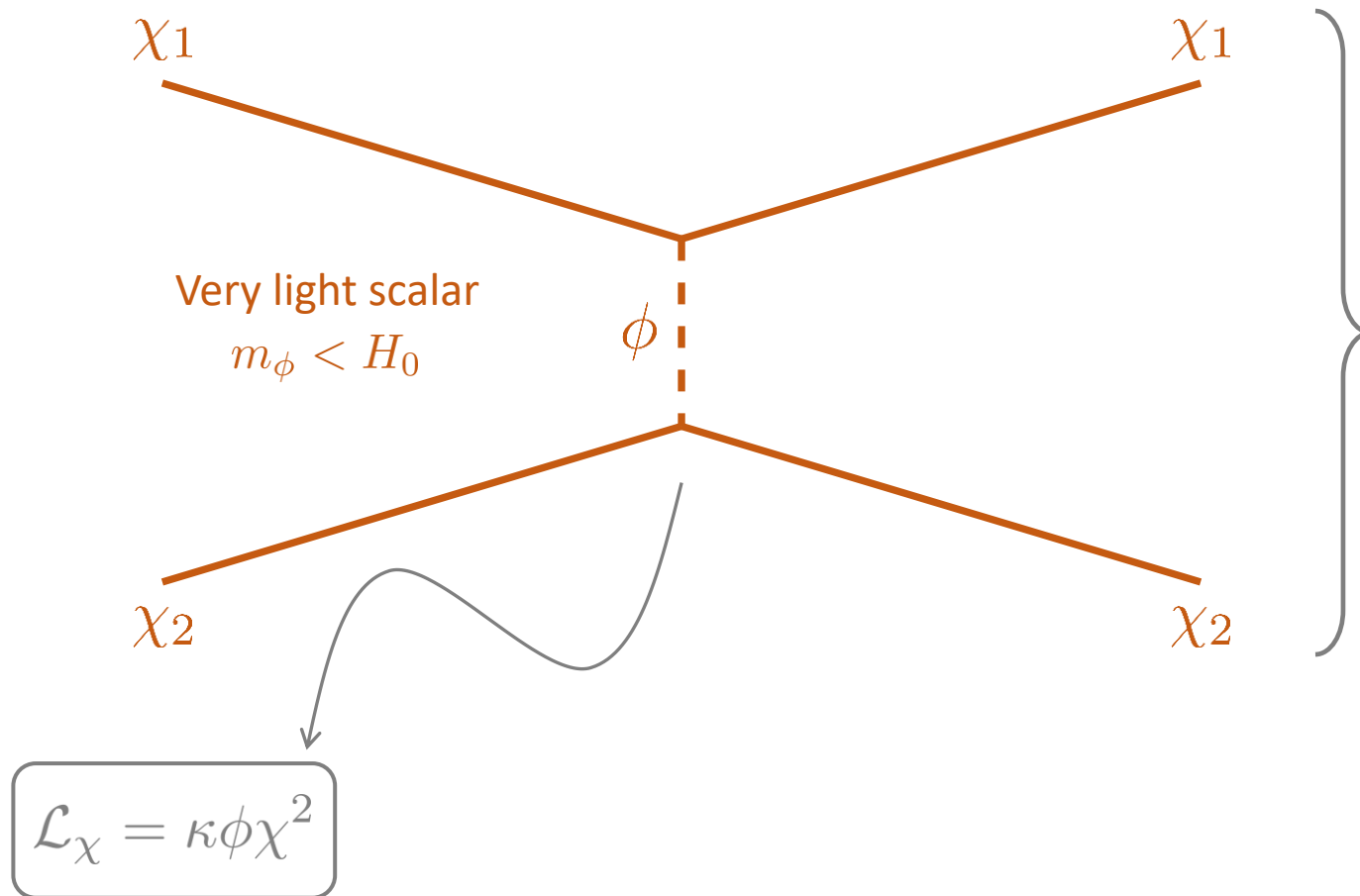
Can we exploit new data from galaxy surveys?

# Dark fifth forces – Minimal model

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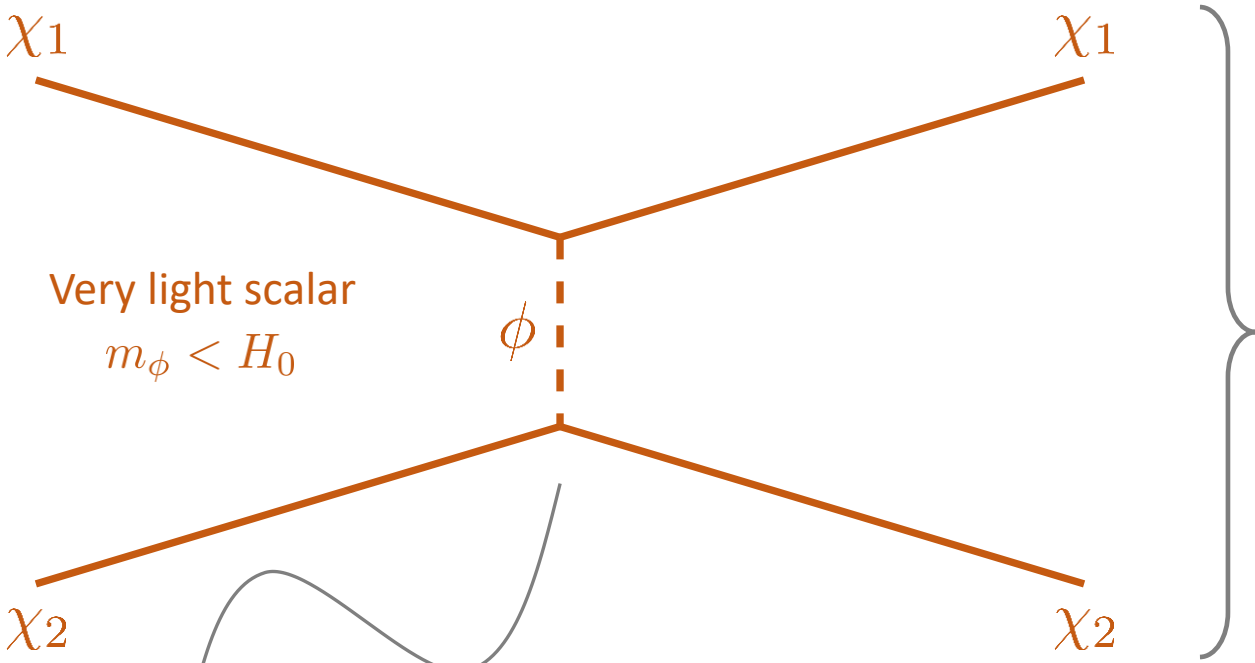


Testable only through cosmology!

$$V_\chi = -4\pi G_N \beta \frac{m_1 m_2}{r} e^{-m_\phi r}$$

$$\beta = \frac{\kappa^2}{4\pi m_\chi^4 G_N}$$

# Dark fifth forces – Minimal model



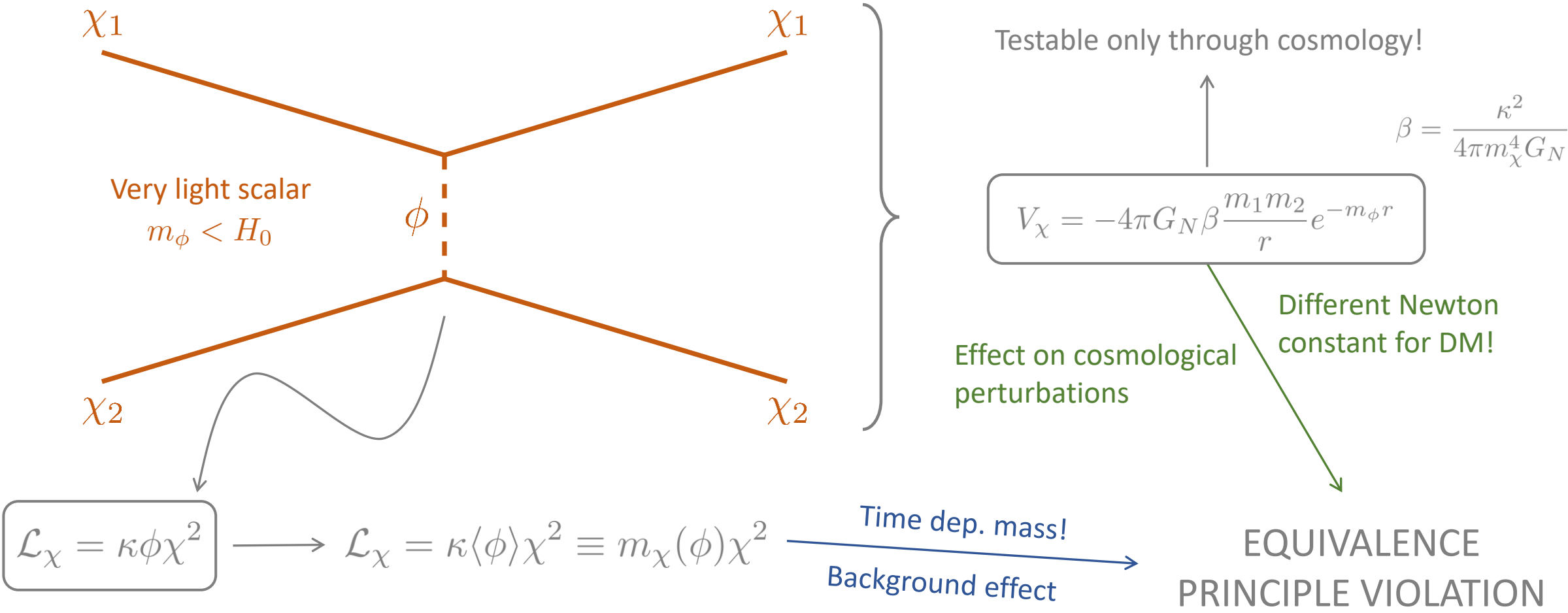
$\mathcal{L}_\chi = \kappa\phi\chi^2 \longrightarrow \mathcal{L}_\chi = \kappa\langle\phi\rangle\chi^2 \equiv m_\chi(\phi)\chi^2$

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# Background dynamics

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Starting point: Klein-Gordon equation for  $\phi$

$$\bar{s}'' + 2\mathcal{H}\bar{s}' + 4\pi\beta G_N a^2 \bar{\rho}_\chi \frac{\partial \log m_\chi(s)}{\partial s} = 0 \quad s = \frac{\kappa}{m_\chi^2} \phi$$

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Scalar evolution sourced by DM

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Solution in MD

$$\bar{s} = \bar{s}_{\text{eq}} - 2\beta \frac{\partial \log m_\chi(s)}{\partial s} f_\chi \log \frac{\tau}{\tau_{\text{eq}}}$$

DM redshifts differently!

Correction to Hubble!

$$\dot{\rho}_\chi = \dot{m}_\chi n_\chi + m_\chi \dot{n}_\chi \implies \Omega_\chi \propto a^{-3} \left( 1 - \beta f_\chi \frac{\partial \log m_\chi(s)}{\partial s} \log \frac{a}{a_{\text{eq}}} \right)$$

$$\mathcal{H} = \mathcal{H}_{\Lambda\text{CDM}} \left( 1 - \beta f_\chi^2 \frac{\partial \log m_\chi(s)}{\partial s} \right)$$

# Cosmological perturbations

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$$\delta_m = f_\chi \delta_\chi + (1 - f_\chi) \delta_b$$

$$\delta_r = \delta_\chi - \delta_b$$

Boltzmann equations

$$\delta'_m + \theta_m = -\nabla_i(\delta_m v_m^i)$$

$$\theta'_m + \left( \mathcal{H} + f_\chi \frac{\partial \log m_\chi(s)}{\partial s} \bar{s}' \right) \theta_m = k^2 \frac{\partial \log m_\chi(s)}{\partial s} f_\chi \delta_s + k^2 \Psi - \nabla_i(v_m^j \nabla_j v_m^i)$$

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Fifth force

Perturbed Klein-Gordon equation  $\longrightarrow$  Poisson equation  $k^2 \delta_s = -\frac{3}{2} \Omega_m \mathcal{H}^2 \beta f_\chi \frac{\partial \log m_\chi(s)}{\partial s} \delta_m$

# Cosmological perturbations

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Linear solution

$$\delta_m^{(1)}(\vec{k}) = \overbrace{D_{1m}^{\Lambda\text{CDM}} \left( 1 + \frac{3}{5} \beta f_\chi^2 \frac{\partial \log m_\chi(s)}{\partial s} \log \frac{a}{a_{\text{eq}}} + \frac{3}{5} \beta f_\chi^2 \frac{\partial \log m_\chi(s)}{\partial s} \log \frac{a}{a_{\text{eq}}} \right)}^{\equiv D_{1m}} \delta_0(\vec{k})$$

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- Background corrections enhance the growth
- No new spatial features in  $\delta_m$  at linear level
- Logarithmically enhanced growth of  $\delta_m$
- Growing relative perturbations
- Different scalings with the DM fraction

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$\approx 8$

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- Same ansatz as in  $\Lambda\text{CDM}$
- Same  $\Lambda\text{CDM}$  kernels at  $\mathcal{O}(\beta f_\chi^2 \log a)$
- New kernels arise at  $\mathcal{O}(\beta f_\chi)$   $\longrightarrow$  relevant if  $f_\chi \lesssim 1/8$

# Conclutions

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## Modified background

- Affects physical distances
- Enhances growth of perturbations

## Linear dynamics

- Log enhanced growth of matter perturbations
- Growing relative modes

Dark fifth  
forces

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graph TD; A[Dark fifth forces] --> B[Modified background]; A --> C[Linear dynamics]; A --> D[Non-linear dynamics];
```

## Non-linear dynamics

- Larger power at non-linear scales
- New spatial features prominent for small DM fractions