

# From charm mesons at hadron colliders to studies of neutrino fluxes produced in the Earth's atmosphere

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Phys.Rev.D 105 (2022) 1, 014001; Eur. Phys. J. C 82 (2022) 3, 236

Phys. Rev. D 96 (2017) 9, 094026

Trans-European School of High Energy Physics

14th-22nd July 2023, Bezmiechowa Górna, Bieszczady mountains, Poland

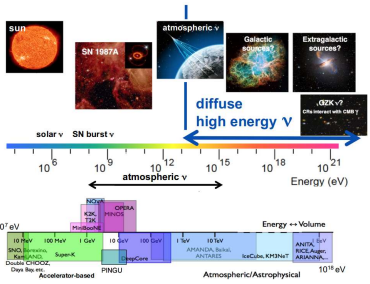
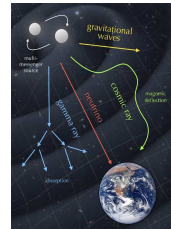




# Motivation from the Neutrino Astronomy

**High-energy cosmic neutrinos** ⇒ excellent cosmic messenger particles

- Universe not transparent to extragalactic photons with  $E_\gamma > 10$  TeV (gamma rays) ⇒ strongly absorbed by interactions with the cosmic microwave background (CMB).
- Neutrinos ⇒ no absorption and no deflection by magnetic fields
  - essentially no mass and no electric charge, weakly interacting
  - can travel cosmic distances without distortion and can point back to their sources
  - can escape dense astrophysical environments where they are produced



## Low-energy extraterrestrial neutrinos

- MeV neutrinos from the Sun (the closet source)
- neutrinos from supernova 1987A

Pushed forward:

- elucidated neutrino properties, neutrino flavor changing puzzle
- fundamental physics, Sun's inner working, supernova physics

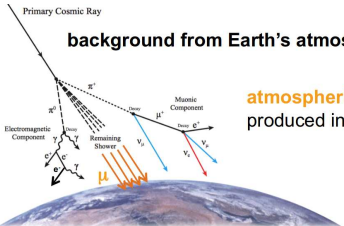
● Diffuse high-energy neutrinos ⇒ information about the mechanism of cosmic ray production and cosmic ray sources

- e.g. probe of the high-energy neutrino-nucleon cross section
- many new physics phenomena (dark matter, leptoquarks, micro black holes, etc.)





# Cosmic neutrinos and atmospheric backgrounds

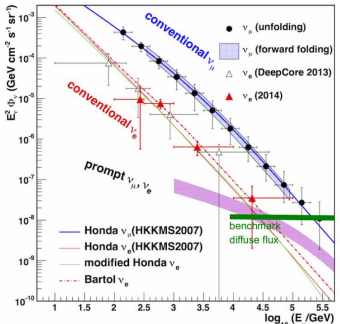
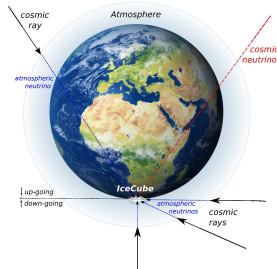


background from Earth's atmosphere

**atmospheric muons**  
produced in cosmic ray air showers

**atmospheric neutrinos**  
produced in the same showers

$1/10^6$



- **conventional  $\nu$ -flux**  $\Rightarrow \Phi_\nu \sim E_\nu^{-3.7}$ 
  - ▷ decays of **lighter mesons**:  $\pi^\pm, K^\pm$
  - ▷ long life-time: interactions occurs before decay
  - ▷ mesons lose energy  $\rightarrow$  steeply falling  $\nu$ -flux
  - ▷ zenith-angle dependent, largest at horizon

- **prompt  $\nu$ -flux** (not yet identified)  $\Rightarrow \Phi_\nu \sim E_\nu^{-2.7}$ 
  - ▷ decays of **heavy mesons**:  $D$  and  $B$
  - ▷ short life-time: decay before interactions
  - ▷ more energy transferred to neutrino  $\rightarrow$  flat  $\nu$ -flux
  - ▷ isotropic



# Cosmic neutrinos point of view vs. QCD point of view

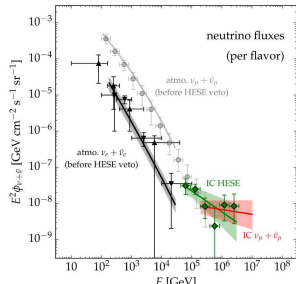
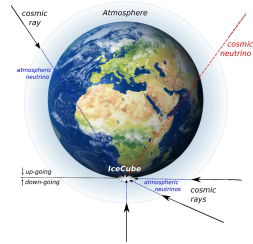
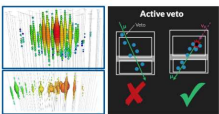
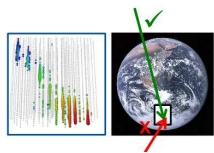
## Two complementary strategies:

### • $\nu_\mu$ tracks from Northern Sky

- ▷ using the Earth as a filter by selecting up-going track events
- ▷ atm. muons sufficiently reduced
- ▷ vertex outside the detector

### • Starting Events (HESE)

- ▷ high-energy  $\nu$  interacting inside the detector
- ▷ all directions in the sky
- ▷ a virtual veto region
- ▷ rejects atmospheric muons and neutrinos



### • Cosmic neutrinos point of view:

HESE veto data  $\Rightarrow$  no atmospheric background  
 $\Rightarrow$  the first observation of high-energy astrophysical neutrinos by IceCube

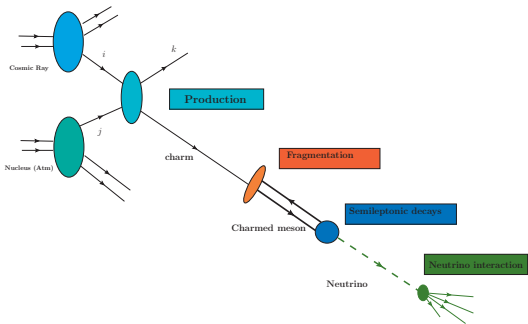
### • QCD physics point of view:

study of the  $\nu_\mu$  tracks data from Northern Sky  
 $\Rightarrow$  could be use to constrain the prompt atmospheric neutrino flux and QCD physics behind in the kinematical limits beyond the LHC  
 (IceCube Collaboration, *Astrophys. J.* 833 (2016))



# From cosmic ray to prompt neutrino flux detection

Theoretical predictions of the prompt atmospheric neutrino flux at the detector level  $\Rightarrow$



- a multi-stage problem with many sources of uncertainties
  - ▷ the initial cosmic ray flux: shape and composition
  - ▷ **strong interaction cross section**: charm production, fragmentation, parton densities, nuclear effects, intrinsic charm
  - ▷ **charm hadronization**
  - ▷ **semileptonic decay**
  - ▷ **neutrino interaction cross section**

high-energy neutrinos ( $E_\nu > 10^5$  GeV)  $\Rightarrow$  charmed meson production at very high energies and large forward rapidities

- QCD methods for charmed meson production in the kinematics beyond the LHC
  - validity of the collinear factorization in the forward kinematics
  - forward hadronization, subleading fragmentation of light partons, recombination mechanisms, etc.
  - **the presence (or not) of intrinsic heavy quarks in the hadronic wave function**
  - **the presence (or not) of nonlinear (saturation) effects**



# Development of air-showers and lepton fluxes

- may be described by a set of **CASCADE EQUATIONS**

The flux  $\phi_j(E_j, X)$  of a particle  $j$  with energy  $E_j$  that has traversed a slant depth  $X$  is given by:

$$\frac{d\phi_j}{dX} = -\frac{\phi_j}{\lambda_j} - \frac{\phi_j}{\lambda_j^{\text{dec}}} + \sum_k S_{kj}(E_j, X),$$

where  $\lambda_j$  is the interaction length (the average amount of atmosphere (in g/cm<sup>2</sup>) traversed between successive collisions with air nuclei),  $\lambda_j^{\text{dec}}$  is the decay length, and  $S_{kj}$  are '(re)generation functions' describing the production of particle  $j$  from particle  $k$ . The (re)generation function is:

$$S_{kj}(E_j, X) = \int_{E_j}^{\infty} \frac{\phi_k(E'_k, X)}{\lambda_k(E'_k)} \frac{dn(k \rightarrow j; E'_k, E_j)}{dE_j} dE'_k,$$

where  $dn(k \rightarrow j; E'_k, E_j)$  is the differential transition rate between particle species  $k$  and  $j$  (the number of particles  $j$  with energies between  $E_j$  and  $E_j + dE_j$  produced in the collision of the incoming particle  $k$  with an air nucleus)

The equation says that as a particle ( $j$ ) traverses the atmosphere, its flux will decrease when the particle undergoes an interaction (thus losing energy) or decays, as well as increase from the decay or interaction of other particle species ( $k$ )





# Development of air-showers and lepton fluxes

Assuming that the particle flux factorizes into components dependent respectively on the energy  $E$  and the slant depth  $X$ , the (re)generation function can be rewritten more simply in terms of Z-moments as

$$S_{kj}(E_j, X) = \frac{\phi_k(E_j, X)}{\lambda_k(E_j)} Z_{kj}(E_j),$$

with the key property that the moment  $Z_{kj}$ ,

$$Z_{kj}(E_j) = \int_{E_j}^{\infty} \frac{\phi_k(E'_k, X)}{\phi_k(E_j, X)} \frac{\lambda_k(E_j)}{\lambda_k(E'_k)} \frac{dn(k \rightarrow j; E'_k, E_j)}{dE_j} dE'_k,$$

is independent of the slant depth  $X$  (which cancels in the ratio of fluxes)

- **a set of coupled differential equations:**

$$\frac{d\phi_p}{dX} = -\frac{\phi_p}{\lambda_p} + Z_{pp} \frac{\phi_p}{\lambda_p} \quad (\text{protons})$$

$$\frac{d\phi_m}{dX} = -\frac{\phi_m}{\rho d_m(E)} - \frac{\phi_m}{\lambda_m} + Z_{mm} \frac{\phi_m}{\lambda_m} + Z_{pm} \frac{\phi_p}{\lambda_p} \quad (\text{mesons})$$

$$\frac{d\phi_l}{dX} = \sum_m Z_{m \rightarrow l} \frac{\phi_m}{\rho d_m} \quad (\text{leptons})$$



# Development of air-showers and lepton fluxes

The most crucial ingredient is the nucleon to meson moment:  $Z_{pm}$   
 which depends on the charm production cross-section in  $pp$ -collisions:

- the generic  $Z$ -moment can be written as:

$$Z_{kj}(E_j) = \int_{E_j}^{\infty} \frac{\phi_k(E'_k, X) \lambda_k(E_j)}{\phi_k(E_j, X) \lambda_k(E'_k)} \frac{dn(kA \rightarrow j; E'_k, E_j)}{dE_j} dE'_k$$

- $Z_{pD}$ : the number distribution can be related to the differential charm cross-section:

$$\frac{dn(pA \rightarrow D + X; E', E)}{dE} = \frac{1}{\sigma_{pA}(E')} \frac{d\sigma(pA \rightarrow D + X; E', E)}{dE}$$

- we assume:  $\sigma(pA \rightarrow D + X) \simeq \langle A \rangle \sigma(pp \rightarrow D + X)$

The charmed hadron  $Z$ -moments are given by:

$$Z_{pD}(E_D) = \int_{E_D}^{\infty} \frac{\phi_p(E'_p)}{\phi_p(E_D)} \frac{\langle A \rangle}{\sigma_{pA}(E_D)} \frac{d\sigma(pp \rightarrow D + X; E'_p, E_D)}{dE_D} dE'_p$$

$$Z_{pD}(E_D) = \int_0^1 \frac{dx_F}{x_F} \frac{\phi_p(E_D/x_F)}{\phi_p(E_D)} \frac{\langle A \rangle}{\sigma_{pA}(E_D)} \frac{d\sigma_{pp \rightarrow D}(E_D/x_F)}{dx_F},$$

where  $E$  is the energy of the  $D$ -meson,  $x_F = E_D/E'_p$  is the Feynman variable,

$\sigma_{pA}$  is the inelastic  $p$ -Air cross section and

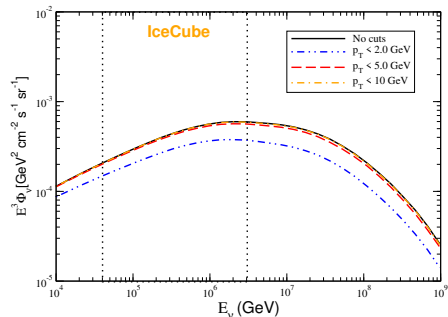
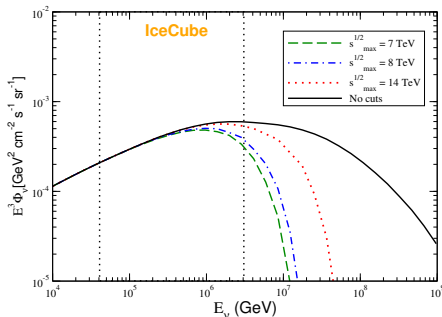
$d\sigma/dx_F$  is the differential cross section for the charmed meson production  $\Rightarrow$  **INPUT**



# Kinematics probed with the IceCube prompt neutrino flux

Mapping the dominant regions of the phase space associated with  $c\bar{c}$ -pair production relevant for the **prompt flux at IceCube**

(V.P. Goncalves, R.M., R. Pasechnik, A. Szczurek, Phys.Rev.D 96 (2017) 9, 094026)



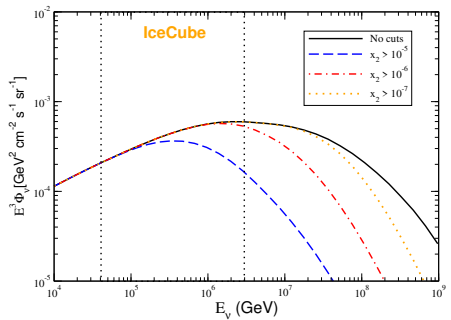
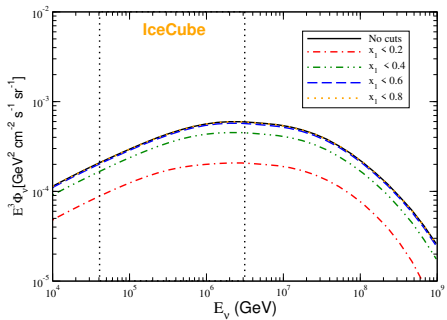
- recent: up to  $E_\nu = 3 \cdot 10^6 \text{ GeV} \Rightarrow$  the LHC energy range
- future:  $E_\nu > 10^7 \text{ GeV} \Rightarrow$  energy range beyond that probed in the LHC Run2
- flux sensitive to the  $p_T < 5 \text{ GeV}$



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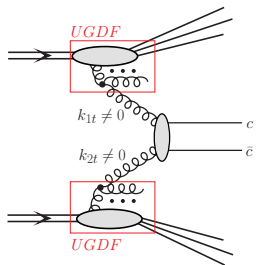


- projectile:  $0.2 < x_1 < 0.6$
- target:  $10^{-6} < x_2 < 10^{-5}$  (IceCube recently)  
and even  $10^{-8} < x_2 < 10^{-5}$  (future)
- far-forward production beyond the LHC range  $\Rightarrow$  very asymmetric kinematics

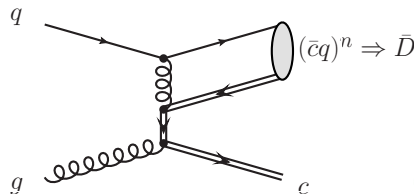
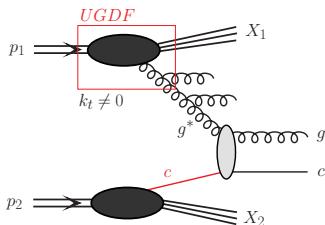




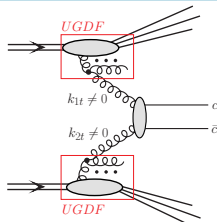
# QCD charm production mechanisms at forward directions



- $g^* g^* \rightarrow c \bar{c} \Rightarrow$  the standard QCD mechanism (and usually considered as a leading) of gluon-gluon fusion with off-shell initial state partons, calculated both in the full  $k_T$ -factorization approach and in the hybrid model
- $g^* c \rightarrow g c \Rightarrow$  the mechanism driven by the **intrinsic charm** component of proton calculated in the hybrid approach with off-shell initial state gluon and collinear intrinsic charm quark
- $g q \rightarrow \bar{D} c \Rightarrow$  the **recombination mechanism** calculated in the leading-order collinear approach



# The $k_T$ -factorization (high-energy factorization) approach



## off-shell initial state partons $\Rightarrow$

initial transverse momenta explicitly included  $k_{1,t}, k_{2,t} \neq 0$

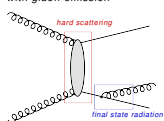
- additional hard dynamics coming from transverse momenta of incident partons (virtualities taken into account)
- very efficient for less inclusive studies of kinematical correlations
- more exclusive observables, e.g. pair transverse momentum or azimuthal angle very sensitive to the incident transverse momenta

multi-differential cross section:

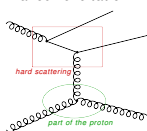
$$\frac{d\sigma}{dy_1 dy_2 d^2 p_{1,t} d^2 p_{2,t}} = \int \frac{d^2 k_{1,t}}{\pi} \frac{d^2 k_{2,t}}{\pi} \frac{1}{16\pi^2 (x_1 x_2 s)^2} \overline{|\mathcal{M}_{g^* g^* \rightarrow Q\bar{Q}}|^2} \times \delta^2(\vec{k}_{1,t} + \vec{k}_{2,t} - \vec{p}_{1,t} - \vec{p}_{2,t}) \mathcal{F}_g(x_1, k_{1,t}^2, \mu) \mathcal{F}_g(x_2, k_{2,t}^2, \mu)$$

- the LO off-shell matrix elements  $\overline{|\mathcal{M}_{g^* g^* \rightarrow Q\bar{Q}}|^2}$  available (analytic form)
- the  $2 \rightarrow 3$  and  $2 \rightarrow 4$  processes (higher-order) only at tree-level (KaTie Monte Carlo)
- $\mathcal{F}_g(x, k_t^2, \mu)$  - transverse momentum dependent - unintegrated PDFs (uPDFs)

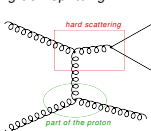
pair creation  
with gluon emission



flavour excitation



gluon splitting

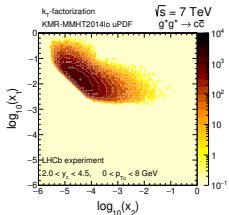


- part of higher-order (real) corrections might be effectively included in uPDF



# Forward open charm production at the LHCb

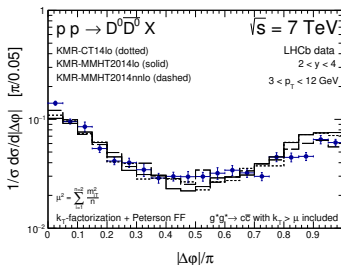
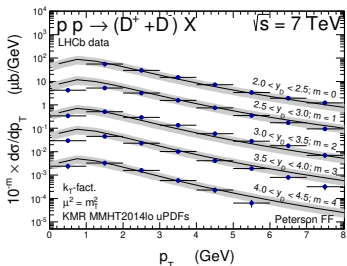
## Open charm LHCb data in $pp$ -scattering at $\sqrt{s}=7, 13$ TeV:



Detector acceptance:  $2.0 < y < 4.5$  and  $0 < p_T < 8$  GeV

- inclusive  $D$ -meson spectra and  $D\bar{D}$ -pair correlation observables ( $M_{inv}$ ,  $\Delta\varphi$ ,  $p_T$ -pair)
- longitudinal momentum fractions probed:  $10^{-3} < x_1 < 10^{-1}$  and  $10^{-5} < x_2 < 10^{-3}$
- $p_T$ -differential cross section well described in different  $y$ -bins
- correct shapes of the correlation observables

(R.M., A. Szczurek, Phys.Rev.D 100 (2019) 5, 054001)



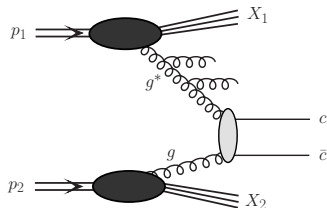
- $k_T$ -factorization:  $g^* g^* \rightarrow c\bar{c} + \text{KMR uPDF} \Rightarrow$  works very well





# Moving more forward: The hybrid factorization

How to treat theoretically the asymmetric configuration?



**The hybrid approach** for far-forward production  $\Rightarrow$

- combined collinear- and  $k_T$ -factorization
- used in many phenomenological studies
- the differential cross section for  $gg^* \rightarrow c\bar{c}$  mechanism:

$$d\sigma_{pp \rightarrow charm}(gg^* \rightarrow c\bar{c}) = \int dx_1 \int \frac{dx_2}{x_2} \int d^2 k_t$$

$$\times g(x_1, \mu^2) \cdot \mathcal{F}_g(x_2, k_t^2, \mu^2) \cdot d\hat{\sigma}_{gg^* \rightarrow c\bar{c}}$$

- $g(x_1, \mu^2) \Rightarrow$  collinear large- $x$  gluon  
we use the CT14nnlo PDF
- $\mathcal{F}_g(x_2, k_t^2, \mu^2) \Rightarrow$  off-shell small- $x$  gluon  
we use the KMR/MRW and the KS linear/nonlinear uPDFs
- $d\hat{\sigma}_{gg^* \rightarrow c\bar{c}}$  is the hard partonic cross section obtained from a gauge invariant off-shell tree-level amplitudes (available in KaTie)
- a derivation of the hybrid factorization from the dilute limit of the Color Glass Condensate approach can be found in the literature



# Charm production driven by the intrinsic charm

What if there is a non-perturbative charm content of the proton?

**The charm quark in the initial state**  $\Rightarrow$

- perturbative: extrinsic charm (from gluon splitting)
- non-perturbative: **intrinsic charm (IC)**
- the differential cross section for  $cg^* \rightarrow cg$  mechanism:

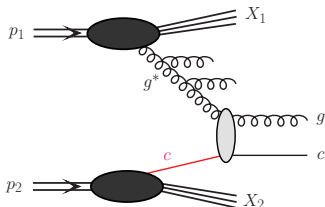
$$d\sigma_{pp \rightarrow \text{charm}}(cg^* \rightarrow cg) = \int dx_1 \int \frac{dx_2}{x_2} \int d^2 k_t$$

$$\times c(x_1, \mu^2) \cdot \mathcal{F}_g(x_2, k_t^2, \mu^2) \cdot d\hat{\sigma}_{cg^* \rightarrow cg}$$

- $c(x_1, \mu^2) \Rightarrow$  collinear charm quark PDF (large- $x$ )
- $\mathcal{F}_g(x_2, k_t^2, \mu^2) \Rightarrow$  off-shell gluon uPDF (small- $x$ )
- $d\hat{\sigma}_{cg^* \rightarrow cg} \Rightarrow$  only in the massless limit (also available in KaTie)
- regularization needed at  $p_T \rightarrow 0 \Rightarrow$  we use PYTHIA prescription:

$$F_{sup}(p_T) = \frac{p_T^2}{p_{T0}^2 + p_T^2}, \quad \alpha_S(\mu_R^2 + p_{T0}^2), \quad \text{where } p_{T0} = 1.5 \text{ GeV (free parameter)}$$

- the charm quark PDF with IC content is taken at the initial scale:  $c(x_1, \mu_0^2)$ , where  $\mu_0 = 1.3 \text{ GeV}$  so the perturbative charm contribution is intentionally not taken into account



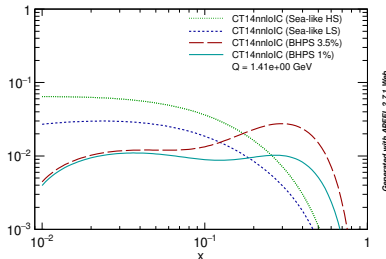
# The concept of intrinsic charm in the nucleon

The intrinsic charm quarks  $\Rightarrow$  multiple connections to the valence quarks of the proton

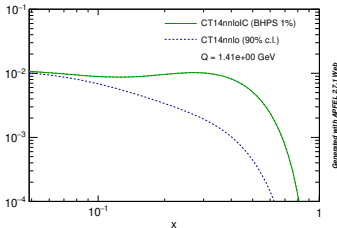
- strong evidence for internal strangeness and somewhat smaller for internal charm

- global experimental data put only loose constraints on the  $P_{ic}$  probability
- different pictures of non-perturbative  $c\bar{c}$  content:
  - sea-like models
  - valence-like models
- we use the IC distributions from the Brodsky-Hoyer-Peterson-Sakai (BHPS) model as adopted in the CT14nnloIC PDF

xc(x,Q), comparison



xc(x,Q), comparison



- the presence of an intrinsic component implies a large enhancement of the charm distribution at large  $x$  ( $>0.1$ ) in comparison to the extrinsic charm prediction
- the models do not allow to predict precisely the absolute probability  $P_{ic}$

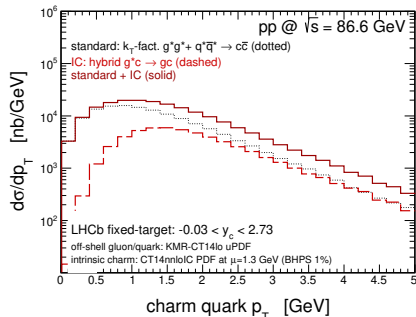
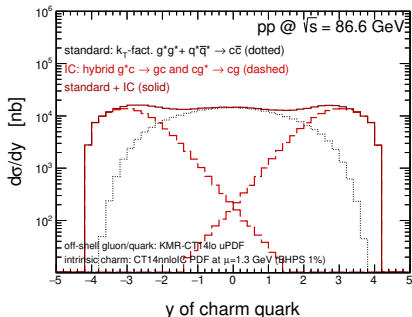


# Intrinsic charm at the LHC

A possible impact of the intrinsic charm component on the forward charm particle production in already existing or future experiments at different energies:

(R.M, A. Szczurek, JHEP 10 (2020) 135)

- Fixed-target LHCb mode at  $\sqrt{s} = 86.6$  GeV ( $D$ -meson production)



- at the lower energy  $\Rightarrow$  the intrinsic charm important already at  $|y| > 1$

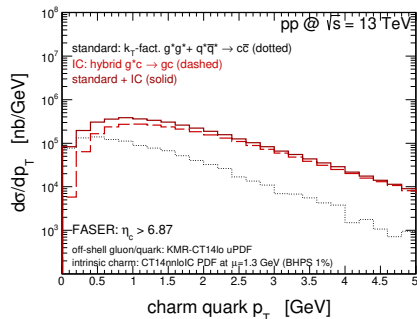
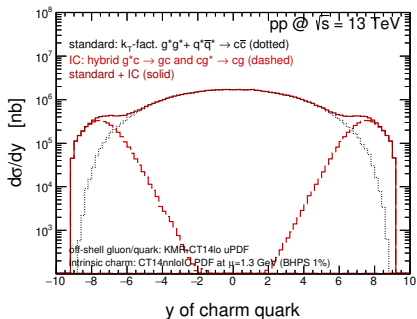


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- **FASER at the LHC** (dedicated to a measurement of forward neutrinos originating from semileptonic decays of  $D$  mesons)

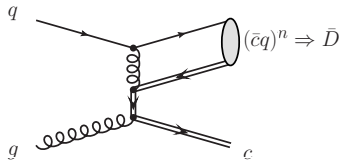


- the intrinsic charm important at  $|y| > 6$
- transverse momentum distribution visibly enhanced



# The $c\bar{q}$ -recombination mechanism of charm production

Braaten-Jia-Mechen (BJM) recombination:  $q + g \rightarrow (\bar{c}q)^n + c$



- short-distance process (in contrast with fragmentation)
- $(\bar{c}q)^n$ :  $q$  has small momentum in the  $\bar{c}$  rest frame
- $q$  and  $\bar{c}$  are in a state with definite color and angular momentum quantum numbers specified by  $n$
- direct meson:  $qg \rightarrow \bar{D}c$  and  $\bar{q}g \rightarrow D\bar{c}$
- subsequent fragmentation of the associated  $c$ -quark
- **the direct recombination leads to  $D/\bar{D}$  production asymmetry**

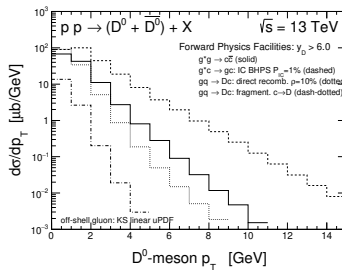
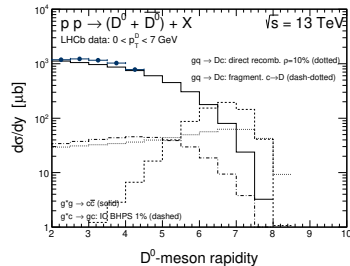
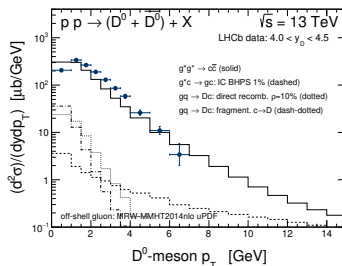
- the differential cross section for  $qg \rightarrow \bar{D}c$  mechanism:

$$\frac{d\sigma}{dy_1 dy_2 d^2 p_t} = \frac{1}{16\pi^2 \hat{s}^2} [x_1 q_1(x_1, \mu^2) x_2 g_2(x_2, \mu^2) |\overline{\mathcal{M}}_{qg \rightarrow \bar{D}c}(s, t, u)|^2 + x_1 g_1(x_1, \mu^2) x_2 q_2(x_2, \mu^2) |\overline{\mathcal{M}}_{gq \rightarrow \bar{D}c}(s, t, u)|^2]$$

- $|\overline{\mathcal{M}}_{qg \rightarrow Dc}(s, t, u)|^2 = |\overline{\mathcal{M}}_{qg \rightarrow (\bar{c}q)^n c}|^2 \cdot \rho$
- $|\overline{\mathcal{M}}_{qg \rightarrow (\bar{c}q)^n c}|^2 \Rightarrow$  explicit form of the matrix element squared available
- $\rho$  can be interpreted as a probability to form real meson  
 $\Rightarrow$  can be extracted from experimental data  
 e.g. fixed-target LHCb data on  $D/\bar{D}$  production asymmetry!



# The $c\bar{q}$ -recombination mechanism of charm production



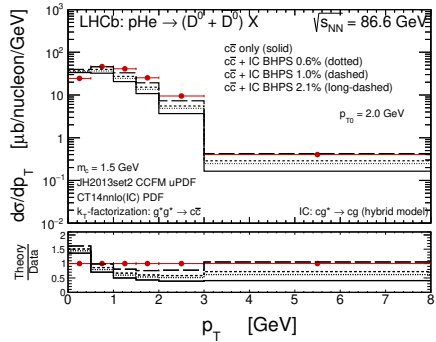
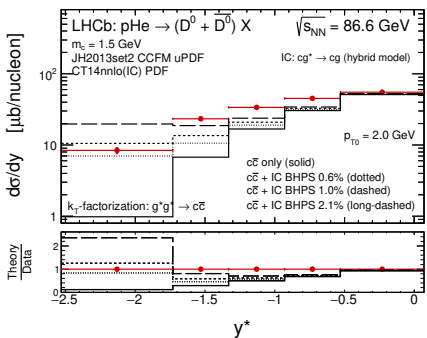
- both IC and recombination negligible at the LHCb in collider mode:  
 $\sqrt{s} = 13 \text{ TeV}, 2 < y < 4.5$
- situation changes when approaching larger rapidities
- $y > 6$ : IC dominates over the standard mechanism
- $y > 6$ : recombination and the standard mechanism of similar size



# Fixed-target charm data: Intrinsic Charm

The fixed-target data on forward open charm meson production already exists:

- Fixed-target LHCb mode at  $\sqrt{s} = 86.6$  GeV ( $D$ -meson production)



- some problems with understanding the LHCb fixed-target open charm data identified (R.M., Phys.Rev.D 102 (2020) 1, 014028)
- a new scenario proposed with the intrinsic charm contribution needed to describe the data points in the backward direction and at larger  $p_T$ 's
- $\chi^2_{\min}$ :  $P_{ic} \sim 1.65\%$  but large uncertainties  
R.M, A. Szczurek, Phys.Rev.D 105 (2022) 014001

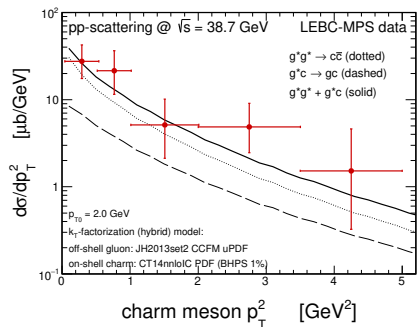
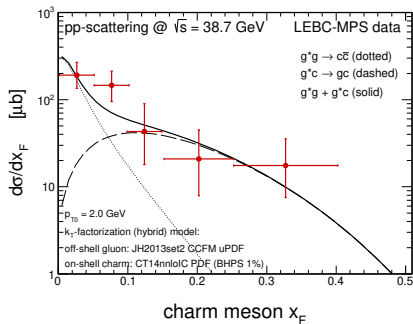




# Fixed-target charm data: Intrinsic Charm

The fixed-target data on forward open charm meson production already exists:

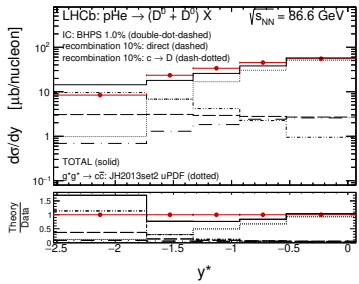
- Fermilab (1986):  $D$ -meson production in  $pp$ -scattering at  $\sqrt{s} = 38.7$  GeV



- we obtain a very good description of the  $x_F$ -distribution within our model with the same set of parameters as in the LHCb case
- the intrinsic charm component crucial for large- $x_F$  data



# Fixed-target charm data: Intrinsic Charm + Recombination

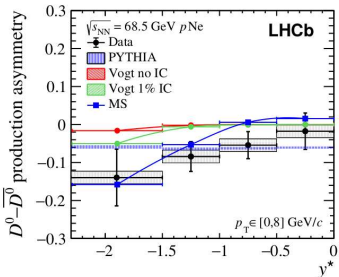
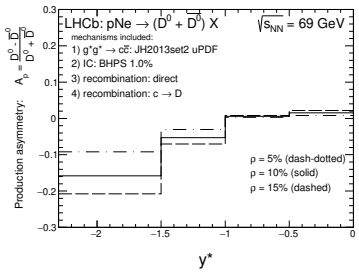


⇐ the rapidity distribution for  $D^0$ -meson:

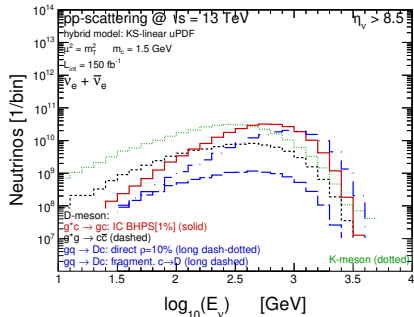
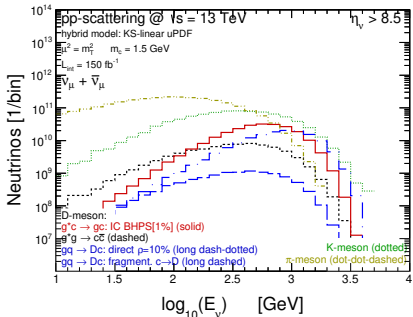
- there is a room for the recombination mechanism with  $\rho = 10\%$  together with the intrinsic charm contribution with  $P_{IC} = 1.0\%$

⇓ very recent LHCb fixed-target data on the  $D^0/\overline{D}^0$  production asymmetry: arXiv:2211.11633 [hep-ph]

- our predictions consistent with the LHCb data taking  $\rho = 10\%$ !



# FASER $\nu$ 2: Far-forward neutrino fluxes

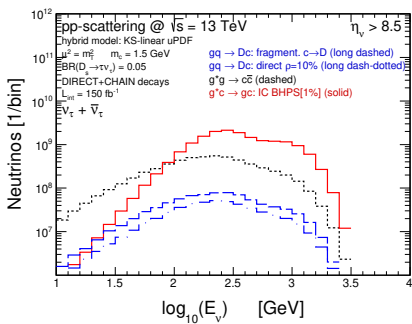


## Semileptonic decays of $D^0, D^+, \Lambda_c \Rightarrow$ source of $\nu_e, \nu_\mu$

- $E_\nu > 100$  GeV  $\Rightarrow$  intrinsic charm and recombination larger than standard mechanism
- both IC and recombination of similar size
- $\nu_\mu$ : large backgrounds from  $\pi$  and  $K$   
 $\Rightarrow$  IC and recombination completely covered even at large energies
- $\nu_e$ : large background from  $K$  but  
 $\Rightarrow$  both IC and recombination win at  $E_\nu > 1000$  GeV



# FASERν2: Far-forward neutrino fluxes

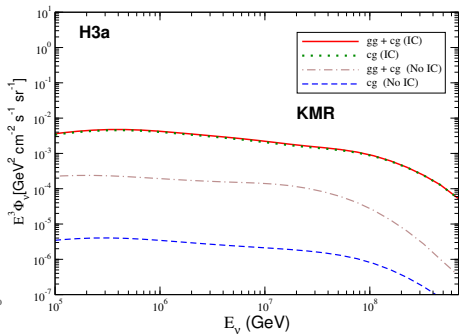
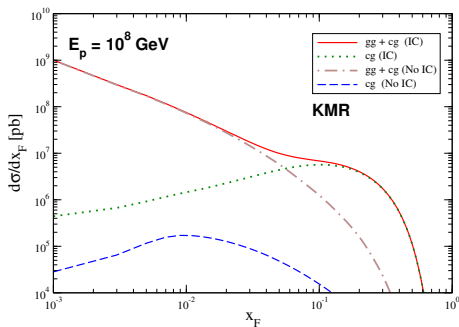


## $D_s^+$ meson decays $\Rightarrow$ dominant source of $\nu_\tau$

- direct  $D_s^+ \rightarrow \tau^+ \nu_\tau$  and chain  $D_s^+ \rightarrow \tau^+ \rightarrow \bar{\nu}_\tau$  decays
- no background from light mesons due to limited phase space for  $\tau$  production in the  $D_s$  decay
- $s(x) \ll u_{val}(x), d_{val}(x) \Rightarrow$  recombination reduced
- $E_\nu > 100$  GeV  $\Rightarrow$  intrinsic charm larger than standard mechanism
- flux dominated by intrinsic charm
- optimal to pin down the IC contribution in the nucleon



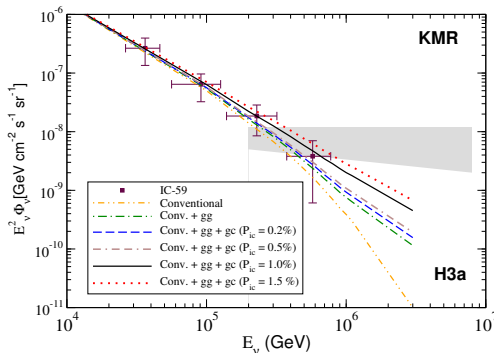
# IceCube: Prompt neutrino fluxes and intrinsic charm



- intrinsic charm very important
- extrinsic charm negligible
- the inclusion of the  $cg^* \rightarrow cg$  mechanism driven by the intrinsic charm (IC) has a strong effect on the prompt neutrino flux
- the flux is enhanced by one order of magnitude when intrinsic charm is present ( $P_{ic} = 1\%$  here)



# IceCube: Predictions and limits for intrinsic charm



- the impact of the prompt flux is small in the current kinematical range probed by IceCube as long as only the gluon-gluon fusion mechanism is taken into account
- the intrinsic charm mechanism implies a large enhancement of the prompt flux at large  $E_\nu$ , with the associated magnitude being dependent on the value of  $P_{ic}$
- linear QCD dynamics  $\Rightarrow P_{ic} \leq 1.5\%$
- similar to the central CT14nnloIC PDF set



# Conclusions

We have shown that **the intrinsic charm** and **recombination** mechanisms can be extremely important for **far-forward charm production** at the LHC and beyond:

- D-meson at fixed-target LHCb experiments
  - a scenario proposed with the intrinsic charm contribution needed to describe the data points in the backward direction and at larger  $p_T$ 's
  - extract the intrinsic charm probability  $P_{IC}$  ( $\lesssim 1\%$ )
  - still a room for recombination mechanism
  - the recombination probability from  $D/\bar{D}$ -production asymmetry ( $\approx 10\%$ )
- Neutrino fluxes at Forward Physics Facilities (FPF) at the LHC (FASER $\nu$ , FLArE)
  - both IC and recombination important
  - $\nu_e, \nu_\mu$  fluxes difficult because of large backgrounds from light mesons
  - $\nu_\tau$  flux at high energies dominated by intrinsic charm (recombination suppressed) therefore optimal to pin down the IC contribution in the nucleon
- Prompt neutrino flux at IceCube Neutrino Observatory
  - upper limit on the intrinsic charm probability  $P_{IC}$  ( $\lesssim 1\%$ )
  - next step to include recombination



Thank You!



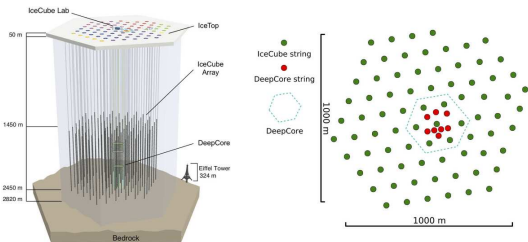


## Backup Slides



# IceCube Detector

## The detector volume is instrumented with:

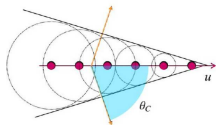


- 5160 Digital Optical Modules (DOMs)
- distributed on 86 read out and support cables ("strings")
- deployed between 1.5 and 2.5 km below the surface
- neutrino energy threshold about 10 GeV

The DOMs register the Cherenkov light emitted by relativistic charged particles passing through the detector

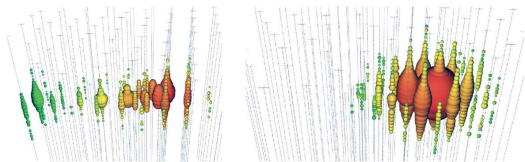
- Cherenkov light is emitted when particle velocity exceeds the speed of light in the given medium
- it is emitted by a charged particle: either prompt (like atm. muons) or resulting from neutrino interaction with ice or bedrock

Cherenkov angle:  $\cos \theta_c = 1/(\beta n)$ ,  $\theta_c = 42^\circ$  water



# Experimental signatures

There are two principle classes of Cherenkov events (**red early in time, blue late in time**):

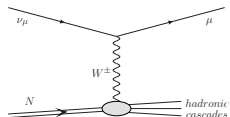


**Fig. 2** Two examples of events observed with IceCube. The left plot shows a muon track from a  $\nu_\mu$  interaction crossing the detector. Each coloured dot represents a hit DOM. The size of the dot is proportional to the amount of light detected and the colour code is related to the

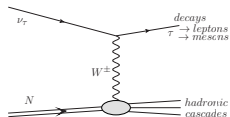
relative timing of light detection: red denotes earlier hits, blue, later hits. The right plot shows a  $\nu_e$  or  $\nu_\tau$  charged-current (or any flavour neutral-current) interaction inside the detector

- **TRACKS**: through-going track-like pattern (left panel)
- **CASCADES**: spherical light distribution (right panel)
- starting tracks (cascade + track)

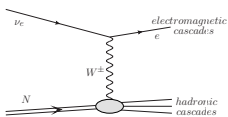
● **CC:  $\nu_\mu + N \rightarrow \mu + \text{hadrons}$  (tracks)**



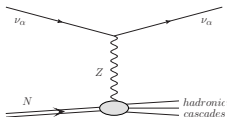
● **CC:  $\nu_\tau + N \rightarrow \tau + \text{hadrons}$  (double cascades)**



● **CC:  $\nu_e + N \rightarrow e + \text{hadrons}$  (cascades)**

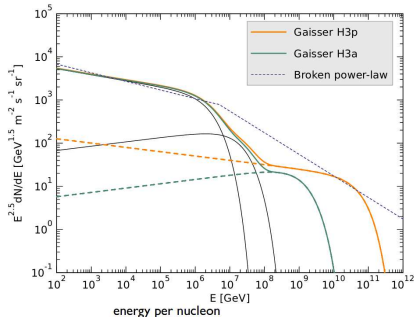
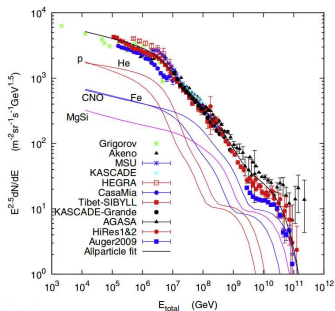


● **NC:  $\nu_\alpha + N \rightarrow \nu_\alpha + \text{hadrons}$  (cascades)**



# Initial cosmic ray (CR) flux

The energy spectra of cosmic rays on top of the Earth atmosphere



## Parametrization by Gaisser

(Gaisser, *Astropart. Phys.*35, 801 (2012))

$$\phi_i(E) = \sum_{j=1}^3 a_{i,j} E^{-\gamma_{i,j}} \times \exp\left[-\frac{E}{Z_i R_{c,j}}\right]$$

- 5 nuclei groups: H, He, CNO, Fe, MgSi
- 3 populations characterised by different rigidities (1st: supernova remnants, 2nd: higher energy galactic, 3rd: extragalactic component)
- H3a and H3p (only protons in the 3rd pop.)

## Broken power-law

$$\phi_p^0(E) = 1.7E^{-2.7} \text{ for } E < 5 \cdot 10^6 \text{ GeV}$$
$$\phi_p^0(E) = 174E^{-3} \text{ for } E > 5 \cdot 10^6 \text{ GeV}$$

- used in earlier works
- overestimates the highest energies



# Development of air-showers and lepton fluxes

Next step: **Simulation of the propagation of high energy particles and their decay products through the atmosphere**

- The aim is to solve a series of coupled differential equations dependent on **the slant depth**  $X(l, \theta)$  measuring the amount of atmosphere traversed by a particle:

$$X(l, \theta) \equiv \int_l^\infty \rho[h(l', \theta)] dl',$$

where  $\rho$  is the density of the atmosphere dependent on the distance from the ground  $l$  (along the particle trajectory) as well as on the zenith angle  $\theta$

- **an isothermal model of the atmosphere**  $\Rightarrow$  appropriate for atmospheric depths 10–40 km within which the bulk of particle production occurs:

$$\rho(h) = \rho_0 \exp(-h/h_0), \quad \rho_0 = 2.03 \times 10^{-3} \text{ gm cm}^{-3}, \quad h_0 = 6.4 \text{ km}.$$

- the horizontal depth of the atmosphere is  $X \simeq 3.6 \times 10^4 \text{ gm cm}^{-2}$  while its vertical depth is  $\simeq 1.3 \times 10^3 \text{ gm cm}^{-2}$  (values which adequately describe the density of the stratosphere)
- concerning the atmospheric composition, a good approximation, valid up to a height of 100 km, is 78.4% nitrogen, 21.1% oxygen and 0.5% argon. This leads to an average atomic number of  $\langle A \rangle = 14.5$

for a detailed discussion of the cascade formalism see e.g. R. Gauld et al., JHEP (2016) 130, or M. Thunman, G. Ingelman, P. Gondolo, Astropart.Phys. 5 (1996) 309-332



# Development of air-showers and lepton fluxes

The solution of these equations is in general quite involved (Monte Carlo methods needed)

- but there are simple (approximate) asymptotic analytic solutions  $\Rightarrow$

The equation for the proton flux can be trivially integrated to give

$$\phi_p(E, X) = \phi_p^{(0)}(E) \exp(-X/\Lambda_p(E)) ,$$

where  $\Lambda_p(E) \equiv \lambda_p(E)/(1 - Z_{pp}(E))$  is the nucleon attenuation length that depends in general on the nucleon's interaction length in the atmosphere:  $\lambda_p(E) = \langle A \rangle / N_0 \sigma_{pA}(E)$ , where  $\langle A \rangle = 14.5$  is the average atomic number of air molecules,  $N_0$  is Avogadro's number, and the total inelastic proton-air cross-section is denoted by  $\sigma_{pA}$ .

Then, the meson flux in the two asymptotic regions reads:

- at low energies the interaction and regeneration terms neglected

$$\phi_m^{\text{low}}(E) = \phi_p^{(0)}(E) \frac{Z_{pm}(E)}{\Lambda_p(1 - Z_{pp})} \rho_{dm} e^{-X/\Lambda_p}$$

- at high energies the decay terms neglected

$$\phi_m^{\text{high}}(E) = \phi_p^{(0)}(E) \frac{Z_{pm}(E)}{(1 - Z_{pp})} \frac{(e^{-X/\Lambda_m} - e^{-X/\Lambda_p})}{1 - \Lambda_p/\Lambda_m}$$



# Development of air-showers and lepton fluxes

The final vertical flux of leptons expected at the detector:

$$\phi_{l,m}^{\text{low}}(E) = \phi_p^{(0)}(E) \frac{Z_{pm}(E)}{1 - Z_{pp}} Z_{ml}^{\text{low}}(E) \quad E < \epsilon_m$$

$$\phi_{l,m}^{\text{high}}(E) = \phi_p^{(0)}(E) \frac{\epsilon_m}{E} \frac{Z_{pm}(E)}{1 - Z_{pp}} \frac{\ln(\Lambda_m/\Lambda_p)}{1 - \Lambda_p/\Lambda_m} Z_{ml}^{\text{high}}(E) \quad E > \epsilon_m$$

where  $\epsilon_m$  is a critical energy below which the probability of a meson to decay is greater than it is to interact:

$$\epsilon_m = \frac{m_m c^2 h_0}{c \tau_m \cos \theta} \simeq 3.7 - 9.5 \times 10^7 \text{ GeV}$$

- the smaller the critical energy, the longer the decay length, hence the more energy the particle will lose by interactions in the atmosphere before it actually decays.

**The final step in solving the cascade equations in the Z-moment approach is the geometrical interpolation of the low- and high-energy asymptotic solutions:**

$$\phi_l(E) = \sum_m \frac{\phi_{l,m}^{\text{low}}(E) \times \phi_{l,m}^{\text{high}}(E)}{\phi_{l,m}^{\text{low}}(E) + \phi_{l,m}^{\text{high}}(E)}$$

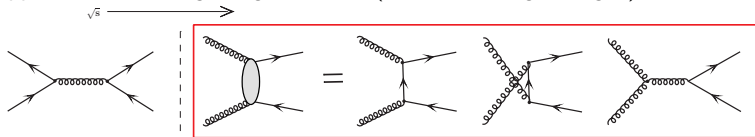
- sum over mesons contributing to the prompt flux (the leptonic decays of):  $D^0$ ,  $\bar{D}^0$ ,  $D^\pm$ ,  $D_s^\pm$  and  $\Lambda_c^\pm$



# Charm cross section in QCD

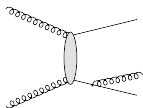
The basic ingredient for the prompt neutrino flux  $\Rightarrow$  **pQCD charm quark production**

- the **leading-order (LO)** partonic processes for  $Q\bar{Q}$  production  $\Rightarrow$   $q\bar{q}$ -annihilation and gluon-gluon fusion (dominant at high energies)

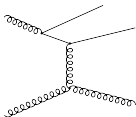


- main classes of the **next-to-leading order (NLO)** diagrams:

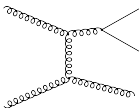
pair creation  
with gluon emission



flavour excitation



gluon splitting



the NLO and the NNLO corrections  
of a special importance for charm  
 $p_T$ -differential cross section!

**collinear approach:**

- state of the art for single particle spectra at NLO (FONLL, GM-VFNS)
- MC@NLO+PS for correlations
- NNLO not available for charm/bottom

**$k_T$ -factorization (high-energy factorization):**

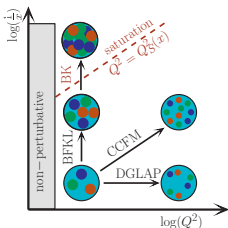
- exact kinematics from the very beginning
- correlation observables directly calculable
- some contributions even beyond the NLO available (also differentially)

prompt neutrino flux  $\Rightarrow$  high energy limit and far-forward charm production





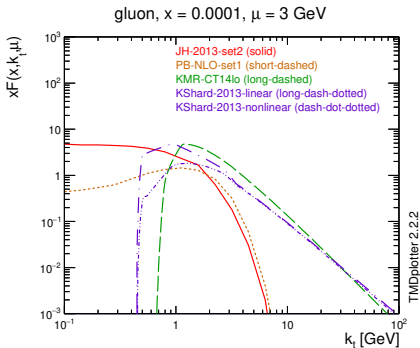
# Unintegrated parton distribution functions (uPDFs)



## Transverse momentum dependent PDFs: $\mathcal{F}_g(x, k_t^2, \mu)$

- CCFM evolution: Jung-Hautmann (JH2013)
- Parton Branching + DGLAP: Bermudez Martinez-Connor-Jung-Lelek-Zlebcik
- linear/nonlinear BK (saturation): Kutak-Sapeta (KS)
- modified DGLAP-BFKL: Kimber-Martin-Ryskin-Watt (KMR, MRW)
- modified BFKL-DGLAP: Kwieciński-Martin-Staśto (KMS)

- hard emissions from the uPDF  $\Rightarrow$  resummation of higher-order corrections
- $k_T$ -fact.  $g^* g^* \rightarrow c\bar{c} + \text{KMR uPDF}$  works very well for inclusive open charm and bottom mesons at the LHC (as well as for correlation observables)
- saturation effects possible to be studied within the KS uPDF
- open charm at the LHC: small- $x$  and small/intermediate scales



# The quark to meson transition

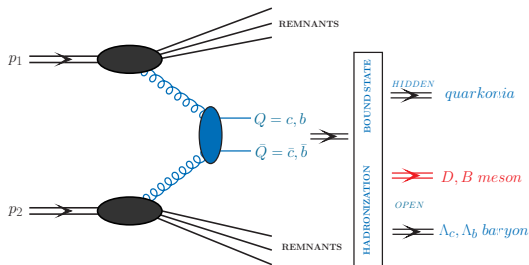
## Heavy quark to open heavy meson fragmentation: $c \rightarrow D$ and $\bar{c} \rightarrow \bar{D}$

The independent parton fragmentation picture:

- the charmed meson  $x_F$ -distributions at large  $x_F$  can be obtained from the charm quark/antiquark  $x_F^c$ -distributions as:

$$\frac{d\sigma_{pp \rightarrow D}(x_F)}{dx_F} = \int_{x_F}^1 \frac{dz}{z} \frac{d\sigma_{pp \rightarrow \text{charm}}(x_F^c)}{dx_F^c} D_{c \rightarrow D}(z),$$

- where  $x_F^c = x_F/z$  and  $D_{c \rightarrow D}(z)$  is the relevant fragmentation function (FF)
- the fragmentation procedure leads to a decrease of the  $x_F$  range for meson with respect to  $x_F^c$  of the parent quark



- $c \rightarrow D$ : Peterson( $z$ ),  $\epsilon = 0.05$  (well known from  $e^+e^-$  data)
- $\eta_D = \eta_c$ ,  $x_F = z \cdot x_F^c$ ,  $z \in (0, 1)$
- fragmentation fractions well known (Particle Data Group)

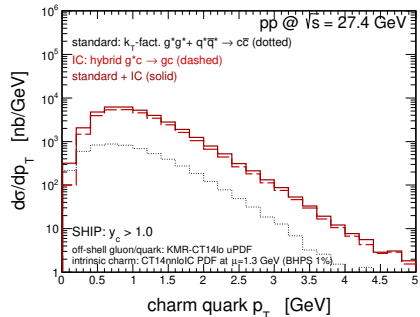
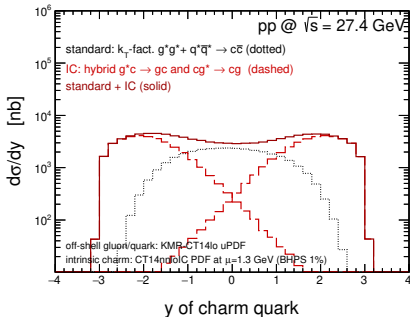


# Intrinsic charm at the LHC and beyond

A possible impact of the intrinsic charm component on the forward charm particle production in already existing or future experiments at different energies:

(R.M, A. Szczurek, JHEP 10 (2020) 135)

- **SHIP at the SPS CERN at  $\sqrt{s} = 27.4$  GeV** (dedicated to a measurement of forward  $\nu_\tau$  neutrinos originating from semileptonic decays of  $D_s$  mesons)



- at the lower energy  $\Rightarrow$  the intrinsic charm important in the whole rapidity spectrum
- transverse momentum distribution visibly enhanced

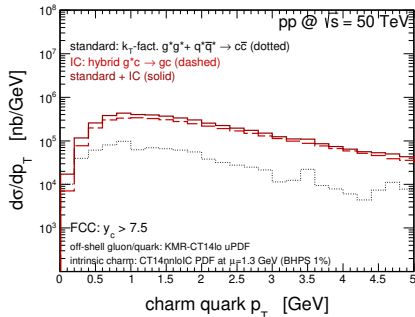
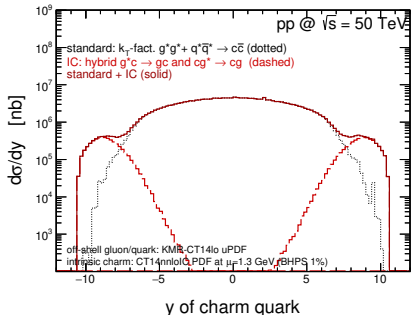


# Intrinsic charm at the LHC and beyond

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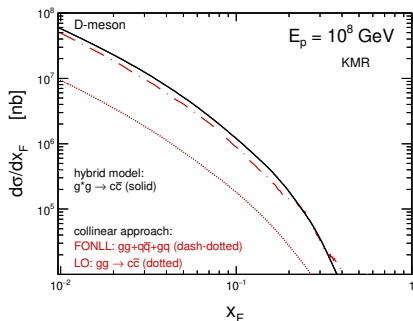
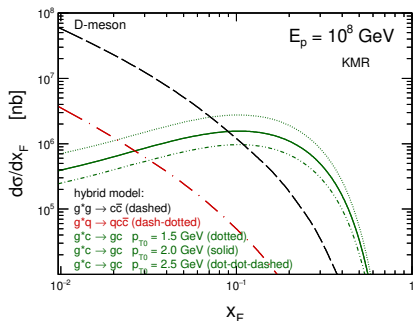
- **Future Circular Collider (FCC) (*D*-meson production)**



- the intrinsic charm important at  $|y| > 7$
- transverse momentum distribution visibly enhanced



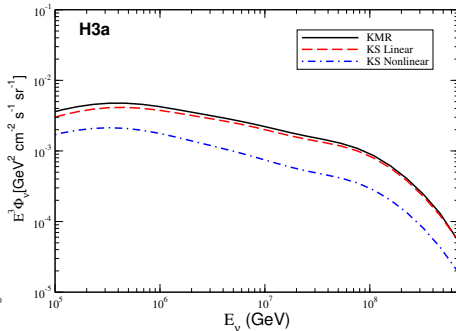
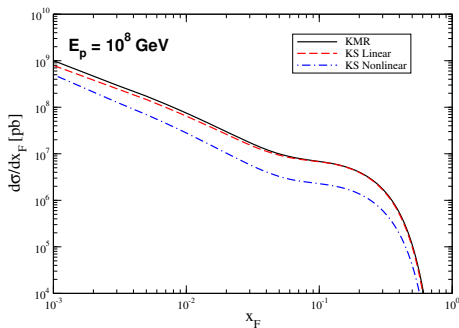
# Predictions of our model for charm $x_F$ -distributions



- when intrinsic charm is included the behavior of the  $x_F$ -distribution is strongly modified in the  $0.03 \leq x_F \leq 0.6$  range
- the Feynman  $x_F$ -distribution for large  $x_F$  is dominated by the  $cg^* \rightarrow cg$  mechanism with intrinsic charm
- our predictions for the standard charm production mechanism obtained with the hybrid model are consistent with the NLO collinear calculations by FONLL



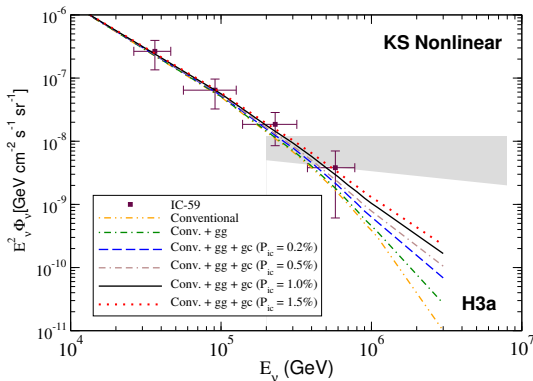
# Prompt neutrino fluxes and saturation effects



- sum of both production mechanisms:  $gg^*$ -fusion and the  $cg^*$  with IC BHPS 1%
- the KMR and KS linear predictions are similar  
⇒ BFKL effects not important for IceCube (which probes  $0.2 < x_F < 0.5$ )
- the KS nonlinear is a factor  $\approx 3$  smaller for  $x_F = 0.2$   
⇒ saturation effects strongly modifies the magnitude of the distribution



# Predictions and IceCube limits including saturation



- within the saturation scenario the impact of the prompt flux driven by the gluon-gluon fusion mechanism is even smaller and becomes negligible
- nonlinear QCD dynamics  $\Rightarrow P_{ic} \leq 2.0\%$
- slightly higher than the central CT14nnloIC PDF set

