

Recent developments in the spectroscopy of open charm mesons

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Colour meets Flavour: Quantum Chromodynamics and Quark Flavour Physics Khodjamirian Fest

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Open charm/beauty states

- $D_0(2308)$, $D'_1(2440)$
- $D_{s0}^*(2317)$, $D'_{s1}(2460)$
- $D(2550)$, $D(2600)$, $D(2750)$, $D(2760)$
- $D_{sJ}(2632)$
- $D_{sJ}(2860)$, $D_{sJ}(2710)$, $D_{sJ}(3040)$

- $B_1(5734)$, $B_2^*(5738)$
- $B_{s1}(5830)$, $B_{s2}^*(5840)$

Open charm/beauty states

- $D_0(2308)$, $D'_1(2440)$
- $D_{s0}^*(2317)$, $D'_{s1}(2460)$
- $D(2550)$, $D(2600)$, $D(2750)$, $D(2760)$
- ~~$D_{sJ}(2632)$~~ \longrightarrow Seen only by SELEX, never confirmed
- $D_{sJ}(2860)$, $D_{sJ}(2710)$, $D_{sJ}(3040)$

- $B_1(5734)$, $B_2^*(5738)$
- $B_{s1}(5830)$, $B_{s2}^*(5840)$

Open charm/beauty states

- $D_0(2308)$, $D'_1(2440)$

- $D_{s0}^*(2317)$, $D'_{s1}(2460)$

- $D(2550)$, $D(2600)$, $D(2750)$, $D(2760)$

- ~~$D_{sJ}(2632)$~~ \longrightarrow Seen only by SELEX, never confirmed

- $D_{sJ}(2860)$, $D_{sJ}(2710)$, $D_{sJ}(3040)$

- $B_1(5734)$, $B_2^*(5738)$

- $B_{s1}(5830)$, $B_{s2}^*(5840)$

Hadrons containing a single heavy quark Q

Spin of the heavy quark and of the light degrees of freedom decoupled in the $m_Q \rightarrow \infty$ limit

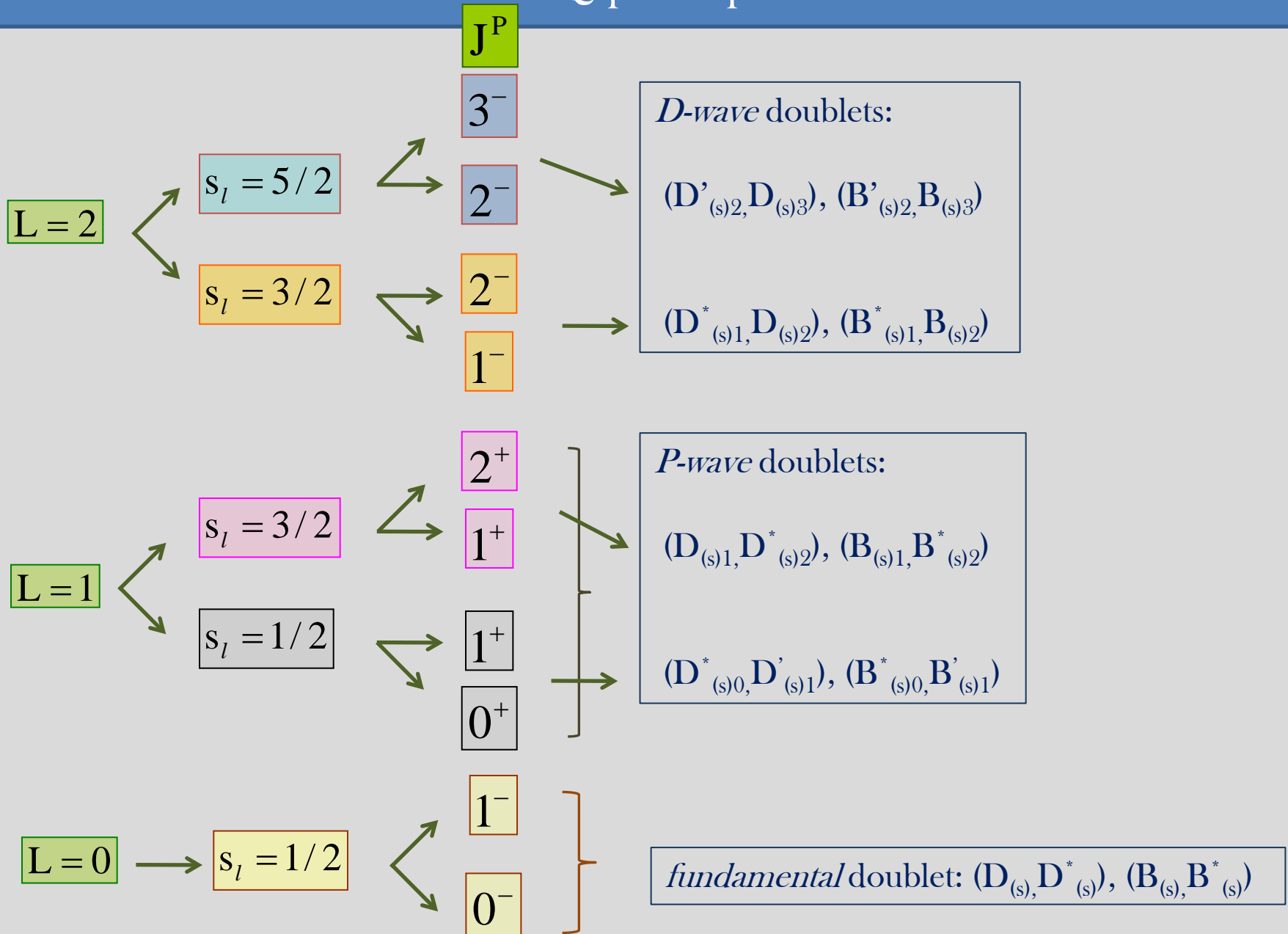
$$\vec{J}_M = \vec{s}_\ell + \vec{s}_Q \quad \text{spin}$$

$$\vec{s}_\ell = \vec{L} + \vec{s}_q \quad \text{angular momentum of the light degrees of freedom (conserved)}$$

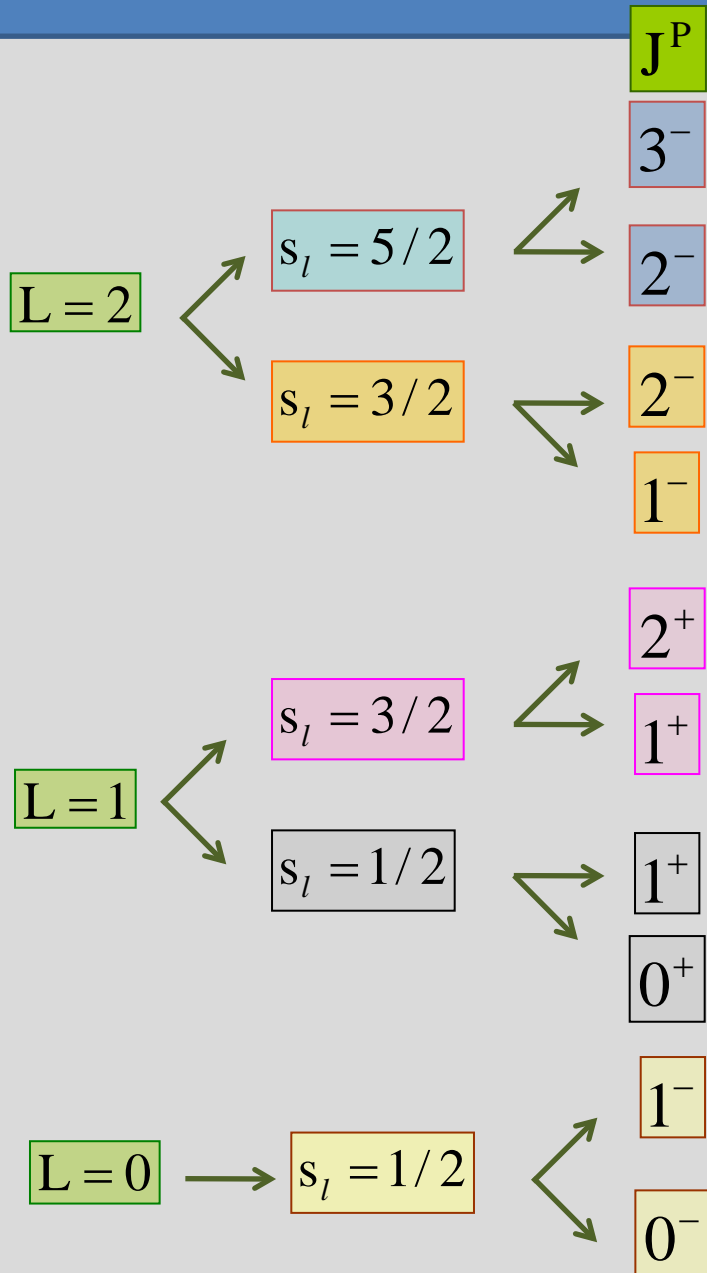
Mesons classified as doublets

- In the HQ limit:
 - states with the same s_f^P degenerate
- finite m_Q corrections
 - remove degeneracy between the states of the same doublet
 - induce mixing between states with the same J^P

Qq̄ multiplets



Qq̄ multiplets

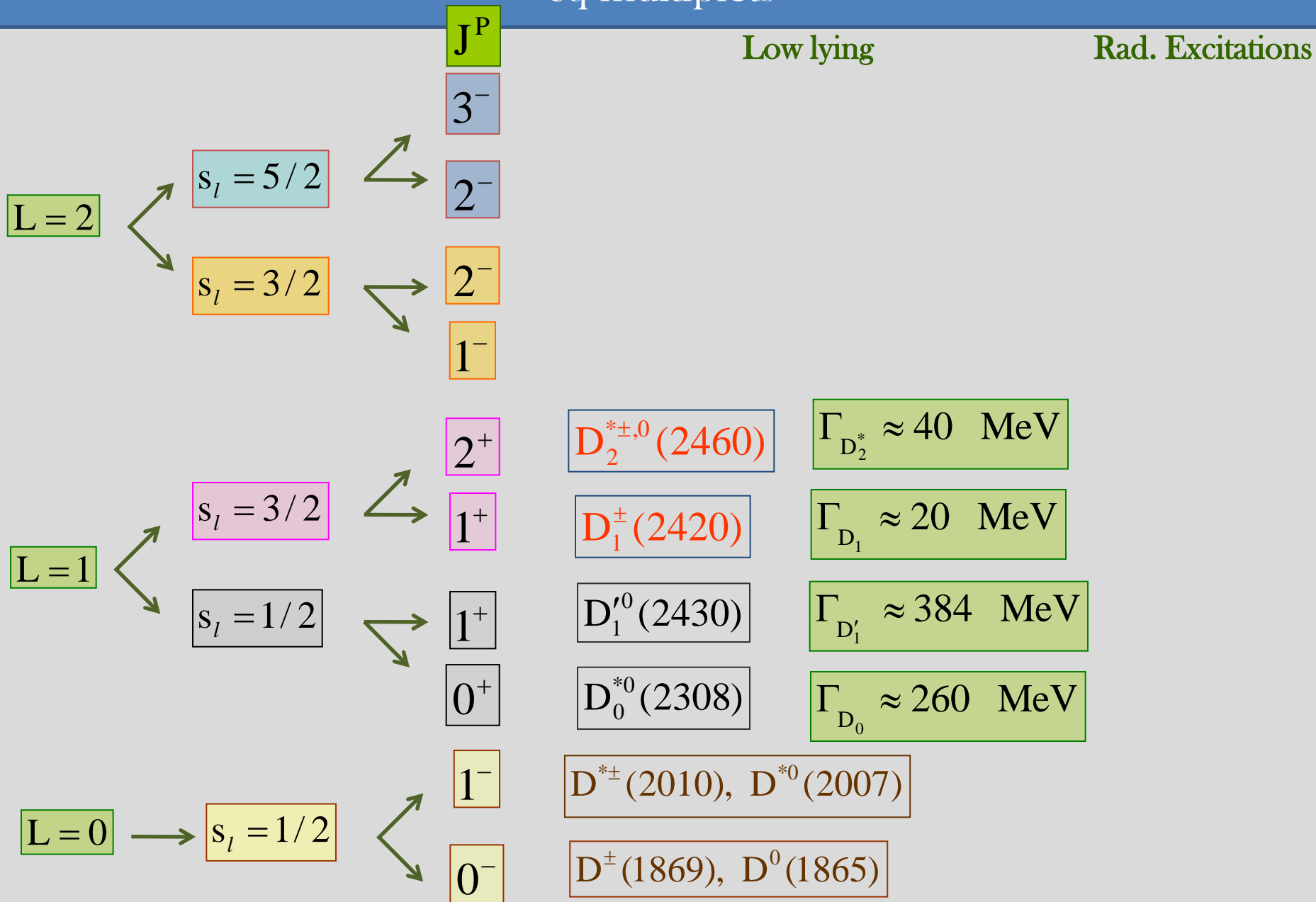


Strong transitions between multiplets

$\frac{3^+}{2} \rightarrow \frac{1^-}{2} + \text{pseudoscalar meson}$
 d-wave transition
 $\frac{3^+}{2}$ mesons are expected to be narrow

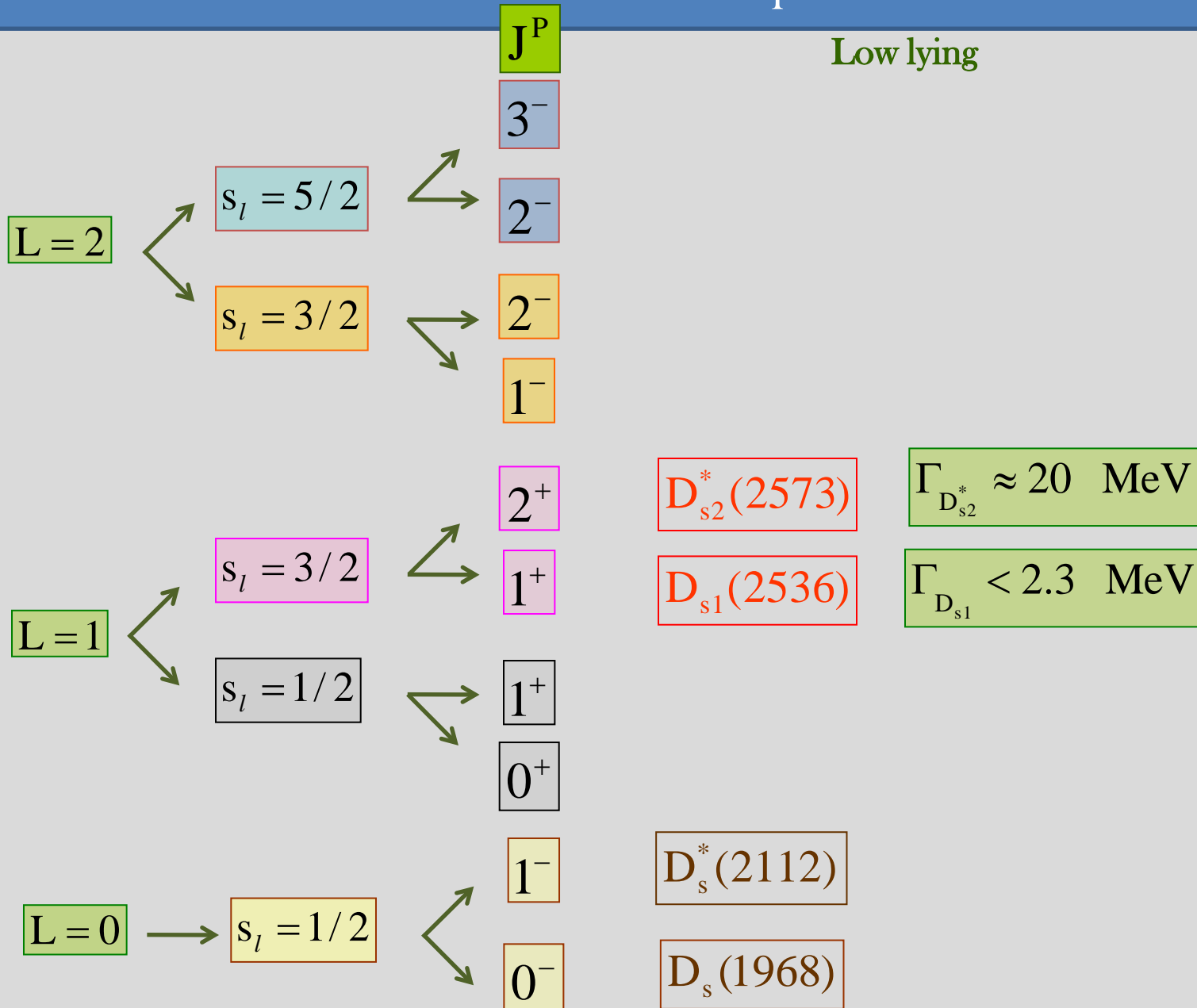
$\frac{1^+}{2} \rightarrow \frac{1^-}{2} + \text{pseudoscalar meson}$
 s-wave transition
 $\frac{1^+}{2}$ mesons are expected to be **broad**

$c\bar{q}$ multiplets



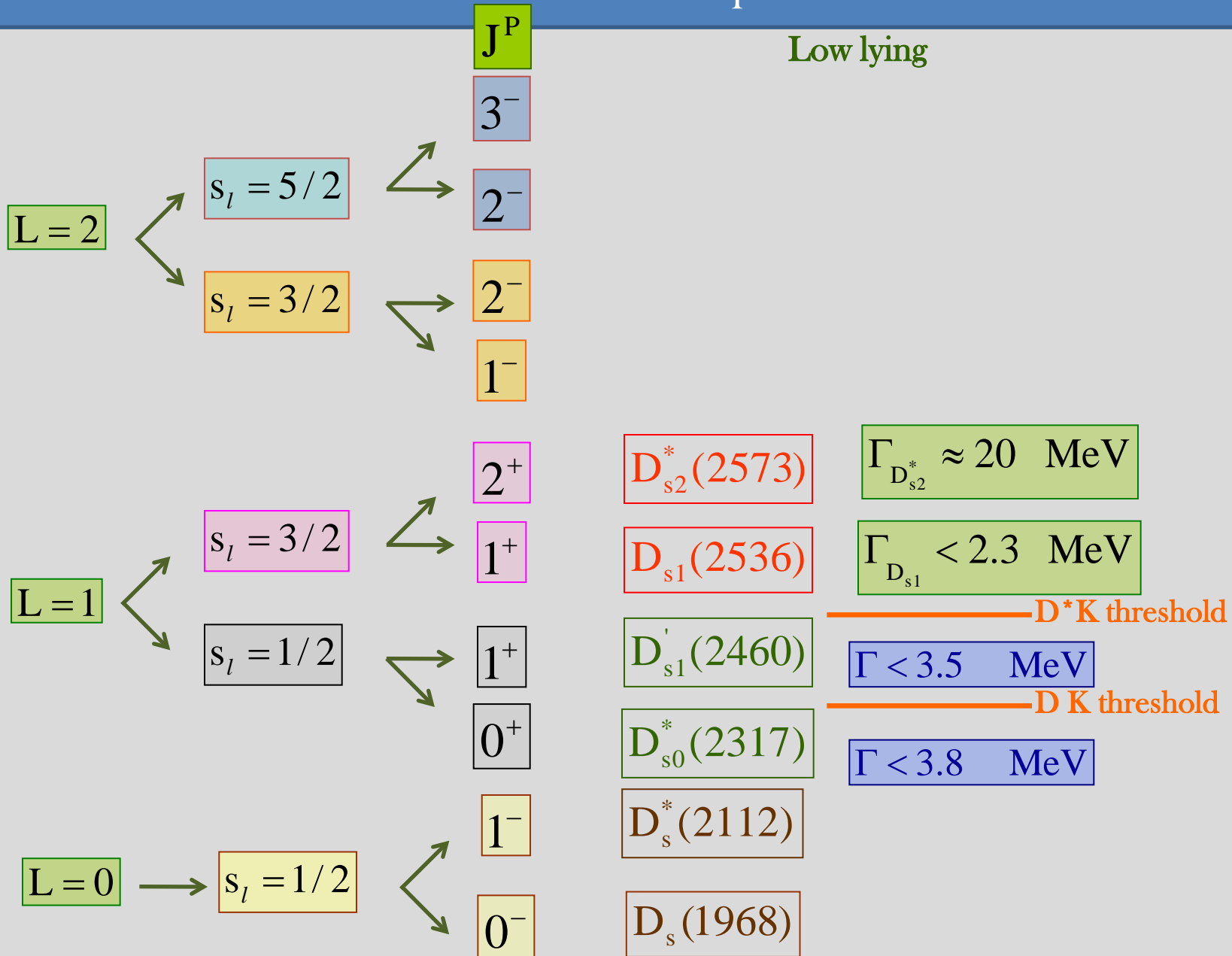
$c\bar{s}$ multiplets

Low lying



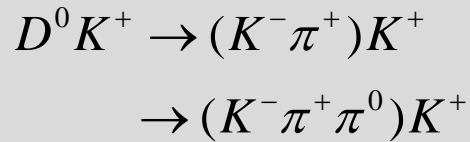
$c\bar{s}$ multiplets

Low lying

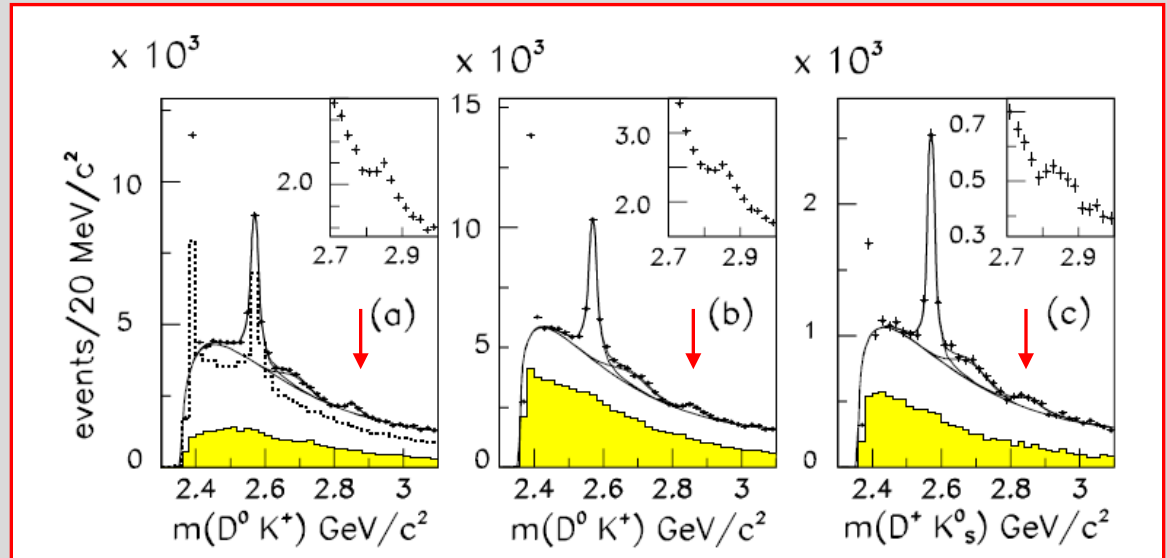


$D_{sJ}(2860)$

- Discovered by BaBar Collab.
- Reconstructed in



and in $D^+ K_S^0$



$$M = 2856.6 \pm 1.5 \pm 5.0 \quad \text{MeV}$$

$$\Gamma = 48 \pm 7 \pm 10 \quad \text{MeV}$$

BaBar Collab., PRL 97 (06) 222001

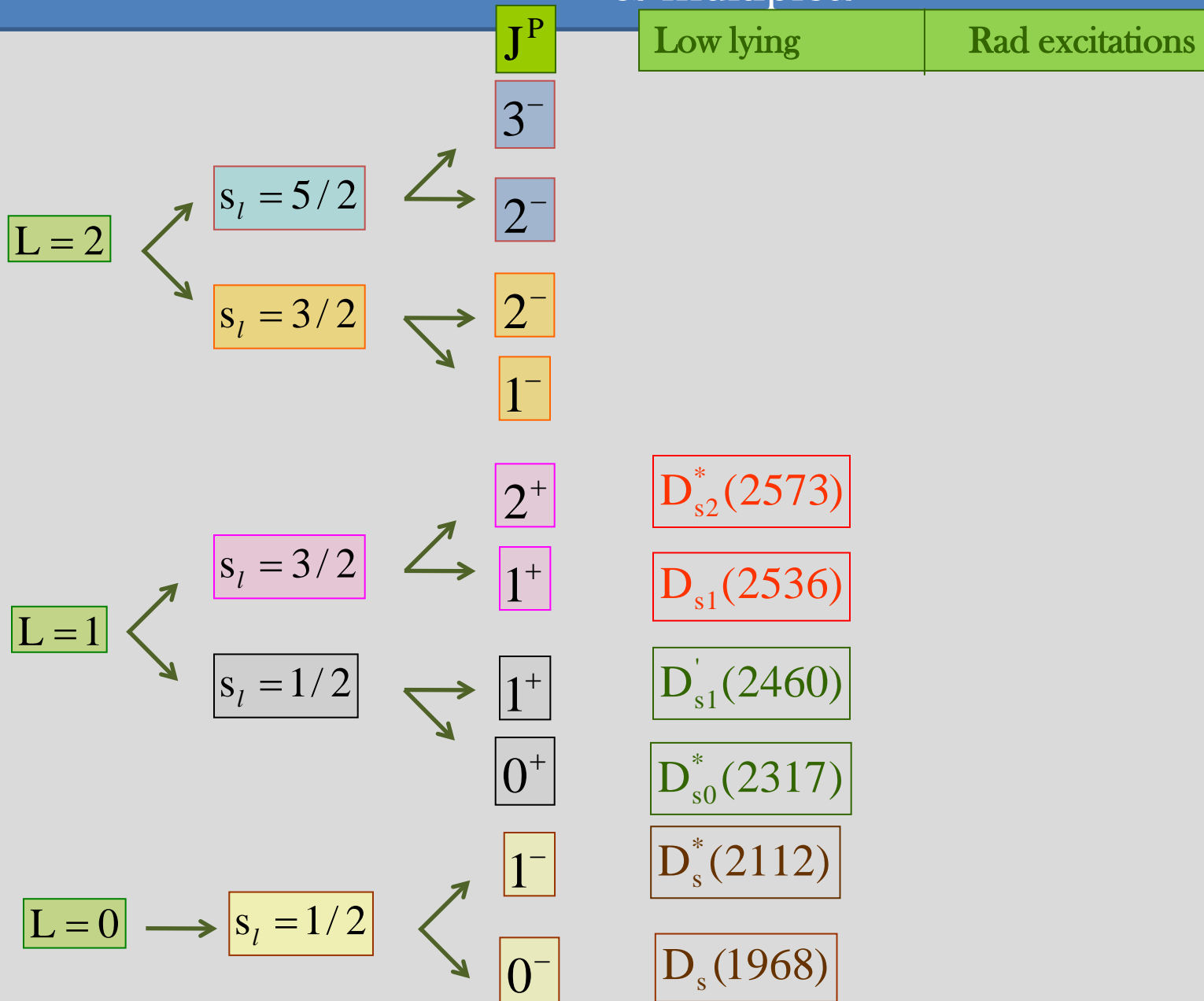
Quantum number assignment required in order to identify it

Possibilities: - low lying state not yet observed

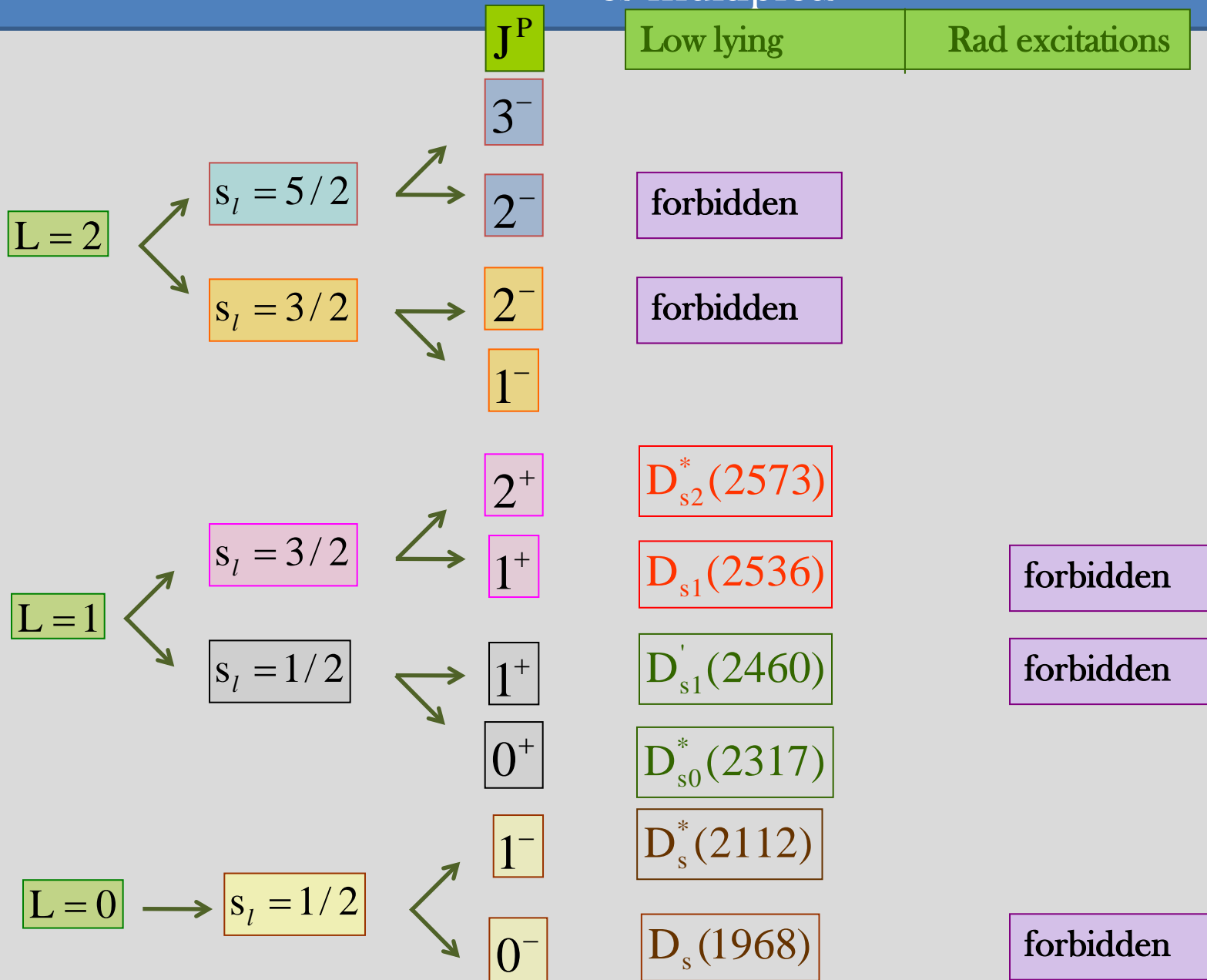
- radial excitation of an already observed state

Only states that can decay to the observed mode **DK** are allowed

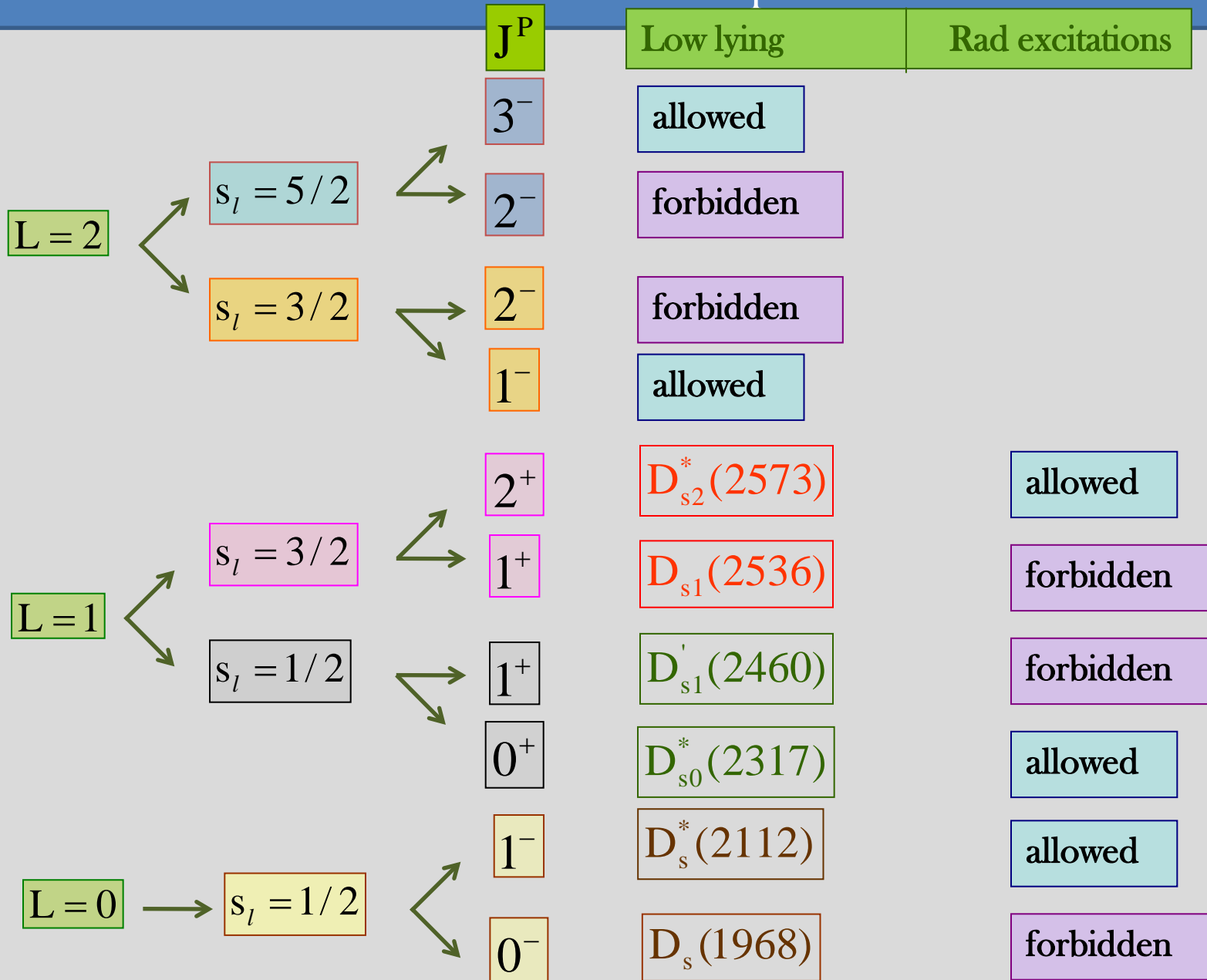
$c\bar{s}$ multiplets



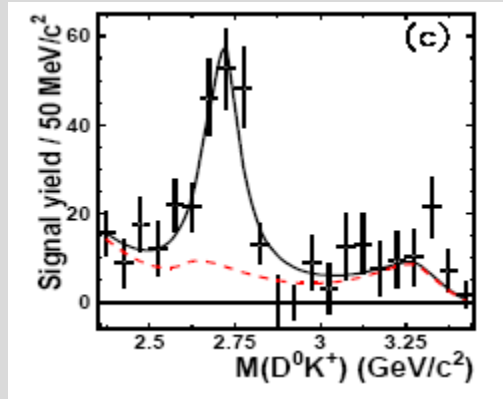
$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



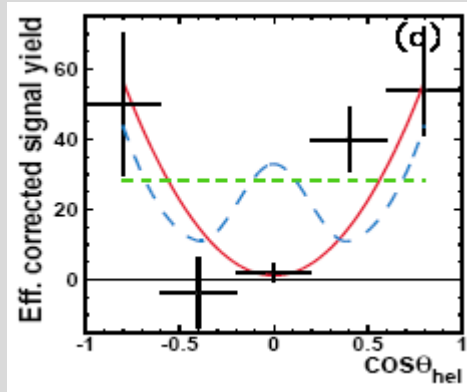
Belle Collab.: analysis of the mode



New resonance decaying to $D^0 K^+$ with:

$$M = 2708 \pm 9 \pm_{10}^{11} \text{ MeV} \quad \Gamma = 108 \pm 23 \pm_{31}^{36} \text{ MeV}$$

$1^- \rightarrow 0^- 0^-$ implies $P=-1$

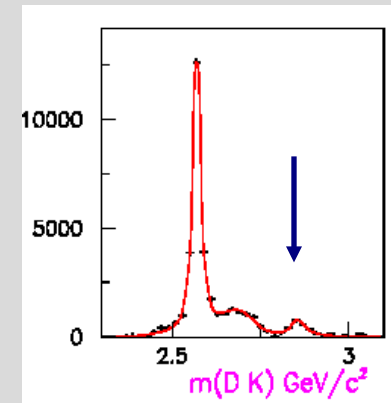


- - - $J=0$
 — $J=1$
 - - - $J=2$

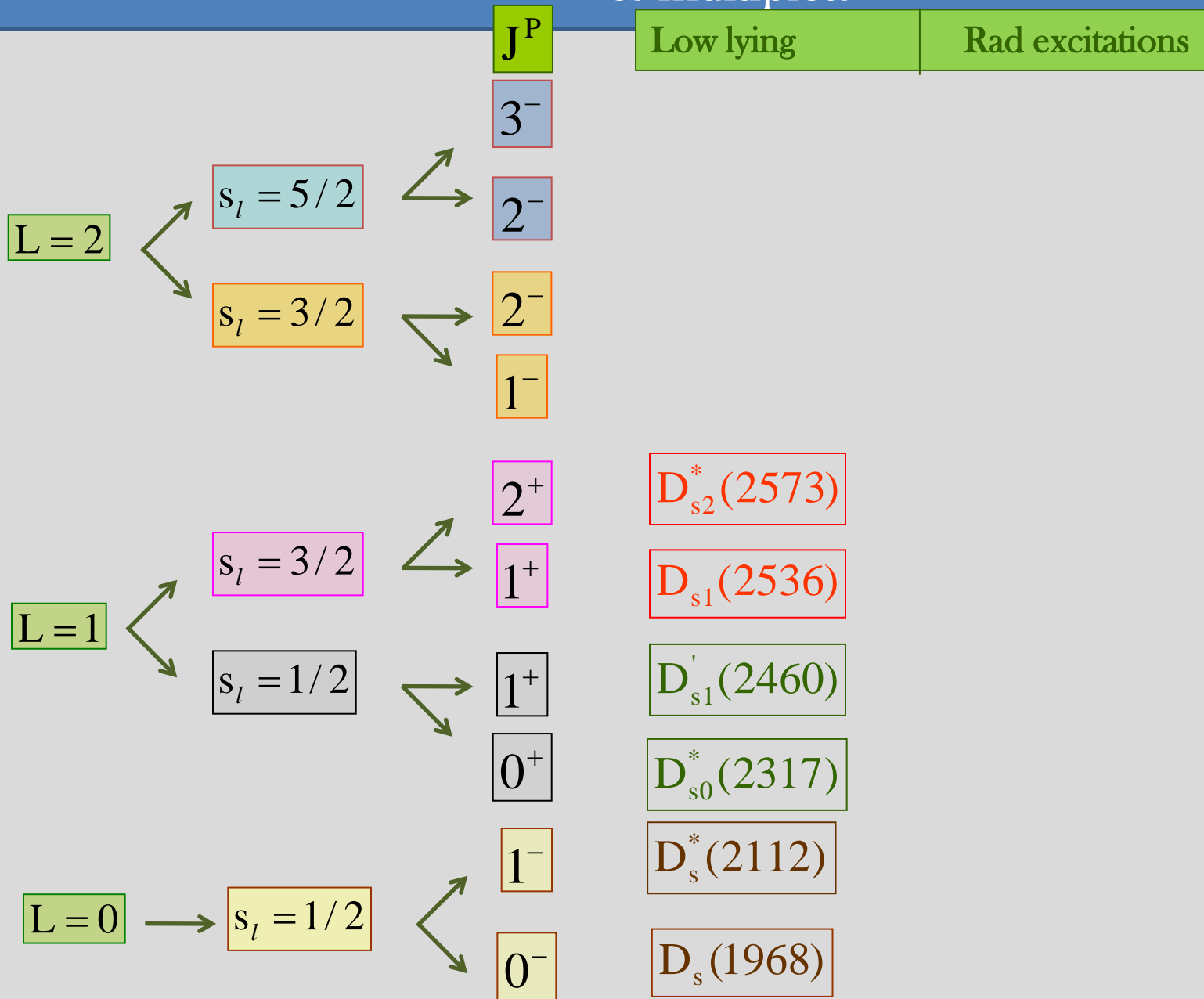


$J^P=1^-$ favoured

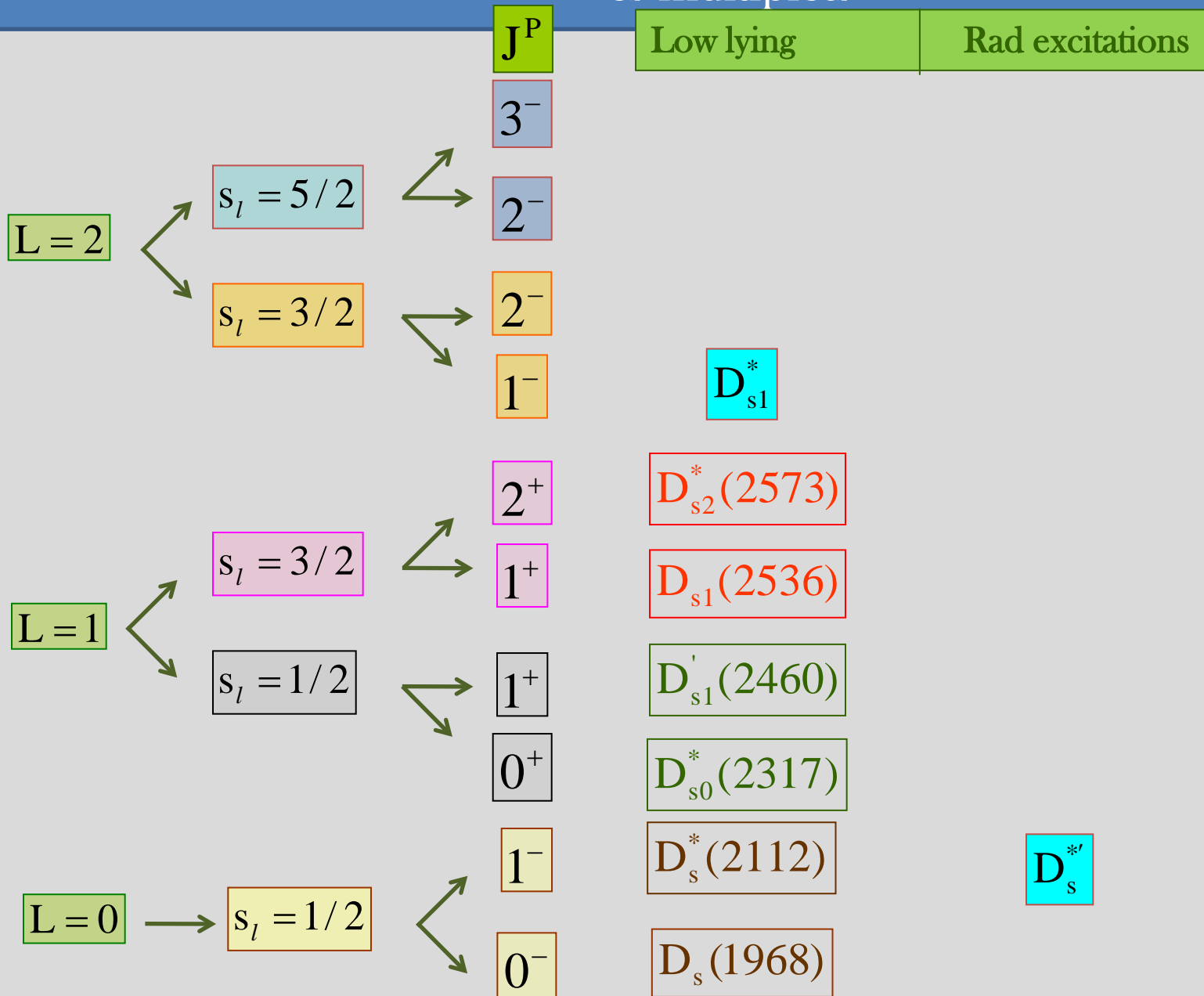
A broad structure at $M=2688 \text{ MeV}$ with $\Gamma=112 \text{ MeV}$ was found by BaBar in the DK mass distribution



$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



$D_{sJ}(2860)$ & $D_{sJ}(2710)$

predictions on allowed decay rates can help to distinguish among the various possibilities

HQ limit: the members of the doublets are described by effective fields:

L=0	{	$S_\ell^P = \frac{1^-}{2}$	$H_a = \frac{1 + \not{v}}{2} [P_{a\mu}^* \gamma^\mu - P_a \gamma_5]$
L=1	{	$S_\ell^P = \frac{1^+}{2}$	$S_a = \frac{1 + \not{v}}{2} [P_{1a}^{\prime\mu} \gamma_\mu \gamma_5 - P_{0a}^*]$
	{	$S_\ell^P = \frac{3^+}{2}$	$T_a^\mu = \frac{1 + \not{v}}{2} \left\{ P_{2a}^{\mu\nu} \gamma_\nu - P_{1av} \sqrt{\frac{3}{2}} \gamma_5 \left[g^{\mu\nu} - \frac{1}{3} \gamma^\nu (\gamma^\mu - v^\mu) \right] \right\}$
L=2	{	$S_\ell^P = \frac{3^-}{2}$	$X_a^\mu = \frac{1 + \not{v}}{2} \left\{ P_{2a}^{*\mu\nu} \gamma_5 \gamma_\nu - P_{1av}^{*'} \sqrt{\frac{3}{2}} \left[g^{\mu\nu} - \frac{1}{3} \gamma^\nu (\gamma^\mu - v^\mu) \right] \right\}$
	{	$S_\ell^P = \frac{5^-}{2}$	$X_a^{\prime\mu\nu} = \frac{1 + \not{v}}{2} \left\{ P_{3a}^{\mu\nu\sigma} \gamma_\sigma - P_{2a}^{*'\alpha\beta} \sqrt{\frac{5}{3}} \gamma_5 \left[g_\alpha^\mu g_\beta^\nu - \frac{1}{5} \gamma_\alpha g_\beta^\nu (\gamma^\mu - v^\mu) - \frac{1}{5} \gamma_\beta g_\alpha^\mu (\gamma^\nu - v^\nu) \right] \right\}$

D_{sJ}(2860) & D_{sJ}(2710)

Interactions with the emission of a light pseudoscalar meson described by effective Lagrangian terms

$$\mathcal{L}_H = g \text{Tr}[\bar{H}_a H_b \gamma_\mu \gamma_5 \mathcal{A}_{ba}^\mu], \quad \mathbf{H} \longrightarrow \mathbf{H} \pi$$

$$\mathcal{L}_S = h \text{Tr}[\bar{H}_a S_b \gamma_\mu \gamma_5 \mathcal{A}_{ba}^\mu] + \text{h.c.}, \quad \mathbf{S} \longrightarrow \mathbf{H} \pi$$

$$\mathcal{L}_T = \frac{h'}{\Lambda_\chi} \text{Tr}[\bar{H}_a T_b^\mu (i D_\mu \mathcal{A} + i \not{D} \mathcal{A}_\mu)_{ba} \gamma_5] + \text{h.c.}, \quad \mathbf{T} \longrightarrow \mathbf{H} \pi$$

$$\mathcal{L}_X = \frac{k'}{\Lambda_\chi} \text{Tr}[\bar{H}_a X_b^\mu (i D_\mu \mathcal{A} + i \not{D} \mathcal{A}_\mu)_{ba} \gamma_5] + \text{h.c.}, \quad \mathbf{X} \longrightarrow \mathbf{H} \pi$$

$$\mathcal{L}_{X'} = \frac{1}{\Lambda_\chi^2} \text{Tr}[\bar{H}_a X_b'^{\mu\nu} \{k_1 \{D_\mu, D_\nu\} \mathcal{A}_\lambda + k_2 (D_\mu D_\nu \mathcal{A}_\lambda + D_\nu D_\lambda \mathcal{A}_\mu)\}_{ba} \gamma^\lambda \gamma_5] + \text{h.c.}, \quad \mathbf{X}' \longrightarrow \mathbf{H} \pi$$

$$\mathcal{A}_{\mu ba} = \frac{i}{2} (\xi^\dagger \partial_\mu \xi - \xi \partial_\mu \xi^\dagger)_{ba}$$

$$\xi = e^{\frac{i\mathcal{M}}{f\pi}}$$

$$\mathcal{M} = \begin{pmatrix} \sqrt{\frac{1}{2}}\pi^0 + \sqrt{\frac{1}{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\sqrt{\frac{1}{2}}\pi^0 + \sqrt{\frac{1}{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\sqrt{\frac{2}{3}}\eta \end{pmatrix}$$

Analogous terms describe interactions involving radial excitation doublets: $g \rightarrow \tilde{g}$, $h \rightarrow \tilde{h}, \dots$

$D_{sJ}(2860)$: results for width ratios

P. Colangelo, S. Nicotri, FDF
PLB 642, 48

$D_{sJ}(2860)$	$D_{sJ}(2860) \rightarrow DK$	$\frac{\Gamma(D_{sJ}(2860) \rightarrow D^* K)}{\Gamma(D_{sJ}(2860) \rightarrow DK)}$	$\frac{\Gamma(D_{sJ}(2860) \rightarrow D_s \eta)}{\Gamma(D_{sJ}(2860) \rightarrow DK)}$
1 $s_\ell^P = \frac{1}{2}^-, J^P = 1^-, n = 2$	p-wave	1.23	0.27
2 $s_\ell^P = \frac{1}{2}^+, J^P = 0^+, n = 2$	s-wave	0	0.34
3 $s_\ell^P = \frac{3}{2}^+, J^P = 2^+, n = 2$	d-wave	0.63	0.19
4 $s_\ell^P = \frac{3}{2}^-, J^P = 1^-, n = 1$	p-wave	0.06	0.23
5 $s_\ell^P = \frac{5}{2}^-, J^P = 3^-, n = 1$	f-wave	0.39	0.13



Would explain the observed narrowness

$D_{sJ}(2860)$

Our supported option:

5

$$s_\ell^P = \frac{5}{2}^-, J^P = 3^-, n = 1$$

- **Signal expected in D^*K**
- Small signal expected also in $D_s \eta$

In this case the small width can be attributed to the suppression due to the kaon momentum factor:

$$\Gamma(D_{sJ} \rightarrow DK) = \frac{6}{35} \frac{(k_1 + k_2)^2}{\pi f_\pi^2 \Lambda_\chi^4} \frac{M_D}{M_{D_{sJ}}} q_K^7 \left. \vphantom{\Gamma(D_{sJ} \rightarrow DK)} \right\} \text{f-wave transition}$$



Assuming the experimentally measured width would predict in the typical range of these couplings $k_1 + k_2 \approx 0.5$

The spin 2 partner could decay in p-wave due to the effect of $1/m_Q$ corrections



may escape detection

Our conclusion:

$D_{sJ}(2860)$ is likely to be a $J^P=3^-$ state



Should decay to D^*K

Identifying $D_{sJ}(2710)$ through its decay modes

P. Colangelo, S. Nicotri, M. Rizzi, FDF
Phys. Rev. D77, 014012

$$R_1 = \frac{\Gamma(D_{sJ} \rightarrow D^* K)}{\Gamma(D_{sJ} \rightarrow DK)}$$

$$R_2 = \frac{\Gamma(D_{sJ} \rightarrow D_s \eta)}{\Gamma(D_{sJ} \rightarrow DK)}$$

$$R_3 = \frac{\Gamma(D_{sJ} \rightarrow D_s^* \eta)}{\Gamma(D_{sJ} \rightarrow DK)}$$



the dependence on the (unknown) couplings drops out

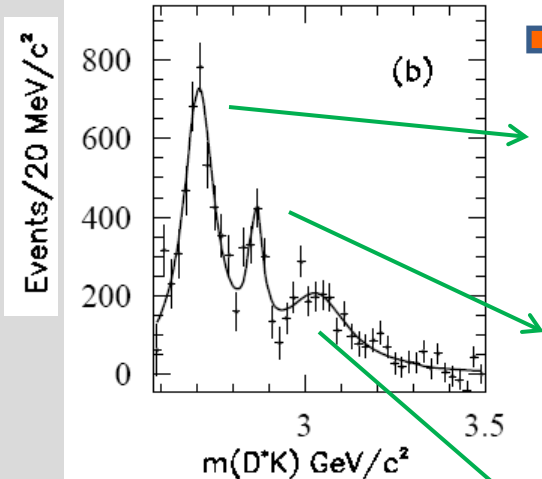
	$R_1 \times 10^2$	$R_2 \times 10^2$	$R_3 \times 10^2$
D_s^{*l}	91 ± 4	20 ± 1	5 ± 2
D_{s1}^*	4.3 ± 0.2	16.3 ± 0.9	0.18 ± 0.07



The $D^* K$ decay is the signal that must be investigated in order to distinguish the two possible assignments

BaBar Analysis of $D^* K$ final states

- $D^* K$ invariant mass spectrum (background-subtracted)



Three peaks are visible:

$$m(D_{s1}^*(2710)^+) = 2710 \pm 2_{stat} \pm 7_{syst}^{12} \text{ MeV}$$

$$\Gamma(D_{s1}^*(2710)^+) = 149 \pm 7_{stat} \pm 52_{syst}^{39} \text{ MeV}$$

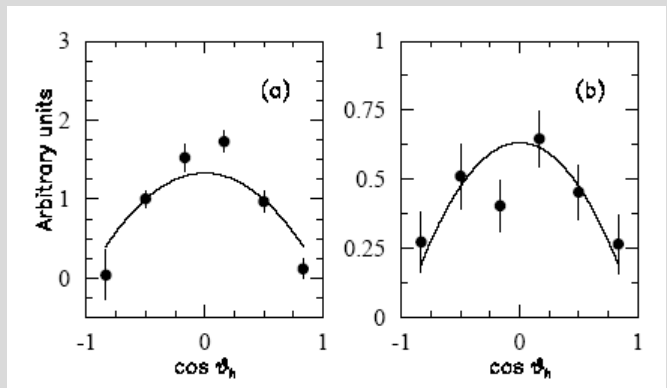
$$m(D_{sJ}(2860)^+) = 2862 \pm 2_{stat} \pm 2_{syst}^5 \text{ MeV}$$

$$\Gamma(D_{sJ}(2860)^+) = 48 \pm 3_{stat} \pm 6_{syst} \text{ MeV}$$

$$m(D_{sJ}(3040)^+) = 3044 \pm 8_{stat} \pm 5_{syst}^{30} \text{ MeV}$$

$$\Gamma(D_{sJ}(3040)^+) = 239 \pm 35_{stat} \pm 42_{syst}^{46} \text{ MeV}$$

- angular analysis



The angular distribution is consistent with the expectations for states with natural parity ($0^+, 1^-, 2^+, 3^-, \dots$) for $D_{s1}(2710)$ and $D_{sJ}(2860)$

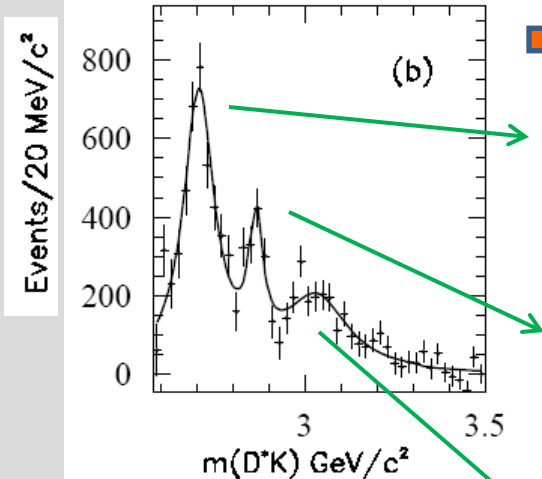


excluded by the observation of the $D^* K$ mode

BaBar, PRD80 (09)092003

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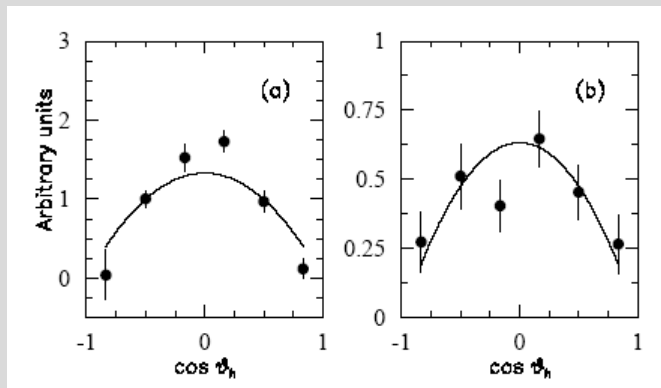
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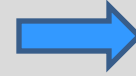
excluded by the observation of the $D^* K$ mode

BaBar, PRD80 (09)092003

to be discussed later...

Branching fractions

$$\frac{B(D_{s1}(2710)^+ \rightarrow D^* K)}{B(D_{s1}(2710)^+ \rightarrow DK)} = 0.91 \pm 0.13_{stat} \pm 0.12_{syst}$$



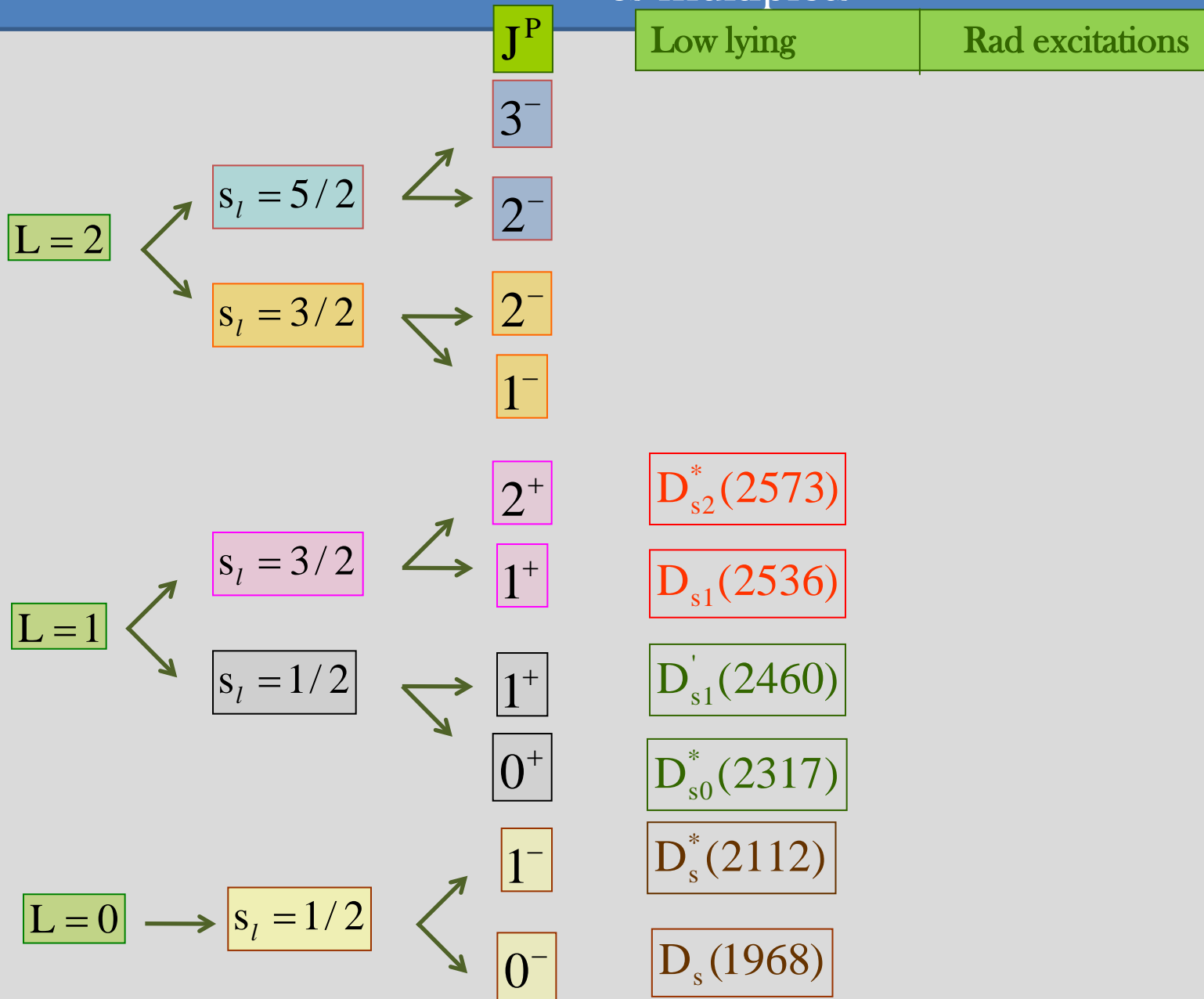
Supports the identification of $D_{s1}(2710)$ with 2^3S_1 (first radial excitation of D_s^*)

$$\frac{B(D_{sJ}(2860)^+ \rightarrow D^* K)}{B(D_{sJ}(2860)^+ \rightarrow DK)} = 1.10 \pm 0.15_{stat} \pm 0.19_{syst}$$

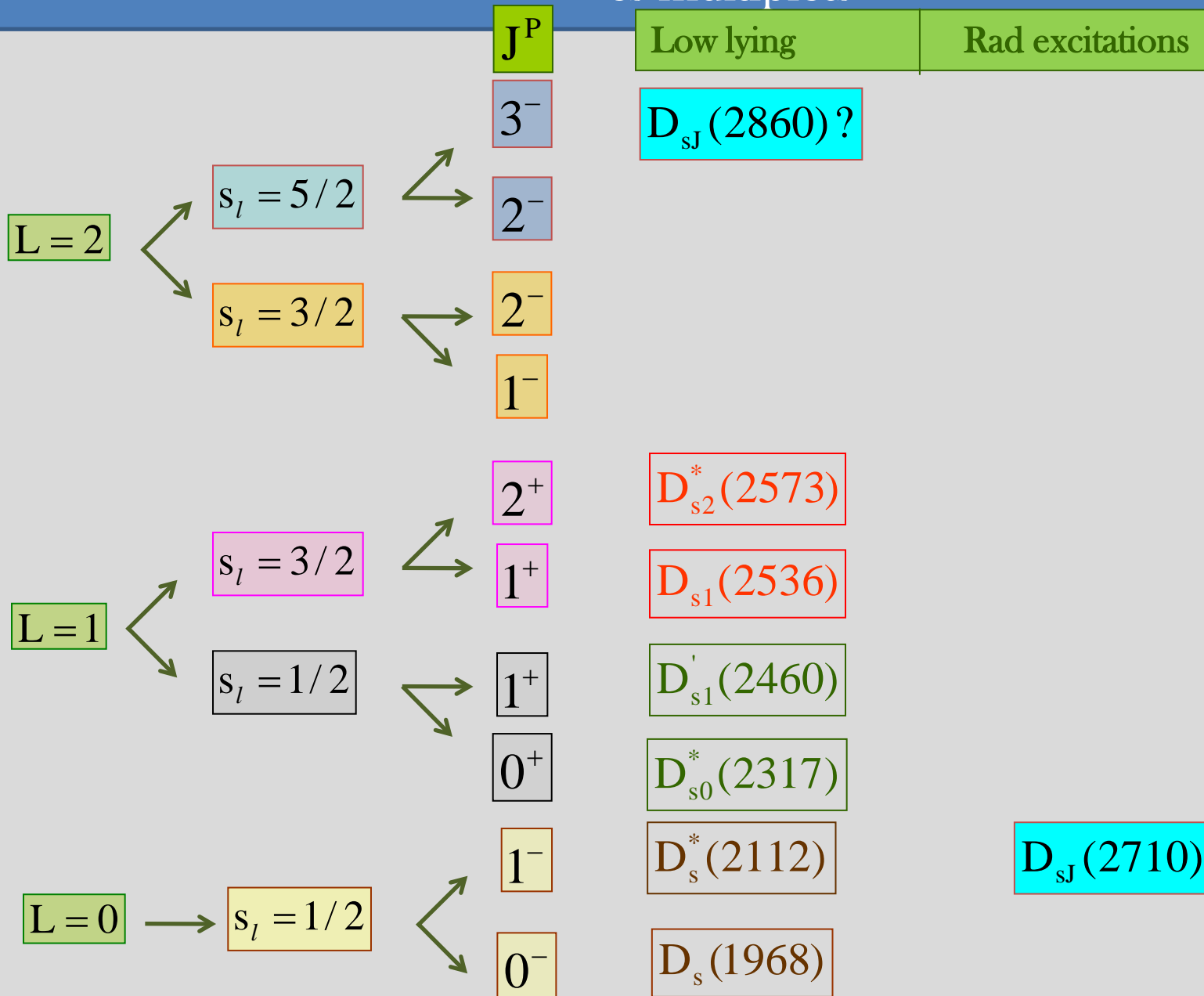


Does not support or discard unambiguously any interpretation:
still to be understood

$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



$c\bar{q}$ mesons: the non strange partner of $D_{sJ}(2700)$

States with the same quantum numbers of $D_{sJ}(2700)$ but with a different light quark flavour:

D_J^+ and D_J^0

Assuming $M(D_J) = 2600 \pm 50$ MeV:

	$\mathcal{B}(D_J^+ \rightarrow D^0 \pi^+)$	$\mathcal{B}(D_J^+ \rightarrow D^+ \pi^0)$	$\mathcal{B}(D_J^+ \rightarrow D_s \bar{K}_S^0)$	$\mathcal{B}(D_J^+ \rightarrow D^+ \eta)$	$\mathcal{B}(D_J^+ \rightarrow D^{*0} \pi^+)$	$\mathcal{B}(D_J^+ \rightarrow D^{*+} \pi^0)$	$\mathcal{B}(D_J^+ \rightarrow D^{*+} \eta)$
D^{*+}	$(27.0 \pm 2.1)\%$	$(13.3 \pm 1.0)\%$	$(2.3 \pm 0.8)\%$	$(5.3 \pm 1.0)\%$	$(32.4 \pm 0.8)\%$	$(16.1 \pm 0.4)\%$	$(1.2 \pm 1.8)\%$
	$\mathcal{B}(D_J^0 \rightarrow D^+ \pi^-)$	$\mathcal{B}(D_J^0 \rightarrow D^0 \pi^0)$	$\mathcal{B}(D_J^0 \rightarrow D_s K^-)$	$\mathcal{B}(D_J^0 \rightarrow D^0 \eta)$	$\mathcal{B}(D_J^0 \rightarrow D^{*+} \pi^-)$	$\mathcal{B}(D_J^0 \rightarrow D^{*0} \pi^0)$	$\mathcal{B}(D_J^0 \rightarrow D^{*0} \eta)$
D^{*0}	$(26.5 \pm 2.1)\%$	$(13.5 \pm 1.1)\%$	$(4.9 \pm 1.6)\%$	$(5.5 \pm 1.0)\%$	$(32.0 \pm 0.7)\%$	$(16.3 \pm 0.4)\%$	$(1.3 \pm 1.9)\%$

The strong coupling constant entering in these modes can be fixed from $D_{sJ}(2700)$ decays

$$\tilde{g} = 0.26 \pm 0.05$$



$$\Gamma(D^{*+ (0)}) = (128 \pm 61) \text{ MeV}$$

$c\bar{q}$ mesons

BaBar observes four new states with charm and without strangeness:

BaBar, PRD 82 (10) 111101

state	Mass (MeV)	Width (MeV)	decays to
$D(2550)^0$	$2539.4 \pm 4.5 \pm 6.8$	$130 \pm 12 \pm 13$	$D^{*+}\pi$
$D^*(2600)^0$	$2608.7 \pm 2.4 \pm 2.7$	$93 \pm 6 \pm 13$	$D^+\pi, D^{*+}\pi$
$D^*(2600)^+$	$2608.7 \pm 2.4 \pm 2.7$	$93 \pm 6 \pm 13$	$D^0\pi^+$
$D(2750)^0$	$2752.4 \pm 1.7 \pm 2.7$	$71 \pm 6 \pm 11$	$D^{*+}\pi$
$D^*(2760)^0$	$2763.3 \pm 2.3 \pm 2.3$	$60.9 \pm 5.1 \pm 3.6$	$D^+\pi$
$D^*(2760)^+$	$2769.7 \pm 3.8 \pm 1.5$	$60.9 \pm 5.1 \pm 3.6$	$D^0\pi^+$

$c\bar{q}$ mesons

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BaBar, PRD 82 (10) 111101

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in agreement with previous predictions for the members of the non strange partners of $D_{sJ}(2700)$

$c\bar{q}$ mesons

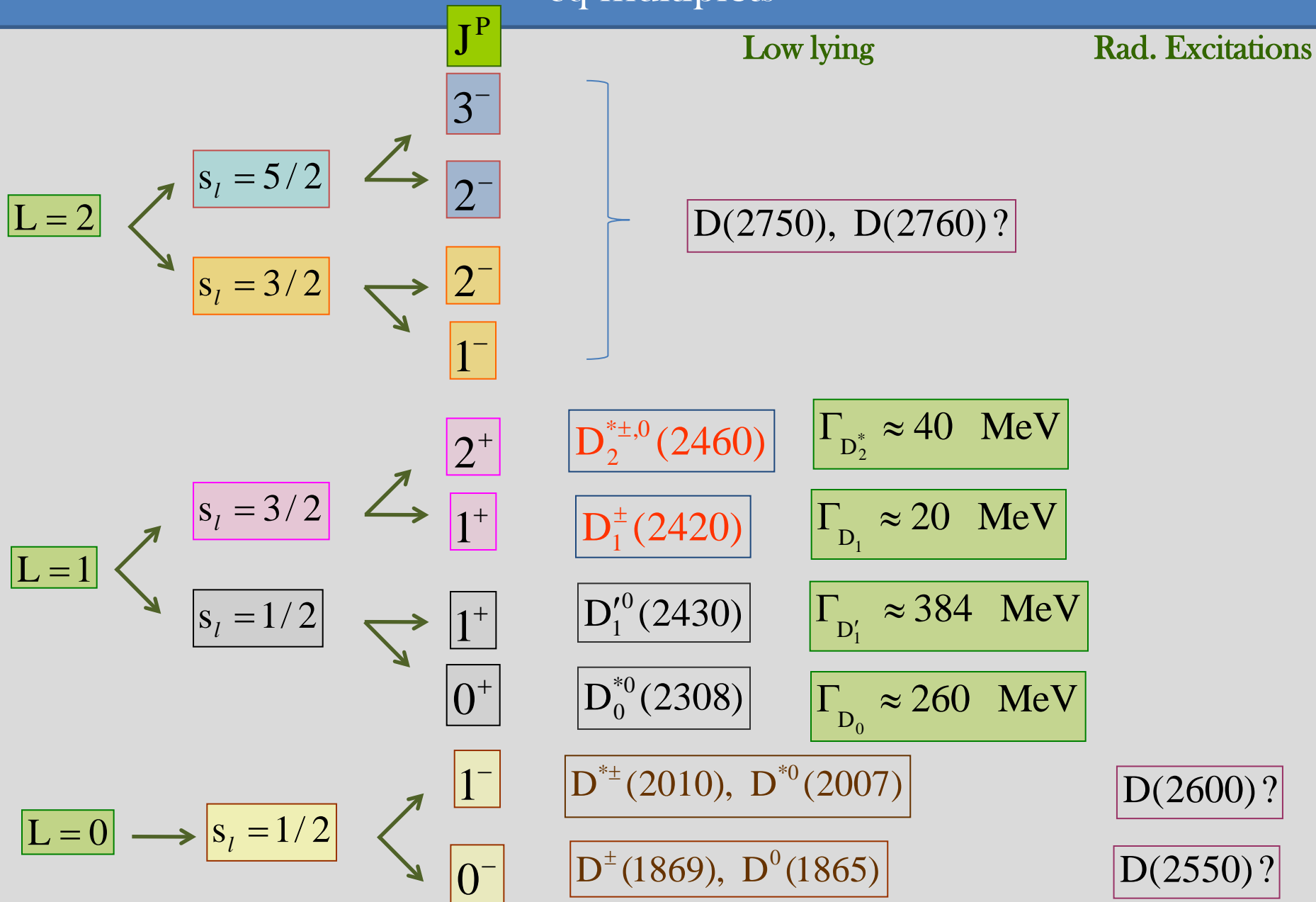
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BaBar, PRD 82 (10) 111101

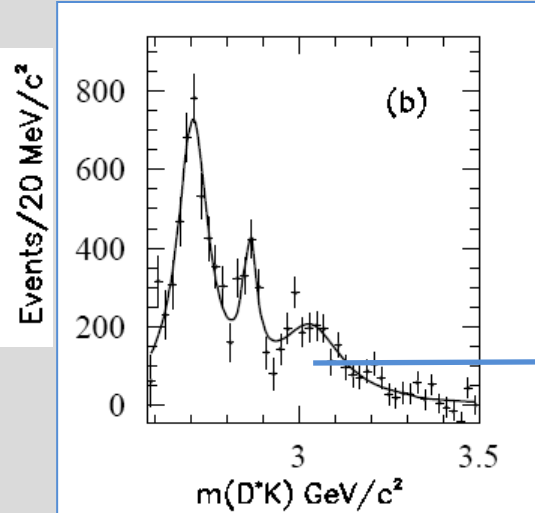
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$D^*(2760)^+$	$2769.7 \pm 3.8 \pm 1.5$	$60.9 \pm 5.1 \pm 3.6$	$D^0\pi^+$

still need to be identified
likely to be L=2 states

$c\bar{q}$ multiplets



$D_{sJ}(3040)$



$$M(D_{sJ}(3040)) = 3044 \pm 8_{\text{stat}} \left(\begin{smallmatrix} +30 \\ -5 \end{smallmatrix} \right)_{\text{syst}} \text{ MeV}$$
$$\Gamma(D_{sJ}(3040)) = 239 \pm 35_{\text{stat}} \left(\begin{smallmatrix} +46 \\ -42 \end{smallmatrix} \right)_{\text{syst}} \text{ MeV}$$

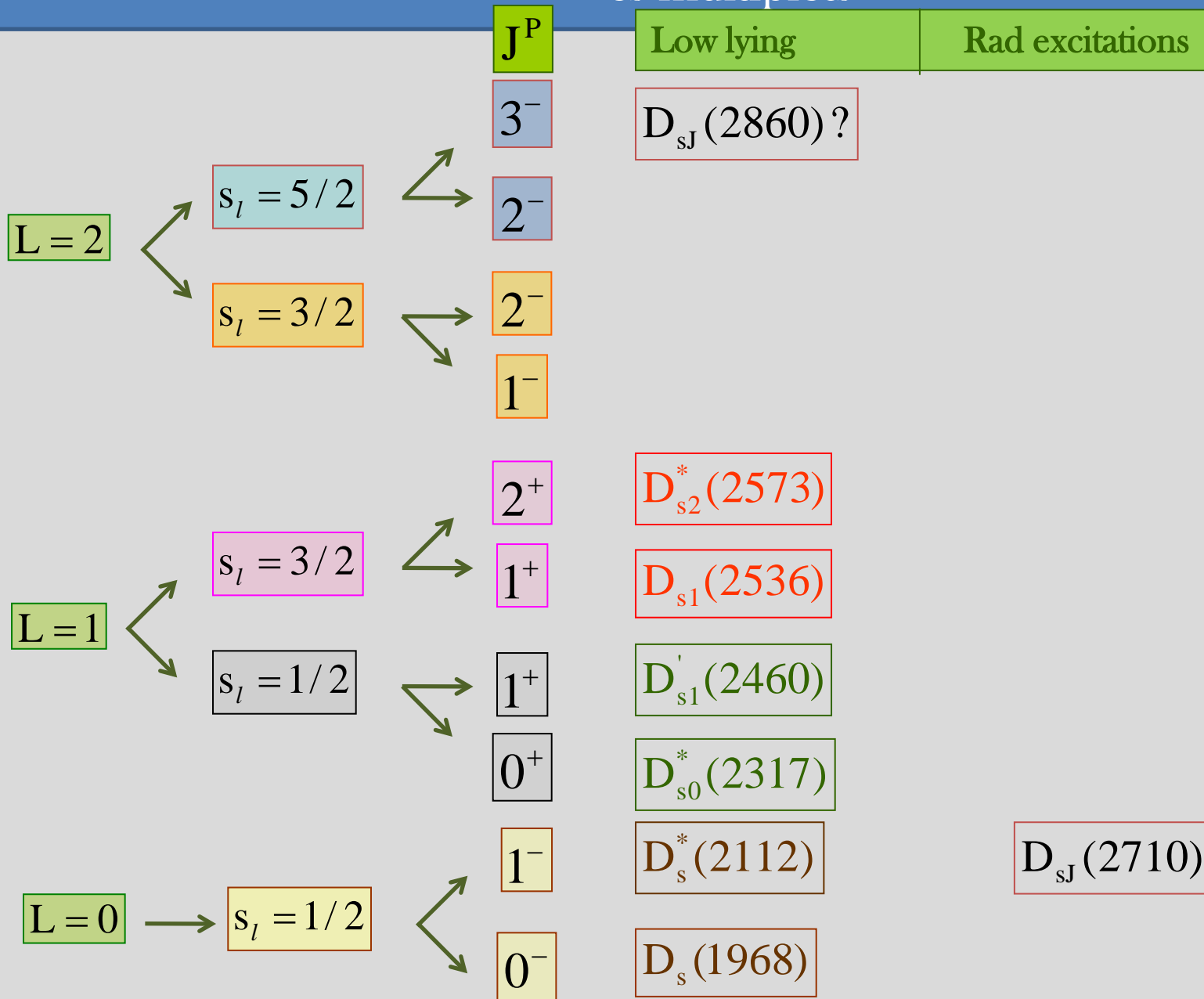
The only additional information is that it decays

$\rightarrow D^*K$	YES
$\rightarrow DK$	NO

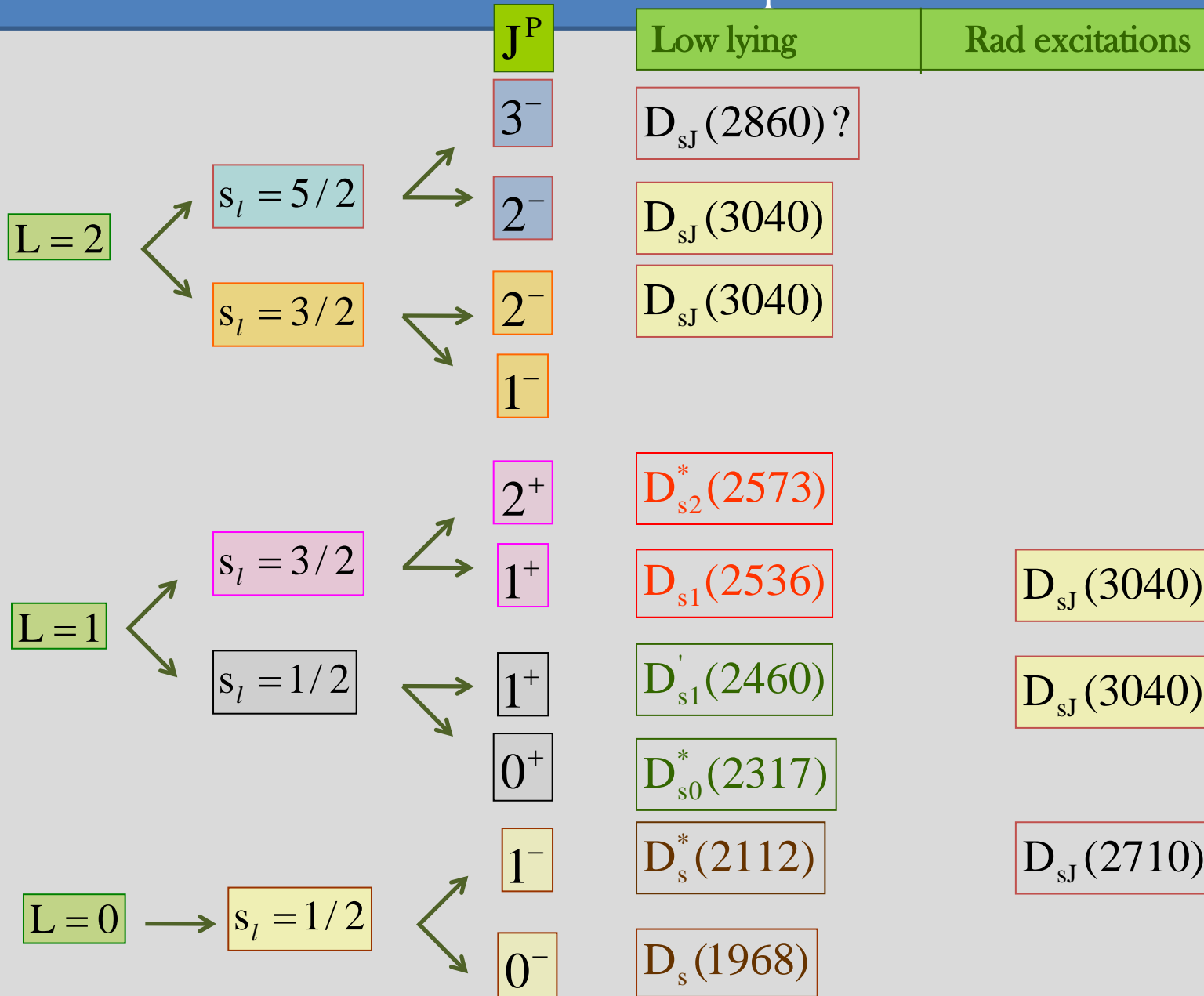


$J^P=1^+, 2^-, 3^+, \dots$

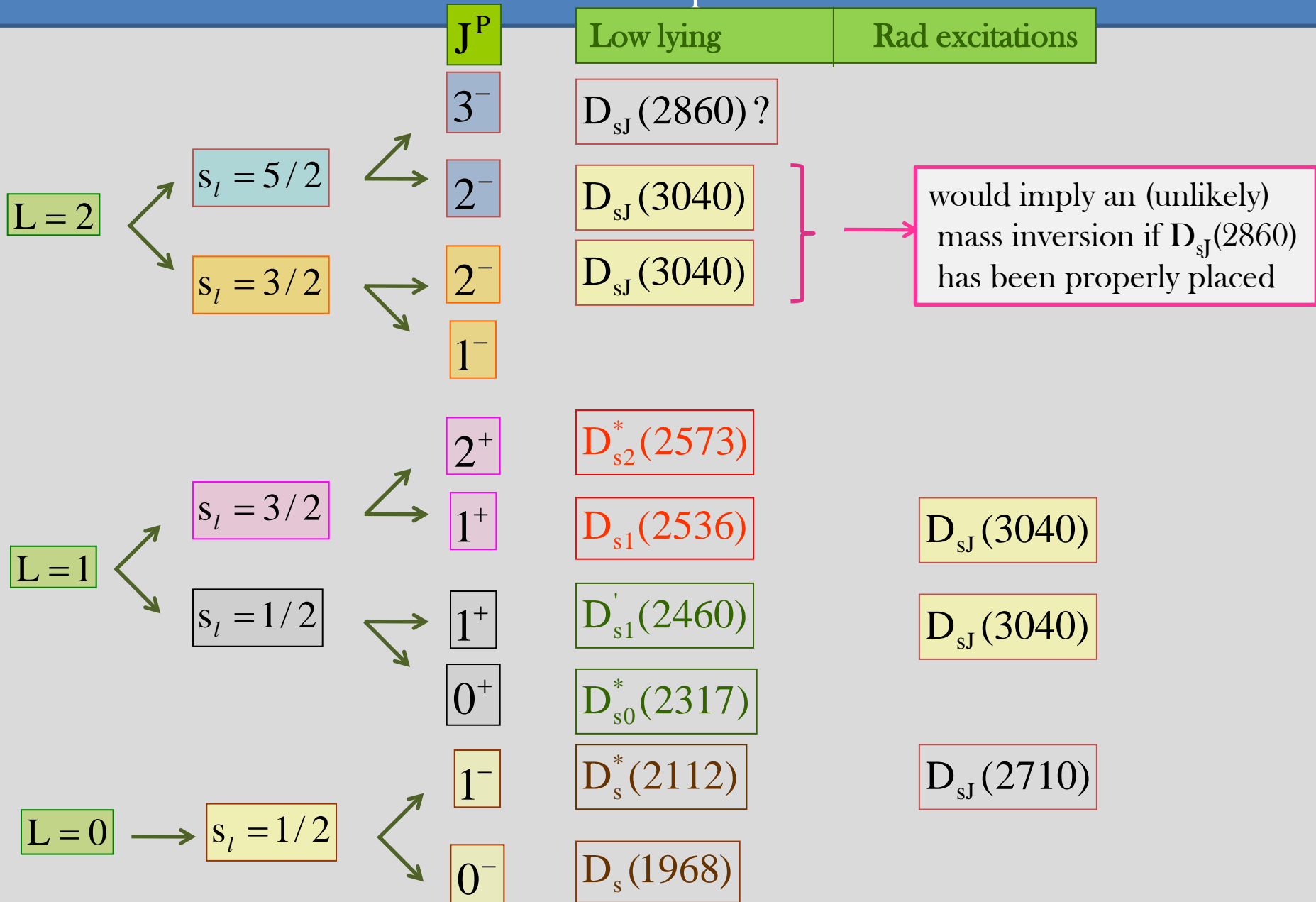
$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



$D_{sJ}(3040)$: how to discriminate among the four possibilities?

- info from Relativistic Quark Model (RQM)



$$M(\tilde{D}_{s1})^{(RQM)} = 3114 \text{ MeV},$$

$$M(\tilde{D}'_{s1})^{(RQM)} = 3165 \text{ MeV},$$

$$M(D_{s2})^{(RQM)} = 2953 \text{ MeV},$$

$$M(D_{s2}^{*'})^{(RQM)} = 2900 \text{ MeV}.$$

- Allowed strong decays:

- to $D_{(s)}^*$ + light pseudoscalar meson

$$D^*K, D_{s0}^*\eta$$



$$R_1 = \frac{\Gamma(D_{sJ}(3040) \rightarrow D_s^*\eta)}{\Gamma(D_{sJ}(3040) \rightarrow D^*K)}$$

- to members of higher doublets + a light pseudoscalar meson

$$D_0^*K, D_{s0}^*, D_1'K$$

$$D_1K, D_2^*K$$

- to $D_{(s)}$ + a light vector meson

$$DK^*, D_s\phi$$

$D_{sJ}(3040)$: how to discriminate among the four possibilities?

Decay modes	$\tilde{D}'_{s1} (n = 2, J_{s\ell}^P = 1_{1/2}^+)$	$\tilde{D}_{s1} (n = 2, J_{s\ell}^P = 1_{3/2}^+)$	$D_{s2} (n = 1, J_{s\ell}^P = 2_{3/2}^-)$	$D_{s2}^* (n = 1, J_{s\ell}^P = 2_{5/2}^-)$
$D^*K, D_s^*\eta$	s wave	d wave	p wave	f wave
R_1	0.34	0.20	0.245	0.143
$D_0^*K, D_{s0}^*\eta, D_1'K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	...	d wave
D_2^*K	p wave	p wave	s wave	d wave
$DK^*, D_s\phi$	s wave $\Gamma \simeq 140$ MeV	s wave $\Gamma \simeq 20$ MeV	p wave Negligible	p wave Negligible
		Spin partner		
	$\tilde{D}_{s0}^* (n = 2, J_{s\ell}^P = 0_{1/2}^+)$	$\tilde{D}_{s2}^* (n = 2, J_{s\ell}^P = 2_{3/2}^+)$	$D_{s1}^* (n = 1, J_{s\ell}^P = 1_{3/2}^-)$	$D_{s3} (n = 1, J_{s\ell}^P = 3_{5/2}^-)$
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$D^*K, D_s^*\eta$...	d wave	p wave	f wave
$D_0^*K, D_{s0}^*\eta$	d wave	...
$D_1'K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	s wave	d wave
D_2^*K	...	p wave	...	d wave

- \tilde{D}'_{s1} decays in s -wave to $D^*K, D_s^*\eta$ (broader), has the largest R_1 , the largest width to light vector mesons

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$D_{sJ}(3040)$: how to discriminate among the four possibilities?

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- the two 2^- states should not be observed in the decay to light vector mesons

$D_{sJ}(3040)$: how to discriminate among the four possibilities?

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$D_1'K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	s wave	d wave
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$D_0^*K, D_{s0}^*\eta$	d wave	...
$D_1'K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	s wave	d wave
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- look at the features of the spin partner

$D_{sJ}(3040)$: how to discriminate among the four possibilities?

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Concluding remarks

- all the observed $c\bar{s}$ states classified as ordinary mesons
- $D_{sJ}(2700)$ identified with D_{sJ}^{*} $D_J(2600)$ most likely its non strange partner
- Still to be understood: $D_{sJ}(2860)$ ($J^P = 3^- ?$)
 $D_{sJ}(3040)$ → various allowed decay modes may help in the classification
- the most intriguing challenge remains to understand why
 $D_{s0}^*(2317)$ and $D'_{s1}(2460)$ have masses below the $D^{(*)}K$ threshold
- HQ symmetry predicts analogous states in the beauty system :

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$$M(B_{s0}^*)=5721 \text{ MeV decaying to } B_s \pi^0$$
$$M(B'_{s1})=5762 \text{ MeV decaying to } B_s^* \pi^0$$