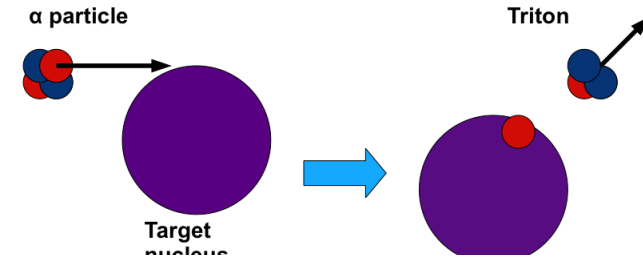
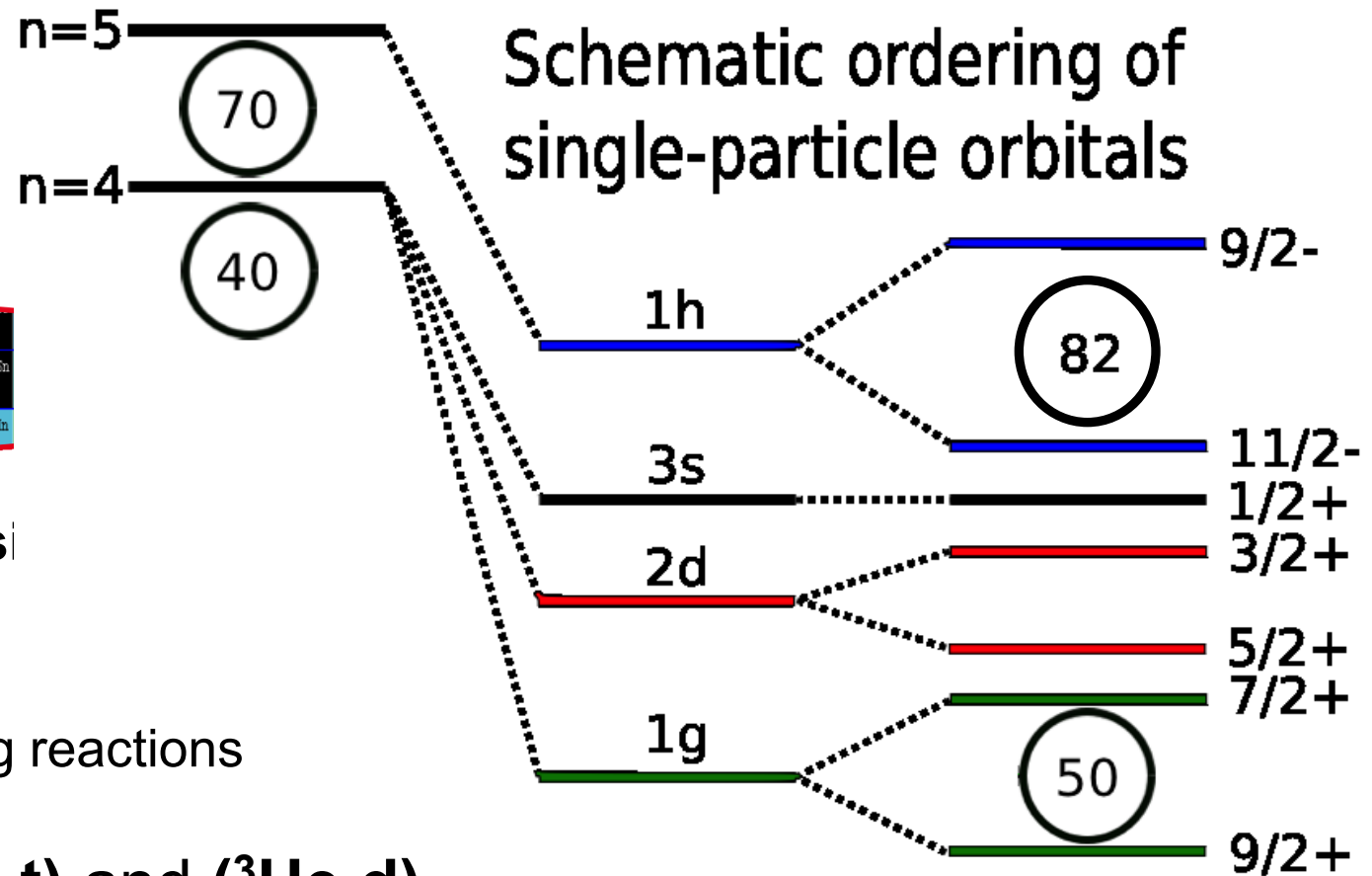
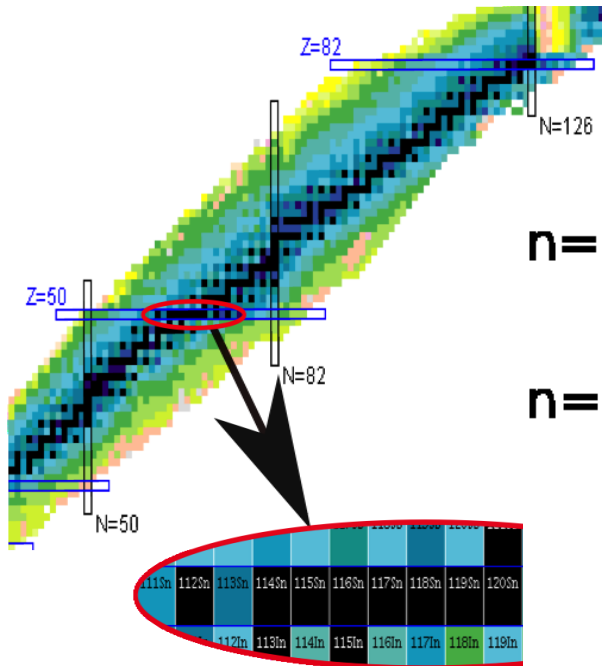


# Investigating trends in proton single-particle states outside $Z=50$ isotopes

**AJ Mitchell**

**NPPD Conference – Glasgow 2011**

# Single-particle states



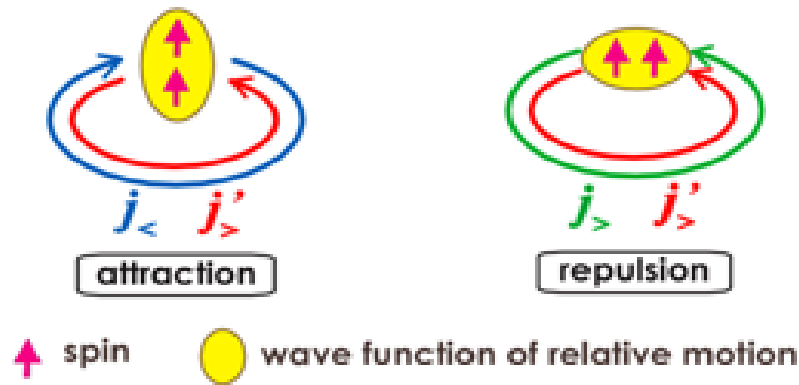
- Investigate **proton s** states with increasing

- Single-proton adding reactions on **Z=50** core:

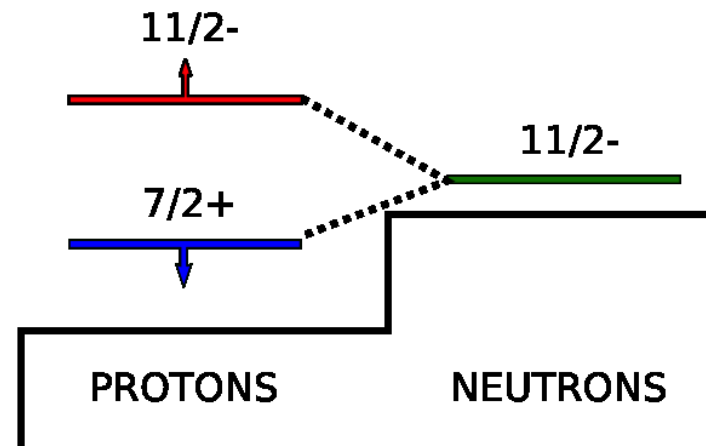
=> ( $\alpha, t$ ) and ( $^3\text{He}, d$ )

# Motivation – Tensor Interaction

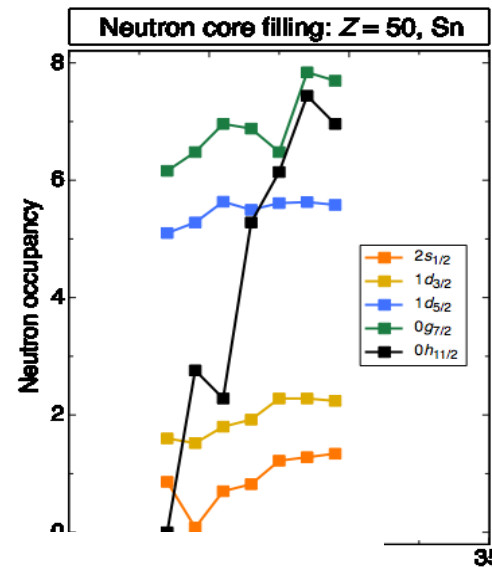
**Tensor interaction:** Driving force behind evolution of single-particle states?



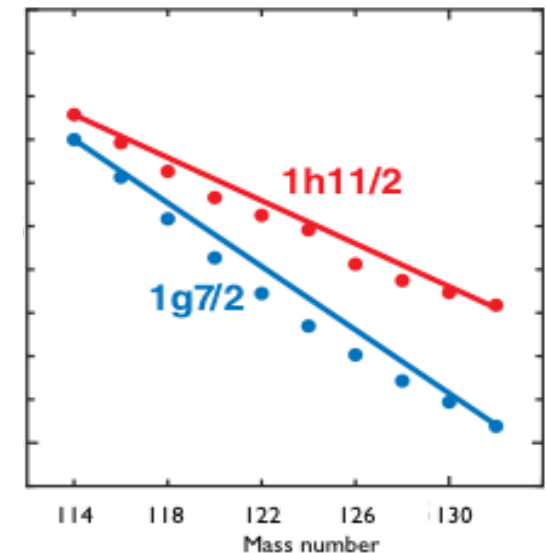
Schematic representation of the **monopole interaction** produced by the tensor force between  $\nu j_{<}$  and  $\pi j_{>}$  orbitals.



Expect increase in  $\pi g_{7/2}$  and  $\pi h_{11/2}$  or



Neutrons predominantly fill  $\nu h_{11/2}$  orbital (previous (d,p) measurements).



# Single-Particle Transfer

## Transfer reactions:

- Single-step processes
- Change of single degree of freedom
- Highly selective in populating discrete low-lying states in the atomic nucleus

Can be modelled using the distorted-wave Born approximation (**DWBA**):

- Distorted wave describes relative motion of the nuclei
- Generated by realistic potential between nucleons in the entrance and exit channels –

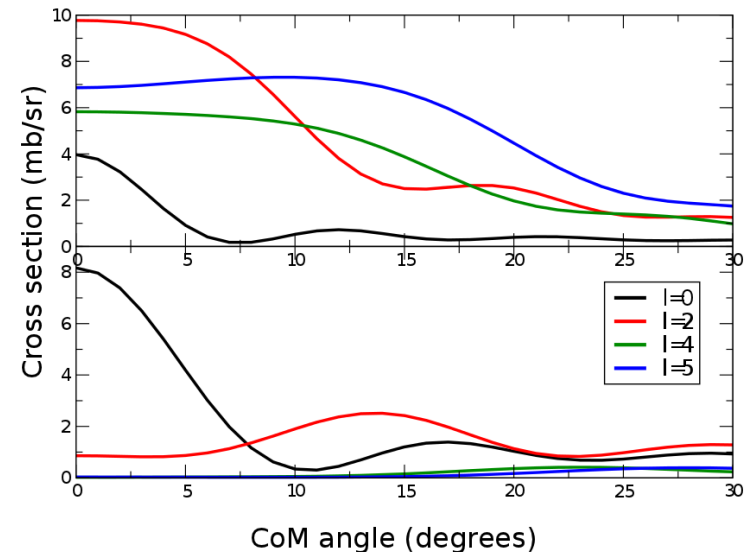
## Optical Potential:

$$V(r) = -V_f(r) - iW_f(r) + V_c + V_{so} \frac{1}{r} \frac{df(r)}{dr} (L \cdot S)$$

where

$$f(r) = \frac{1}{1 + \exp\left(\frac{r - R}{a}\right)}$$

Theoretical distributions of ( $\alpha$ ,t) and ( $^3\text{He}$ ,d) reactions on  $^{124}\text{Sn}$  target



( $\alpha$ ,t)  
37.5  
MeV

( $^3\text{He}$ ,d)  
25.0  
MeV

Transfer of angular momentum depends on reaction kinematics

$\Rightarrow$  ( $\alpha$ ,t) high  $j$

$\Rightarrow$  ( $^3\text{He}$ ,d) low  $j$

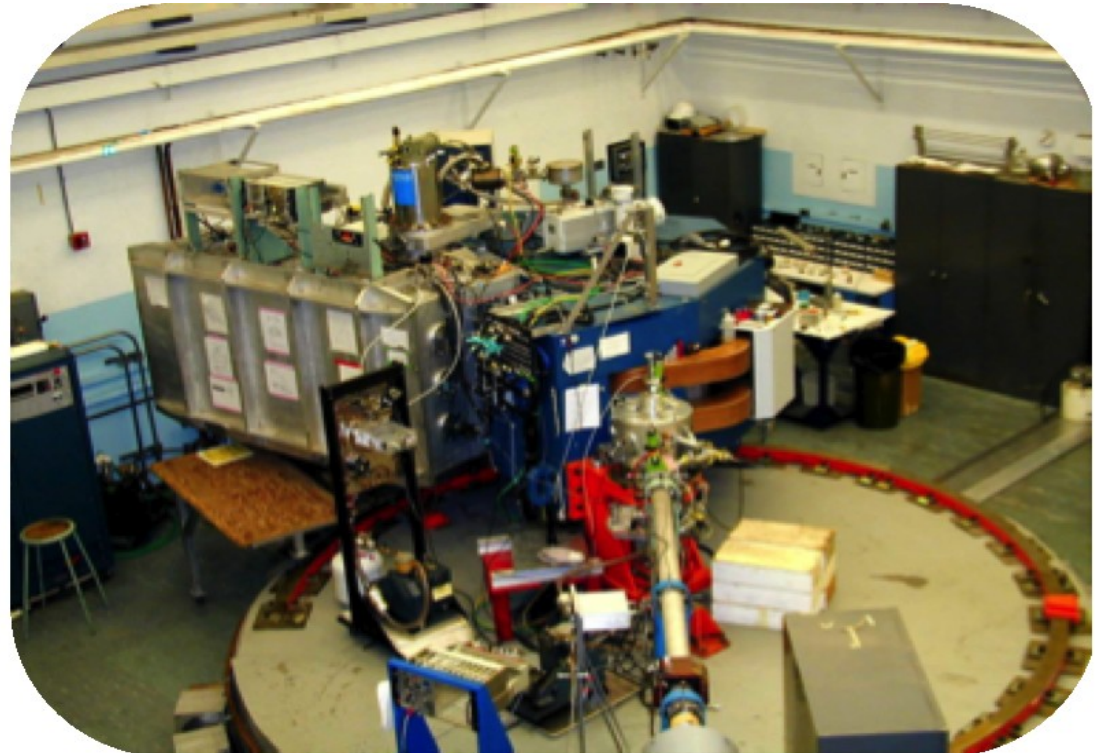
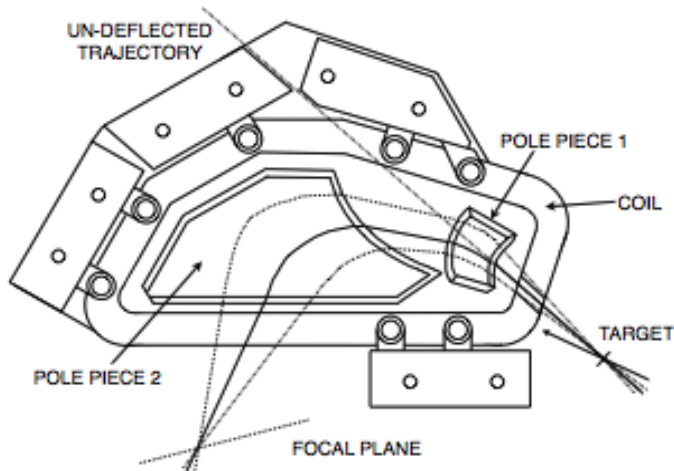
Reactions performed at **peaks** of distributions – more reliable

# Experimental set up – A. W. Wright Nuclear Structure Laboratory

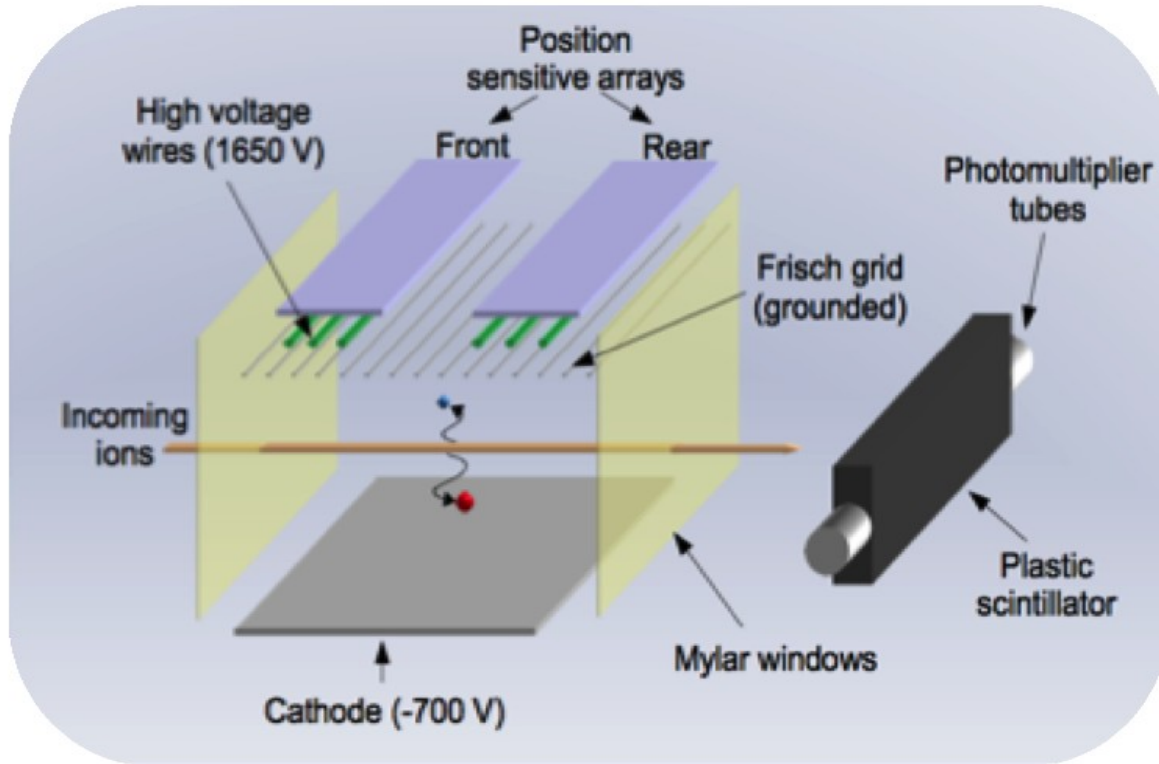


**ESTU tandem Van de Graaff accelerator:**

- **15.0 MeV  $\alpha$  particles for elastic scattering**
- **37.5 MeV  $\alpha$  particles for  $(\alpha, t)$  reactions**
- **25.0 MeV  $^3\text{He}$  nuclei for  $(^3\text{He}, d)$  reactions**



# Data acquisition

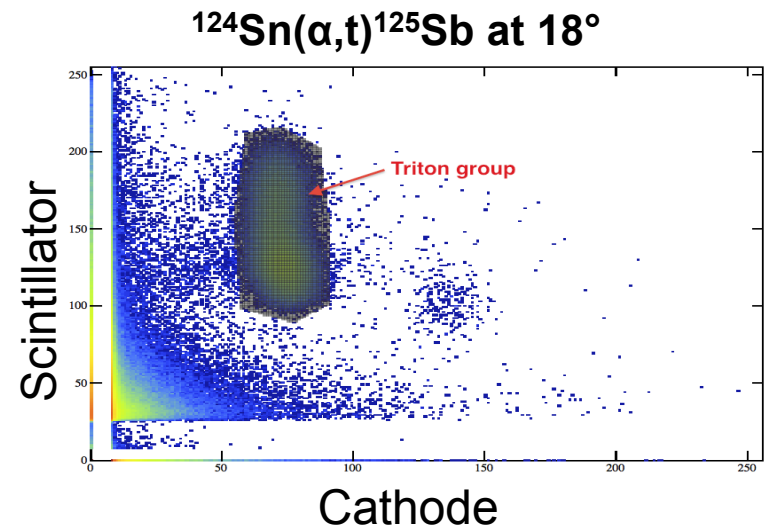


Simplified schematic of particle detection system

- **High voltage wires** – position in focal plane
- **Cathode** – energy loss of particles,  $\Delta E$
- **Scintillator** – final energy of particles,  $E$

These measurements are used in particle identification.

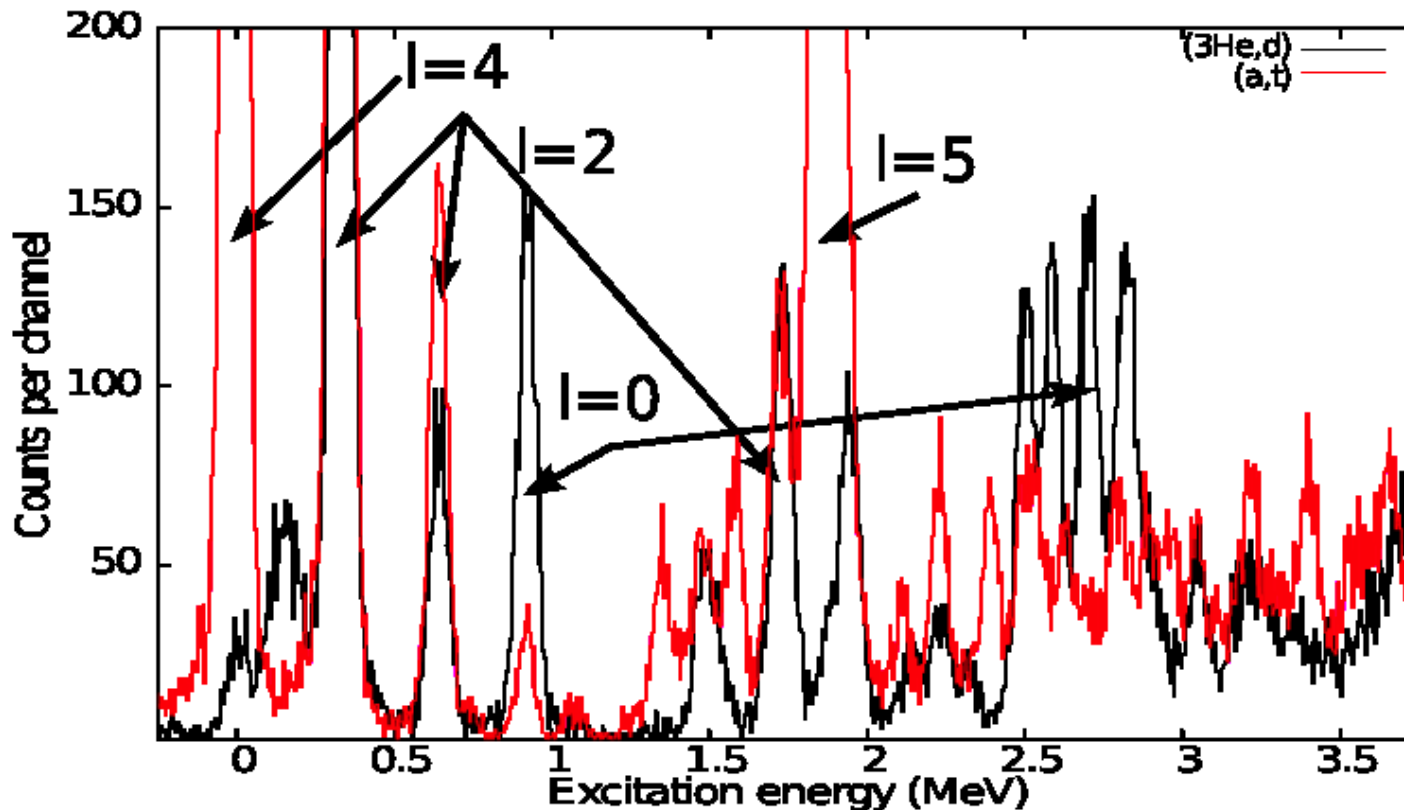
Software gates exclude unwanted data from final spectra to be analysed.





# Energy spectra

$^{125}\text{Sb}$  energy spectra from  $(\alpha,t)$  and  $(^3\text{He},d)$  reactions



- $(^3\text{He},d)$  scaled for comparison with  $(\alpha,t)$  spectrum
- High- $j$  dominant in  $(\alpha,t)$ , low- $j$  dominant in  $(^3\text{He},d)$
- $I=2$  appear in both
- Typical resolution
  - $(\alpha,t)$   
~ 60 – 75 keV
  - $(^3\text{He},d)$   
~ 50 – 75 keV

# Analysis

- **Target thicknesses** determined using elastic scattering of  $\alpha$  particles.
- Subsequent calculations use product of target thickness and aperture size to minimise error.

**Differential cross section** for the population of each state is obtained from the yield of the corresponding peak at the focal-plane:

$$\frac{d\sigma}{d\Omega} = \frac{Y}{N_b N_t \Delta\Omega \epsilon}$$

Y: Yield at the focal plane

$N_b$ : number of beam ions

$N_t$ : target thickness

$\Delta\Omega$ : entrance aperture of spectrometer

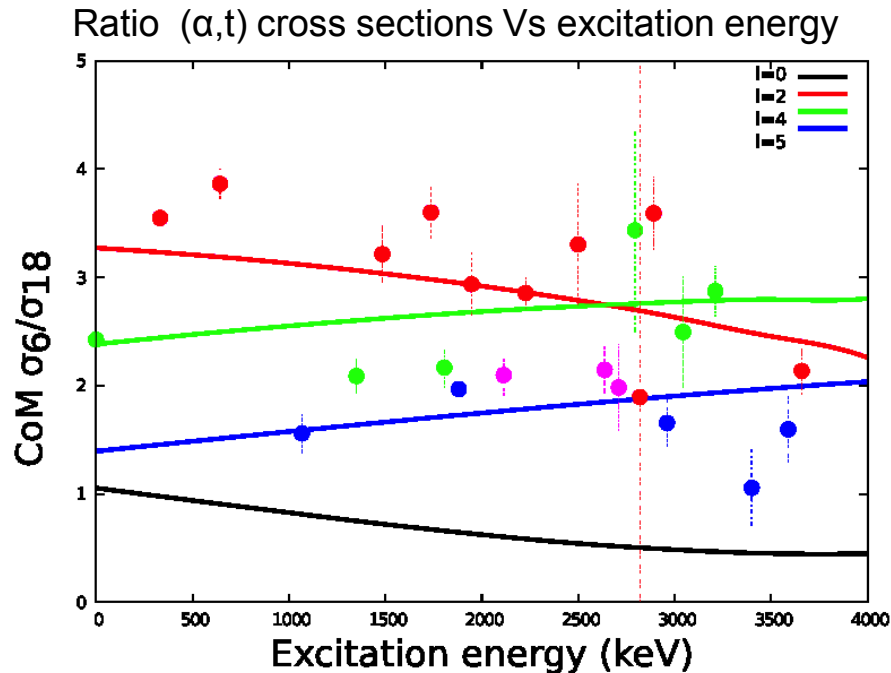
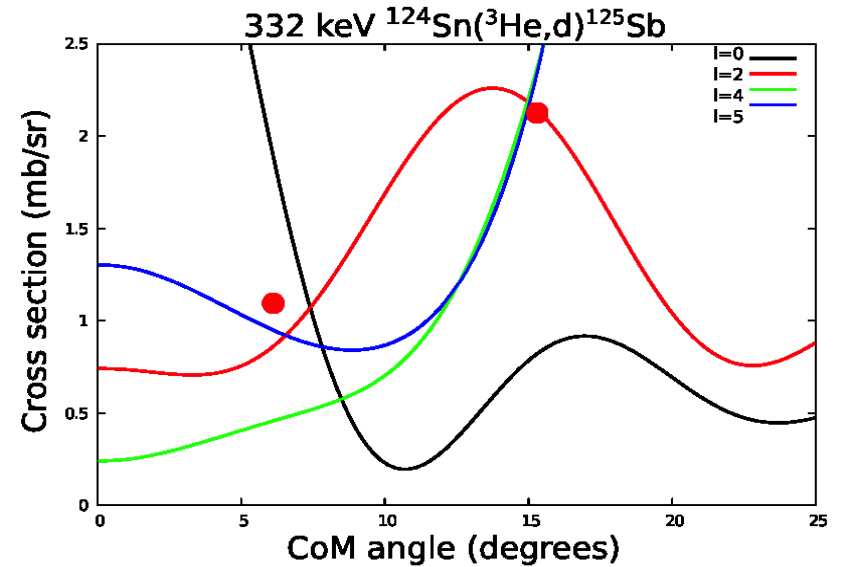
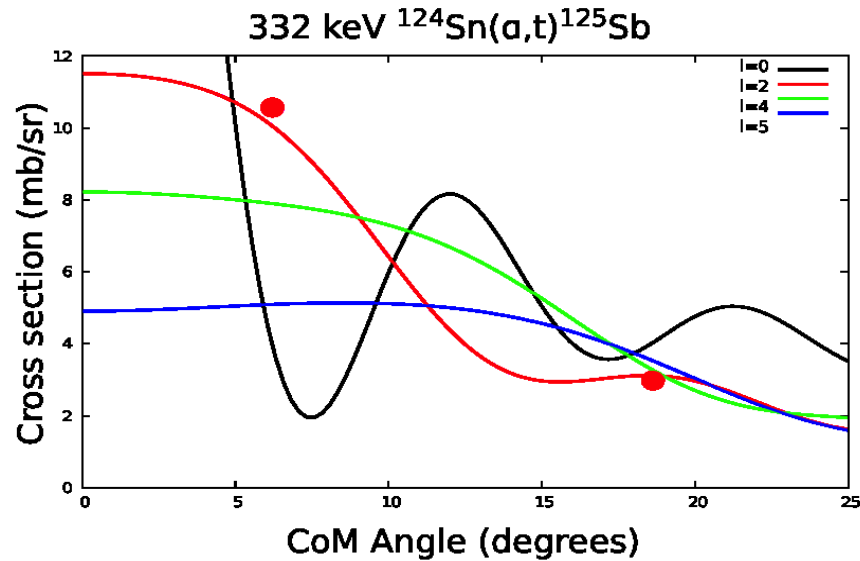
$\epsilon$ : efficiency

Target	Thickness ( $\mu\text{g cm}^{-2}$ )	Enrichment (%)
$^{112}\text{Sn}$	107.0(5)	80.04(5)
$^{114}\text{Sn}$	223.3(7)	61.23(5)
$^{116}\text{Sn}$	211.6(6)	95.60(5)
$^{118}\text{Sn}$	137.5(5)	97.79(5)
$^{120}\text{Sn}$	168.5(6)	98.05(5)
$^{122}\text{Sn}$	100.9(4)	92.19(5)
$^{124}\text{Sn}$	86.8(4)	96.17(5)

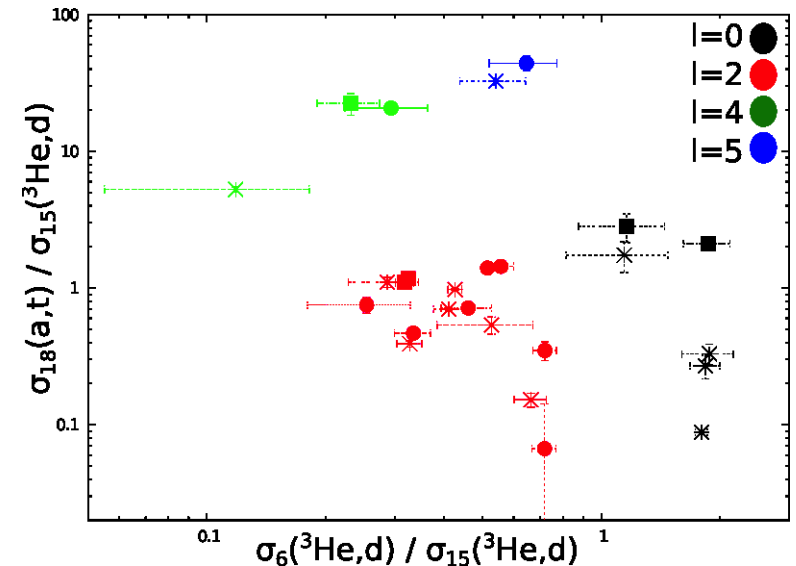
Each populated state corresponds to a particular **spin-parity** – need to find out which...



# Spin-parity assignments



Reaction ratios for  $^{121}\text{Sb}$ ,  $^{123}\text{Sb}$  and  $^{125}\text{Sb}$   
 Circle =  $^{125}\text{Sb}$ , Square =  $^{123}\text{Sb}$ , Star =  $^{121}\text{Sb}$



# Spectroscopic factors

## – work ongoing

**Independent particle model** – single-proton orbitals.

**Reality** – residual interactions create fragmentation of single-particle strength.

**Spectroscopic factor** – measure of single-particle nature of a state:

$$S_{ij} = \sigma_{\text{exp}} / \sigma_{\text{DWBA}}$$

$S_{\text{MAX}} = 1$  for single-proton adding on closed shell.

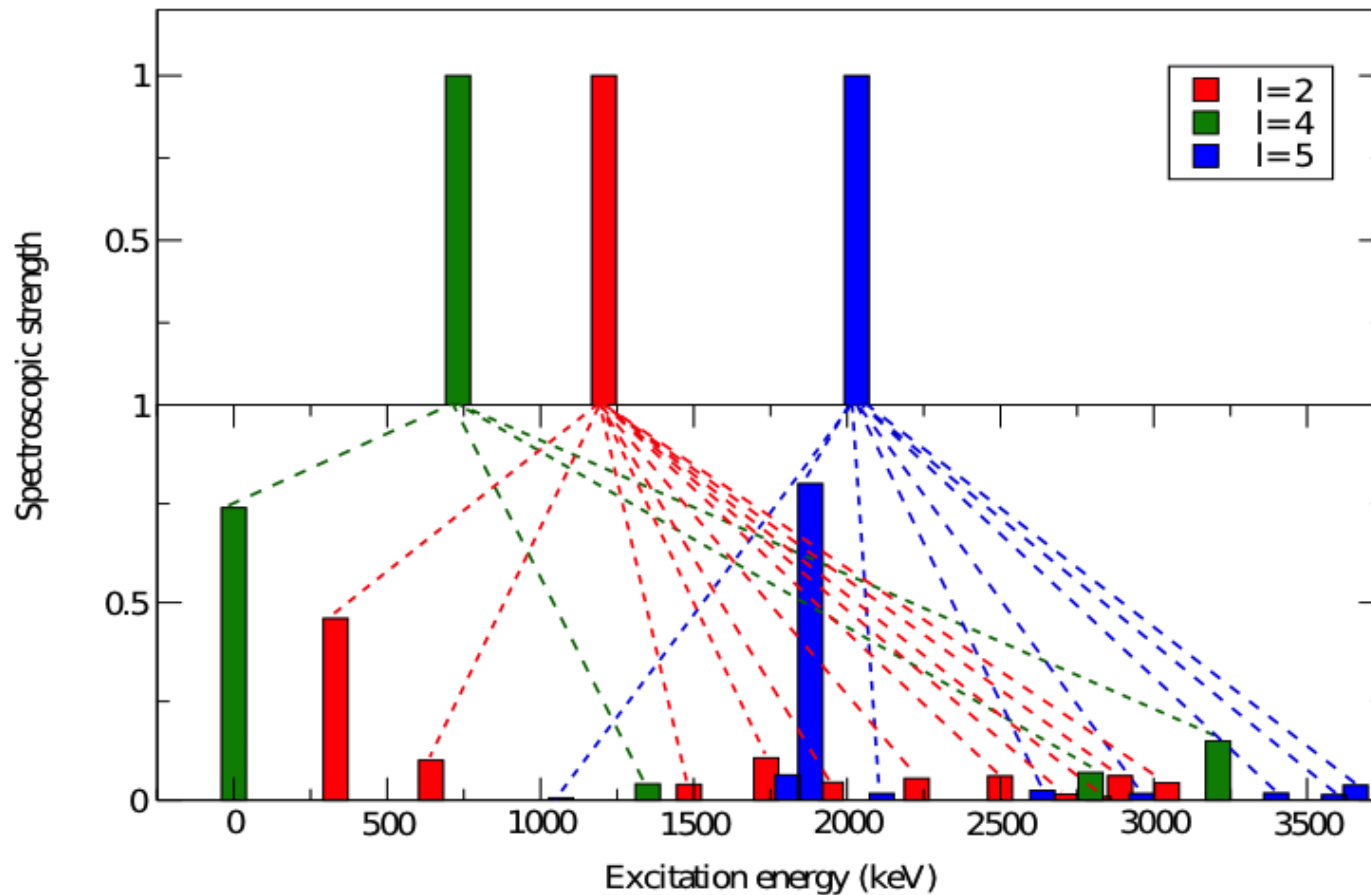
Require common normalisation across all orbitals and targets to obtain **relative spectroscopic factors**.

Summed spectroscopic factors from ( $\alpha, t$ ) measurements

SP orbital	<sup>121</sup> Sb	<sup>123</sup> Sb	<sup>125</sup> Sb
l = 2	2.79(5)	2.86(3)	2.93(5)
l = 4	1.47(1)	1.54(1)	1.60(2)
l = 5	1.44(5)	1.20(1)	1.54(2)

# Fragmentation and energy centroids

Fragmentation of normalised spectroscopic strength in  $^{125}\text{Sb}$

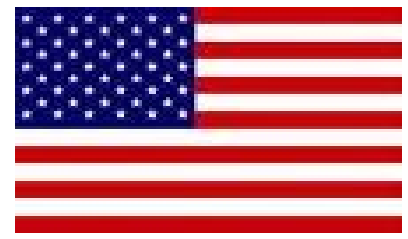


# Future work

- Extend analysis to include lower mass isotopes.
- Determine relative spectroscopic factors via a common normalisation across all targets and states.
- Reproduce energy centroids for all spin-parity orbitals.
- Investigate evolution of effective single-proton energies with increasing neutron excess.



Thank you for listening



## Acknowledgements

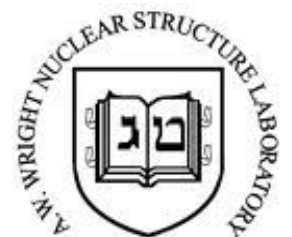
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C.M. Deibel<sup>2,3</sup>, C. R. Hoffman<sup>2</sup>, A.M Howard<sup>1</sup>, B.P. Kay<sup>2</sup>,  
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# Focal plane spectra

$^{125}\text{Sb}$  focal plane spectra

