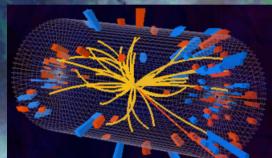
Light on dark matter

Subir Sarkar University of Oxford

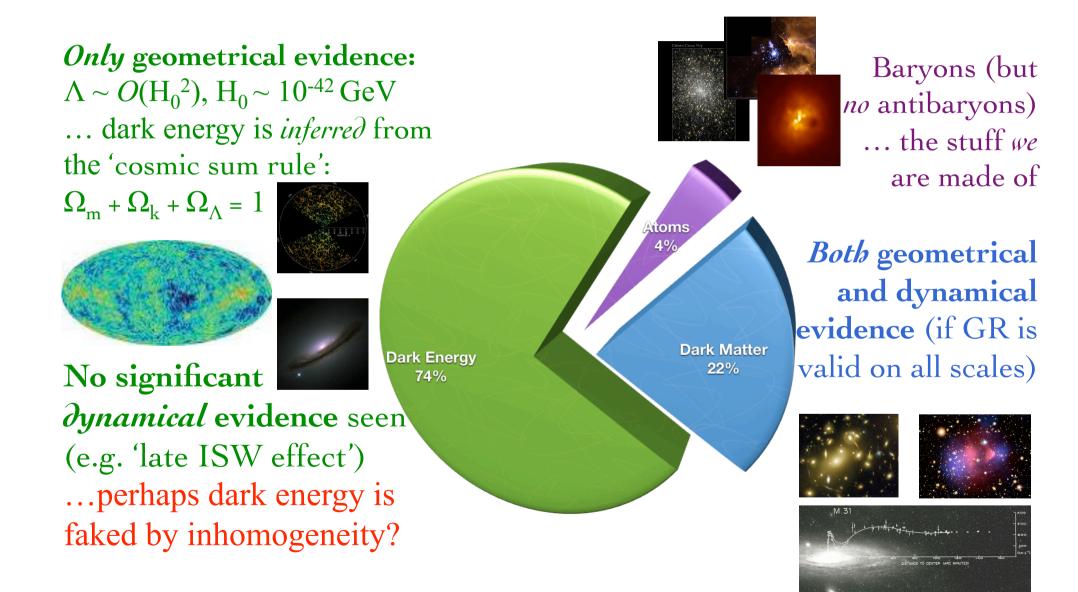


A dungeon horrible, on all sides round. As one great furnace flamed; yet from those flames No light; but rather darkness visible ...

'Paradise Lost' – Milton

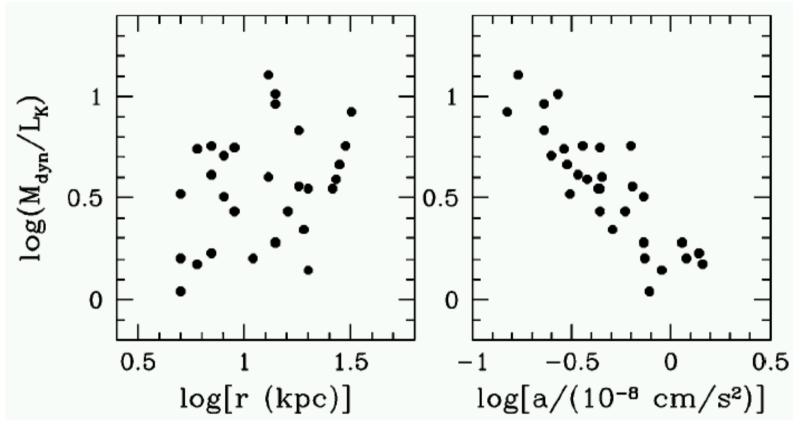
IoP Nuclear & Particle Physics Divisional Conference, Glasgow, 4-7 April 2011

What is the world made of?

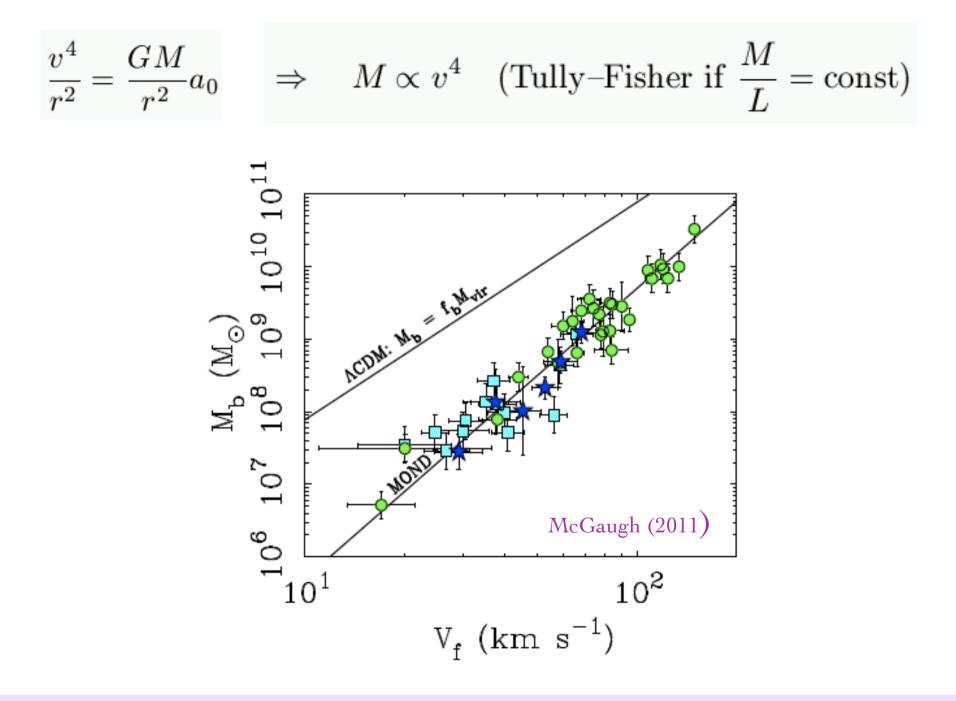


Dark matter seems to be required only where the test particle acceleration is low (< $a_0 \sim cH_0$) - it is *not* a scale-dependent effect

Milgrom (1983)



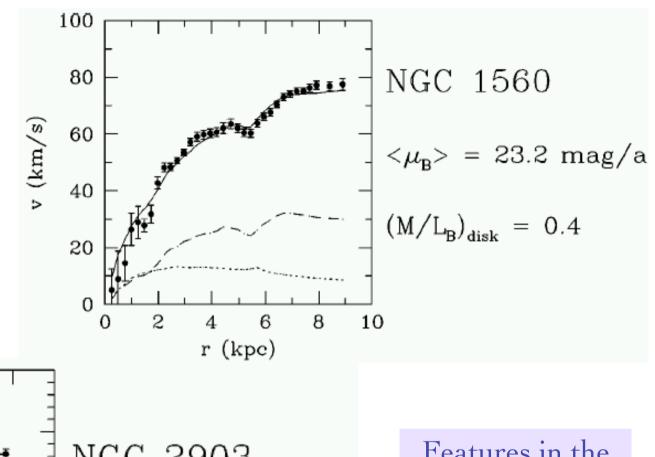
What if Newton's law is modified in weak fields?

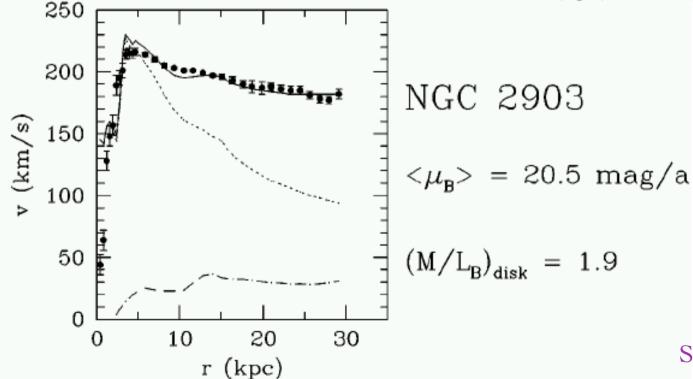


This is an impressive correlation which dark matter cannot explain

MOND fits galactic rotation curves with $a_0=1.2 \times 10^{-8}$ cm s⁻²

... fitted M/L agrees well with expectation from stellar evolution

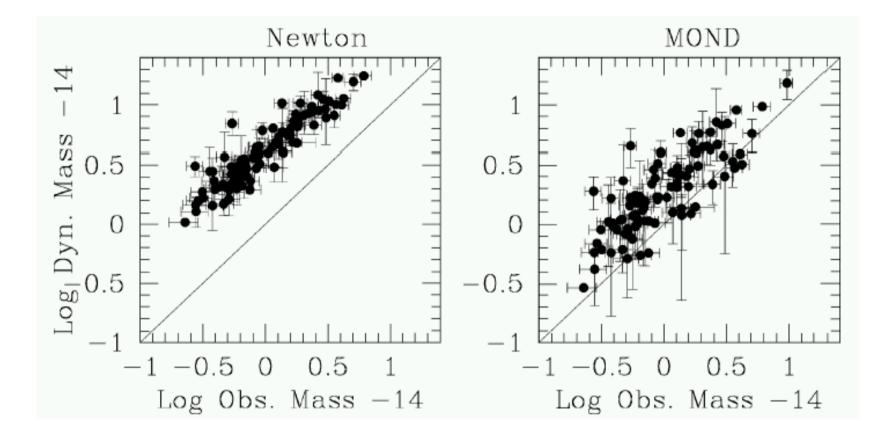




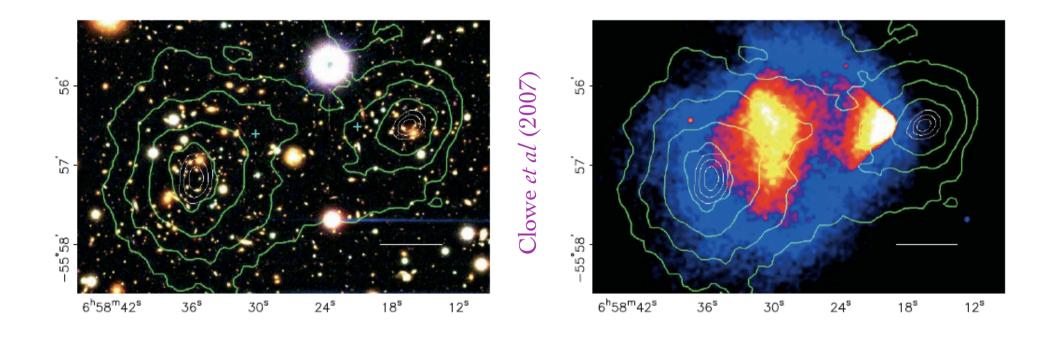
Features in the light profile are reproduced in the rotation curve!

Sanders & McGaugh (2002)

However MOND fails on the scale of clusters of galaxies

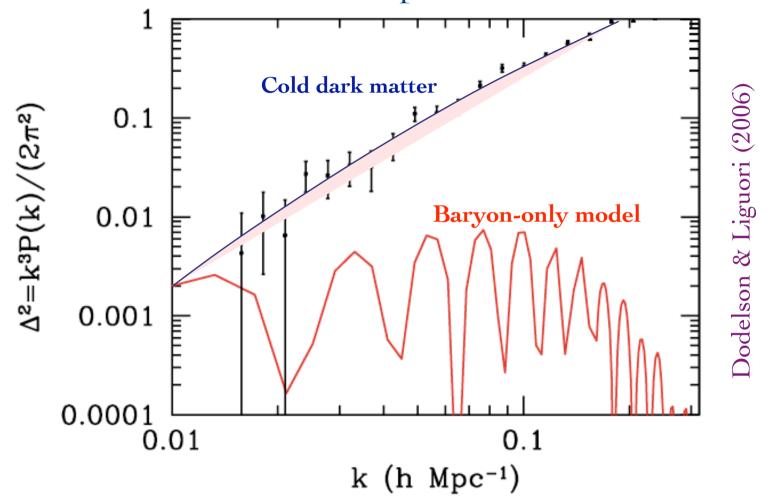


The "missing mass" *cannot* be accounted for entirely by invoking MOND ... dark matter *is* required (vindicating the original proposal of Zwicky) In the 'bullet cluster' the X-ray emitting **baryonic matter** is clearly *displaced* from the **dark matter** (the spatial distribution of which is inferred from gravitational lensing *assuming* GR) ... this seems to be convincing evidence for dark matter



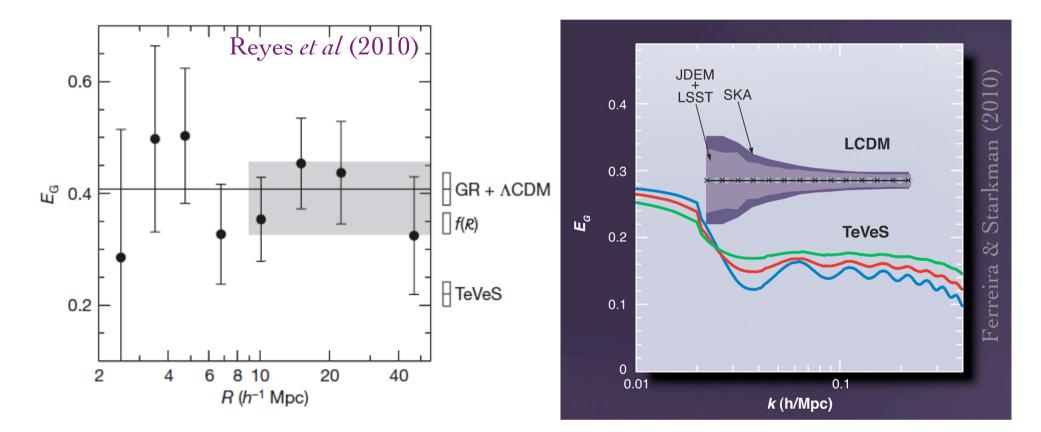
The *new* dynamics underlying MOND may, in principle, account for this, however no such compelling alternative to GR has been presented ...

Moreover the observed large-scale structure *requires* $\Omega_m \gg \Omega_B$ if it has resulted from the growth under gravity (GR) of small initial density fluctuations ... which left their imprint on the CMB at last scattering



Detailed modelling of WMAP and 2dF/SDSS $\Rightarrow \Omega_{\rm m} \sim 0.3$, $\Omega_{\rm B} \sim 0.05$... *No* MOND-like theory (e.g. TeVeS) can fit the data so well

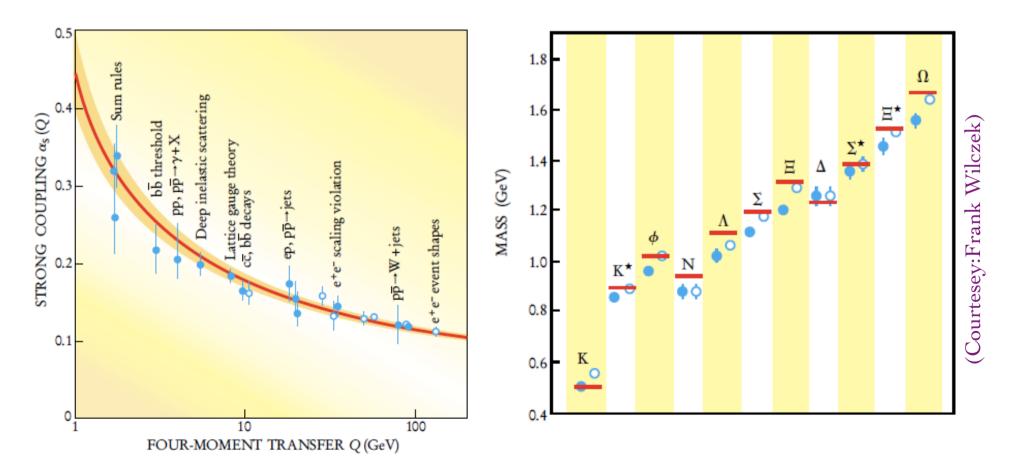
Although *new* gravitational physics (underlying MOND) can in principle provide adequate growth of cosmological structure, there will always be an observable distinction – the 'gravitational slip' – between GR and the new theory



This can be tested through measurements of 'weak lensing' (shearing of galaxy shapes) and its cross-correlation with the galaxy density field

What *should* the world be made of ?

Mass scale	Particle	Symmetry/	Stability	Production	Abundance
		Quantum #			
$\Lambda_{ m QCD}$	Nucleons	Baryon number	$\tau > 10^{33} yr$ (dim-6	'freeze-out' from thermal equilibrium	$\Omega_{ m B}$ ~10 ⁻¹⁰ cf. observed
			OK)		$\Omega_{\rm B} \sim 0.05$



What do we expect for the *symmetric* thermal relic abundance of baryons?

$$\dot{n} + 3Hn = -\langle \sigma v \rangle (n^2 - n_{\rm T}^2)$$
Chemical equilibrium is maintained
as long as annihilation rate exceeds
the Hubble expansion rate
'Freeze-out' occurs when annihilation rate:
$$\Gamma = n\sigma v \sim m_N^{3/2}T^{3/2}e^{-m_N/T}\frac{1}{m_{\pi}^2}$$
becomes comparable to the expansion rate
$$H \sim \frac{\sqrt{gT^2}}{M_{\rm P}}$$
 where $g \Rightarrow \#$ relativistic species

i.e. freeze-out occurs at
$$T \sim m_N/45$$
, with: $\frac{n_N}{n_\gamma} = \frac{n_{\bar{N}}}{n_\gamma} \sim 10^{-19}$

However the observed ratio is 10^9 times *bigger* for baryons, and there are *no* antibaryons, so we must invoke an **initial asymmetry**: $\frac{n_B - n_{\bar{B}}}{n_B + n_{\bar{B}}} \sim 10^{-9}$

1000

<u>Sakharov conditions for baryogenesis:</u> 1. Baryon number violation 2. *C* and *CP* violation 3. Departure for thermal equilibrium

Baryon number violation occurs even in the Standard Model through non-perturbative (sphaleron-mediated) processes ... but *CP*-violation is *too weak* (also out-of-equilibrium conditions are not available since the electroweak symmetry breaking phase transition is in fact a 'cross-over')

Thus the generation of the observed matter-antimatter asymmetry *requires* new BSM physics (could be related to neutrino masses ... **possibly due to violation of lepton number → leptogenesis)**

$$\text{`See-saw':} \quad \mathcal{L} = \mathcal{L}_{SM} + \lambda_{\alpha J}^* \overline{\ell}_{\alpha} \cdot HN_J - \frac{1}{2} \overline{N_J} M_J N_J^c \qquad \lambda M^{-1} \lambda^{\mathrm{T}} \langle H^0 \rangle^2 = [m_{\nu}]$$

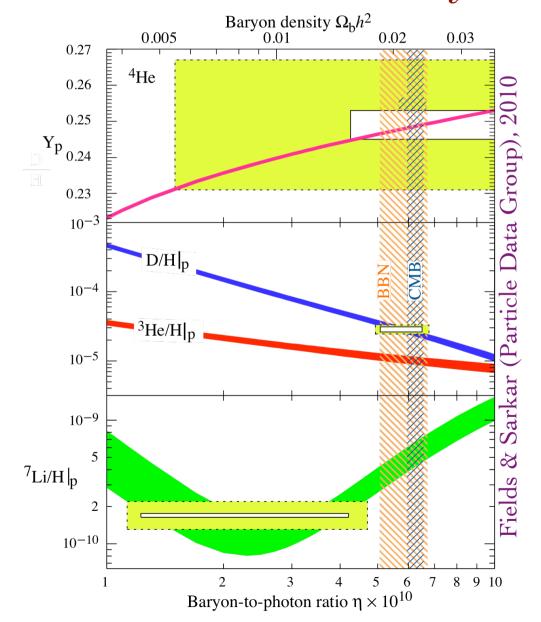
$$\nu_{L\alpha} \xrightarrow{\qquad m_D^{\alpha A} \qquad M_A \qquad m_D^{\beta A}} \qquad \nu_{L\beta}$$

$$\Delta m_{atm}^2 = m_3^2 - m_2^2 \simeq 2.6 \times 10^{-3} \text{eV}^2 \qquad \Delta m_{\odot}^2 = m_2^2 - m_1^2 \simeq 7.9 \times 10^{-5} \text{eV}^2$$

Asymmetric baryonic matter

Any primordial lepton asymmetry (from the *out*-of-equilibrium decays of the right-handed N) would be redistributed by B+L violating processes (which *conserve B-L*) amongst *all* fermions which couple to the electroweak anomaly

Although **leptogenesis** is not directly testable experimentally (unless the lepton number violation occurs as low as the TeV scale), it is an elegant paradigm for the origin of baryons ... but in any case we accept that the only kind of matter which we *know* originated *non*-thermally in the early universe Although vastly *overabundant* compared to the natural expectation, baryons *cannot* close the universe (BBN • CMB concordance) ... the dark matter must therefore mainly be *non*-baryonic



The Standard
$$SU(3)_{c} \ge SU(2)_{L} \ge U(1)_{Y}$$
 Model provides an exact
description of all *microphysics* (up to some high energy cut-off scale *M*)
 $\mathcal{L}_{eff} = M^{4} + M^{2}\Phi^{2}$ $\stackrel{Higgs mass divergence}{m_{H}^{2}} \simeq \frac{h_{t}^{2}}{16\pi^{2}} \int_{0}^{M^{2}} dk^{2} = \frac{h_{t}^{2}}{16\pi^{2}}M^{2}$ super-renormalisable
 $+ (D\Phi)^{2} + \bar{\Psi} / D\Psi + F^{2} + \bar{\Psi}\Psi\Phi + \Phi^{2}$ renormalisable
 $+ \frac{\bar{\Psi}\Psi\Phi\Phi}{M} + \frac{\bar{\Psi}\Psi\bar{\Psi}\Psi}{M^{2}} + \dots$ non-renormalisable

The effects of *new* physics beyond the SM (neutrino mass, nucleon decay, FCNC ...) \rightarrow **non-renormalisable operators** suppressed by M^n ... which 'decouple' as $M \rightarrow M_P$

But as *M* is raised, the effects of the super-renormalisable operators are *exacerbated* Solution for 2^{nd} term \rightarrow 'softly broken' supersymmetry at *M* ~ 1 TeV (10² new parameters)

This suggests possible mechanisms for **baryogenesis**, candidates for **dark matter**, ... (as also do other proposed extensions of the SM, e.g. new dimensions @ TeV scale)

For example, the lightest supersymmetric particle (typically the neutralino χ), *if* protected against decay by *R*-parity, is a candidate for thermal dark matter

But if the Higgs is *composite* (as in **technicolor** models of $SU(2)_L \ge U(1)_Y$ breaking) then there is *no need* for supersymmetry ... and light TC states can be dark matter

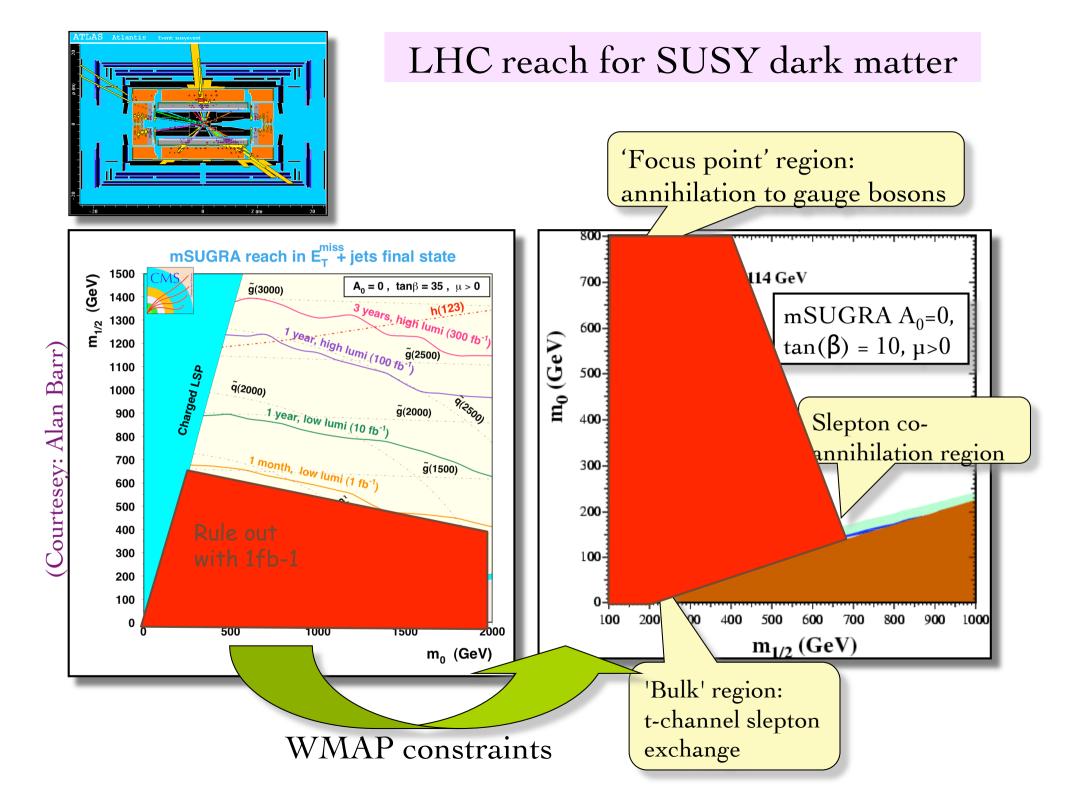
What *should* the world be made of ?

Mass	Particle	Symmetry/	Stability	Production	Abundance
scale		Quantum #			
$\Lambda_{ m QCD}$	Nucleons	Baryon	$\tau > 10^{33} yr$	freeze from	$\Omega_{ m B}$ ~10 ⁻¹⁰
		number	(dim-6 OK)	thermal equilibrium	<i>cf.</i> observed
				Asymmetric	$\Omega_{ m B} \sim 0.05$
				baryogenesis	
$\Lambda_{ m Fermi} \sim G_{ m F}^{-1/2}$	Neutralino?	R-parity?	Violated? (matter parity adequate for <i>p</i> stability)	'freeze-out' from thermal equilibrium	$\Omega_{\rm LSP} \sim 0.25$

$$H - \bigcup_{\tilde{t}}^{t} H \qquad H = \bigcup_{H \to H}^{\tilde{t}} H$$

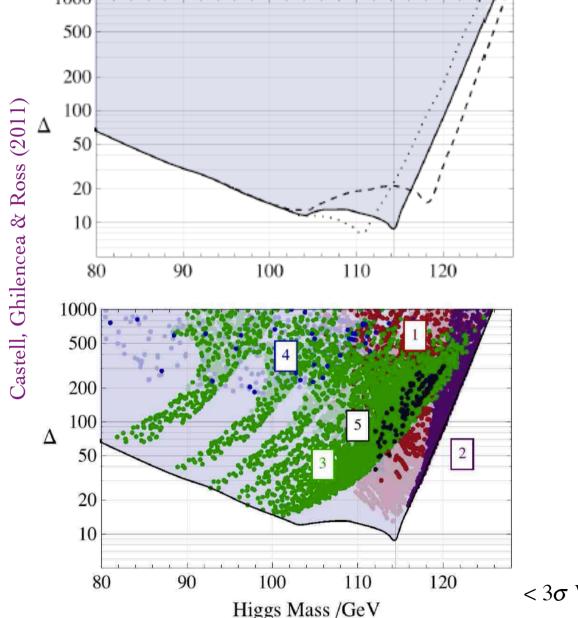
$$L^{SM}_{effective} \supset M_A A_\mu A^\mu + m_f \overline{f_L} f_R + M^2_{_H} |H|^2$$

For (softly broken) supersymmetry we have the 'WIMP miracle': $\Omega_{\chi}h^{2} \simeq \frac{3 \times 10^{-27} \text{cm}^{-3} \text{s}^{-1}}{\langle \sigma_{\text{ann}} v \rangle_{T=T_{\text{f}}}} \simeq 0.1 \quad \text{, since } \langle \sigma_{\text{ann}} v \rangle \sim \frac{g_{\chi}^{4}}{16\pi^{2} m_{\chi}^{2}} \approx 3 \times 10^{-26} \text{cm}^{3} \text{s}^{-1}$



'Natural' parameter space in the CMSSM

Heavy sparticles \rightarrow fine tuning of terms ... with measure: $\Delta(a_i) = \left| \frac{a_i}{M_Z} \frac{\partial M_Z}{\partial a_i} \right|$



 $\begin{array}{l} \displaystyle \begin{array}{l} \displaystyle \mbox{Relic density unrestricted} \\ \displaystyle \mbox{SUSY particle masses} \\ \displaystyle \begin{array}{l} \displaystyle 3.20 < 10^4 \ \mbox{Br}(b \rightarrow s \gamma) < 3.84 \\ \displaystyle \mbox{Br}(b \rightarrow \mu \mu) < 1.8 \times 10^{-8} \\ \displaystyle \quad \mbox{\delta} a_\mu < 292 \times 10^{-11} \\ \displaystyle -0.0007 < \delta \rho < 0.0012 \\ \displaystyle \begin{array}{l} \displaystyle \mbox{\Delta}_{\mbox{Min}} = 9, \quad \mbox{m}_h = 114 \pm 2 GeV \end{array} \end{array}$

Relic density restricted

- 1 h^0 resonant annihilation
- 2 \tilde{h} t-channel exchange
- 3 τ co-annihilation
- 4 \tilde{t} co-annihilation
- 5 A^0 / H^0 resonant annihilation

 $< 3\sigma$ WMAP: $\Delta_{Min} = 18$, $m_h = 115.9 \pm 2GeV$

What *should* the world be made of ?

Mass scale	Particle	Symmetry/ Quantum #	Stability	Production	Abundance
$\Lambda_{ m QCD}$	Nucleons	Baryon number	$\tau > 10^{33}yr$	'Freeze y from	$\Omega_{\rm B}$ ~10 ⁻¹⁰ cf.
			(dim-6 OK)	thermai equilibrium	observed
				Asymmetric	$\Omega_{\rm B} \sim 0.05$
				baryogenesis	
$\Lambda_{ m Fermi}$ ~	Neutralino?	R-parity?	violated?	'Freeze-out' from	$\Omega_{\rm LSP} \sim 0.25$
$G_{\rm F}^{-1/2}$		L. V		thermal equilibrium	201
СF	Technibaryon?	(walking) Technicolour	$\tau \sim 10^{18} yr \\ e^+ excess ? !$	Asymmetric (like the <i>observed</i> baryons)	$\Omega_{\mathrm{TB}} \sim 0.25$

A new particle would *share* in the B/L asymmetry if it is e.g. charged under a new global U(1) symmetry which has a mixed anomaly with SU(2) gauge symmetry ... this can *explain* the ratio of dark to baryonic matter!

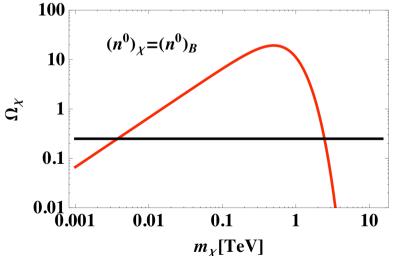
For example a TeV mass technibaryon would naturally have (Nussinov 1985):

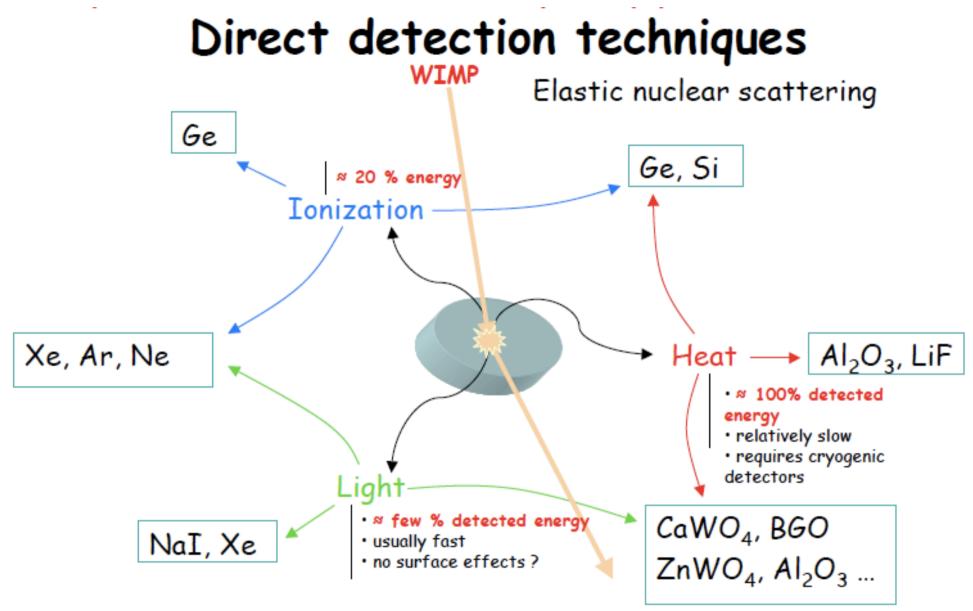
$$\frac{\rho_{\rm DM}}{\rho_{\rm B}} \sim \frac{m_{\rm DM}}{m_{\rm B}} \left(\frac{m_{\rm DM}}{m_{\rm B}}\right)^{3/2} {\rm e}^{-m_{\rm DM}/T_{\rm sphaleron}} \simeq 5$$

What *should* the world be made of ?

Mass	Particle	Symmetry/	Stability	Production	Abundance
scale		Quantum #			
$\Lambda_{ m QCD}$	Nucleons	Baryon	$\tau > 10^{33} yr$	'Freeze out' from	$\Omega_{\rm B} \sim 10^{-10} cf.$
, c		number	(dim-6 OK)	thermal equ. "brium	observed
				Asymmetric	$\Omega_{ m B} \sim 0.05$
				baryogenesis (how?)	
$\Lambda_{ m QCD}, \sim 5\Lambda_{ m QCD}$	Dark baryon	$U(1)_{\rm DB}$?	Asymmetric (like the <i>observed</i> baryons)	$\Omega_{\mathrm{DB}} \sim 0.25$
$\Lambda_{ m Fermi}$ ~	Neutralino?	R-parity?	violated?	'Freeze-out' from	$\Omega_{\rm LSP} \sim 0.25$
$G_{\rm F}^{-1/2}$				thermal equilibrium	
	Technibaryon?	(walking) Technicolour	$ au \sim 10^{18} \mathrm{yr}$ $e^+ \mathrm{excess}$?!	Asymmetric (like the <i>observed</i> baryons)	$\Omega_{TB} \sim 0.25$

For ~5 GeV mass the required abundance is *even* more natural (Gelmini *et al* 1987) and there are candidate particles in *bidden* sectors (Kaplan 1992, Hooper *et al* 2005, Kaplan *et al* 2009, Kribs *et al* 2009, Sannino & Zwicky 2010, An *et al* 2010, Cohen *et al* 2010, Frandsen *et al* 2011) with characteristic collider signatures ...





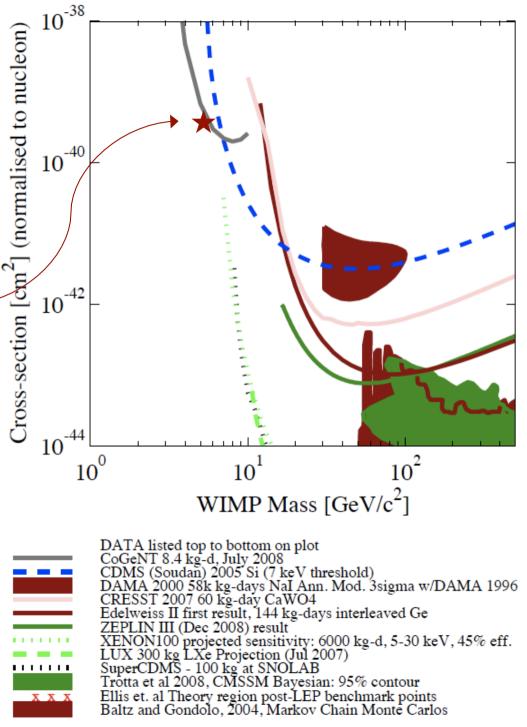
(Drukier & Stodolsky 1984; Goodman & Witten 1985)

No detection so far ... upper limits ($\sim 10^{-43}$ cm²) on scattering cross-section of ~ 100 GeV WIMPs, assuming local halo dark matter density ~ 0.3 GeV cm⁻³

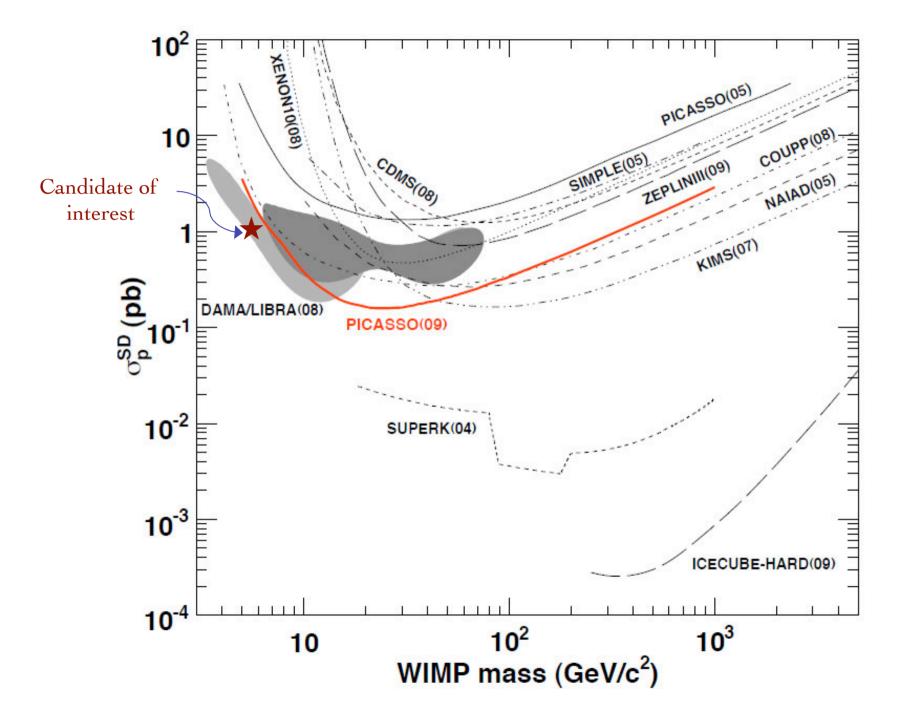
Experiments to directly detect dark matter through nuclear recoil are optimised for heavy WIMPs (motivated by SUSY) ... they have little sensitivity for low mass particles $\Rightarrow O(\text{keV})$ recoil energy

A ~5 GeV dark matter particle⁻⁻ may have gone undetected even if its interaction cross-section is as high as ~10⁻⁴⁰-10⁻³⁹ cm²

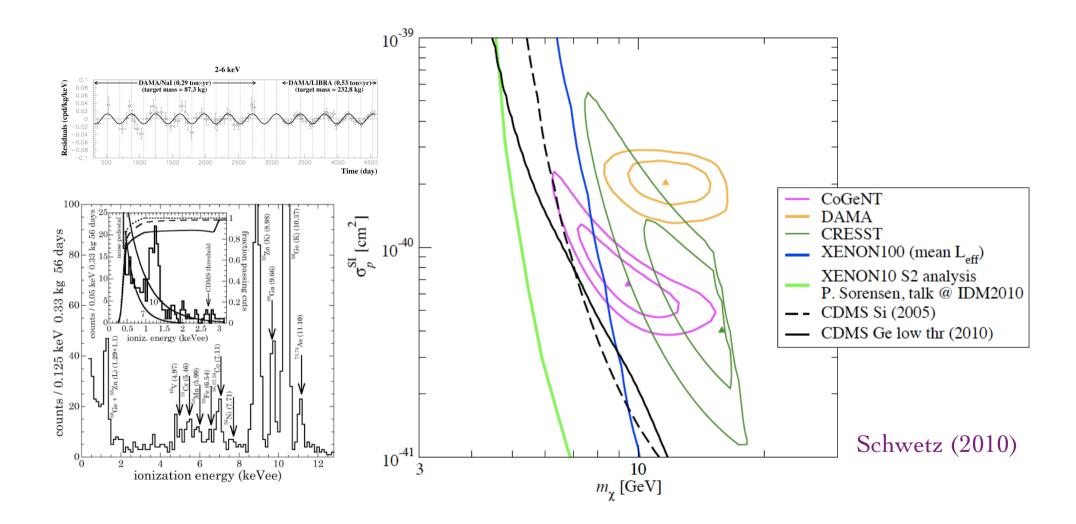
To detect such particles will require *low* threshold detectors



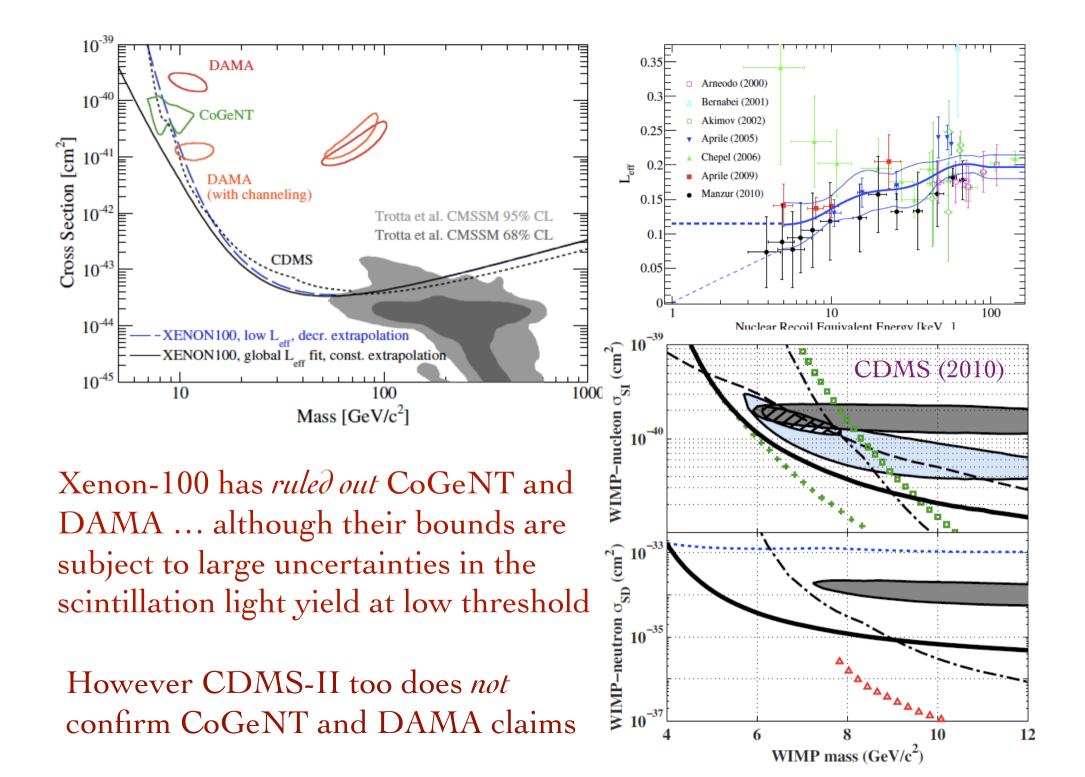
The spin *dependent* DM-nucleon cross-section can be as high as 10⁻³⁶ cm²



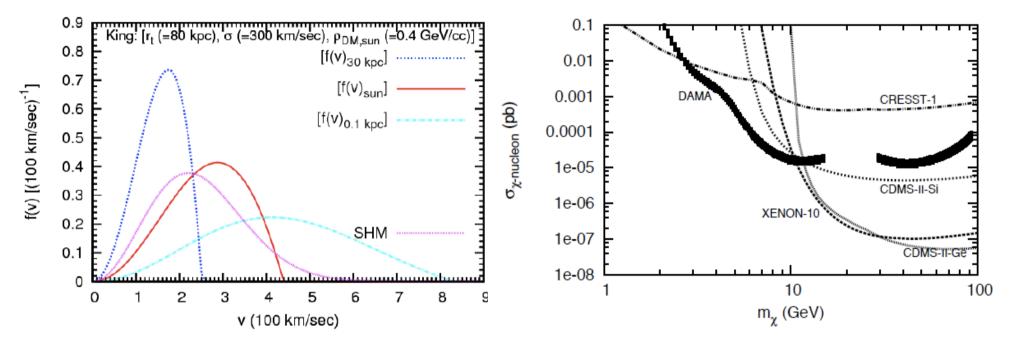
Some experiments (CoGeNT, DAMA, ...) have reported *possible* signals for ~5-10 GeV mass dark matter with $\sigma_{SI} \sim 10^{-40} \cdot 10^{-39} \text{ cm}^2$!



Efforts are currently underway to test these claims with low threshold detectors (XENON, CCDs ...)



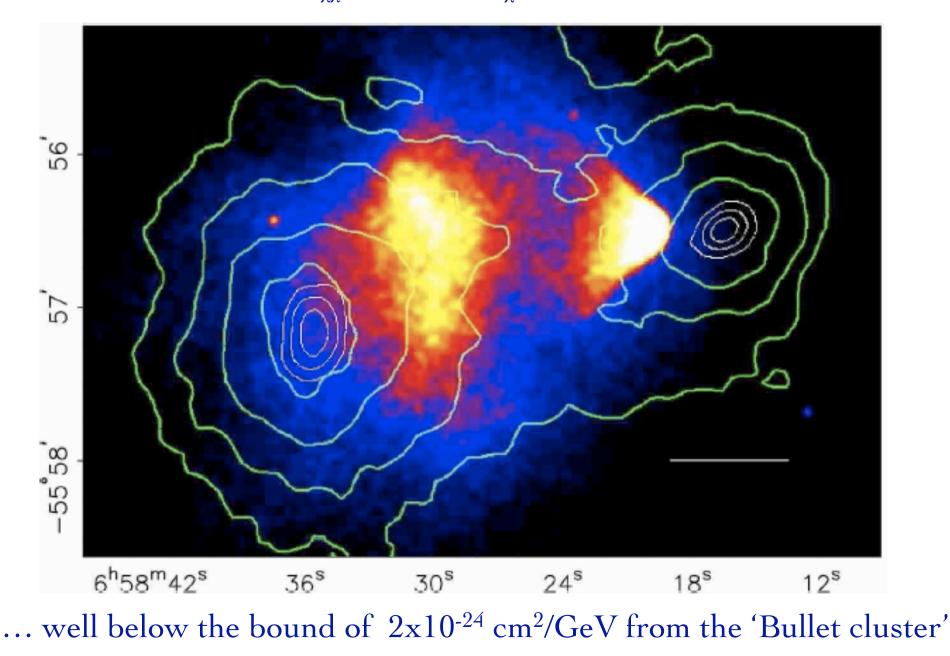
However all exclusion limits are sensitive to the *assumed* velocity distribution of dark matter in the Galaxy ... e.g. a *non*-Maxwellian distribution (determined self-consistently, taking into account the effect of baryons) changes the picture considerably (Chaudhury, Bhattacharjee & Cowsik, 2010)



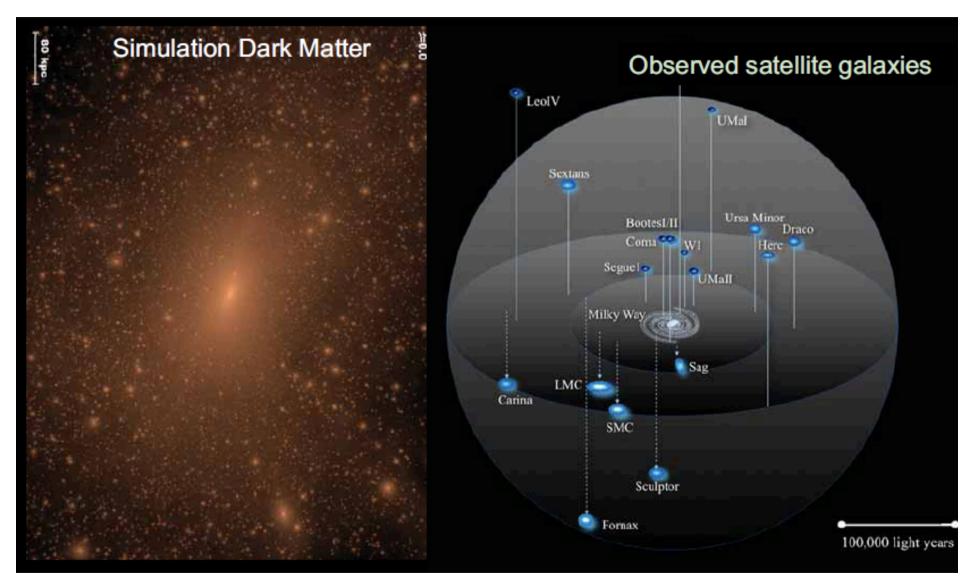
Moreover the escape velocity from the Galaxy and even the Sun's orbital velocity are not known very accurately and the local density of dark matter is uncertain by at least a factor of ~2 ... varying these parameters alters the limits Expect improved measurements from *GAIA* (2012)



ADM particles would be naturally **self-interacting** with a typical cross-section: $\sigma_{\chi\chi} \sim \sigma_{nn} (m_n/m_{\chi})^2$, where $\sigma_{nn} \sim 10^{-23} \text{ cm}^2$

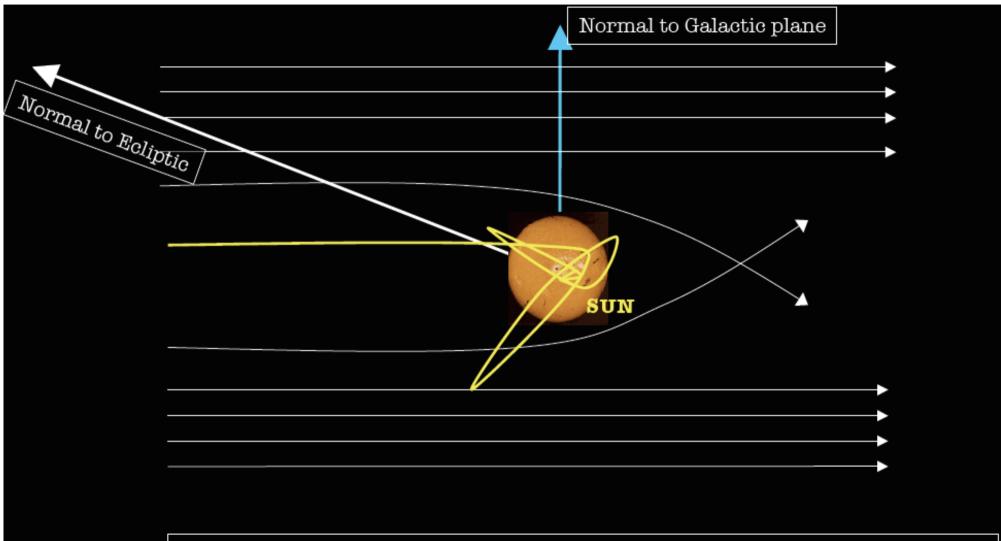


Self-interacting dark matter (Spergel & Steinhardt 2000) can reduce the excessive substructure seen in simulations of *collisionless* dark matter ...



e.g. the Milky Way has only ~25 dwarf galaxies, while >10³ are expected (not all are expected to be luminous, nevertheless there $i \omega$ a problem)

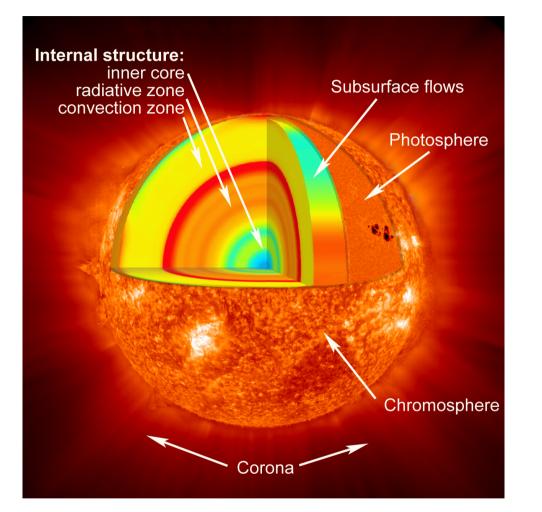
The Sun has been accreting dark matter particles for ~4.6 x 10⁹ yr as it orbits around the Galaxy ... these will orbit *inside* affecting energy transport



Flux of Dark Matter particles: 0.3 GeV /cm^3, at an average velocity v=270 km /s

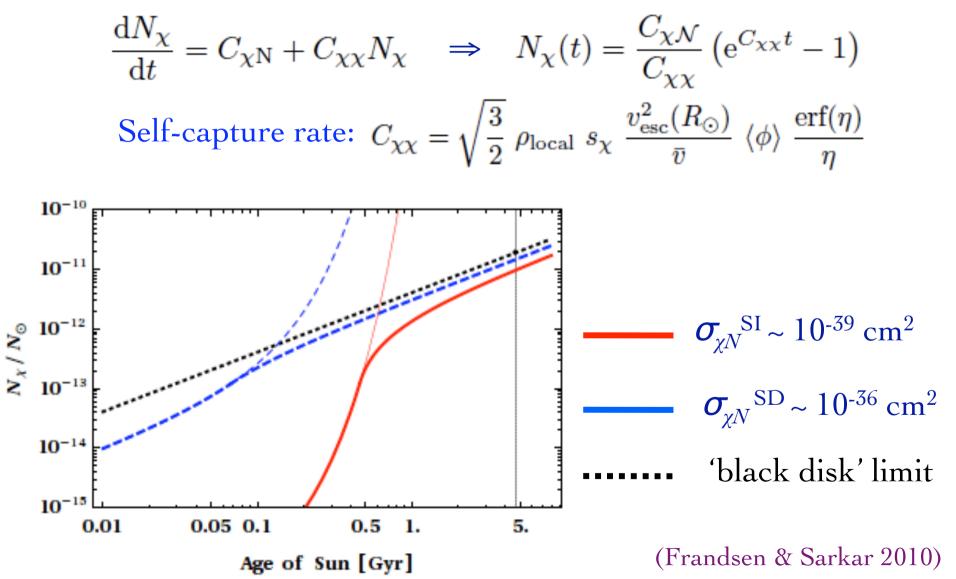
The flux of Solar neutrinos is *very* sensitive to the core temperature and can thus be affected (Faulkner *et al* 1985, Press & Spergel 1985, Gould 1987)

The particle mass must be ~5-10 GeV to have an effect on energy transport (too light and they 'evaporate', too heavy and their orbits do not extend out far enough)



Dark matter forms thermal core within the star with $r_{th} \sim \left[\frac{9kT}{8\pi G\rho_c m_{\chi}}\right]^{1/2}$ For the Sun and 5 GeV DM, this is ~ 4 x 10⁹ cm (orbit period ~ 10⁴ s) ... compare with Solar radius ~7x10¹⁰ cm (thermal diffusion time ~10¹⁵ s) Self-interactions will *increase* capture rate in the Sun (Zentner 2009)

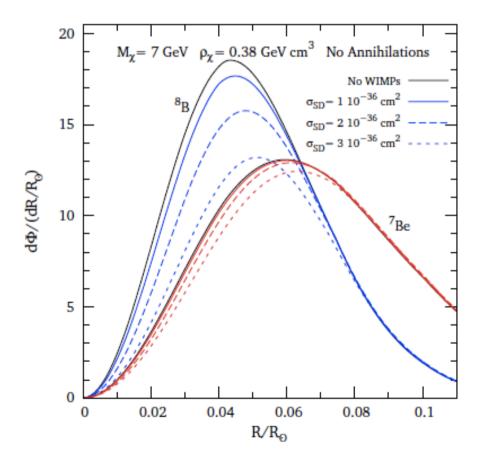
The abundance of *asymmetric* dark matter is not depleted by annihilation ... so grows exponentially (until geometric limit set by Solar radius)

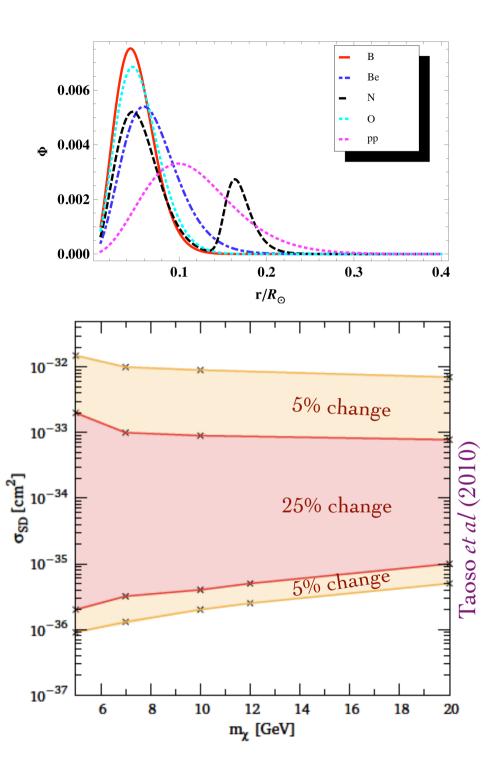


ADM will transport heat in the Sun:

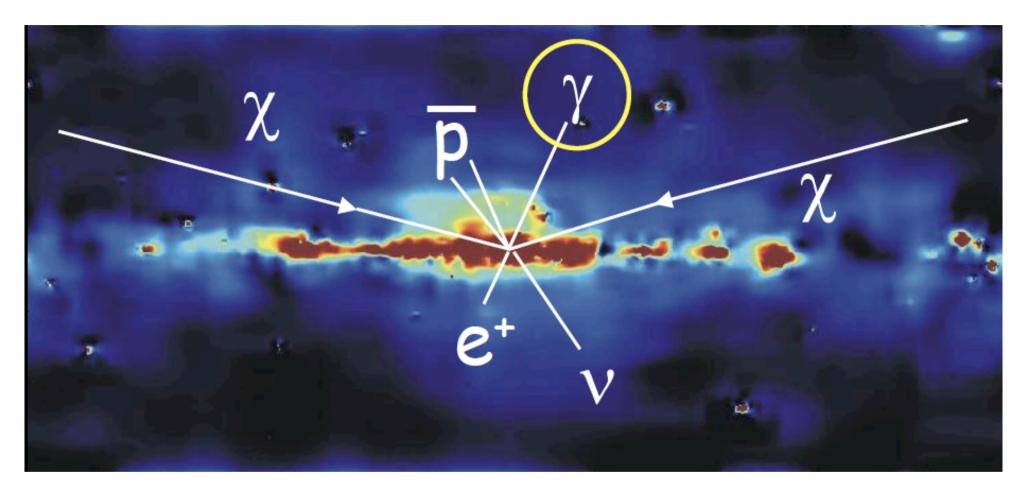
$$L_{\chi} \sim 4 \times 10^{12} L_{\odot} \frac{N_{\chi}}{N_{\odot}} \frac{\sigma_{\chi \rm N}}{\sigma_{\odot}} \sqrt{\frac{m_{\rm N}}{m_{\chi}}}$$

Modification of the luminosity profile will *reduce* low energy neutrino fluxes: ... this is testable by Borexino & SNO⁺





Many techniques for indirect detection ... and many claims!



The *PAMELA* 'excess' (e^+), *Fermi* 'excess' ($e^+ + e^-$), *WMAP* 'haze' (radio), ... have all been ascribed to dark matter annihilations or decays

These probe dark matter *elsewhere* in the Galaxy so usefully complement direct detection experiments ... but have other systematic uncertainties

The PAMELA 'anomaly'

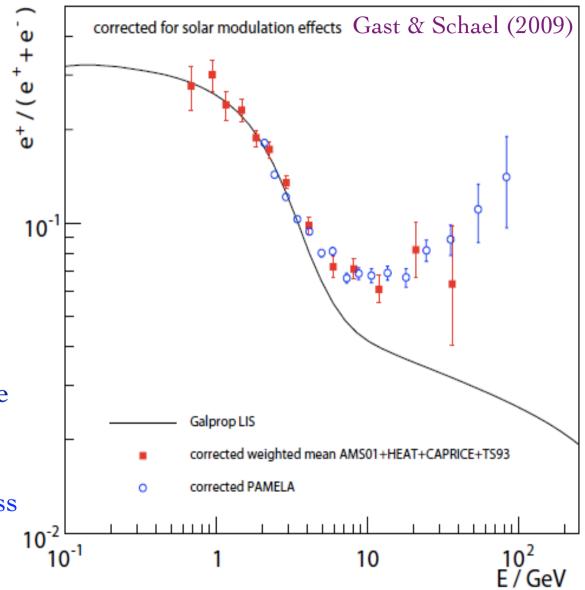
PAMELA has measured the positron fraction:

 $\frac{\phi_{e^+}}{\phi_{e^+}+\phi_{e^-}}$

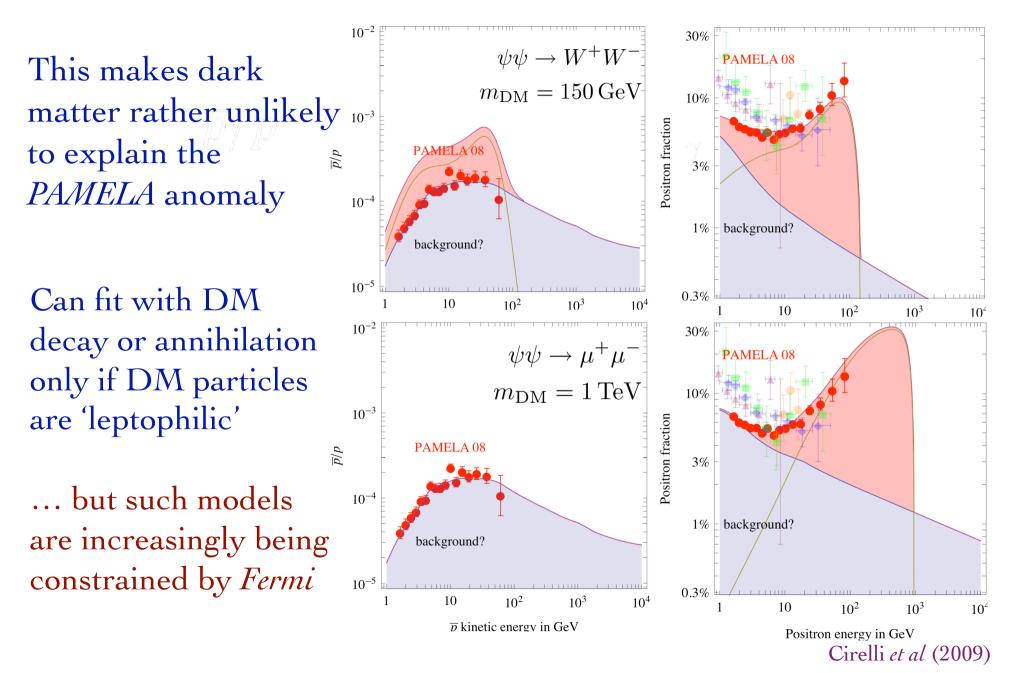
Anomaly \Rightarrow excess above 'astrophysical background'

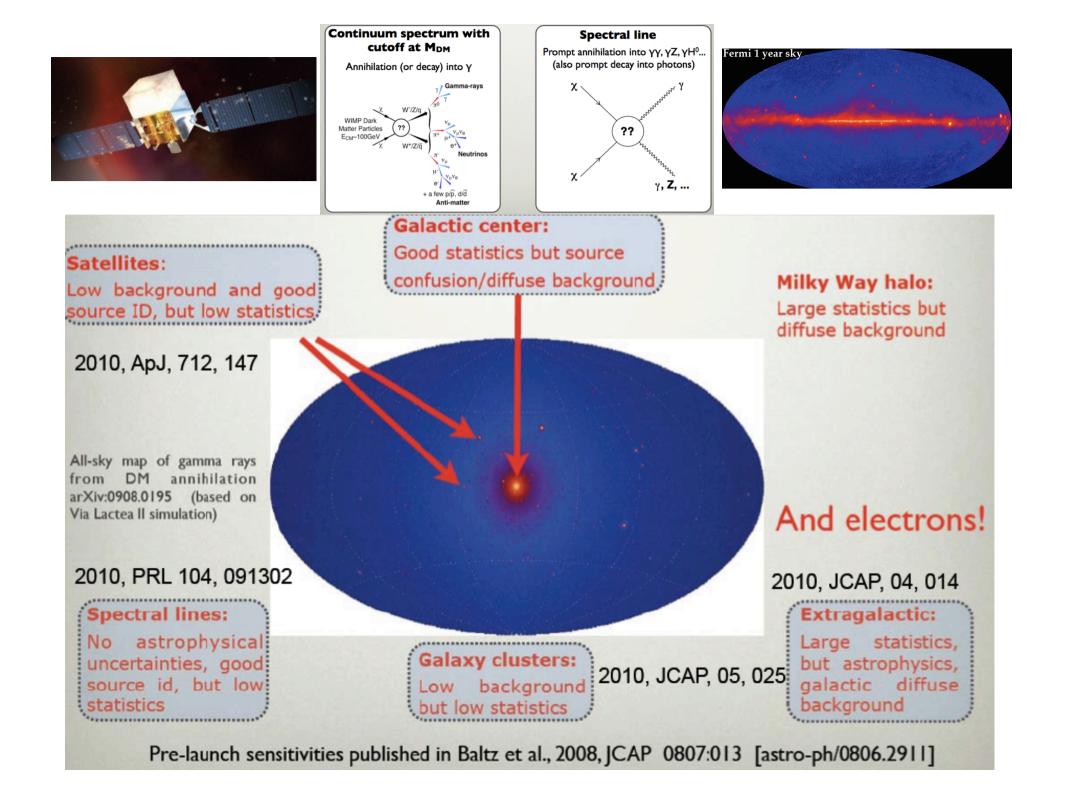
Widely attributed to dark matter annihilations/decays ... fits the spectral shape!

However predicted amplitude typically ~10-10⁴ too *small* ... while 'boost factor' due to clumping of dark matter is less than a factor of ~2-10

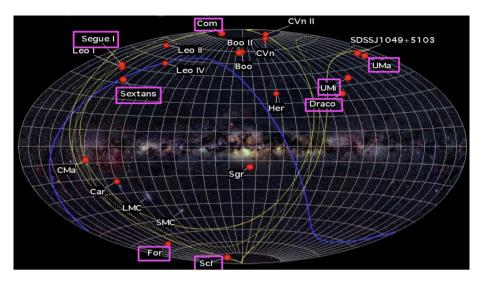


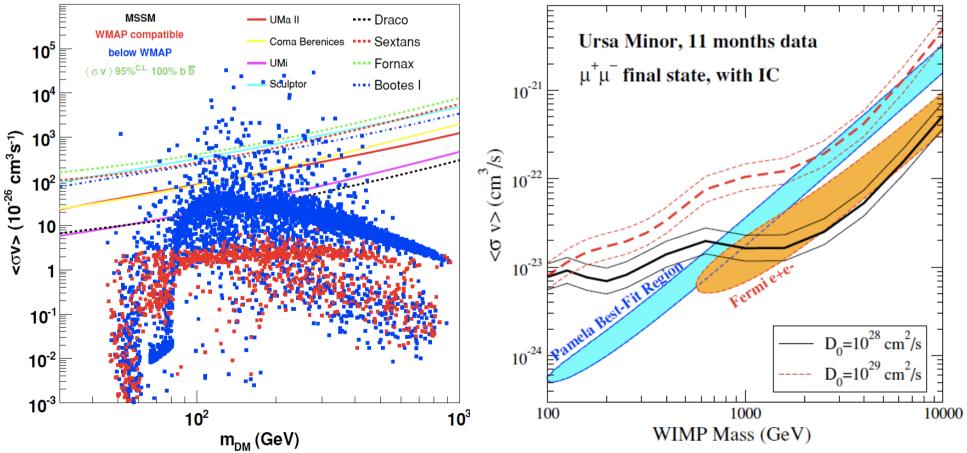
Moreover the observed antiproton flux is *consistent* with the background expectation (from standard cosmic ray propagation in the Galaxy)





Sensitivity to the annihilation signal from dSphs is however *very* dependent on how the dark matter distribution is modelled ... cored halos would reduce the signal by $\sim 10^2 - 10^3$ *cf.* cusps





What *should* the world be made of ?

Mass scale	Lightest stable particle	Symmetry/ Quantum #	Stability ensured?	Production	Abundance •
Λ _{QCD}	Nucleons	Baryon number	τ> 10 ³³ yr	'Freeze-out' from thermal equilibrium Asymmetric baryogenesis (how2)	$\Omega_{\rm B} \sim 10^{-10}$ cf. observed $\Omega_{\rm B} \sim 0.05$
$\Lambda_{\rm QCD}$, ~ 5 $\Lambda_{\rm QCD}$	Dark baryon	$U(1)_{\rm DB}$?	Asymmetric (due the observed haryons)	$\Omega_{\mathrm{DB}} \sim 0.3$
$\Lambda_{ m Fermi} \sim G_{ m F}^{-1/2}$	Neutralino? Technibaryon?	R-parity? (walking) Technic kur	violated? t~ 10 ¹⁸ yi	'freeze-out' from thermal equilibrium Asymmetric (like the observed baryons)	$\Omega_{\rm LSP} \sim 0.3$ $\Omega_{\rm TB} \sim 0.3$
$\Lambda_{ m hidden\ sector}\sim (\Lambda_{ m F} M_{ m P})^{1/2}$	Crypton? hidden valley?	Discrete (prodél-dependent)	€≥ 10 ¹⁸ yr	Varying gravitational field during inflation	$\Omega_{\rm X} \sim 0.3?$
$\begin{array}{c} \Lambda_{\text{see-saw}} \\ \sim \Lambda_{\text{Fermi}}^{2/} / \Lambda_{\text{B-L}} \end{array}$	Neutrinos	L toton oumber	Stable _.	Thermal (like CMB)	$\Omega_v > 0.003$
$\mathbf{M}_{ ext{string}}$ $\mathbf{M}_{ ext{Planck}}$	Kaluza-Kleiz states? Axions	? Peccei- Quinn	? stable	? Field oscillations	? $\Omega_{a} \gg 1!$

Summary

Experimental situation reminiscent of search for temperature fluctuations in the CMB in the '80s ... there were clear theoretical predictions but only upper limits on detection (on verge of causing crisis for theory) Finally breakthrough that transformed cosmology!

The theoretical expectations for dark matter are not as clear (being based on BSM physics) but there are many experimental approaches and interesting complementarities between them

There are bound to be some false alarms but it is a reasonable expectation that the nature of dark matter will be clarified soon experimentally