

Swampland program, extra dimensions and supersymmetry breaking

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Workshop on the Standard Model and Beyond

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Co-founder of Corfu meetings since 1982

1st Hellenic School on Elementary Particle Physics

Bibliographic information

Title	Proceedings of the 1st Hellenic School on Elementary Particle Physics, Corfu, Greece, 12-30 September 1982
Contributors	Th Papadopoulos, N. D. Tracas
Publisher	World Scientific, 1983
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STRONG CP VIOLATION AND AXION MECHANISM

[Ignatios Antoniadis](#) (Ecole Polytechnique)

1982

19 pages

Contribution to: [1st Hellenic School on Elementary Particle Physics](#), 613-631

then 1998 as a lecturer and regularly since 2005

Since 2004: European networks funded & organised Corfu meetings:

- “Quest for Unification” 2004-08
EP, U Lisbon, UA Madrid, U Bonn, Oxford, U Thessaloniki, U Valencia,
U Warsaw, INFN, SISSA, CEA-Saclay, CERN
- “Unification in the LHC era” 2009-13
- Also an ERC advanced grant
“Mass Hierarchy and Particle Physics at the TeV Scale” 2008-14

The European Institute for Sciences and their Applications (EISA)
is a big step forward promoting science and fundamental research
in Corfu island and Greece in general

THANK YOU GEORGE

Not all effective field theories can consistently coupled to gravity

- anomaly cancellation is not sufficient
- consistent ultraviolet completion can bring non-trivial constraints

those which do not, form the 'swampland'

criteria \Rightarrow conjectures

supported by arguments based on string theory and black-hole physics

Some well established examples:

- No exact global symmetries in Nature
- Weak Gravity Conjecture (WGC): gravity is the weakest force

\Rightarrow minimal non-trivial charge: $q \geq m$ in Planck units $8\pi G = \kappa^2 = 1$

Arkani-Hamed, Motl, Nicolis, Vafa '06

Distance/duality conjecture

At large distance in field space $\phi \Rightarrow$ tower of exponentially light states
 $m \sim e^{-\alpha\phi}$ with $\alpha \sim \mathcal{O}(1)$ parameter in Planck units

- provides a weakly coupled dual description up to the species scale

$$M_* = M_P / \sqrt{N} \qquad \text{Dvali '07}$$

- tower can be either

- 1 a Kaluza-Klein tower (decompactification of d extra dimensions)

$$M_* = M_P^{(4+d)} = (m^d M_P^2)^{1/(d+2)} \quad ; \quad m \sim 1/R, \quad \phi = \ln R$$

- 2 a tower of string excitations

$$M_* = m \sim \text{the associated string scale} = g_s M_P \quad ; \quad \phi = -\ln g_s$$

emergent string conjecture

Lee-Lerche-Weigand '19

smallness of physical parameters : large distance corner of landscape?

Theorem:

assuming a light gravitino (or gaugino) present in the string spectrum

$$M_{3/2} \ll M_P$$

$\Rightarrow \exists$ a tower of states with the same quantum numbers and masses

$$M_k = (2Nk + 1)M_{3/2}; \quad k = 1, 2, \dots; \quad N \text{ integer (not too large)}$$

Proof:

2D free-fermionic constructions $\Rightarrow N \lesssim 10$

2D bosonic lattices $\Rightarrow N \lesssim 10^3$

\Rightarrow compactification scale $m = \lambda_{3/2}^{-1} M_{3/2}$ with $\lambda_{3/2} = 1/2N$

Dark dimension proposal for the dark energy

$$m = \lambda^{-1} \Lambda^a \quad (M_P = 1) \quad ; \quad 1/4 \leq a \leq 1/2 \quad \text{Montero-Vafa-Valenzuela '22}$$

- distance $\phi = -\ln \Lambda$ Lust-Palti-Vafa '19
- $a \leq 1/2$: unitarity bound $m_{\text{spin-2}}^2 \geq 2H^2 \sim \Lambda$ Higuchi '87
- $a \geq 1/4$: estimate of 1-loop contribution $\Lambda \gtrsim m^4$

observations: $\Lambda \sim 10^{-120}$ and $m \gtrsim 0.01$ eV (Newton's law) $\Rightarrow a = 1/4$

astrophysical constraints $\Rightarrow d = 1$ extra dimension

\Rightarrow species scale (5d Planck mass) $M_* \simeq \lambda^{-1/3} 10^8$ GeV

$$10^{-4} \lesssim \lambda \lesssim 10^{-1}$$

Obviously such a low m cannot correspond to a string tower

Gravitino Mass Conjecture ^[6]

Cribiori-Lust-Scalisi, Castellano-Font-Herraez-Ibanez '21

$$m_2 = \lambda_{3/2}^{-1} M_{3/2}^n \quad (M_P = 1) \quad n > 0$$

4d supergravity in flat space: $M_{3/2} = \varkappa M_{\text{SUSY}}^2 \leftarrow$ VEV of F (or D) auxiliary

Low energy SUSY (linear or non-linear) $\Rightarrow M_{3/2} < M_{\text{SUSY}} \leq M_*$

However Standard Model soft terms depend on the mediation mechanism

- gravity mediation: $M_{\text{soft}} \sim M_{\text{SUSY}}^2 \sim M_{3/2}$
- gauge mediation: $M_{\text{soft}} \sim \alpha M_{\text{SUSY}}^2 / M_{\text{mess}} \leftarrow$ messenger mass $\gtrsim M_{\text{SUSY}}$
 \swarrow loop factor

Combine GMC with Dark Dimension proposal \Rightarrow two possibilities:

- ① one KK tower: $m_2 = m$
- ② two different towers: $m = m_1$ for DE and m_2 for SUSY breaking

Anchordoqui-I.A.-Cribiori-Lust-Scalisi '23

scenario 1: single KK tower

$$\Lambda = (\lambda/\lambda_{3/2})^4 M_{3/2}^{4n}$$

identified as leading non-vanishing power of $\text{Str}\mathcal{M}^{2k} \Rightarrow 2n$ is integer ≥ 1

requiring $M_{\text{SUSY}} \leq M_* \Rightarrow n \leq 2$ while $M_{\text{SUSY}} \gtrsim 10 \text{ TeV} \Rightarrow n \geq 1$

n	$M_{3/2} \times (\lambda_{3/2})^{-\frac{1}{n}} \text{ GeV}^{-1}$	$M_{\text{SUSY}} \times \varkappa^{\frac{1}{2}} (\lambda_{3/2})^{-\frac{1}{2n}} \text{ GeV}^{-1}$
1	2.5×10^{-9}	7.8×10^4
3/2	2.5×10^0	2.5×10^9
2	7.8×10^4	4.4×10^{11}

$n = 1$ requires gauge mediation

while $n = 2$ (with tuning of $\varkappa(\lambda_{3/2})^{-\frac{1}{2n}}$) gravity mediation

also $n = 3/2$

More physics implications of the dark dimension

- natural explanation of neutrino masses introducing ν_R in the bulk

recent analysis of ν -oscillation data with 3 bulk neutrinos \Rightarrow

$$m \gtrsim 2.5 \text{ eV} \quad (R \lesssim 0.4 \mu\text{m}) \quad \text{Forero-Giunti-Ternes-Tyagi '22}$$

$$\Rightarrow \lambda \lesssim 10^{-3} \text{ and } M_* \sim 10^9 \text{ GeV}$$

the bound can be relaxed in the presence of bulk ν_R -neutrino masses

Lukas-Ramond-Romanino-Ross '00, Carena-Li-Machado²-Wagner '17

support on Dirac neutrinos by the sharpened WGC

non-SUSY AdS vacua (flux supported) are unstable Ooguri-Vafa '16

avoid 3d AdS vacuum of the Standard Model with Majorana neutrinos

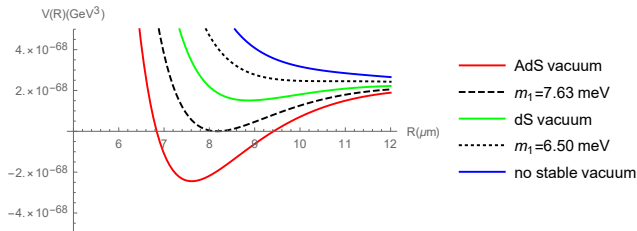
radion stabilisation: 4d cosmological constant versus Casimir energy

Arkani-Hamed, Dubovsky, Nicolis, Villadoro '07

⇒ Dirac neutrinos with a lightest mass \lesssim few eV

Ibanez, Martin-Lozano, Valenzuela '17

or a light gravitino in the meV range Anchordoqui-I.A.-Cunat '23



More physics implications of the dark dimension

- 3 candidates of dark matter:

- ① 5D primordial black holes in the mass range $10^{15} - 10^{21}$ g
with Schwarzschild radius in the range $10^{-4} - 10^{-2}$ μ m

Anchordoqui-I.A.-Lust '22

- ② KK-gravitons of decreasing mass due to internal decays (dynamical DM)
from \sim MeV at matter/radiation equality ($T \sim$ eV) to \sim 50 keV today

Gonzalo-Montero-Obied-Vafa '22

possible equivalence between the two

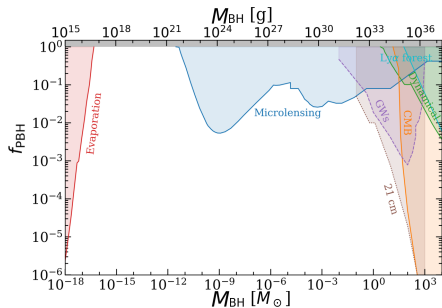
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- ultralight radion as a fuzzy dark matter

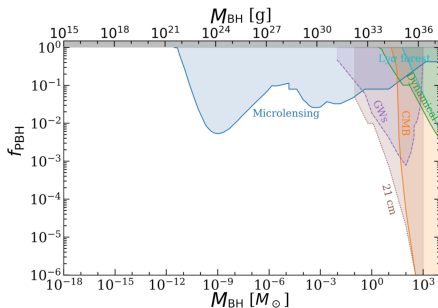
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Primordial Black Holes as Dark Matter

4d PBH



5d PBH



5D BHs live longer than 4D BHs of the same mass

Fuzzy dark matter & the Pulsar Timing Array signal

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FDM: ultralight bosonic particles with wave-like behavior at galactic scales

$$\lambda_{\text{dB}} \equiv \frac{2\pi}{mv} = 4.8 \text{ kpc} \left(\frac{10^{-23} \text{ eV}}{m} \right) \left(\frac{250 \text{ km/s}}{v} \right)$$

⇒ at larger distances FDM behaves as CDM

PTA signal: time arrival stochastic sinusoidal oscillations

of amplitude $\mathcal{A} \sim 10^{-15}$ at frequency $f \sim$ a few nHz

Similar signal can be produced by FDM

of mass $m \sim 10^{-23}$ eV using $\rho_{\text{DM}} \sim 0.4 \text{ GeV/cm}^3$

oscillations generate fluctuations in metric perturbations

⇒ (quasi) stabilised **radion as fuzzy dark matter**

Dark dimension radion as fuzzy dark matter

Anchordoqui-IA-Lust '23

- radion mass: $m_\phi \sim \sqrt{V_{\phi\phi}} \sim \sqrt{\Lambda_4}/M_p$ $f = \omega/(2\pi) = m/\pi$
- radion production: (inflaton decay) via unstable KK gravitons

$$\Gamma_R^{\text{KK}} = \sum_{I' < I} \Gamma_{RI'}^I \sim \frac{1}{2\pi} \frac{m_I m_{\text{KK}}^3}{m M_p^2} \langle \varphi_{I'} \rangle \simeq \frac{1}{2\pi} \frac{m_I m_{\text{KK}}^3 (RM_*)}{m M_p^2}$$

Mohapatra, Nussinov, Perez-Lorenzana

$$= \frac{1}{2\pi} \frac{m_I m_{\text{KK}}^3}{m M_*^2} \sim 10^6 \text{ s}^{-1} \quad m_{\text{KK}} = 10 \text{ eV}$$

⇒ KK-tower → radion before the QCD phase transition age $\sim 20 \mu\text{s}$

- suppress radion coupling to matter: add a localised kinetic term

$$\delta S_{\text{radion}}^{\text{localised}} = \zeta \int [d^4x] \left(\frac{\partial R}{R} \right)^2 \quad \zeta : \text{VEV of a brane field}$$

also Albrecht-Burgess-Ravndal-Skordis '01

Conclusions

smallness of some physical parameters might signal

a large distance corner in the string landscape of vacua

such parameters can be the scales of dark energy and SUSY breaking

mesoscopic dark dimension proposal: interesting phenomenology

neutrino masses, dark matter, cosmology, SUSY breaking

- minimal scenario for SUSY breaking very attractive

$M_{3/2} \sim \text{eV}$, $M_{\text{SUSY}} \sim \text{ten's of TeV}$, require gauge mediation

- 2 more cases are possible: $M_{3/2} \sim (1/R)^{1/n}$ for $n = 3/2, 2$

$M_{\text{SUSY}} \sim M_* \sim 10^9 \text{ GeV}$ with $M_{3/2} \sim \mathcal{O}(\text{GeV-TeV})$

Large extra dimensions from higher dim inflation

- connect the weakness of gravity to the size of the observable universe