

# B anomalies in the post- $R_K$ era

**Nazila Mahmoudi**

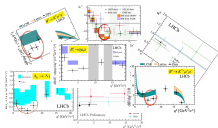
Lyon University and CERN

In collaboration with T. Hurth and S. Neshatpour



**Workshop on Standard Model and Beyond  
Corfu, 27 August - 7 September 2023**

- Status of anomalies

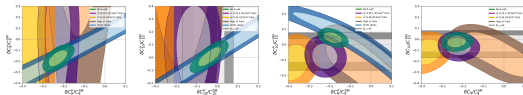


- Theoretical framework and issues

$$\mathcal{A}_\lambda^{(\text{had})} = -i \frac{e^2}{q^2} \int d^4x e^{-iq \cdot x} \langle \ell^+ \ell^- | J_\mu^{\text{em, lept}}(x) | 0 \rangle$$

$$\times \int d^4y e^{iq \cdot y} \langle \bar{K}_\lambda^* | T \{ J^{\text{em, had}, \mu}(y) \mathcal{H}_{\text{eff}}^{\text{had}}(0) \} | \bar{B} \rangle$$

- New Physics implications



- Conclusions

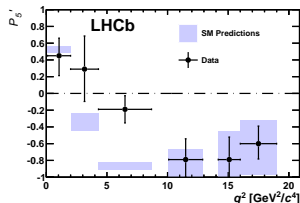
$B^0 \rightarrow K^{*0} \mu^+ \mu^-$  angular observables, in particular  $P'_5 / S_5$

- 2013 ( $1 \text{ fb}^{-1}$ ): disagreement with the SM for  $P_2$  and  $P'_5$  (PRL 111, 191801 (2013))
- March 2015 ( $3 \text{ fb}^{-1}$ ): confirmation of the deviations (LHCb-CONF-2015-002)
- Dec. 2015: 2 analysis methods, both show the deviations (JHEP 1602, 104 (2016))

$3.7\sigma$  deviation in the 3rd bin

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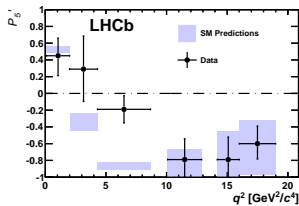


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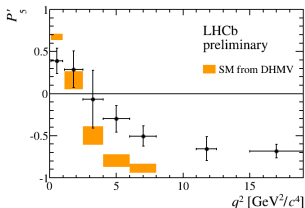
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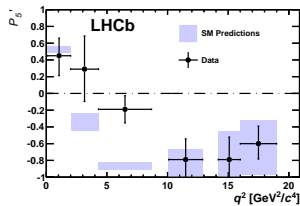


2.9 $\sigma$  in the 4th and 5th bins  
(3.7 $\sigma$  combined)

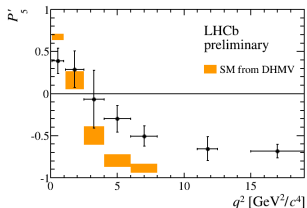
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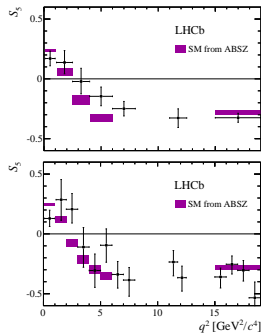
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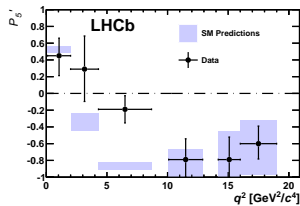


3.4 $\sigma$  combined fit (likelihood)

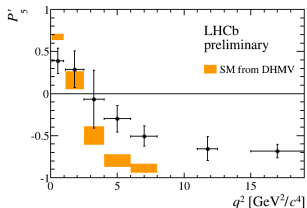
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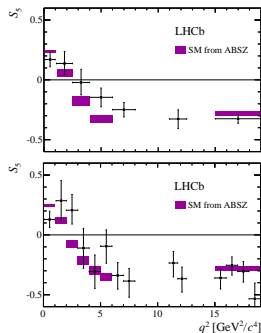
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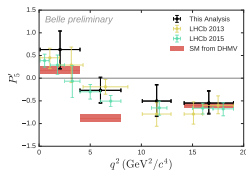


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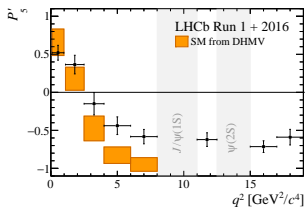


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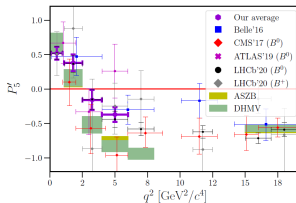
Belle supports LHCb  
(arXiv:1604.04042)  
tension at 2.1 $\sigma$



$P_5'(B^0 \rightarrow K^{*0} \mu^+ \mu^-)$ : 2020 LHCb update with  $4.7 \text{ fb}^{-1}$ :  $\sim 2.9\sigma$  local tension



Phys. Rev. Lett. 125, 011802 (2020)

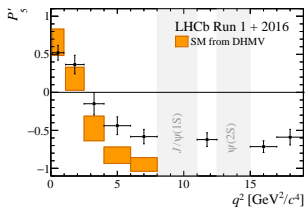


ATLAS-CONF-2017-023; CMS-PAS-BPH-15-008

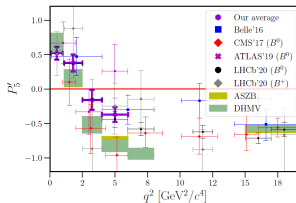


## Tension in the angular observables - 2020 updates

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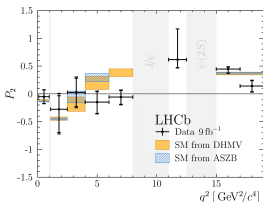


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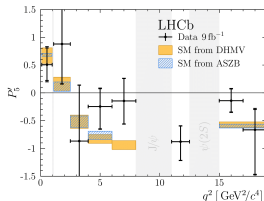


ATLAS-CONF-2017-023; CMS-PAS-BPH-15-008

First measurement of  $B^+ \rightarrow K^{*+} \mu^+ \mu^-$  angular observables using the full Run 1 and Run 2 dataset ( $9 \text{ fb}^{-1}$ ):

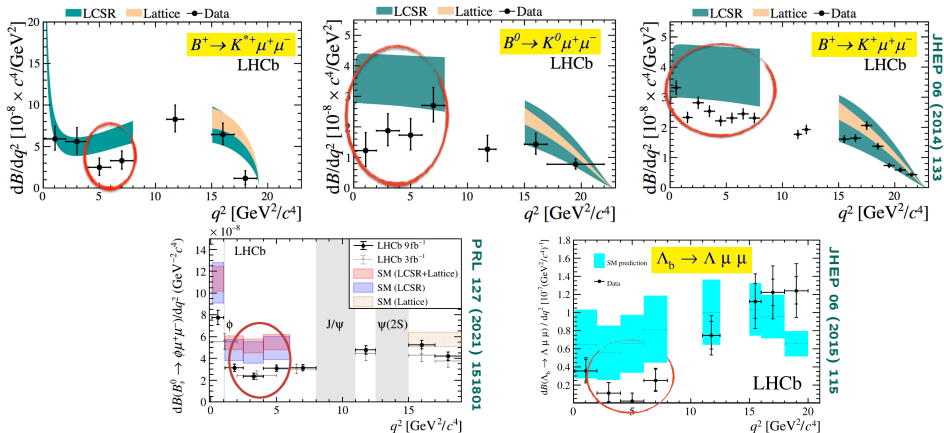


Phys. Rev. Lett. 126, 161802 (2021)



The results confirm the global tension with respect to the SM!

# Tension in the $b \rightarrow s \ell \ell$ Branching Ratios



- consistent deviation pattern with the SM predictions
- significance of the deviations between  $\sim 2$  and  $3.5 \sigma$
- general trend:  $\text{EXP} < \text{SM}$  in low  $q^2$  regions
- ... but the branching ratios have very large theory uncertainties!

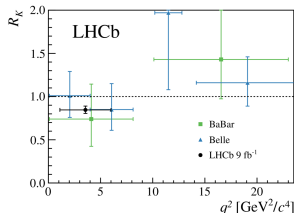
## Lepton flavour universality in $B^+ \rightarrow K^+ \ell^+ \ell^-$

$$R_K = BR(B^+ \rightarrow K^+ \mu^+ \mu^-) / BR(B^+ \rightarrow K^+ e^+ e^-)$$

- SM prediction very accurate:  $R_K^{\text{SM}} = 1.0006 \pm 0.0004$
- March 2021 using  $9 \text{ fb}^{-1}$

$$R_K^{\text{exp}} = 0.846^{+0.042}_{-0.039}(\text{stat})^{+0.013}_{-0.012}(\text{syst})$$

- $3.1\sigma$  tension in the  $[1.1-6] \text{ GeV}^2$  bin



Nature Phys. 18 (2022) 3, 277

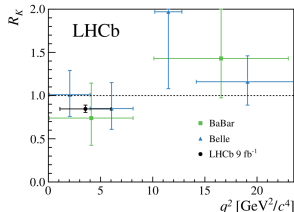
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## Lepton flavour universality in $B^0 \rightarrow K^{*0} \ell^+ \ell^-$

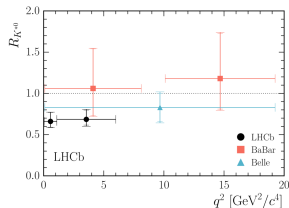
$$R_{K^*} = BR(B^0 \rightarrow K^{*0} \mu^+ \mu^-) / BR(B^0 \rightarrow K^{*0} e^+ e^-)$$

- LHCb measurement from April 2017 using  $3 \text{ fb}^{-1}$
- Two  $q^2$  regions: [0.045-1.1] and [1.1-6.0]  $\text{GeV}^2$

$$R_{K^*}^{\text{exp, bin1}} = 0.66_{-0.07}^{+0.11}(\text{stat}) \pm 0.03(\text{syst})$$

$$R_{K^*}^{\text{exp, bin2}} = 0.69_{-0.07}^{+0.11}(\text{stat}) \pm 0.05(\text{syst})$$

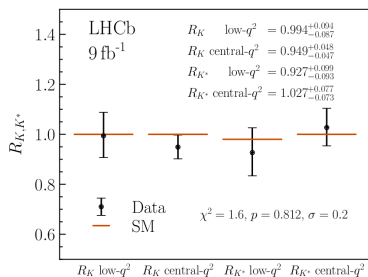
- $2.2\text{-}2.5\sigma$  tension in each bin



JHEP 08 (2017) 055

## December 2022 update

- LHCb measurement from Dec 2022 using  $9 \text{ fb}^{-1}$
- New modelling of residual backgrounds due to misidentified hadronic decays
- Results fully compatible with the SM



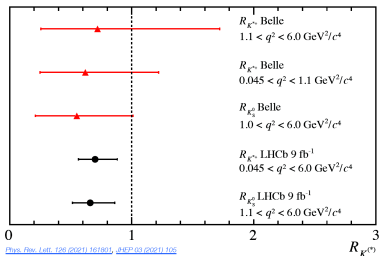
LHCb, [arXiv:2212.09152](https://arxiv.org/abs/2212.09152), [arXiv:2212.09153](https://arxiv.org/abs/2212.09153)

## Two other LFU measurements (October 2021) with $9 \text{ fb}^{-1}$ :

$$B^+ \rightarrow K^{*+} \ell^+ \ell^- \text{ and } B^0 \rightarrow K_S^0 \ell^+ \ell^-$$

$$R_{K^{*+}} = 0.70_{-0.13}^{+0.18}(\text{stat})_{-0.04}^{+0.03}(\text{syst}) \text{ and } R_{K_S^0} = 0.66_{-0.15}^{+0.20}(\text{stat})_{-0.04}^{+0.02}(\text{syst})$$

Phys.Rev.Lett. 128 (2022) 19, 191802



## More measurements to come:

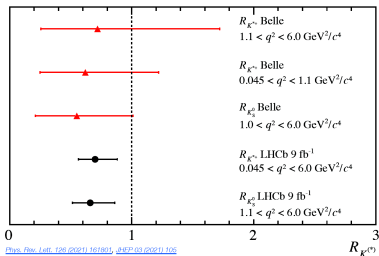
$$B_s^0 \rightarrow \phi \ell^+ \ell^-, B \rightarrow \pi \ell^+ \ell^-, B \rightarrow K \pi^+ \pi^- \ell^+ \ell^-, \dots$$

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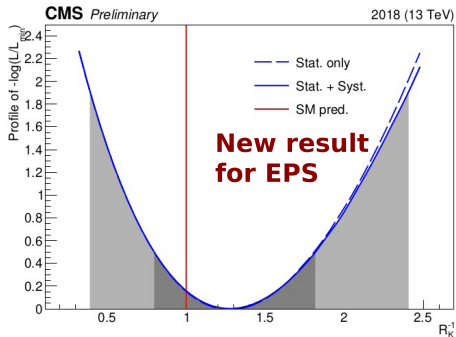
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## More measurements to come:

$$B_s^0 \rightarrow \phi \ell^+ \ell^-, B \rightarrow \pi \ell^+ \ell^-, B \rightarrow K \pi^+ \pi^- \ell^+ \ell^-, \dots$$

## First $R_K$ measurement by CMS (August 2023):

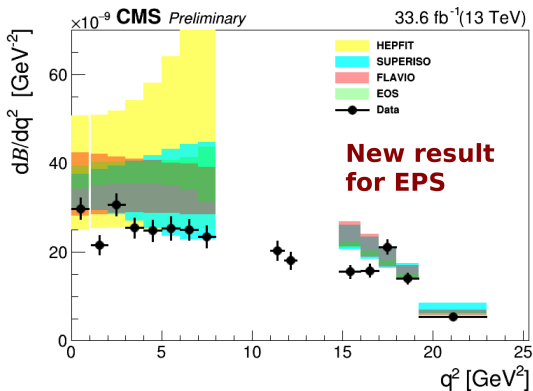


$$R_K = 0.78^{+0.46}_{-0.23}(\text{stat})^{+0.09}_{-0.05}(\text{syst})$$

Uncertainty dominated by the low stats of  $B \rightarrow K_{ee}$

See G. Karathanasis' talk at EPS 2023



Differential BR measurement of  $B^+ \rightarrow K^+ \mu^+ \mu^-$  (August 2023):

See G. Karathanasis' talk at EPS 2023

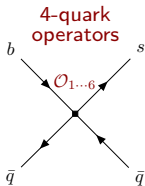
## Effective field theory

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left( \sum_{i=1 \dots 10, S, P} (C_i(\mu) \mathcal{O}_i(\mu) + C_i'(\mu) \mathcal{O}_i'(\mu)) \right)$$

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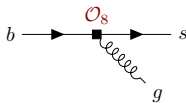
### Operator set for $b \rightarrow s$ transitions:



$$\mathcal{O}_{1,2} \propto (\bar{s} \Gamma_{\mu} c) (\bar{c} \Gamma^{\mu} b)$$

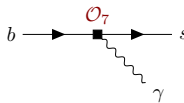
$$\mathcal{O}_{3,4} \propto (\bar{s} \Gamma_{\mu} b) \sum_q (\bar{q} \Gamma^{\mu} q)$$

chromomagnetic dipole operator



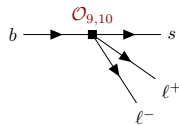
$$\mathcal{O}_8 \propto (\bar{s} \sigma^{\mu\nu} T^a P_R) G_{\mu\nu}^a$$

electromagnetic dipole operator



$$\mathcal{O}_7 \propto (\bar{s} \sigma^{\mu\nu} P_R) F_{\mu\nu}$$

semileptonic operators



$$\mathcal{O}_9^{\ell} \propto (\bar{s} \gamma^{\mu} b_L) (\bar{\ell} \gamma_{\mu} \ell)$$

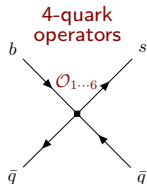
$$\mathcal{O}_{10}^{\ell} \propto (\bar{s} \gamma^{\mu} b_L) (\bar{\ell} \gamma_{\mu} \gamma_5 \ell)$$

+ the chirality flipped counter-parts of the above operators,  $\mathcal{O}'_i$

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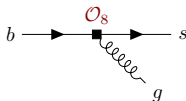
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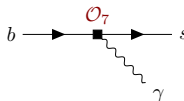
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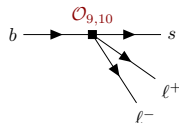
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+ the chirality flipped counter-parts of the above operators,  $\mathcal{O}'_i$

### Wilson coefficients:

The Wilson coefficients are calculated perturbatively and are process independent.

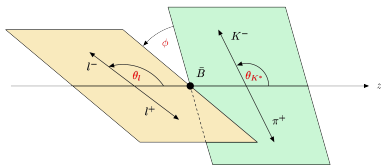
SM contributions known to NNLL (Bobeth, Misiak, Urban '99; Misiak, Steinhauser '04, Gorbahn, Haisch '04; Gorbahn, Haisch, Misiak '05; Czakon, Haisch, Misiak '06,...)

$$C_7 \sim -0.3 \quad C_9 \sim 4.2 \quad C_{10} \sim -4.2$$

$$B \rightarrow K^* \mu^+ \mu^-$$

## $B \rightarrow K^*(\rightarrow K^+ \pi^-) \mu^+ \mu^-$ Angular distributions

Angular behavior of  $K^+$  and  $\pi^- \rightarrow$  additional information on the helicity of  $K^*$



Differential decay distribution:

$$\frac{d^4\Gamma}{dq^2 d \cos \theta_\ell d \cos \theta_{K^*} d\phi} = \frac{9}{32\pi} J(q^2, \theta_\ell, \theta_{K^*}, \phi)$$

$$J(q^2, \theta_\ell, \theta_{K^*}, \phi) = \sum_i J_i(q^2) f_i(\theta_\ell, \theta_{K^*}, \phi)$$

↘ angular coefficients  $J_{1-9}$

↘ functions of the spin amplitudes  $A_0, A_{\parallel}, A_{\perp}, A_t,$  and  $A_S$

Spin amplitudes: functions of Wilson coefficients and form factors

Main operators:

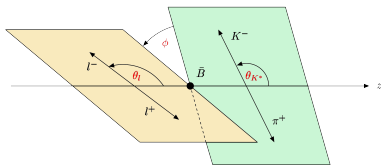
$$\mathcal{O}_9 = \frac{e^2}{(4\pi)^2} (\bar{s} \gamma^\mu b_L) (\bar{\ell} \gamma_\mu \ell), \quad \mathcal{O}_{10} = \frac{e^2}{(4\pi)^2} (\bar{s} \gamma^\mu b_L) (\bar{\ell} \gamma_\mu \gamma_5 \ell)$$

$$\mathcal{O}_S = \frac{e^2}{16\pi^2} (\bar{s}_L^\alpha b_R^\alpha) (\bar{\ell} \ell), \quad \mathcal{O}_P = \frac{e^2}{16\pi^2} (\bar{s}_L^\alpha b_R^\alpha) (\bar{\ell} \gamma_5 \ell)$$

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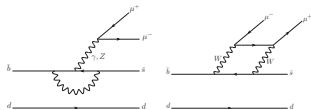
- ↘ angular coefficients  $J_{1-9}$
- ↘ functions of the spin amplitudes  $A_0, A_{\parallel}, A_{\perp}, A_t,$  and  $A_S$

Spin amplitudes: functions of Wilson coefficients and form factors

Main operators:

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$$\mathcal{O}_S = \frac{e^2}{16\pi^2} (\bar{s}_L^\alpha b_R^\alpha) (\bar{\ell} \ell), \quad \mathcal{O}_P = \frac{e^2}{16\pi^2} (\bar{s}_L^\alpha b_R^\alpha) (\bar{\ell} \gamma_5 \ell)$$



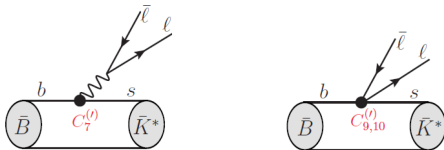
## Issue of the hadronic power corrections

Effective Hamiltonian for  $b \rightarrow s \ell^+ \ell^-$  transitions:  $\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{had}} + \mathcal{H}_{\text{eff}}^{\text{sl}}$

Matrix elements of  $B \rightarrow K^* \ell^+ \ell^-$  decay:

$$\mathcal{H}_{\text{eff}}^{\text{sl}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=7,9,10} C_i^{(\prime)}(\mu) O_i^{(\prime)}(\mu) \right]$$

$\langle \bar{K}^* \ell^+ \ell^- | H_{\text{eff}}^{\text{sl}} | \bar{B} \rangle$ :



$\Rightarrow B \rightarrow K^*$  form factors  $V, A_{0,1,2}, T_{1,2,3}$  or alternatively  $\tilde{V}_\lambda, \tilde{T}_\lambda, \tilde{S}$  ( $\lambda = \text{helicity of } K^*$ )

Helicity amplitudes:

$$H_V(\lambda) \approx -i N' \left\{ (C_9 - C_9') \tilde{V}_\lambda(q^2) + \frac{m_B^2}{q^2} \left[ \frac{2\hat{m}_b}{m_B} (C_7^{\text{eff}} - C_7') \tilde{T}_\lambda(q^2) \right] \right\}$$

$$H_A(\lambda) = -i N' (C_{10} - C_{10}') \tilde{V}_\lambda(q^2)$$

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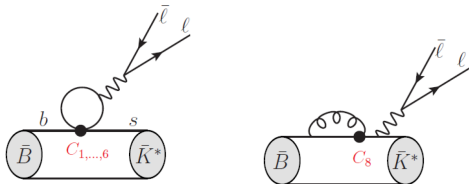
## Issue of the hadronic power corrections

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$H_{\text{eff}}^{\text{had}}$  contributes to  $b \rightarrow s \bar{\ell} \ell$  through virtual photon exchange  $\Rightarrow$  affect only the  $H_V(\lambda)$

Helicity amplitudes:

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In general “naïve” factorization not applicable

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$$(C_9^{\text{eff}} \equiv C_9 + Y(q^2))$$

Helicity amplitudes:

$$H_V(\lambda) = -i N' \left\{ (C_9^{\text{eff}} - C_9') \tilde{V}_\lambda(q^2) + \frac{m_B^2}{q^2} \left[ \frac{2\hat{m}_b}{m_B} (C_7^{\text{eff}} - C_7') \tilde{T}_\lambda(q^2) - 16\pi^2 \mathcal{N}_\lambda(q^2) \right] \right\}$$

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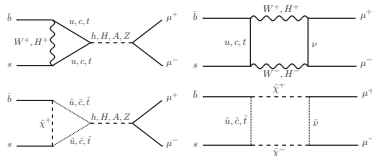
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Largest contributions in SM from a Z penguin top loop and a W box diagram

Main source of uncertainty:

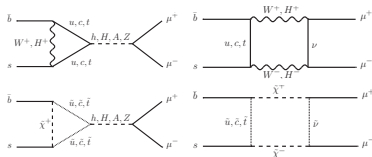
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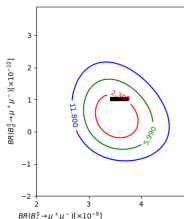
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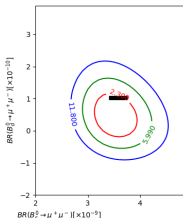
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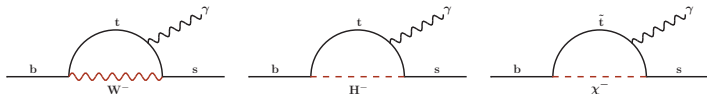
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Contributing loops:



Main operator:  $\mathcal{O}_7$

but higher order contributions from  $\mathcal{O}_1, \dots, \mathcal{O}_8$

- Standard OPE for inclusive decays
- Very precise theory prediction (at NNLO)

$$\text{BR}(\bar{B} \rightarrow X_s \gamma)_{E_\gamma > E_0} = \text{BR}(\bar{B} \rightarrow X_c e \bar{\nu}) \left| \frac{V_{ts}^* V_{tb}}{V_{cb}} \right| \frac{6\alpha_{em}}{\pi C} [P(E_0) + N(E_0)]$$

↓ ↓  
pert non-pert  
~ 96% ~ 4%

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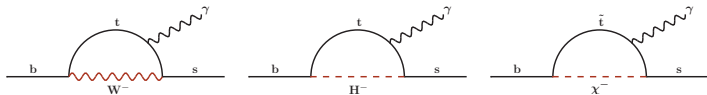
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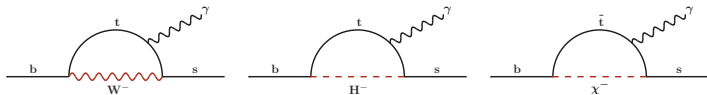
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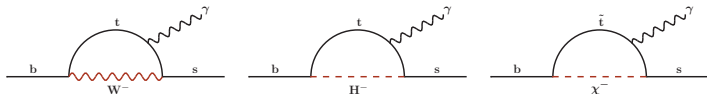
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# Global fits

IF the deviations are from New Physics...

Many observables  $\rightarrow$  **Global fits** of the available data

Relevant Operators:

$$\mathcal{O}_7, \mathcal{O}_8, \mathcal{O}_{9\mu,e}^{(')}, \mathcal{O}_{10\mu,e}^{(')} \quad \text{and} \quad \mathcal{O}_{S-P} \propto (\bar{s}P_R b)(\bar{\mu}P_L \mu)$$

NP manifests itself in the shifts of the individual coefficients with respect to the SM values:

$$C_i(\mu) = C_i^{\text{SM}}(\mu) + \delta C_i$$

- $\rightarrow$  Scans over the values of  $\delta C_i$
- $\rightarrow$  Calculation of flavour observables
- $\rightarrow$  Comparison with experimental results
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## Theoretical uncertainties and correlations

- Monte Carlo analysis
- variation of the “standard” input parameters: masses, scales, CKM, ...
- decay constants taken from the latest lattice results
- $B \rightarrow K^{(*)}$  and  $B_s \rightarrow \phi$  form factors are obtained from the lattice+LCSR combinations, including all the correlations
- Parameterisation of uncertainties from power corrections:

$$A_k \rightarrow A_k \left( 1 + a_k \exp(i\phi_k) + \frac{q^2}{6 \text{ GeV}^2} b_k \exp(i\theta_k) \right)$$

$|a_k|$  between 10 to 60%,  $b_k \sim 2.5a_k$

Low recoil:  $b_k = 0$

⇒ Computation of a (theory + exp) correlation matrix



Global fits of the observables obtained by minimisation of

$$\chi^2 = (\vec{O}^{\text{th}} - \vec{O}^{\text{exp}}) \cdot (\Sigma_{\text{th}} + \Sigma_{\text{exp}})^{-1} \cdot (\vec{O}^{\text{th}} - \vec{O}^{\text{exp}})$$

$(\Sigma_{\text{th}} + \Sigma_{\text{exp}})^{-1}$  is the inverse covariance matrix.

**198 observables** relevant for leptonic and semileptonic decays:

- $\text{BR}(B \rightarrow X_s \gamma)$
- $\text{BR}(B \rightarrow X_d \gamma)$
- $\text{BR}(B \rightarrow K^* \gamma)$
- $\Delta_0(B \rightarrow K^* \gamma)$
- $\text{BR}^{\text{low}}(B \rightarrow X_s \mu^+ \mu^-)$
- $\text{BR}^{\text{high}}(B \rightarrow X_s \mu^+ \mu^-)$
- $\text{BR}^{\text{low}}(B \rightarrow X_s e^+ e^-)$
- $\text{BR}^{\text{high}}(B \rightarrow X_s e^+ e^-)$
- $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$
- $\text{BR}(B_s \rightarrow e^+ e^-)$
- $\text{BR}(B_d \rightarrow \mu^+ \mu^-)$
- $R_K$  in the low  $q^2$  bin
- $R_{K^*}$  in 2 low  $q^2$  bins
- $\text{BR}(B \rightarrow K^0 \mu^+ \mu^-)$
- $B \rightarrow K^+ \mu^+ \mu^-$ :  $BR, F_H$
- $B \rightarrow K^* e^+ e^-$ :  $BR, F_L, A_T^2, A_T^{Re}$
- $B \rightarrow K^{*0} \mu^+ \mu^-$ :  $BR, F_L, A_{FB}, S_3, S_4, S_5, S_7, S_8, S_9$   
in 8 low  $q^2$  and 4 high  $q^2$  bins
- $B^+ \rightarrow K^{*+} \mu^+ \mu^-$ :  $BR, F_L, A_{FB}, S_3, S_4, S_5, S_7, S_8, S_9$   
in 5 low  $q^2$  and 2 high  $q^2$  bins
- $B_s \rightarrow \phi \mu^+ \mu^-$ :  $BR, F_L, S_3, S_4, S_7$   
in 3 low  $q^2$  and 2 high  $q^2$  bins
- $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ :  $BR, A_{FB}^{\ell}, A_{FB}^h, A_{FB}^{\ell h}, F_L$  in the high  $q^2$  bin

Computations performed using **SuperIso** public program

Comparison of one-operator NP fits:

All observables <b>2022</b> ( $\chi_{\text{SM}}^2 = 253.3$ )			
	b.f. value	$\chi_{\text{min}}^2$	Pull <sub>SM</sub>
$\delta C_9$	$-0.95 \pm 0.13$	215.8	$6.1\sigma$
$\delta C_9^e$	$0.82 \pm 0.19$	232.4	$4.6\sigma$
$\delta C_9^\mu$	<b><math>-0.92 \pm 0.11</math></b>	<b>195.2</b>	<b><math>7.6\sigma</math></b>
$\delta C_{10}$	$0.08 \pm 0.16$	253.2	$0.5\sigma$
$\delta C_{10}^e$	$-0.77 \pm 0.18$	230.6	$4.8\sigma$
$\delta C_{10}^\mu$	$0.43 \pm 0.12$	238.9	$3.8\sigma$
$\delta C_{LL}^e$	$0.42 \pm 0.10$	231.4	$4.7\sigma$
$\delta C_{LL}^\mu$	<b><math>-0.43 \pm 0.07</math></b>	<b>213.6</b>	<b><math>6.3\sigma</math></b>

$\delta C_{LL}^\ell$  basis corresponds to  $\delta C_9^\ell = -\delta C_{10}^\ell$ .

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	b.f. value	$\chi_{\text{min}}^2$	Pull <sub>SM</sub>
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$\delta C_9^\mu$	<b><math>-0.92 \pm 0.11</math></b>	<b>195.2</b>	<b><math>7.6\sigma</math></b>
$\delta C_{10}$	$0.08 \pm 0.16$	253.2	$0.5\sigma$
$\delta C_{10}^e$	$-0.77 \pm 0.18$	230.6	$4.8\sigma$
$\delta C_{10}^\mu$	$0.43 \pm 0.12$	238.9	$3.8\sigma$
$\delta C_{LL}^e$	$0.42 \pm 0.10$	231.4	$4.7\sigma$
$\delta C_{LL}^\mu$	<b><math>-0.43 \pm 0.07</math></b>	<b>213.6</b>	<b><math>6.3\sigma</math></b>

All observables <b>2023</b> ( $\chi_{\text{SM}}^2 = 271$ )			
	b.f. value	$\chi_{\text{min}}^2$	Pull <sub>SM</sub>
$\delta C_9$	<b><math>-0.96 \pm 0.13</math></b>	<b>230.7</b>	<b><math>6.3\sigma</math></b>
$\delta C_9^e$	$0.21 \pm 0.16$	269.2	$1.3\sigma$
$\delta C_9^\mu$	$-0.69 \pm 0.12$	240.4	$5.5\sigma$
$\delta C_{10}$	$0.15 \pm 0.15$	270.0	$1.0\sigma$
$\delta C_{10}^e$	$-0.18 \pm 0.14$	269.3	$1.3\sigma$
$\delta C_{10}^\mu$	$0.16 \pm 0.10$	268.3	$1.6\sigma$
$\delta C_{LL}$	$-0.54 \pm 0.12$	249.1	$4.7\sigma$
$\delta C_{LL}^e$	$0.10 \pm 0.08$	269.2	$1.3\sigma$
$\delta C_{LL}^\mu$	$-0.23 \pm 0.06$	257.4	$3.7\sigma$

$\delta C_{LL}^\ell$  basis corresponds to  $\delta C_9^\ell = -\delta C_{10}^\ell$ .

Set: real  $C_7, C_8, C_9, C_{10}, C_S, C_P$  + primed coefficients, 12 degrees of freedom

All observables with $\chi_{\text{SM}}^2 = 271.0$ August 2023 ( $\chi_{\text{min}}^2 = 222.5$ ; $\text{Pull}_{\text{SM}} = 4.7\sigma$ )			
$\delta C_7$ $0.07 \pm 0.03$		$\delta C_8$ $-0.70 \pm 0.50$	
$\delta C'_7$ $-0.01 \pm 0.01$		$\delta C'_8$ $-0.50 \pm 1.20$	
$\delta C_9$ $-1.18 \pm 0.19$	$\delta C'_9$ $0.06 \pm 0.31$	$\delta C_{10}$ $0.23 \pm 0.20$	$\delta C'_{10}$ $-0.05 \pm 0.19$
$C_{Q_1}$ $-0.30 \pm 0.14$	$C'_{Q_1}$ $-0.18 \pm 0.14$	$C_{Q_2}$ $0.01 \pm 0.02$	$C'_{Q_2}$ $-0.03 \pm 0.07$

- Many parameters are weakly constrained at the moment
- The global tension is at the level of  $4.7\sigma$  (assuming 10% uncertainty for the power corrections)

Set: real  $C_7, C_8, C_9, C_{10}, C_S, C_P$  + primed coefficients, 12 degrees of freedom

All observables with $\chi_{SM}^2 = 271.0$ <b>August 2023</b> ( $\chi_{min}^2 = 222.5$ ; $Pull_{SM} = 4.7\sigma$ )			
$\delta C_7$ $0.07 \pm 0.03$		$\delta C_8$ $-0.70 \pm 0.50$	
$\delta C'_7$ $-0.01 \pm 0.01$		$\delta C'_8$ $-0.50 \pm 1.20$	
$\delta C_9$ $-1.18 \pm 0.19$	$\delta C'_9$ $0.06 \pm 0.31$	$\delta C_{10}$ $0.23 \pm 0.20$	$\delta C'_{10}$ $-0.05 \pm 0.19$
$C_{Q_1}$ $-0.30 \pm 0.14$	$C'_{Q_1}$ $-0.18 \pm 0.14$	$C_{Q_2}$ $0.01 \pm 0.02$	$C'_{Q_2}$ $-0.03 \pm 0.07$

- Many parameters are weakly constrained at the moment
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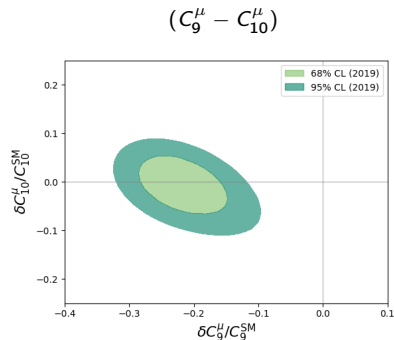
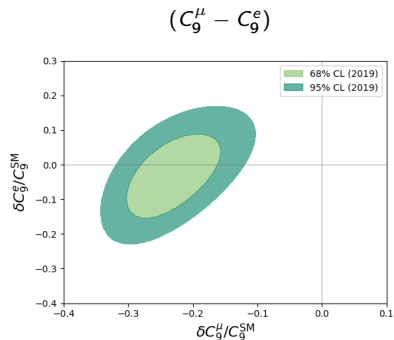
Pull<sub>SM</sub> of 1, 2, 4, 6 and 12 dimensional fit:

All observables ; <b>August 2023</b>				
Set of WC	param.	$\chi^2_{\min}$	Pull <sub>SM</sub>	Improvement
SM	0	271.0	—	—
$C_9$	1	230.7	$6.3\sigma$	$6.3\sigma$
$C_9, C_{10}$	2	230.3	$6.0\sigma$	$0.6\sigma$
$C_7, C_8, C_9, C_{10}$	4	225.3	$5.9\sigma$	$1.7\sigma$
$C_7, C_8, C_9, C_{10}, C_{Q1}, C_{Q2}$	6	224.7	$5.6\sigma$	$0.3\sigma$
All WC (incl. primed)	12	222.5	$4.7\sigma$	$0.1\sigma$

The last row also includes the chirality-flipped counterparts of the Wilson coefficients.

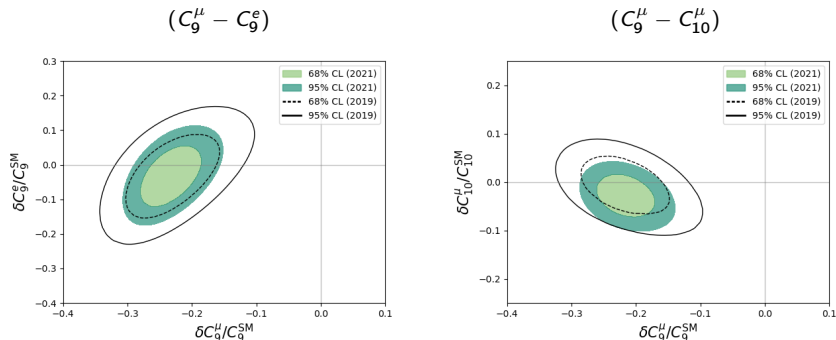
In the last column the significance of improvement of the fit compared to the scenario of the previous row is given.

2D fits to all available data:



2019: Run I results

2D fits to all available data:

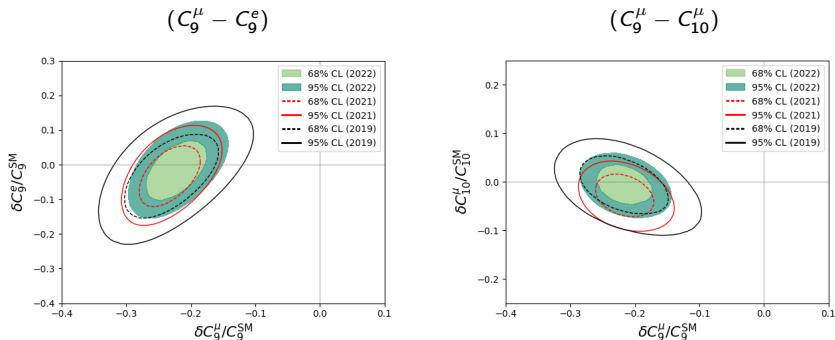


**2019:** Run I results

**2021:** (partial) Run II updates, mainly for  $B \rightarrow K^* \mu^+ \mu^-$ ,  $R_K$  and  $B_s \rightarrow \mu^+ \mu^-$  (LHCb)



2D fits to all available data:

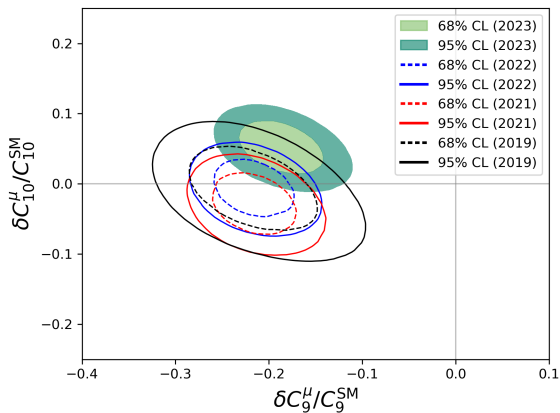


**2019:** Run I results

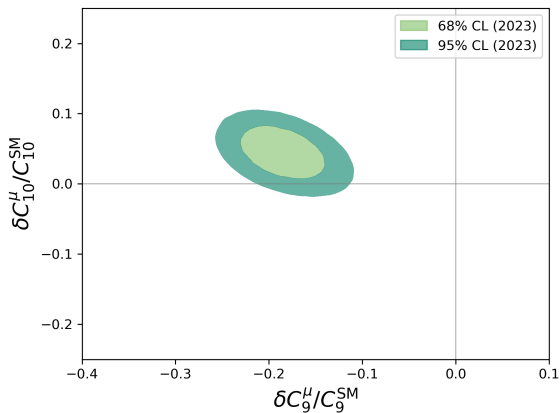
**2021:** (partial) Run II updates, mainly for  $B \rightarrow K^* \mu^+ \mu^-$ ,  $R_K$  and  $B_s \rightarrow \mu^+ \mu^-$  (LHCb)

**2022:** (partial) Run II updates, mainly for  $B_s \rightarrow \mu^+ \mu^-$  (CMS),  $R_{K^{*+}}$ ,  $R_{K_S^0}$  and  $B_s \rightarrow \phi \mu^+ \mu^-$

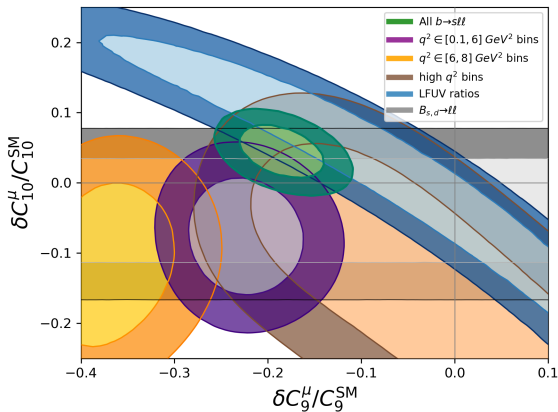
## 2023 (pre-CMS)



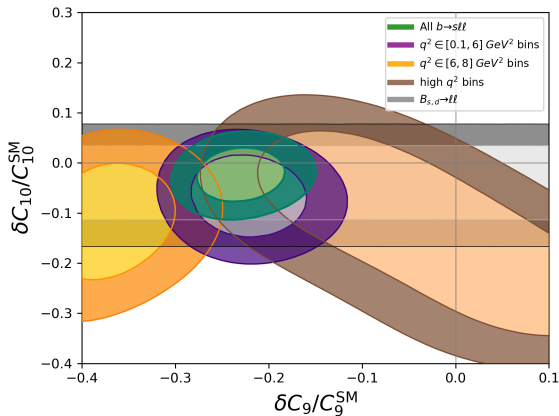
## Current situation (all observables, including CMS Aug. 2023)



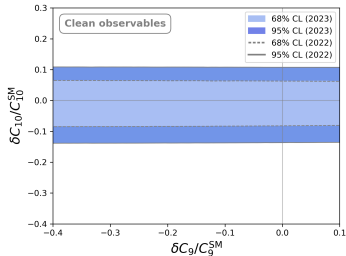
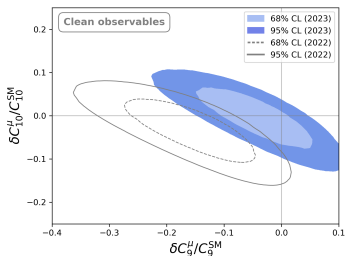
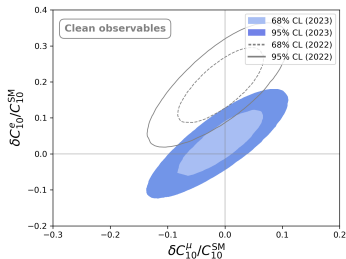
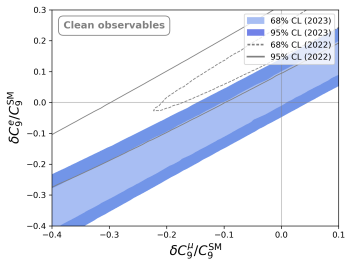
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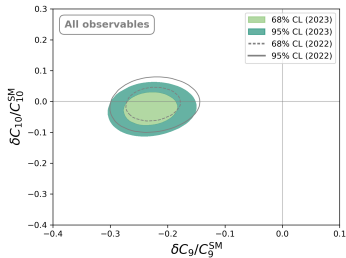
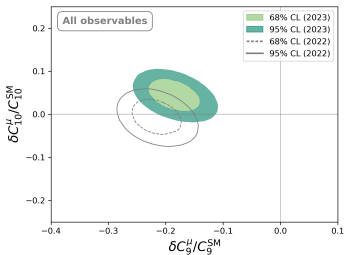
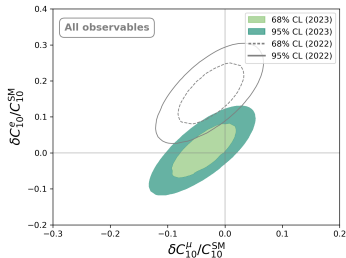
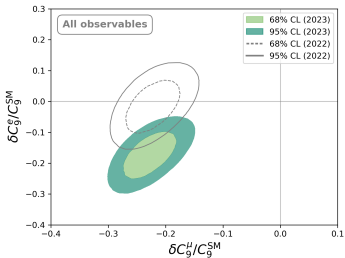
## Fit to universal Wilson coefficients



## Clean observables only



## All observables



- Reduction of the significance of the most preferred NP scenarios
- $C_9$  continues to be the Wilson coefficient which includes most of the NP effects
- LFUV components are mostly suppressed
- High significances for scenarios with universal NP in  $C_9$
- Some tensions in the inner structure of the fit:
  - LFU ratios are SM-like
  - $B \rightarrow K^{(*)} \mu\mu$  observables continue to deviate with high significance

### New Physics or Not New Physics?

- ▶ More work is needed to assess the hadronic uncertainties
- ▶ The measurement of the electron modes will be very important
- ▶ Cross-check with other ratios, and also inclusive modes will be very useful

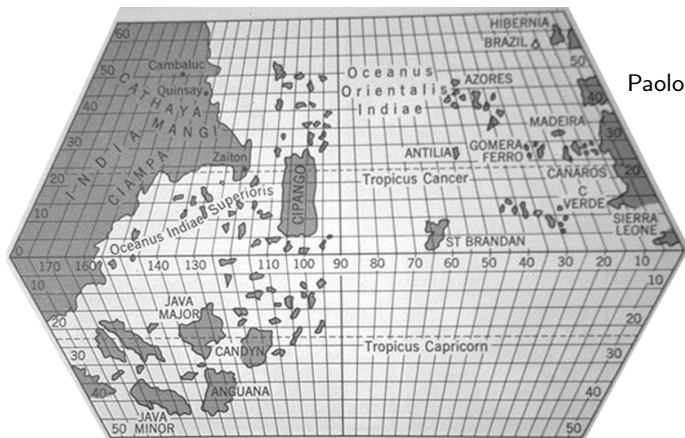


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We may be in such a situation:



Paolo Toscanelli  
1474

Columbus had Toscanelli's map.  
It was terribly wrong, but served the purpose!