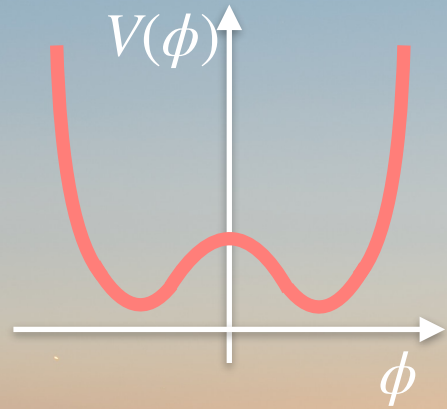


Hunting for di-Higgs in hadronic final states

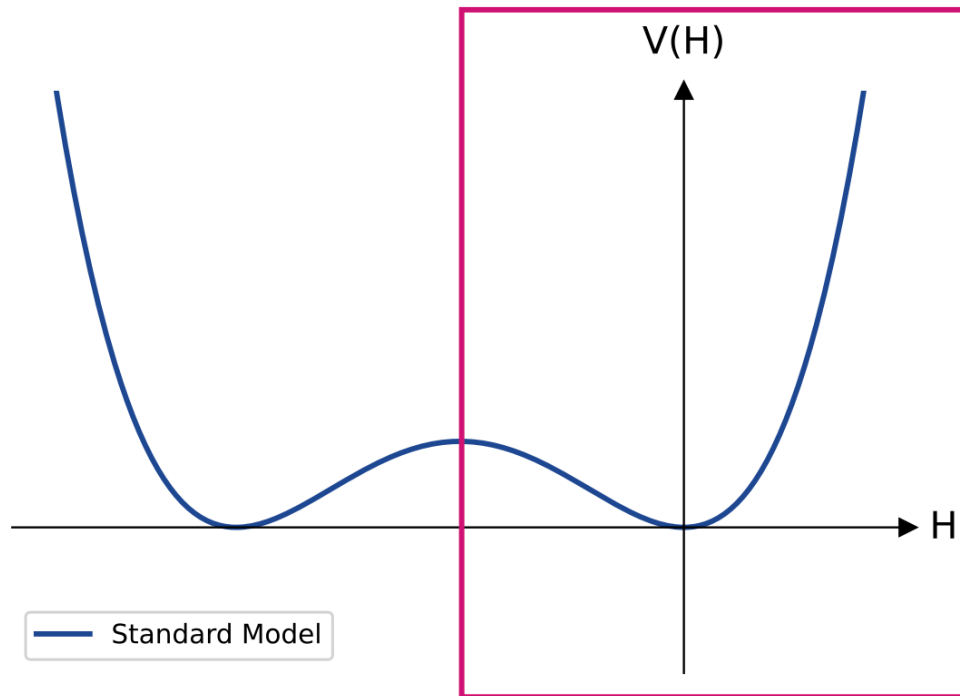


Nicole Hartman
nicole.hartman@tum.de

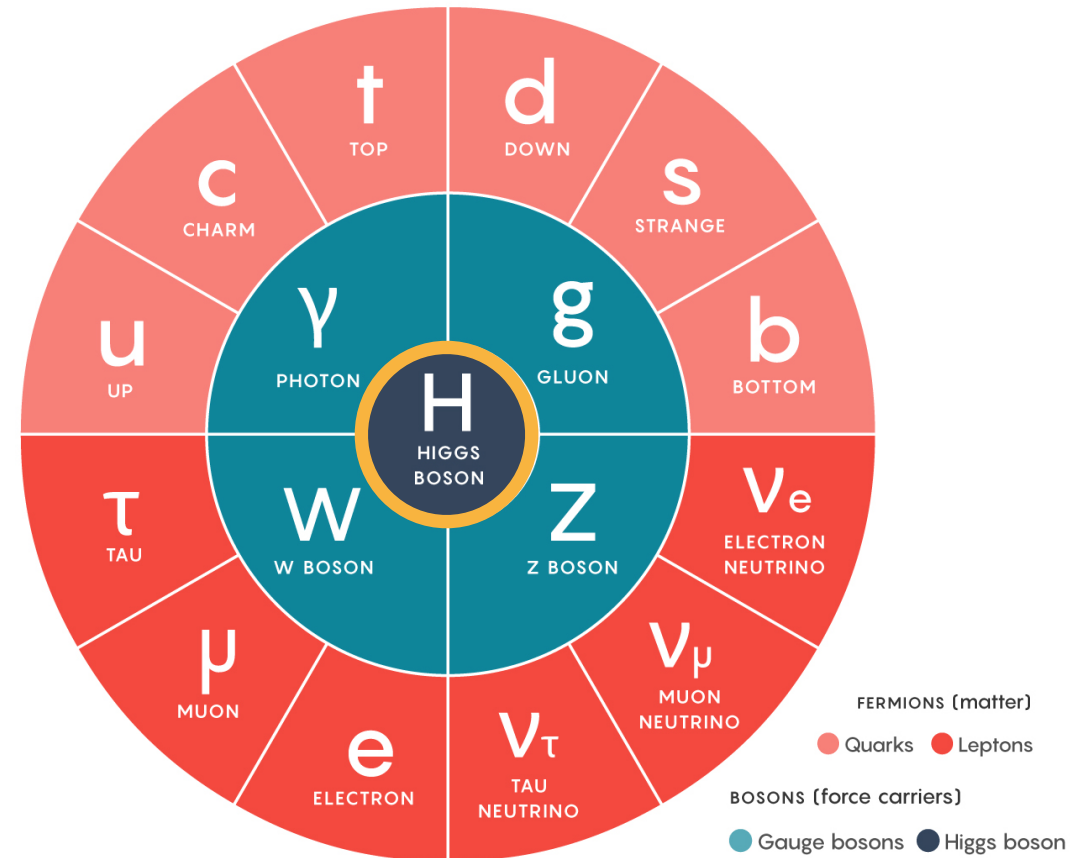
Workshop on Machine Learning and High Energy Physics
Austrian Academy of Sciences
13 Dec 2023

Motivation

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + i\bar{\psi}\gamma_{\mu}D^{\mu}\psi + |D_{\mu}\phi|^2 - \boxed{V(\phi)} + (y_{ij}\bar{\psi}_i\psi_j + \text{h.c.})$$

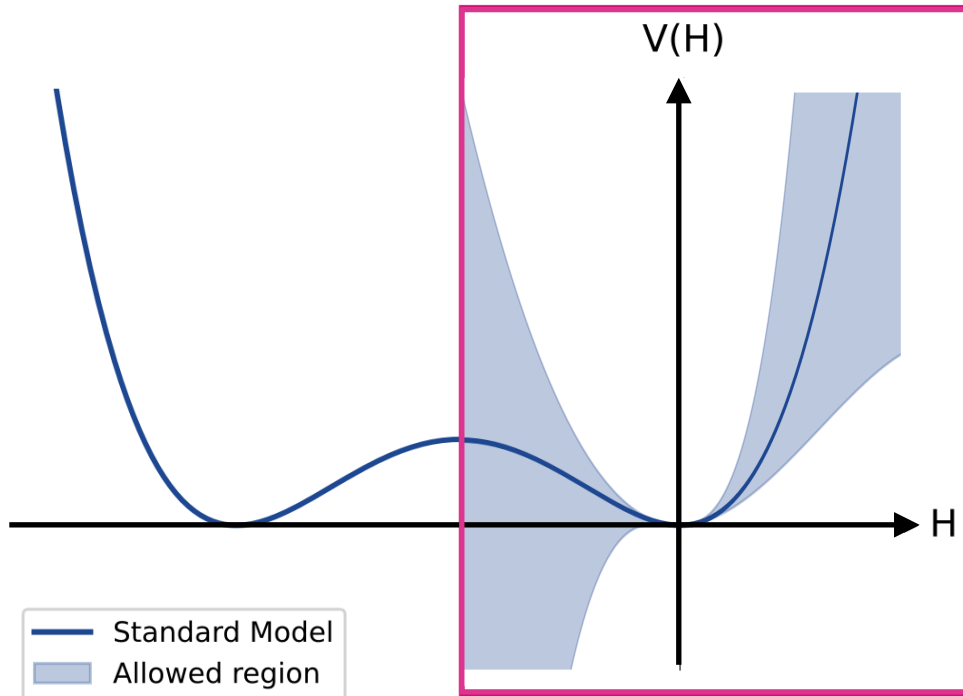


Graphic from B. Moser

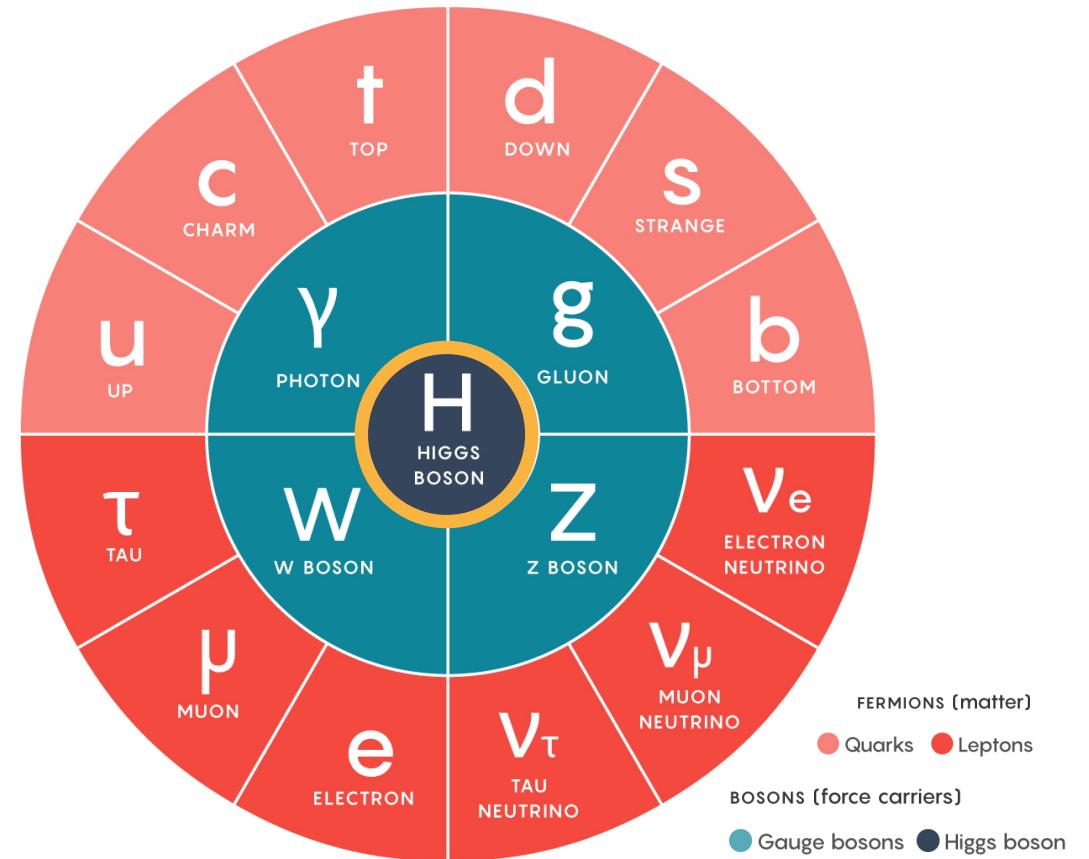


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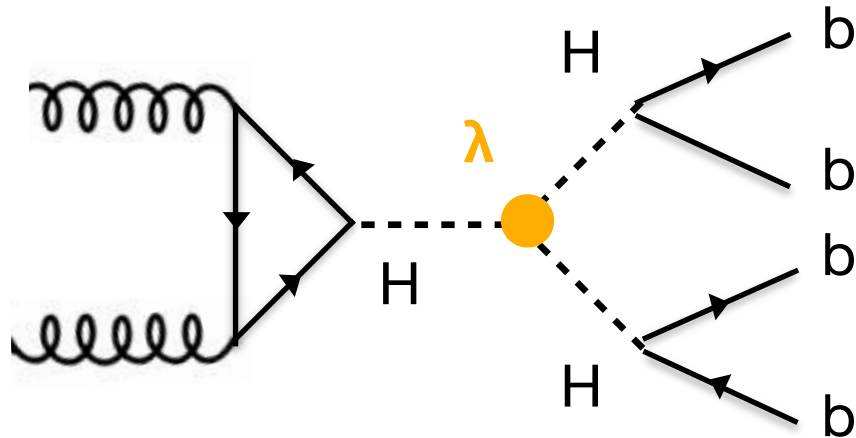
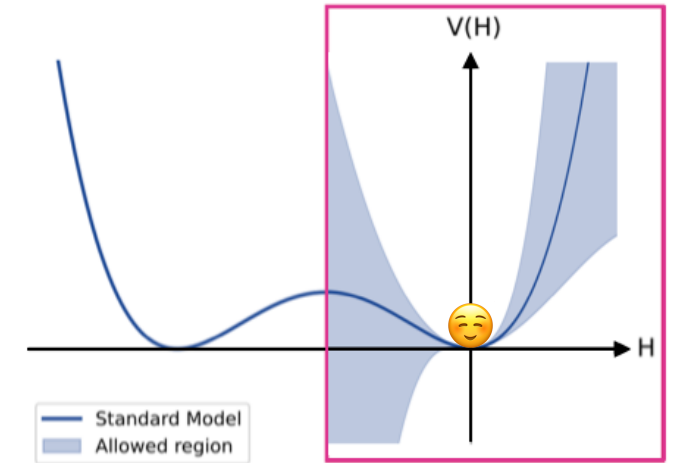


Graphic from B. Moser



Where to look

$$V(\phi) = \mu^2 h(x)^2 + \lambda v h(x)^3 + \frac{1}{4} \lambda h(x)^4$$



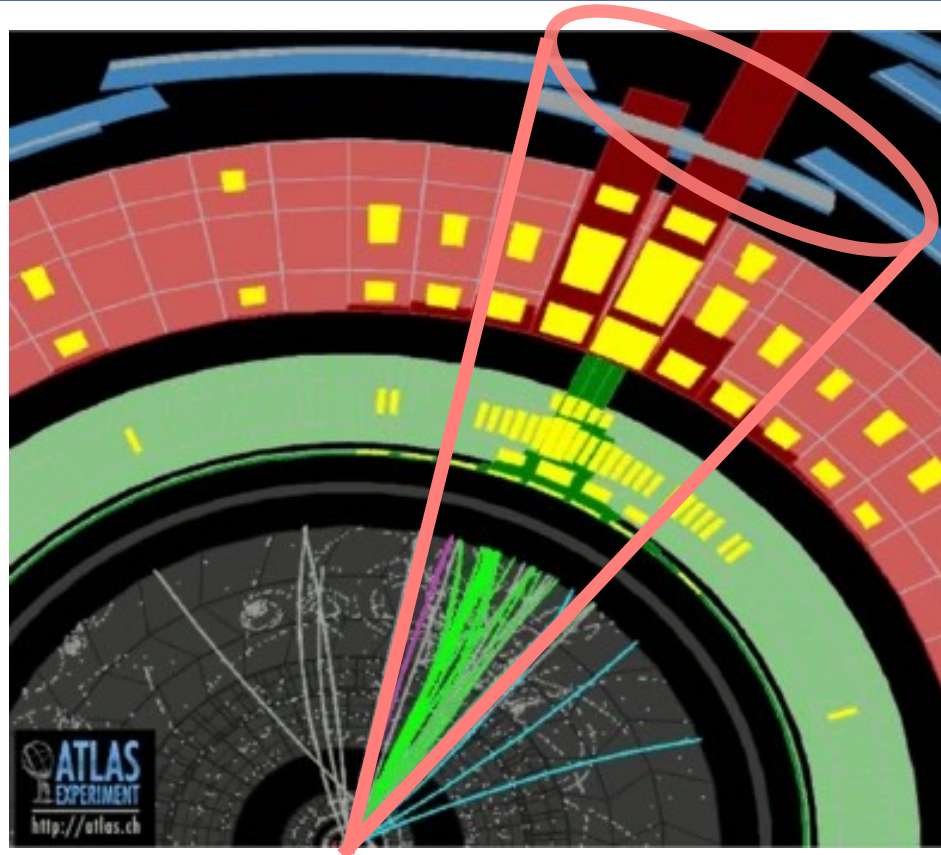
Focus for today!

Higgs 1 decay

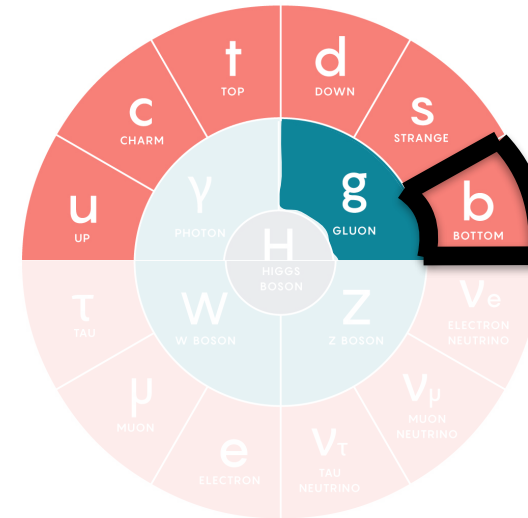
	bb	WW	$\tau\tau$	ZZ	$\gamma\gamma$
bb	34%				
WW	25%	4.6%			
$\tau\tau$	7.3%	2.7%	0.39%		
ZZ	3.1%	1.1%	0.33%	0.069%	
$\gamma\gamma$	0.26%	0.10%	0.028%	0.012%	0.0005%

Other main HH channels

Jets

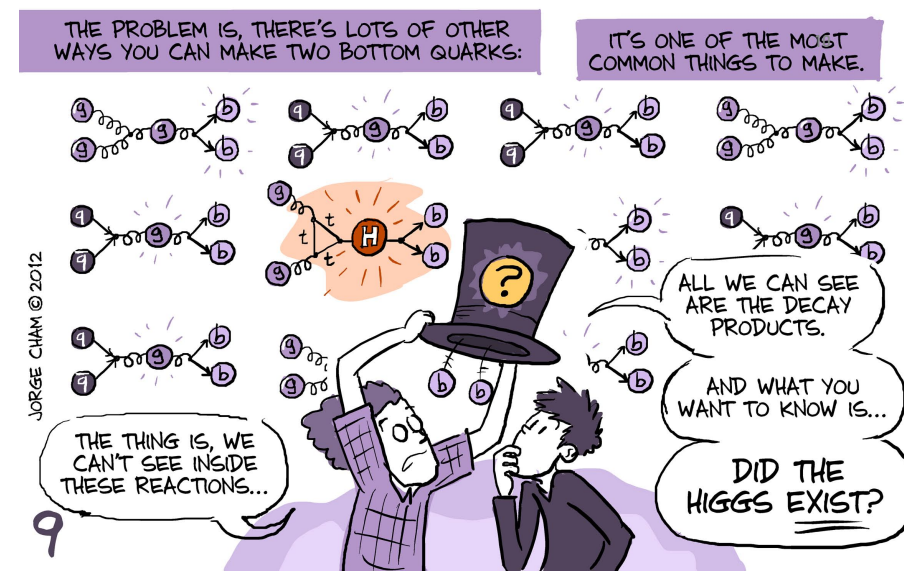


In the detector, quarks create **jets**



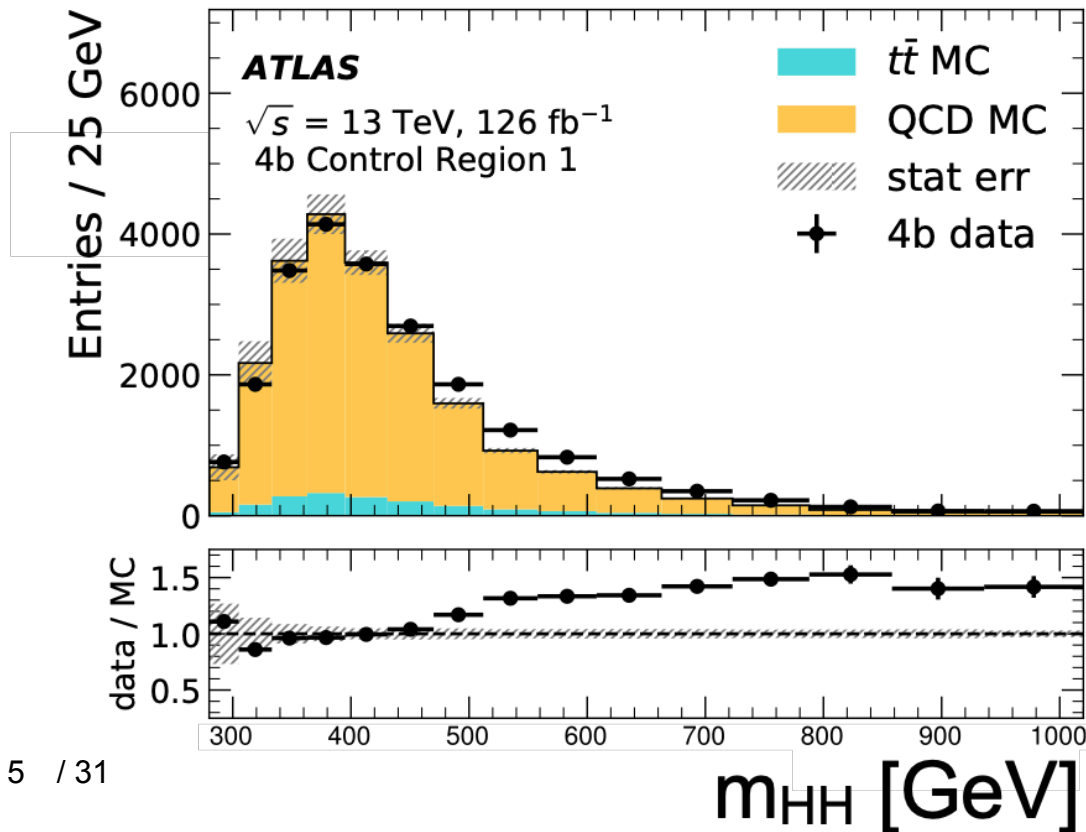
Our favorite jets

Also lots of ways to get **b-jets** other than Higgs bosons!

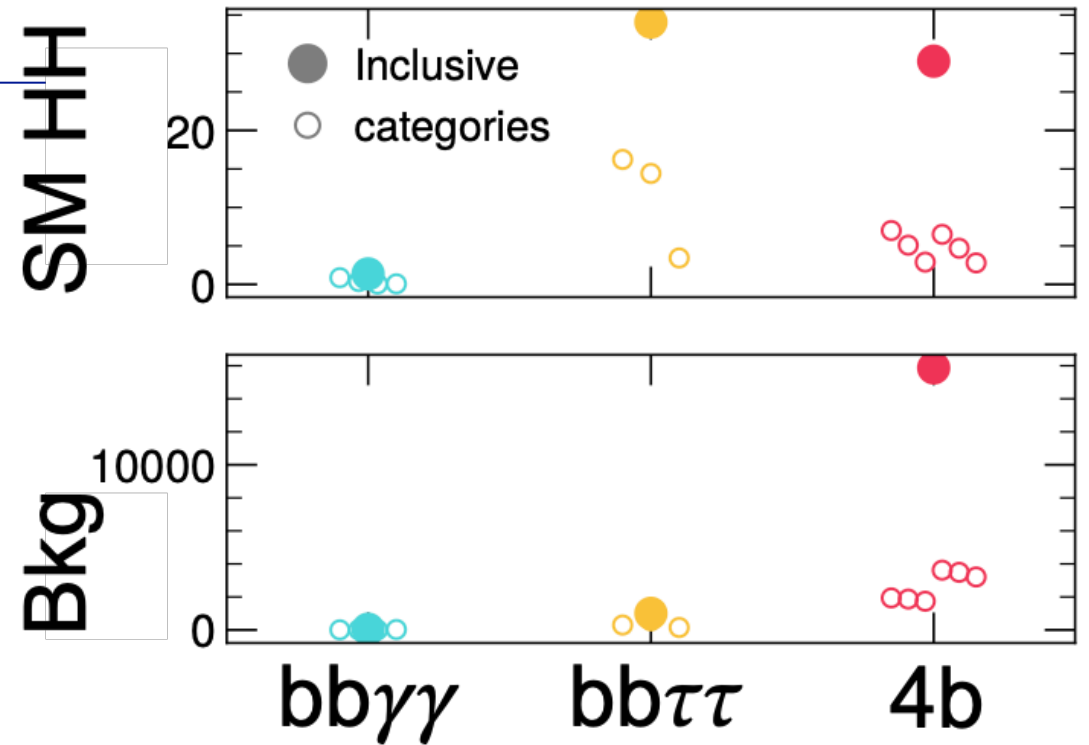


Challenges

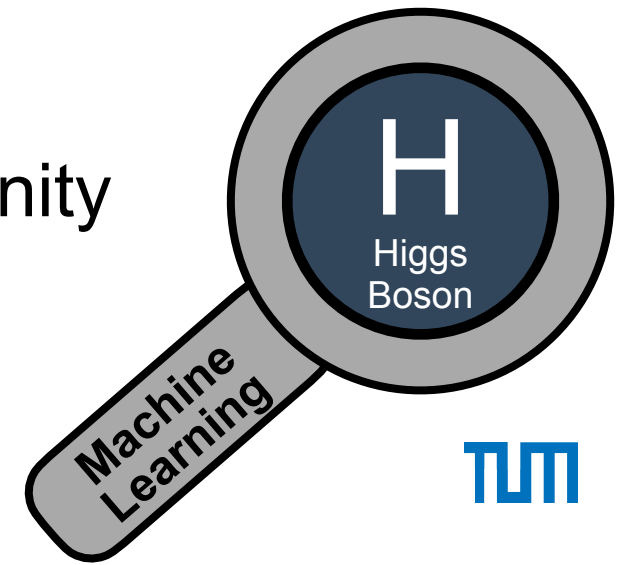
Analyses with jets have large backgrounds \rightarrow
which are challenging to simulate from first principles \downarrow



From ATLAS [bbγγ](#), [bbττ](#), and [4b](#) analyses.

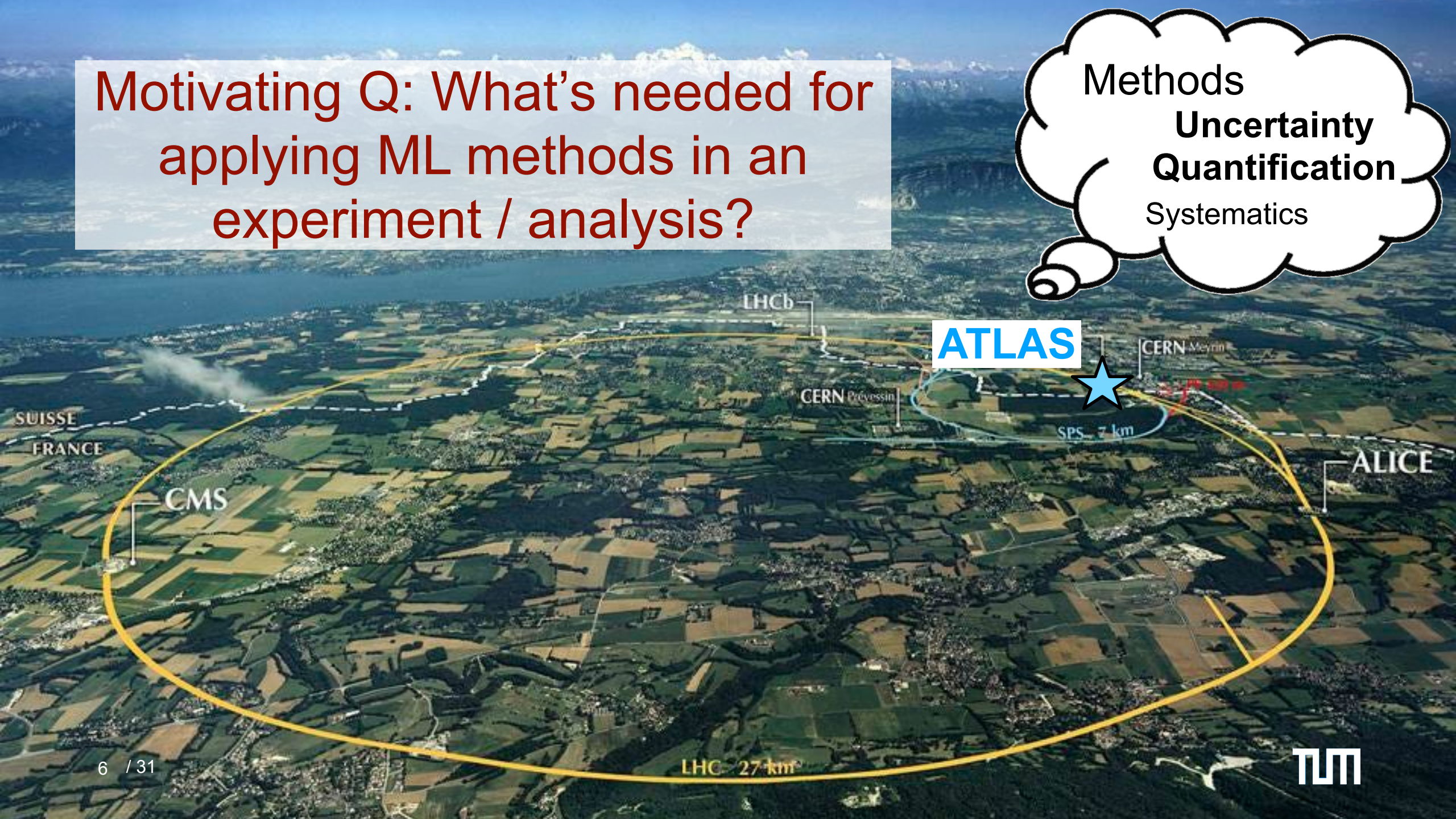


Key opportunity for ML



Motivating Q: What's needed for applying ML methods in an experiment / analysis?

Methods
Uncertainty
Quantification
Systematics

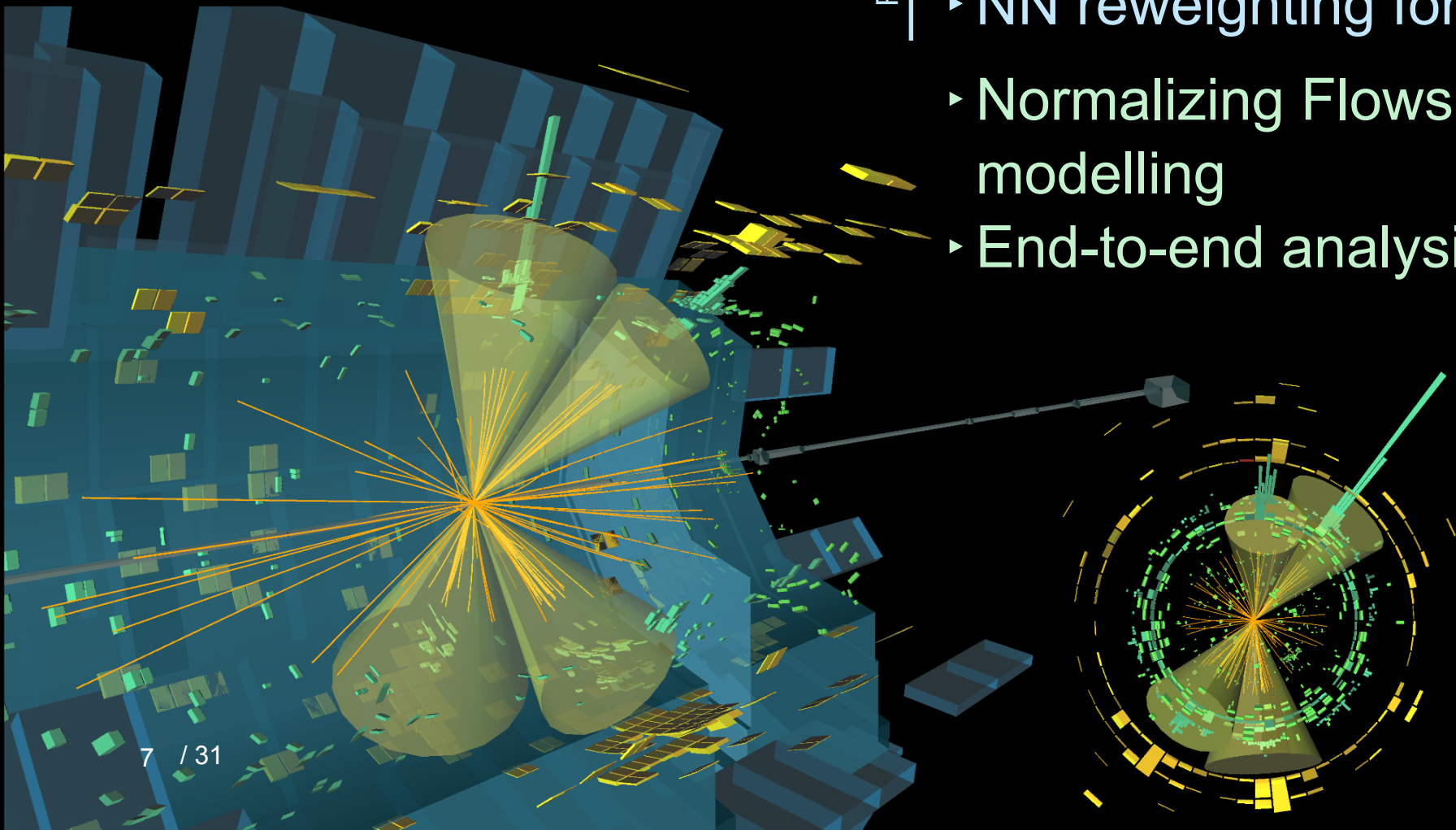


HH \rightarrow 4b analysis

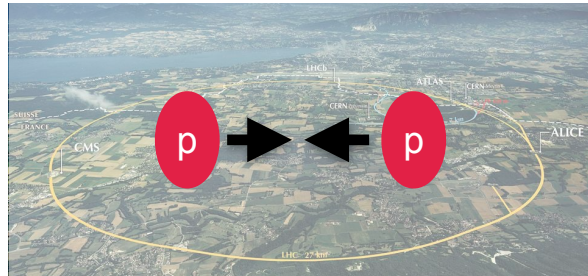
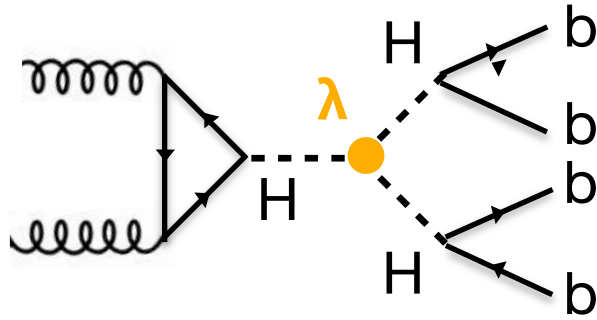
Run 2

- Birds-eye view of analysis
- NN reweighting for background modelling
- Normalizing Flows for background modelling
- End-to-end analysis

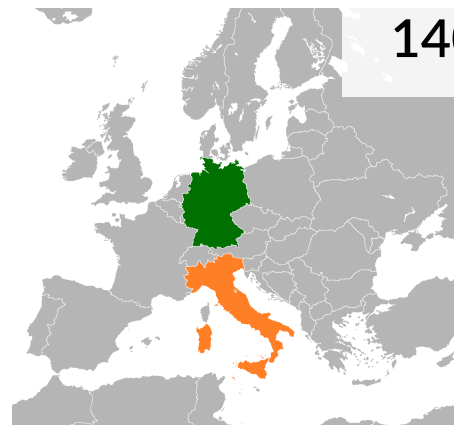
Run 3



The scale of the problem



$$\frac{1 \text{ signal event / (3 hour)}}{1 \text{ billion collisions / second}} = 10^{-13} \quad \frac{\text{signal}}{\text{background}}$$

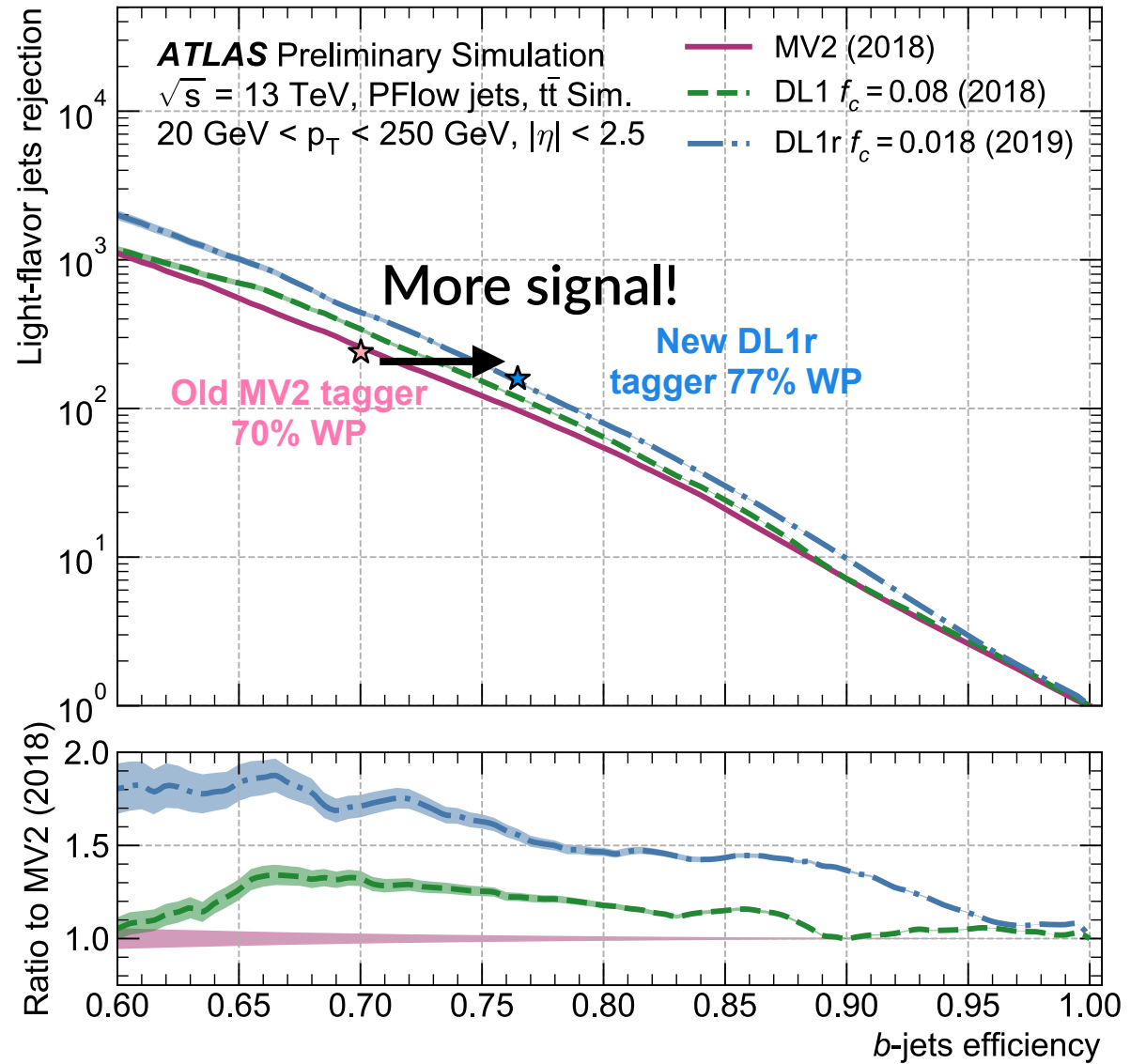
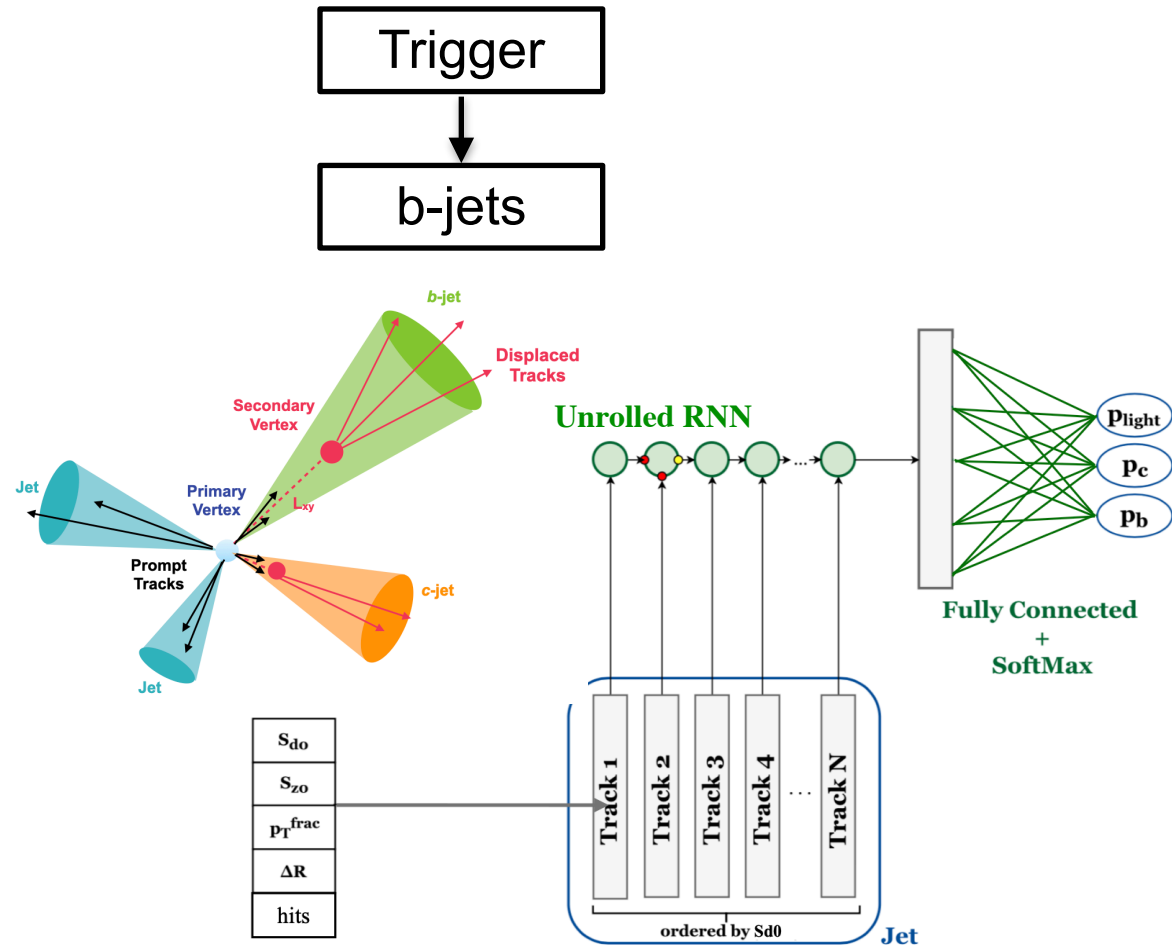


140 million people in **Germany** + **Italy**

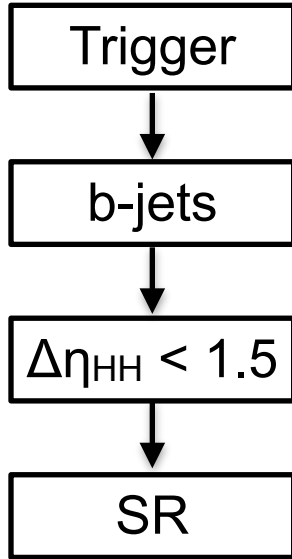
100,000 hairs / person



Analysis overview

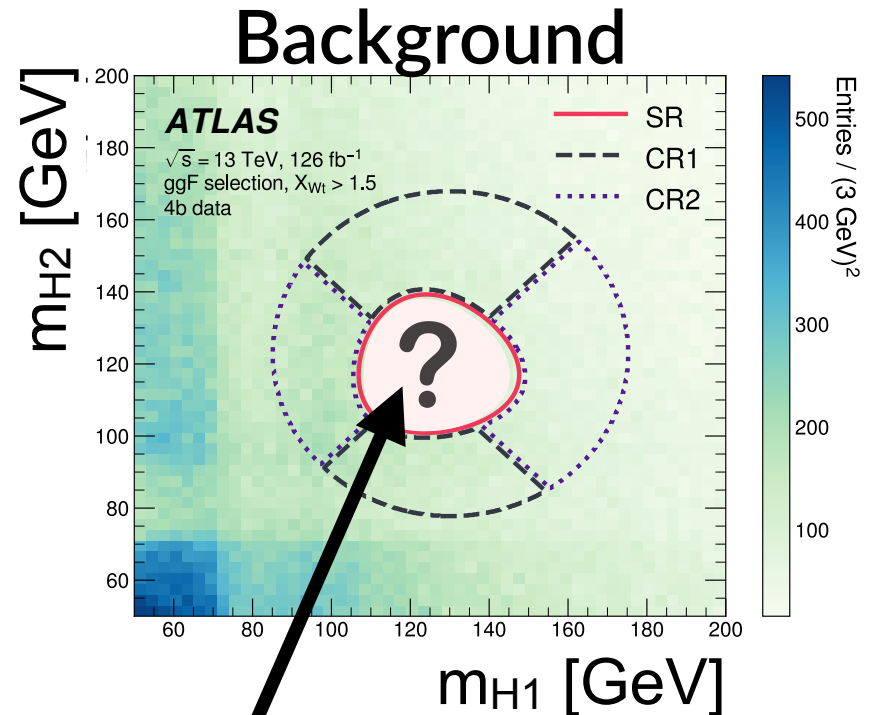
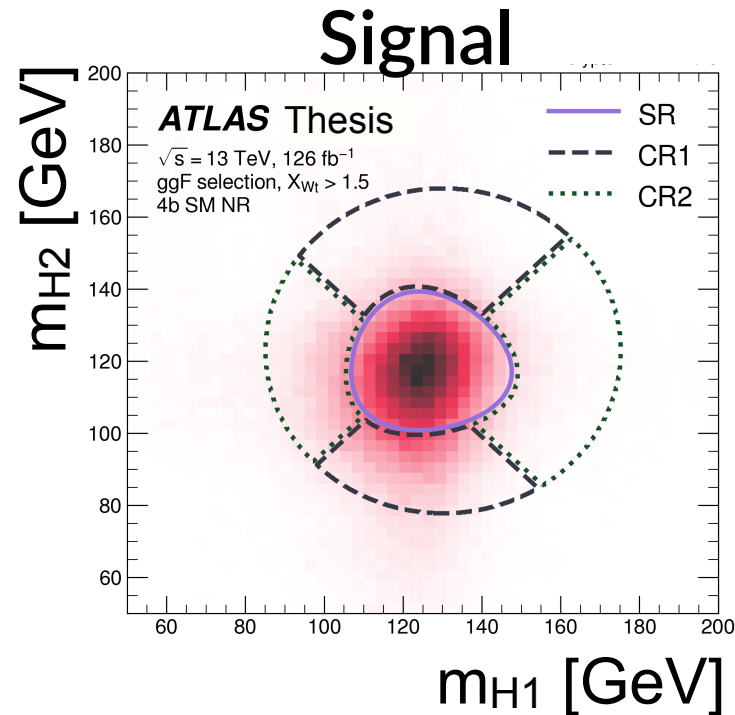


Analysis overview



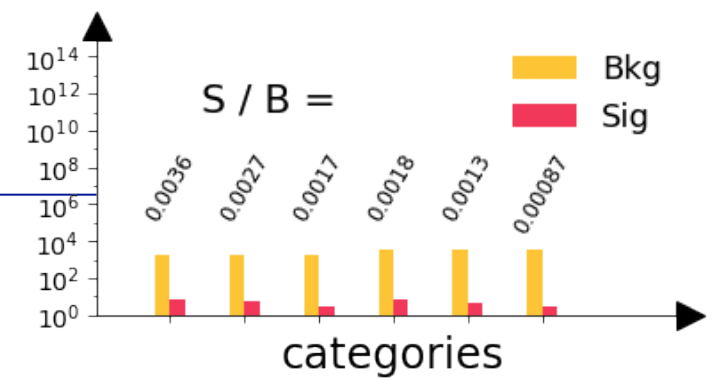
$$X_{HH} = \sqrt{\left(\frac{m_{H1} - 124 \text{ GeV}}{0.1m_{H1}}\right)^2 + \left(\frac{m_{H2} - 117 \text{ GeV}}{0.1m_{H2}}\right)^2}$$

SR: $X_{HH} < 1.6$



How to predict the background here?

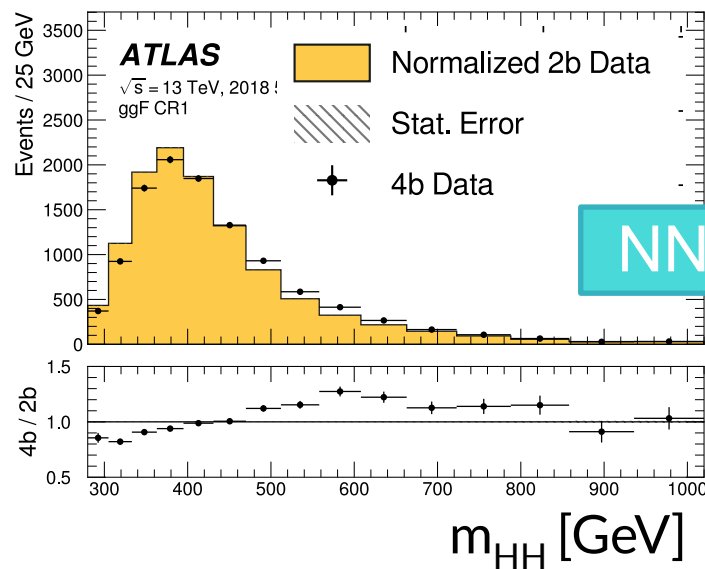
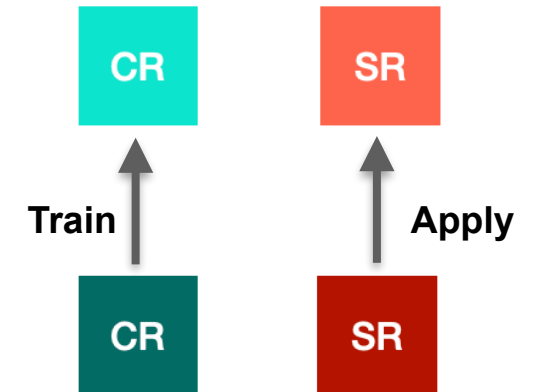
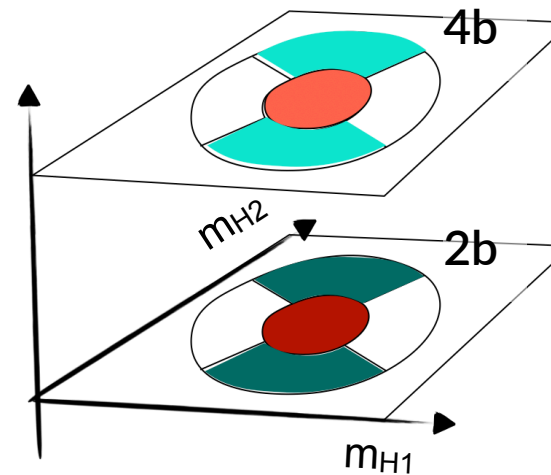
Want to fit a shape with categories... need a multidimensional description of the data.



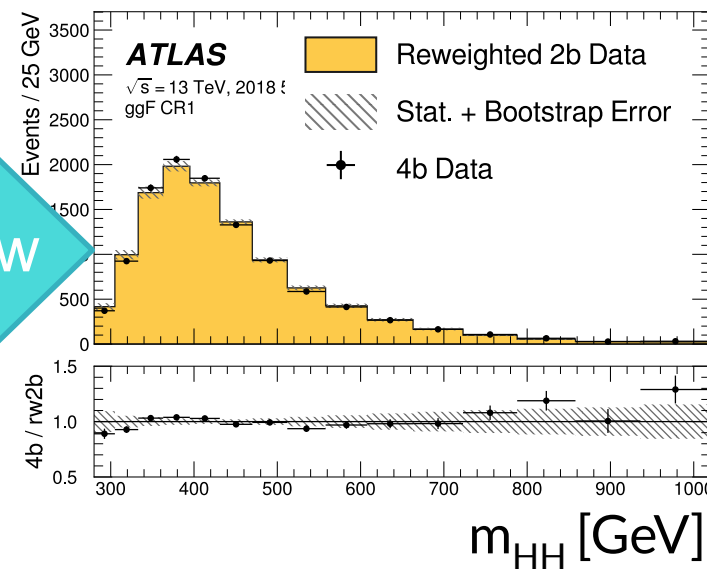
Reweighting for background estimation

Use classifiers to learn likelihood ratios, e.g, $p_{4b}(x)/p_{2b}(x)$

$$p_{4b} = w(x) \cdot p_{2b}(x), x \in \mathbb{R}^d$$



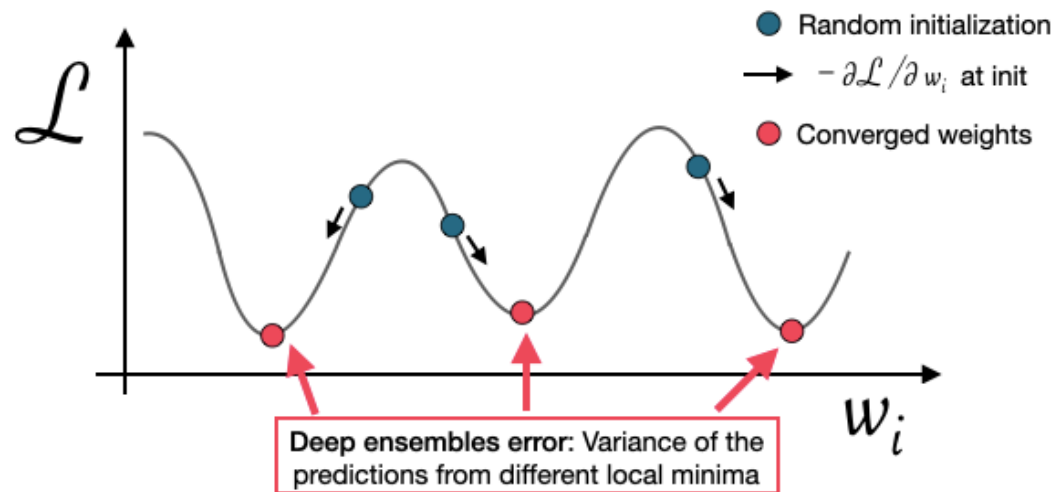
NN rw



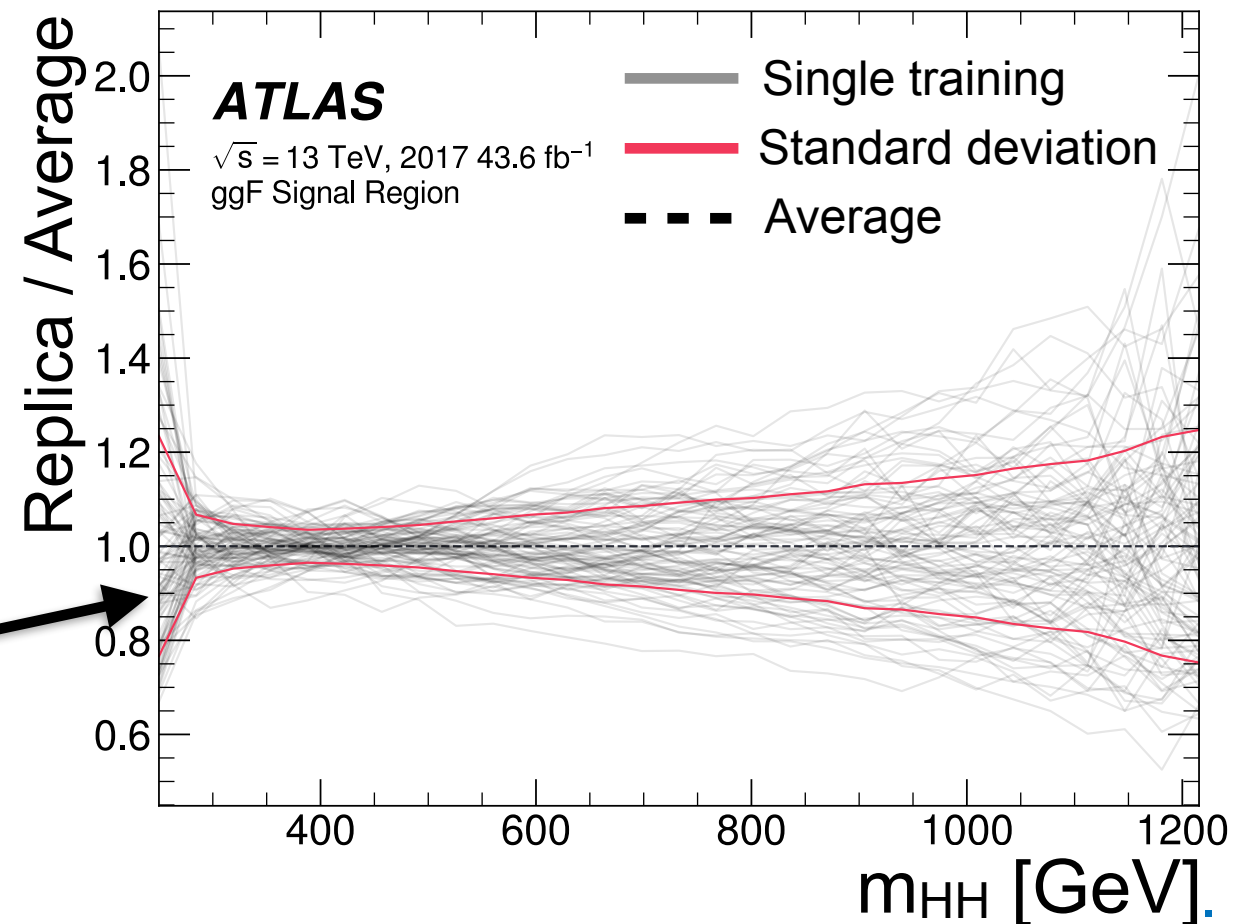
🥳 It works!

Note m_{HH} was not used in the set of reweighting features x .

Uncertainty: NN training

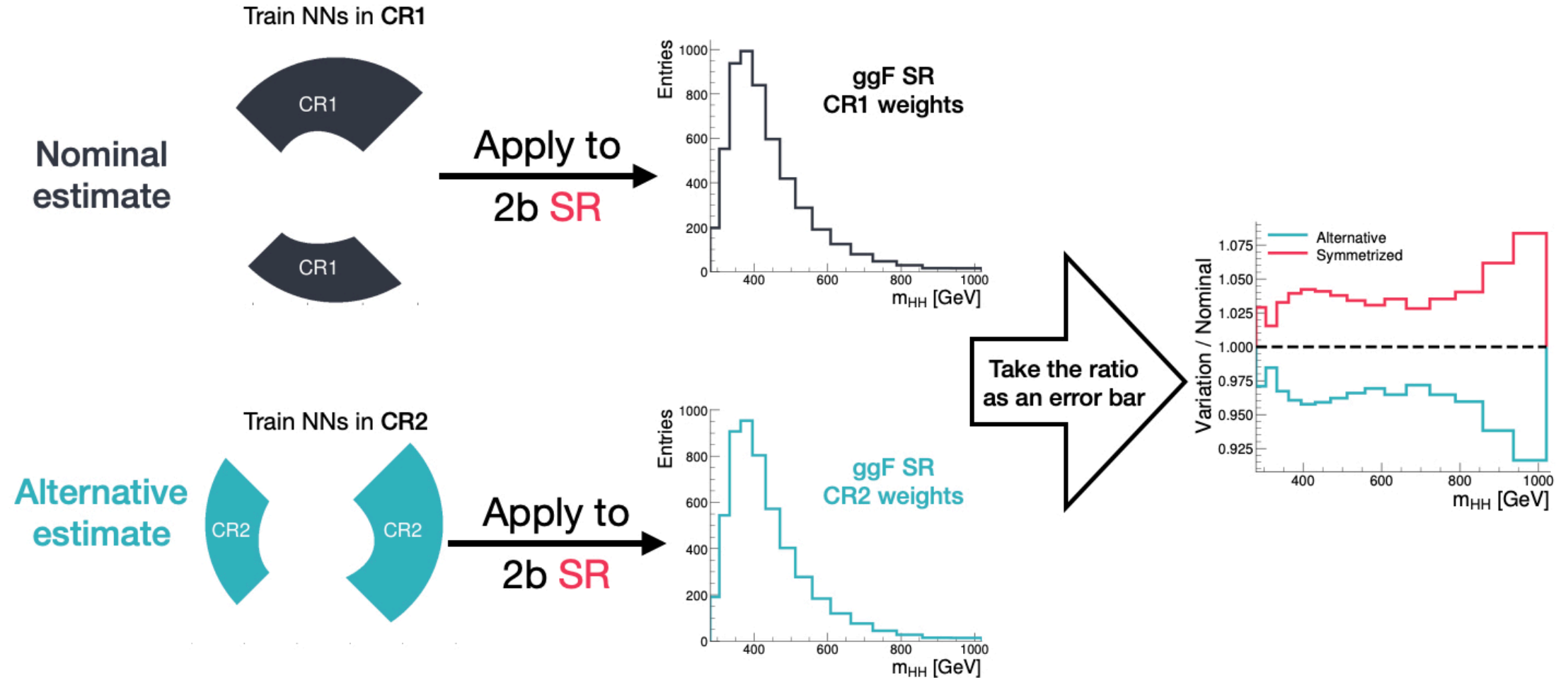


Retraining the NN 100x captures the uncertainty from multiple local minima



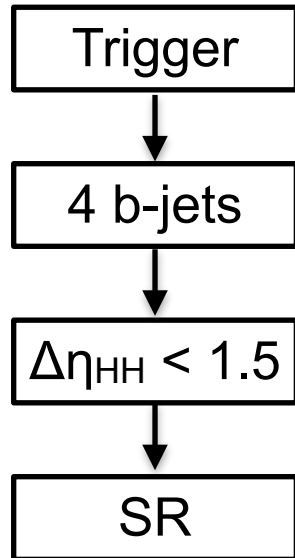
Use the **variation of trainings** as a nuisance parameter

Uncertainty: choice of control region



Background validation

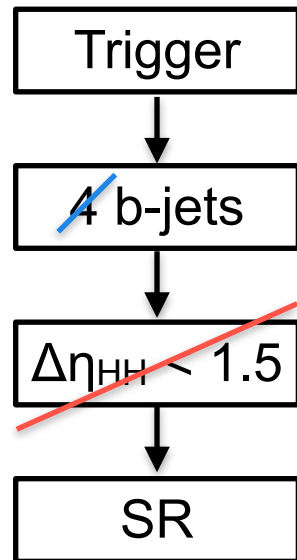
Q: Have we accounted for all uncertainties?



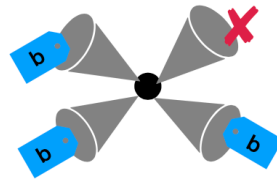
Background validation

Q: Have we accounted for all uncertainties?

→ Invert *every cut!!*

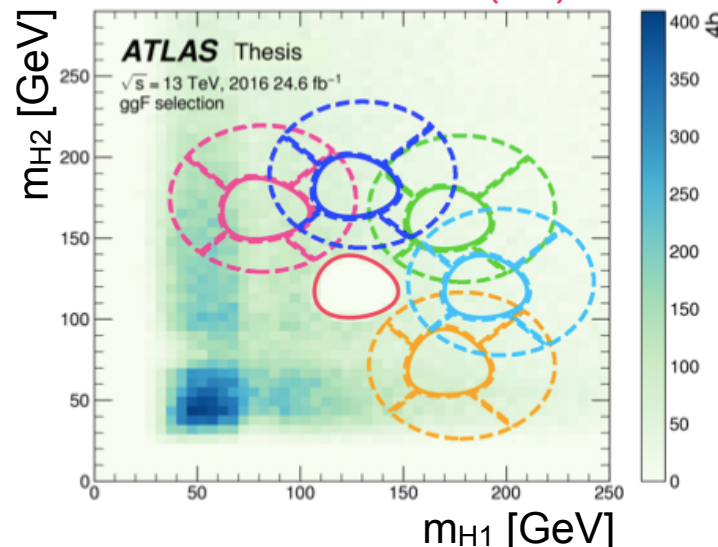


3 b-jets



$\Delta\eta_{HH} > 1.5$

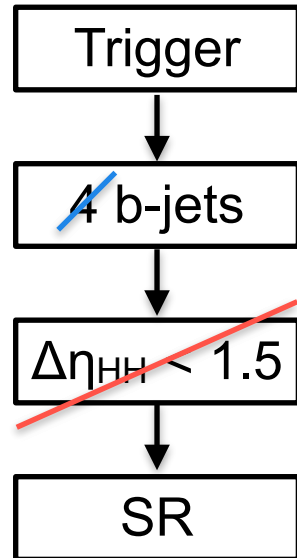
Shift the center (5x)



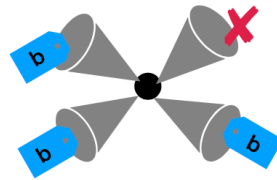
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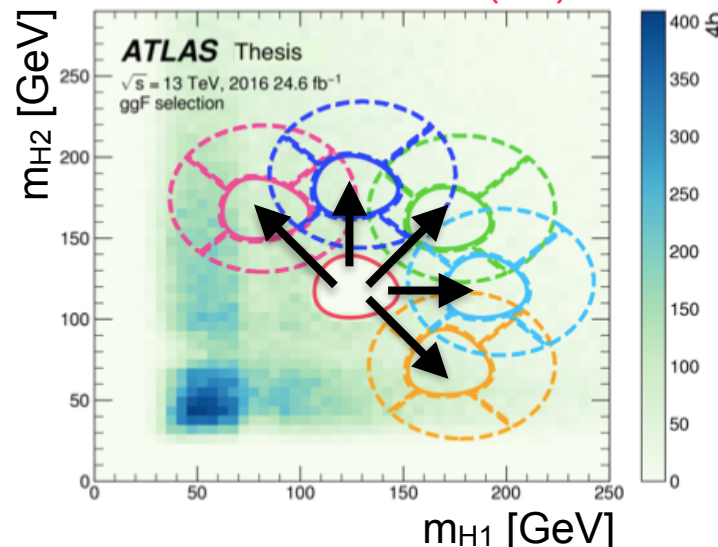


3 b-jets



$\Delta\eta_{HH} > 1.5$

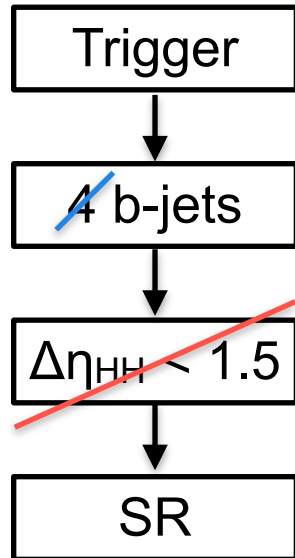
Shift the center (5x)



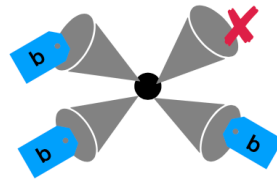
Background validation

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→ Invert *every cut!!*

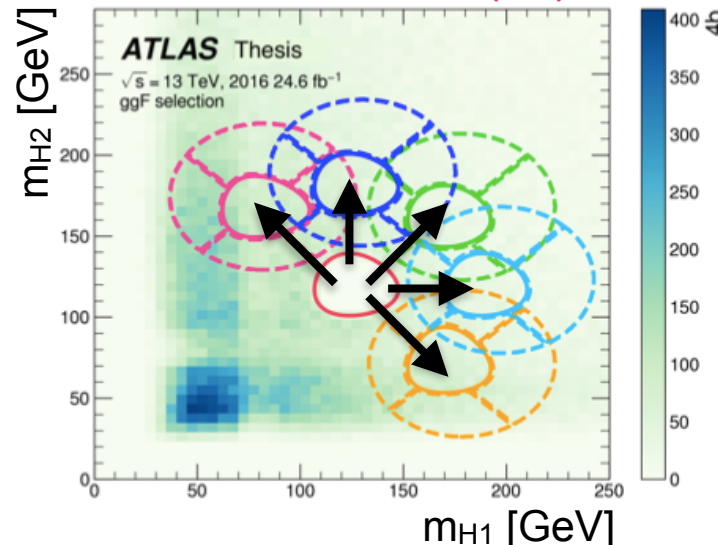


3 b-jets



$\Delta\eta_{HH} > 1.5$

Shift the center (5x)

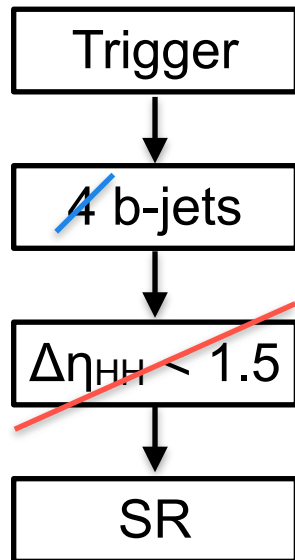


✓ Modeled by existing uncertainties

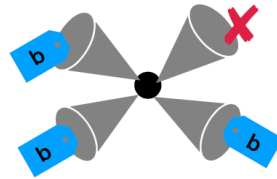
Background validation

Q: Have we accounted for all uncertainties?

→ Invert *every cut!!*



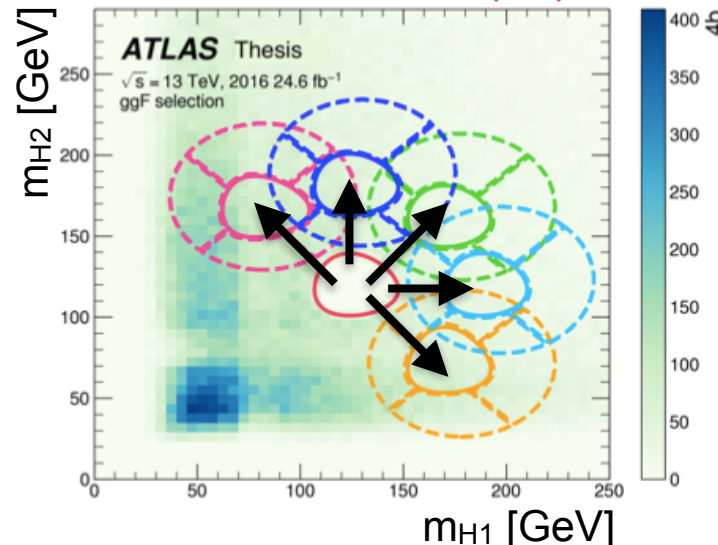
3 b-jets



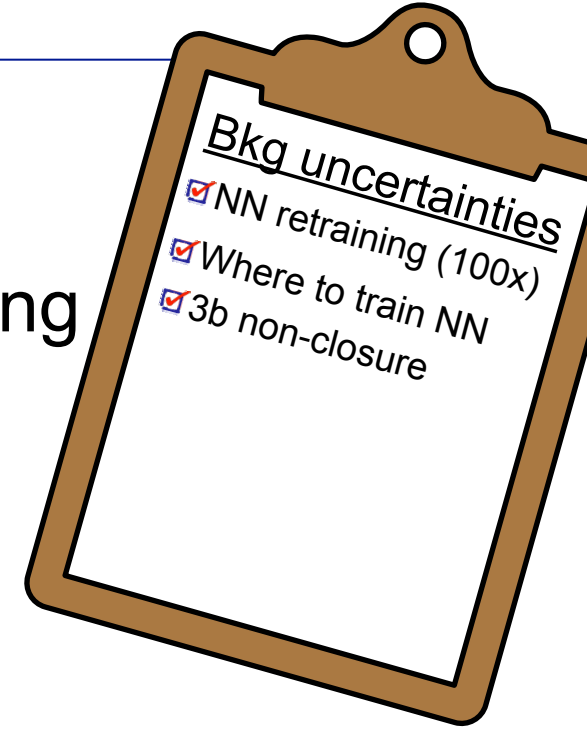
✗ Some mismodeling
→ Add uncertainty

$\Delta\eta_{HH} > 1.5$

Shift the center (5x)

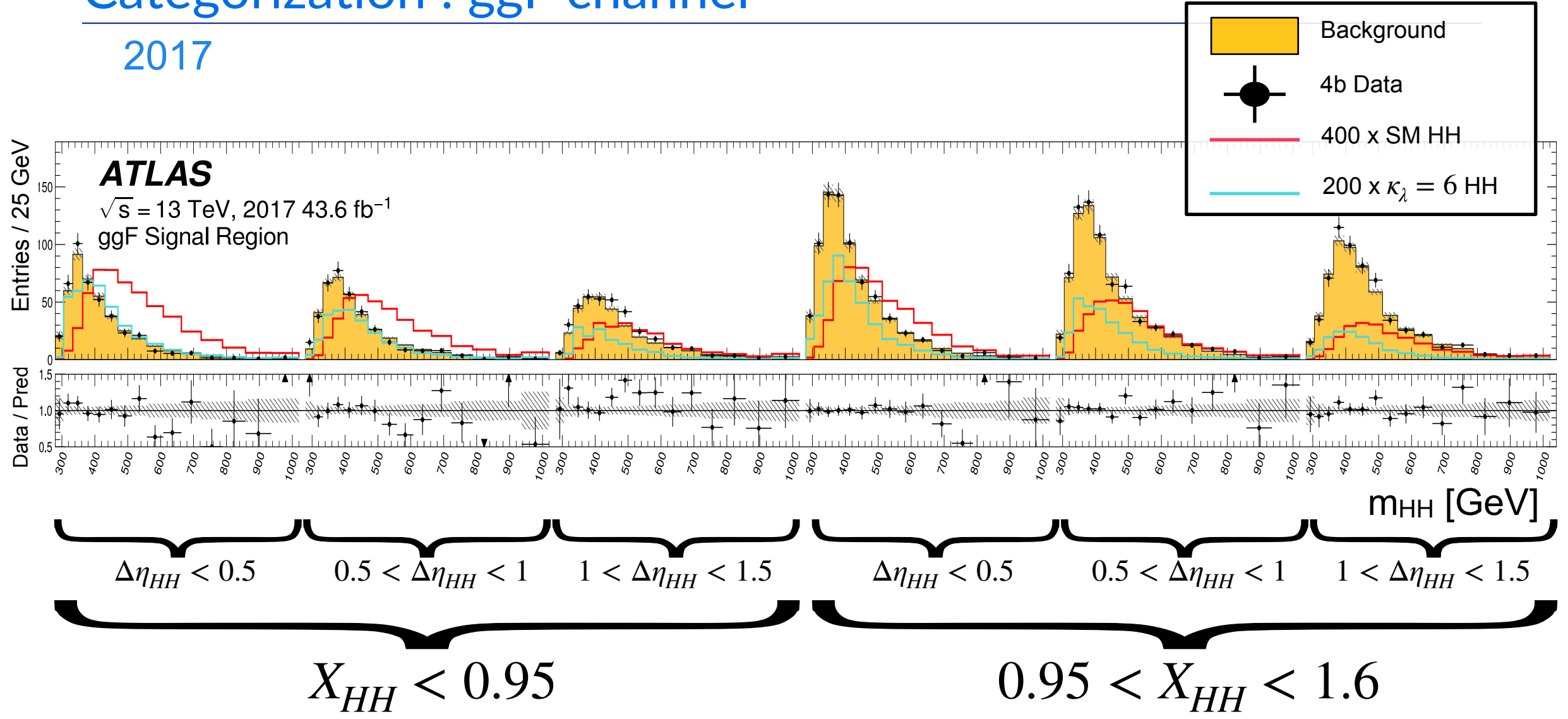


✓ Modeled by existing uncertainties



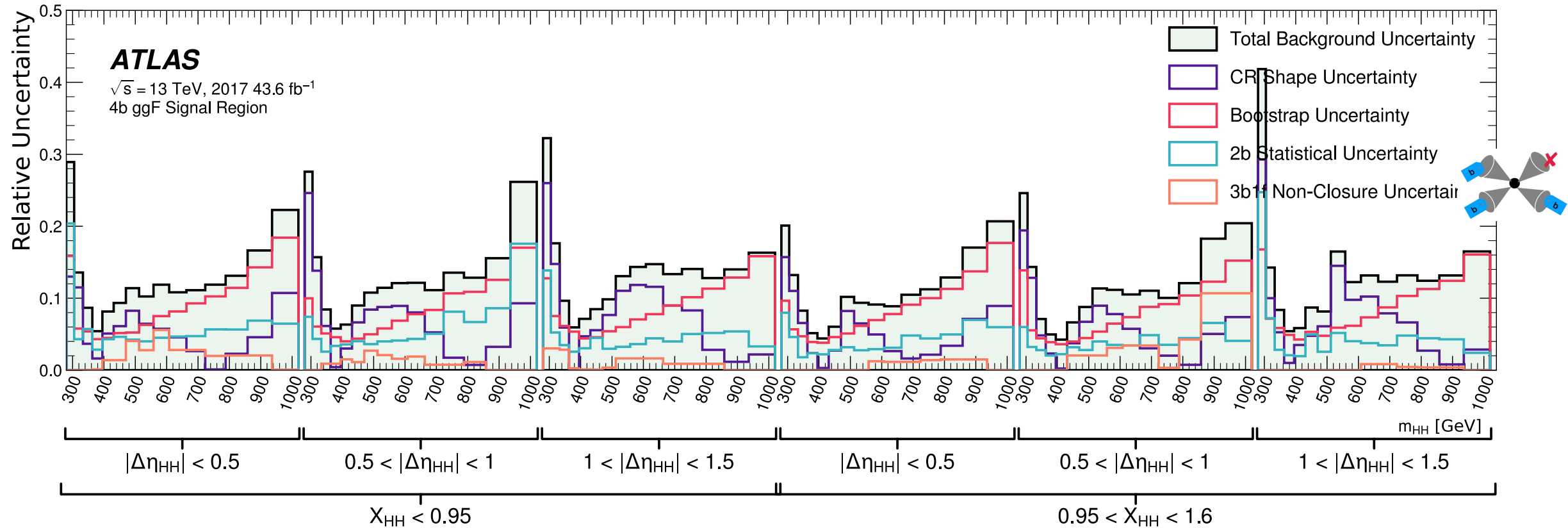
Categorization : ggF channel

2017

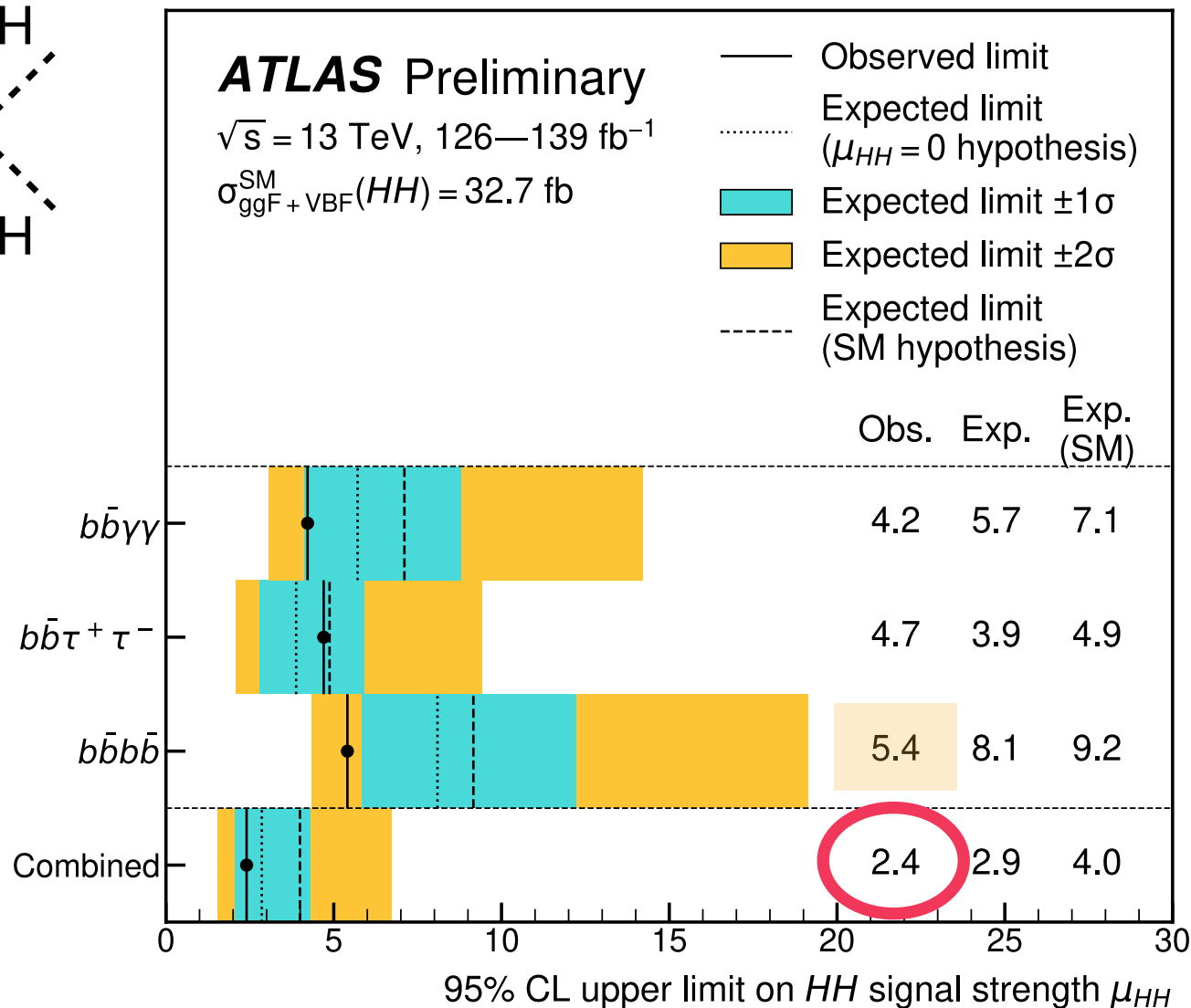
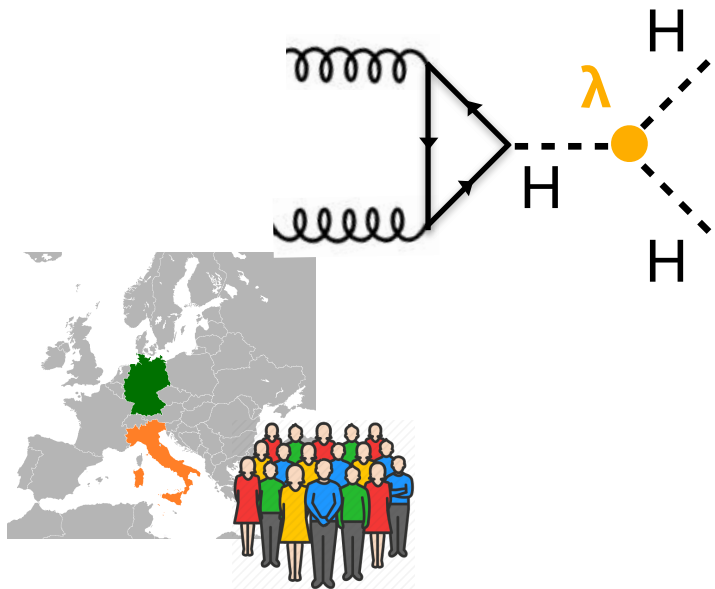


Systematics

2017

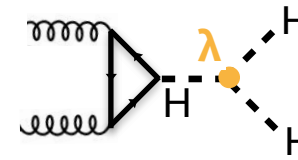


Impact in the combination



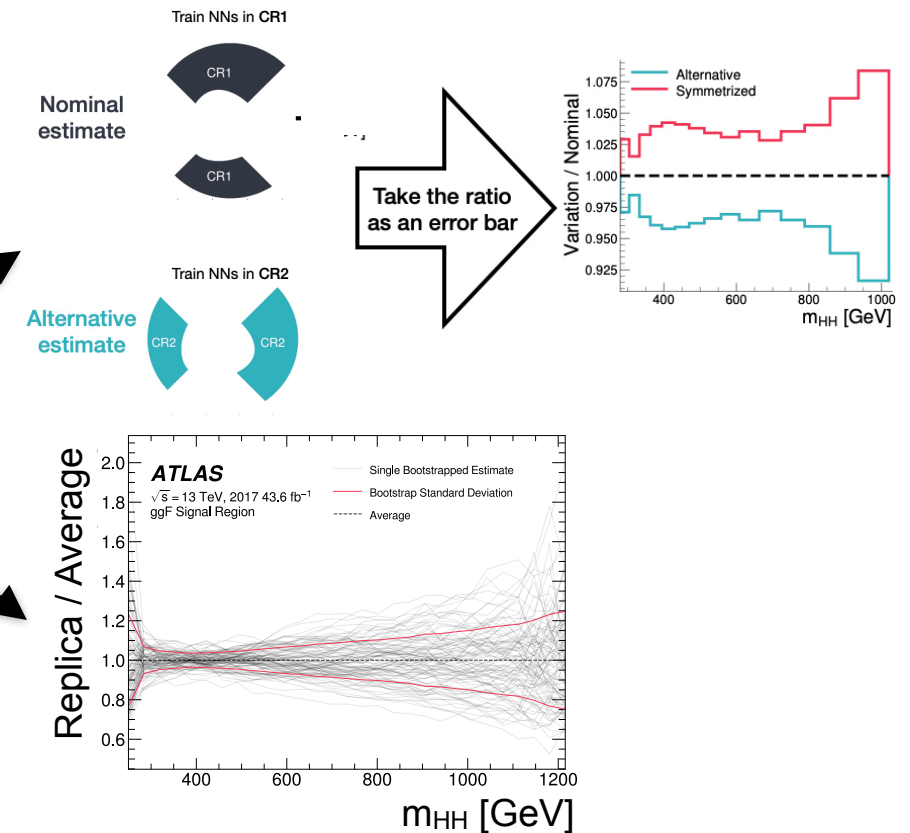
Impact in one analysis

Impact on upper limit on $\sigma(\text{ggF HH})$



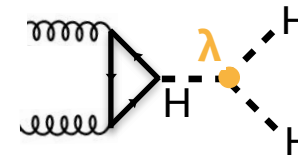
Source of uncertainty		$ \Delta\mu /\mu$
Theoretical	Uncertainty on signal rate	9.0%
	All other theory uncertainties	1.4%
Background modeling	Choice of CR	7.5%
	NN retraining (100x)	7.1%
	3b non-closure	2.0%


All other experimental systematics [FTAG, Jets, ...] < %-level impact



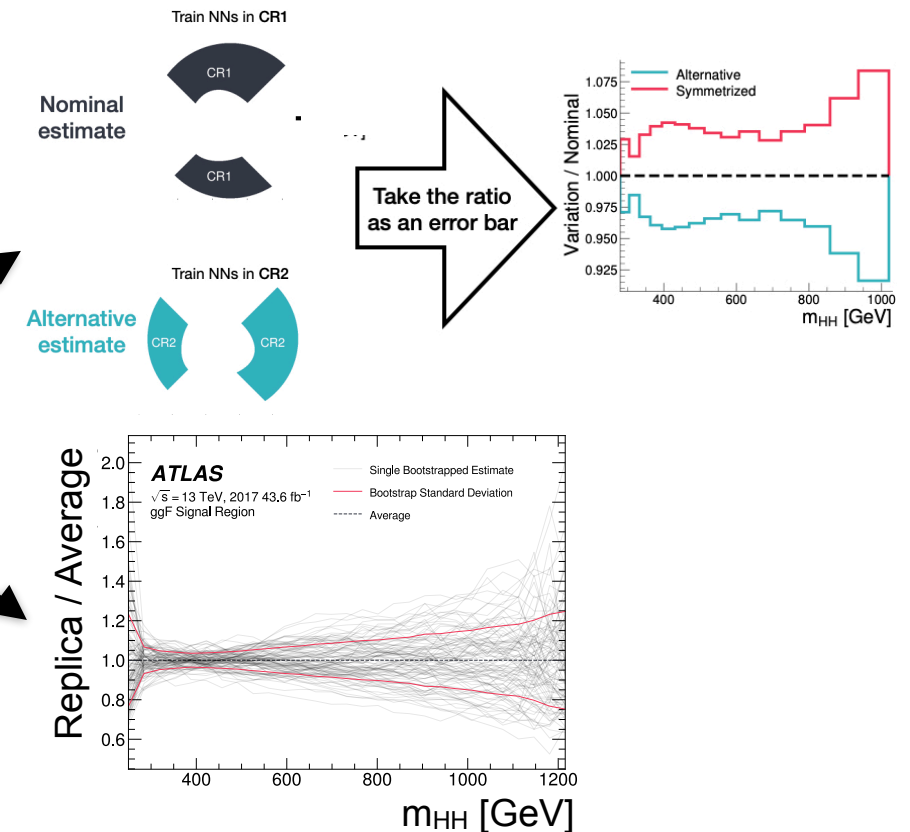
Impact in one analysis

Impact on upper limit on $\sigma(\text{ggF HH})$



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All other experimental systematics [FTAG, Jets, ...] < %-level impact



Better background modelling **key** for improving this analysis!

How will ML continue to improve our analysis?

Better
b-taggers

End-to-end
optimization strategies

Flows for background
modelling

Flows for high dimensional interpolation

Hierarchical model: $p(x, m_{H1}, m_{H2}) = p(x | m_{H1}, m_{H2}) p(m_{H1}, m_{H2})$

Normalizing flow

Gaussian process

x : Event kinematics

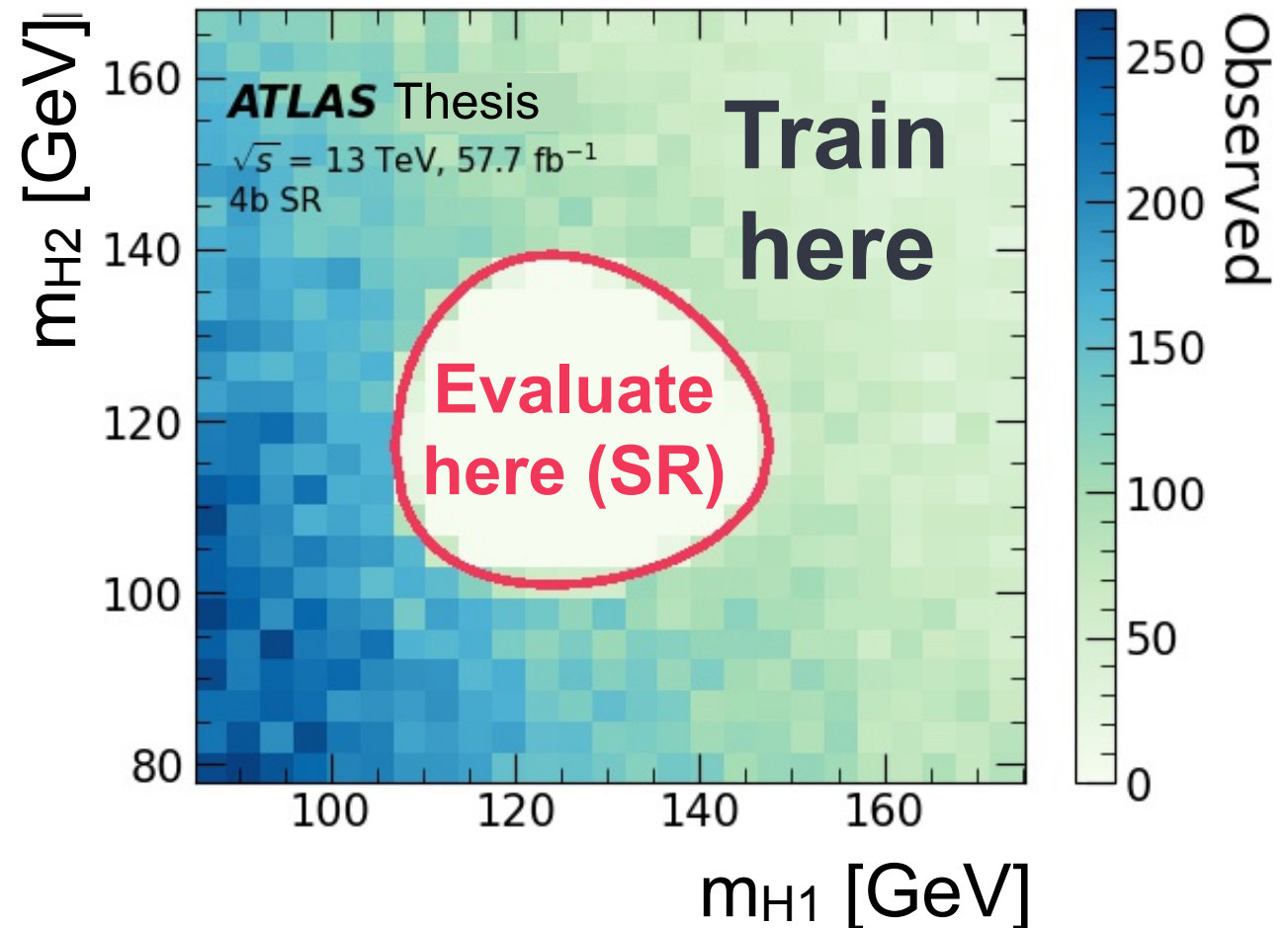
$p_{T,H1}, p_{T,H2}, \eta_{H1}, \eta_{H2}, \Delta\phi_{HH}, X_{wt}$ [top veto]



Use the smoothly varying (m_{H1}, m_{H2}) to predict **SR** kinematics.



Conceptually identical to CATHODE



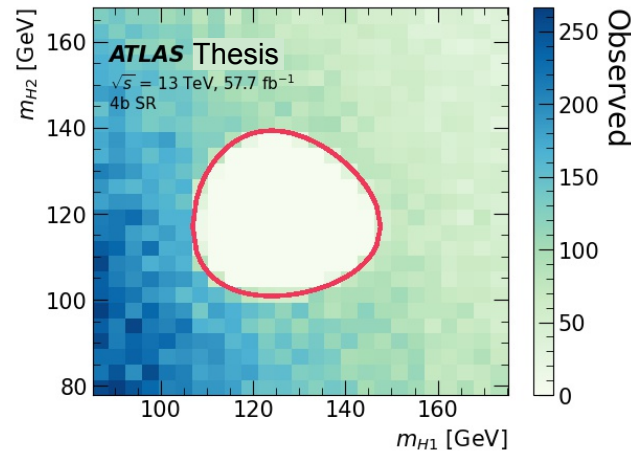
$$p(x, m_{H1}, m_{H2}) = p(x | m_{H1}, m_{H2}) p(m_{H1}, m_{H2})$$

1) GP fits

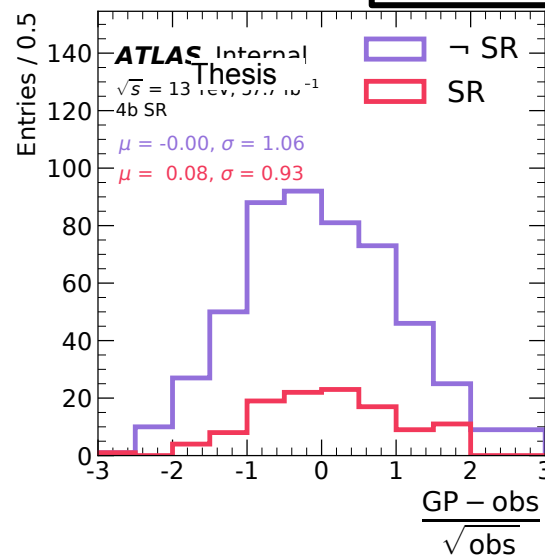
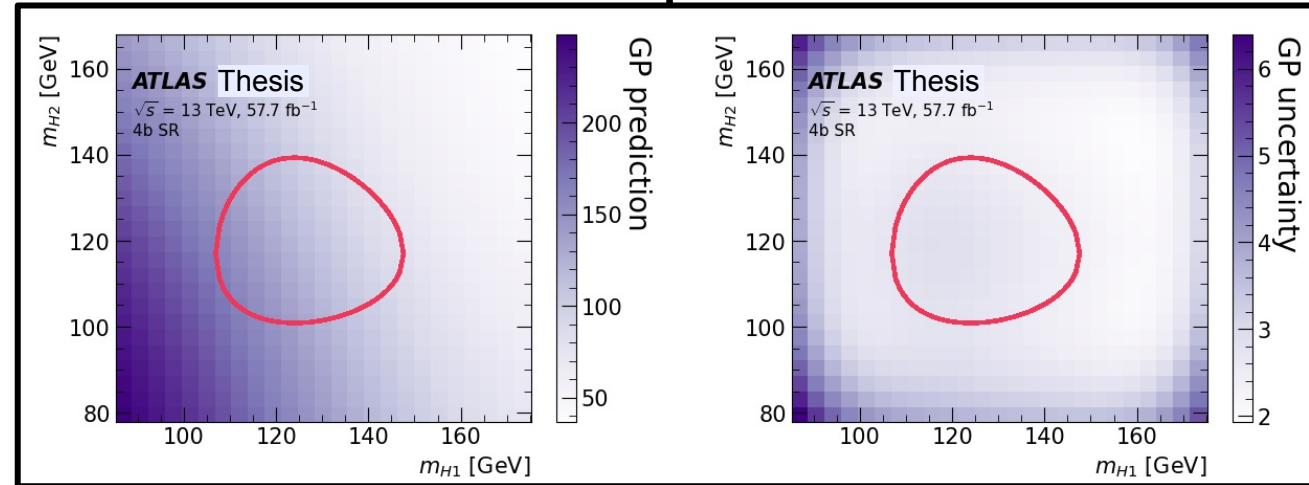
Fit a GP to the 2d (m_{H1}, m_{H2}) histogram

Radial basis function kernel, 2d length scale

Input



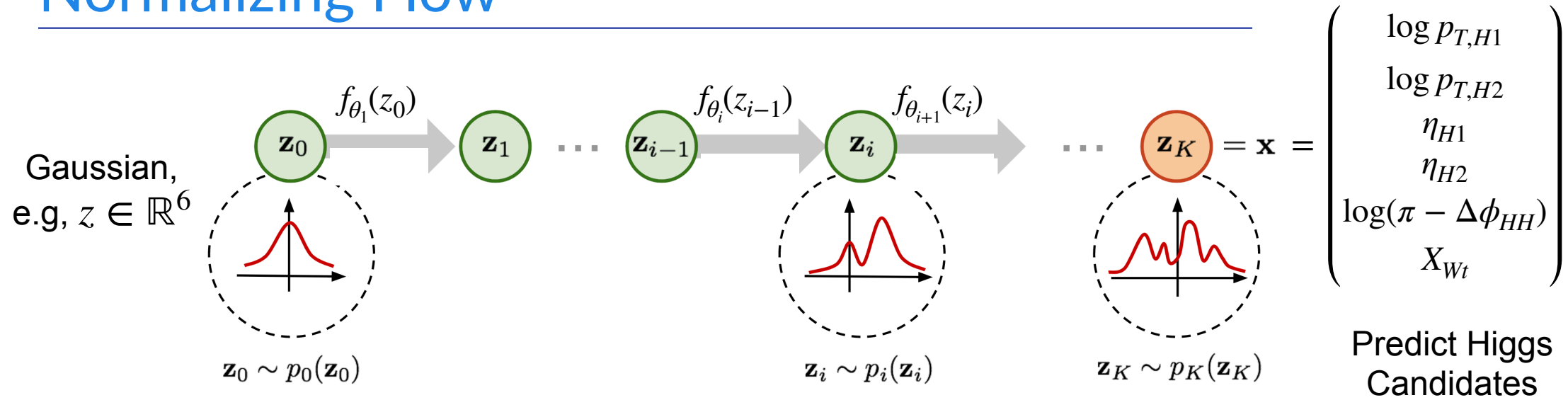
Output



Set the normalization from massplane fit: 

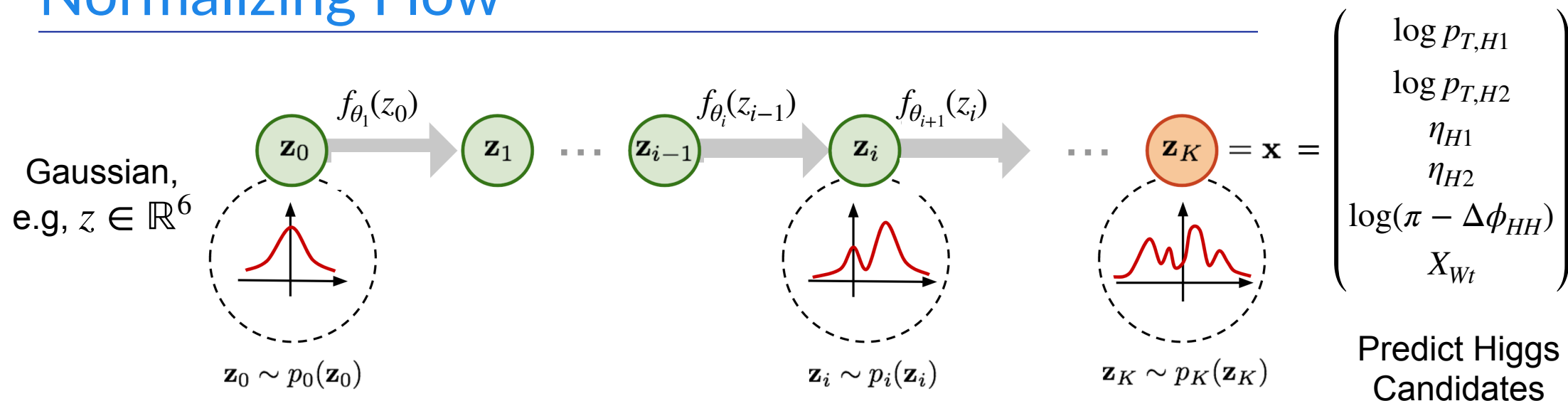
$$\text{SR yield} = \text{obs(not SR)} \frac{\text{pred(SR)}}{\text{pred(} \neg \text{ SR)}}$$

Normalizing Flow



Flow gradually from one distribution into another.

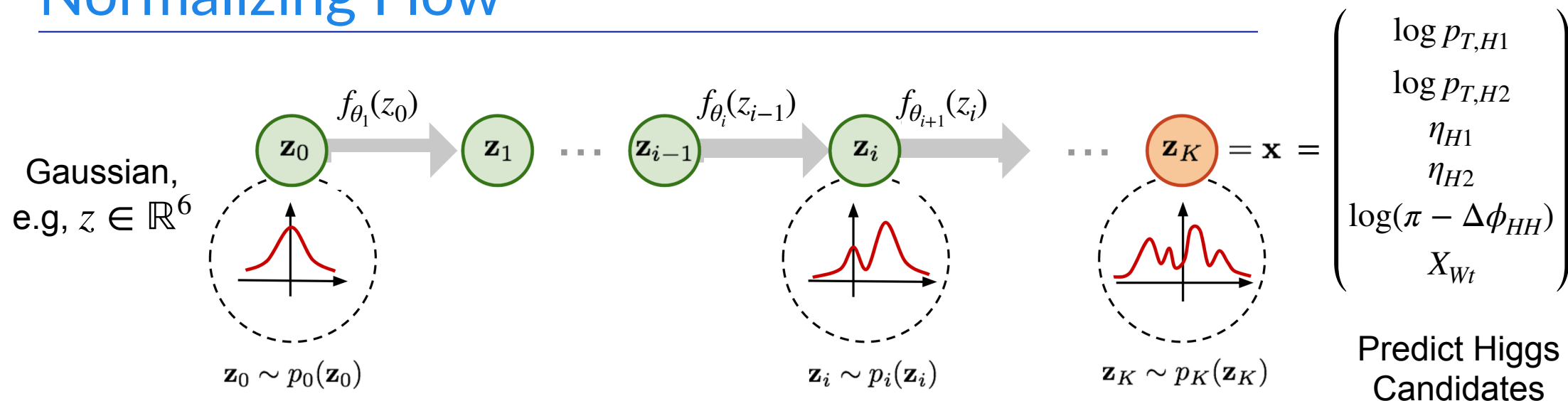
Normalizing Flow



Flow gradually from one distribution into another.

- $f_\theta = f_{\theta_L} \circ \dots \circ f_{\theta_2} \circ f_{\theta_1}$
- Invertible f_{θ_i} allow us to get the density of training samples

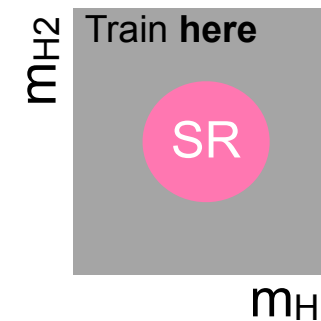
Normalizing Flow



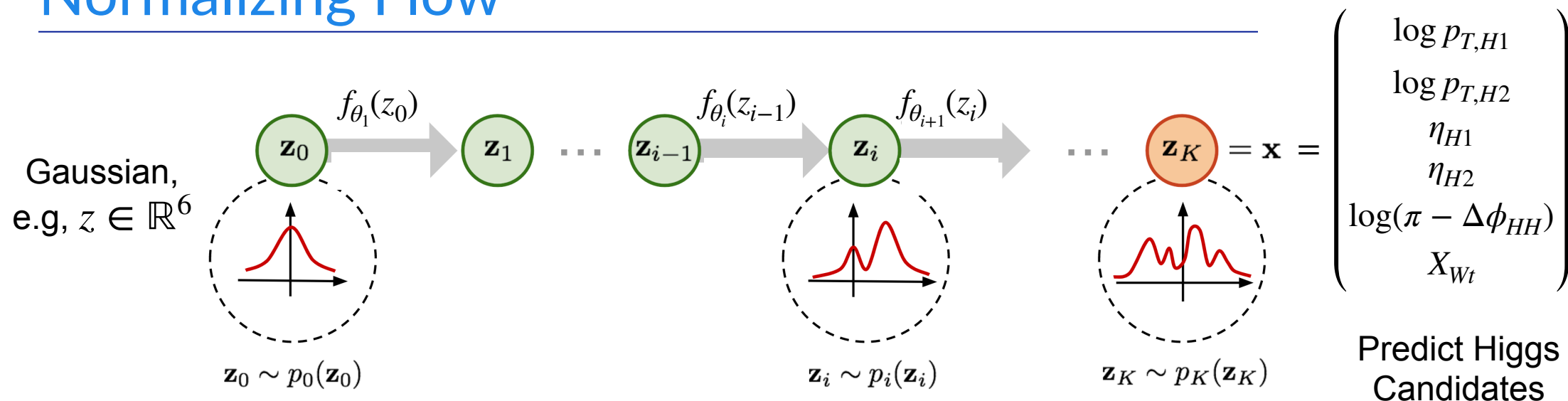
Flow gradually from one distribution into another.

- $f_\theta = f_{\theta_L} \circ \dots \circ f_{\theta_2} \circ f_{\theta_1}$
- Invertible f_{θ_i} allow us to get the density of training samples
- Conditional generative model $p_\theta(x|y)$, $y = (m_{H1}, m_{H2})$

Key for interpolation!



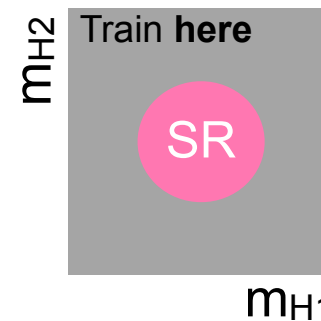
Normalizing Flow



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Key for interpolation!

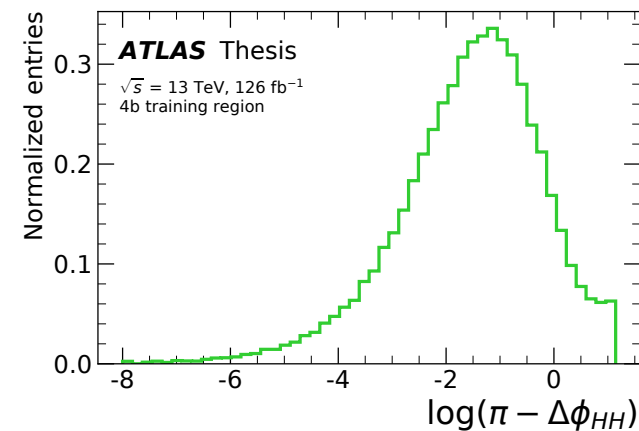
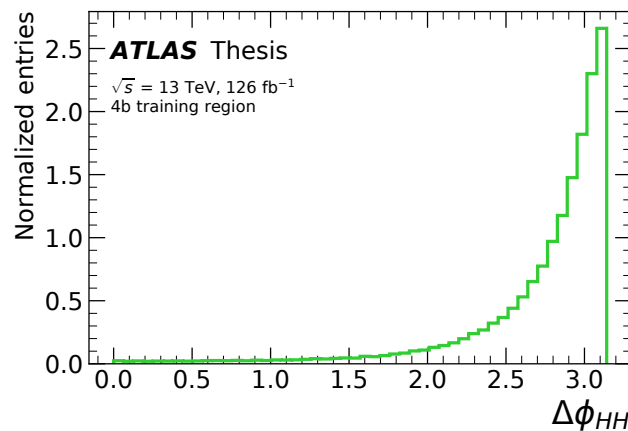
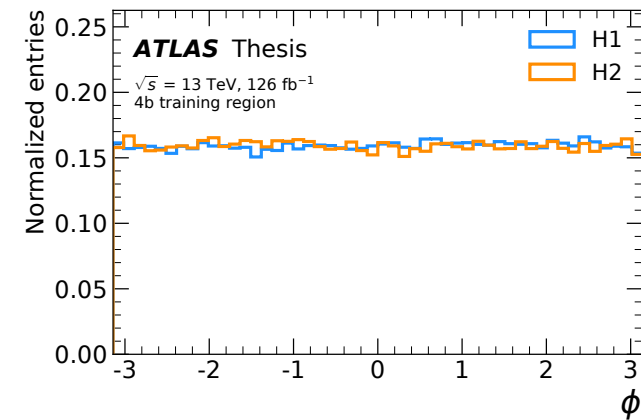
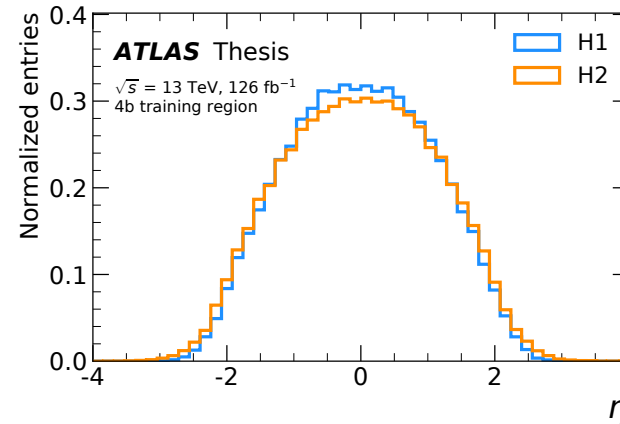
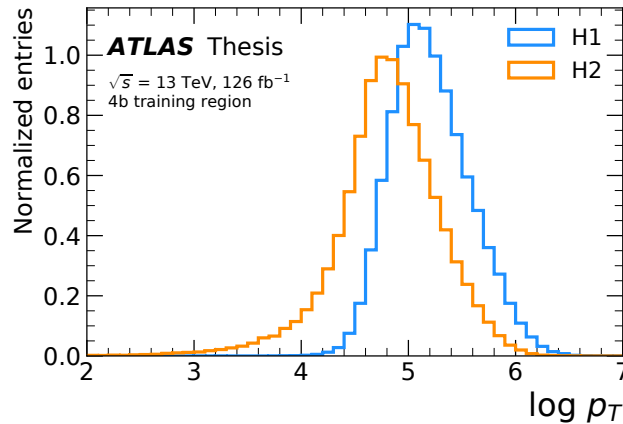


$$\mathcal{L}oss = -\log p_\theta(x|y) = -\log p_z(f_\theta^{-1}(x|y)) - \sum_{i=1}^K \left| \frac{\partial f_{\theta_i}^{-1}}{\partial z_i^T} \right|$$

Input processing: HH \rightarrow 4b background modeling

Conditioning on $m_{h1}, m_{h2} \rightarrow$ ~~5~~ variables left to model

Concerned about modeling b/c no way to know that $-\pi \rightarrow \pi$.



Constant $\Delta\Phi_{HH}$ - will give the same m_{HH}

Azimuthal symmetry baked into the model



Symmetry

model with symmetry

Input processing : HH -> 4b background modeling

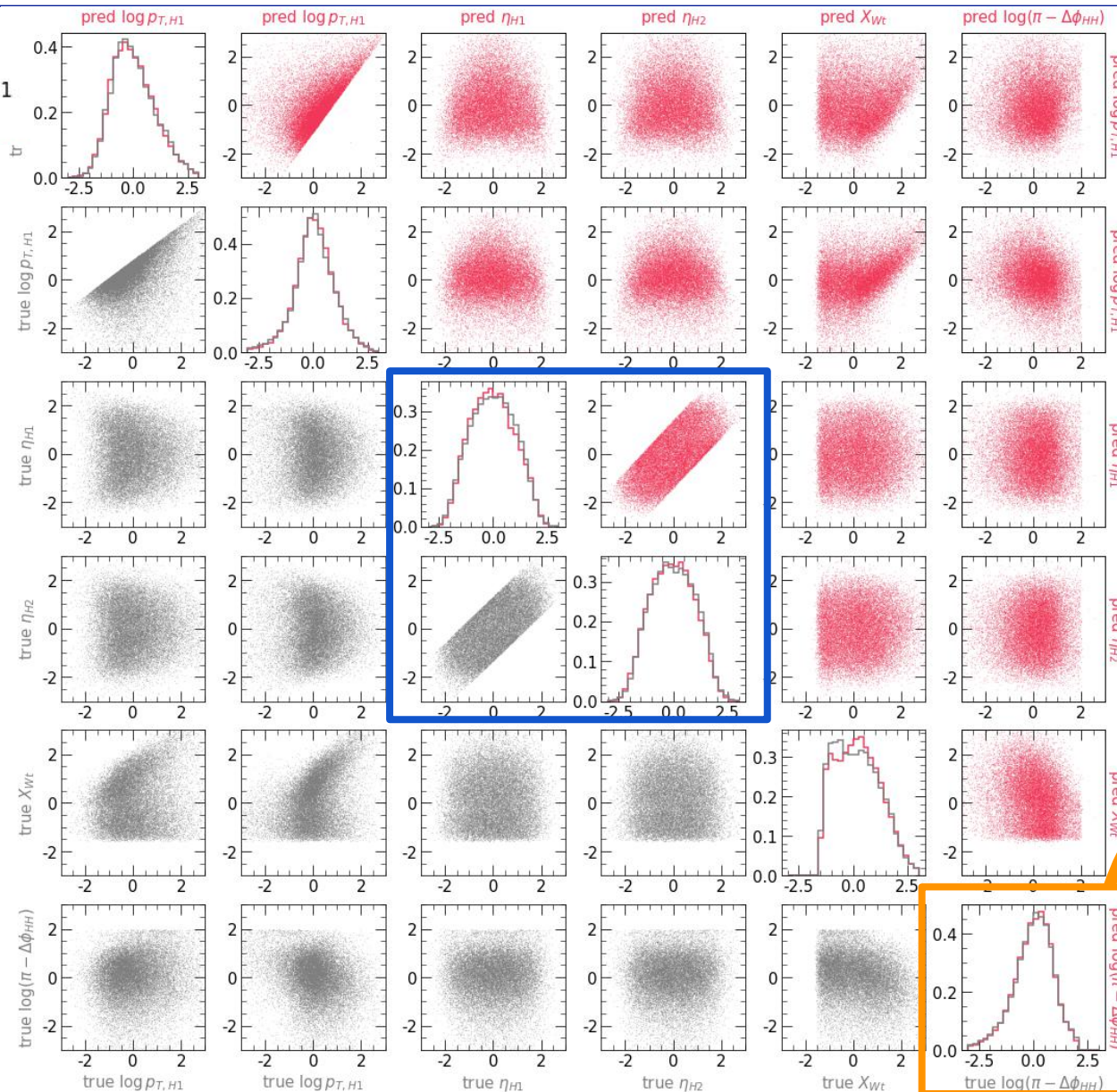
ATLAS Thesis

$\sqrt{s} = 13 \text{ TeV}, 126 \text{ fb}^{-1}$
4b SR

Learns about
preprocessing cut
($\Delta\eta_{\text{HH}} < 1.5$)

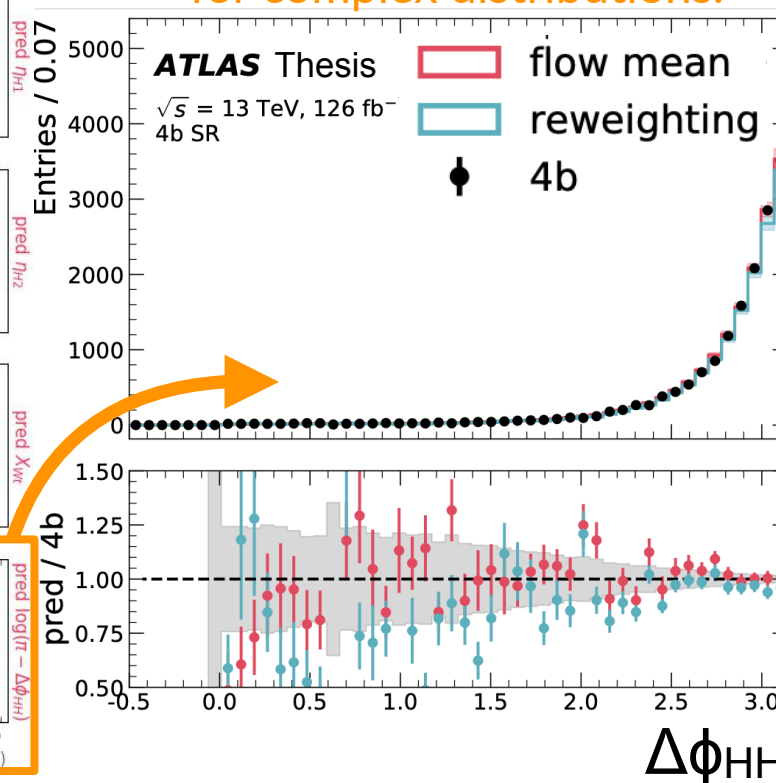
4b data

24 / 31



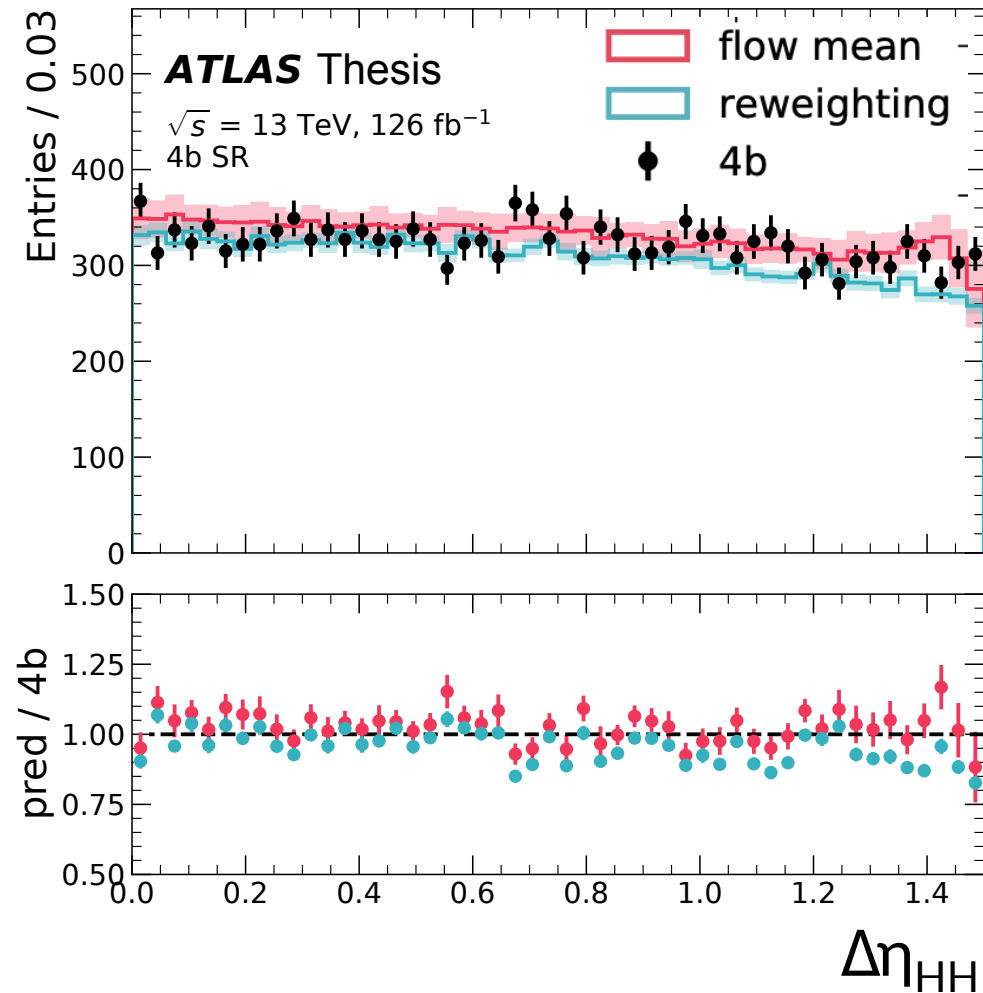
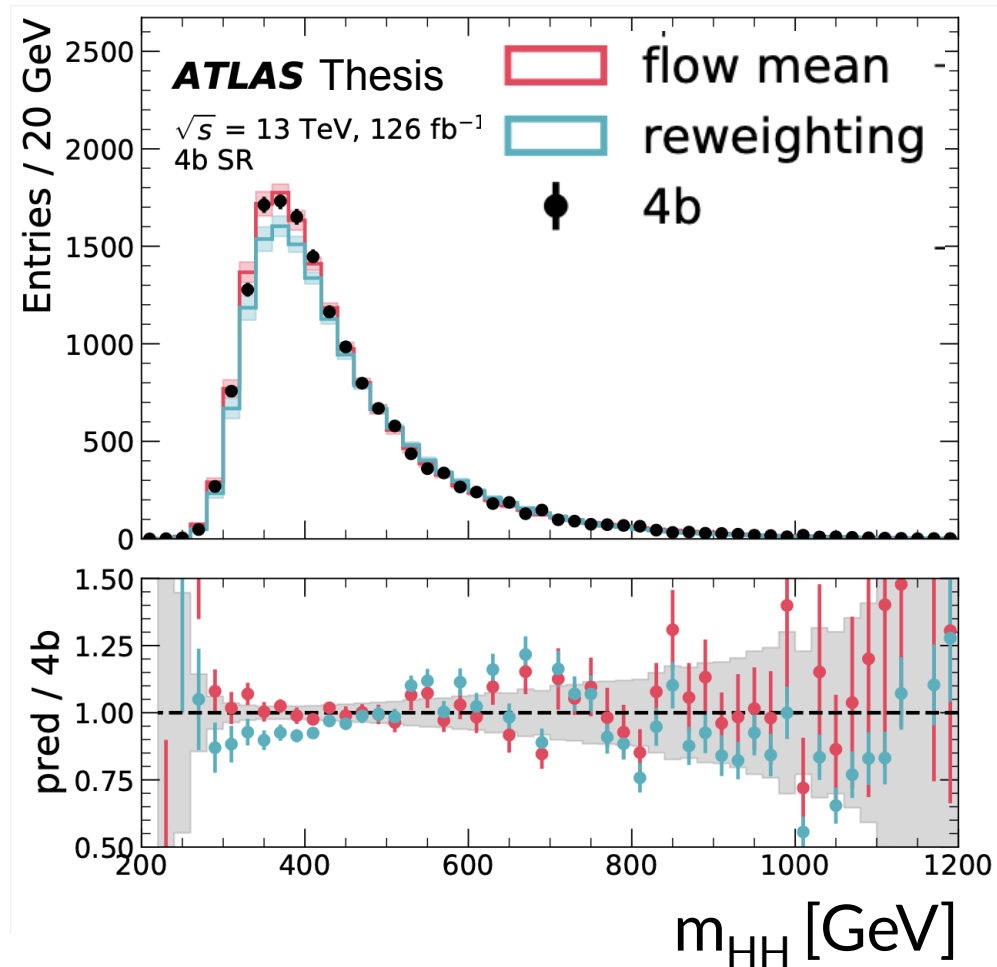
flow
prediction

Good transformations help
for complex distributions.



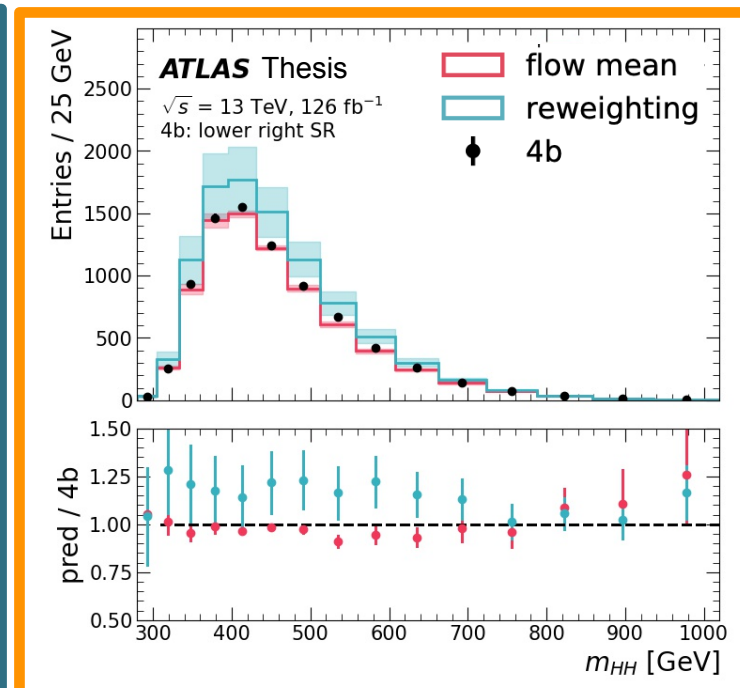
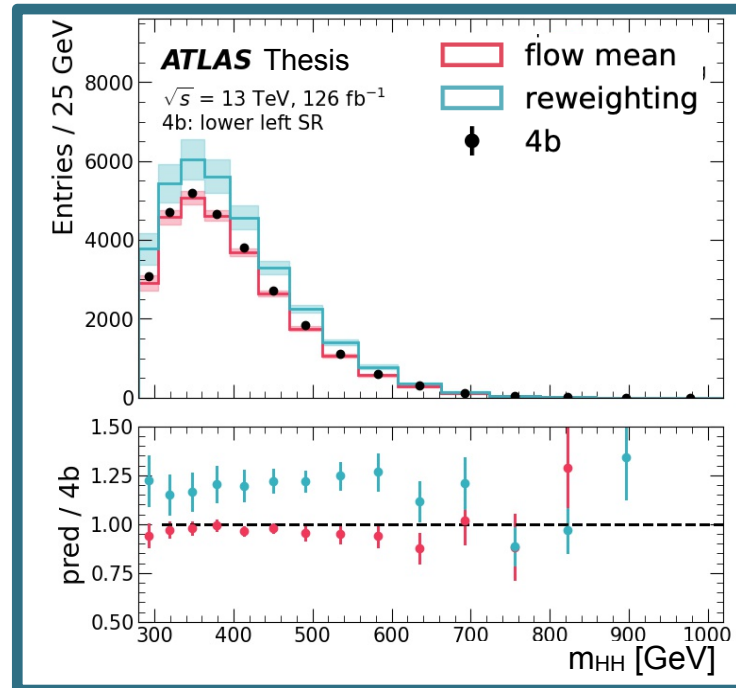
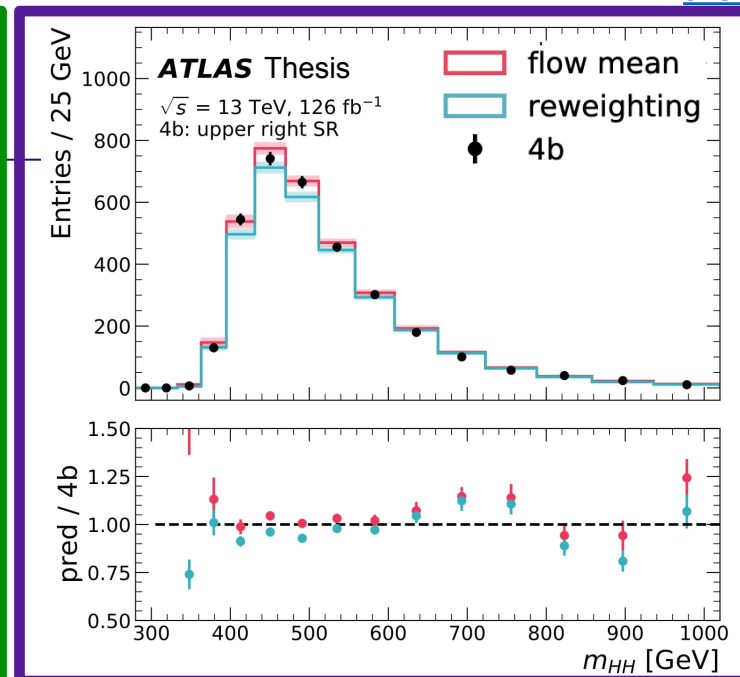
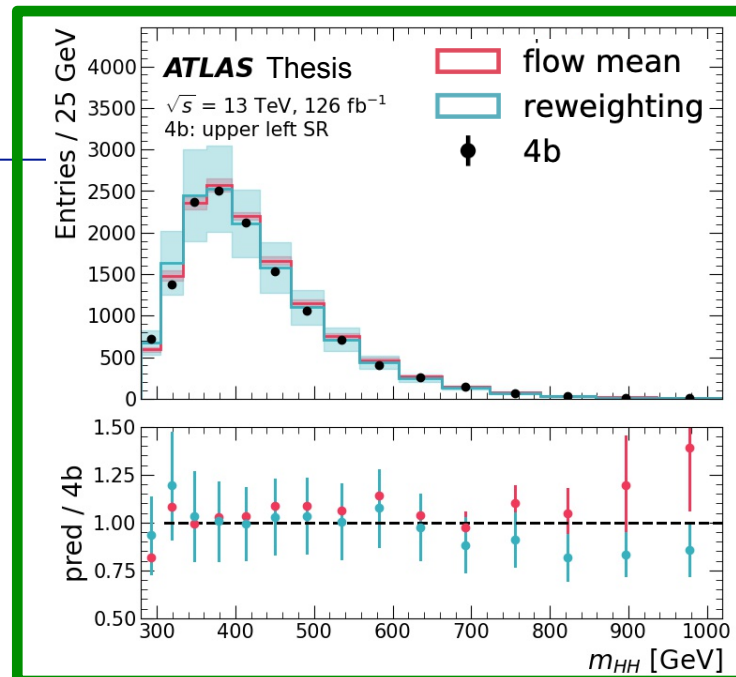
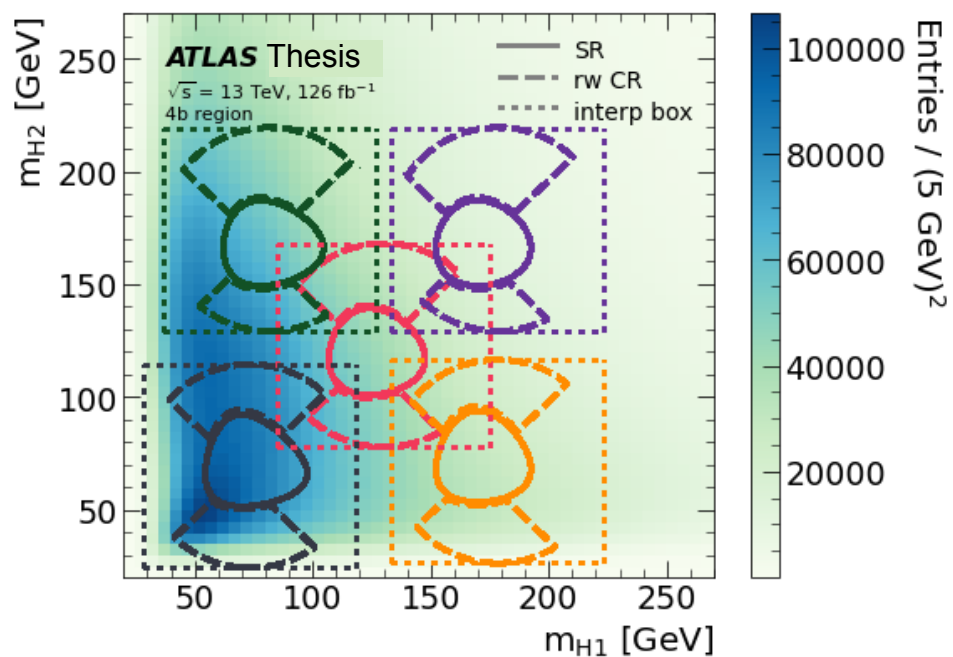
Input processing : HH \rightarrow 4b background modeling

Variable transformations

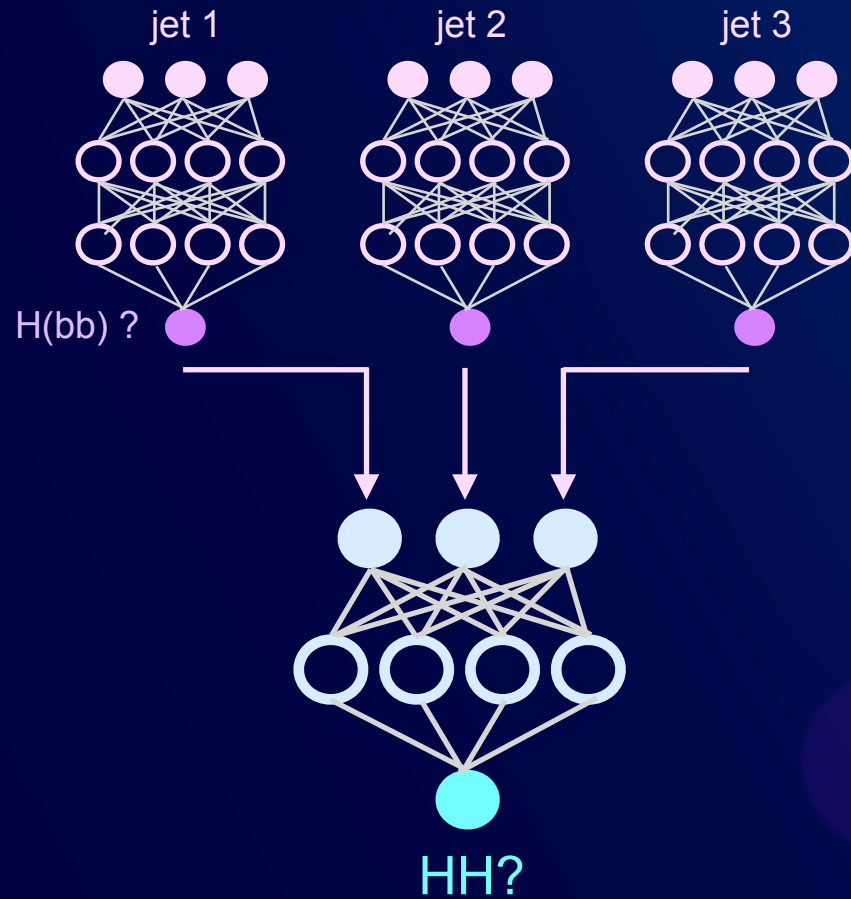


Promising... better closure.

Shifted regions

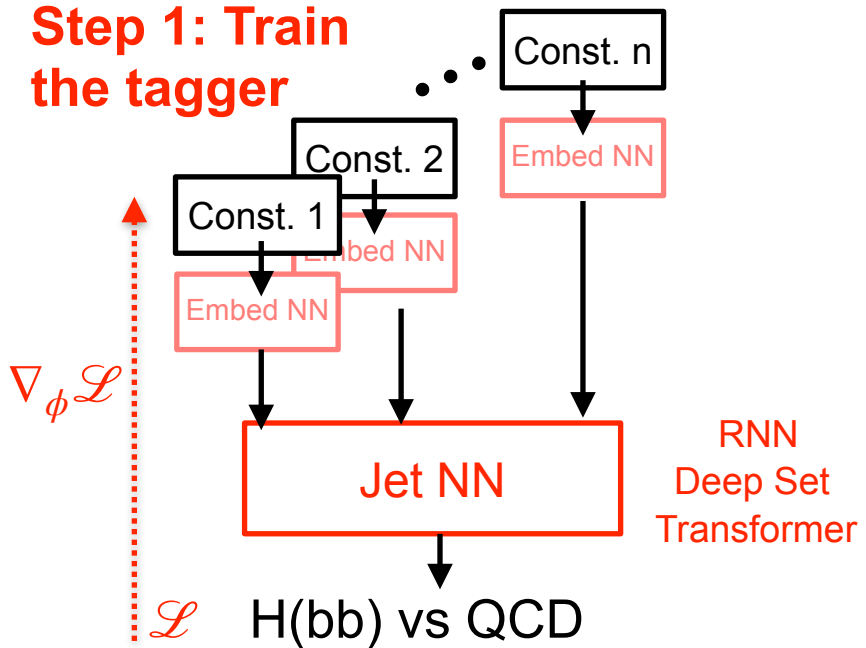


Can we use gradient optimization more?

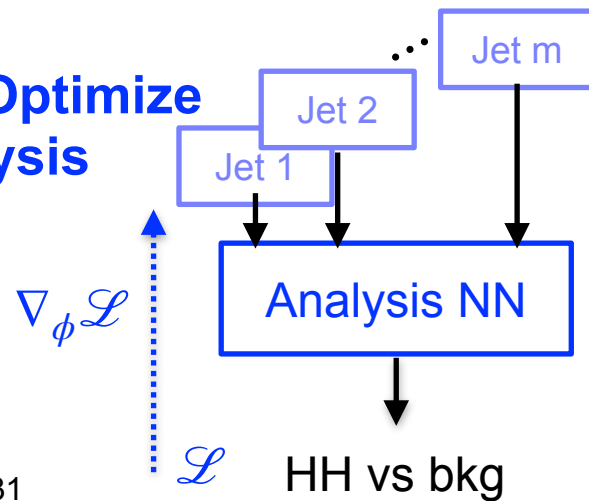


Traditional Analysis

Step 1: Train the tagger



Step 2: Optimize the analysis



Lukas Heinrich



Matthias Vigl

Traditional Analysis

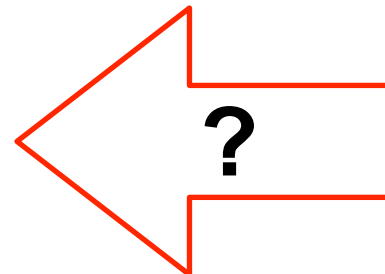
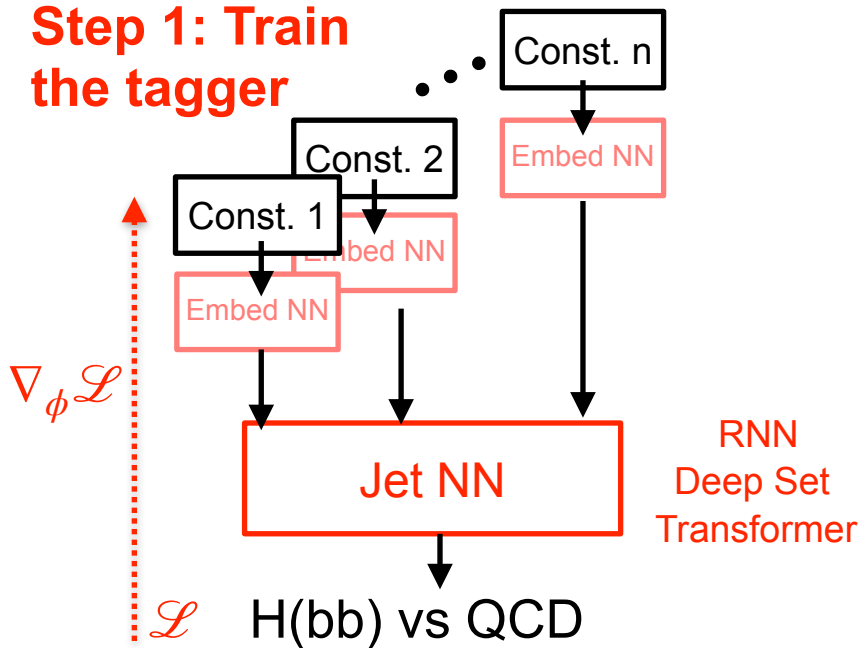


Lukas Heinrich



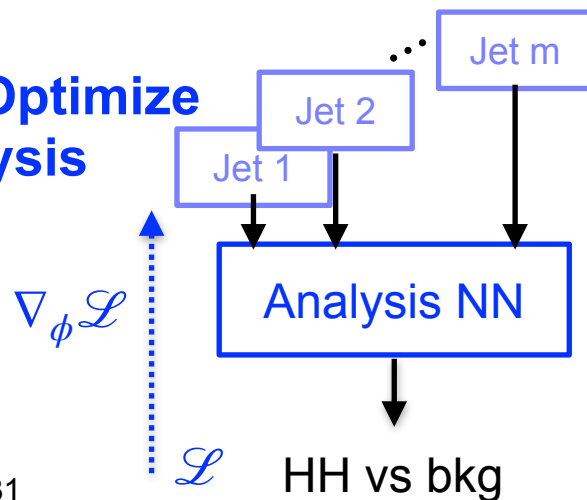
Matthias Vigl

Step 1: Train the tagger



How do you know we this particle classifier is optimal for every analysis?

Step 2: Optimize the analysis



Traditional Analysis

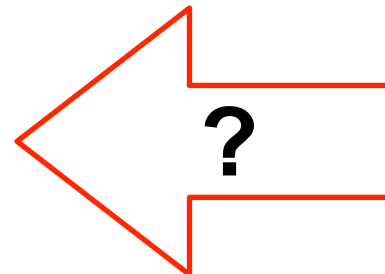
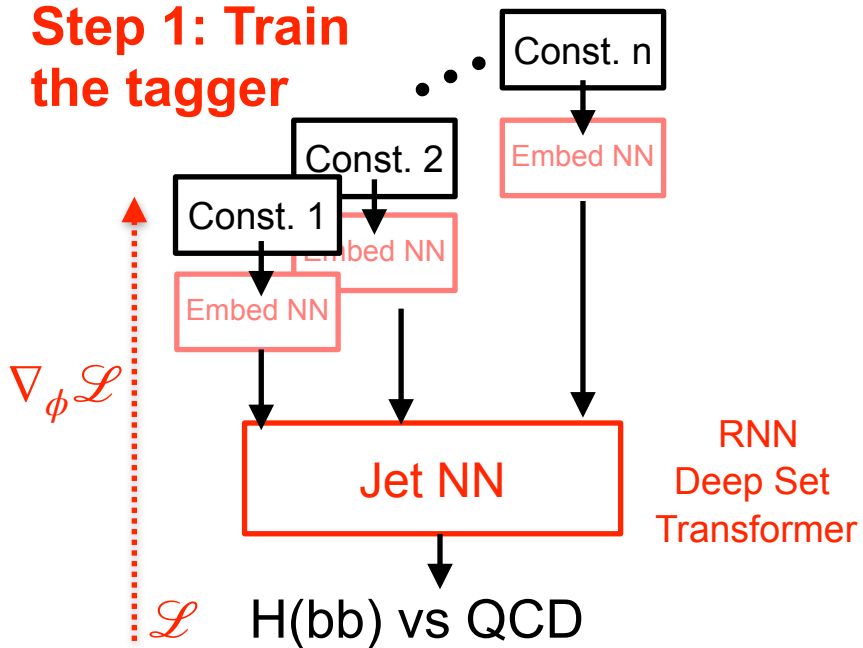


Lukas Heinrich



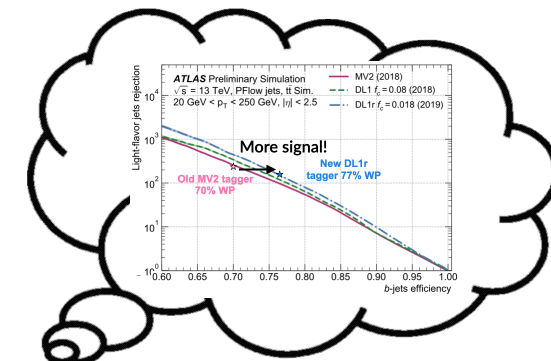
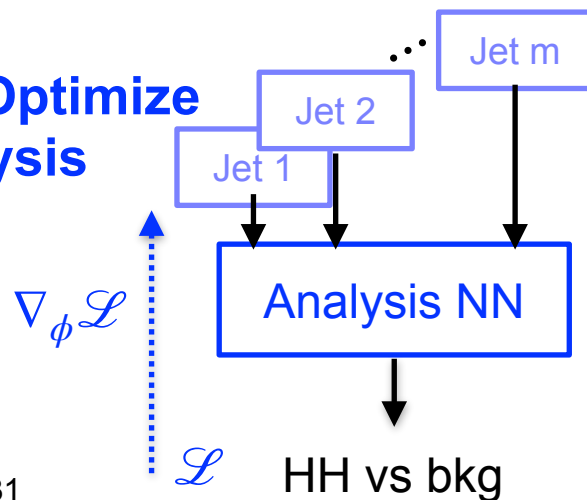
Matthias Vigl

Step 1: Train the tagger



How do you know we this particle classifier is optimal for every analysis?

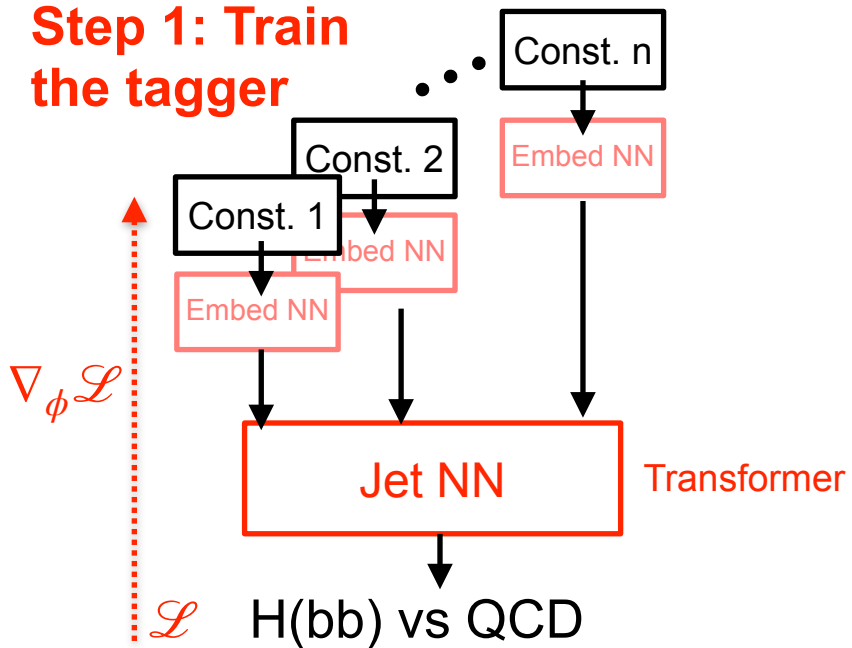
Step 2: Optimize the analysis



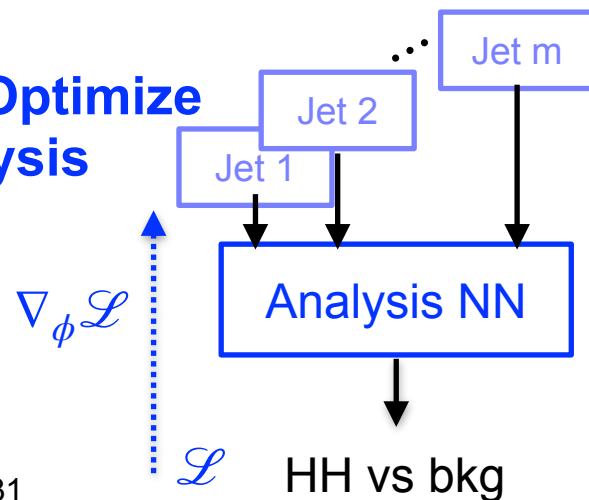
In some sense... we know it's not... analyses optimize tagger "working points"

Traditional Analysis

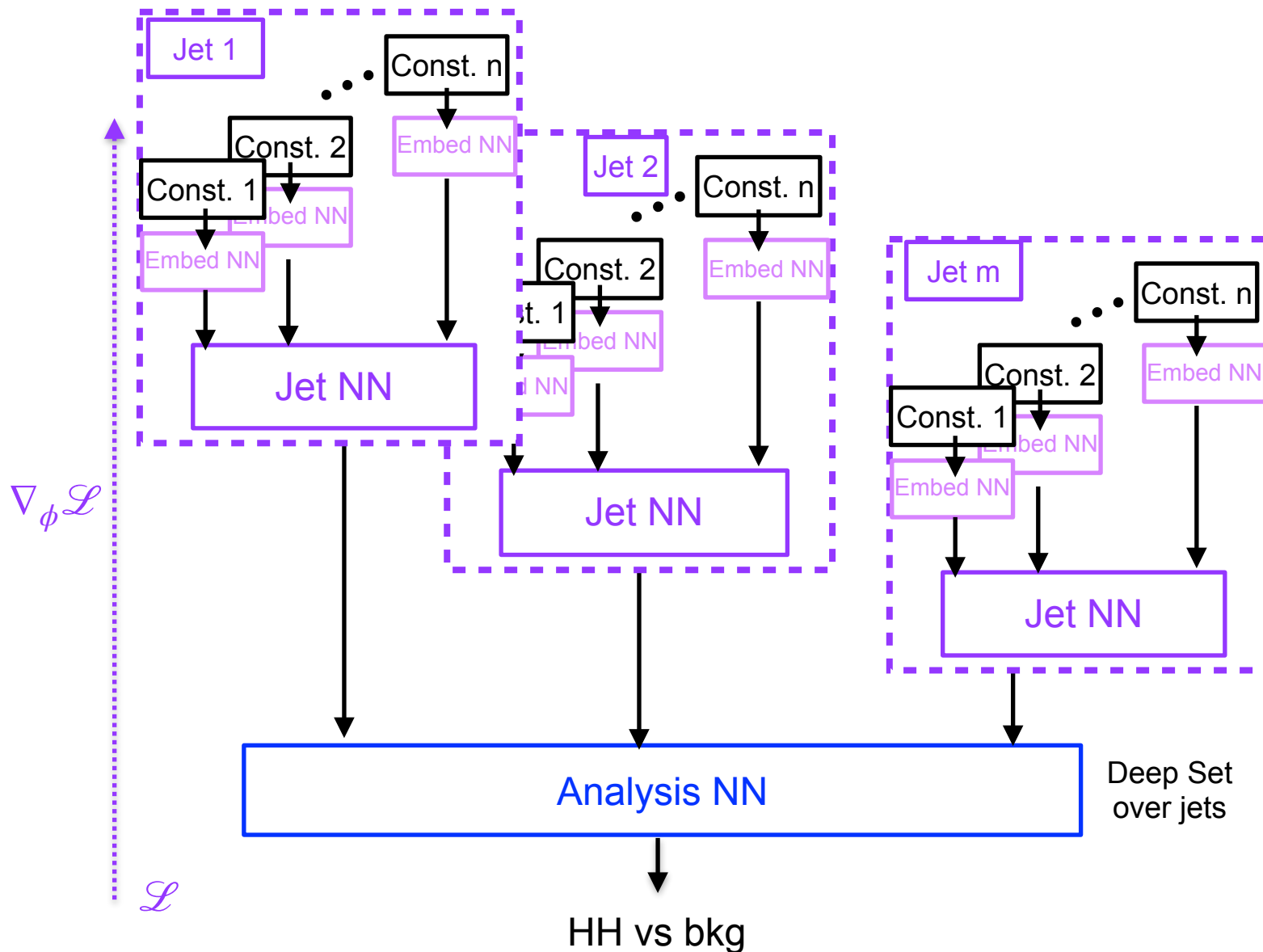
Step 1: Train the tagger



Step 2: Optimize the analysis



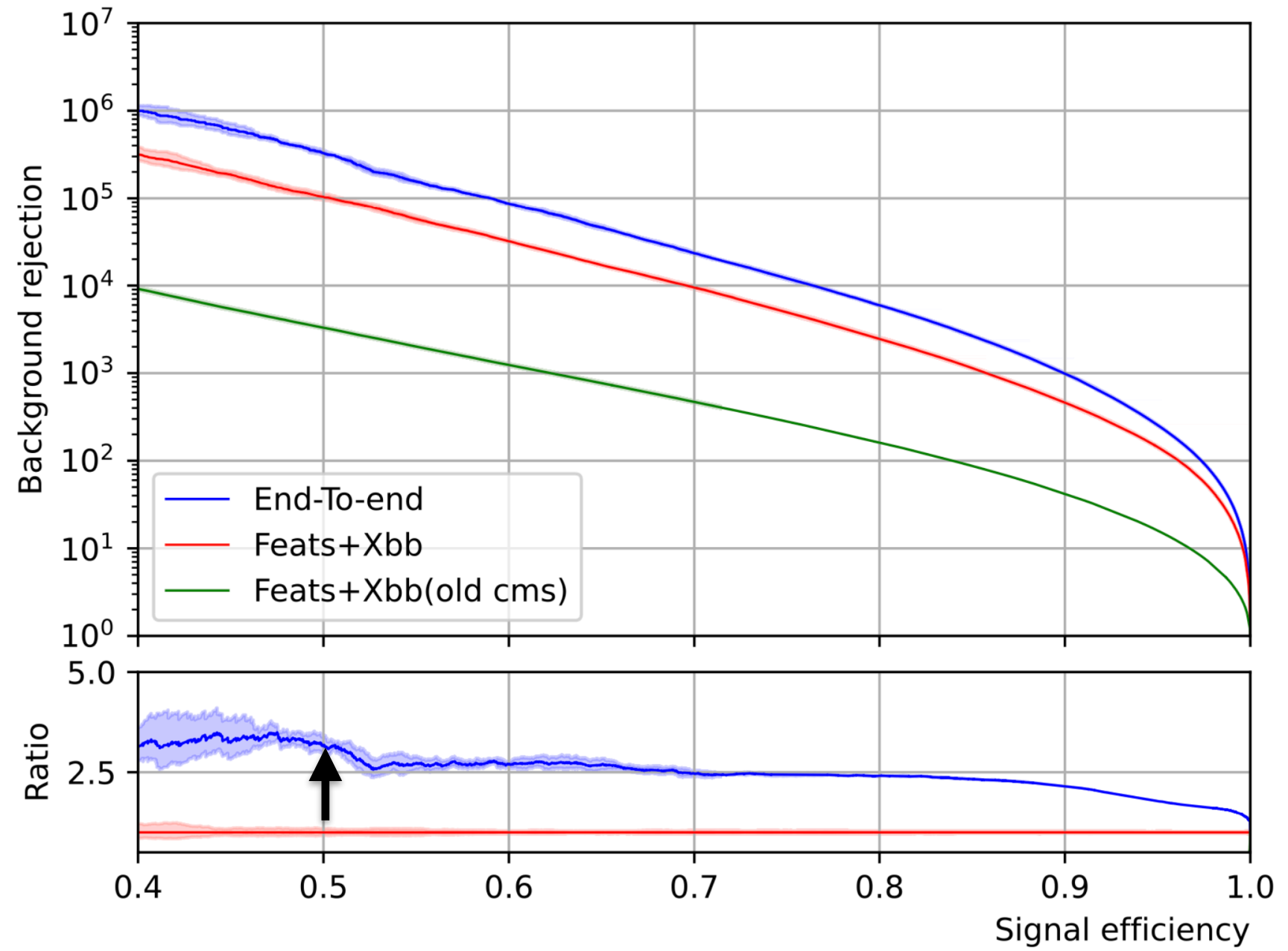
New paradigm



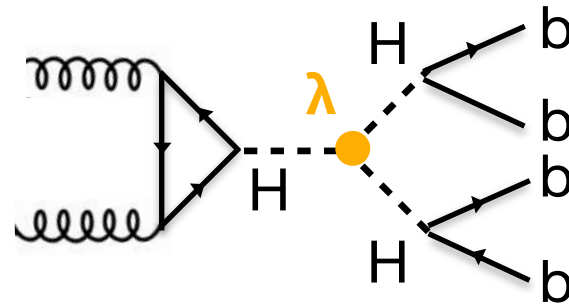
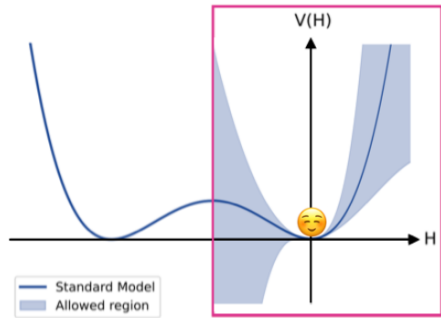
Dataset: CMS Open Data
Signal: $X \rightarrow HH \rightarrow 4b$
Bkg: QCD simulation

Jet Tagger: Transformer,
ParT [2202.03772],
start from published weights
(pre-training with 100m jets
in JetClass dataset)

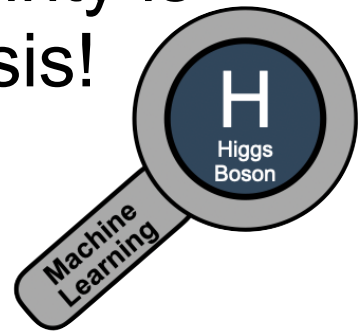
There is a gain with
an end-to-end
analysis!



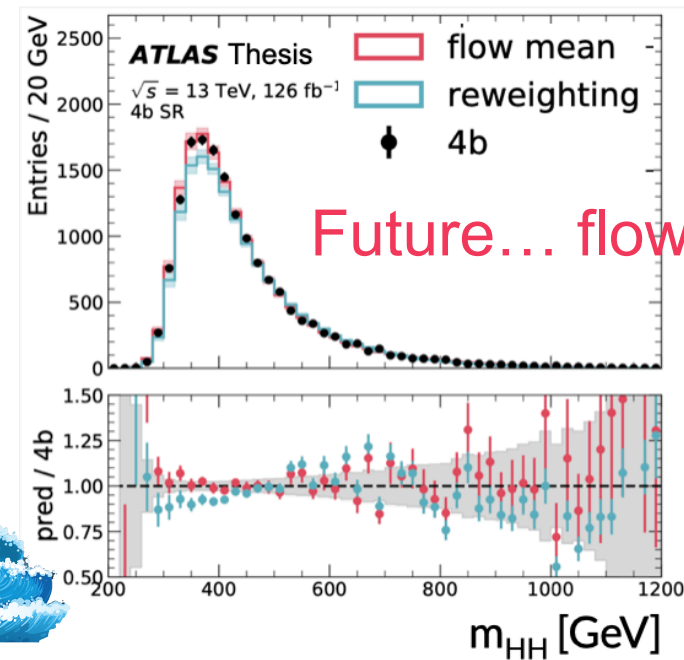
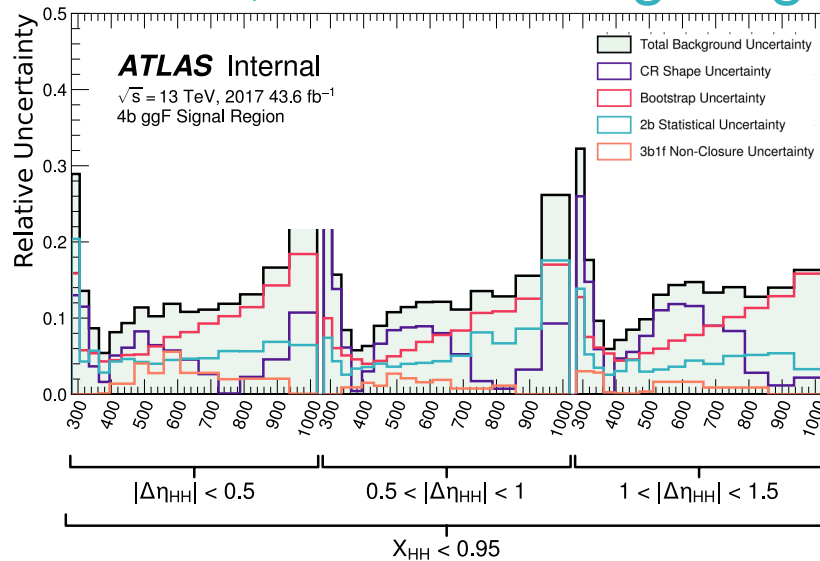
Conclusion



A background model with an accurate uncertainty is **key** to this analysis!

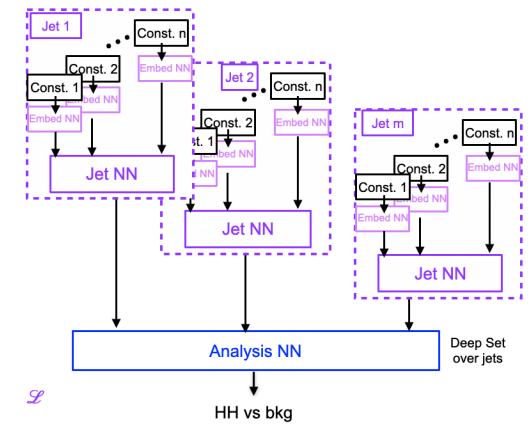


Run 2, neural reweighting



Very exciting time for ML in Run 3 and **bbbb**beyond!

Backup



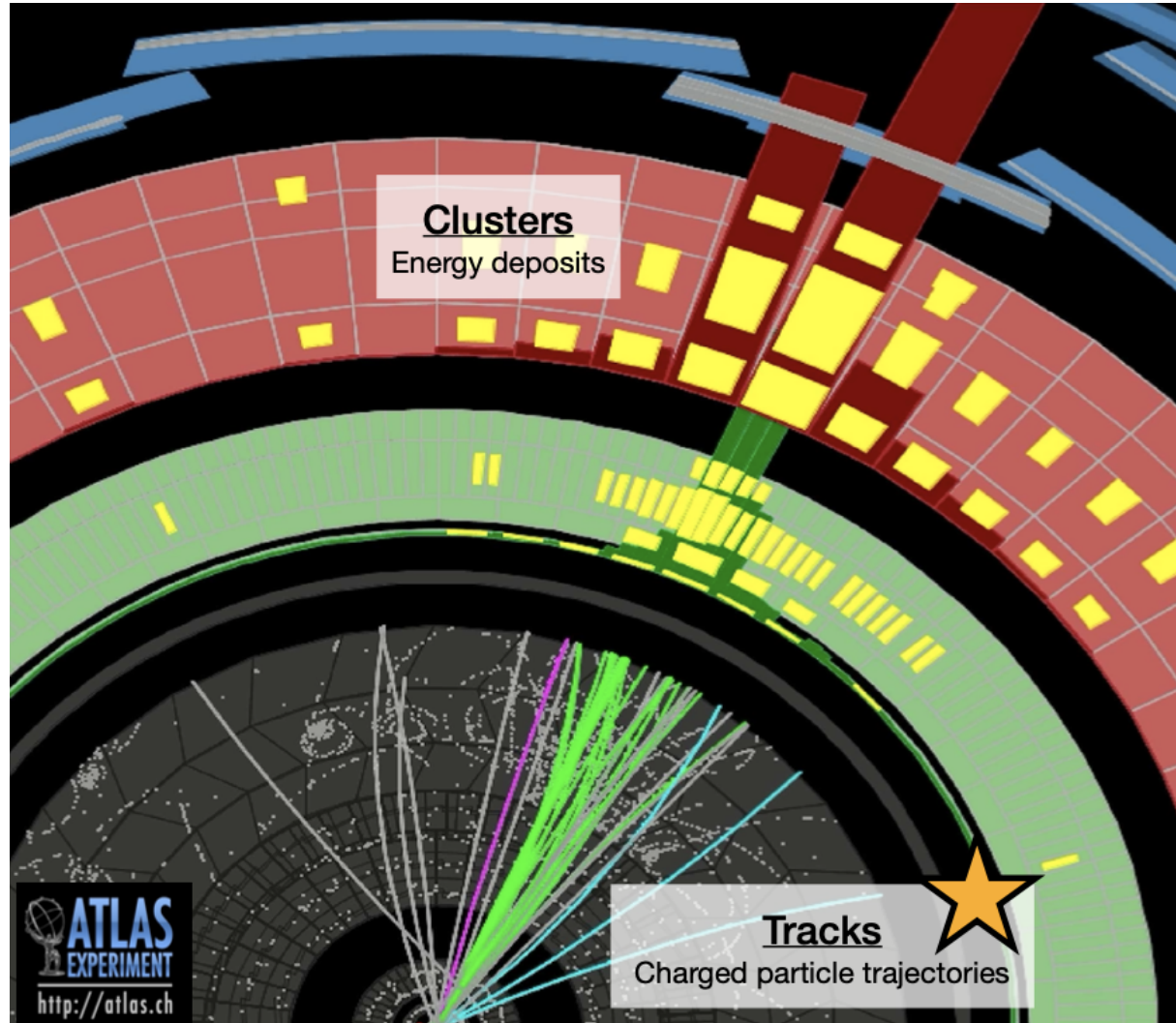
And exciting new ways to start rethinking our analyses...

How can the next generation of ML improve this?

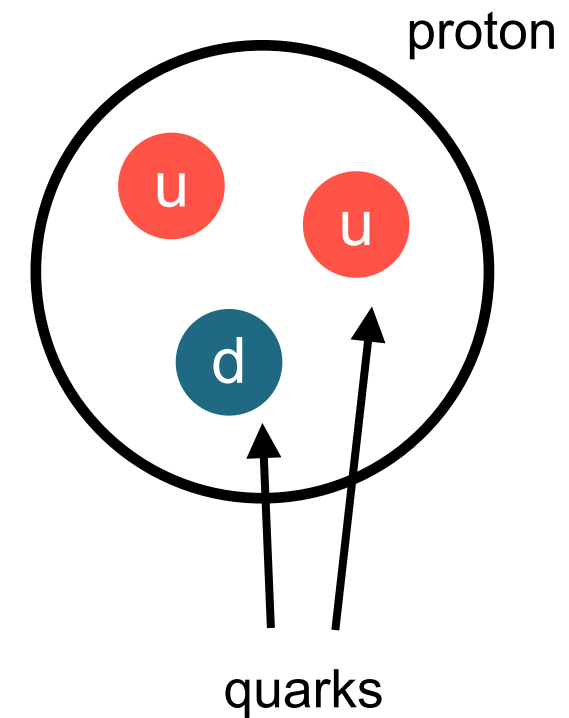
Limitations of reweighting methods:

1. Choice of CR
2. Suffers in regions of finite support
3. Limited by the stats of the “source distribution”

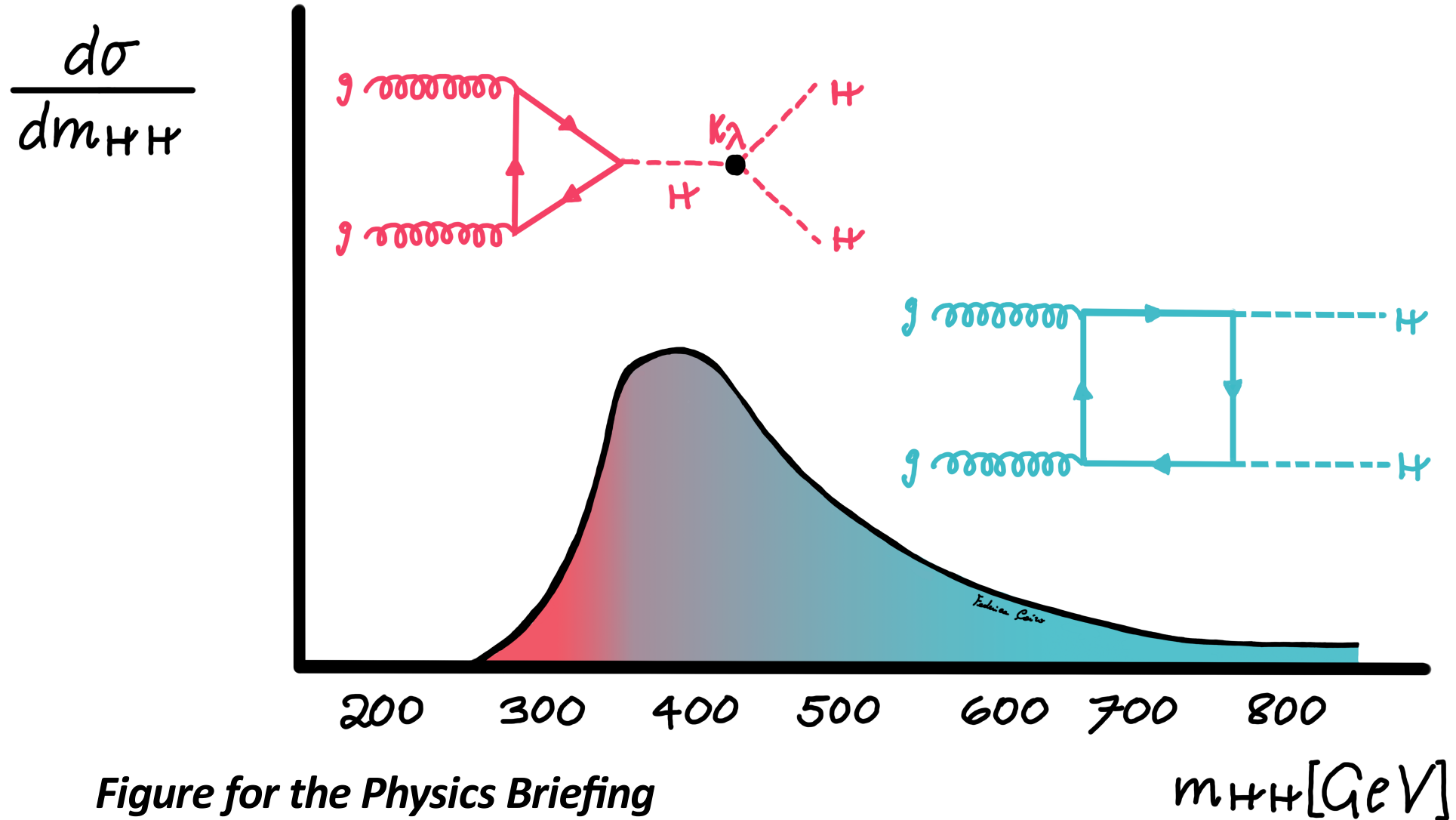
Quark signature



Quark → reconstructed
as collimated spray of
particles



Non resonant signal





b-jet

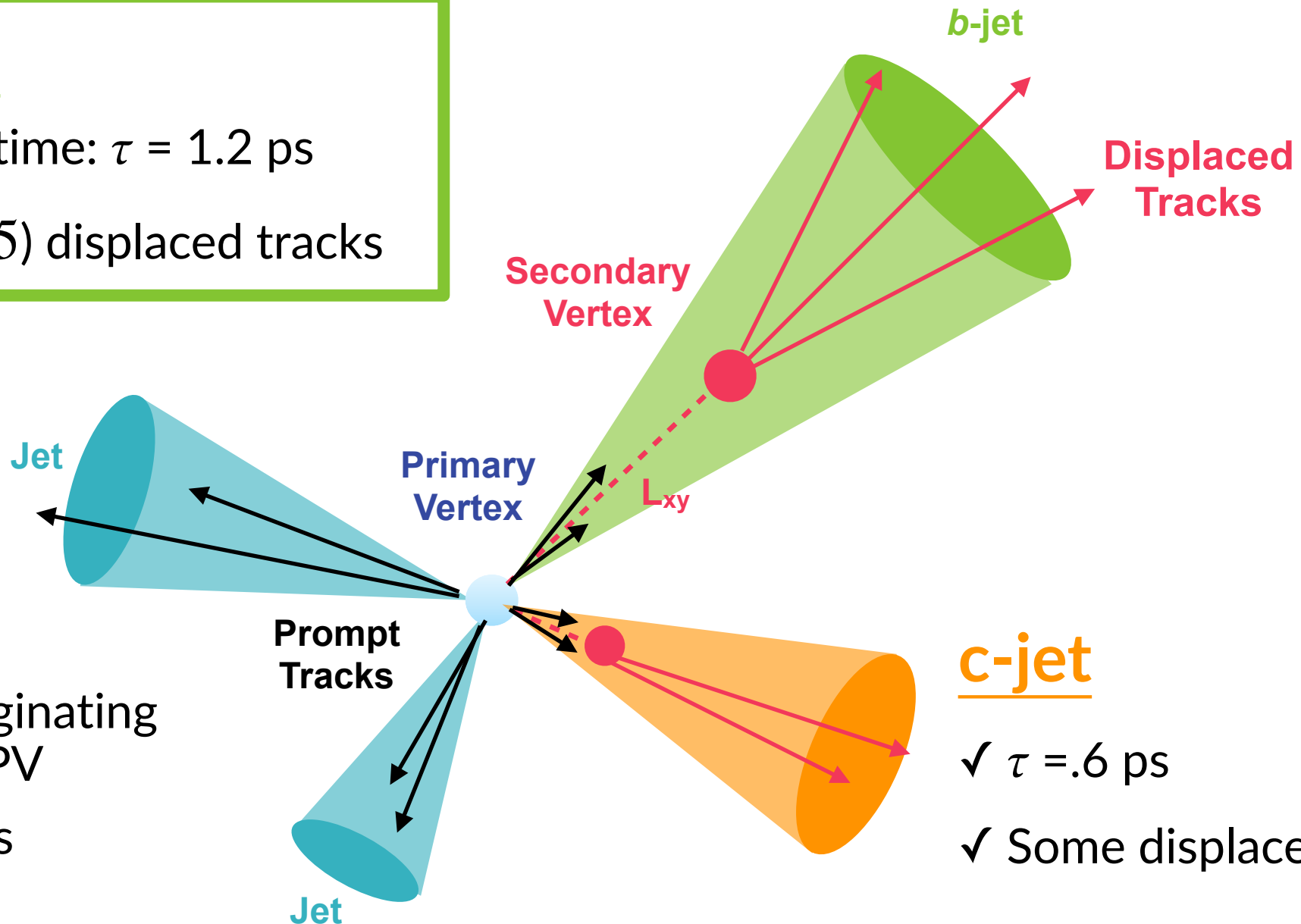
✓ “Long” lifetime: $\tau = 1.2$ ps

✓ Many (≈ 5) displaced tracks

light jet

✓ Tracks originating from the PV

✓ Few tracks



c-jet

✓ $\tau = .6$ ps

✓ Some displaced tracks

💕 b-jet

✓ “Long” lifetime: $\tau = 1.2$ ps

✓ Many (≈ 5) displaced tracks

Variable # of tracks

b-jet

Displaced Tracks

Secondary Vertex

Jet

light jet

✓ Tracks originating from the PV

✓ Few tracks

Prompt Tracks

Vertex

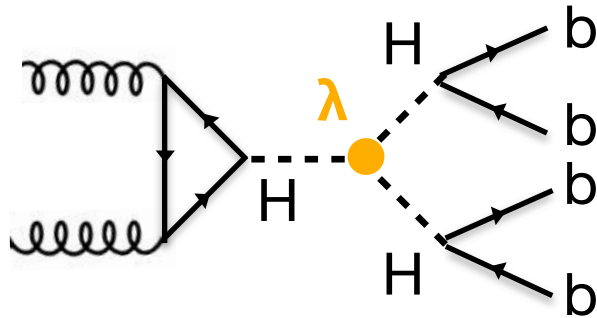
c-jet

$\tau = .6$ ps

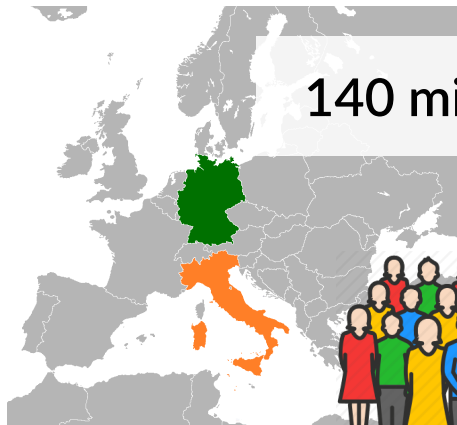
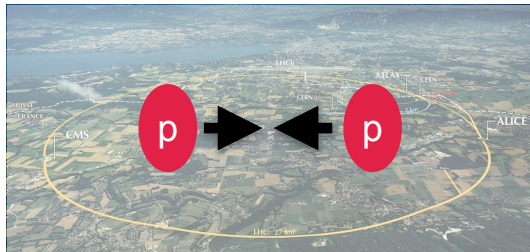
✓ Some displaced tracks

Jet

My research... guess who?

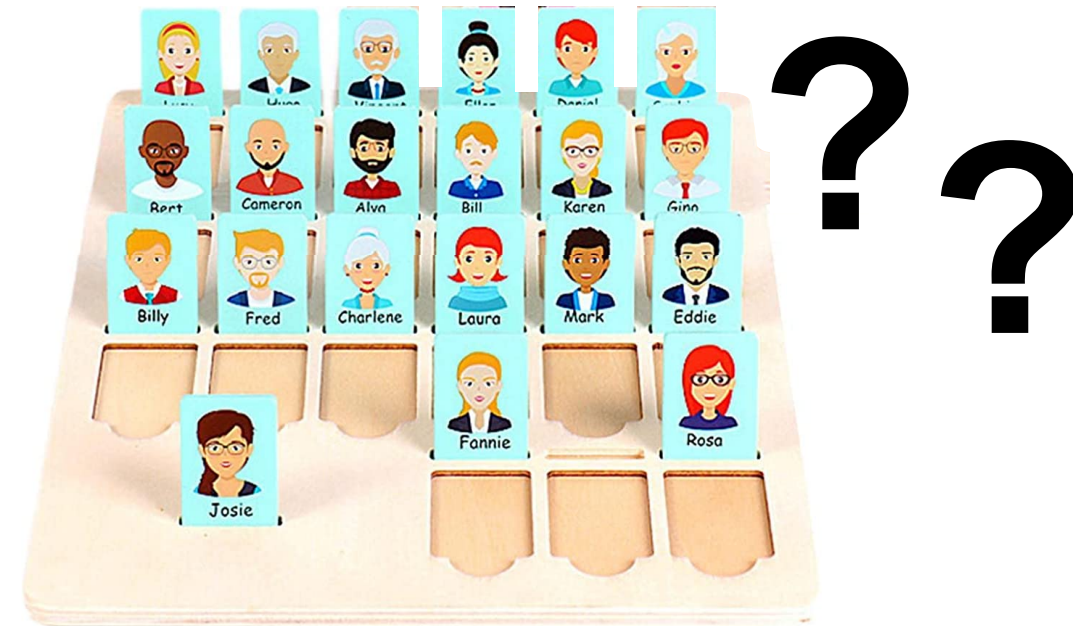


$$\frac{1 \text{ signal event} / (3 \text{ hour})}{1 \text{ billion collisions} / \text{ second}} = 10^{-13} \frac{\text{signal}}{\text{background}}$$



140 million people in **Germany** + **Italy**

100,000 hairs / person



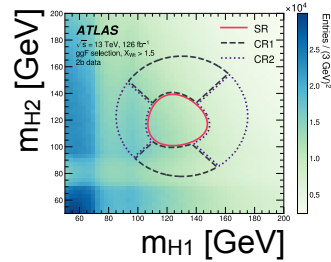
Rate mal wer ich bin??
Indovina Chi?

Examples of reweighting for backgrounds

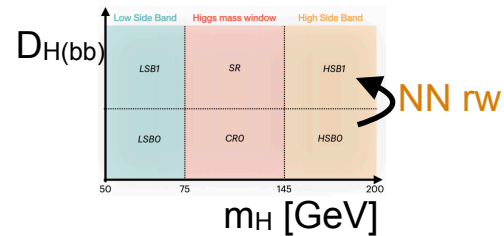
NN

Low \rightarrow
high b-tag

HH \rightarrow 4b
NR [2301.03212](#)
resonant [2202.07288](#)

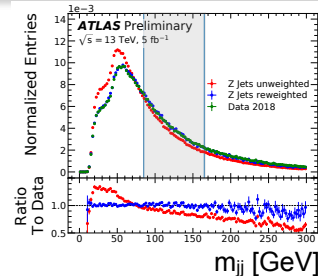


Y \rightarrow XH [2306.03637](#)
Anomalous jets analysis



MC \rightarrow data

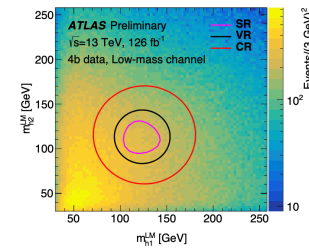
gg tagger
Match MC \rightarrow data
[ATL-PHYS-PUB-2021-027](#)



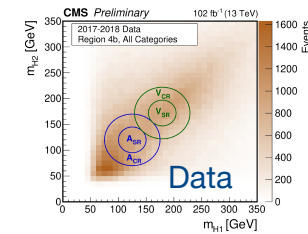
SALAD for CWoLA
Simulation Assisted Likelihood-free Anomaly Detection
MC \rightarrow data rw in sideband
[ATL-COM-PHYS-2023-452](#)

BDT

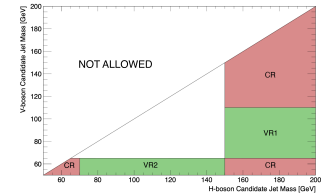
HH4b + MET
[1806.04030](#) and
[ATLAS-CONF-2023-048](#)



CMS HH4b NR
[2202.09617](#)
Higgs Pairs 2022 [talk](#)



VH(qqbb)
[2007.05293](#)



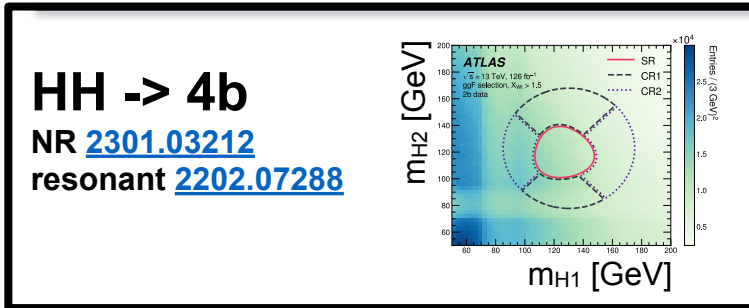
+ many others!

Q: How to quantify the uncertainty on the background model?

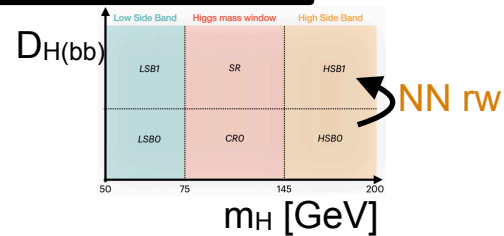
Examples of reweighting for backgrounds

NN

Low \rightarrow
high b-tag

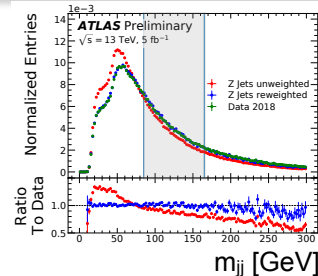


Y \rightarrow XH [2306.03637](#)
Anomalous jets analysis



MC \rightarrow data

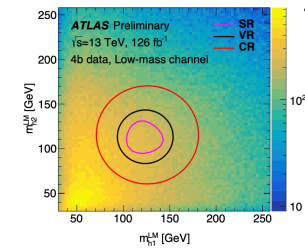
gg tagger
Match MC \rightarrow data
[ATL-PHYS-PUB-2021-027](#)



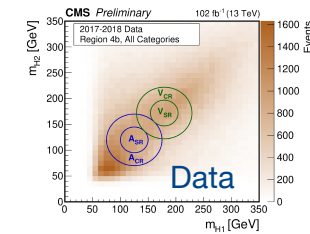
SALAD for CWoLA
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[ATL-COM-PHYS-2023-452](#)

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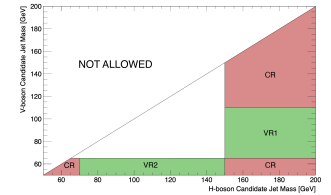
HH4b + MET
[1806.04030](#) and
[ATLAS-CONF-2023-048](#)



CMS HH4b NR
[2202.09617](#)
Higgs Pairs 2022 [talk](#)



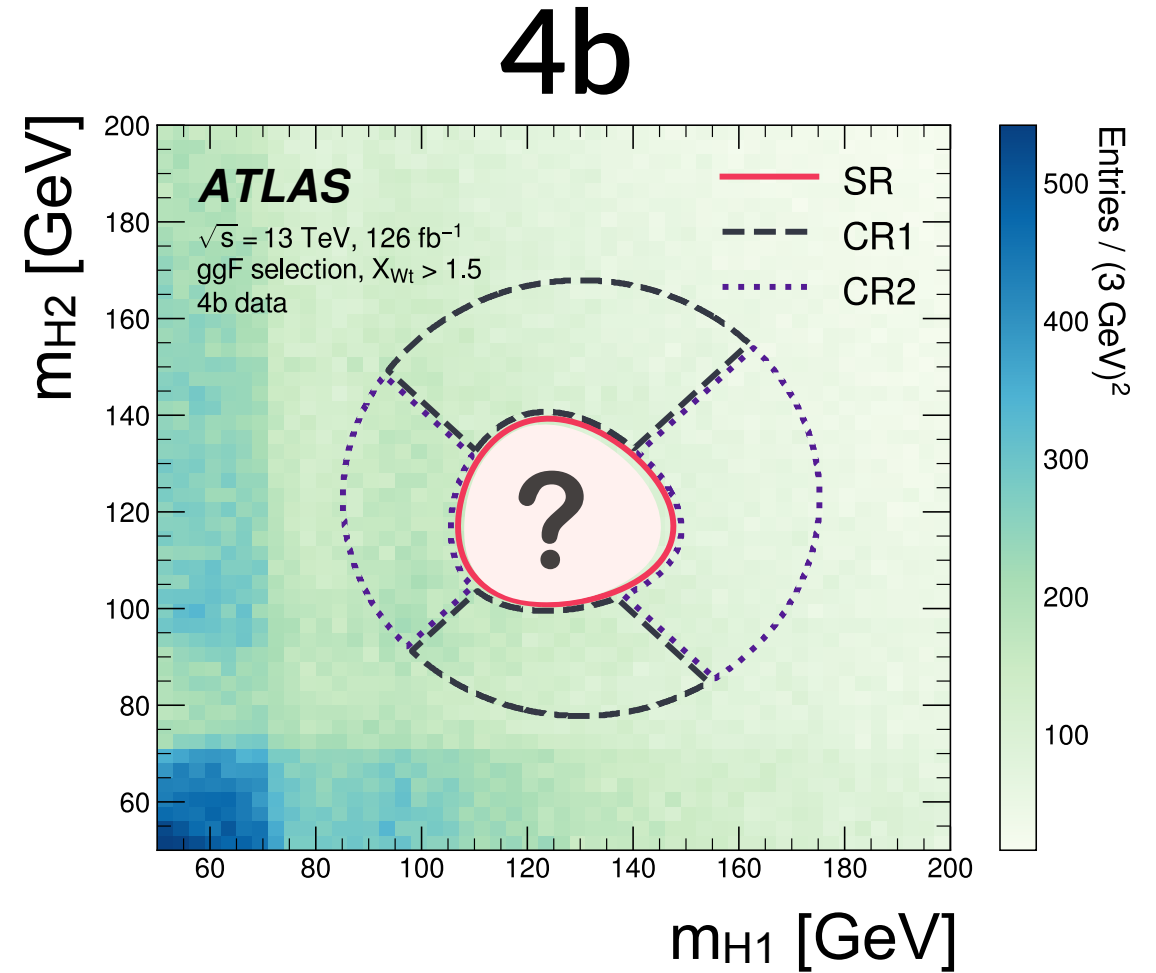
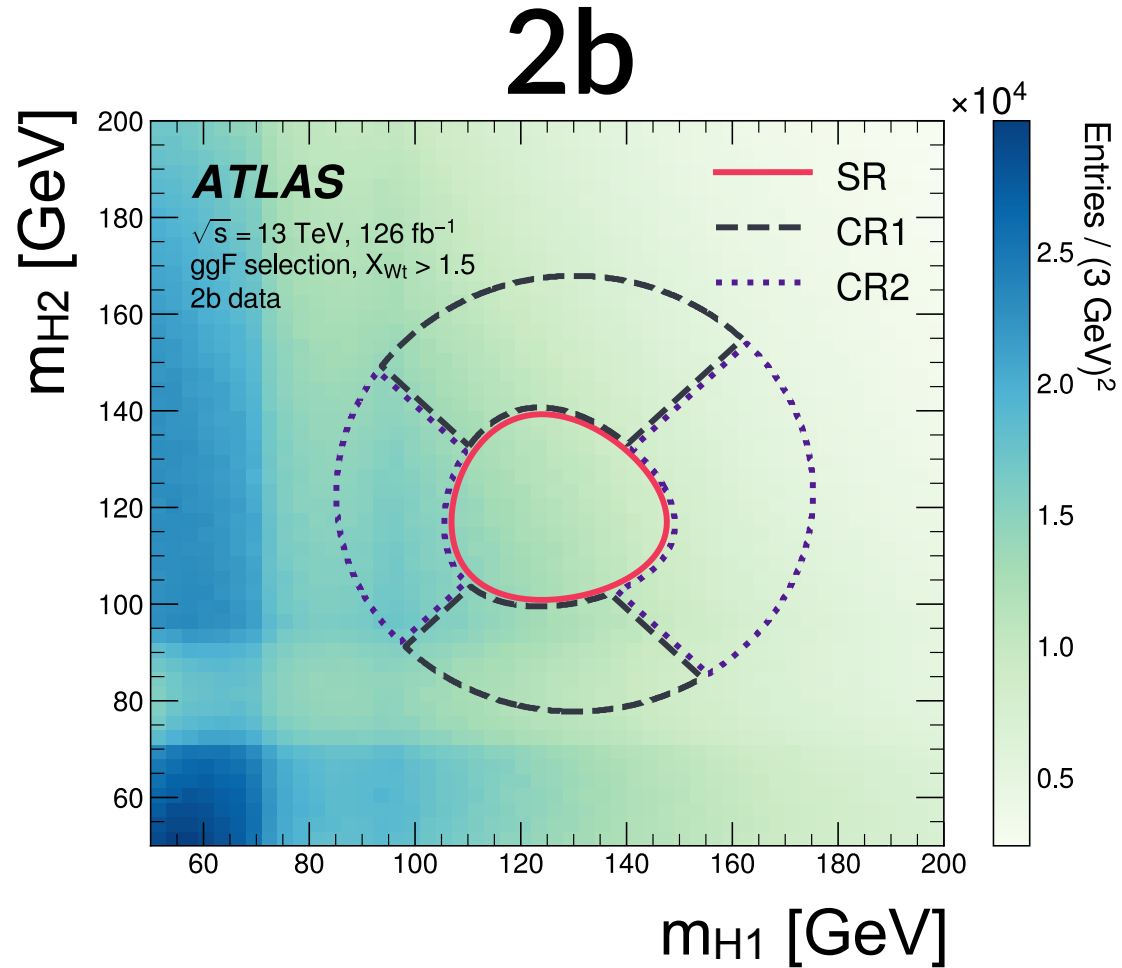
VH(qqbb)
[2007.05293](#)



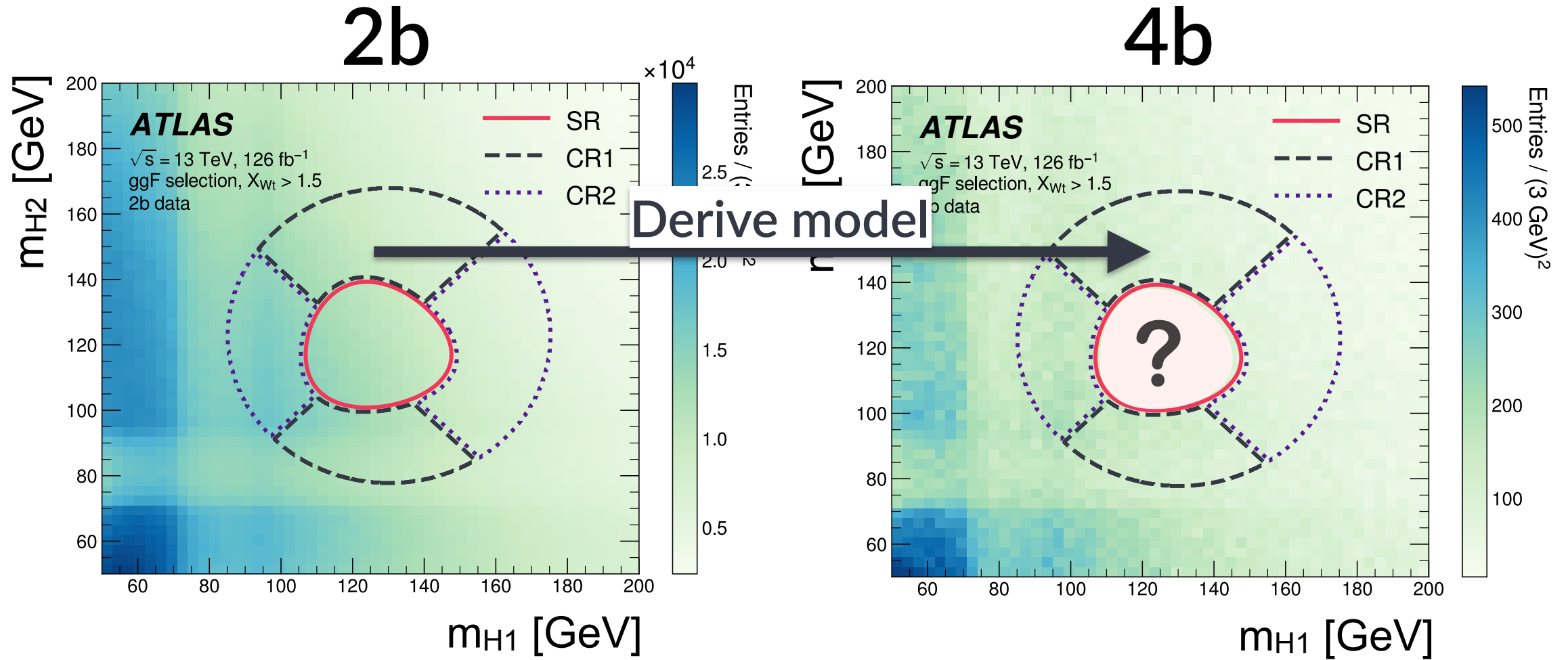
+ many others!

Q: How to quantify the uncertainty on the background model?

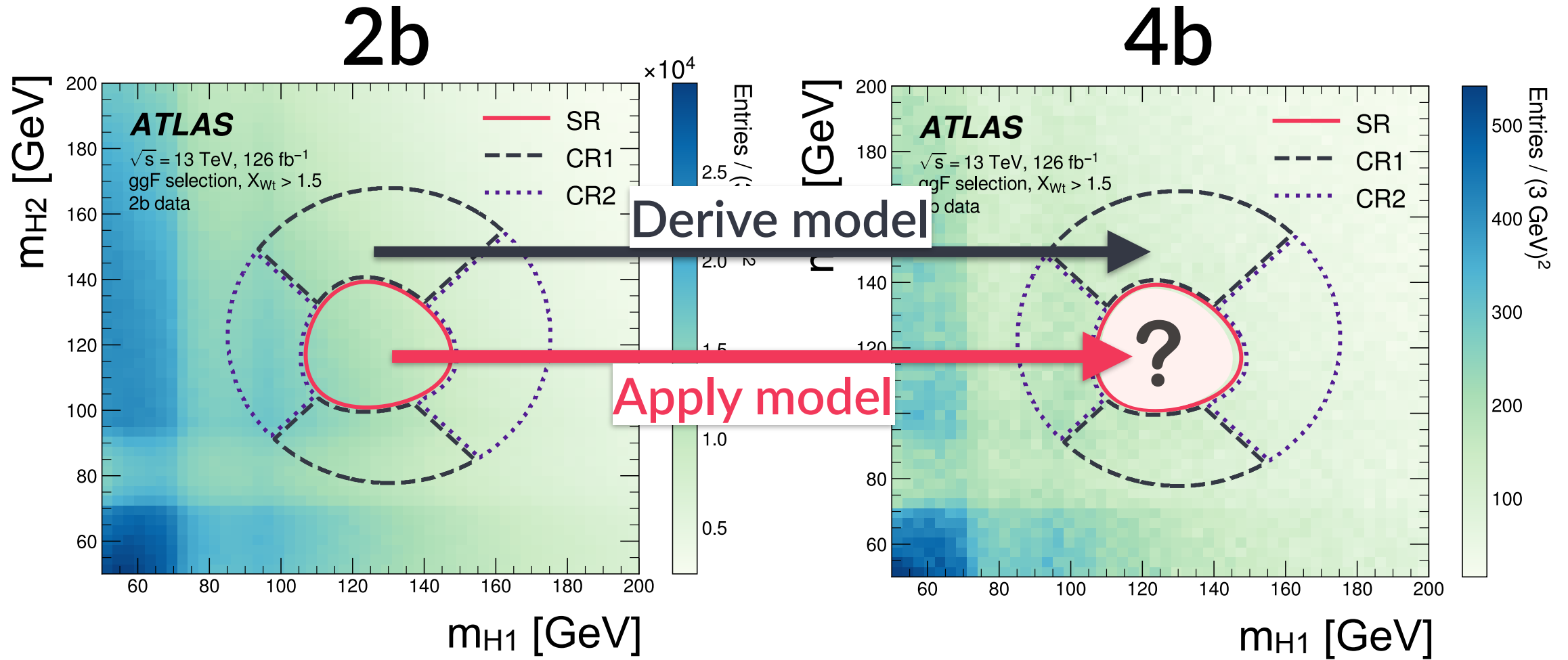
The background model



The background model



The background model



Reweighting – key idea

Multi-dimensional reweighting **2b** → **4b** .
source distribution target distribution

$$p_{4b}(x) = w(x) \cdot p_{2b}(x)$$

Want to learn

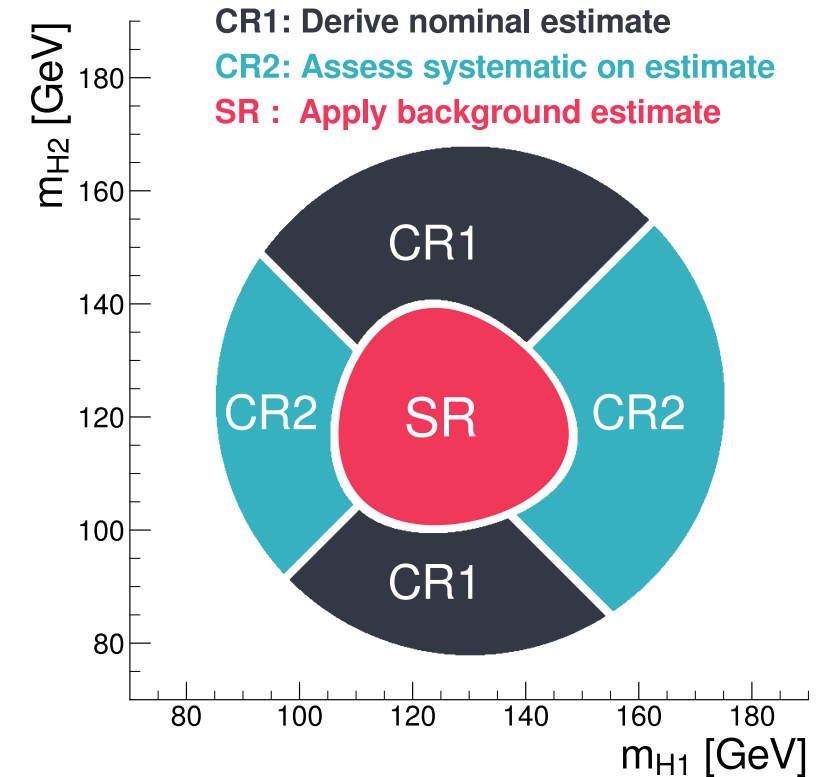
Let $Q(x)$ be a NN mapping from 2b → 4b.

$$\mathcal{L}[Q(x)] = \mathbb{E}_{x \sim p_{2b}} \left[\exp \left(\frac{Q(x)}{2} \right) \right] + \mathbb{E}_{x \sim p_{4b}} \left[\exp \left(-\frac{Q(x)}{2} \right) \right]$$

Minimize loss in **Control Region**.

$$Q^*(x) = \arg \min_Q \mathcal{L}[Q(x)] = \log \frac{p_{4b}(x)}{p_{2b}(x)}$$

$$\implies w(x) = e^{Q^*(x)}$$



Apply $w(x)$ to 2b **Signal Region** to get 4b prediction

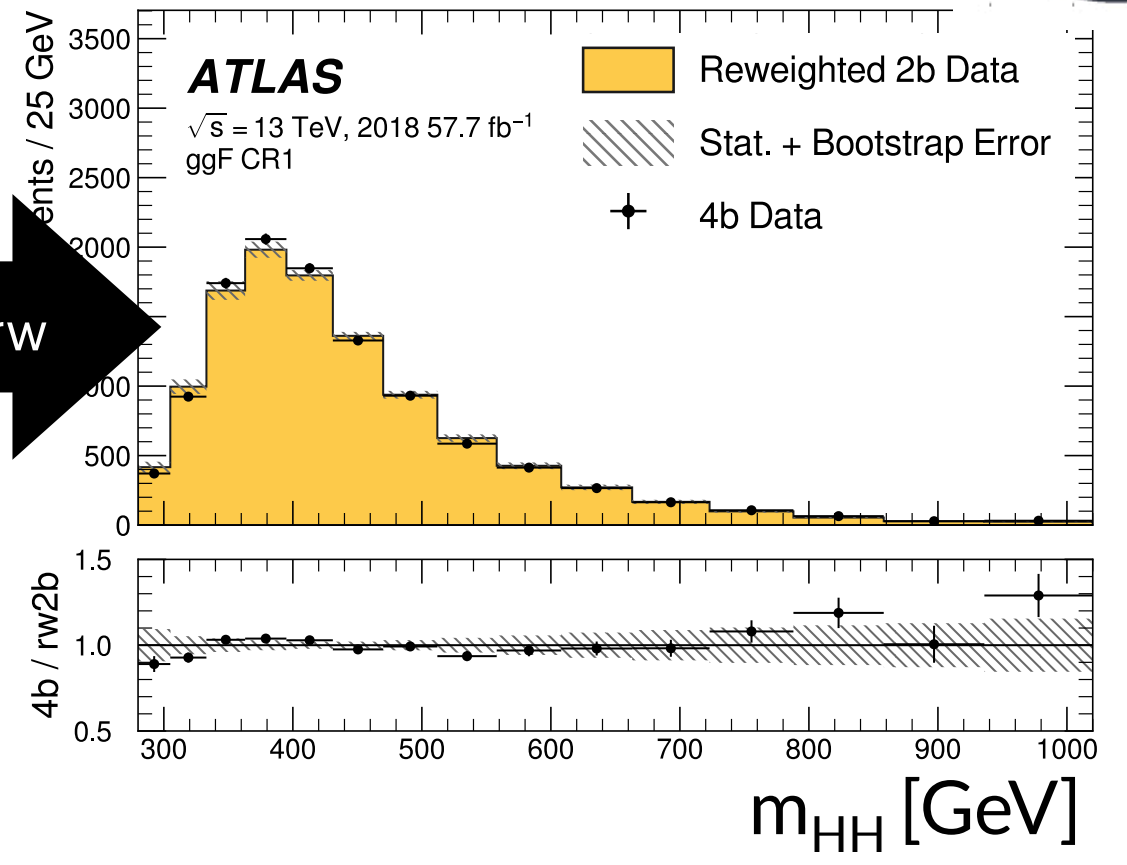
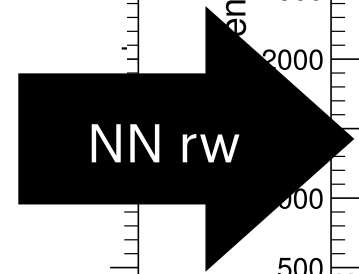
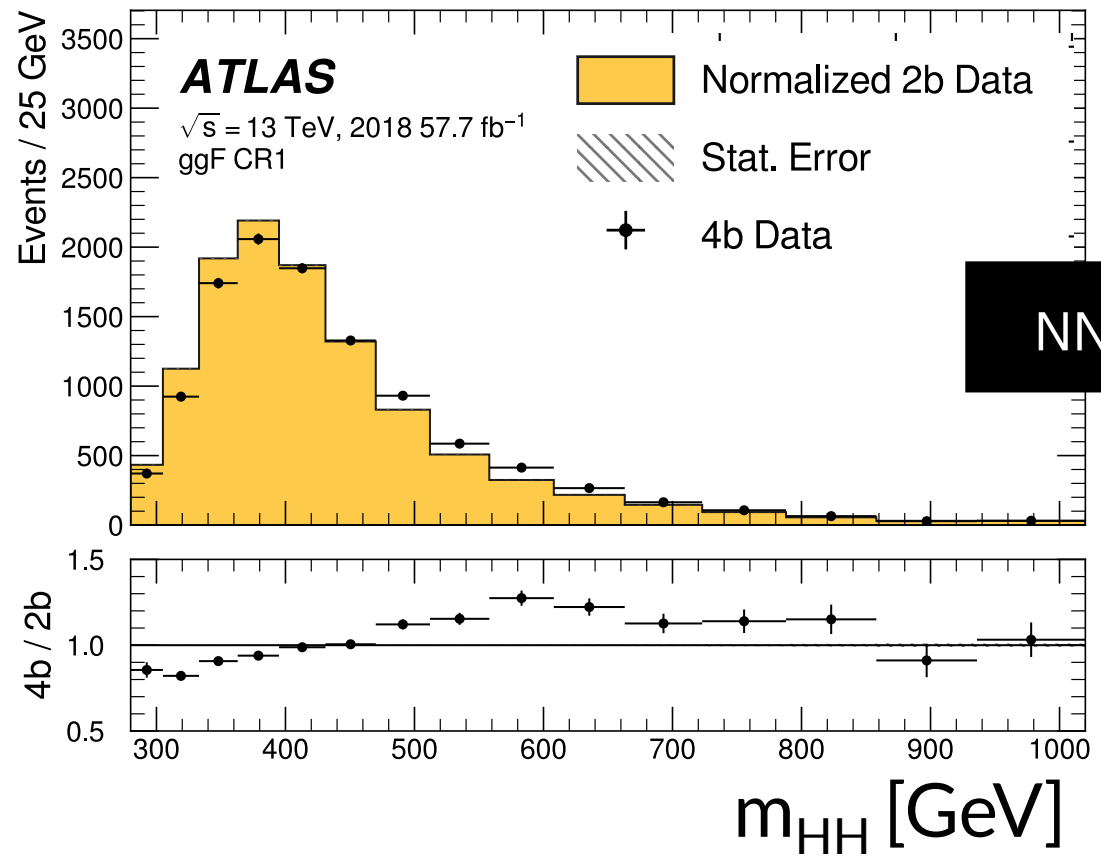
How does it work?

Closure test

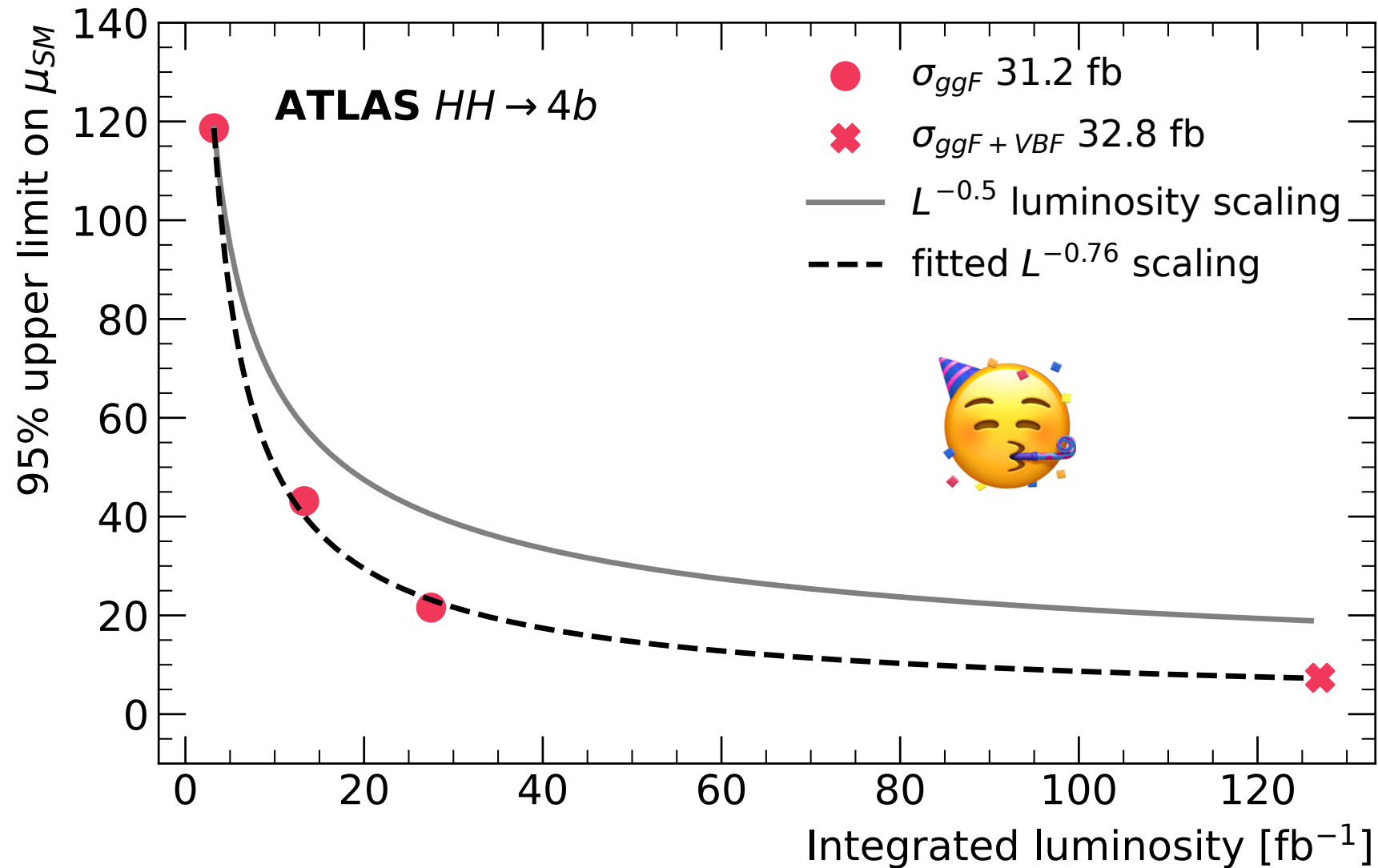


Before

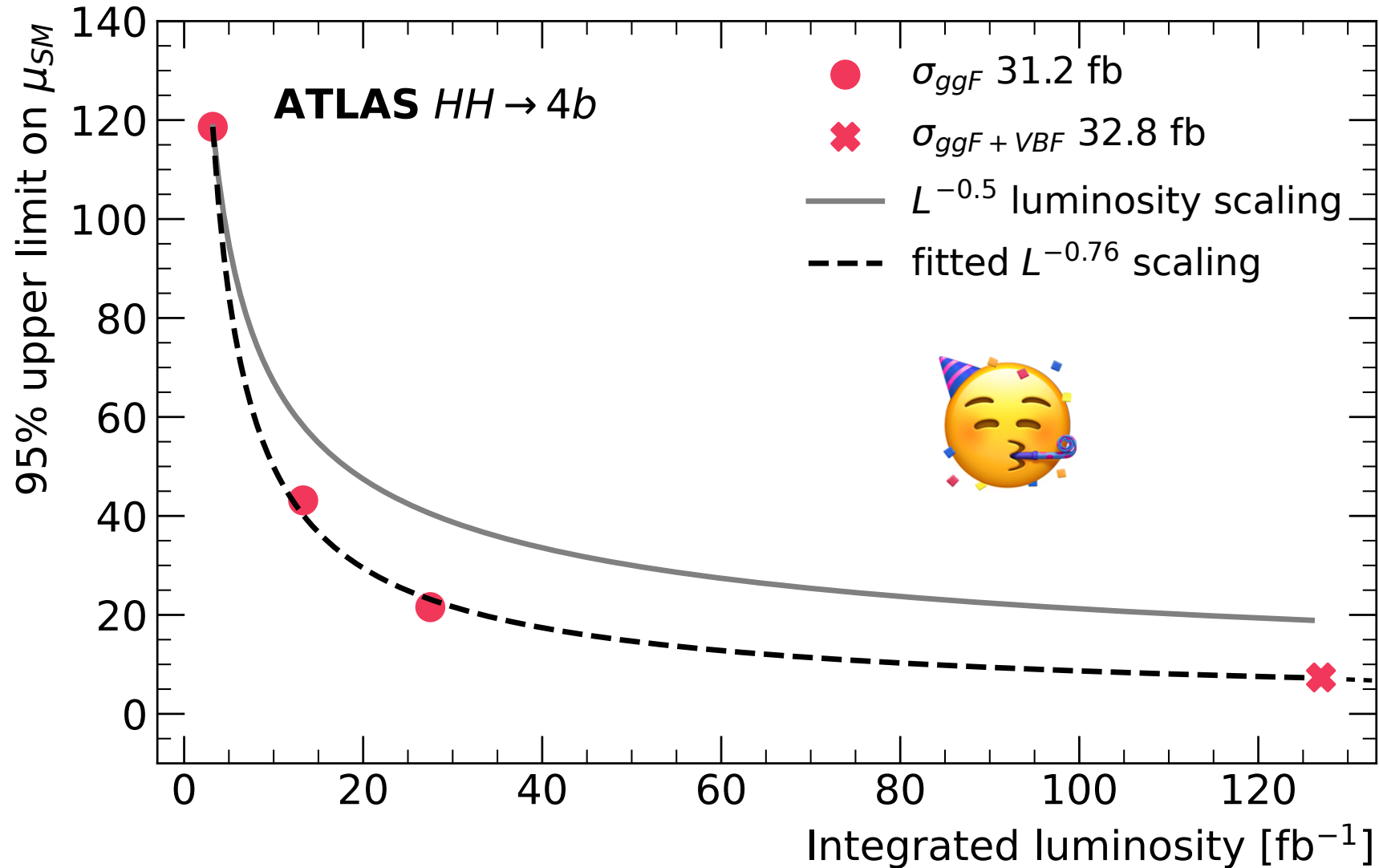
After



What's next?



What's next?

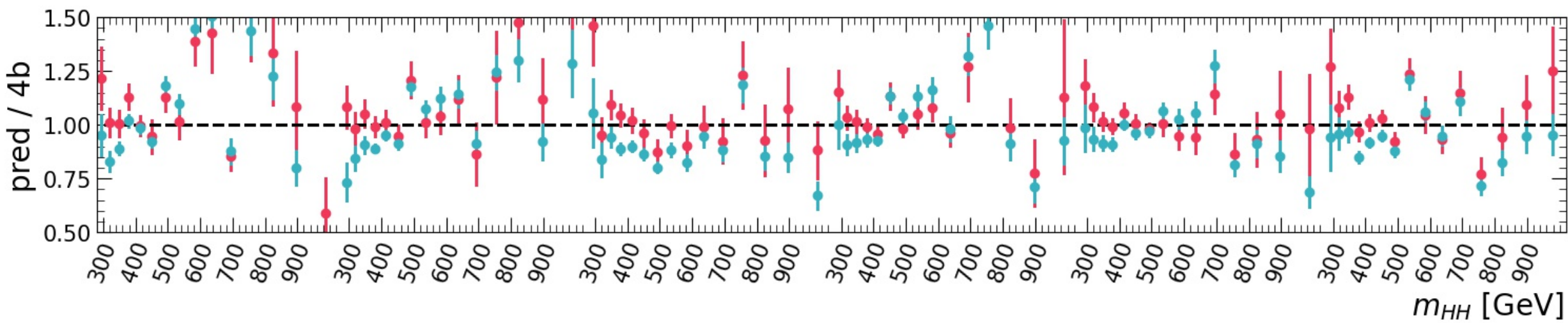
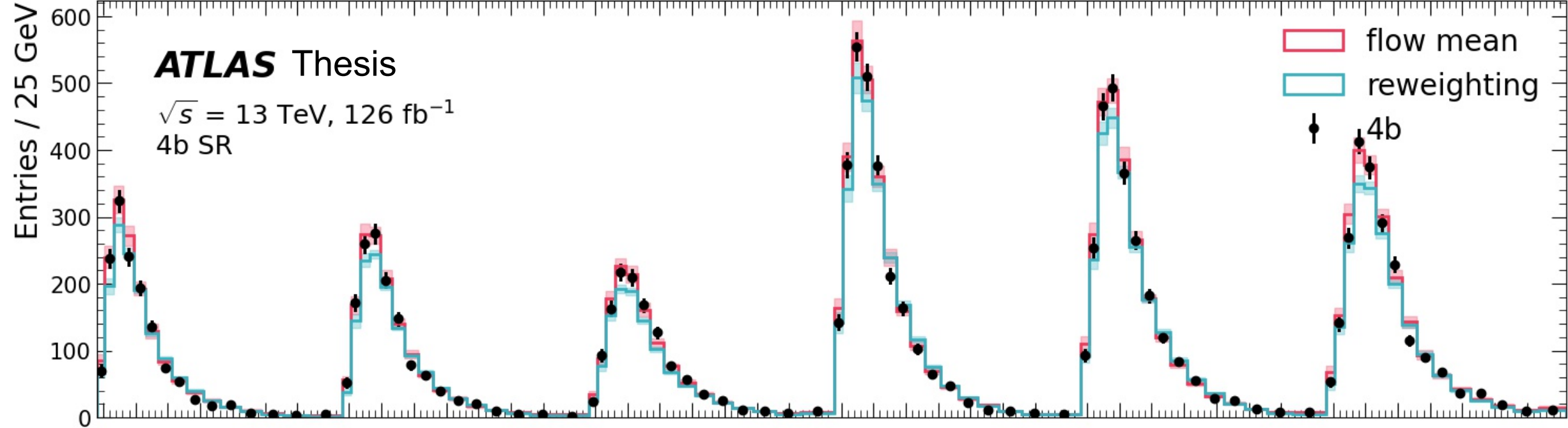


ATLAS Thesis

$\sqrt{s} = 13 \text{ TeV}, 126 \text{ fb}^{-1}$
4b SR

flow mean
reweighting

4b



$\Delta\eta_{HH} < 0.5$

$0.5 < \Delta\eta_{HH} < 1$

$1 < \Delta\eta_{HH} < 1.5$

$\Delta\eta_{HH} < 0.5$

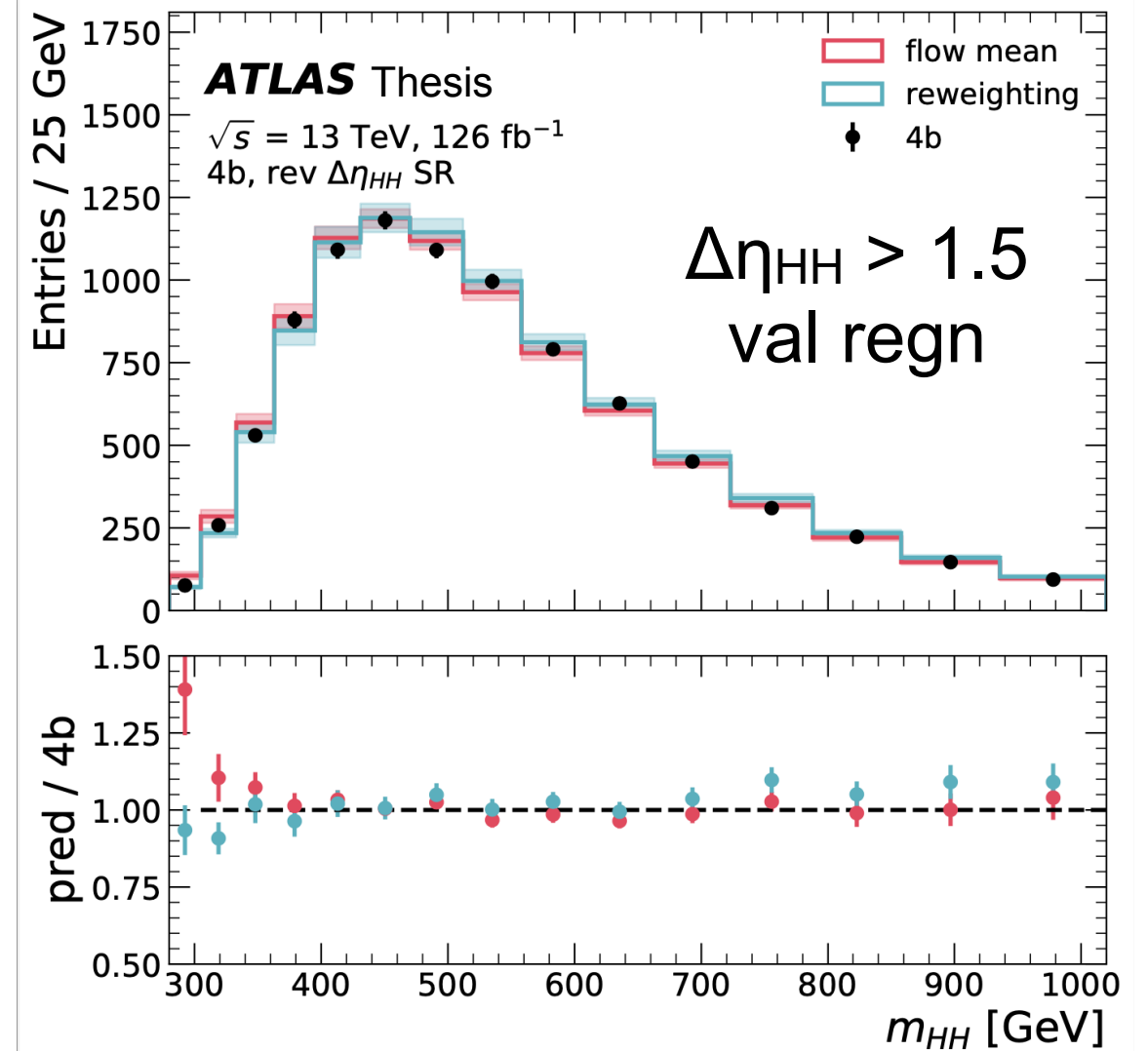
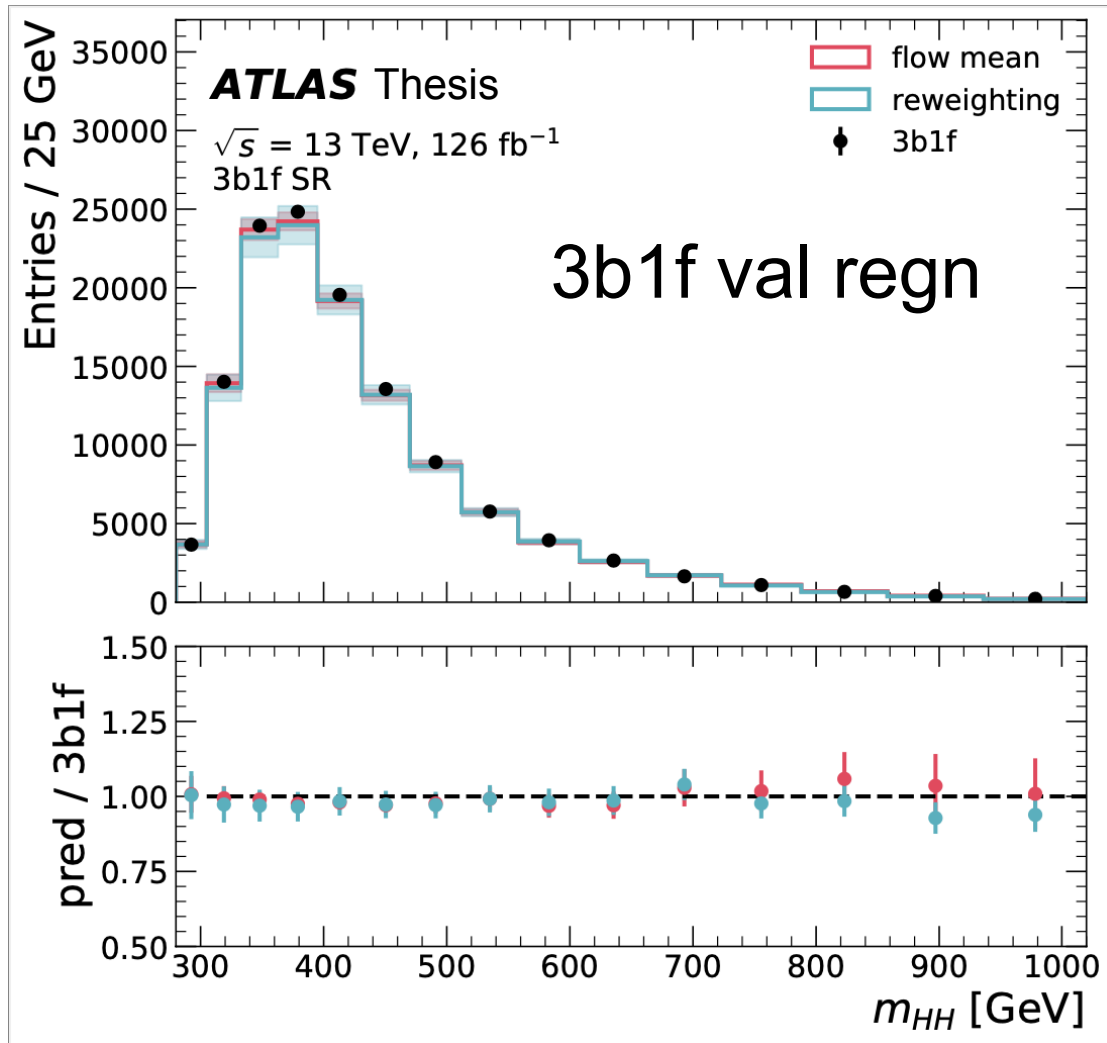
$0.5 < \Delta\eta_{HH} < 1$

$1 < \Delta\eta_{HH} < 1.5$

$X_{HH} < 0.95$

$0.95 < X_{HH} < 1.6$

3b + rev $\Delta\eta_{HH}$



Event reconstruction

1 $m_{h1}, m_{h2} \sim p(m_{h1}, m_{h2})$ [GP]

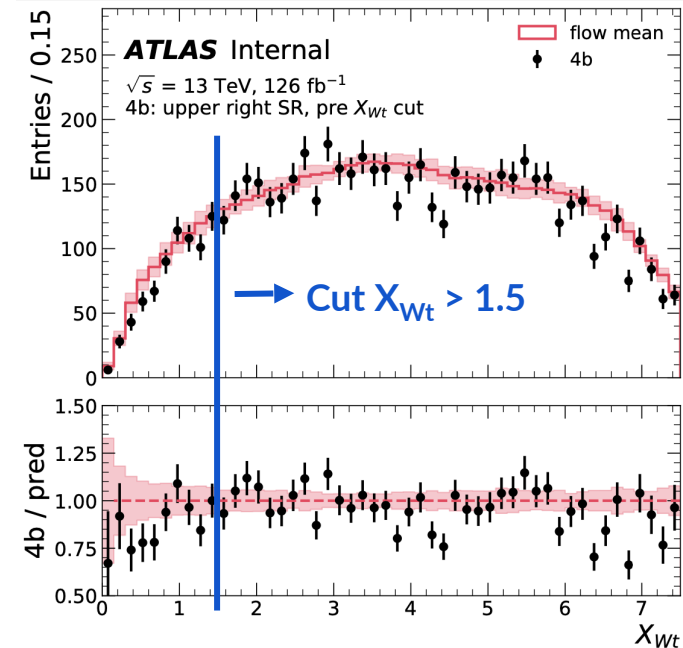
2 $\begin{bmatrix} p_{T,H1}, p_{T,H2} \\ \eta_{H1}, \eta_{H2} \\ \Delta\Phi_{HH}, X_{Wt} \end{bmatrix} \sim p(\text{evt vars} | m_{h1}, m_{h2})$ [flow]

3 Construct Higgs 4-vectors

HC 1: $(p_{T,H1}, \eta_{H1}, 0, m_{H1})$

HC 2: $(p_{T,H2}, \eta_{H2}, \Delta\Phi_{HH}, m_{H2})$

4

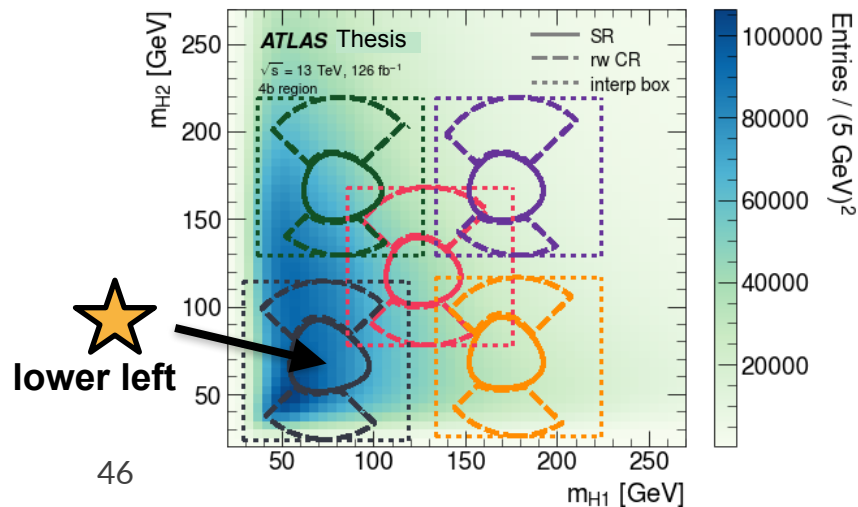


C.f. the 4b NR bkg validation regions

Compare the observed and predicted yields

	obs	rw	flow	1 - rw / obs [%]	1 - flow / obs [%]
3b1f	180044	175817.9	175416.8	2.3	2.6
rev $ \Delta\eta_{HH} $	16113	16462.7	16185.9	-2.2	-0.5
lower left	40578	48708.9	39252.2	-20.0	3.3
lower right	12377	14648.5	11982.7	-18.4	3.2
upper right	5751	5543.0	5825.9	3.6	-1.3
upper left	19075	19504.7	19833.4	-2.3	-4.0
4b	16171	15423.7	16564.8	4.6	-2.4

shifted regions



Shape modelling

Normalize histograms to the target, and compare shapes

reweighting better
GP+flow better

shifted regions

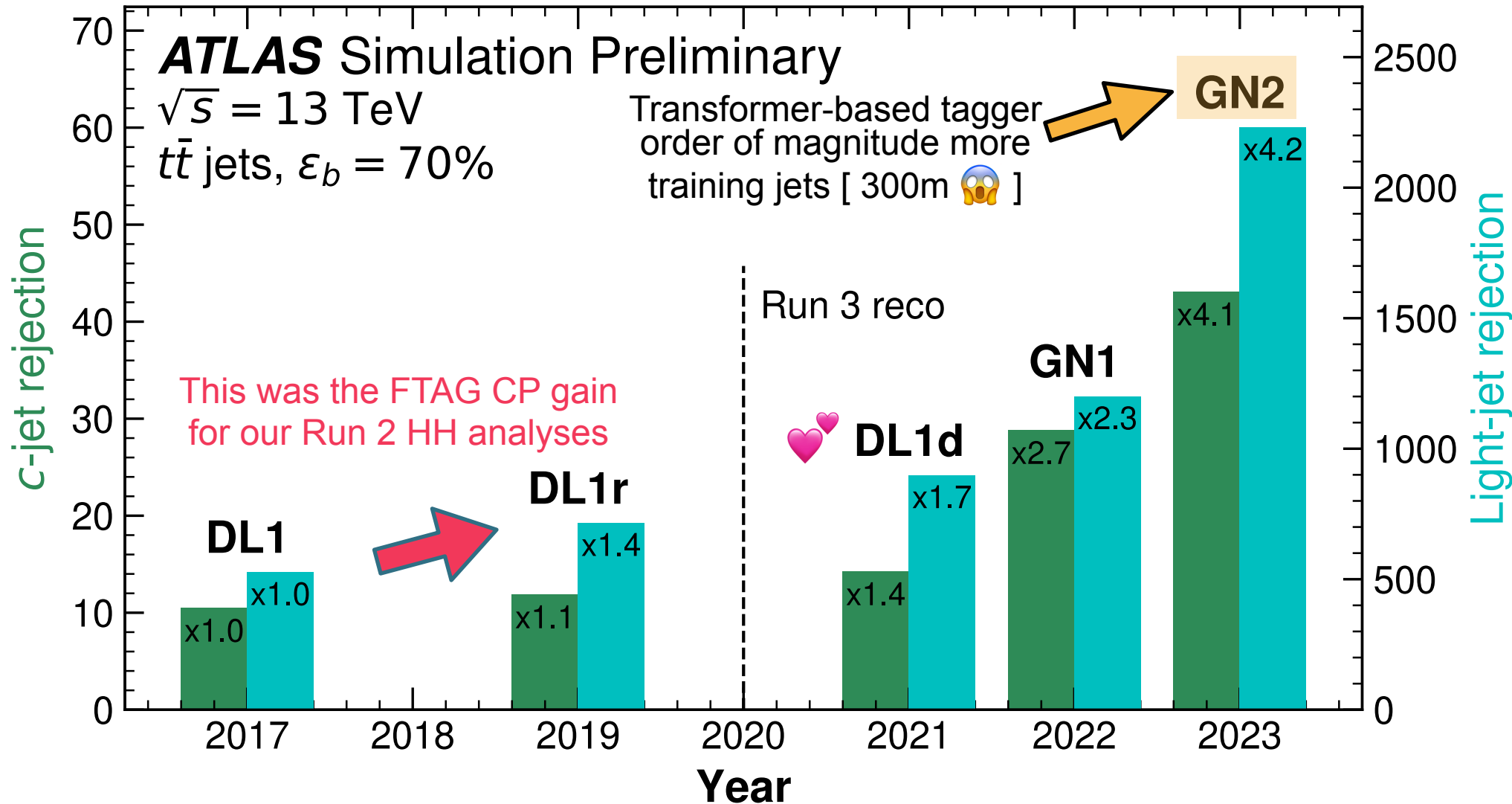
	3b1f		rev $ \Delta\eta_{HH} $		lower left		lower right		upper right		upper left	
	rw	flow	rw	flow	rw	flow	rw	flow	rw	flow	rw	flow
3d disc	1.85	2.24	1.37	1.25	5.52	2.19	1.32	0.98	1.35	0.93	2.54	1.60
m_{HH}	2.29	3.77	1.34	1.60	2.70	1.98	1.26	0.78	1.30	0.91	4.44	4.70
$m_{HH,cor2}$	2.21	3.81	1.63	2.34	8.26	2.21	1.61	1.03	1.97	1.64	2.85	4.49
$\Delta\eta_{HH}$	1.38	1.94	1.16	3.90	6.95	1.37	1.52	1.07	1.51	1.63	1.99	0.98
$p_{T,H1}$	1.61	1.58	1.42	1.48	1.76	0.95	0.70	0.58	1.07	1.14	2.85	1.77
$p_{T,H2}$	2.64	2.50	1.74	1.51	2.81	1.83	2.83	1.17	1.82	1.06	0.92	1.49
η_{H1}	1.99	2.07	2.74	1.51	2.33	1.54	2.24	0.87	1.45	0.82	2.36	1.74
η_{H2}	1.37	1.36	2.07	1.17	2.62	1.35	4.93	1.11	0.85	0.75	1.33	1.16
$\Delta\phi_{HH}$	1.88	1.85	2.08	1.16	9.64	1.46	18.81	1.04	3.23	2.61	2.24	1.40
X_{Wt}	2.49	3.73	1.74	1.71	17.64	1.27	5.29	0.79	1.39	1.45	1.33	0.82
$p_{T,HH}$	2.54	0.93	2.35	0.87	6.06	1.13	1.76	1.00	1.50	1.23	1.80	0.80

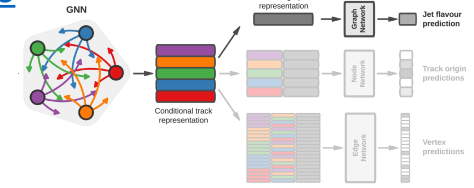
GP fitted length scales

	m_{H1} [GeV]	m_{H2} [GeV]
2016	108.3	50.6
2017	106.1	64.4
2018	105.4	56.4

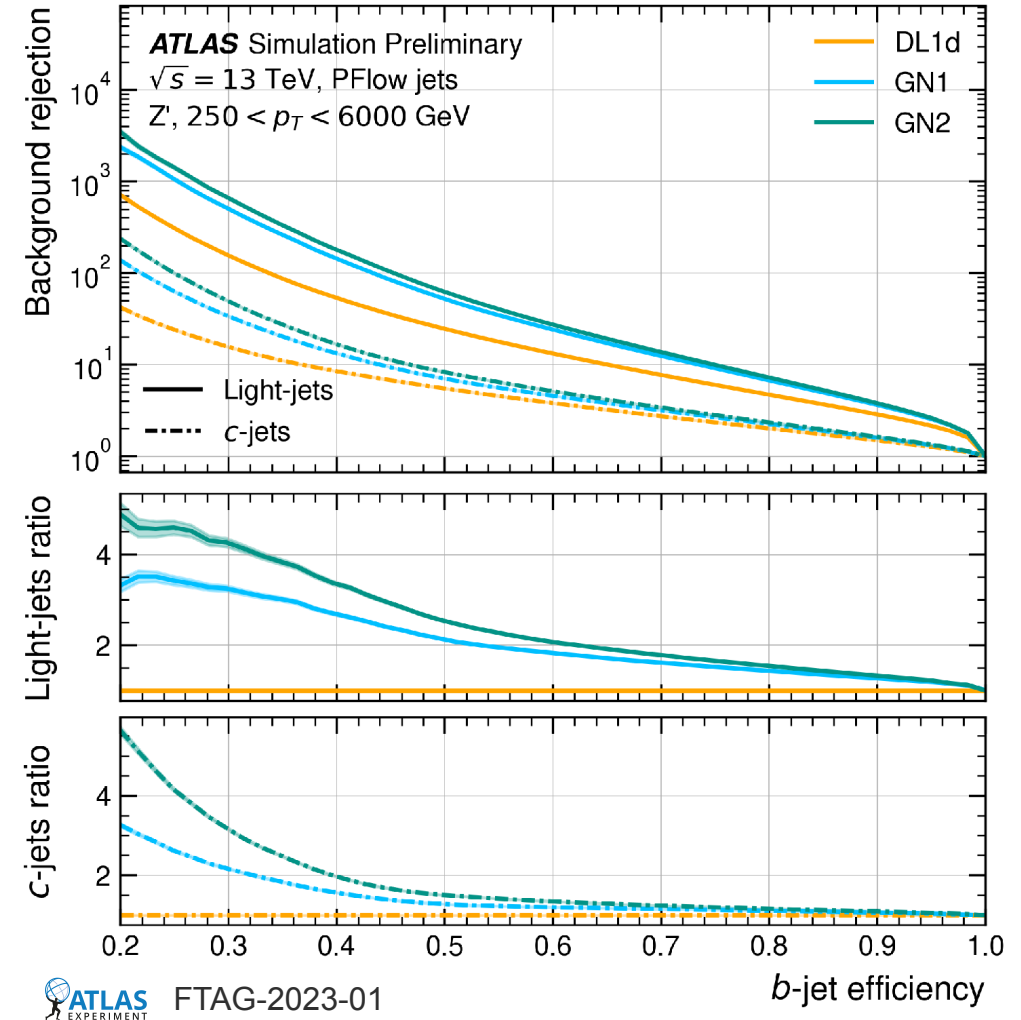
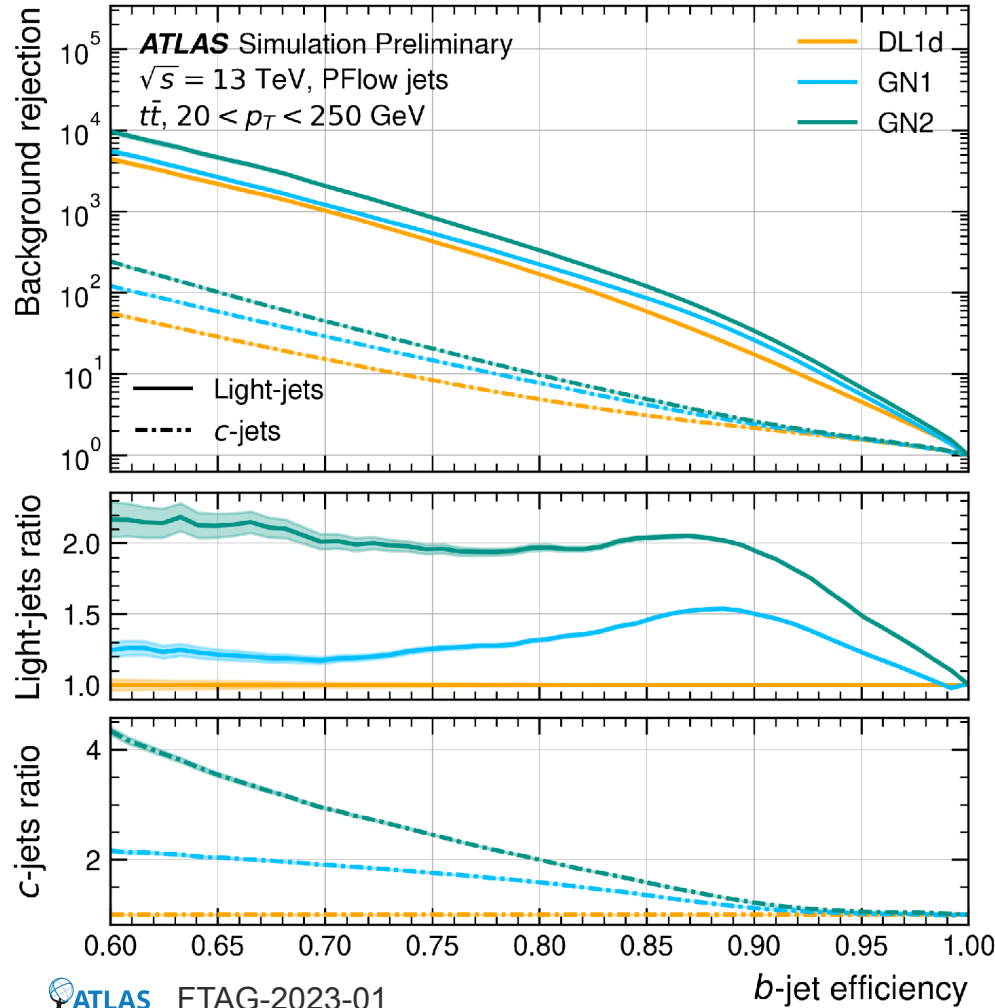
Table 13.1: The fitted length scales for 4b data.

GN2v01





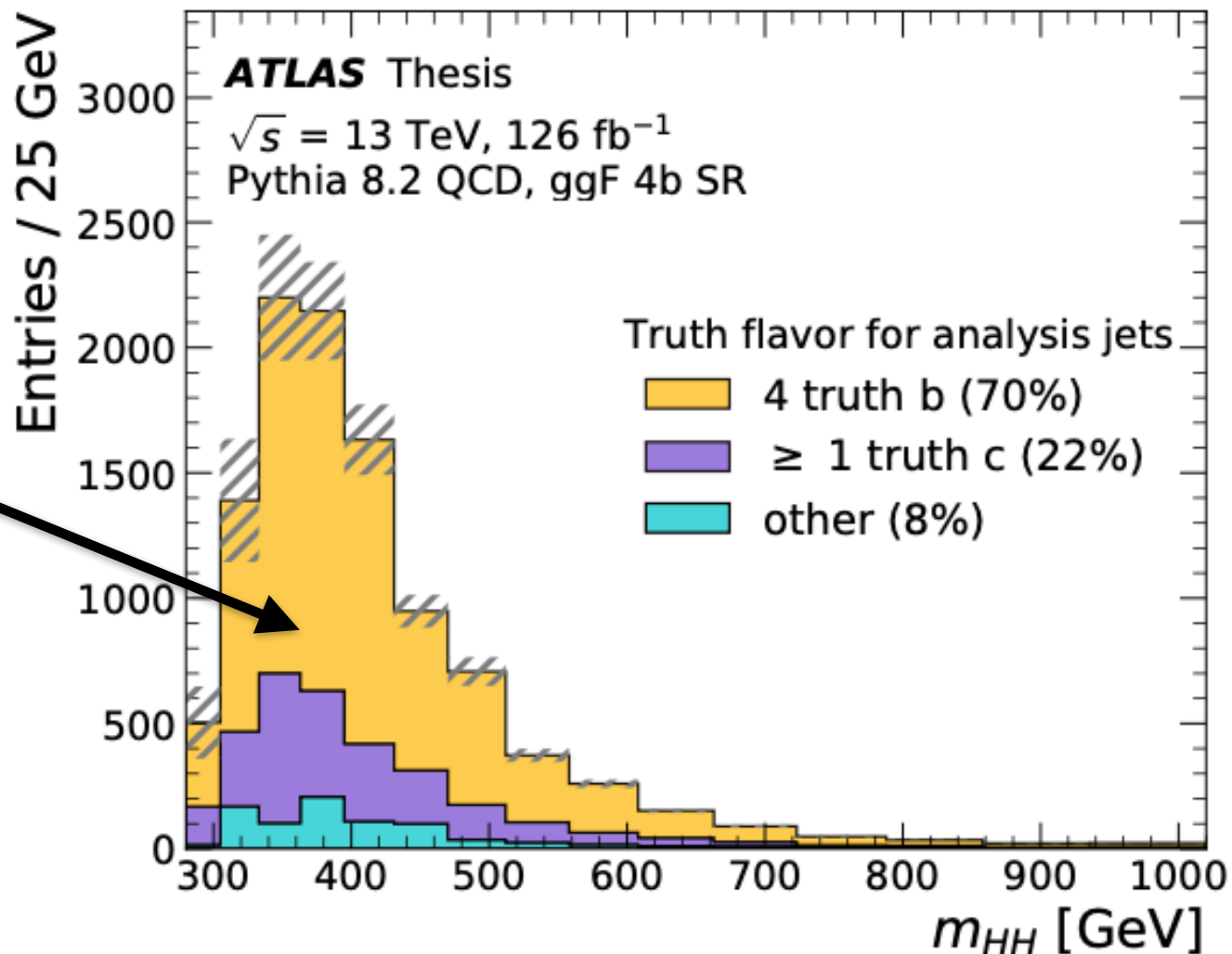
GN2 b-tagging performance



How can we learn more?

70% of our background is *irreducible* at this point (actual 4b events)

Can we leverage event level information to elucidate more signal?

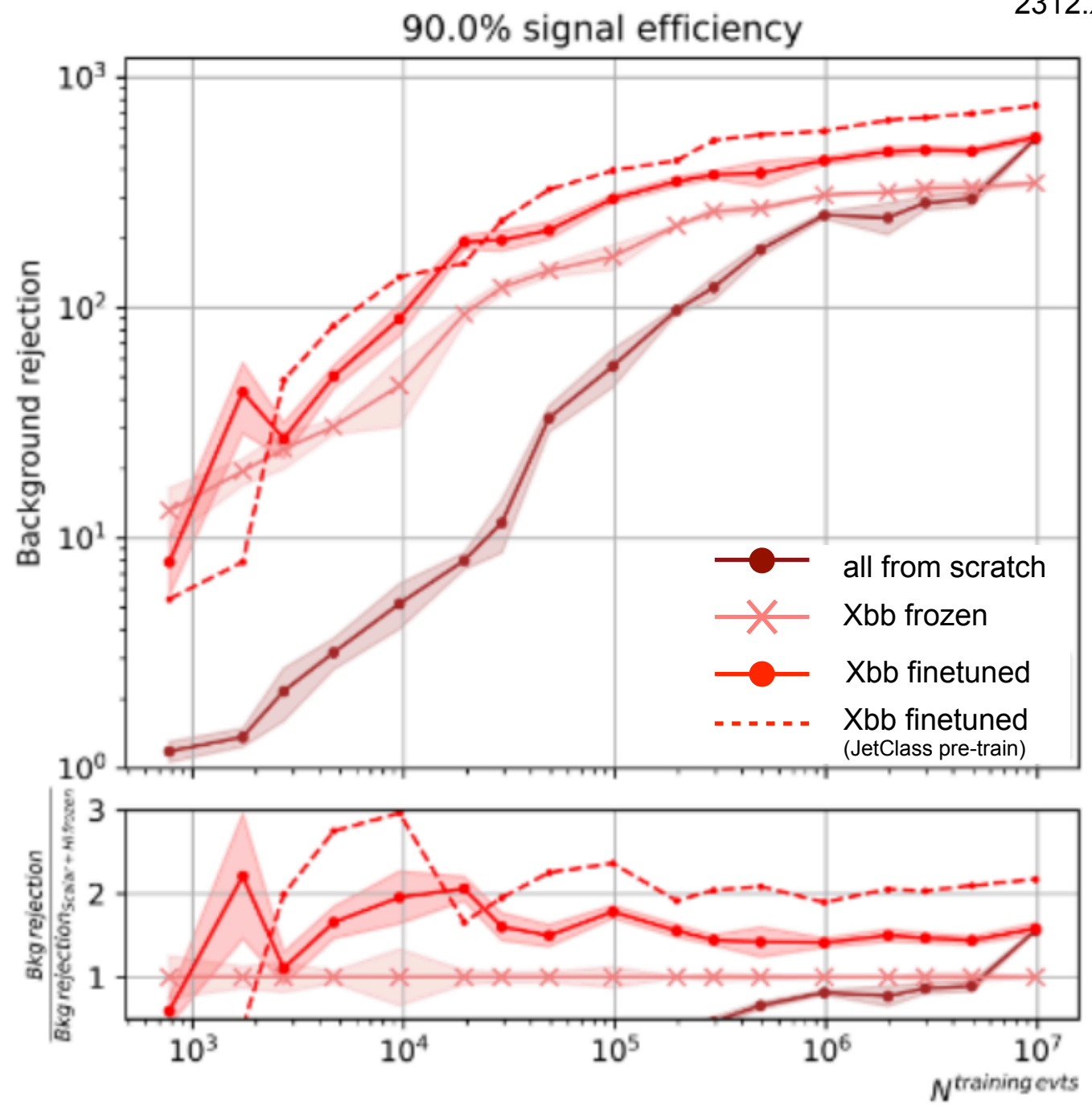


Data efficiency

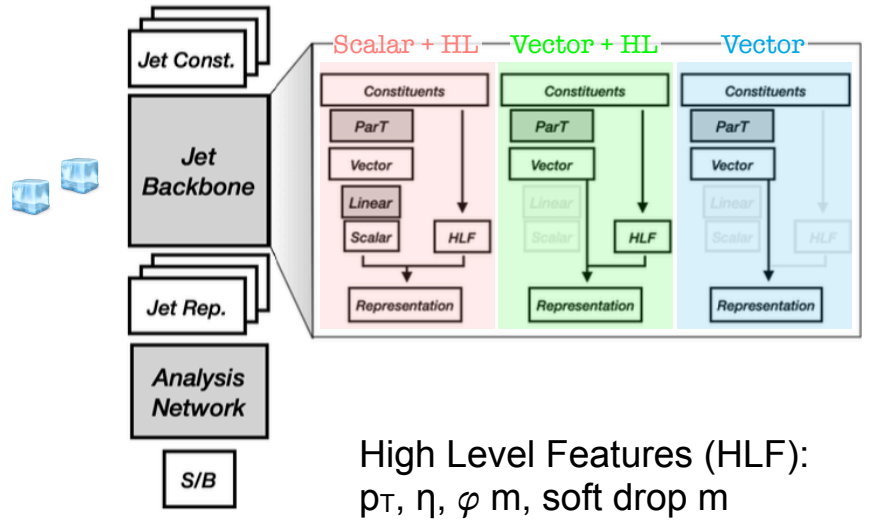
When you train the whole thing from scratch (all on the 10m jets CMS dataset), you eventually get the same level of performance as the finetuned model.

The frozen Xbb score is consistently worse than the finetuned model.

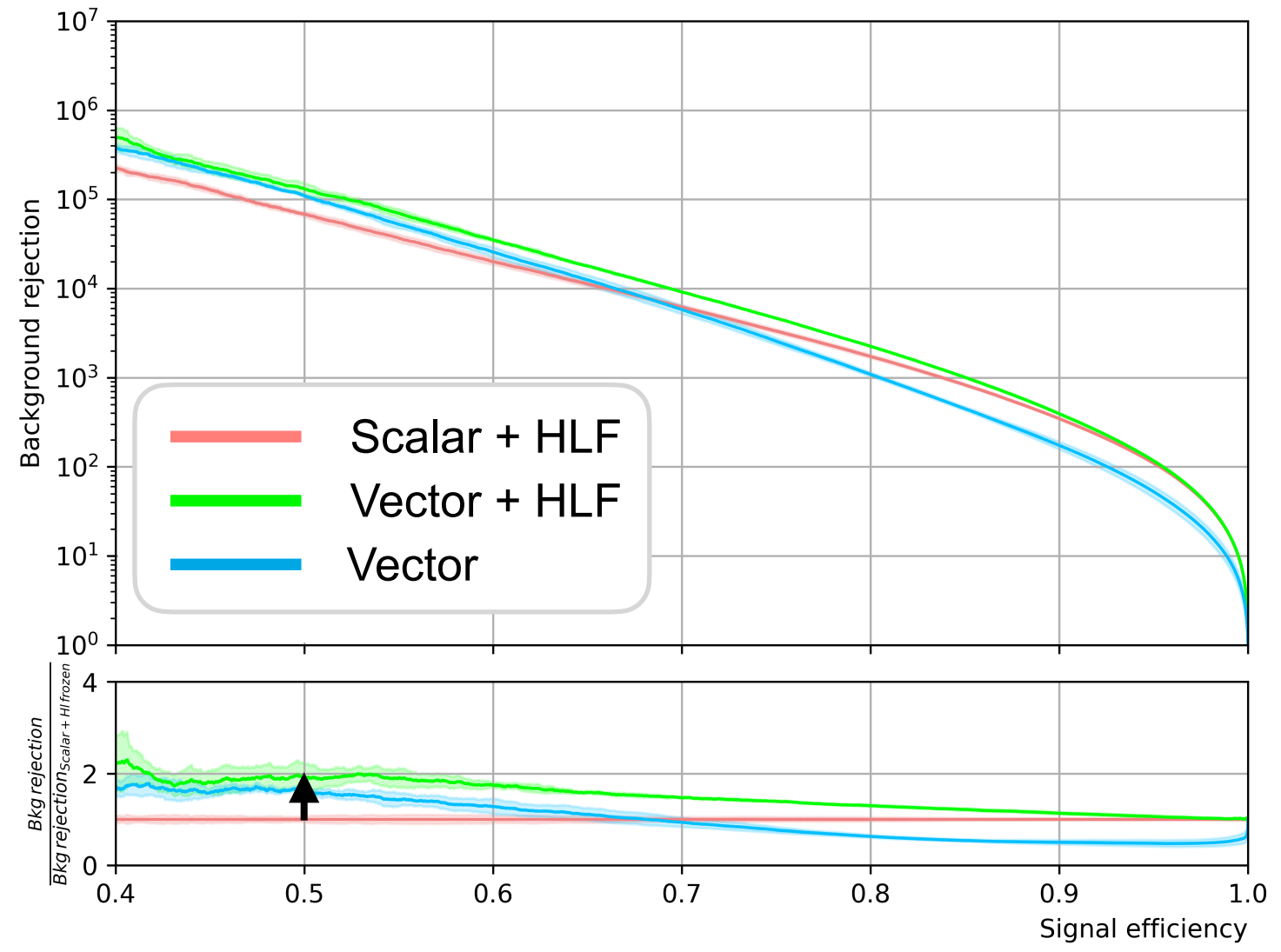
The fine-tuning with pretraining has the best performance once you have more than 10k jets to fine-tune the model on.



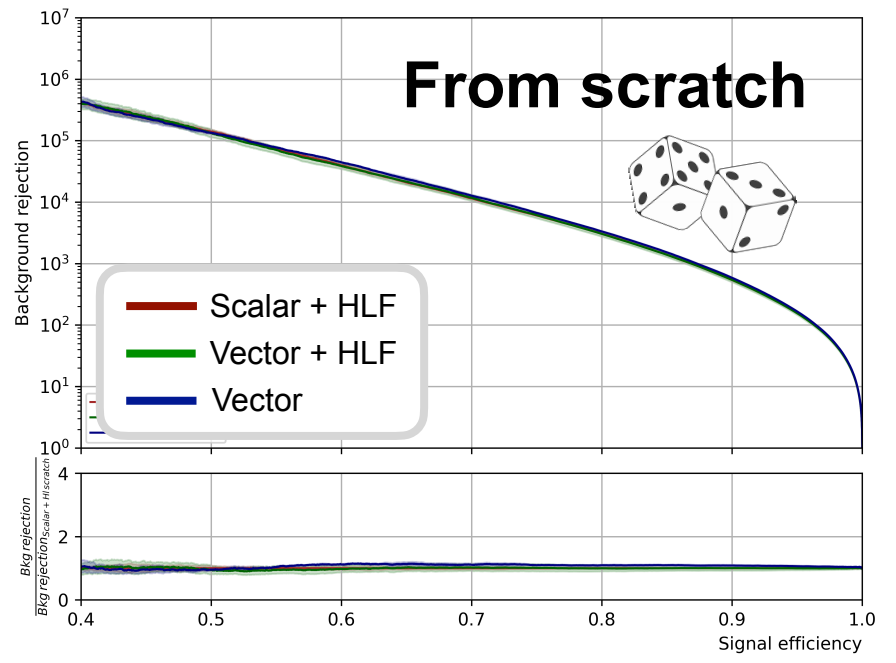
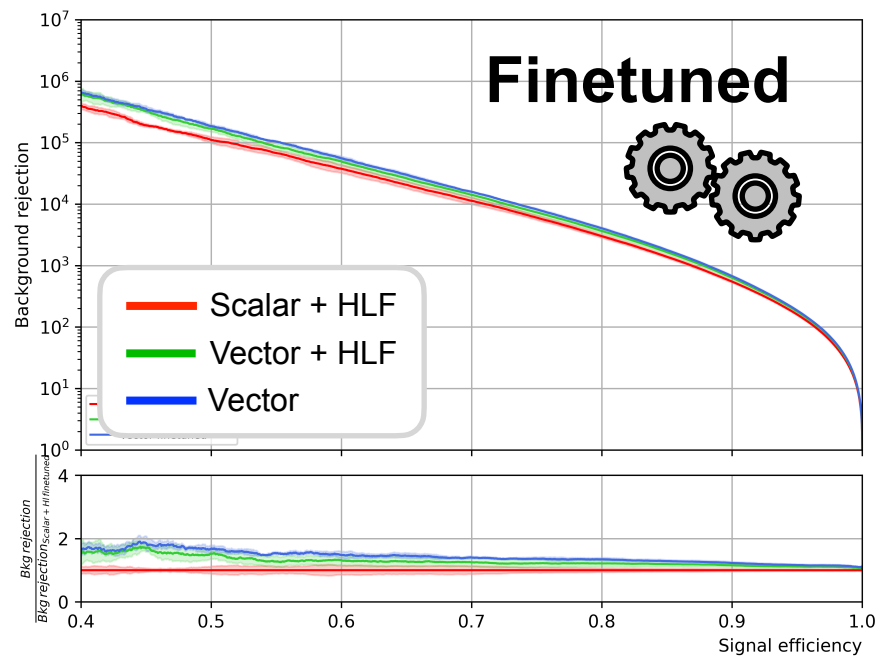
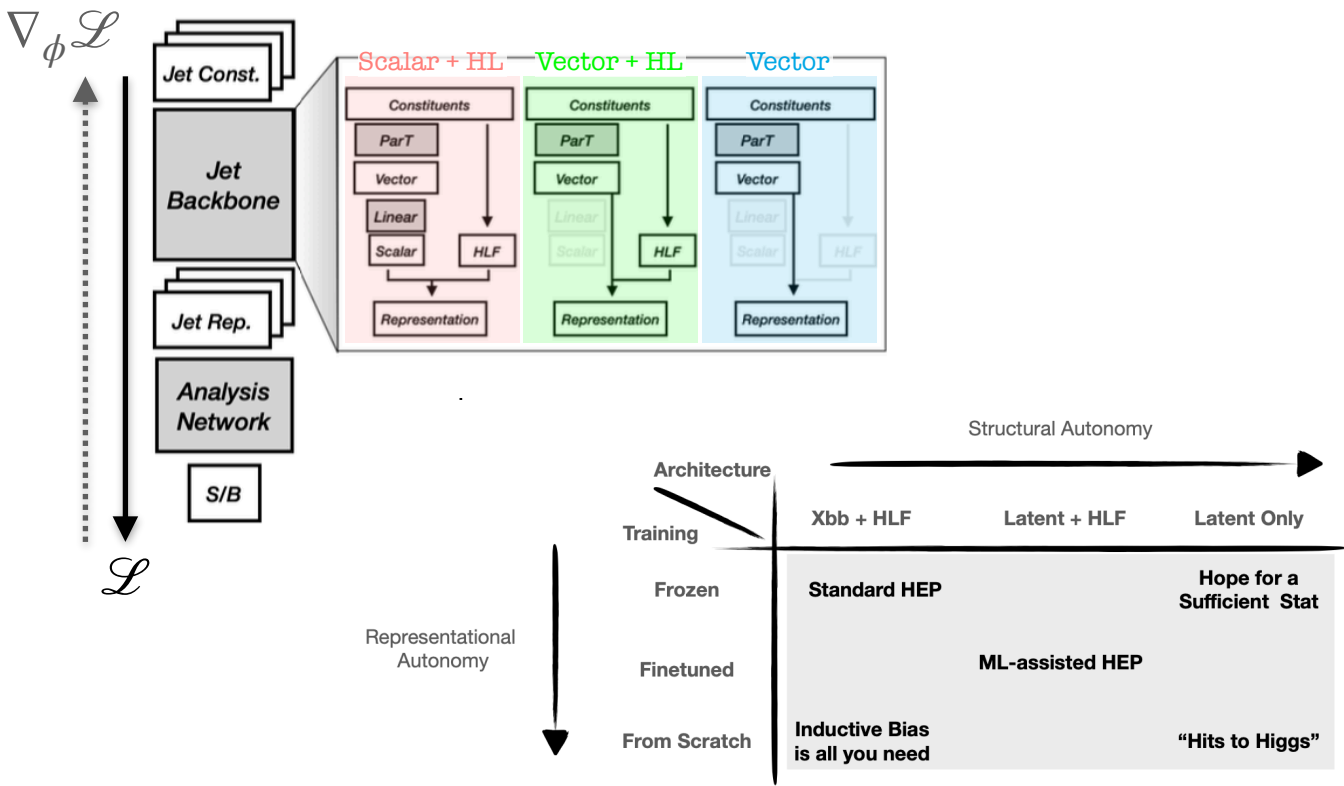
Utility of higher dimensional representation



If the jet level representation is frozen, **vector** performs better than single **scalar**



And with the gradient flow?



With a finetuned model, some benefit from vector info.
 In the from scratch phase, *no benefit from the additional information.*