Results and Perspectives on the Muon g-2 Experiment at Fermilab

Marco Incagli, INFN-Pisa **CERN** seminar 5 September 2023

A Muon g-2 storm seems

to be brewing

What is *"g-2"*?

$$\vec{\mu}_p = -g_p \frac{e}{2m_p} \vec{S}$$

 $a_p = \frac{g_p - 2}{2}$

- *g_P*: proportionality constant between spin and magnetic moment for particle P
- *a_P* : magnetic anomaly
- *a_P* = 0 at tree level (*purely Dirac particle*)
- Using modern language, the term (g-2)/2 reflects the magnitude of the Feynmann diagrams beyond leading order





- QED dominates the value itself
- Uncertainty is dominated by QCD, in particular by the Hadronic Vacuum Polarization (HVP) term
- SM values taken from the Muon g-2 Theory Initiative
- Last compilation in **2020**:

White Paper: Phys. Rept. 887 (2020) 1-166 https://doi.org/10.1016/j.physrep.2020.07.006

https://muon-gm2-theory.illinois.edu/

HVP Calculation: Dispersive (e+e⁻) Method

$$a_m^{HLO} = \frac{1}{4\rho^3} \int_{4m_\rho^2}^{\infty} S_{e^+e^- \to hadr}(s) K(s) ds$$

- Kernel function: $K(s) \propto 1/s$
- Due to the 1/s term, the low energies most important





Standard Model Components of g_{μ} Dirac Equation QED Electroweak $y \in V_{\mu}$ y = 0 + 0.00116584719 + 0.0000000154 + 0.0000000092 +0.000006845)

- Everything in SM needs to be included here: but are we sensitive to some **physics beyond the SM**?
- We can compare experimental & predicted values and ask:

"Is there some New Physics in our experiment that isn't in the Standard Model?"



A rich history of g-2 Theory and Experiment

History of muon anomaly measurements and predictions



Situation before Fermilab exp.: tension between theory and experiment

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Fermilab Run-1 Result (2021)

• BNL E821 (2004) disagreed with SM prediction:



- 7th April 2021, we released our **Run-1** result
- Using only 5% of our data, we confirmed BNL value
- FNAL+BNL average stood
 4.2σ from Theory Initiative White Paper (2020)
- Today's talk is mostly about the new experimental result
- There have also been some new results from the SM prediction side of the plot...



The Fundamental Experimental Principle

• Difference between spin precession and cyclotron revolution for a muon (charged particle with spin) in a magnetic field*:

$$\omega_a = \omega_s - \omega_c = g \frac{e}{2m} B - \frac{e}{m} B = \frac{g-2}{2} \frac{e}{m} B = a_\mu \frac{e}{m} B$$

*s and p are assumed to be in a plane perpendicular to B

- simple classical calculation
- the relativistic approach provides the same result





From single muon to muon beam

• The expression is more complicated when you add in *E*-field focusing and out of plane oscillations



 The motion is very nearly planar and the momentum is very nearly the ideal one, but both effects are not perfect and require corrections

$$\vec{\omega}_a = -\frac{q}{m} \left[a_\mu \vec{B} - a_\mu \left(\frac{\gamma}{\gamma + 1} \right) (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{\mathcal{E}}}{c} \right]$$

0 if "in plane"

Term cancels at 3.094 GeV/c, the "Magic γ "



The Cern3 g-2 experiment

• Emiliio Picasso view of the Cern3 g-2 experiment







Creating the Muon Beam for g-2:

- 8 GeV protons into the Recycler
- Target for pion production
- Long FODO channel to collect $\pi \rightarrow \mu \nu$
- pions decay in ~2km channel
- μ enter storage ring



How do we measure the spin direction?

• Use V-A structure of weak decays to build a polarized beam...



spin anti-parallel to muon momentum

 ... and to measure the muon polarization looking for energetic positrons



high momentum positrons emitted preferentially along muon spin



Measuring the spin precession

• The number of observed positrons above a threshold energy oscillates with the $\omega_a/2\pi$ frequency due to spin precession



- exponential decay modulated by spin precession
- note that the x-axis "wraps up" every 100 μ sec for a total of ~700 μ s \rightarrow ~10 muon lifetimes



Extracting a_µ(simplified)

$$\omega_a = a_{\mu} \left(e/m \right) B \rightarrow a_{\mu} = \omega_a / B \left(m/e \right)$$

by expressing B in terms of the (shielded) proton precession frequency: $(B = \hbar \omega_p'/2\mu_p'):$



 $\widetilde{\omega}'_p$ = (shielded) Proton angular velocity weighted for the muon distribution

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The key ingredients



• $\omega'_p = \omega'_p \cdot M(x, y, \varphi)$ magnetic field weighted by the muon distribution in the Storage Ring

Muon g-2

RING

FIELD

DETECTORS

Inflector

24 Calorimeters + 2 trackers located all around the ring

NMR probes and electronics located all around the ring



SIL

QUADS

Real World Experiment: Storage Ring

• 14 m diameter, 1.45 T C-shaped magnet stores muons





Measuring the Field: NMR Probes

In-vacuum NMR trolley maps field every ~3 days



17 petroleum jelly NMR probes





• 378 fixed probes monitor field during muon storage at 72 locations





Calibration of Field Measurements

 Cross-calibrate using a cylindrical plunging H₂O probe which repeatedly changes places with trolley (petroleum jelly probes)





- This probe is checked against a spherical probe using an MRI magnet at ANL
- Both also cross-checked against a ³He probe (different systematics)



H₂O Probe

³He Probe



Real World Experiment: Muon Injection

• Muons are injected into storage ring & bend in the B field





Real World Experiment: Kicker

• Fast kicker magnet tweaks direction from injection trajectory





Real World Experiment: Quads





Real World Experiment: Decay Positrons

• Experiment measures decay e⁺ which curl inwards as they





Real World Experiment: Trackers

• We measure the decay point with 2 trackers





Muon Distribution from Trackers:



- Measure beam oscillations directly
 - Beam-dynamics corrections
 - Tuning simulations
 - Optimizing experiment running



Muon Distribution from Trackers:



- Measure beam oscillations directly
 - Beam-dynamics corrections
 - Tuning simulations
 - Optimizing experiment running

• Use distribution to weight the field maps by where the muons live



Real World Experiment: Calorimeters

Time & energy of decay e⁺ are measured by 24 calorimeters





Measuring ω_a : 5 parameters fit function

• Fit with simple positron oscillation:

$$N_e(t) = N_0 \exp\left(-t/\tau_{\mu}\right) \left[1 + A\cos(\omega_a t + \varphi)\right]$$

• This simple fit is clearly not sufficient and well defined resonances are observed in the residuals



The complete 22 parameters fit function

 ω_y, ω_{VW} vertical oscillations $\omega_{CBO}, \omega_{2CBO}$ radial oscillations

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 $N_0 e^{-\frac{t}{\gamma \tau}} \left(1 + \mathbf{A} \cdot A_{BO}(t) \cos(\omega_a t + \phi \cdot \phi_{BO}(t))\right) \cdot N_{CBO}(t) \cdot N_{VW}(t) \cdot N_y(t) \cdot N_{2CBO}(t) \cdot J(t)$ $A_{\rm BO}(t) = 1 + A_A \cos(\omega_{\rm CBO}(t) + \phi_A) e^{-\frac{t}{\tau_{\rm CBO}}}$ $\phi_{\rm BO}(t) = 1 + \underline{A_{\phi}}\cos(\omega_{\rm CBO}(t) + \underline{\phi_{\phi}})e^{-\frac{t}{\tau_{\rm CBO}}}$ $N_{\rm CBO}(t) = 1 + A_{\rm CBO}\cos(\omega_{\rm CBO}(t) + \phi_{\rm CBO})e^{-\frac{t}{\tau_{\rm CBO}}}$ $N_{2\text{CBO}}(t) = 1 + A_{2\text{CBO}}\cos(2\omega_{\text{CBO}}(t) + \phi_{2\text{CBO}})e^{-\frac{t}{2\tau_{\text{CBO}}}}$ $N_{\rm VW}(t) = 1 + A_{\rm VW} \cos(\omega_{\rm VW}(t)t + \phi_{\rm VW})e^{-\frac{t}{\tau_{\rm VW}}}$ $N_{y}(t) = 1 + A_{y}\cos(\omega_{y}(t)t + \phi_{y})e^{-\frac{t}{\tau_{y}}}$ Red = free parameters $J(t) = 1 - k_{LM} \int_{t_0}^{t} \Lambda(t) dt$ Lost muons (µ hitting collimators) Blue= fixed parameters $\omega_{\rm CBO}(t) = \omega_0 t + A e^{-\frac{t}{\tau_A}} + B e^{-\frac{t}{\tau_B}}$ $\omega_y(t) = F\omega_{\text{CBO}(t)}\sqrt{2\omega_c/F\omega_{\text{CBO}}(t) - 1}$ $\omega_{\rm VW}(t) = \omega_c - 2\omega_u(t)$

Final fit to get ω_a



Real World Complications: Corrections

• We need to make corrections for several small effects:



Total correction is 622 ppb, dominated by E-field & Pitch...

Run-2/3 Uncertainty Improvement Categories







Analysis Improvements



Run-2/3 Uncertainty Improvement Categories







Analysis Improvements





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Run-2/3 Improvement: Statistics



• Factor 4.7 more data in Run-2/3 than Run-1

Dataset	Statistical Error [ppb]
Run-1	434
Run-2/3	201
Run-1 + Run-2/3	185

Run-2/3 Uncertainty Improvement Categories









Analysis Improvements



Running Conditions: Hall Temperature

• Temperature stability makes magnetic field less variable


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• Temperature stability makes magnetic field less variable





Running Conditions: Kicker Strength

Last 18% of Run-2/3 has upgraded, stronger kicker



- Mom. distribution more centered
- Lower E-field correction C_e

- Phase space matching improved
- Smaller beam oscillations



Run-2/3 Uncertainty Improvement Categories





Running Conditions





Analysis Improvements



Improved Measurements: Quad Transient Field

- Pulsing quads vibrate ⇒ oscillating magnetic fields
- Measured with a **new NMR probe** housed in insulator



- For Run-1 analysis, we had limited measurement positions
- Largest Run-1 systematic: 92 ppb



Improved Measurements: Quad Transient Field

- For Run-2/3 analysis, probe runs on the trolley rails
- Allows full mapping of all quad stations:



Measurement probe mounted on trolley rail train

Azimuth (deg)

• Uncertainty is reduced to **20 ppb**



Improved Measurements: Kicker Transient Field

• Kicker creates eddy currents ⇒ transient magnetic field



- Run-2/3 has lower vibration noise vs. Run-1
- Uncertainty reduces from **37 ppb to 13 ppb**



Run-2/3 Uncertainty Improvement Categories





Analysis Improvements: *Pile-up*



- *Pile-up*: 2 e⁺ arriving at same time → 1 cluster in ECAL
- Probability higher at injection (more muons): can **bias** ω_a
- Clusters with E>3.1GeV are certainly *Pile-up*
- Reduced uncertainty by:
 - Improved reconstruction
 - Improved correction algorithms



Uncertainty Improvements Summary

• Systematic improvements in all parameters





Run-2/3 Uncertainties: Final Values

Quantity	Correction	Uncertainty [ppb]
$\overline{\omega_a^m}$ (statistical)	[ppb]	201
ω_a^m (systematic)	_	25
$\overline{C_e}$	451	32
C_p	170	10
C_{pa}	-27	13
C_{dd}	-15	17
C_{ml}	0	3
$f_{\rm calib} \langle \omega_p'(\vec{r}) \times M(\vec{r}) \rangle$	_	46
B_k	-21	13
B_q	-21	20
$\mu_p'(34.7^\circ)/\mu_e$	_	11
m_{μ}/m_e	_	22
$g_e/2$	—	0
Total systematic	_	(70)
Total external parameters	—	\varkappa
Totals	622	215

Total uncertainty is **215 ppb**

[ppb]	Run-1	Run-2/3	Ratio
Stat.	434	201	2.2
Syst.	157	70	2.2

Near-equal improvement: We're still statistically dominated

Systematic uncertainty of 70 ppb surpasses our proposal goal of 100 ppb!



Blind Analysis

- Perform analysis with software & hardware blinding
- Hardware blind comes from altering our clock frequency



Non-collaborators set frequency to $(40 - \delta)$ MHz

Greg Bock & Joe Lykken

• Clock is locked and value kept secret until analysis completed



July 24th 2023: Unblinding

• Physics week in Liverpool for unblinding meeting:



Photo credits: McCoy Wynne

- Unanimous vote from all collaborators to unblind!
- Secret envelopes were finally opened to reveal the hidden clock frequencies and the result...



... a moment of panic!

- two layers of unblinding: software and hardware
- first the software unblinding was removed and the following image appeared on screen: few seconds of panic!



After inserting the secret frequency ...

• The secret frequency, written in the two envelopes, was inserted in the program



Run-2/3 Result: Measured Value

a_µ(FNAL; Run-2/3) = 0.00 116 592 057(25) [215 ppb]



- Excellent agreement with Run-1 and BNL!
- Uncertainty more than halved to **215 ppb**
- Both FNAL values dominated by statistical error
- Assume systematics are 100% correlated and combine...



Run-2/3 Result: FNAL Run-1 + Run-2/3 Combination

a_u(FNAL) = 0.00 116 592 055(24) [203 ppb]



- FNAL combination:
 203 ppb uncertainty
- Both FNAL and BNL dominated by statistical error



Run-2/3 Result: FNAL + BNL Combination

a_µ(FNAL) = 0.00 116 592 055(24) [203 ppb]



- FNAL combination:
 203 ppb uncertainty
- Both FNAL and BNL dominated by statistical error
 - Combined world average **dominated by FNAL** values.

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a_u(Exp) = 0.00 116 592 059(22) [190 ppb]

Measurements at Different Magnetic Fields

- Datasets were taken at slightly different field settings
- Allows a cross check with one of the most basic "handles":



• Also checked a_u against temperature, day/night & others

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Experiment vs Theory Comparison

• Theory prediction is less clear now, but we can still compare



- Large discrepancy between experiment and WP (2020)
- Significance for Fermilab
 alone get to 5.0σ
 - ... but the theoretical band is not as sharp as it was in the 2021 comparison!



HVP Calculation: Lattice QCD Method

- Ab-initio calculation of HVP on lattice
- Results **not included** in White Paper (2020)





- **BMW** collaboration reached the precision of 0.8%, comparable to R-ratio method
- Their calculation is closer to the experimental result
- Other groups are cross checking
- Intermediate stages agree, but no full HVP calculations to same precision.



Experiment vs Theory Comparison

• Theory prediction is less clear now, but we can still compare



- Include **BMW** result by swapping HVP from WP with their value
- As expected, BMW falls in between WP (2020) and experiment



HVP Calculation: Dispersive (e⁺e⁻) Method

• Calculated from data for $\sigma(e^+e^- \rightarrow hadrons)$



- Uses data from different experiments from 20+ years
- 1/s weights low energy strongly: 73% from $\pi^+\pi^-$ channel



- New results from SND2k and CMD-3 since White Paper
- CMD-3 is discrepant
- ... what is going on?



Data Collection 2018 – 2023

Last update: 2023-07-11 08:26 ; Total = 21.90 (xBNL)





9 July 2023 Director Lia Merminga switches off the beam in *Muon g-2* control room

- Apr. 2021: Run-1 Result (2018 data)
- Aug. 2023: Run-2/3 Result (2019-20 data)
- ~2025: Run-4+5+6 Result (2021-23 data)
 - Reach our proposal goal for statistics (~21 BNL)



The experimental landscape will improve ...

- 1. FNAL Muon g-2 :
 - a_{μ} measured at 0.2 ppm
 - data already available to reduce error to < 0.14 ppm
- 2. A new type of experiment projected at J-Parc using low energy muons (p~300 MeV/c)
 - new technique
 - under construction
 - final goal ~0.4 ppm





The experimental landscape will improve ...

Ongoing work in experimental inputs on $\sigma(e^+e^- \rightarrow hadrons)$

- Initial State Radiation technique:
 - BaBar: new analysis of large $\pi\pi$ data set with better detector
 - KLOE: new analysis of 7x larger $\pi\pi$ set
 - BESIII: new results for $\pi\pi$ channel and $\pi\pi\pi$
 - Belle II: promising greater statistics than BaBar or KLOE and similar or better systematics for low-energy cross sections
- Energy scan (VEPP-2000 machine in Novosibirsk)
 - SND: new results for $\pi\pi$ channel
 - CMD-3: confirmation of their result on $\pi\pi$ channel; more channels to be analyzed

The theoretical landscape will improve ...

- 1. close scrutiny of lattice calculations to establish its solidity
 - how to reconcile it with dispersion approach?
- 2. Use the dispersive approach with t-channel data (*muon-electron* scattering), instead of the standard s-channel
 - Letter Of Intents submitted at CERN: Muone (mu-on-e scattering)



Conclusions

We've determined a_µ to an unprecedented 203 ppb precision



- New result is in excellent
 agreement with Run-1 & BNL
- More than halved the total uncertainty from Run-1
- Smashed our design goal with systematic uncertainty of 70 ppb.
- There's **more data** to analyze and we'll squeeze uncertainty down further in our future results!

EXTRAS

Running Conditions: Damaged Quad Resistors

- Run-1 had damaged resistors in 2/32 quad plates leading to unstable beam storage
- Resistors re-designed & replaced before Run-2

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- C_{pa} uncertainty is reduced (75 ppb \rightarrow 13 ppb)
- Beam oscillation frequencies are also more stable

Experiment vs Theory Comparison

• Theory prediction is less clear now, but we can still compare

Disclaimer from A. Keshavarzi's Lattice 2023 talk:

IMPORTANT: THIS PLOT IS VERY ROUGH!

- + TI White Paper result has been substituted by CMD-3 only for 0.33 \rightarrow 1.0 GeV.
- The NLO HVP has not been updated.
- It is purely for demonstration purposes → should not be taken as final!

Following A. Keshavarzi at Lattice 2023...

- Substitute CMD-3 data for HVP below 1 GeV
- Cherry-picking one experiment but gives a bounding case
- **SND2k** cannot be processed in this way, but would fall closer to WP (2020).
- Many parallel efforts are underway to resolve the theoretical ambiguity

Theory Prediction Lattice QCD

HVP Calculation: Lattice QCD Method Status

- Other groups are working to reproduce BMW result
- Start with "windowing" method and compare in easiest region

- Cut off effects suppressed
- No signal-to-noise problem
- Finite-volume effects small

HVP Calculation: Lattice QCD Method Status

Simon Kuberski, Lattice 2023

THE INTERMEDIATE-DISTANCE WINDOW

- 3.8 σ tension between lattice QCD and data-driven evaluation [Colangelo et al., 2205.12963].
- This accounts for 50% of the difference between BMW 20 and the White Paper average for $a_{\mu}^{\rm hvp}$.

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HVP Calculation: Lattice QCD Method Status

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THE INTERMEDIATE-DISTANCE WINDOW

- 3.8 σ tension between lattice
 QCD and data-driven evaluation
 [Colangelo et al., 2205.12963].
- This accounts for 50% of the difference between BMW 20 and the White Paper average for $a_{\mu}^{\rm hvp}$.
- Agreement across many actions for the light-connected contribution (87%).
- Data-driven estimate:
 [Benton et al., 2306.16808] [Golterman]

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Theory Prediction Future Prospects

Dispersive Approach: Future Prospects for HVP

A. El-Khadra P5 town hall, 21-24 Mar 2023

Ongoing work on experimental inputs:

- BaBar: new analysis of large data set in $\pi\pi$ channel, also $\pi\pi\pi$, other channels, other channels
- KLOE: new analysis of large data in $\pi\pi$ channel, other channels
- SND: new results for $\pi\pi$ channel, other channels in progress
- BESIII: new results in 2021 for $\pi\pi$ channel, continued analysis also for $\pi\pi\pi$, other channels
- Belle II: <u>arXiv:2207.06307</u> (Snowmass WP) Better statistics than BaBar or KLOE; similar or better systematics for low-energy cross sections
- STCF: arXiv:2203.06961
- Need blind analyses to resolve the tensions (esp. for $\pi\pi$ channel)

Ongoing work on theoretical aspects:

- Developing NNLO Monte Carlo generators (STRONG 2020 workshop https://agenda.infn.it/event/28089/) [m appendix]
- radiative corrections using FsQED (scalar QED + pion form factor)
- charge asymmetry (CMD-3 measurement) vs radiative corrections [Ignatov + Lee, arXiv:2204.12235]
- development of new dispersive treatment of radiative corrections in ππ channel [Colangelo at al, arXiv2207.03495]
- including τ decay data: requires nonperturbative evaluation of IB correction [M. Bruno et al, arXiv:1811.00508]

If the differences between experiments are resolved:

data-driven evaluations of HVP with $\sim 0.3~\%\,$ feasible by ${\sim}2025$

Lattice QCD: Future Prospects for HVP





Theory vs Experiment



Differences between a_µ values:

Sigma deviation between different predictions/measurements

	FNAL 2023 (World Ave)	WP 2020	BMW	CMD-3
Ехр	-			
WP 2020	5.0 (5.1)	-		
BMW	1.6 (1.7)	2.0	-	
CMD-3	1.4 (1.5)	2.8	0.4	-

- Comparisons are taken from the whole a_u value.
- They're accurate when comparing to experiment
- But e.g. WP (2020) & BMW both include same H-LbL components and error, so significance of difference between them is a little underestimated (2.0 vs 2.2σ).



BSM Physics



Discrepancy and New Physics:

(Experimentalist's (mis)Understanding)

D. Stöckinger:





Discrepancy and New Physics:

(Experimentalist's (mis)Understanding)

D. Stöckinger:

https://arxiv.org/abs/2104.03691



Detectors



Calorimeter Location

• 24 EM calorimeters inside the ring to measure decay e⁺





Calorimeter Design

- Array of 54 PbF₂ crystals 2.5 x 2.5 cm² x 14 cm (15X₀)
- Readout by SiPMs to 800 MHz WFDs (1296 channels)







GAIN stability established to ~few x 10⁻⁴

State-of-the-art Laser-based calibration system also allows for pseudo data runs for DAQ







Muon Distribution M_µ

- Want the field actually experienced by muons, so need to know where muons are in the field map
- Measured with two straw trackers inside storage vacuum







Muon's view of a tracker ilab

Tracker: Hawk-Eye with Muons

• Each tracker is made up of 8 modules inside vacuum chamber:





Tracker: Hawk-Eye with Muons

• A muon decays to a positron which travels through tracker



- e⁺ position is recorded in tracker modules
- Hits are grouped and reconstructed into a track
- Track is extrapolated backwards to beam storage region



Corrections



E-field & Pitch Corrections:

Non-simplified spin-motion is described by BMT equation:

$$\frac{d(\hat{\beta}\cdot\vec{S})}{dt} = -\frac{q}{m}\vec{S}_T \cdot \begin{bmatrix} a_\mu\hat{\beta}\times\vec{B} + \beta \begin{pmatrix} p_\mu = 3.094 \text{ GeV} \\ q_\mu & \gamma^2 - 1 \end{pmatrix} \frac{\vec{E}}{c} \end{bmatrix}$$

Jackson Eq. (11.171)

- Muons travel in E-field from focusing quadrupoles: experience a motional magnetic field in their rest frame
- Term vanishes at "magic" momentum (p_µ = 3.094 GeV)
- But not all muons are at p_{magic}
- C_E comes from p_µ distribution measured using timing data from calorimeters

$$C_{E} = 489 \pm 53 \text{ ppb}$$



E-field & Pitch Corrections:

Non-simplified spin-motion is described by BMT equation:

$$\frac{d(\hat{\beta}\cdot\vec{S})}{dt} = -\frac{q}{m}\vec{S}_T\cdot\left[a_{\mu}\hat{\beta}\times\vec{B}+\beta\left(a_{\mu}-\frac{1}{\gamma^2-1}\right)\frac{\vec{E}}{c}\right]$$

Jackson Eq. (11.171)

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• Muons oscillate vertically (pitch) so $\hat{\beta} \times \vec{B}$ term is reduced





E-field Correction: C_E

• Imagine injecting uniform momentum & time distributions:



 Higher momentum muons have further to travel, so have lower cyclotron freq.

E-field Correction: C_E

• Over time, lower momentum will catch higher momentum:



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 The way that the gaps are filled in is related to the momentum distribution of the stored beam

E-field Correction: C_E

• Effect is a strong feature of the data at early times:



- Less pronounced when all calos are added together
- Either Fourier analysis or χ^2 fit are used to get momentum distribution



ω_a Systematics: Phase Shifts

- Many systematics come from effects that change the phase of the detected e⁺ over time
- These make us mis-measure ω_a with no other indications that we're getting it wrong

$$cos(\omega_a t + \phi(t)) = cos(\omega_a t + \phi_0 + \phi' t + ...)$$
$$= cos((\omega_a + \phi')t + \phi_0 + ...)$$

- In general, anything that changes from early-to-late within each muon fill can be a cause of systematic error.
- Most phase shifts are eliminated by design or before fitting the data, but we must correct for two effects (C_{ML} & C_{PA})

C_{PA} – Phase-Acceptance Correction

• Remember $\phi \rightarrow \phi(t)$ causes us to mis-measure ω_a



- Due to acceptance, φ depends on muon decay position (x,y)
- Not an issue if the muon distribution doesn't change shape over a fill

- But in Run 1, equipment failure led to beam instability
- 2/32 quad HV resistors died
 → Focusing E-field changed
 → Beam width changed





- Beam width changes couples to phase "map" to cause $\phi(t)$
- -158 ppb correction with a 75 ppb uncertainty in Run 1
- Fixed by Run 2: majority of correction & uncertainty disappears



Why phase varies with decay position

• Average detected phase changes with decay position:



- Origin is acceptance: if e⁺ decays outwards then it will have a longer path length to a detector
- We see fewer events from top/bottom of storage region as they miss the detectors vertically

a_{μ} from Measurement



What do we really measure?



 ω_a : e⁺ oscillation frequency

 $\tilde{\omega}_p'(T_r)$: magnetic field from precession of protons in H₂0, weighted by muon distribution

Proposal Goal: 140 ppb = 100 ppb (stat) ① 100 ppb (syst) $\frac{\mu_e(H)}{\mu_p'(T)}$ Measured to 10.5 ppb accuracy at T = 34.7°C Metrologia **13**, 179 (1977)

 μ_e ____ Bound-state QED (exact)

 $\mu_e(H)$ Rev. Mod. Phys. **88** 035009 (2016)

 m_{μ} Known to 22 ppb from muonium hyperfine splitting

- *m_e* Phys. Rev. Lett. **82**, 711 (1999)
- $\underline{g_e}$ Measured to 0.28 ppt 2 Phys. Rev. A 83 052
- 2 Phys. Rev. A 83, 052122 (2011)

Total < 25 ppb



 $a_{\mu} \propto \frac{\omega_a}{D}$

Systematics vs BNL



Systematic Errors on ω_a (ppb)

	BNL (E821)	Proposal	Run 1	Run-2/3
Gain	120	20	10	5
Pileup	80	40	30	7
СВО	70	30	40	20
E & Pitch	50	30	55	33
Lost Muons	90	20	5	3
Phase Acceptance	-	-	75	15
Total	180	70	108	42

Numbers are approximate Category mapping is imperfect



Systematic Errors on ω_p (ppb)

	BNL 2001 (E821)	Proposal	Run 1	Run-2/3
Absolute Calibration	50	35	19	13
Trolley Calibration	90	30	32	14
Trolley Baseline	50	30	40	38
Fixed Probe Baseline	70	30	23	16
Muon Weighting	30	10	18	10
Quad Transient	*	*	92	20
Kicker Transient	*	*	37	13
*Others	100	50	-	-
Total	170	70	114	53

Numbers are approximate Category mapping is imperfect





Magnet Design & Shimming

- 14.2 m diameter "C"-shape magnet with 1.45 T vertical field
- Shimming campaign from 2015-16 resulted in very uniform field
- 14 ppm RMS across full azimuth & 3x better than at BNL







- Many "knobs" for shimming:
 - 72 Poles
 - Shaping & homogeneity



- Many "knobs" for shimming:
 - 72 Poles
 - Shaping & homogeneity
 - 864 Wedges
 - Quadrupole asymmetry



- Many "knobs" for shimming:
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 - Quad/sextapole asymme
 - 8000 Surface Iron Foils
 - Local changes of effective
 - 100 Active Surface Coils



g-2 Magnet in Cross Section

108 5/sep/23 Croantrolagurinemtito add ring-wide average field moments
Shimming the Magnet

• Progress towards a uniform field from Oct '15 to Sep '16:



Dipole field (p-p & RMS) improved by factor 3 compared to BNL

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ω_a Measurement



Why do decay e⁺ tell us about muon spin?

• Muon spin information is encoded in **parity violating** decay



- Highest energy positrons are emitted back-to-back with neutrinos
- Neutrino helicity is fixed, so high energy positrons are emitted in direction of muon spin



Simple fit: residuals

• Simplest form for fit is an exponentially decaying oscillation:



 Beam oscillations couple to acceptance & change number of e⁺ detected with time, and exponential isn't perfect

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Fit with beam dynamics terms

• Add terms to fit function to deal with complications:

$$N_0 e^{-t/\tau} (1 + A\cos(\omega_a t + \phi))$$

 $f(t) = N_0 e^{-t/\tau} \Lambda(t) N_{cbo}(t) N_{2cbo}(t) \left(1 + A_{cbo}(t) \cos(\omega_a t + \phi_{cbo}(t))\right)$

• Muons that are lost from storage ring before they decay:

$$\Lambda(t) = 1 - \kappa_{loss} \int_{t_0}^t L(t') e^{(t'/\tau)} dt'$$

• Beam oscillations that modulate decay rate:

e.g. $N_{cbo}(t) = (1 + A_{cbo-N} \cdot e^{-t/\tau_{cbo}} \cdot \cos(\omega_{cbo}(t) \cdot t + \phi_{cbo-N}))$



Fit with beam dynamics terms: residuals

• Adding terms tames the beast:



- Important to get it right: ω_a changes by **2.2 ppm**
- Good residuals & χ^2 are necessary, but not sufficient condition.



Systematic Cause: Time-Dependent Phase

• If average phase of muon population changes over time then we can mis-measure ω_a :



$$N_0 e^{-t/\tau} (1 + A\cos(\omega_a t + \phi))$$

But if $\phi \rightarrow \phi(t)$, then

$$\cos(\omega_a t + \phi(t)) = \cos(\omega_a t + \phi_0 + \phi' t + \dots)$$
$$= \cos((\omega_a + \phi')t + \phi_0 + \dots)$$

If higher order terms are small, then we measure (ω_a + φ') instead of ω_a and still get good χ²



Main Systematic Issues

- 3 main systematics for ω_a measurement
- Variety of mitigation strategies
- Well under control total is
 56 ppb





Dedicated laser calibration system

Systematic Issues: Gain

 Calorimeter gain takes time to recover from "flash" when beam first enters storage ring:



- Phase is energy dependent so gain change generates another time-dependent phase & normalization issues
- Correct based on gain measurements from laser system and cross-check with tracker





• Pile up happens less often as the muons decay so phase changes with time and we get ω_a wrong

 Derive a pile up correction from data and check validity above 3.1 GeV



Muon EDM



Muon Electric Dipole Moment

- Muon EDM is essentially zero in SM.
- Any observation would be a sign of new physics:



- Muon is the best option for a higher flavour gen. search
- And it's free of nuclear / molecular effects
- But, needs non-mass-scaling BSM effects to see anything given e⁻ EDM limit



EDMs: Theory & Experiment

Muon EDM: Tracker Search

A non-zero muon EDM would modify the spin equation

$$\vec{\omega}_{a\eta} = a_{\mu} \frac{e}{m} \vec{B} + \eta \frac{e}{2m} \left[\frac{\vec{E}}{c} + \vec{\beta} \times \vec{B} \right]$$

- $\vec{\beta} \times \vec{B}$ dominates, so precession plane is tilted. $\boldsymbol{\omega}_{a} \boldsymbol{\wedge} \boldsymbol{\delta} \boldsymbol{\wedge} \boldsymbol{\omega}$

B

X

 ω_{η}

 $\omega_a >>>> \omega_\eta$

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S

ß

$$\omega = \sqrt{\omega_a^2 + \omega_\eta^2} = \sqrt{\omega_a^2 + \left(\frac{e\eta\beta B}{2m}\right)^2}$$

 Search for an up-down oscillation, out of phase with ω_a .

Muon EDM: Tracker Search

• Search was done with tracker at BNL:



- Previous tracker search was statistics limited
 - $\begin{array}{ll} \mbox{Tracker:} & |d_{\mu}| < 3.2 \times 10^{-19} \, e \, {\rm cm} \, (95\% {\rm CL}) \\ \mbox{Tracker \& Calo:} & |d_{\mu}| < 1.8 \times 10^{-19} \, e \, {\rm cm} \, (95\% {\rm CL}) \\ \mbox{SM:} & |d_{\mu}| < 10^{-38} \\ \end{array}$ (World's best for muon EDM)

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We're aiming to improve this limit to 10⁻²¹ e cm

Electron Anomaly: a_e



Why a_{μ} and not a_{e} ?

- Coupling of virtual loops goes as m² (dimensional analysis)
- Therefore, while a_{μ} is measured ~20x less precisely than the a_{e} , it has better sensitivity to heavy physics scales:

$$\left(\frac{m_{\mu}}{m_{e}}\right)^{2} \simeq 43,000$$

- E.g. lowest-order hadronic contribution to a_e is $a^{had,LO} = (1.875 \pm 0.017) \times 10^{-12}$ (1.5 ppb of a_e)
- By comparison, the muon's hadronic contribution is ~60 ppm.

g_e and α :

• New measurement of g_e in 2023:

0.13 ppt on g_e

Measurement of the Electron Magnetic Moment

X. Fan, T. G. Myers, B. A. D. Sukra, and G. Gabrielse Phys. Rev. Lett. **130**, 071801 – Published 13 February 2023

https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.130.071801

 Ability to compare with prediction hampered by disagreement in the value of α:





J-PARC Experiment



J-PARC muon g-2/EDM experiment



J-PARC Experiment

- Complementary technique
 - μ beam accelerated from rest
 - no E fields
 - smaller magnet
- Aiming for a result comparable to Run-1 result towards the end of the decade



Muon anomalous magnetic moment $a_{\mu} \times 10^9$ - 1165900

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- Under construction aiming for data taking from 2028.
- Succeeded to deliver a surface muon beam to H-line.
- Constructed the experimental area for muon cooling and the first stage of the acceleration.
- Currently taking data to demonstrate the muon cooling by using the laser ionization of muonium, followed by RF acceleration tests.