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UON Collider  
Collaboration



# Mechanical concepts for 40T Final Cooling Solenoid for the Muon Collider

C. Accettura, A. Bertarelli, B. Bordini

With several contributions from L. Bottura, A. Dudarev, A.  
Kolehmainen, F. Sanda

Muons Magnets Working Group

<https://indico.cern.ch/e/1313020>

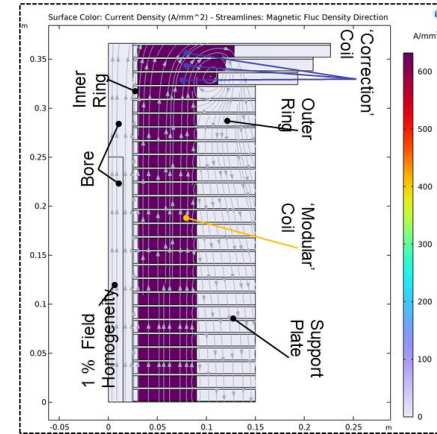
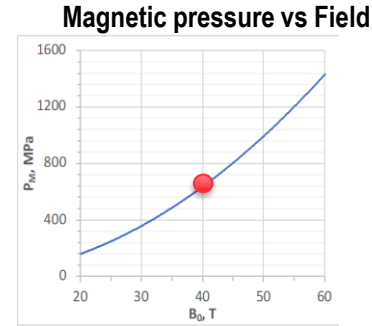
14/12/2023, CERN

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- Introduction and motivation
- Pre-compression concepts
- FEA simulations for different concepts and parameters
- Conclusions and perspective

# Introduction and Motivations

- Design proposed for the Final Cooling solenoid based on single and compact coil → critical stress management:
  - $P_M = B_0^2 / 2\mu_0 \sim 600 \text{ MPa}$
  - Hoop stress  $\sim 1.4\text{-}2.2P_M$  (compact coil)

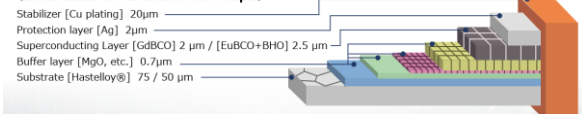


See [B. Bordini, Technology options for the final cooling solenoids, IMCC Annual Meeting 2023, Orsay](#)

# Introduction and Motivations

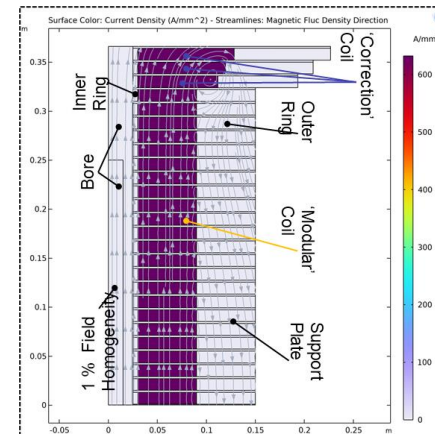
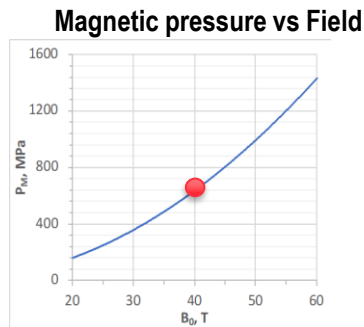
- Design proposed for the Final Cooling solenoid based on single and compact coil → critical stress management:
  - $P_M = B_0^2 / 2\mu_0 \sim 600\text{MPa}$
  - Hoop stress  $\sim 1.4\text{-}2.2P_M$  (compact coil)
- Non-homogeneous and anisotropic material:
  - Maximum allowable stress very weak in certain direction
  - Scarce literature
  - Reduced safety margin

<Schematic of RE-based HTS tape>



Reference Conductor Fujikura FESC-SH12.

<https://www.fujikura.co.jp/eng/products/newbusiness/superconductors/01/superconductor.pdf>



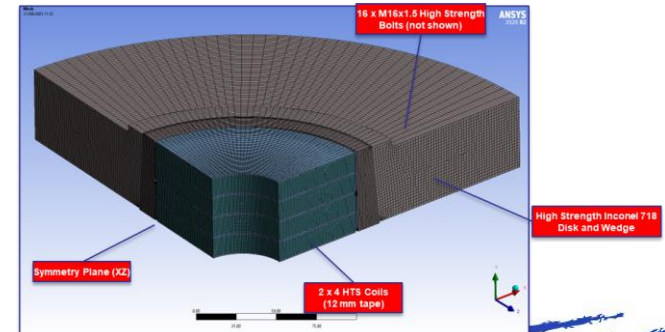
See [B. Bordini, Technology options for the final cooling solenoids, IMCC Annual Meeting 2023, Orsay](#)

REBCO conductor	
Axial tensile stress	700MPa
Axial tensile strain	0.4%
Transverse compressive stress	>100MPa
Transverse tensile stress	10-100MPa
Max shear stress	>19MPa

- A pre-compression of  $\sim 200\text{MPa}$  is needed to remain below this value

# Pre-compression

- How to obtain the pre-compression?
- Mechanical concept is based on **encapsulating** HTS pancake coils in an **external structure**, generating high **radial compressive stresses**. **Three concepts analysed:**
  1. Thermally-induced shrink fitting
  2. Adjustable shrink-discs with conical surfaces
  3. Hybrid solution (1+2)





# Shrink Fitting



- Coil surrounded by a cylindrical shell with  $r_{in\_shell} < r_{ext\_coil}$
- Shell is pre-heated → fitting of the coil inside → cool-down of the shell and thermal contraction
- Simple analytical evaluation:  $\sigma_{hoop} = -500\text{MPa} \rightarrow 200\text{MPa} \rightarrow \text{interference gap } \sim 220\mu\text{m} \rightarrow T_{shell} \sim 170^\circ\text{C}$

$$\sigma_{\theta} = -\frac{\rho^2 + \beta^2}{\rho^2} \frac{1}{1 - \beta^2} P_e$$

$$\delta = \delta_{i2} - \delta_{e1} = \left[ \frac{1}{E_2} \left( \frac{1 + \beta_2^2}{1 - \beta_2^2} + \nu_2 \right) + \frac{1}{E_1} \left( \frac{1 + \beta_1^2}{1 - \beta_1^2} - \nu_1 \right) \right] r_{e1} P_f$$

- Some practical aspects must be considered:

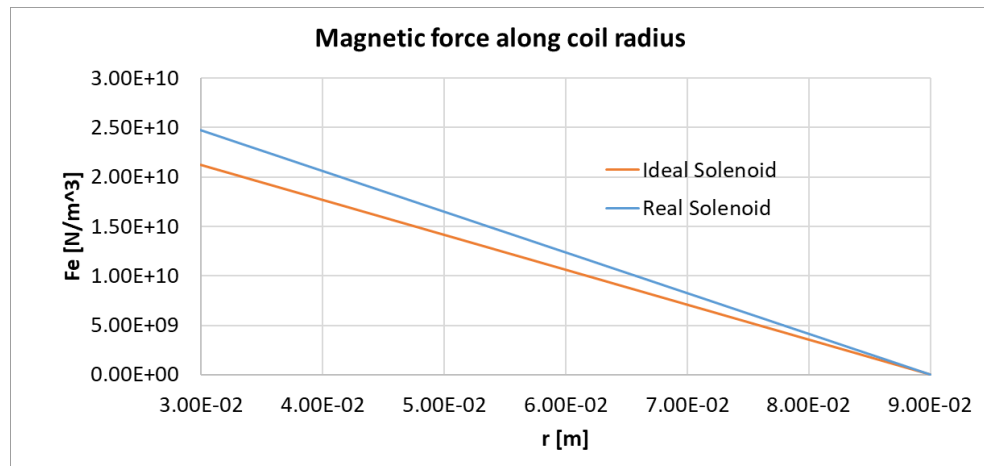
- Differential contraction during cooldown
- Strength of the cylinder
- Impact of the joints
- Plasticity
- Mechanical tolerances: 1MPa/μm lost
- Buckling

- FEA simulations at different levels of complexity

# Assumptions

- 2D axisymmetric
- Electromagnetic Forces

- Ideal Solenoid ( $J_{ideal} = \frac{B_{MAX}}{\mu_0(r_{co} - r_{ci})} = 531 \text{ A/mm}^2$ )
- Real Solenoid ( $J_{real} = J_{ideal} \frac{t_{coil} + t_{supportplate}}{t_{coil}} = 620 \text{ A/mm}^2$ )



All  
Unit: N/mm<sup>3</sup>  
Max: 22.343  
Min: 0  
06/12/2023 09:49

22.343  
19.86  
17.378  
14.895  
12.413  
9.9302  
7.4477  
4.9651  
2.4826  
0



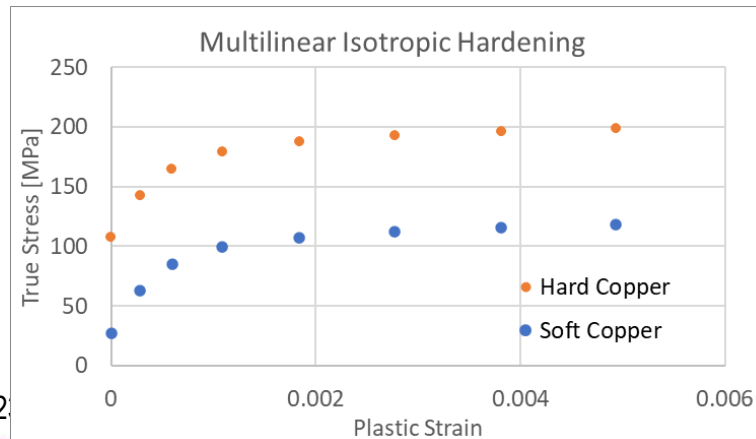
# Reference model

- Coil material (Hastelloy\_50+Copper\_30)
- Copper hard
- Copper soft
- Hastello
- Shell

Homogeneous  
tape properties

Needed to keep the pre-compression.  
Soft copper was resulting in a lower  
pre-compression

Ha to avoid radial tensile and  
shear stress after cooldown



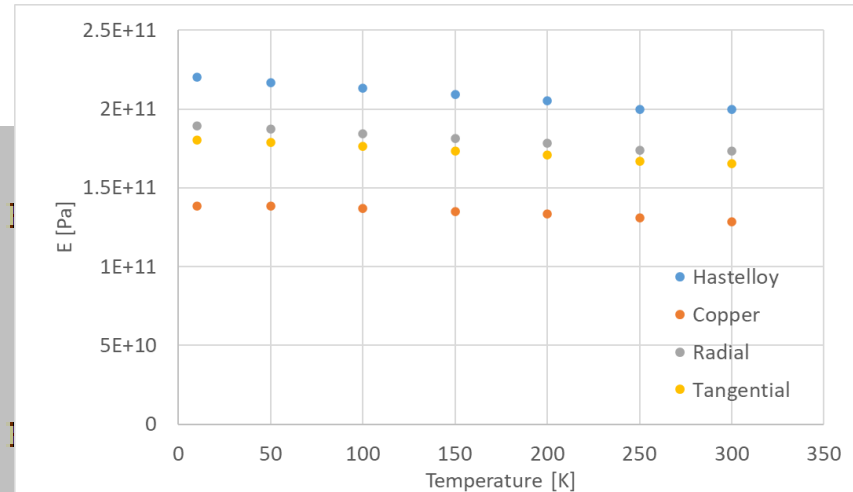
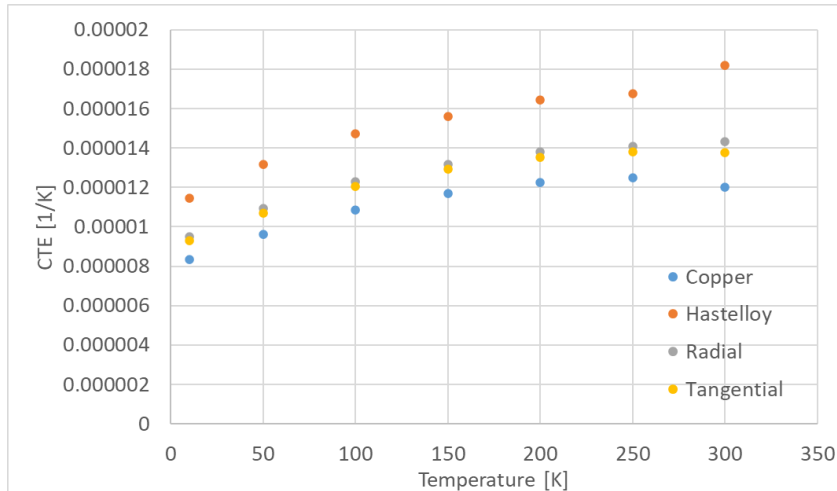


# Homogeneization

- Radial direction → springs in series
- Tangential direction → springs in parallel

$$E_{radial} = \frac{E_{Cu} \cdot t_{Cu} + E_{Ha} \cdot t_{Ha}}{t_{tot}}$$

$$E_{tangential} = t_{tot} \cdot \left( \frac{t_{Cu}}{E_{Cu}} + \frac{t_{Ha}}{E_{Ha}} \right)^{-1}$$



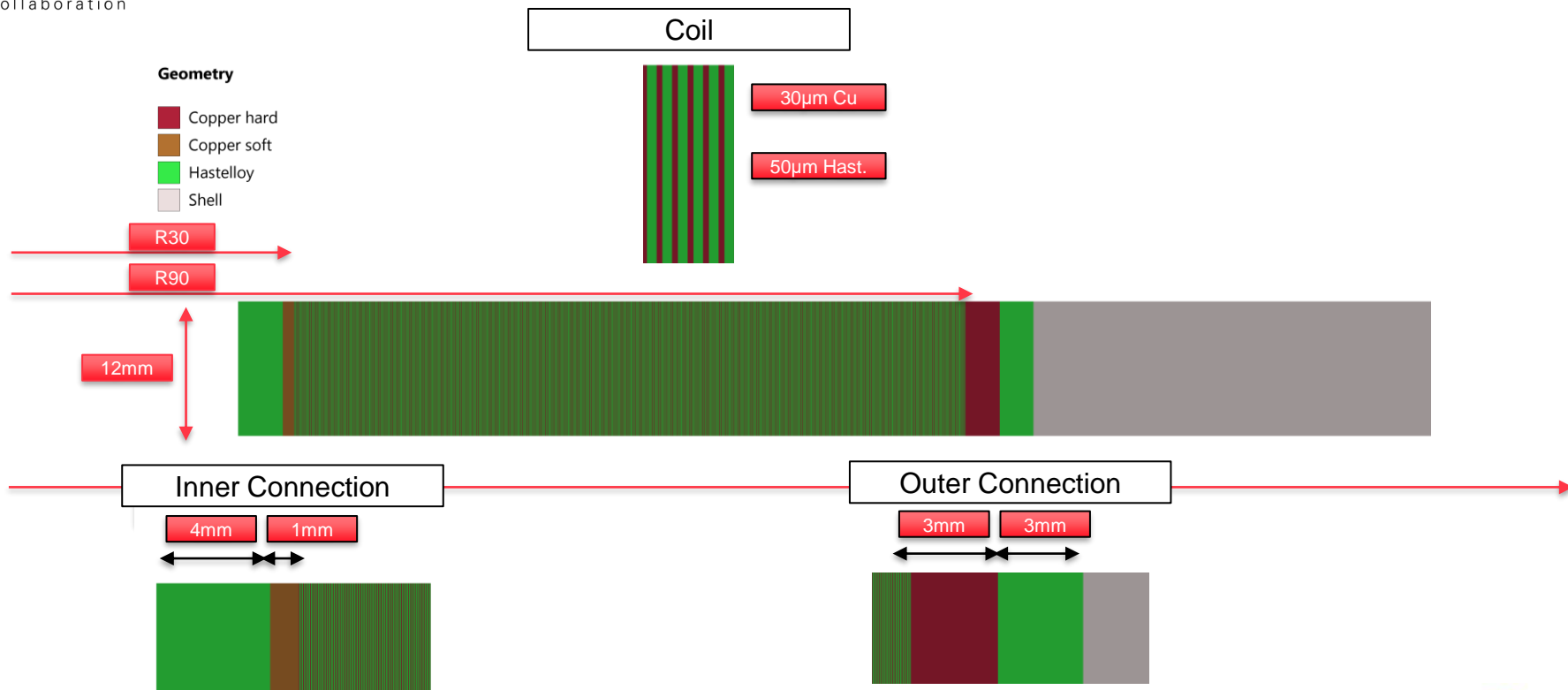
# Layered model

## Geometry

- Copper hard
- Copper soft
- Hastelloy
- Shell



# Geometry and Materials



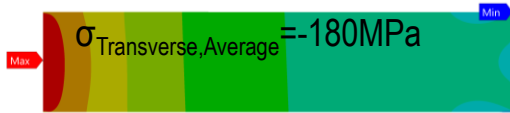
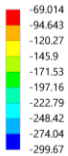
# Validity of homogeneous model



**Step 1: Shrink fitting (T external shell =250°C)**

$$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$$

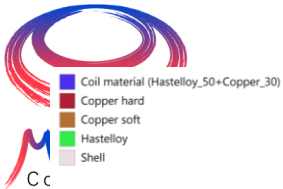
**Step 2: Cool-down**



**Step 3: Energization**



Y  
x  
oup, 14/12/2023



# Validity of homogeneous model

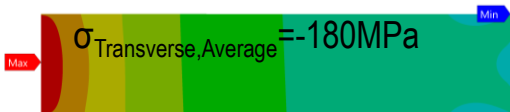
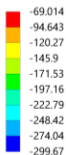


Step 1: Shrink fitting

$$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$$

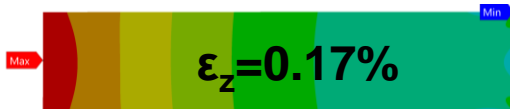
Step 2: Cool-down

$$\sigma_{\text{Transverse,Average}} = -180\text{MPa}$$



Step 3: Energization

$$\epsilon_z = 0.17\%$$



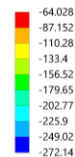
750 layers: 30μm+50 μm

Step 1: Shrink fitting

$$\sigma_{\text{Transverse,Average}} = -215\text{MPa}$$

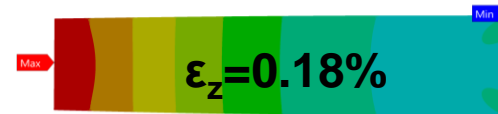
Step 2: Cool-down

$$\sigma_{\text{Transverse,Average}} = -170\text{MPa}$$



Step 3: Energization

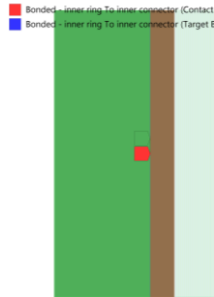
$$\epsilon_z = 0.18\%$$



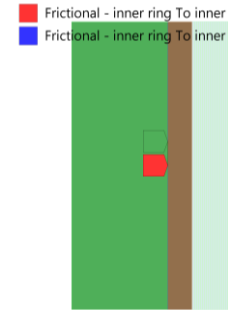
oup, 14/12/2023

0,000 10,000 20,000 (mm)

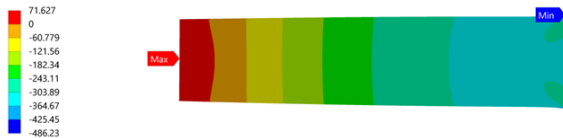
# Effect of the inner joint properties



Let the ring detach to limit radial tensile stress



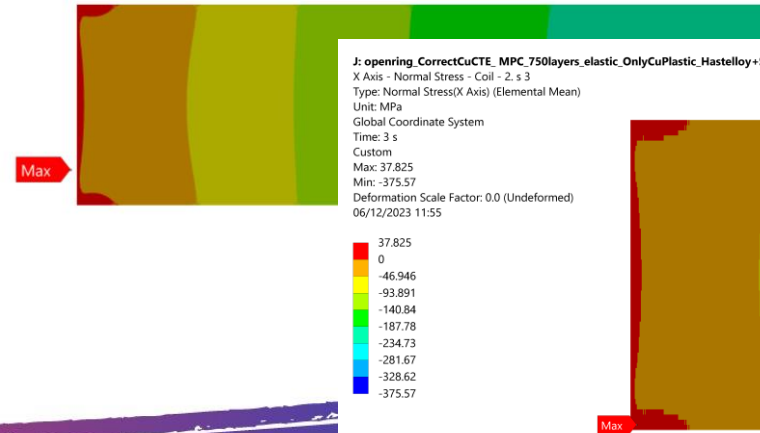
**G: CorrectCuCTE\_MPC\_750layers\_elastic\_OnlyCuPlastic\_Hastelloy+SoftCu INSIDE\_HardCu+Hastelloy OUTSIDE\_Orthotropic\_1supportfrictionless\_FRICTIONLESS\_2D\_axyal**  
 X Axis - Normal Stress - All layer + 1 - 3.s  
 Type: Normal Stress(X Axis)  
 Unit: MPa  
 Global Coordinate System  
 Time: 3 s  
 Custom  
 Max: 71.627  
 Min: -486.23  
 Deformation Scale Factor: 56 (Six Auto)  
 06/12/2023 10:04



Max: 73.473  
 Min: -502.27  
 Deformation Scale Factor: 0.0 (Undeformed)  
 06/12/2023 11:52



**J: opening\_CorrectCuCTE\_MPC\_750layers\_elastic\_OnlyCuPlastic\_Hastelloy+**  
 X Axis - Normal Stress - Coil - 2.s 3  
 Type: Normal Stress(X Axis) (Elemental Mean)  
 Unit: MPa  
 Global Coordinate System  
 Time: 3 s  
 Custom  
 Max: 37.825  
 Min: -375.57  
 Deformation Scale Factor: 0.0 (Undeformed)  
 06/12/2023 11:55



# Effect of the tape plasticity

step	$\sigma_x$ -radial[MPa]			$\epsilon_z$ -hoop
	min	max	ave	max
1	-289	-57	-210	
2	-224	-67	-164 (200*)	
3	-416	77	-213	0.30%
1	-308	-54	-214	
2	-272	-63	-171 (210*)	
3	-502	73	-224	0.22%

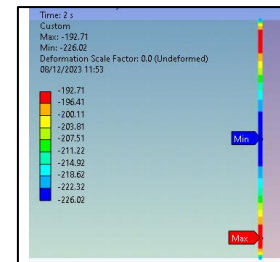
Plastic

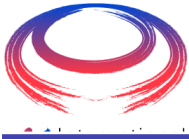
Elastic

L: opening\_CorrectCuTE MPC\_750layers\_plastic\_OnlyCuPlastic\_Hastelloy+SoftCu INSIDE\_HardCu+Hastelloy OUTSIDE\_Orthotropic\_1supportfrictionless\_FRICTIONLESS\_2D\_axisym\_1coil\_cor  
 X Axis - Normal Stress - All layer=1 - 3, s  
 Type: Normal Stress(X Axis)  
 Unit: MPa  
 Global Coordinate System  
 Time: 3 s  
 Custom Obsolete  
 Max: 77.203  
 Min: -415.95  
 Deformation Scale Factor: 56 (5x Auto)  
 06/12/2023 12:07



\*Average on the external edge





# Effect of the tape properties



step	$\sigma_x$ -radial[MPa]			$\epsilon_z$ -hoop
	min	max	ave	max
1	-291	-55	-208	
2	-264	-60	-171 (215*)	
3	-484	75	-218	0.24%
1	-289	-57	-210	
2	-224	-67	-164 (200*)	
3	-416	77	-213	0.30%

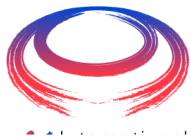
\*Average on the external edge

Experiments and FE modeling of stress–strain state in ReBCO tape under tensile, torsional and transverse load

To cite this article: K Ilin et al 2015 *Supercond. Sci. Technol.* **28** 055006

Reference



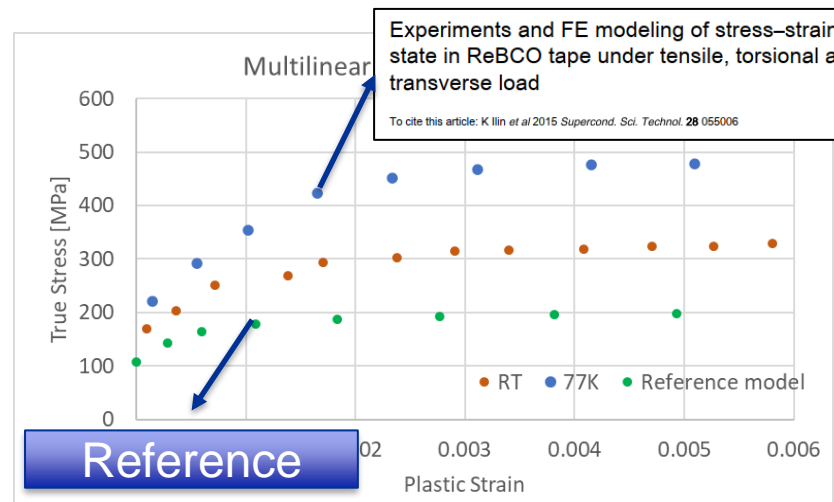


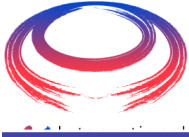
# Effect of the tape properties



step	$\sigma_x$ -radial[MPa]			$\epsilon_z$ -hoop
	min	max	ave	max
1	-291	-55	-208	
2	-264	-60	-171(215*)	
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1	-289	-57	-210	
2	-224	-67	-164 (200*)	
3	-416	77	-213	0.30%

\*Average on the external edge





# Effect of the tape properties

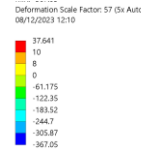
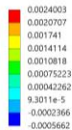


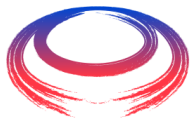
step	$\sigma_x$ -radial[MPa]			$\epsilon_z$ -hoop
	min	max	ave	max
1	-291	-55	-208	
2	-264	-60	-171(215)	
3	-484	75*	-218	0.24%

$\epsilon_z=0.24\%$  ✓

\*Localized effect

$\sigma_x \sim 10\text{MPa}$  ✓





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- Copper hard
- Copper tape
- Hastelloy
- Hastelloy ortho
- Hastelloy tape
- Shell

# Alternative Inner Joint-1

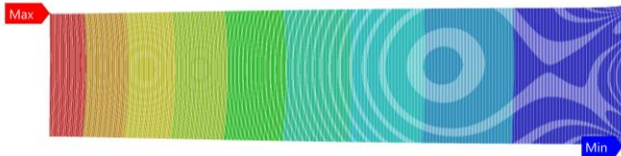
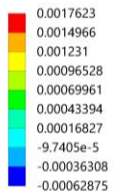


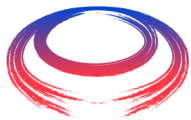
Hastelloy orthotropic	
Ex-radial[GPa]	Ey,z-hoop[GPa]
100	200



$\epsilon_z = 0.17\%$

$\sigma_x = 80\text{MPa}$



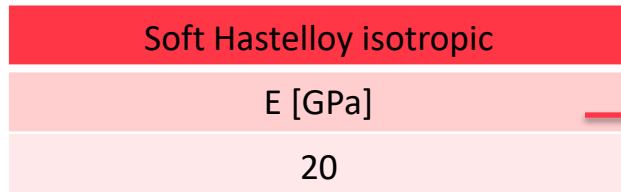


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# Alternative Inner Joint-2

- Copper hard
- Copper tape
- Hastelloy
- Hastelloy tape
- Shell

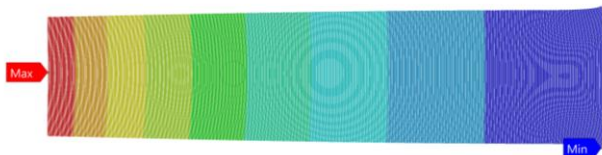
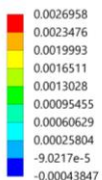


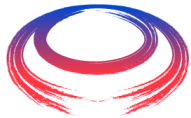
Model simplification, important to have a 3D design of the inner ring to take into account the real stiffness of the structure



$$\epsilon_z = 0.27\% \quad \checkmark$$

$$\sigma_x = 12\text{MPa} \quad \checkmark$$





# Shrink Fitting

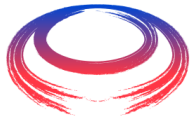


- Coil surrounded by a cylindrical shell with  $r_{in} < r_{ext\_coil}$
- Shell is pre-heated → fitting of the coil inside → cool-down of the shell and thermal contraction
- Simple analytical evaluation: 600MPa → 200MPa → interference gap ~300μm → ~250°C

$$\sigma_{\theta} = -\frac{\rho^2 + \beta^2}{\rho^2} \frac{1}{1 - \beta^2} P_e$$

$$\delta = \delta_{i2} - \delta_{e1} = \left[ \frac{1}{E_2} \left( \frac{1 + \beta_2^2}{1 - \beta_2^2} + \nu_2 \right) + \frac{1}{E_1} \left( \frac{1 + \beta_1^2}{1 - \beta_1^2} - \nu_1 \right) \right] r_{e1} P_f$$

- Some practical aspects must be considered:
  - Differential contraction during cooldown
  - Strength of the cylinder
  - Impact of the joints
  - Plasticity
  - Mechanical tolerances: 2MPa/μm lost**
  - Buckling**
- FEM simulations at different levels of complexity

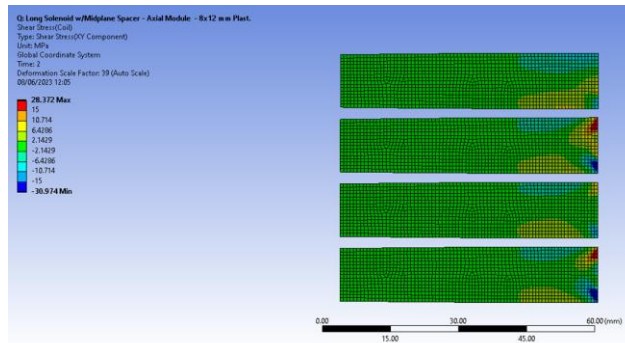
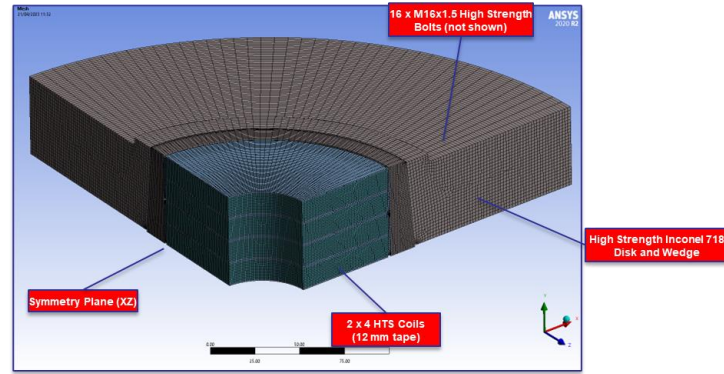


# Mechanical considerations - Second concept



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- 2 Load Steps:
  - Shrink Disk displacement (5 mm)
  - Energization
- Max. Hoop Stress (after energization): 620.4 MPa
- Max. Hoop Strain (after energization): 0.344 %
- Shear Stresses globally lower than 15 MPa
- However, locally they can reach after energization  $\sim |30|$  MPa

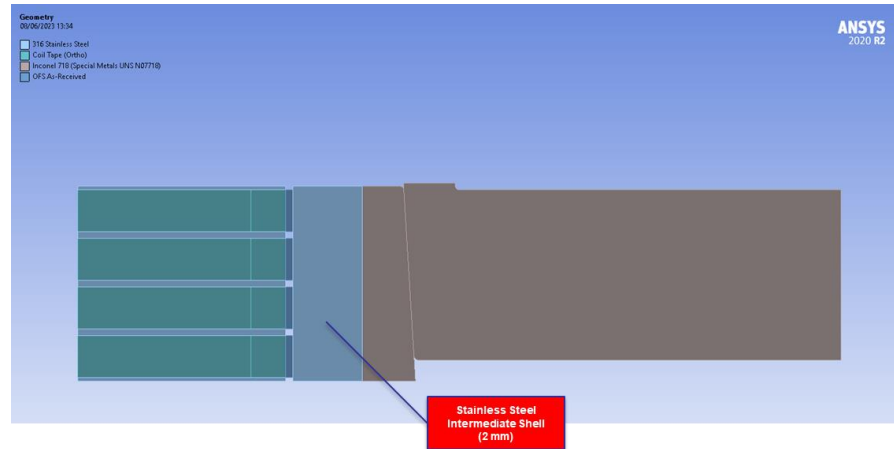




# Mechanical considerations - Third concept



- To limit shear stresses, an intermediate steel shell is added (ID 184 mm; OD 224 mm)
- ~ 150  $\mu\text{m}$  interference with coil pack created by differential heating
- 3 Load Steps: 1. Shell/Coil Interference; 2. Shrink Disk Displacement (2.2 mm); 3. Energization
- Min. Hoop Stress after shrinking: -426 MPa
- Max. Hoop Stress after energization: 598 MPa
- Max. Hoop Strain after energization: 0.332 %
- Local peak shear stress ~ 10 MPa
- Max Shear after energization |9.2| MPa





# Mechanical considerations - Third concept



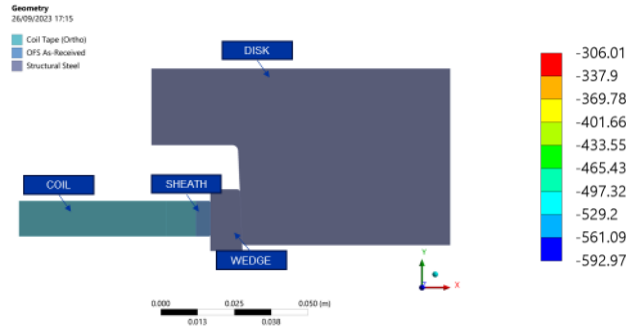
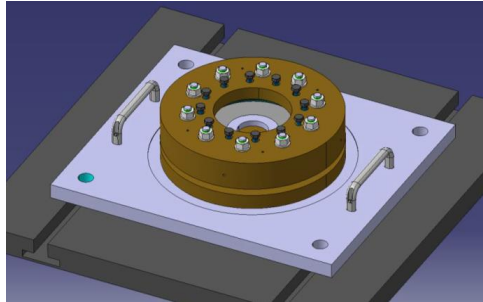
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- Local peak shear stress ~ 10 MPa
- Max Shear after energization |9.2| MPa

REBCO conductor	
Axial tensile stress	700MPa
Axial tensile strain	0.4%
Transverse compressive stress	>100MPa
Transverse tensile stress	10-100MPa
Max shear stress	>19MPa

- Preliminary is ok, but **limited safety margins** → Fundamental to have a good understanding of the **material limits** and **failure mode**



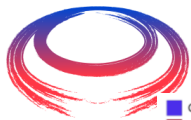
# Testing



- $\sigma_{hoop} \sim -600\text{MPa}$  reached on the inner radius of the coil
- The required compression is achieved with 10 M16 bolts
- System equipped with strain gauges and digital image correlation to characterize the coil

# Conclusion and next step

- The final cooling solenoid requires a pre-compression to operate at 40T:
  - Shrink fitting, mechanical jigs or a combined solution can provide the required pre-compressions
  - Tape properties impacting the results → important to benchmark them with experimental tests
  - The design of the inner and outer rings is critical: 2 possible solutions identified, more modelling work is needed to finalize the design
  - Different FEM models ready to investigate more options
  - Extensive work of design of the tooling for the experimental characterization of the tape



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- Coil material (Hastelloy\_50+Copper\_30)
- Copper hard
- Copper soft
- Hastelloy
- Shell

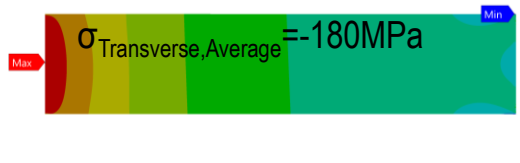
# Validity of homogeneous model



Step 1: Shrink fitting (T external shell =250°C)

$$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$$

Step 2: Cool-down

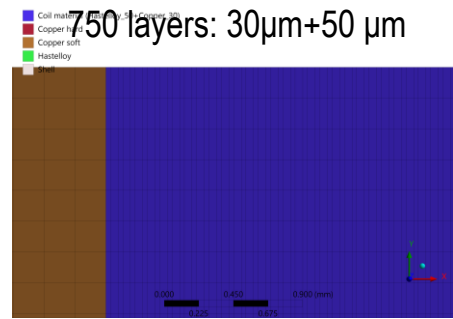


- 69.014
- 94.643
- 120.27
- 145.9
- 171.53
- 197.16
- 222.79
- 248.42
- 274.04
- 299.67

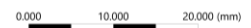
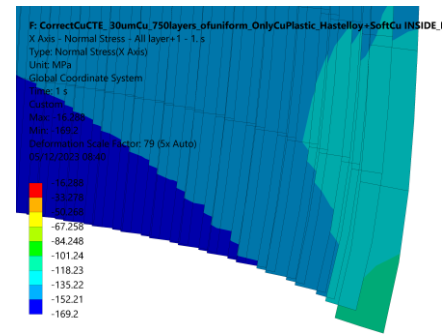
Step 3: Energization



- 59.761
- 0
- 70.094
- 140.19
- 210.28
- 280.38
- 350.47
- 420.56
- 490.66
- 560.75



$$\sigma_{\text{Transverse,Average}} = -85\text{MPa}$$



oup, 14/12/2023



International  
Collaboration

- Coil material (Hastelloy\_50+Copper\_30)
- Copper hard
- Copper soft
- Hastelloy
- Shell

# Validity of homogeneous model



Step 1: Shrink fitting (T external shell =250°C)

$$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$$

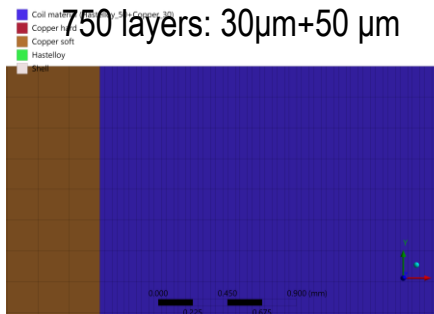
Step 2: Cool-down

$$\sigma_{\text{Transverse,Average}} = -180\text{MPa}$$

Step 3: Energization

$$\sigma_{\text{Transverse,Average}} = -215\text{MPa}$$

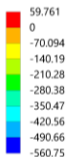
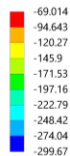
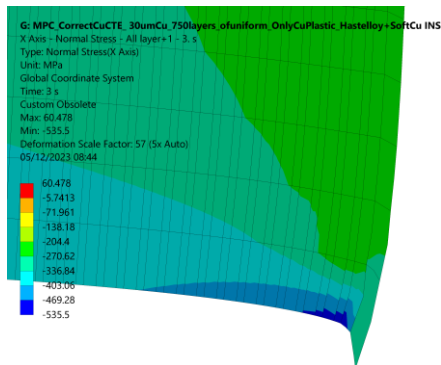
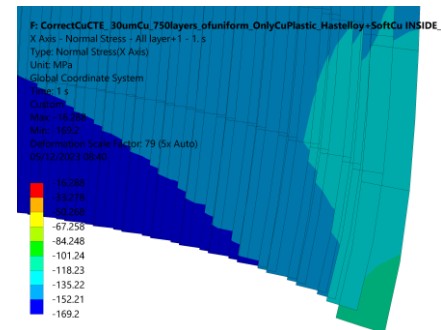
750 layers: 30 $\mu\text{m}$ +50  $\mu\text{m}$



$$\sigma_{\text{Transverse,Average}} = -85\text{MPa}$$

MPC CONTACT

$$\sigma_{\text{Transverse,Average}} = -215\text{MPa}$$



cup, 14/12/2023