


Benchmarks on Double Higgs production for Singlet Extension



Miguel Angel Soto Alcaraz
Collaborating with: I. Lewis; M. Sullivan; J. Scoot

Particle Physics on the plains
October 14th 2023

Going beyond the Standard Model of Elementary Particles

	three generations of matter (fermions)			interactions / force carriers (bosons)	
	I	II	III		
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 124.97 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
	u up	c charm	t top	g gluon	H higgs
	d down	s strange	b bottom	γ photon	
	e electron	μ muon	τ tau	Z Z boson	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	

QUARKS (left side of fermion table)

LEPTONS (left side of fermion table)

GAUGE BOSONS VECTOR BOSONS (bottom center)

SCALAR BOSONS (right side)

- Many open questions:
 - Dark Matter?
 - Neutrino masses?
 - Baryon asymmetry?

$m=?$

0

0

S

Higgs 2

Help in further understanding of EW phase transition

Model Extension

- The simplest extension is the addition of a gauge real singlet $S = s + x$

$$V(H, S) = -\mu^2 H^\dagger H + \lambda (H^\dagger H)^2 + \frac{a_1}{2} H^\dagger H S + \frac{a_2}{2} H^\dagger H S^2 \\ + b_1 S + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4.$$

- Only coupling to Higgs doublet H , with neutral component having a vev of

$$\langle \phi_0 \rangle = \frac{v}{\sqrt{2}} = v_{\text{EW}} = 246 \text{ GeV}$$

- EWSB at the minimum of potential

$$0 = \frac{v}{2} (-2\mu^2 + 2\lambda v^2 + a_1 x + a_2 x^2)$$

$$0 = x \left(b_2 + b_3 x + b_4 x^2 + \frac{a_2 v^2}{2} \right) + b_1 + \frac{a_1 v^2}{4}$$

- The possible minimums for (v, x) are

$$(v_{EW}, 0), \quad (v_{\pm}, x_{\pm}), \quad (0, x_{1,2,3})$$

- Only real minimums interested
- One by construction and the other analytically

FREE PARAMETERS

- From $(v, x) = (v_{EW}, 0)$, it is found

$$\mu^2 = \lambda v_{EW}^2, \quad b_1 = -\frac{v_{EW}^2}{4} a_1$$

- Rewrite in terms of the mass eigenstates. If $U = (h \ S)$

$$V_m = \frac{1}{2} U M^2 U^T \quad \Rightarrow \quad \begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = R(\theta)^T U^T,$$

- The next constraints can be found

$$a_1 = \frac{m_1^2 - m_2^2}{v_{EW}} \sin 2\theta, \quad \lambda = \frac{m_1^2 \cos^2 \theta + m_2^2 \sin^2 \theta}{2v_{EW}}.$$

$$b_2 = m_1^2 \sin^2 \theta + m_2^2 \cos^2 \theta - \frac{a_2 v_{EW}^2}{2},$$

More Constraints

- Vacuum Stability yields

$$V^{(4)} = 4\lambda\phi_0^4 + 2a_2\phi_0^2s^2 + b_4s^4 > 0 \Rightarrow a_2 \geq -2\sqrt{\lambda b_4}.$$

- The following couplings terms will be used

$$V \supset \frac{\lambda_{211}}{2} h_2 h_1^2 + \frac{\lambda_{2222}}{4!} h_2^4$$

- First for h_2 decay, and the second for limit in b_4

- Partial width at tree level decay is given by

$$\Gamma(h_2 \rightarrow h_1 h_1) = \frac{\lambda_{211}^2}{32\pi m_2} \sqrt{1 - \frac{4m_1^2}{m_2}}, \quad \Rightarrow \quad m_2 \geq 2m_1$$

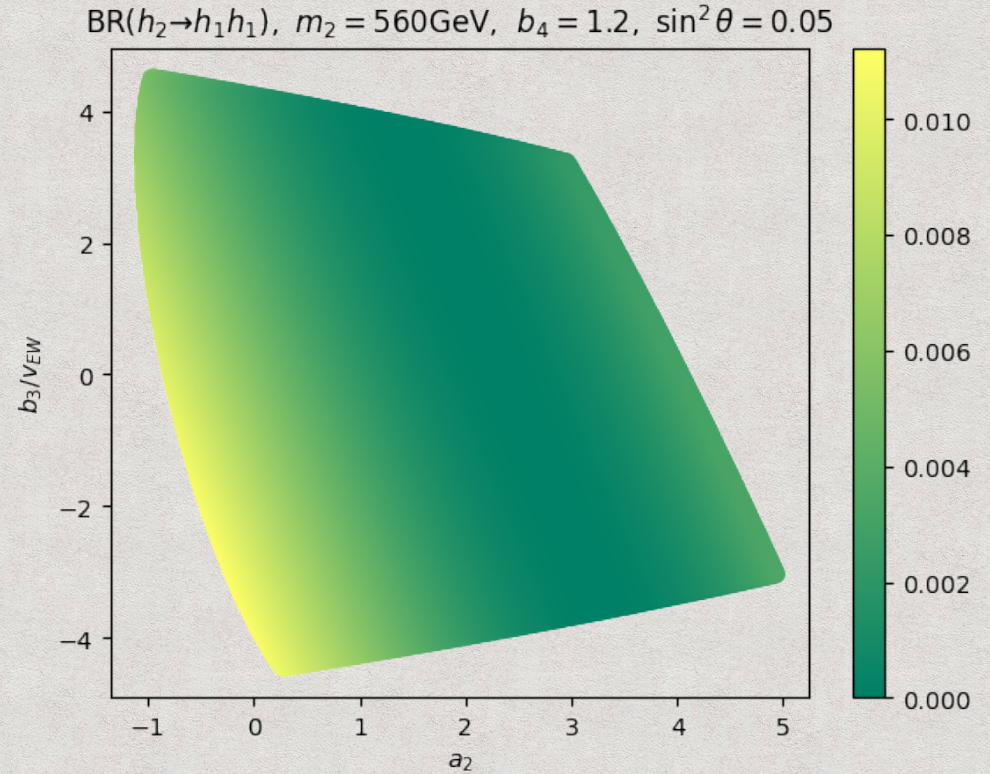
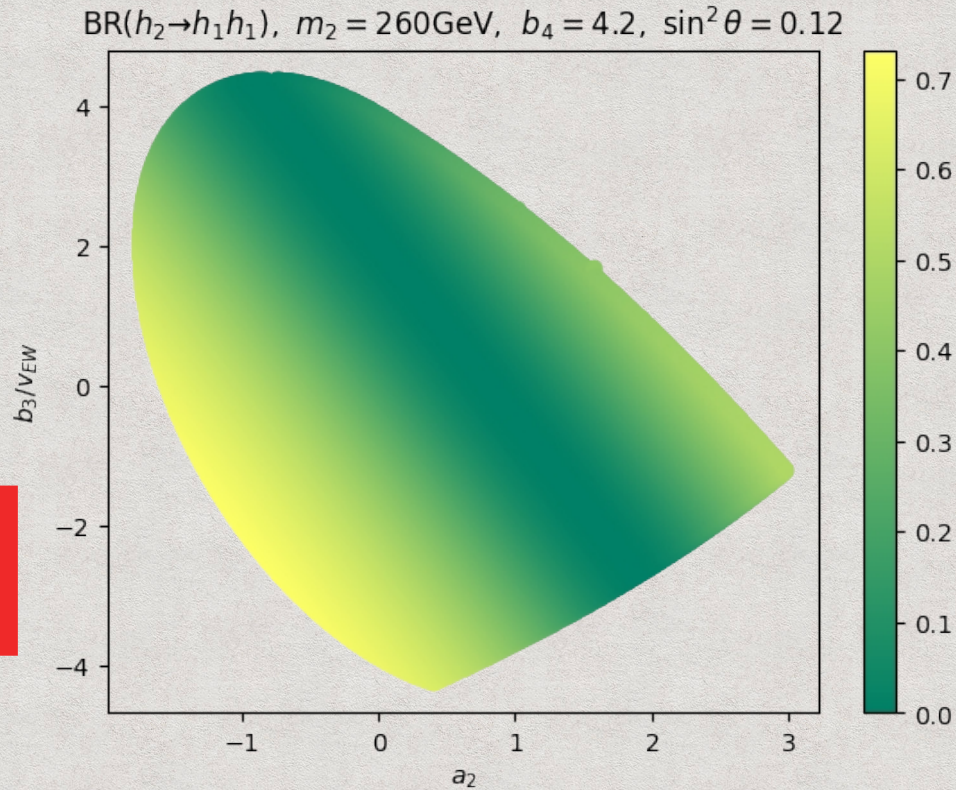
- From the scattering $h_2 h_2 \rightarrow h_2 h_2$, perturbative unitarity is used

$$\mathcal{M} = 16\pi \sum_i (2i + 1) a_i P_i(\cos \theta), \quad \lambda_{2222} = 6b_4 + \mathcal{O}(\theta^2)$$

- With restriction of $|a_0| \leq 1/2$

$$a_0 = \frac{3b_4}{8\pi}, \quad \Rightarrow \quad b_4 \leq 4.2$$

Valid a_2 and b_3 for some values of free parameters



For given angle and mass, max area with $b_4 = 4.2$

PRODUCTION

- Results must agree with

$$\text{BR}(h_1 \rightarrow f_{\text{SM}}) = \text{BR}_{\text{SM}}(h_1 \rightarrow f_{\text{SM}})$$

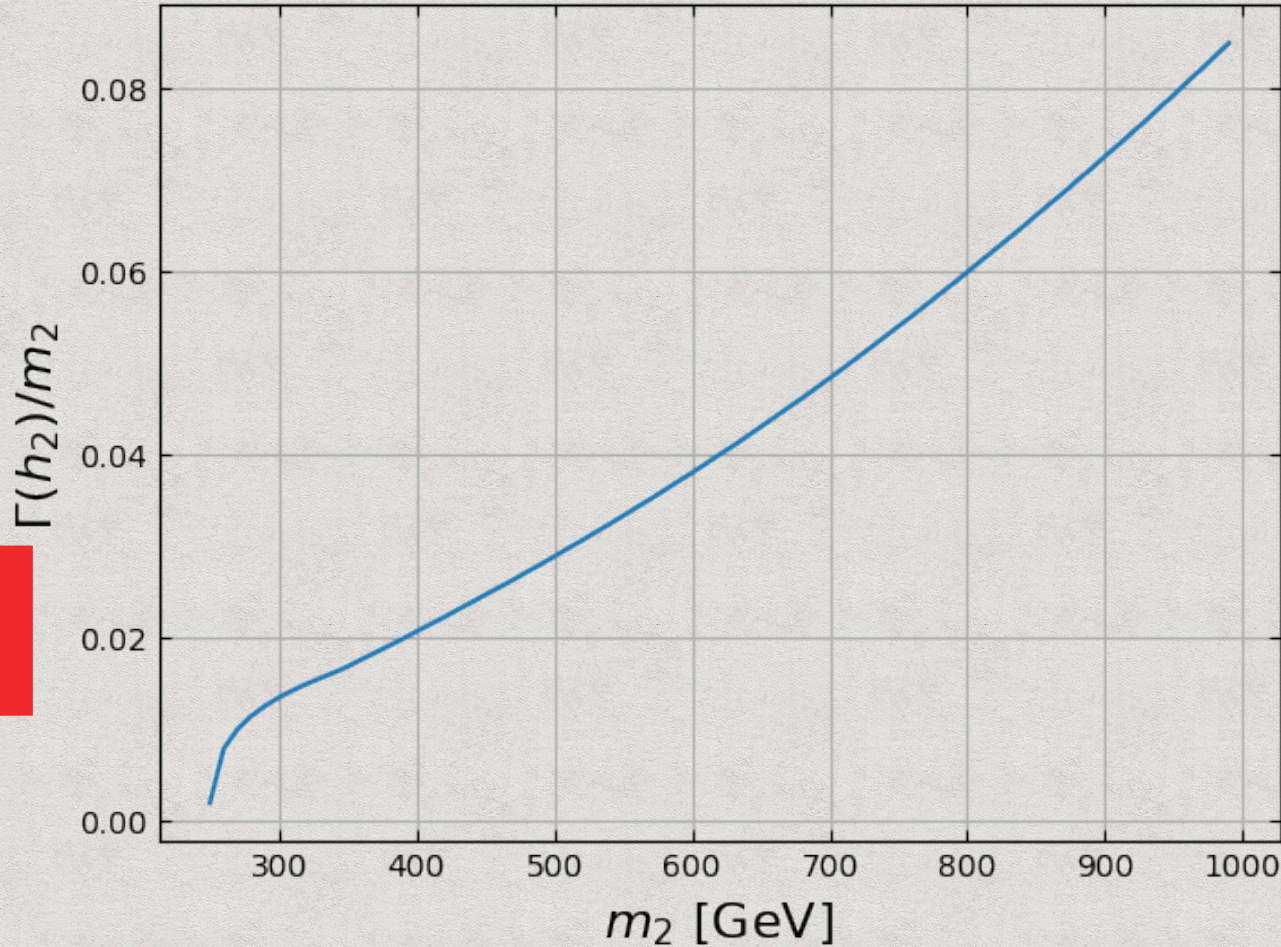
- While BR are suppressed by a factor of $\sin^2 \theta$

$$\Gamma(h_2 \rightarrow f_{\text{SM}}) = \sin^2 \theta \Gamma_{\text{SM}}(h_2 \rightarrow f_{\text{SM}})$$

- Leading to a total width of

$$\Gamma(h_2) = \Gamma(h_2 \rightarrow h_1 h_1) + \Gamma(h_2 \rightarrow f_{\text{SM}})$$

- With $\Gamma(h_2 \rightarrow f_{\text{SM}})_{\text{SM}}$ being the SM Higgs decay with mass m_2



Ratio between maximum width and mass, sticking to the previous constraints.

Fair to use then

$$\Gamma(h_2) \leq 0.1m_2$$

Allowing to do Narrow width approximation

- Due to last constraint, a narrow width approximation can be used

$$\sigma(pp \rightarrow h_2 \rightarrow h_1 h_1) \approx \sigma(pp \rightarrow h_2) \text{BR}(h_2 \rightarrow h_1 h_1)$$

- Due to mixing with Higgs, couplings to SM fermions and gauge boson proportional to $\sin \theta$

$$\sigma(pp \rightarrow h_2) = \sin^2 \theta \sigma_{\text{SM}}(pp \rightarrow h_2)$$

- Maximization of production

$$\frac{\sigma(pp \rightarrow h_2 \rightarrow h_1 h_1)}{\sigma_{\text{SM}}(pp \rightarrow h_2)} \approx \sin^2 \theta \text{BR}(h_2 \rightarrow h_1 h_1)$$

- Current constraints given by ATLAS $\sin^2 \theta \leq 0.12$
- Future Collider benchmarks so far given by:

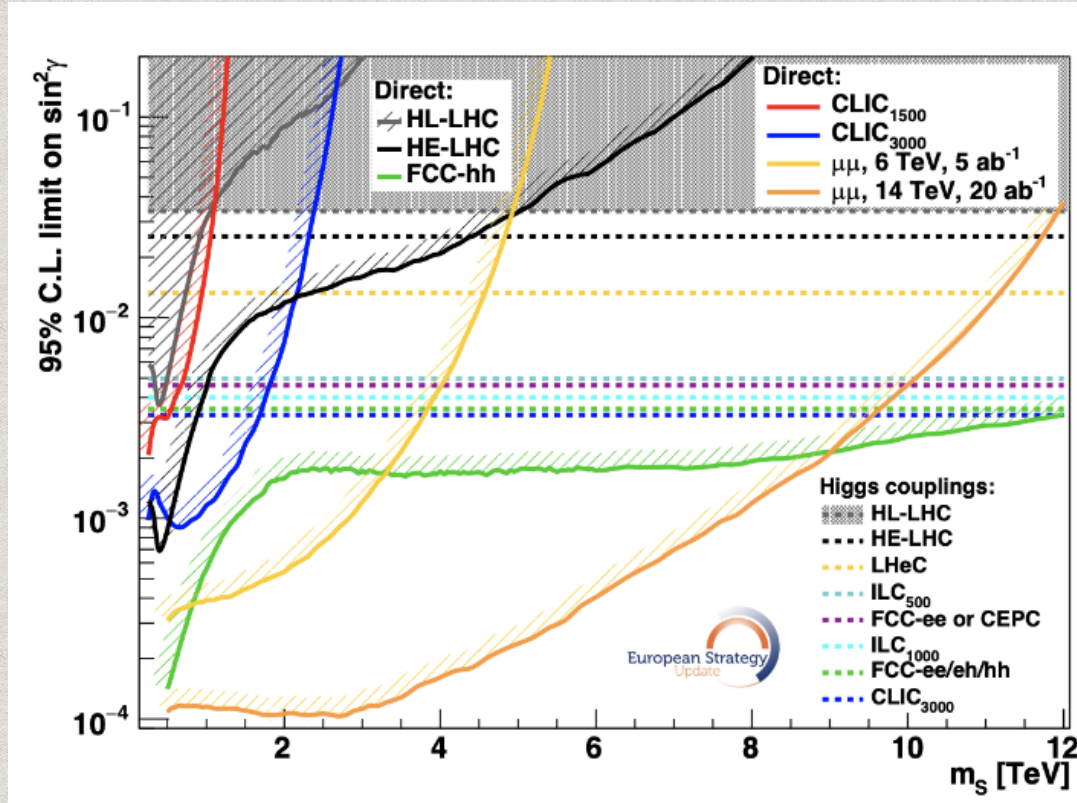
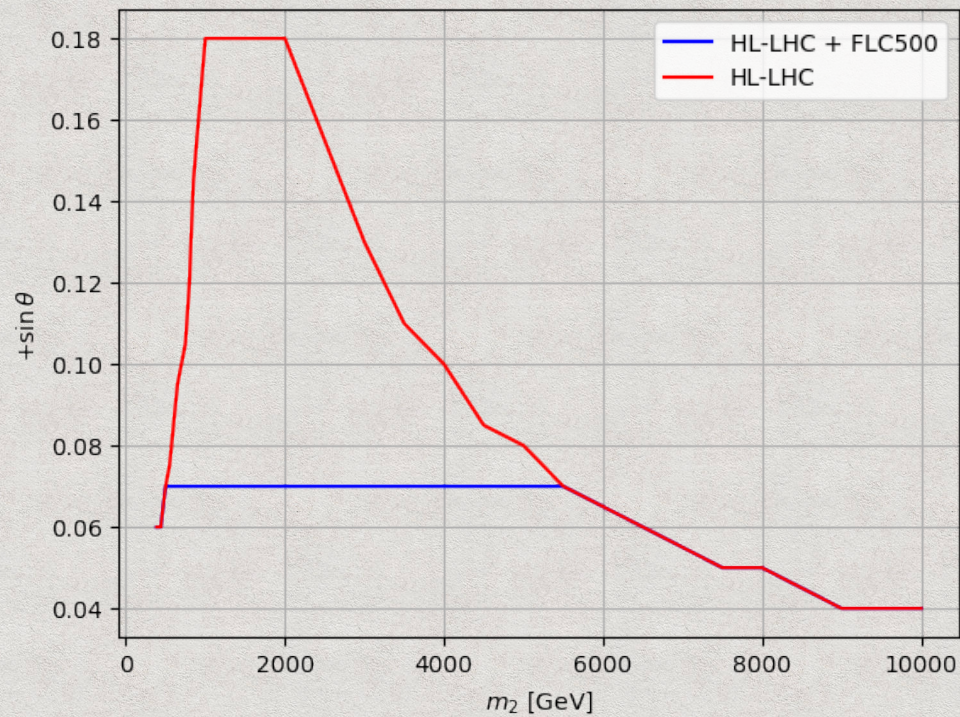
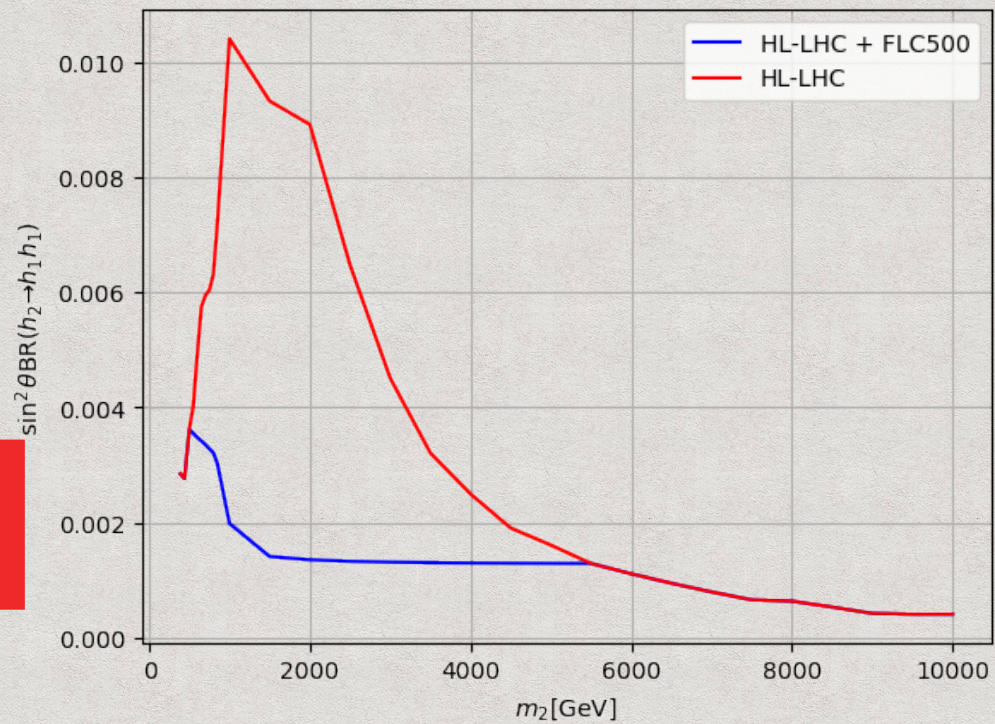


Figure taken from:
arXiv:1910.11775 [hep-ex].

Benchmarks for some future colliders



- **Finale:**
- Add real gauge singlet to model
- Identify free parameters and make scan
- Maximize production rate
- **What's next?**
- Use new data to apply further constraints to $\sin \theta$



Coming soon...?