



by Cari Cesarotti

# $\mu$ TRISTAN

Ryuichiro Kitano (KEK)

Based on 2201.06664, Yu Hamada (KEK -> DESY), RK, Ryutaro Matsudo (KEK -> NTU),  
Hiromasa Takaura (KEK -> YITP), Mitsuhiro Yoshida (KEK)

2210.11083, Yu Hamada (KEK -> DESY), RK, Ryutaro Matsudo (KEK -> NTU),  
Hiromasa Takaura (KEK -> YITP)

2304.14020, Kåre Fridell (KEK/Florida State U.), RK, Ryoto Takai (KEK/Sokendai)

Also, study in progress with Koji Nakamura (KEK), Sayuka Kita (Tsukuba U.),  
Toshiaki Kaji (Waseda U.), Taiki Yoshida (Waseda U.), Kohei Yorita (Waseda U.)

**MuC physics benchmark workshop@Pittsburgh, November 16-18, 2023**

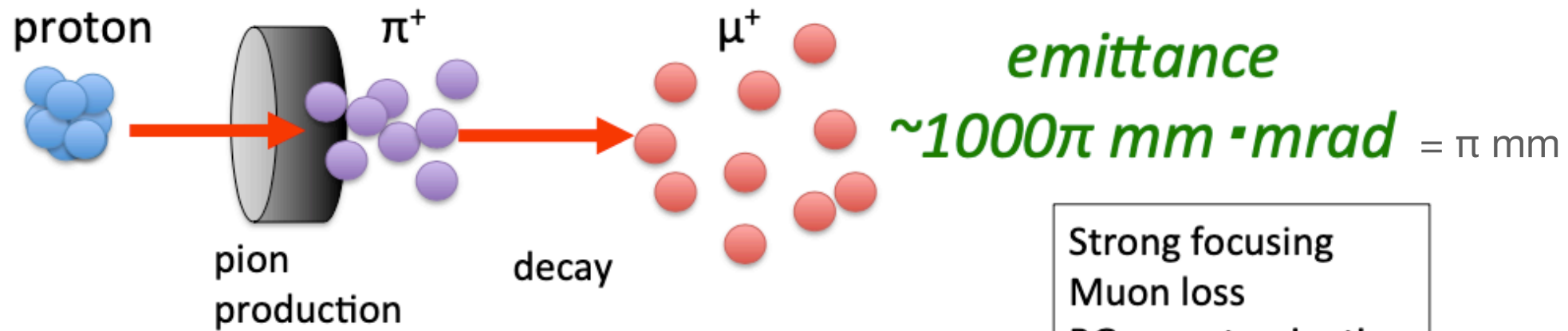
Today, I talk about possibly a realistic scenario of  $\mu^+$  based colliders.

As you know, the most important (difficult) part of muon colliders is to obtain enough **luminosity** for particle physics.

# Muon beam

## Conventional muon beam

Too much spread.



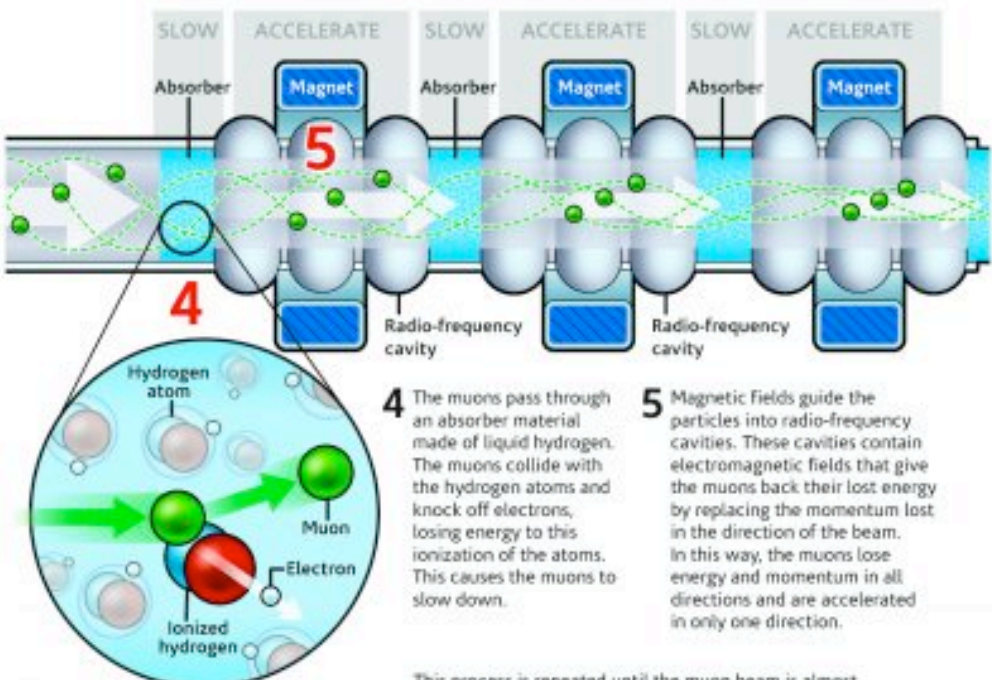
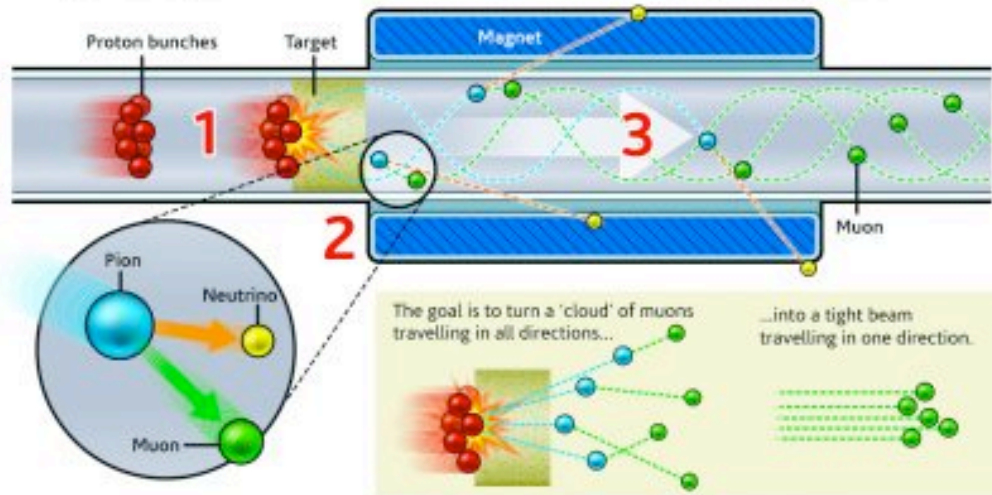
Taken from Mibe-san's lecture slide

# Muon cooling

## MICE Muon Ionization Cooling Experiment

MICE has made the first ever demonstration of the ionization cooling of muons – a major step in the journey to create the world's most powerful particle accelerator.

- 1 Bunches of protons are accelerated into a target of dense material (such as tungsten or mercury). The atoms within the target emit a particle called a pion.
- 2 Pions are unstable and they quickly decay into a muon and a neutrino.
- 3 The neutrinos, being virtually massless and without charge, pass out of the experiment. Magnets direct charged muons of the correct energy moving in the right direction.

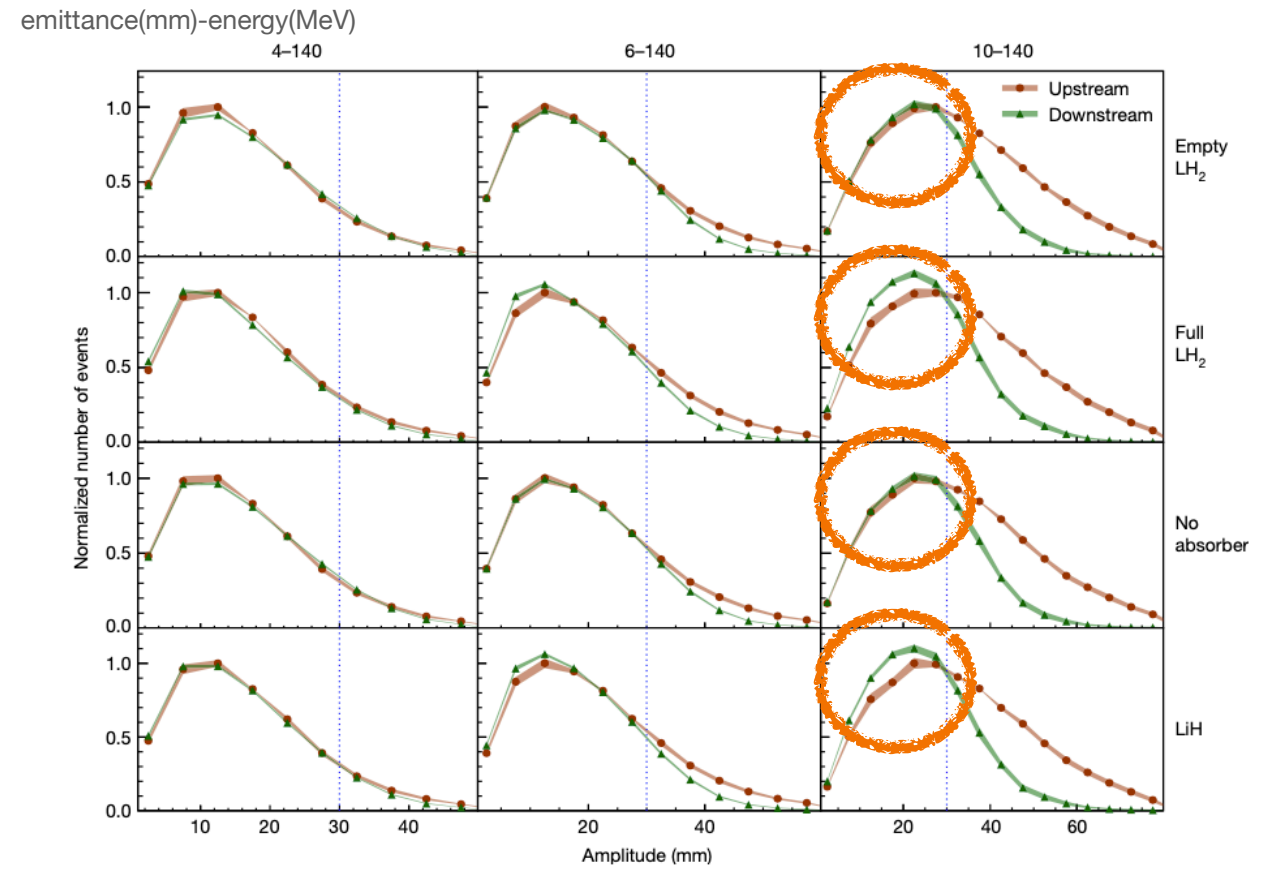


Infographic: STFC, Ben Gilliland

This process is repeated until the muon beam is almost laser-like, ready for injection into the main accelerator.

Principle works.

[Nature 2020, MICE collaboration]



simulation and plan for muon cooling of the MAP design

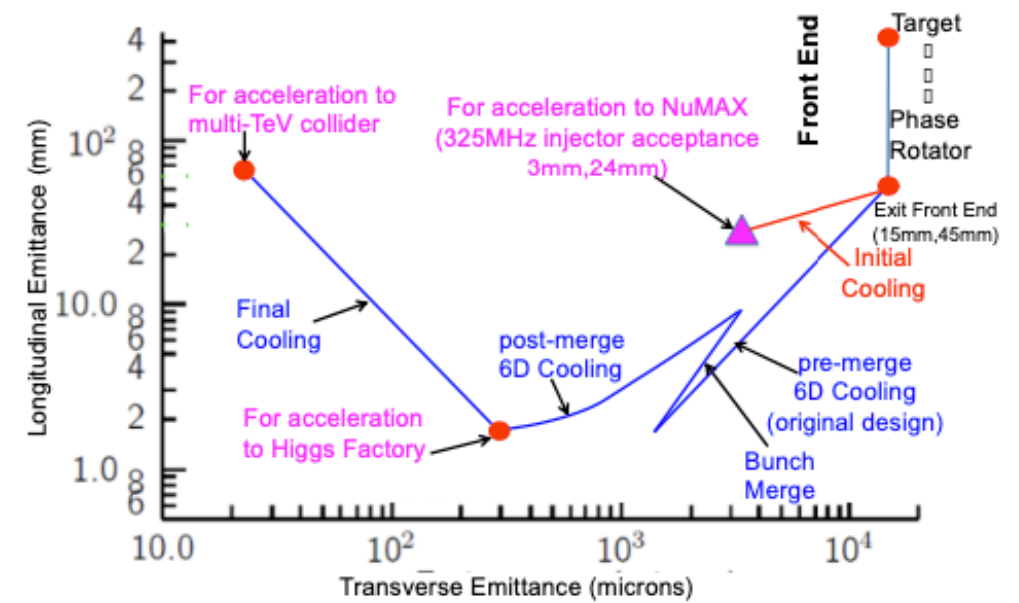


Figure 3. Ionization Cooling path in the 6D phase space.

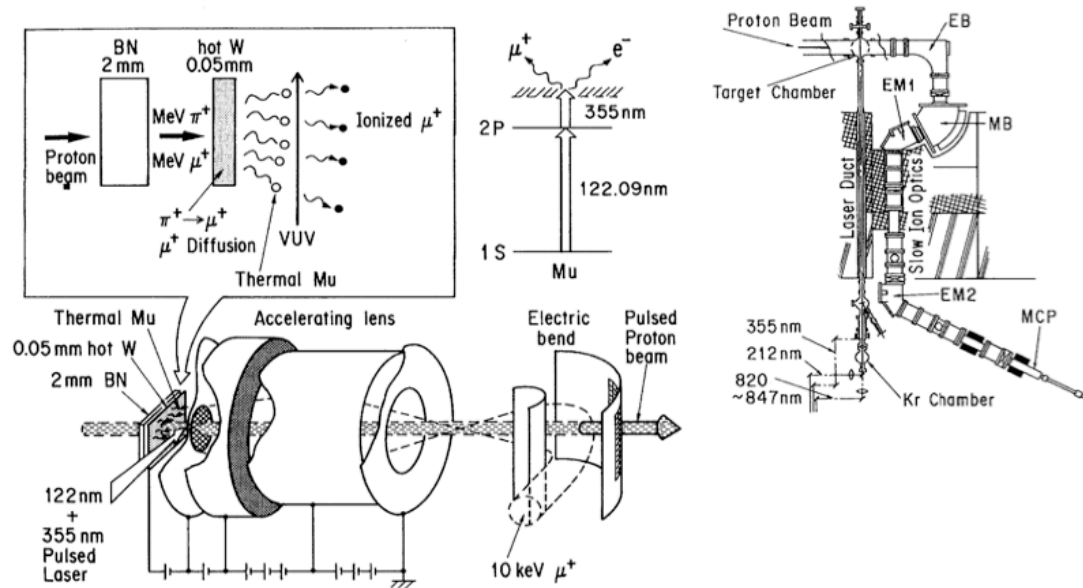


# Muon cooling which works for $\mu^+$

There is a rather matured(?) technology only works for  $\mu^+$ .

Ultracold muon technology

[K.Nagamine et al. 1995]



## ミュオンg-2/EDMと極冷ミュオンビーム

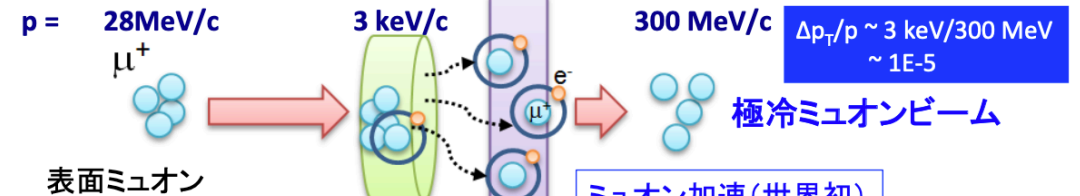
J-PARCで行う新しいミュオンg-2/EDM精密測定 [www.g-2.kek.jp](http://www.g-2.kek.jp)

- BNLが報告した標準模型からのズレ(3 $\sigma$ )の検証(0.1ppm)
- 全く新しいコンセプトで主要系統誤差要因を払拭
  - ゼロ電場
  - コンパクトな蓄積磁石(0.7 m  $\ll$  14 m)
- 通常に比べてエミッタンスが1/1000程度小さいミュオンビーム (極冷ミュオンビーム) が必須

ミュオニウムMu ( $\mu^+e^-$ )のレーザー共鳴イオン化

Nagamine et al. PRL 74 (1995)  
P. Bakule et al. INM B266(2008)

Laser 122nm, 355nm



ミュオニウム生成・放出

従来 : 高温金属(タングステン箔)  
本研究: シリカエアロゲルを用いて  
室温で高効率生成に成功

This has been the key technology for the J-PARC muon g-2 experiment.

ultra-cold muon is here. ●

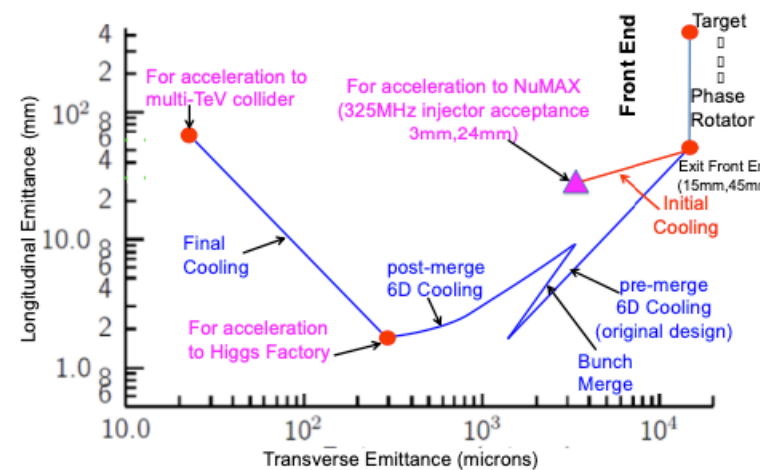


Figure 3. Ionization Cooling path in the 6D phase space.

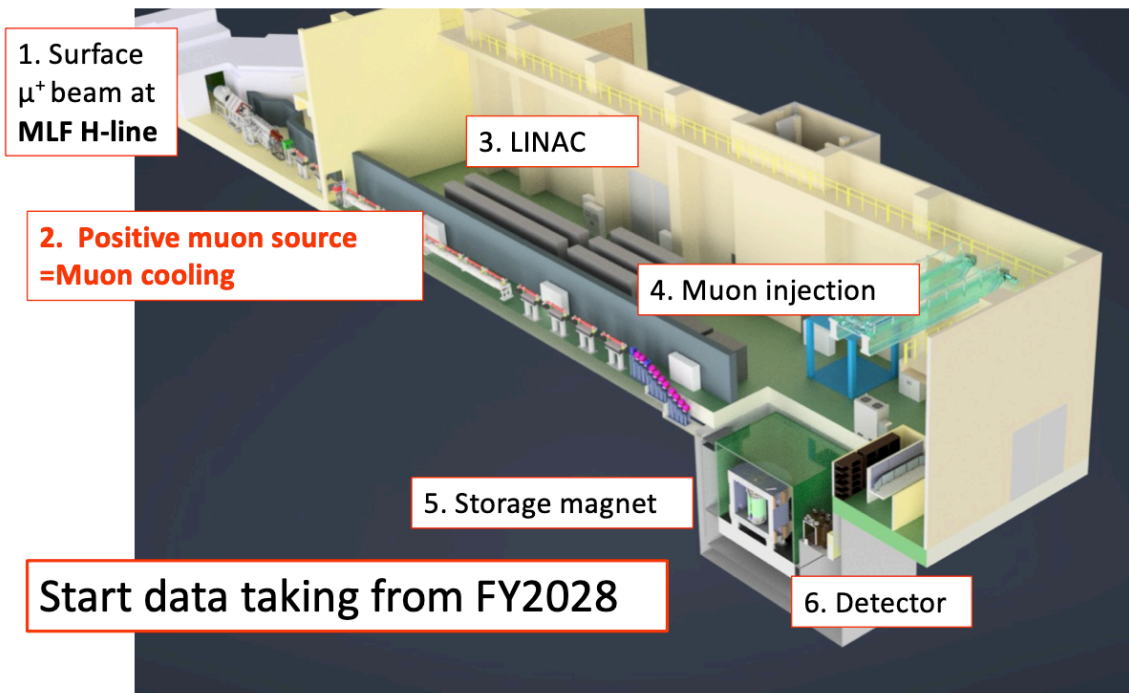
Mibe-san's slide

Looks like there is a good chance of realizing a low-emittance  $\mu^+$  beam!

# g-2/EDM experiment @ KEK J-PARC

## Muon g-2/EDM experiment at J-PARC

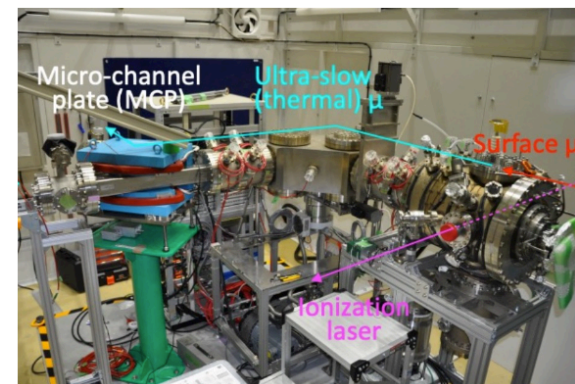
A new muon g-2/EDM measurement featuring a low emittance  $\mu^+$  beam



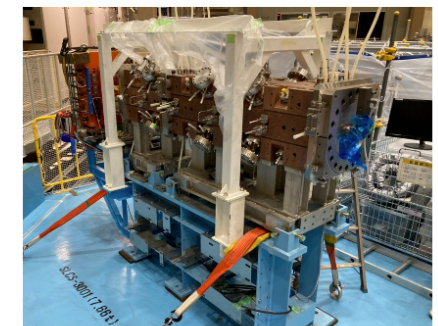
## Demonstration @ MLF S-line

- Collaborating with Muonium 1S-2S spectroscopy experiment.
  - A 244-nm pulsed laser developed by Okayama univ.
- Q-scan measurement is underway to evaluate the initial phase space.
- RFQ acceleration of cooled muon will be performed after in 2024.

MCP for counting event rate & Beam profile monitor to measure USM beam size after extraction



World 1st acceleration of USM will be performed soon



21

S. Kamioka (talk@muon acceleration workshop, Nov. 2, 2023)

Yes, it has already been cooled and to be accelerated soon!!

(Actually, the acceleration of the  $\mu^+e^-e^-$  bound state has already been demonstrated!!)

# $\mu$ TRISTAN

$\mu^+e^-/\mu^+\mu^+$  collider with 1 TeV  $\mu^+$  beam.

**PTEP**

Prog. Theor. Exp. Phys. **2022** 053B02(16 pages)  
DOI: 10.1093/ptep/ptac059

30 GeV  $e^-$  / 1 TeV  $\mu^+$  : Higgs factory,  $\sqrt{s}=346\text{ GeV}$   
1 TeV  $\mu^+$  / 1 TeV  $\mu^+$  : new physics search,  $\sqrt{s}=2\text{ TeV}$

## $\mu$ TRISTAN

Yu Hamada<sup>1</sup>, Ryuichiro Kitano<sup>1,2</sup>, Ryutaro Matsudo<sup>1</sup>, Hiromasa Takaura<sup>1,\*</sup>, and Mitsuhiro Yoshida<sup>2,3</sup>

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<sup>2</sup>Graduate University for Advanced Studies (Sokendai), Tsukuba 305-0801, Japan

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The ultra-cold muon technology developed for the muon  $g-2$  experiment provides a low-emittance  $\mu^+$  beam which can be accelerated and used for experiments. We consider the possibility of new collider experiments by  $\mu^+$  beam up to 1 TeV. Allowing the  $\mu^+$  beam to collide with a high-intensity TRISTAN energy,  $E_{e^-} = 30\text{ GeV}$ , in a storage ring with the same size as TRISTAN (circumference of 3 km), one can realize a collider experiment with the center-of-mass energy  $\sqrt{s} = 346\text{ GeV}$ , which allows the production of Higgs bosons through vector boson fusion processes. We estimate the deliverable luminosity with existing accelerator technology.  $\mu^+\mu^+$  colliders up to  $\sqrt{s} = 2\text{ TeV}$  are also possible using the same storage ring. They have the capability of producing the superpartner of the muon up to TeV energy.

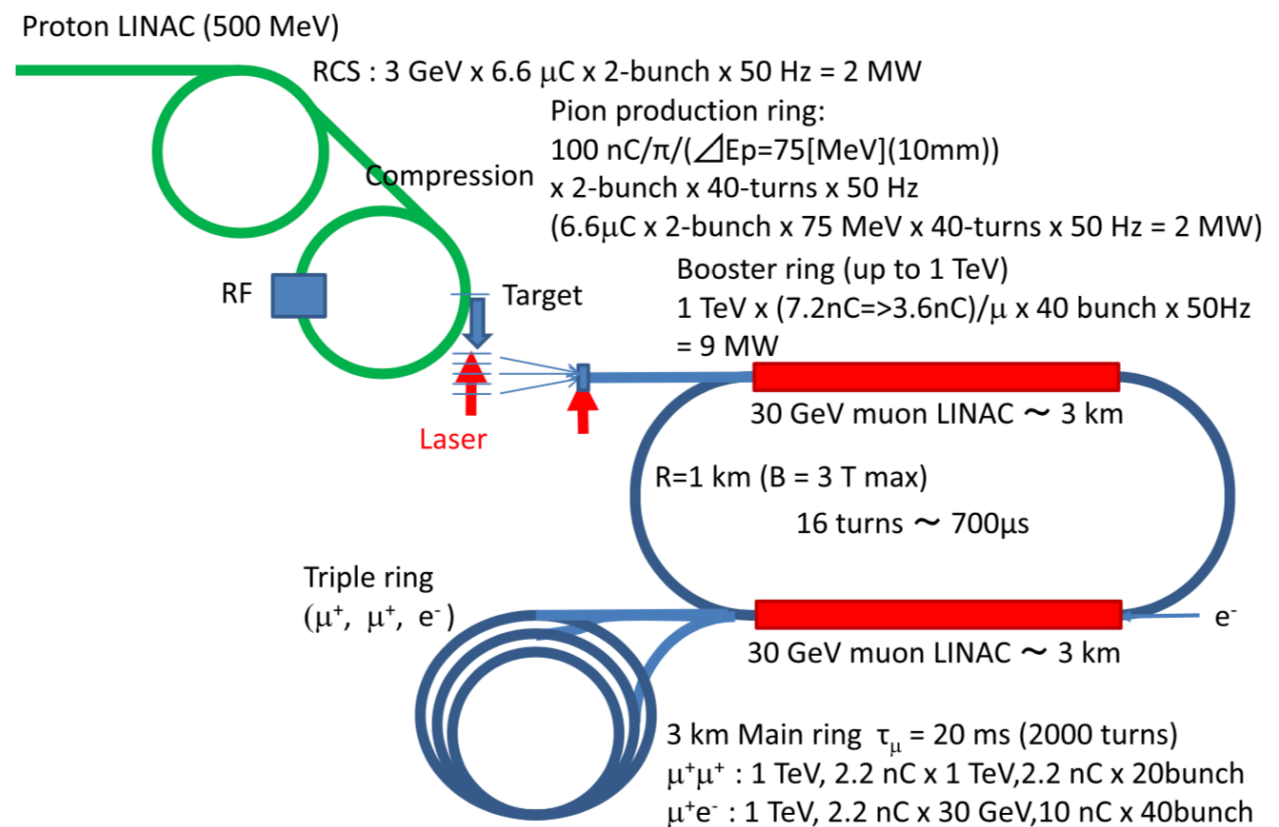


Fig. 1. Conceptual design of the  $\mu^+e^-/\mu^+\mu^+$  collider.



# How many cold muons?

1/(20ms) where 20ms is the lifetime of the 1TeV muon

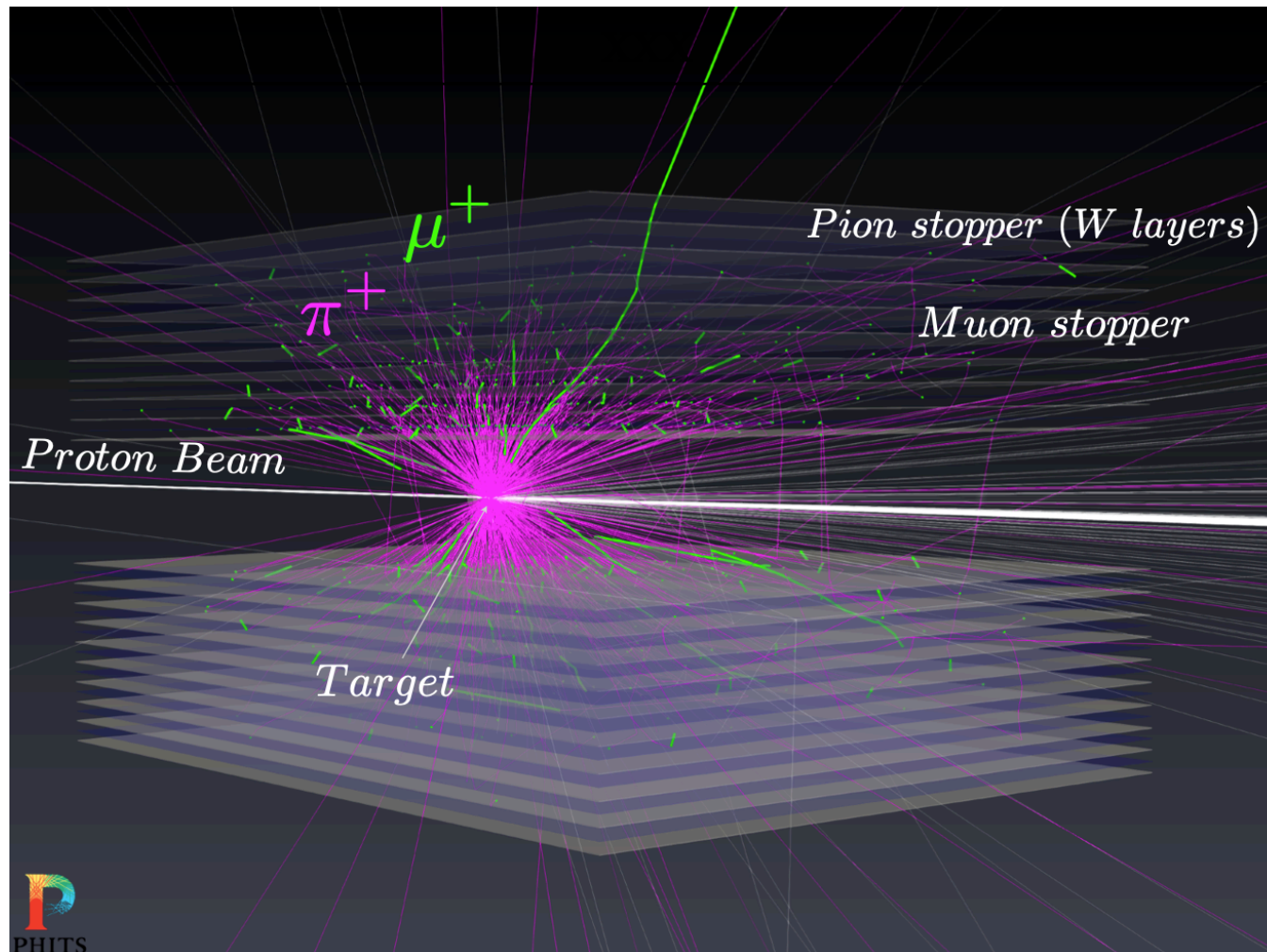
J-PARC like proton driver:  $6.6 \mu\text{C} * 50 \text{ Hz} * 2 \text{ bunches} = 4.1 \times 10^{15} \text{ protons/s}$

pion production target: 40 hits/bunch 0.016  $\pi^+$ /proton  $2.6 \times 10^{15} \pi^+$ /s

pion stopping target: 0.5 stopping efficiency \* 0.07 muons/ $\pi^+$   $9 \times 10^{13} \mu^+$ /s

simulation: (Yoshida, Sakaki ... in progress)

$10^5$  larger than J-PARC MLF.  
Super muon factory!



(Thermal muon production rate)  
 = (Muon stopping number on the layers)  
 × (MC correction for pion production)  
 × (Muonium formation)  
 × (Vacuum yield)  
 × (Loss of muoniums due to the decay)  
 =  $1.4 * 10^{-3} \mu/p$   
 →  **$2.4 * 10^{14} \mu/s$**  (J-PARC RCS:  $6.6 \mu\text{C}$ , 2bunch 40 turns)

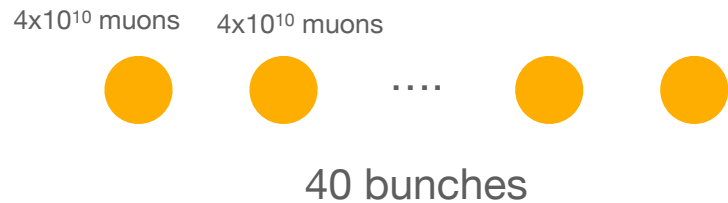
PTEP 2022 (2022) 5, 053B02

**$O(10^{13} \mu/s)$  will be available for collider experiment**



# Luminosity?

$$6.6 \mu\text{C} \times 2 \times 0.016 \times 0.5 \times 0.07 \sim 7 \text{ nC} / \text{bunch} \sim 4 \times 10^{10} \text{ muons/bunch}$$



accelerate up to 1TeV → bunch charge reduced to half by decay  
 storage ring → 2000 turns. further reduced by half

$$N_\mu \sim 10^{10} \quad N_e \sim 6 \times 10^{10}$$

$$\sigma \sim 2\text{-}3 \mu\text{m} \quad (\beta^* \sim \text{cm})$$

$$f_{\text{rep}} \sim (c/3\text{km}) \times 40 \text{ bunches} \\ \sim 100 \text{ kHz} \times 40 \text{ bunches} = 4 \text{ MHz}$$

storage ring  
 1μs for one turn.  
 2000 turns before next beam  
 is coming.

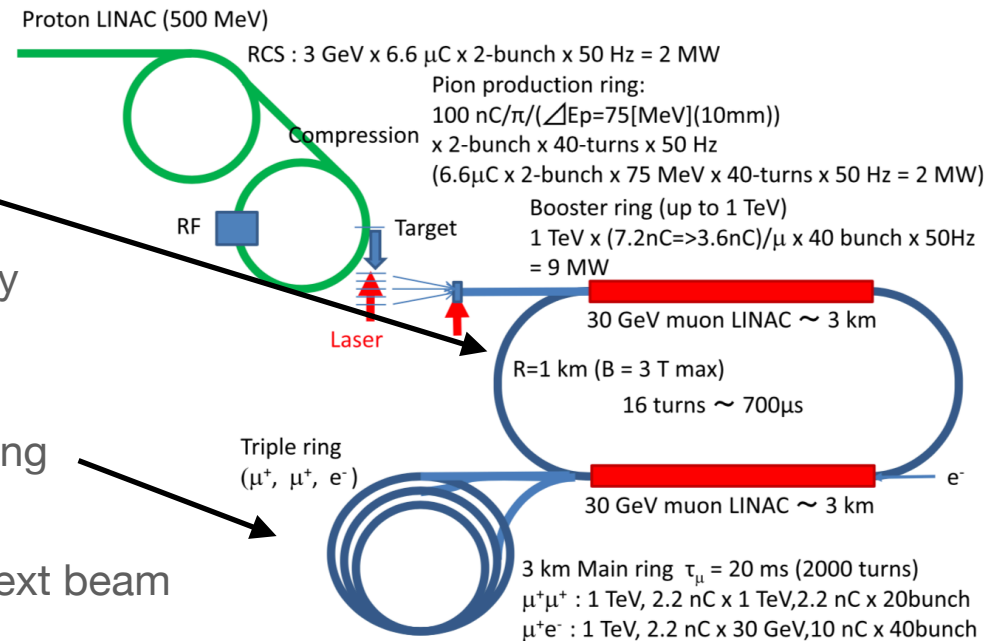
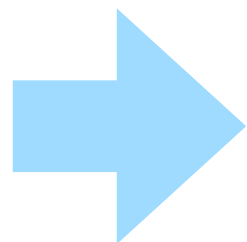


Fig. 1. Conceptual design of the μ<sup>+</sup>e<sup>-</sup>/μ<sup>+</sup>μ<sup>+</sup> collider.



$$\mathcal{L}_{\mu^+e^-} = 4.6 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}.$$

$$\mathcal{L}_{\mu^+\mu^+} = 5.7 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}.$$

ab<sup>-1</sup> level for 10yrs running.

not bad.

Actually, these numbers are pretty much conservative ones compared to MAP estimates.

# Luminosity comparison

	<b>MAP</b>	<b><math>\mu</math>TRISTAN(<math>\mu^+\mu^+</math>)</b>
<b>normalized emittance</b>	25 $\pi$ mm mrad	0.1-1 $\pi$ mm mrad
<b>bunch length</b>	1 cm	0.01-0.1 cm
<b>efficiency</b>	0.1	0.01 - 0.07
<b>total luminosity (arb. unit)</b>	1	2.5 - 10000

(eff)<sup>2</sup> / (emittance \* bunch length)

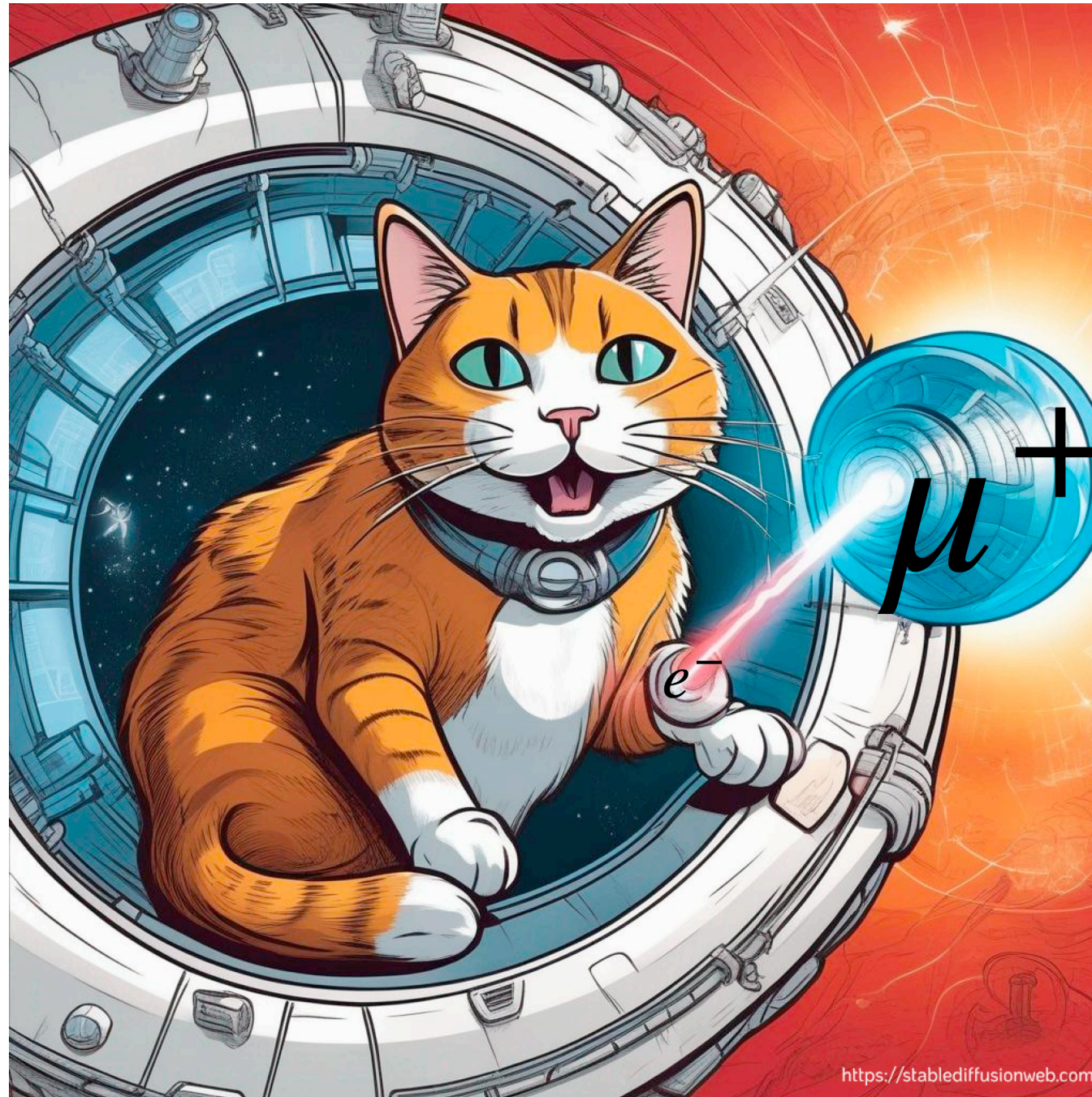
(could be much better for  $\mu^+e^-$ )

Number of muons may be smaller, but

we see that if we only use  $\mu^+$ , we can have (much) better luminosities.

And, the technology is more matured! Express ticket for muon colliders?

mewTRISTAN

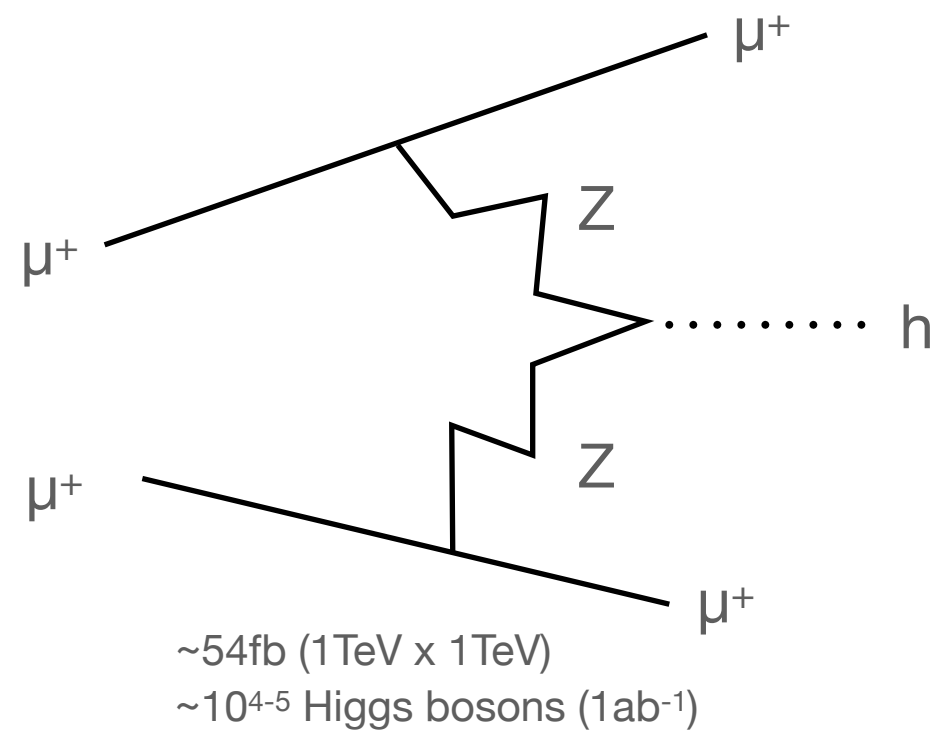
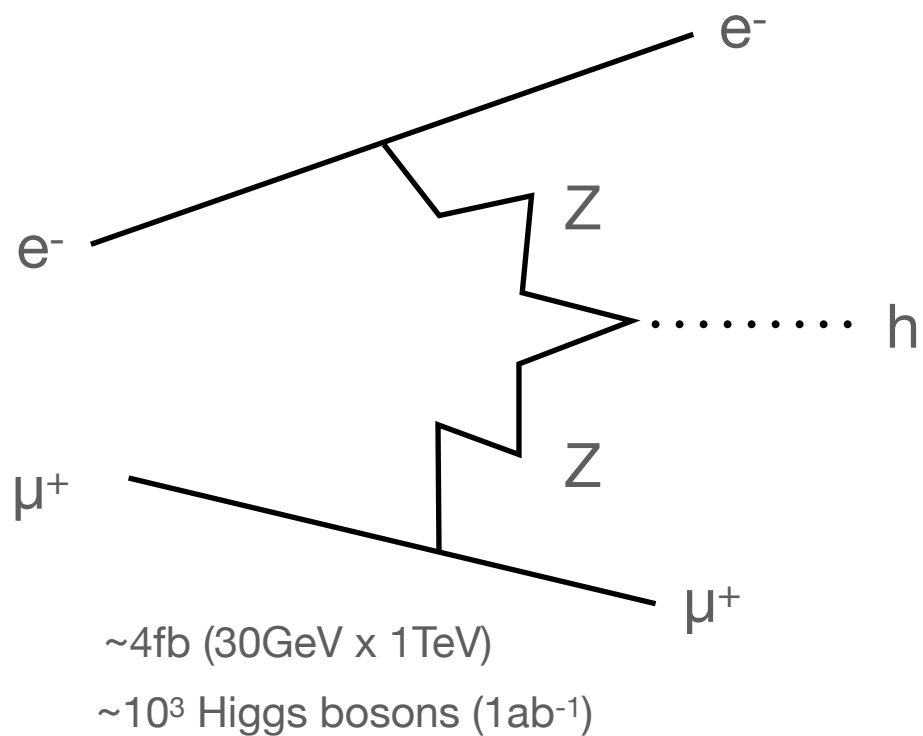
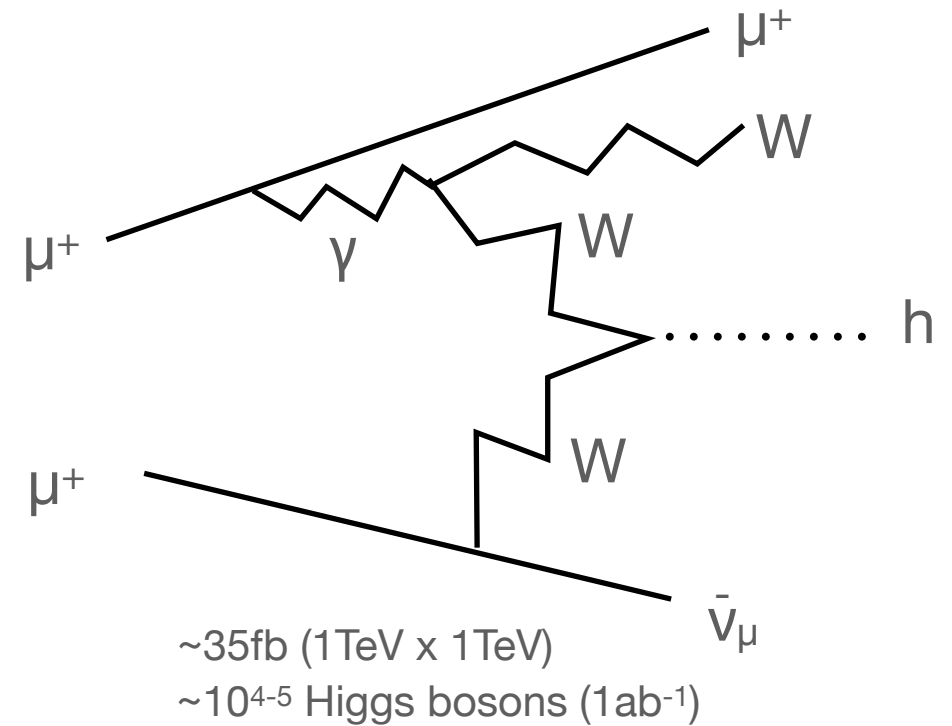
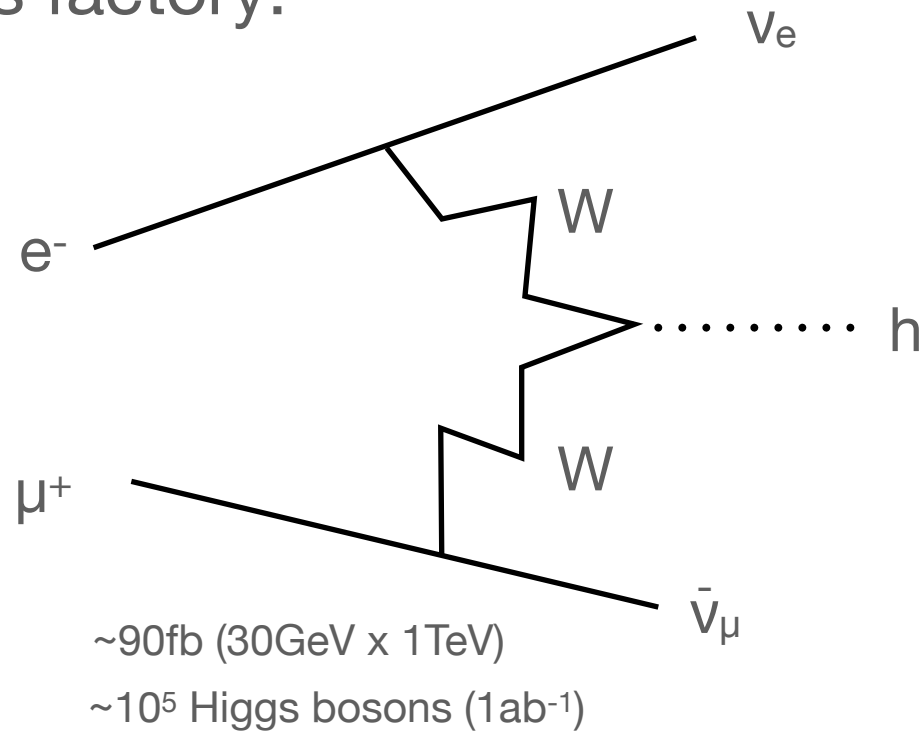


<https://stablediffusionweb.com>

by Cari Cesarotti

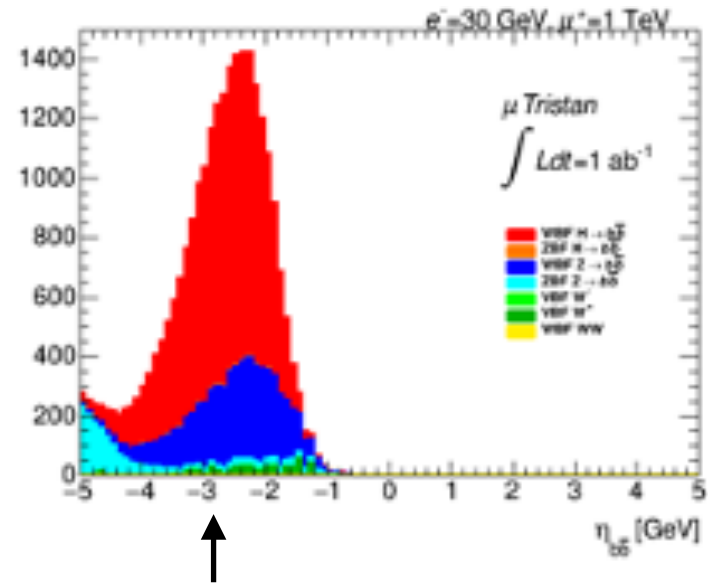
# What can we do at $\mu$ TRISTAN?

Higgs factory:



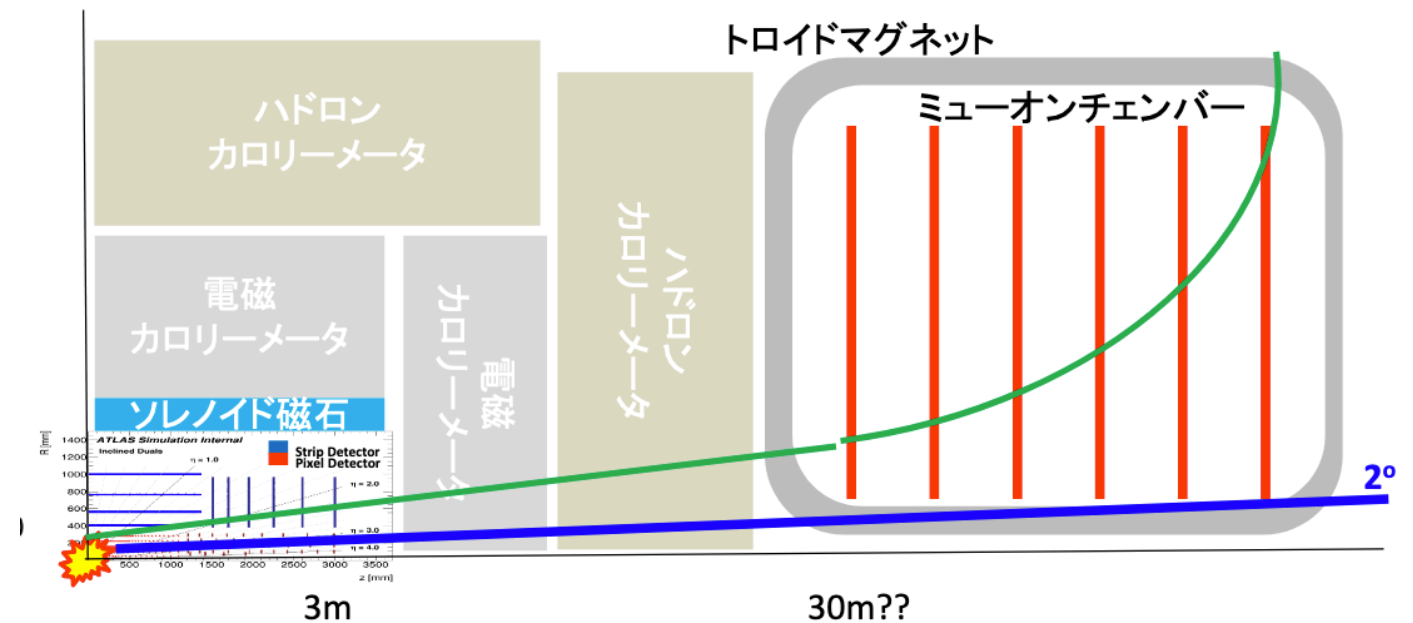
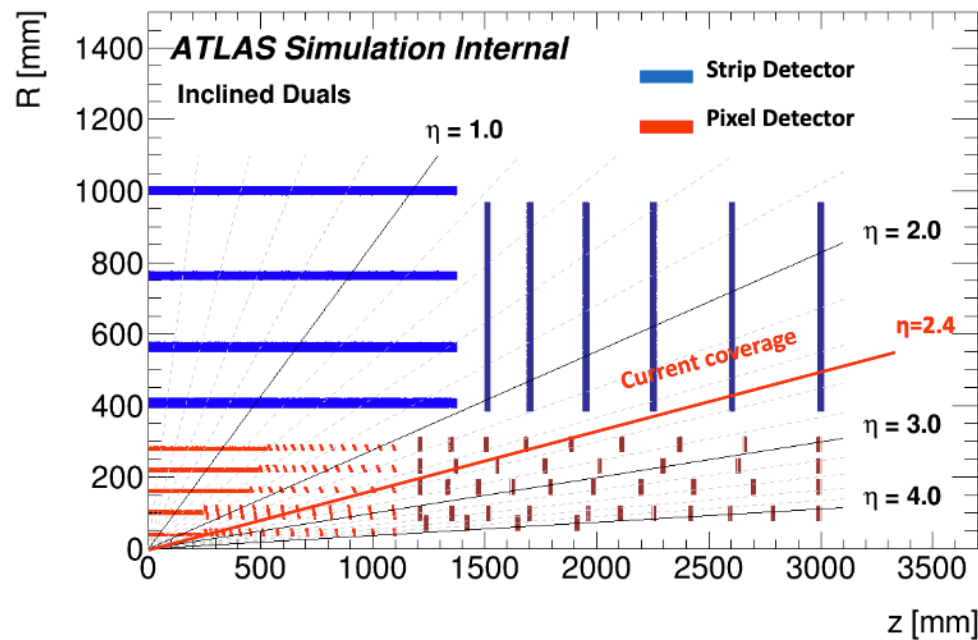


# $\mu^+e^-$ : Very asymmetric



All the particles go to the direction of the muon.

We need a coverage of  $\eta \sim -4$  ( $2^\circ$ ), which is the same level as the design of the ATLAS at HL-LHC.

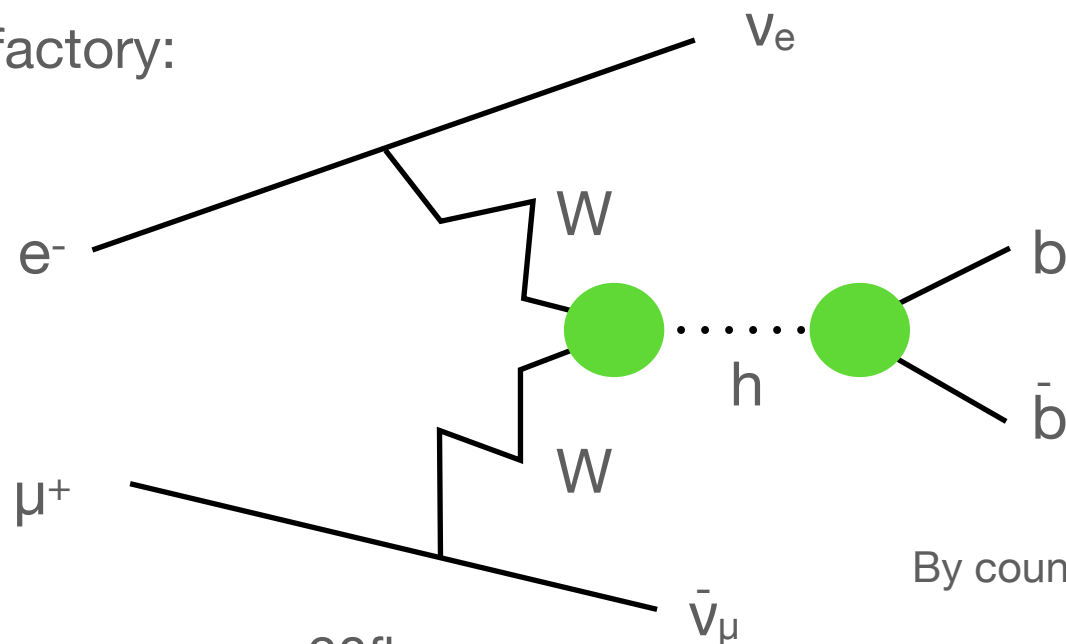


# Higgs coupling

Study in progress in collaboration with Koji Nakamura and Sayuka Kita.

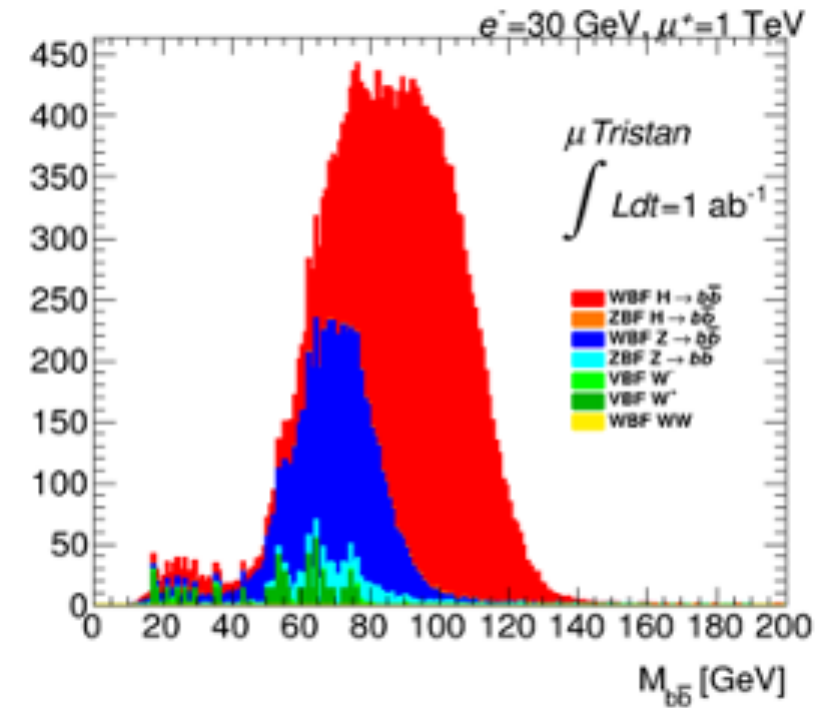
simulation with the ATLAS detector for HL-LHC

Higgs factory:



$\sim 90\text{fb}$

$\sim 10^5$  Higgs bosons



acceptance  $\sim 23\%$

(This should improve a lot with a detector designed for this collider.)

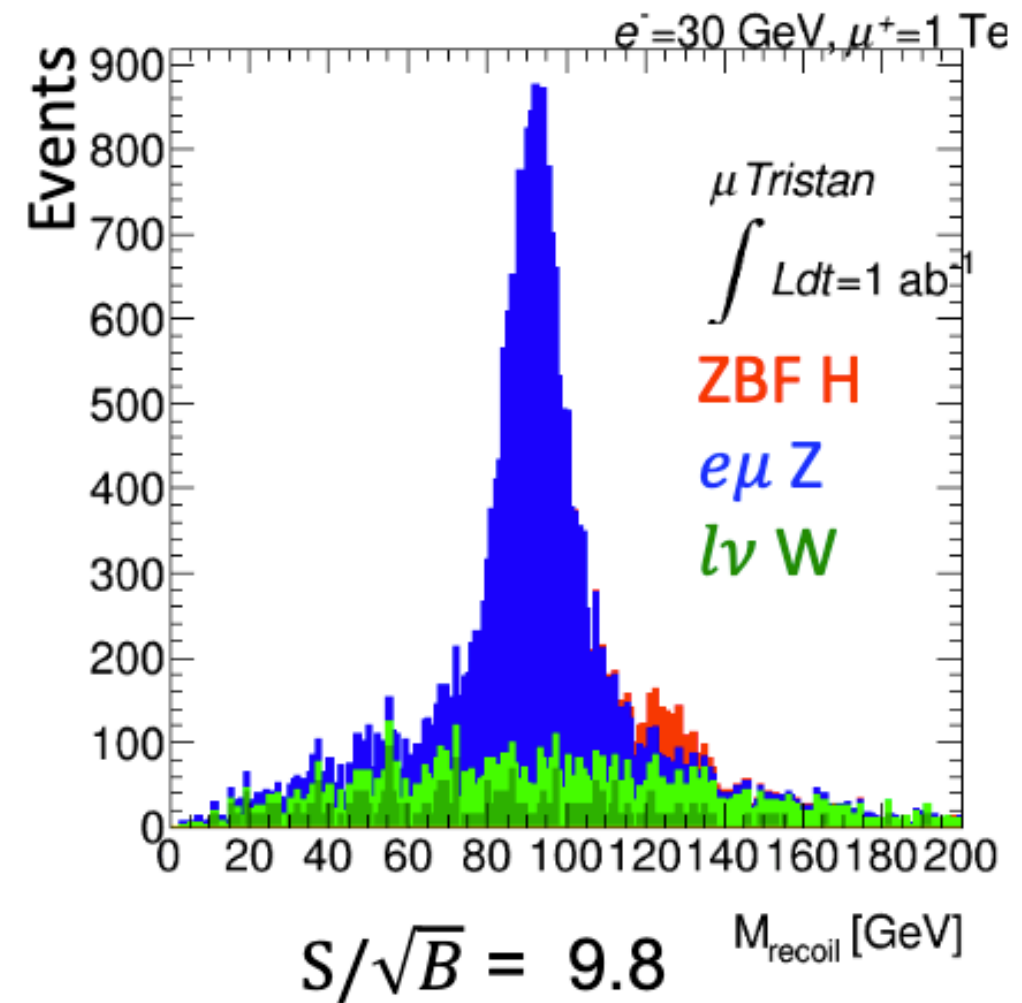
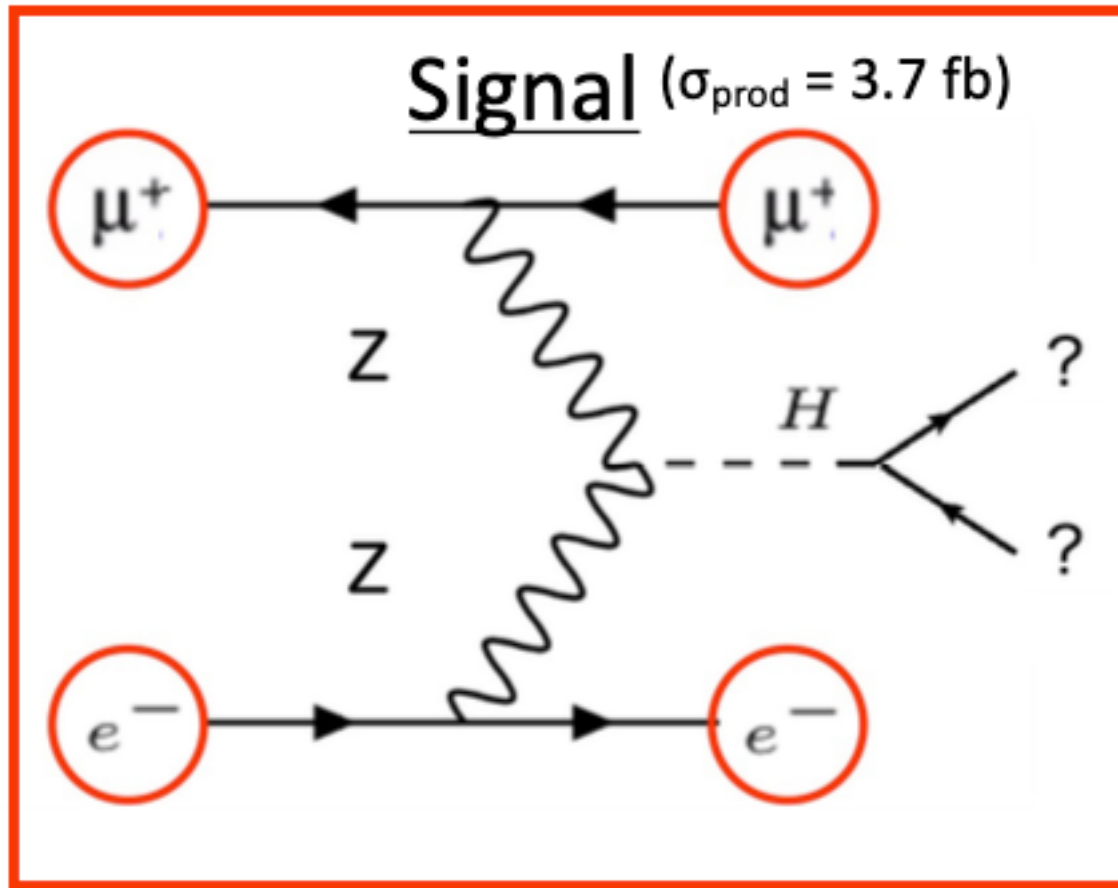
By counting the number of events and compare with the SM prediction

$$\Delta(\kappa_W + \kappa_b - \kappa_H)_{\text{stat}} = \frac{1}{2} \frac{1}{\sqrt{N(\text{WBF}) \times \text{Br}(h \rightarrow b\bar{b}) \times \text{efficiency}}}$$

$$= 3.1 \times 10^{-3} \times \left( \frac{\text{integrated luminosity}}{1.0 \text{ ab}^{-1}} \right)^{-1/2} \left( \frac{\text{efficiency}}{0.5} \right)^{-1/2}$$

sub percent level measurements.

# Z boson fusion recoil mass



→ 1k events @ 1  $\text{ab}^{-1}$

Total width may be measured.

# Detector matters

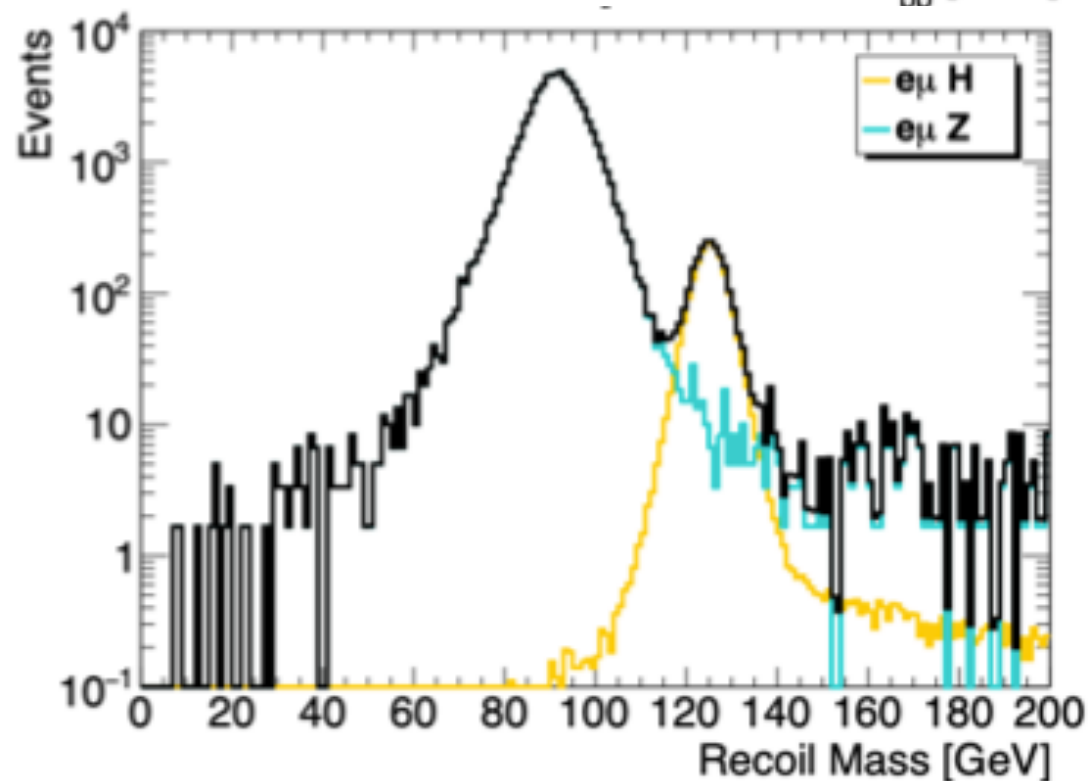
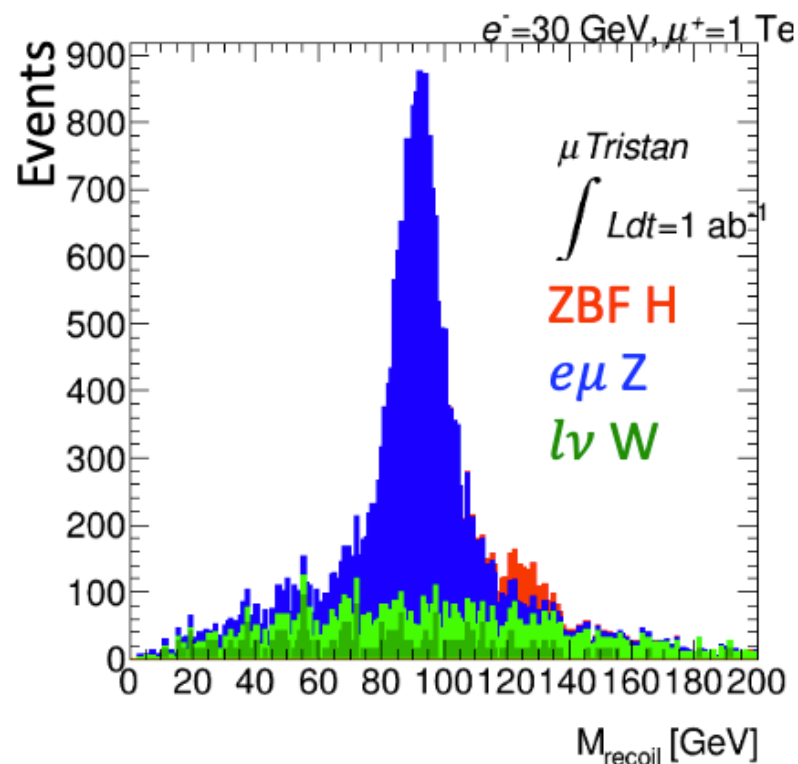
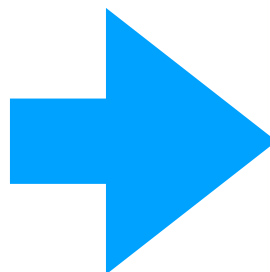
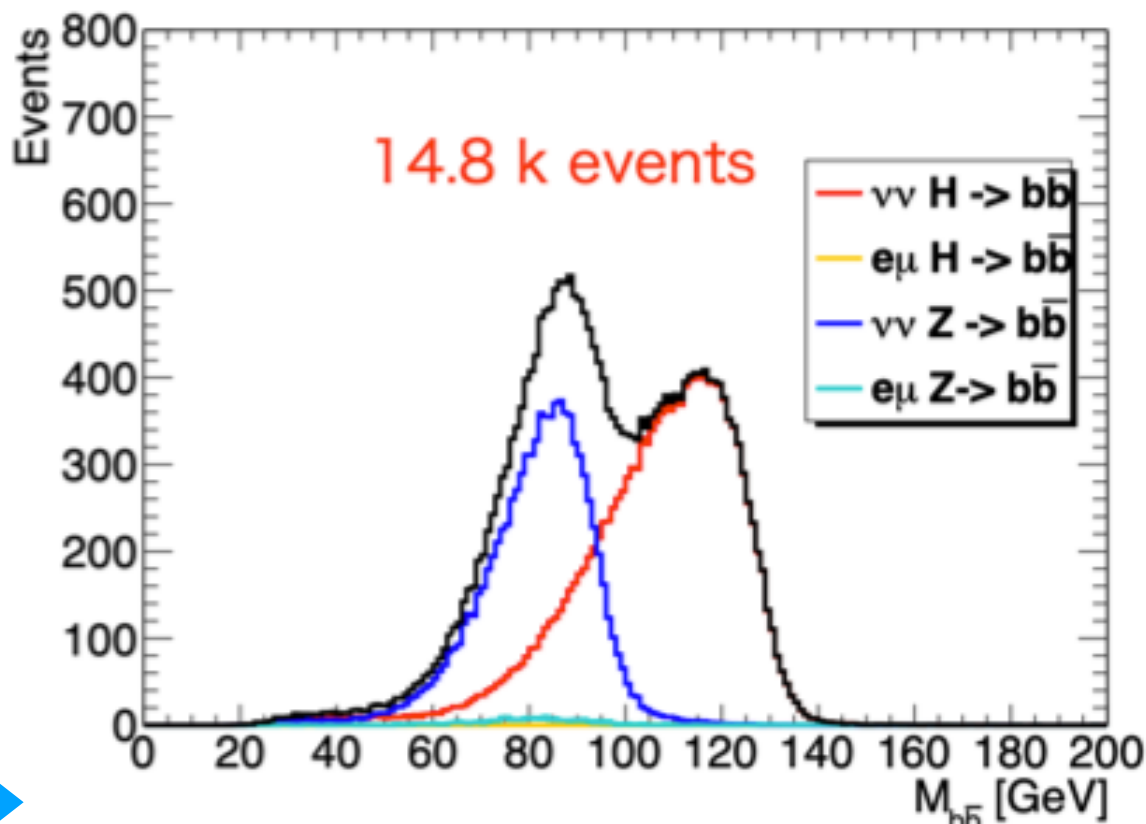
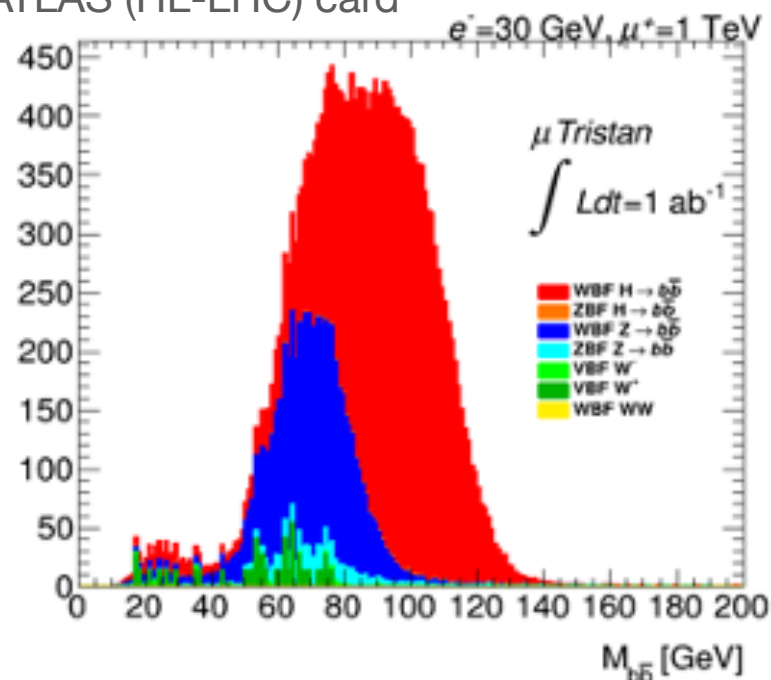
Delphes

Much better!

ATLAS (LHC) card with a larger forward coverage

Delphes

ATLAS (HL-LHC) card

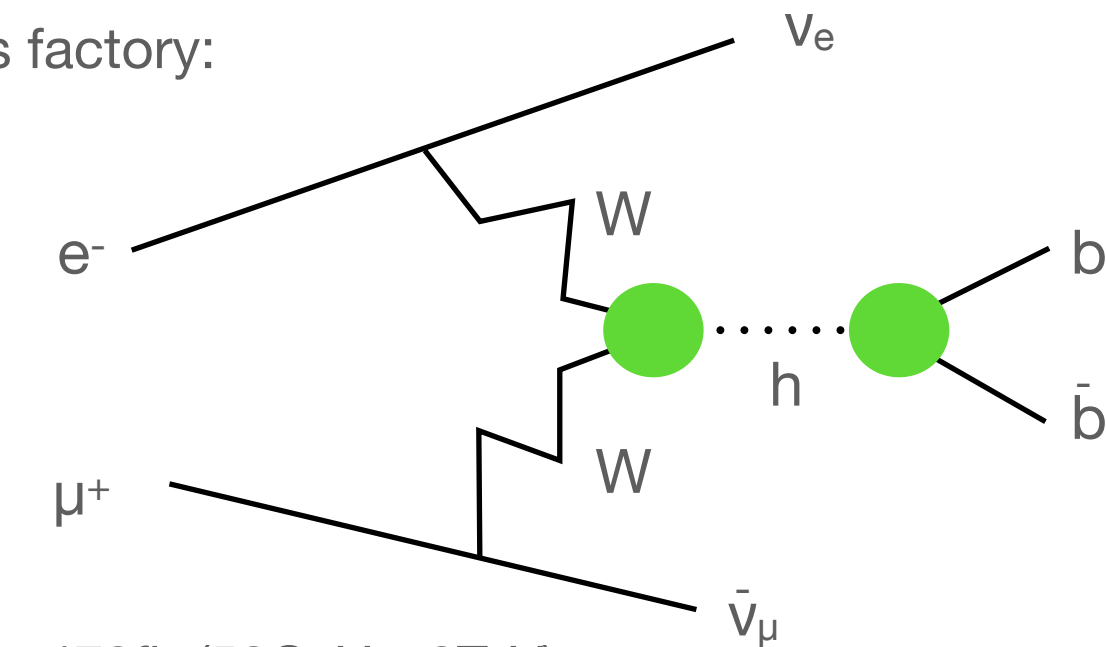


Studies underway.



# Higher energy? $\mu$ Tevatron?

Higgs factory:



$\sim 472 \text{ fb}$  ( $50 \text{ GeV} \times 3 \text{ TeV}$ )

$\sim 5 \times 10^5$  Higgs bosons ( $\text{ab}^{-1}$ )

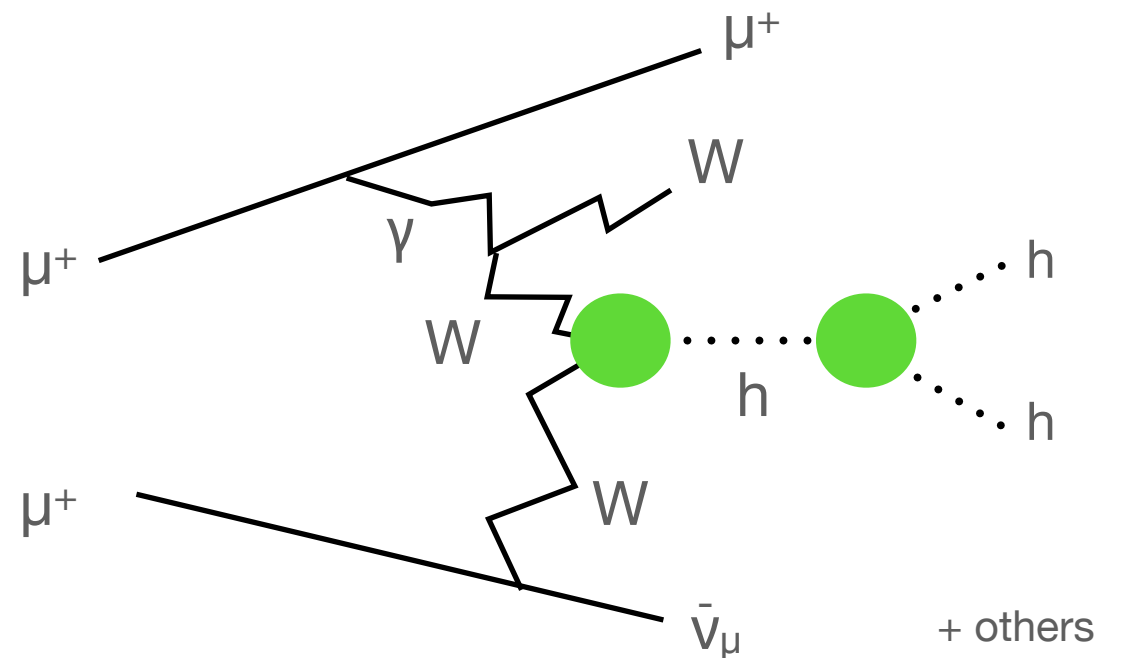
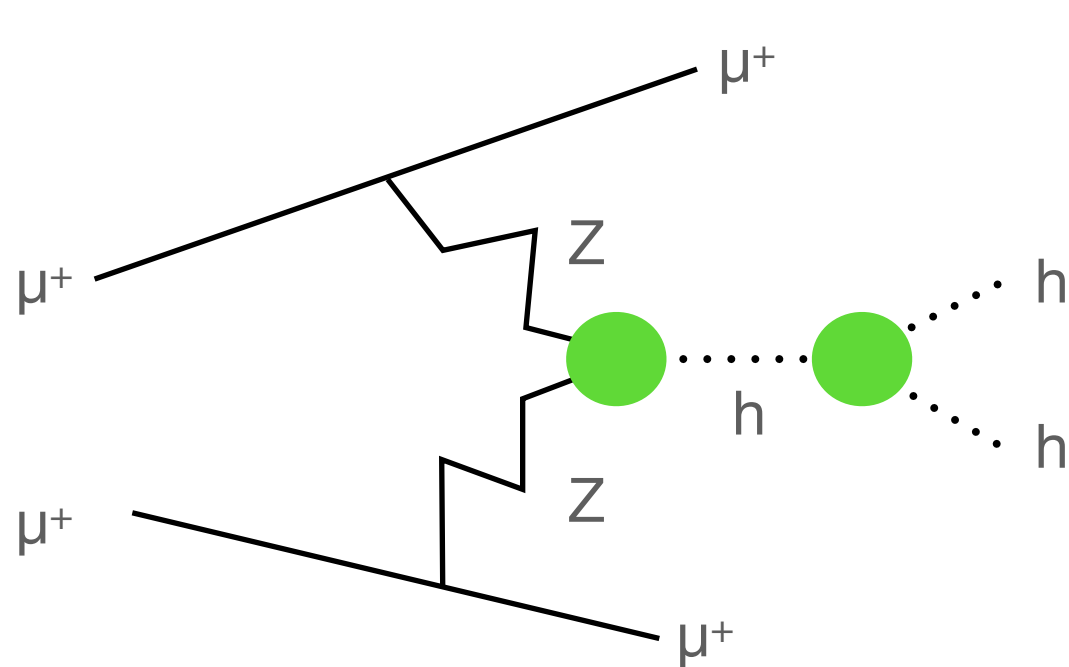
50 GeV electron + 3 TeV muon at a **6 km** ring

$$\sqrt{s} = 775 \text{ GeV}$$

hh production: 89 events/ $\text{ab}^{-1}$  (maybe we need more for coupling measurements)



# Higgs production@ $\mu^+\mu^+$

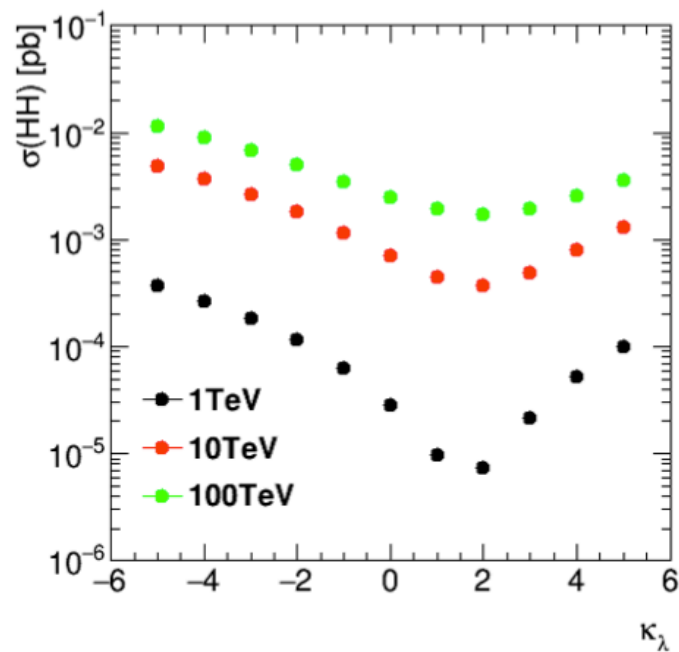


about 1/3 of  $\mu^+\mu^-$

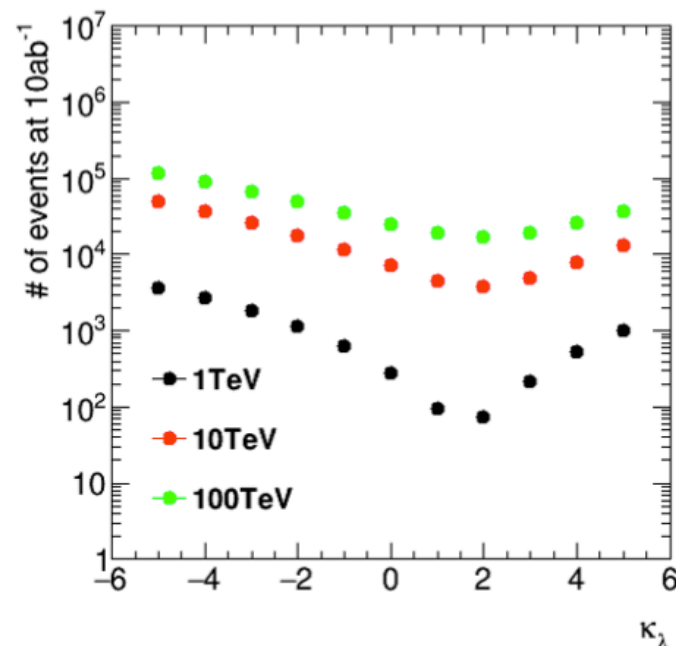
$\sqrt{s}$ [TeV]	ZBF [fb]	Photon emission [fb]
2	0.075	0.010
10	0.62	0.30
20	1.1	0.75

ZBF:

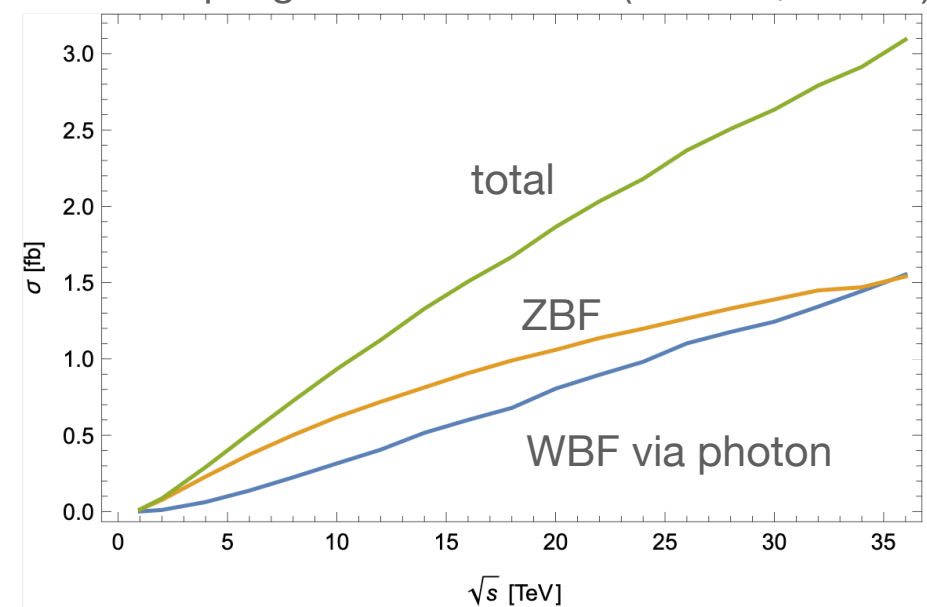
## Cross section



## # of Events in 10ab<sup>-1</sup>

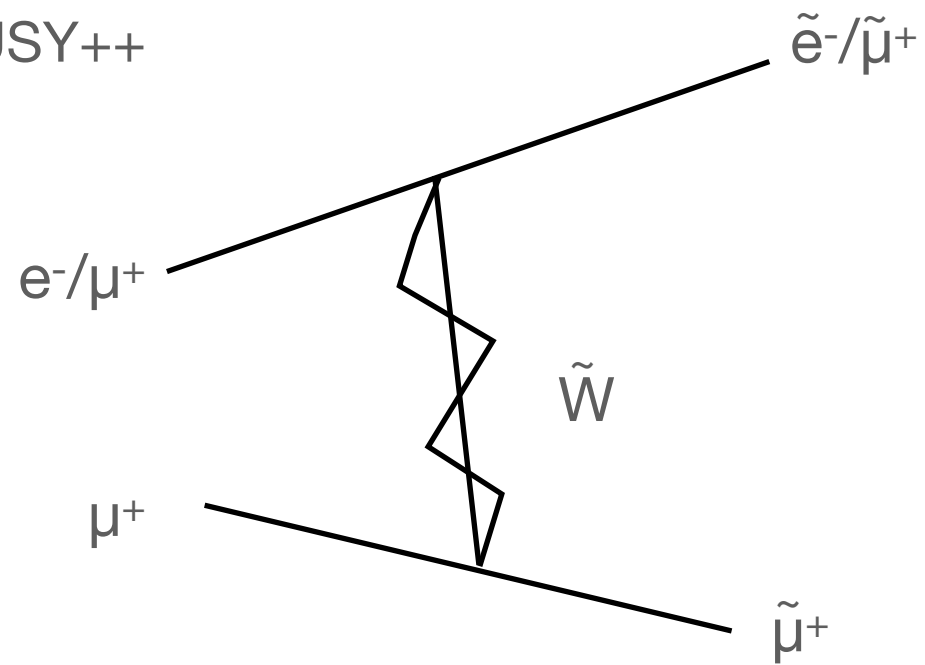


hhh coupling at 5-10% level? (@10TeV, 10ab<sup>-1</sup>)



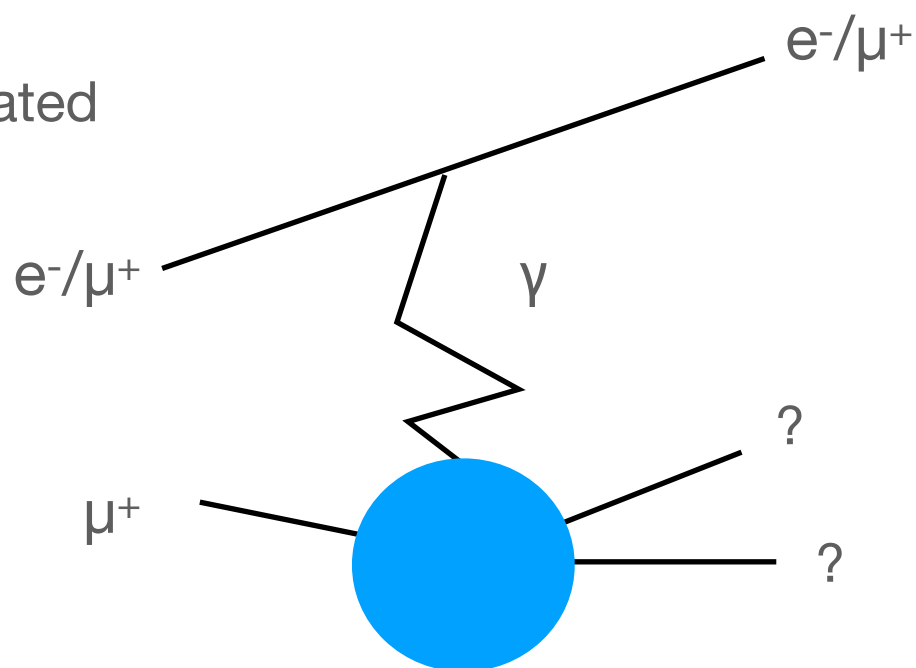
# New physics?

SUSY<sub>++</sub>

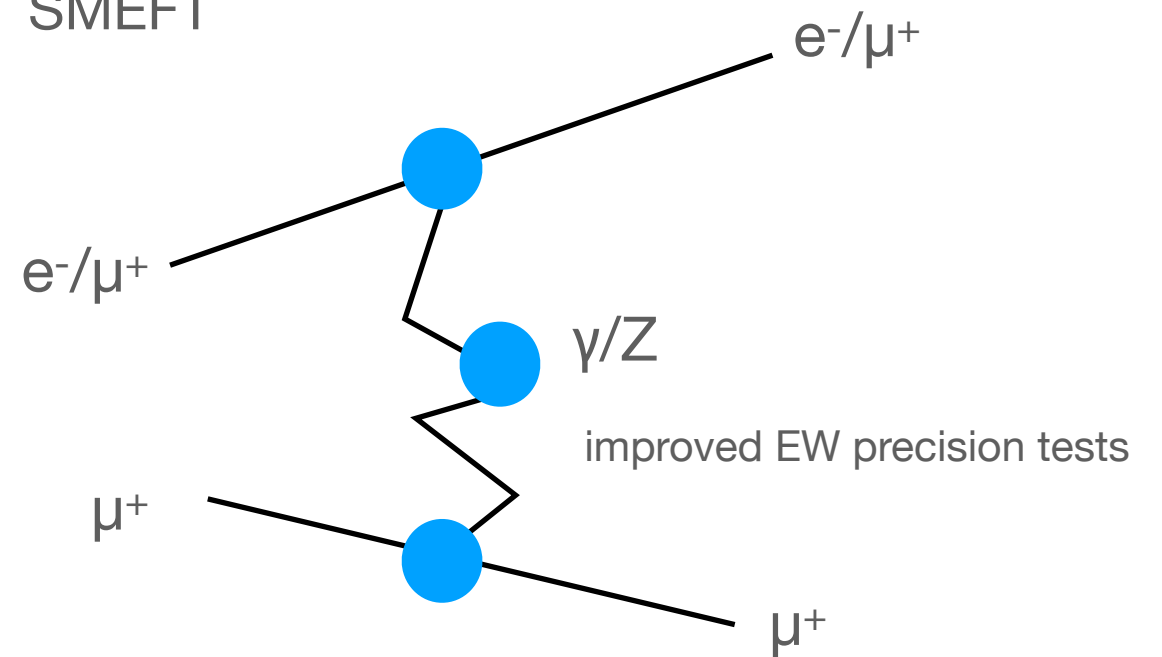


TeV mass new particles

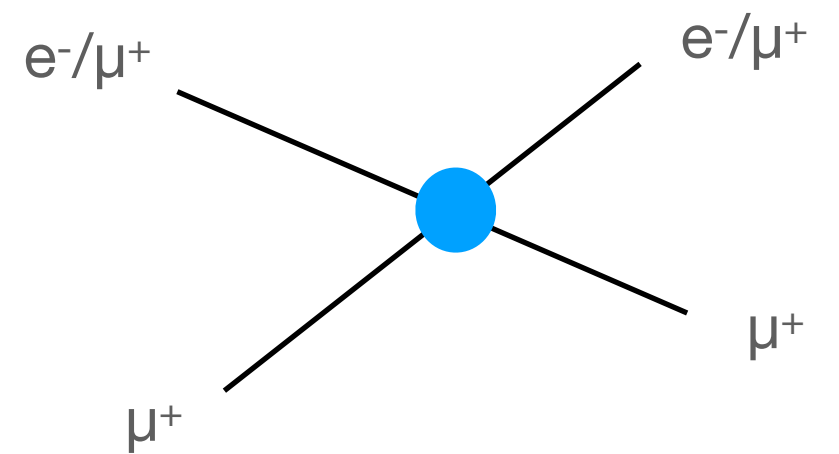
$g-2$  motivated



SMEFT



improved EW precision tests

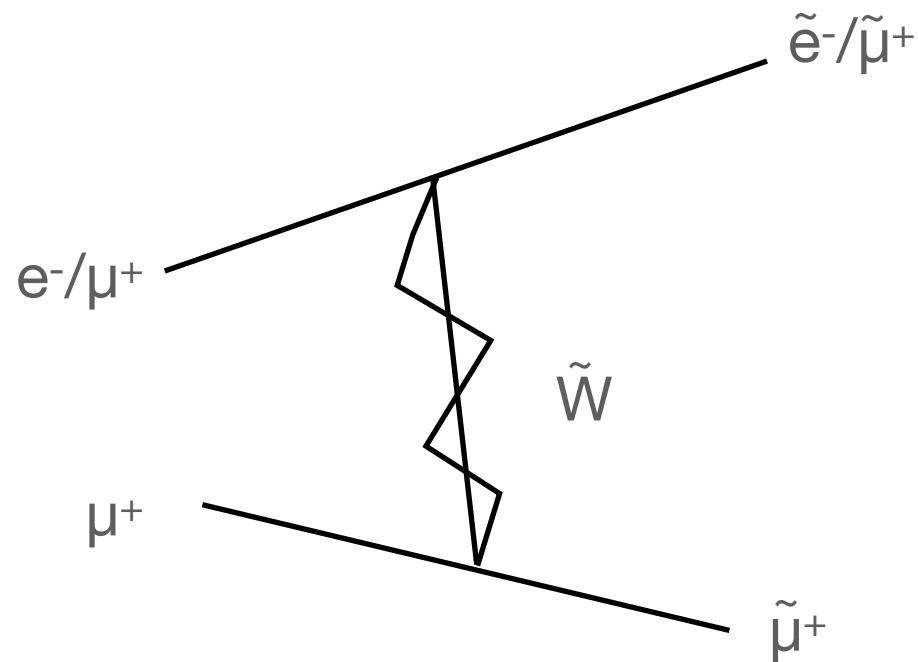
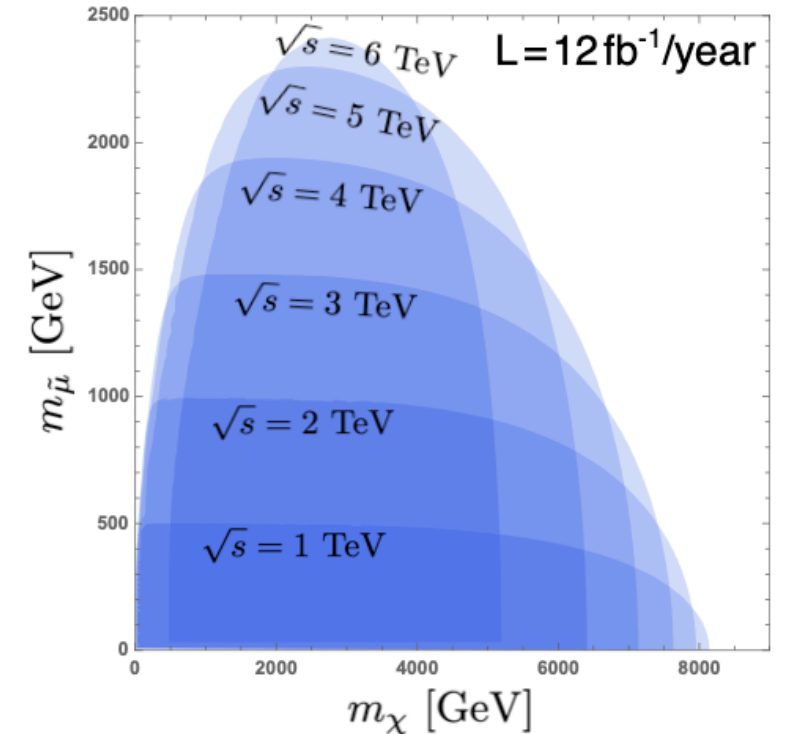
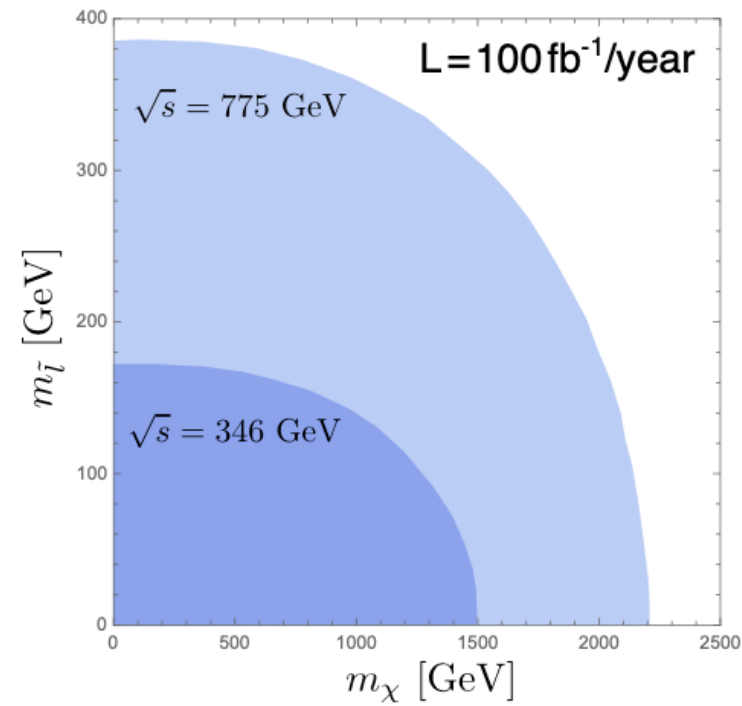


probe 100TeV scale physics!?



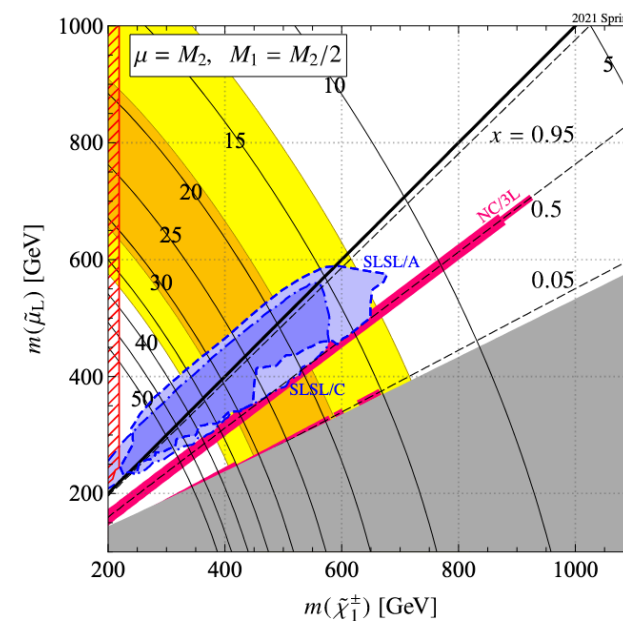
# Supersymmetry

Regions for  $N_{\text{event/year}} > 100$ .

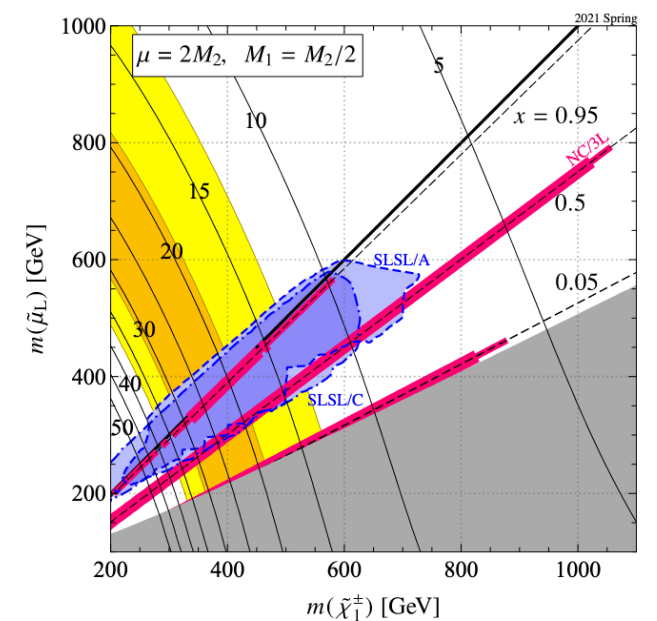


Scalar muons up to TeV even for very heavy gauginos.  
Almost completely cover the muon  $g-2$  motivated region.

[Endo, Hamaguchi, Iwamoto, Kitahara '21]



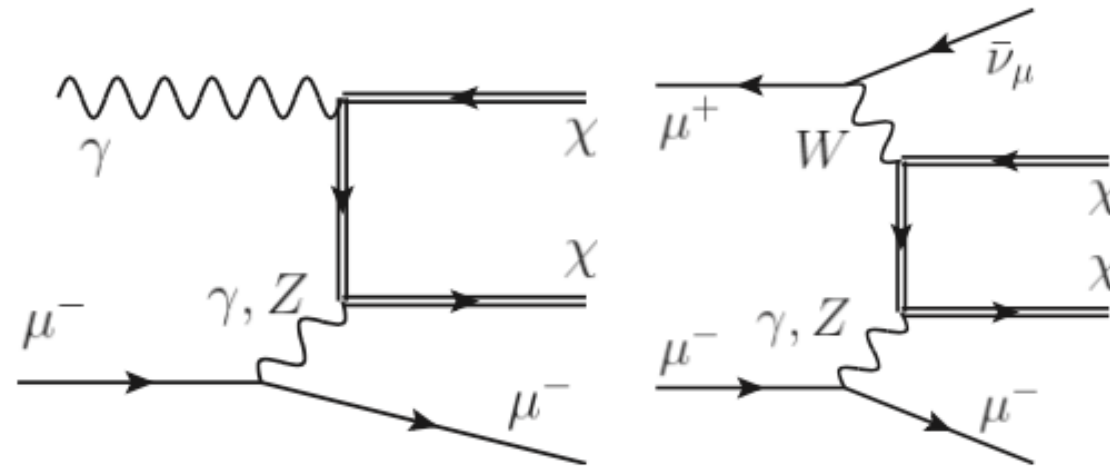
(A)  $\mu = M_2, M_1 = M_2/2$ .



(B)  $\mu = 2M_2, M_1 = M_2/2$ .

# DM?

study@ $\mu^+\mu^-$  [Han et al. '20]



same search is possible at  $\mu^+\mu^+$

mono- $\mu$

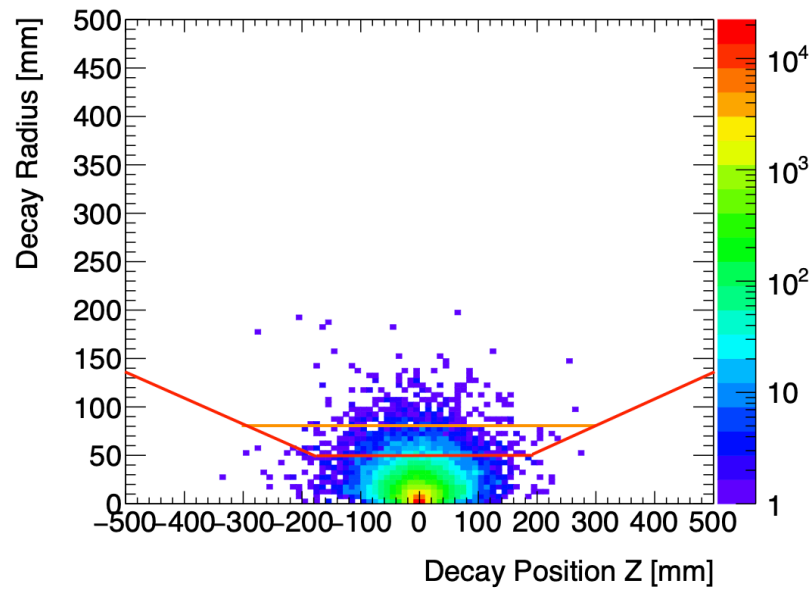
S/B is good in this process.

10TeV machine can cover 1TeV Higgsino and 1-2TeV Wino.

track + VBF search?

indirect search: [Fukuda, Moroi, Niki, Wei '23]

$\sqrt{s} = 10$  TeV, 質量 1 TeV Higgsino の崩壊マップ



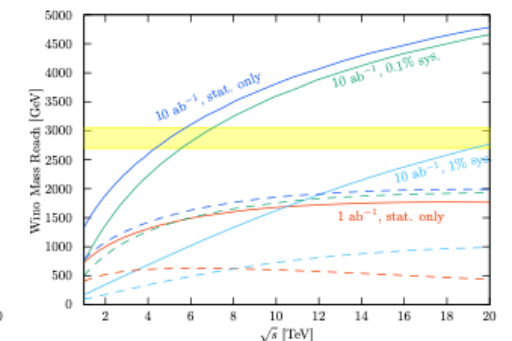
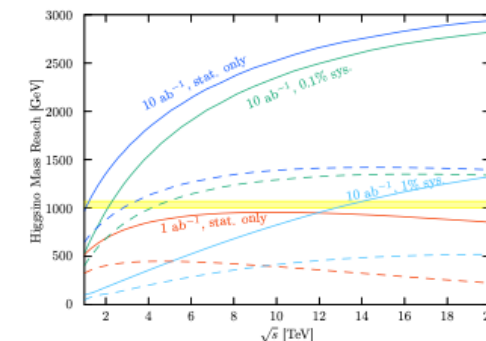
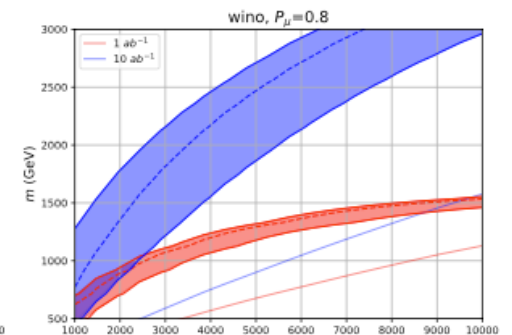
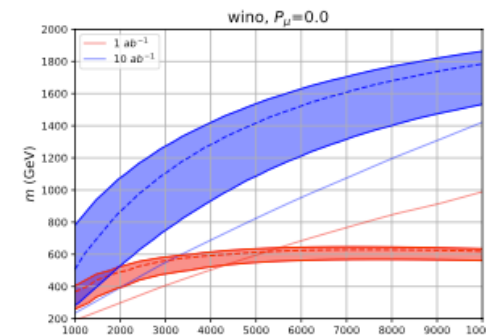
崩壊半径

- Case A > 80 mm
- Case B > 50 mm

$|\eta| < 2.0$

を再構成できると仮定

[with T. Kaji, T. Yoshida, K. Yorita in progress]

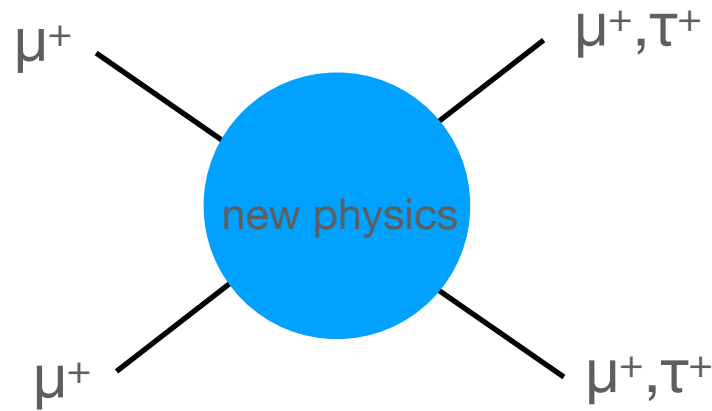


(a) Higgsino

(b) Wino

[Okabe, Shirai '23]

# muon specific



$\mu^+\mu^+$  has a big advantage in looking for new physics associated with the muon.

reach to O(100)TeV physics!

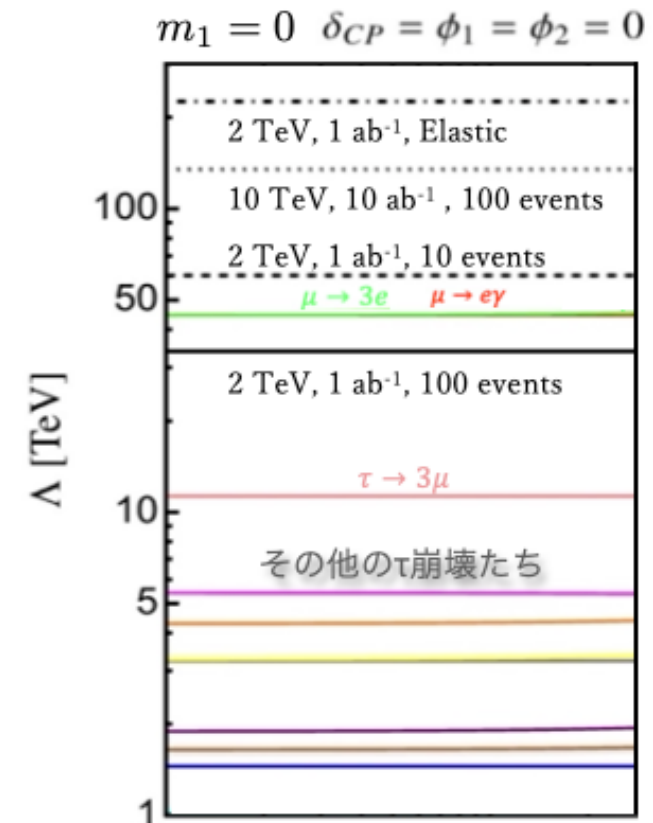
elastic scattering and lepton flavor violating scattering.

[Fridell, RK, Takai '23]

[Hamada, RK, Matsudo, Takaura '22]

	RR	LL	RL
$C_{HWB}$	10 TeV	9.4 TeV	2.3 TeV
$C_{HD}$	5.5 TeV	3.5 TeV	2.3 TeV
$C_{H\ell}^{(1)}$	8.0 TeV	0	4.9 TeV
$C_{H\ell}^{(3)}$	14 TeV	7.0 TeV	6.7 TeV
$C_{H\tau}$	0	7.5 TeV	5.3 TeV
$C_{\ell\ell}$	7.7 TeV	5.0 TeV	3.3 TeV
$C_{\ell\ell}^{\mu\mu\mu\mu}$	100 TeV	0	0
$C_{ee}^{\mu\mu\mu\mu}$	0	100 TeV	0
$C_{le}^{\mu\mu\mu\mu}$	0	0	46 TeV

Table 1: Constraints on SMEFT operators at 2-sigma level.  $\sqrt{s} = 2$  TeV. The bin size for  $\theta$  is taken as  $1^\circ$  and each bin covers the range  $\theta_i - 0.5^\circ < \theta < \theta_i + 0.5^\circ$ . The considered range of  $\theta_i$  is  $16^\circ \leq \theta_i \leq 164^\circ$ .



# Summary

$\mu^+$  may have a better chance. Interesting to consider a km size experiment as a relatively near future project.

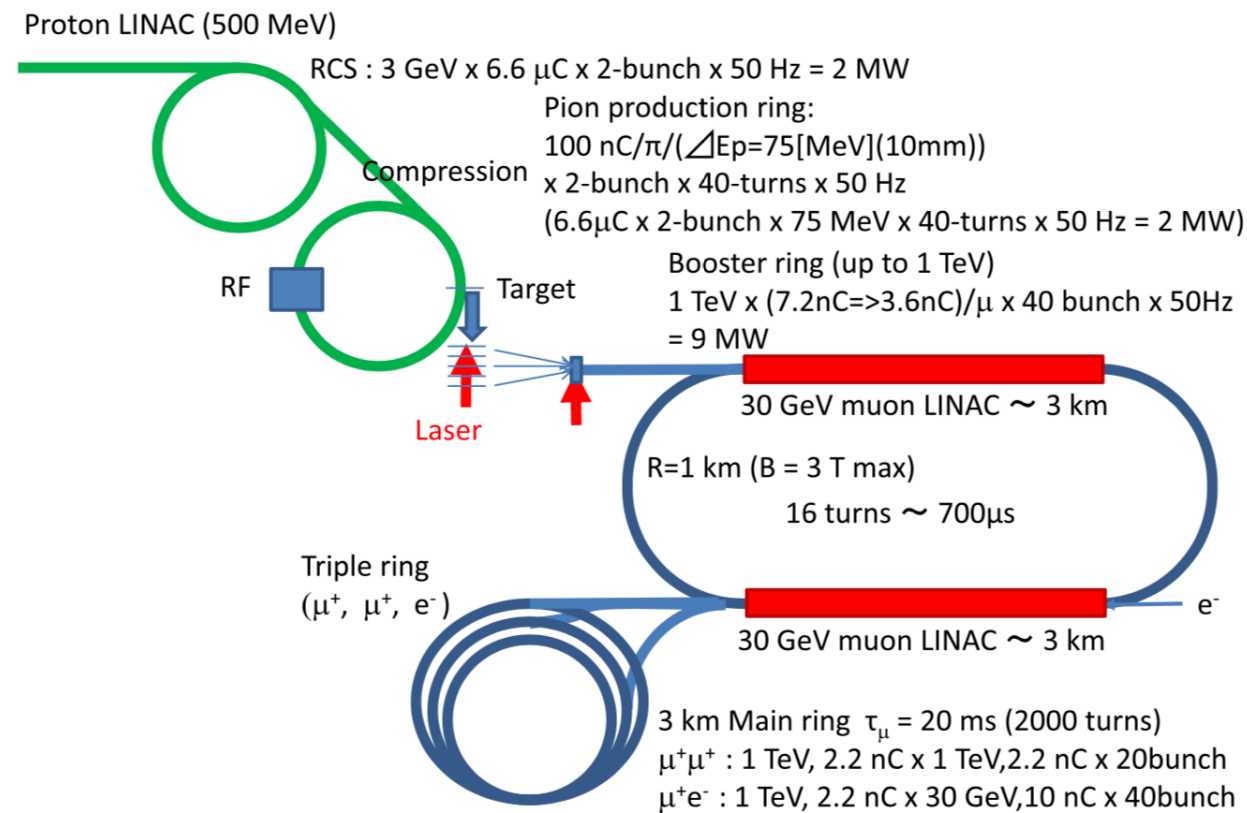


Fig. 1. Conceptual design of the  $\mu^+e^-/\mu^+\mu^+$  collider.



by Cari Cesarotti