

CLOSING IN ON WIMP DM AT THE MUON COLLIDER

ROBERTO FRANCESCHINI

November 18th 2023 - Pittsburgh

AN ATTEMPT TO A REVIEW

AND WORKS WITH SALVATORE BOTTARO, MARCO COSTA, LUDOVICO VITTORIO, XIAORAN ZHAO AND DARIO BUTTAZZO, PAOLO PANCI, DIEGO REDIGOLO

2107.09688, 2205.04486, 2212.11900



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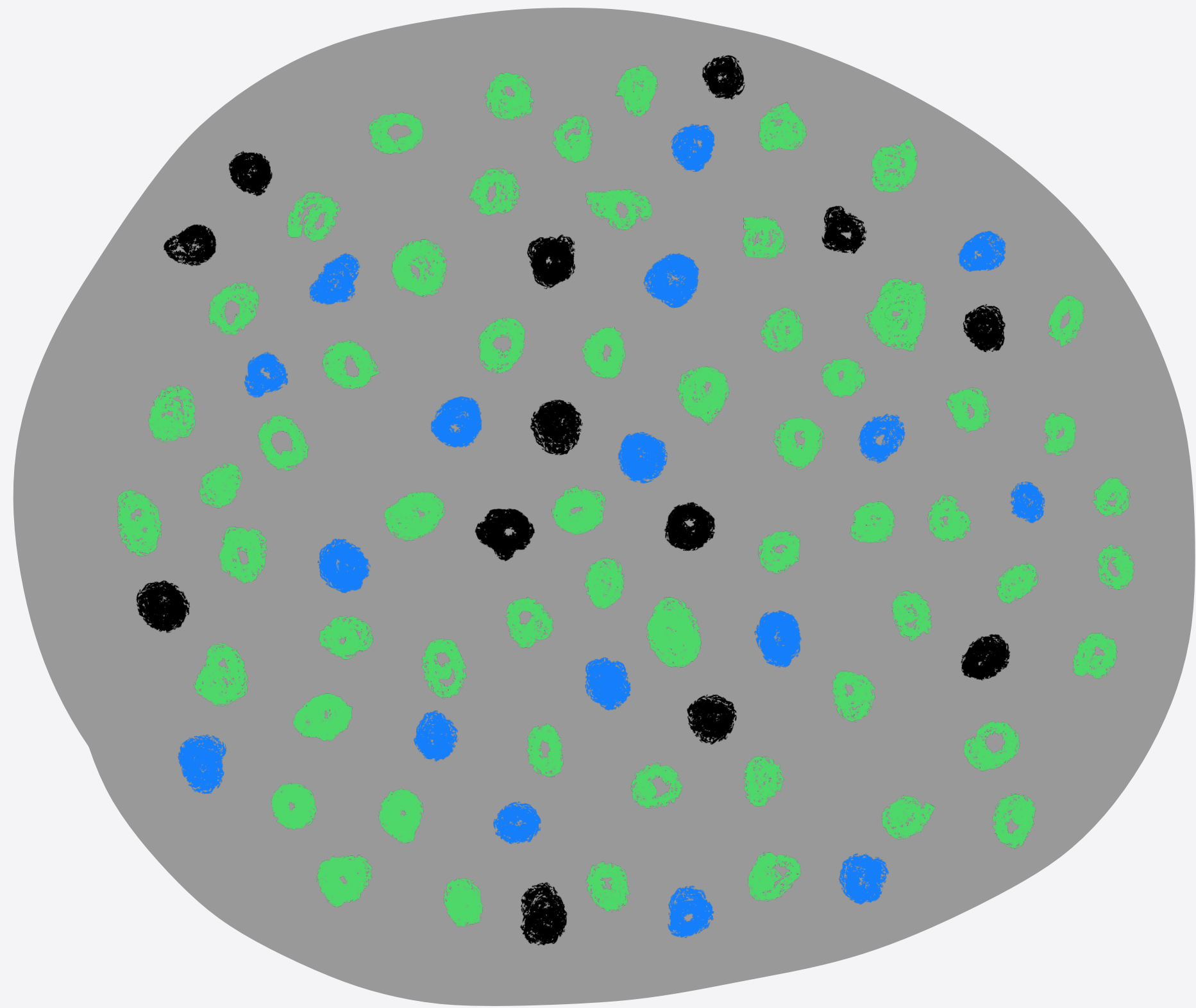
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INTRO

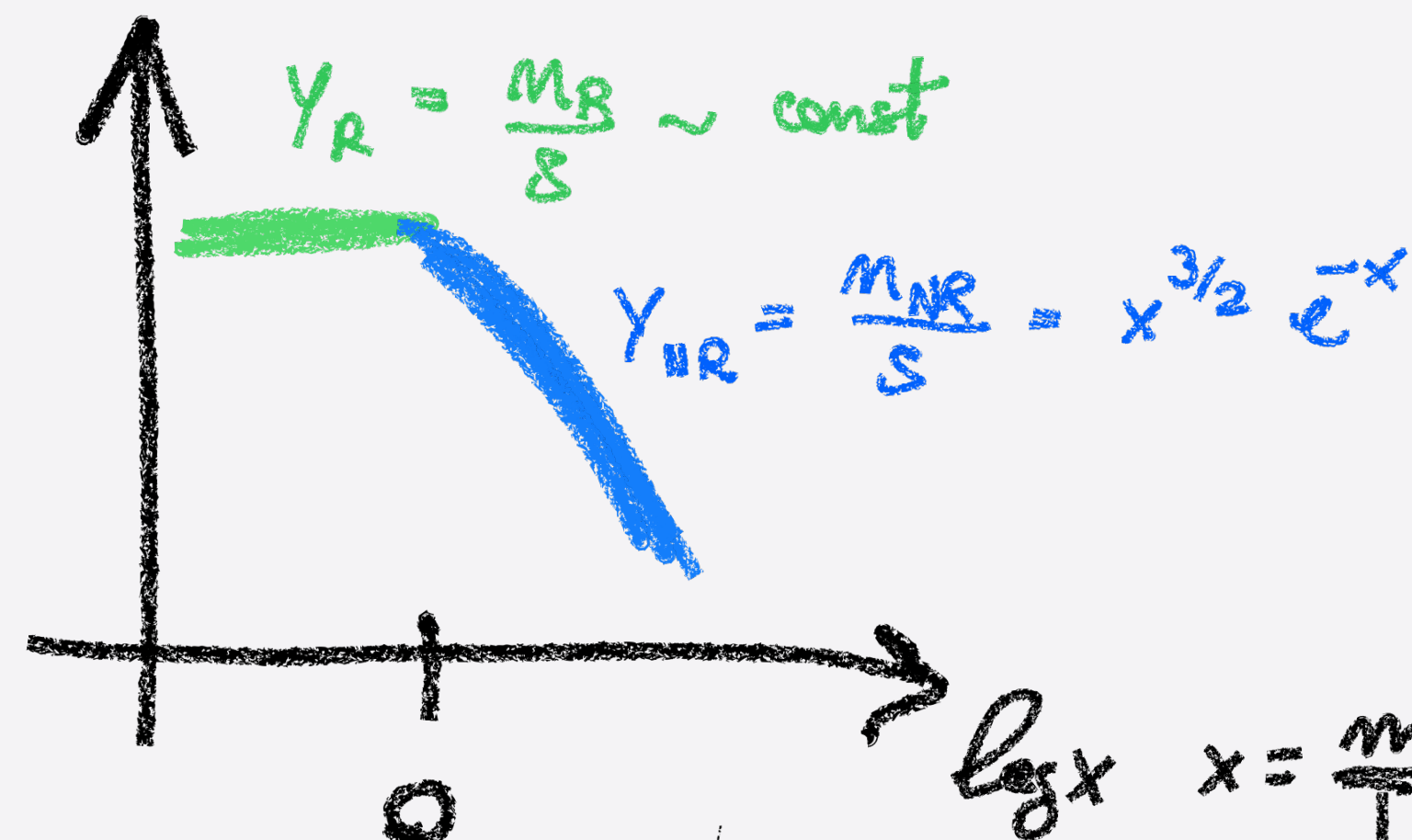
A SIMPLEST EXPLANATION FOR ITS PRODUCTION



- SM RELATIVISTIC
- DARK MATTER
- SM NON-RELATIVISTIC

Following equilibrium thermodynamics the number density of a specie can be predicted at all times it is in equilibrium. Once it drops out from equilibrium Y freezes out and the relic density is fixed.

$$\log \left(\frac{N(m/x)}{N(\infty)} \right)$$



$$\frac{dY}{dx} = \frac{-x \langle \sigma_a v \rangle S}{H/w} (Y^2 - Y_{eq}^2)$$

$$= \# m M_{pl} \bar{\sigma}_0 x^{-k-2}$$

$$Y_\infty = \# \frac{(x_f)^{k+1}}{M_{pl} m \bar{\sigma}_0} \sim \# \frac{m}{M_{pl}} (x_f)^{k+1}$$

THE WIMP "CATALOG"

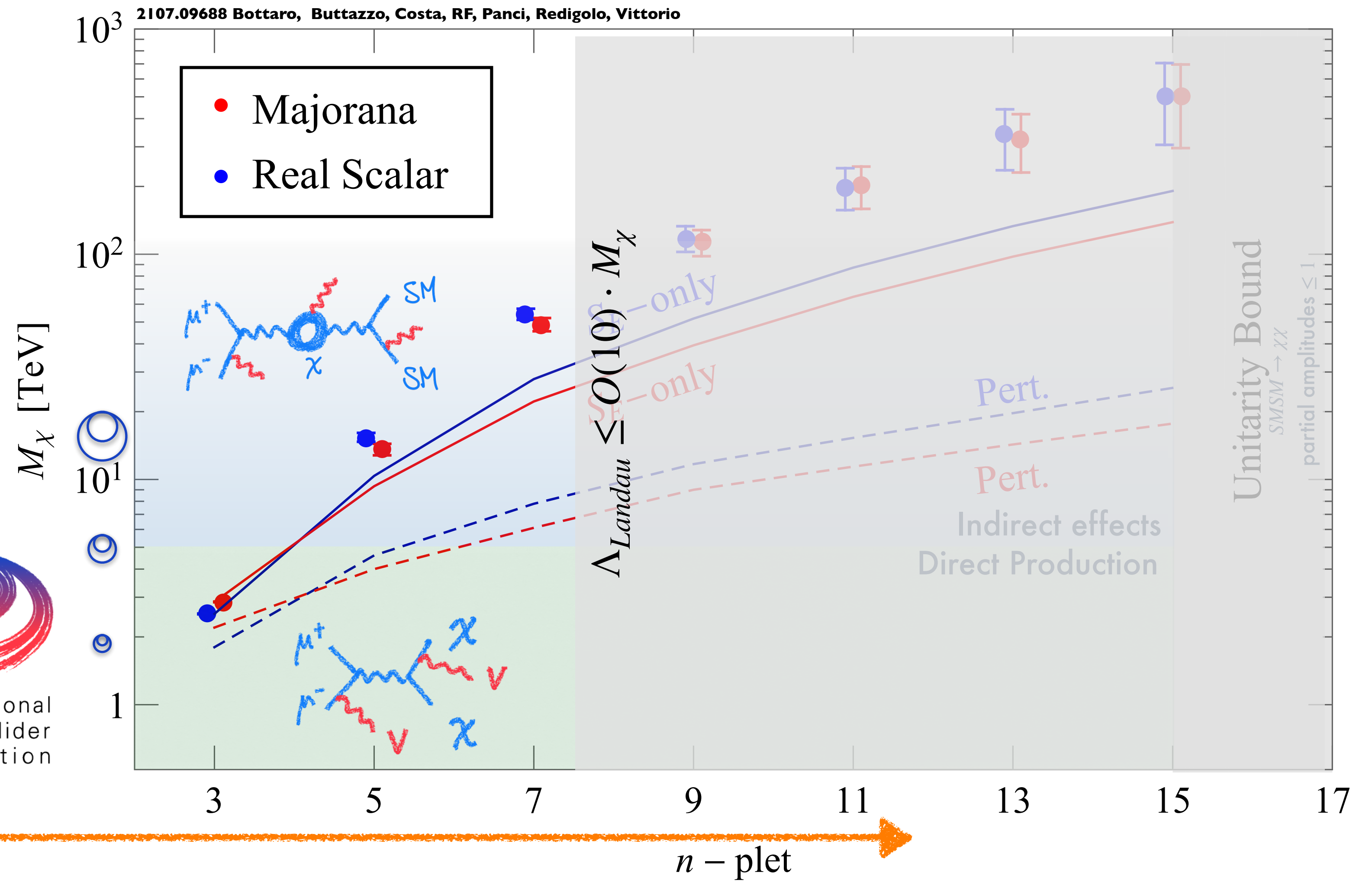
Following equilibrium thermodynamics the number density of a specie can be predicted at all times it is in equilibrium. Once it drops out from equilibrium Y freezes out and the relic density is fixed.

$$\Omega_{nr} \sim \frac{1}{\sigma_{ann}} \sim \frac{M^2}{C_n \cdot g^2}$$

mass of the DM

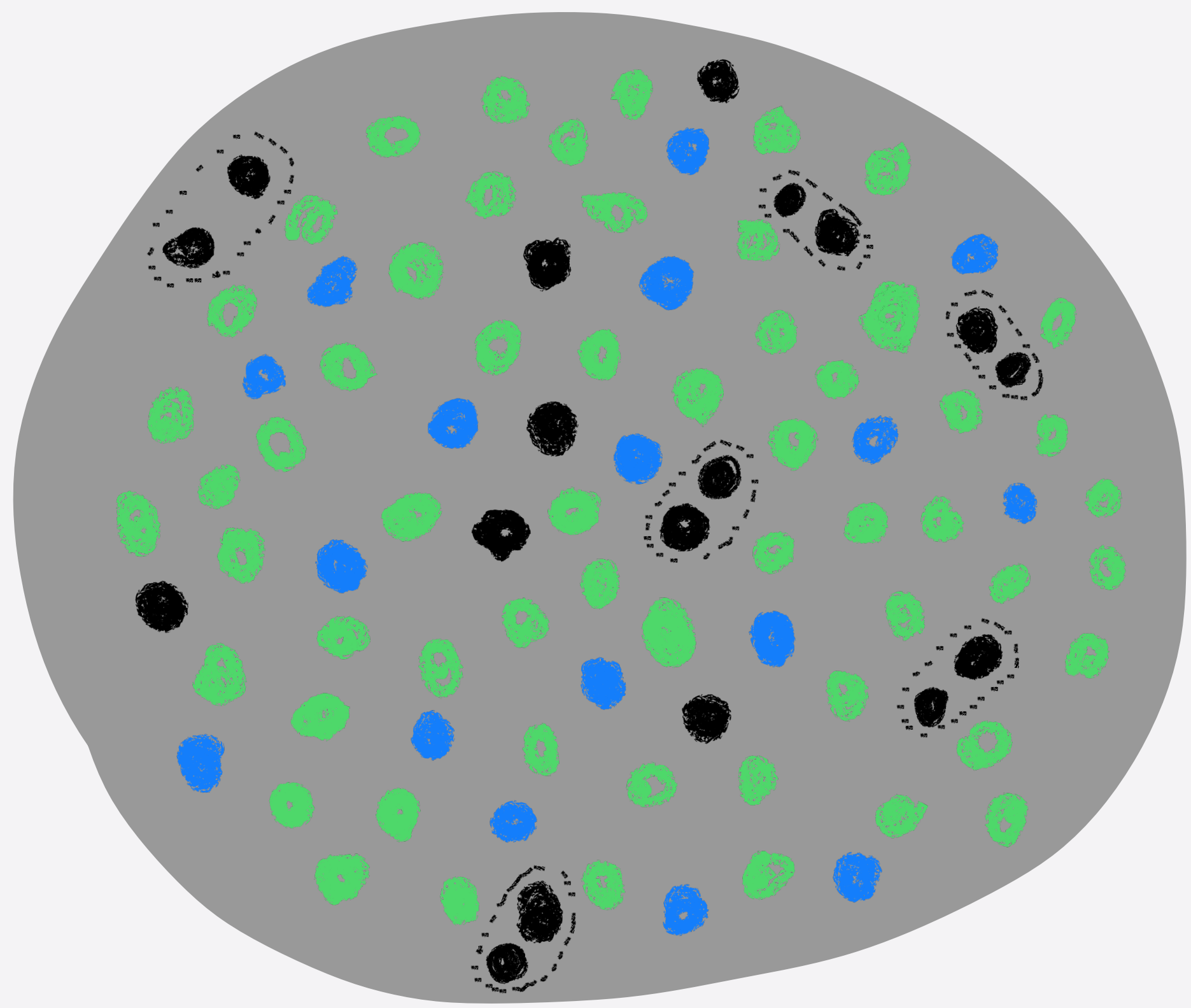


weak charge of the DM



WIMPs are clearly "muon collider material"

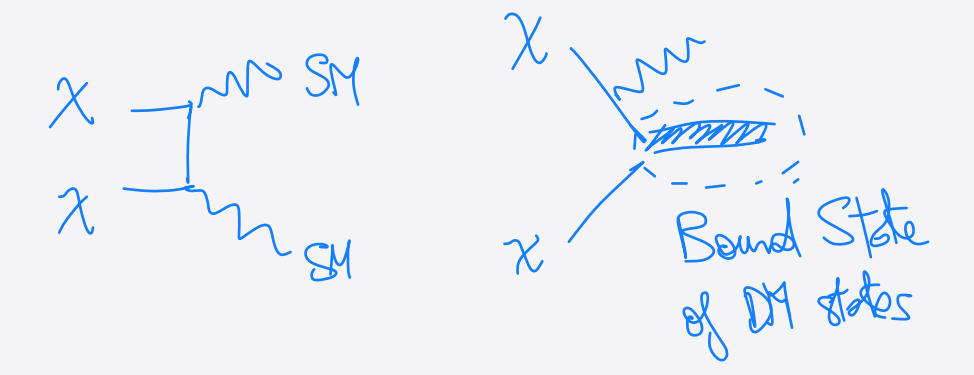
A STILL SIMPLE EXPLANATION FOR ITS PRODUCTION



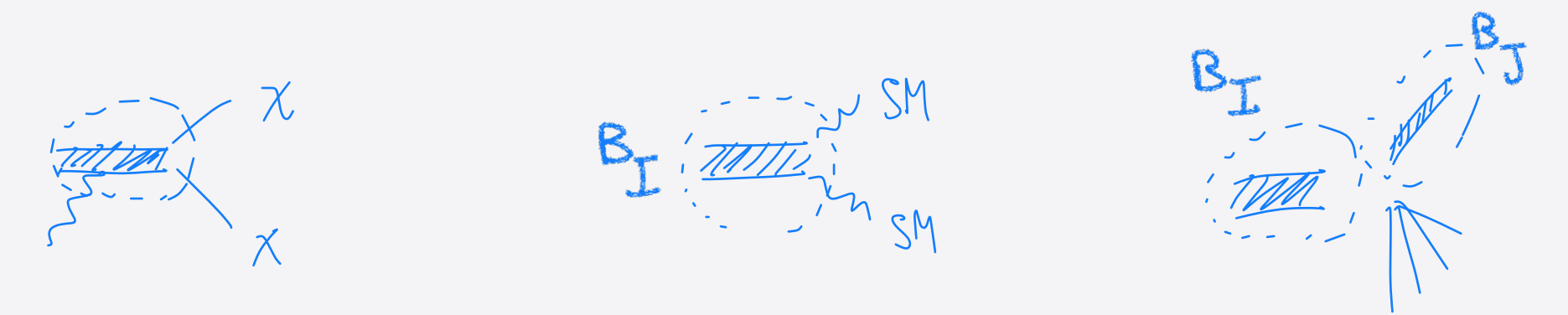
- SM RELATIVISTIC
 - DARK MATTER
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- DARK MATTER BOUND STATES

Following equilibrium thermodynamics the number density of a specie can be predicted at all times it is in equilibrium. Once it drops out from equilibrium Y freezes out and the relic density is fixed.

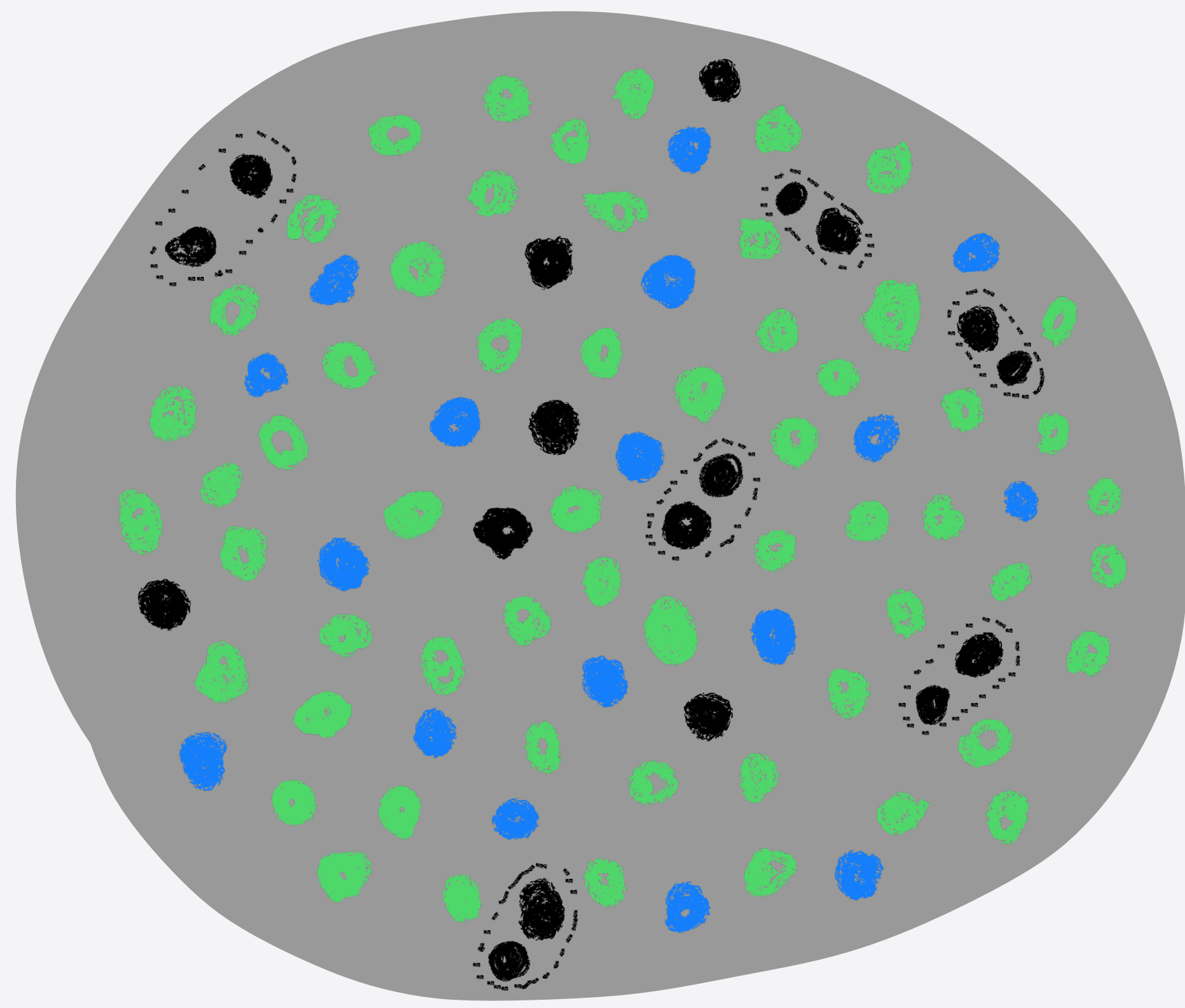
$$z \approx H(T) \frac{dY}{dx} = -\gamma \left(\frac{Y_{DM}^2}{Y_{eq}^2} - 1 \right) - \sum \gamma_i \left(\frac{Y_{DM}}{Y_{eq}^2} - \frac{Y_i}{Y_{eq}} \right)$$



$$s z H \frac{dY_{B_I}}{dx} = \Gamma_{B_I, \text{prod}} \left(\frac{Y_{DM}^2}{Y_{eq}^2} - \frac{Y_{B_I}}{Y_{B_I}^{eq}} \right) + \Gamma_{B_I, \text{ann}} \left(1 - \frac{Y_{B_I}}{Y_{B_I}^{eq}} \right) + \sum \Gamma_{I,J} \left(\frac{Y_{B_I}}{Y_{B_I}^{eq}} - \frac{Y_{B_J}}{Y_{B_J}^{eq}} \right)$$



A STILL SIMPLE EXPLANATION FOR ITS PRODUCTION

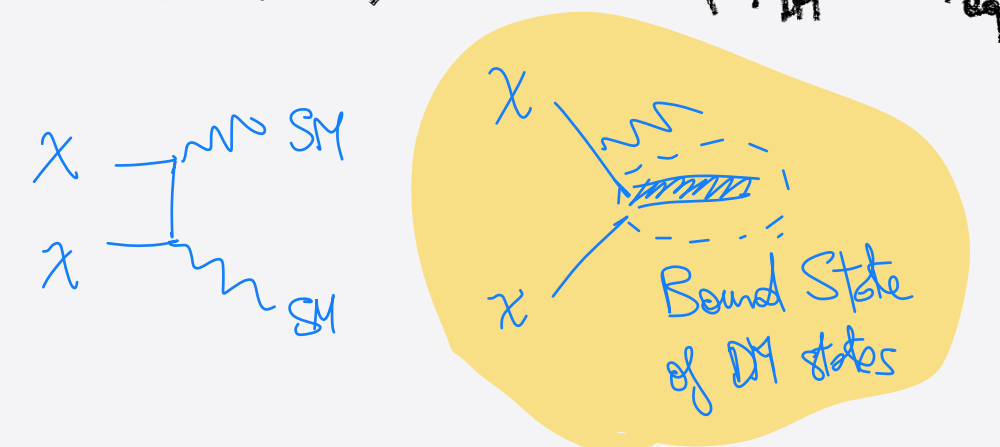


- SM RELATIVISTIC
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 DARK MATTER BOUND STATES

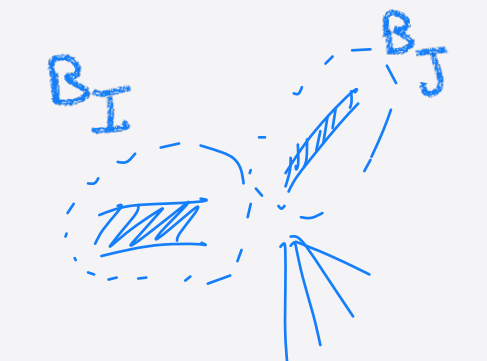
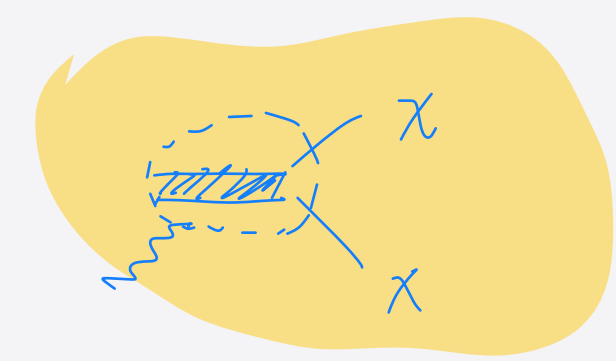
Following equilibrium thermodynamics the number density of a specie can be predicted at all times it is in equilibrium. Once it drops out from equilibrium Y freezes out and the relic density is fixed.

$$z_s H(\tau) \frac{dY}{dx} = -\gamma_2 \left(\frac{Y_{DM}^2}{Y_{eq}^2} - 1 \right) - \sum \gamma_2 \left(\frac{Y_{SM}^2}{Y_{eq}^2} - \frac{Y_{SM}}{Y_{eq}} \right)$$

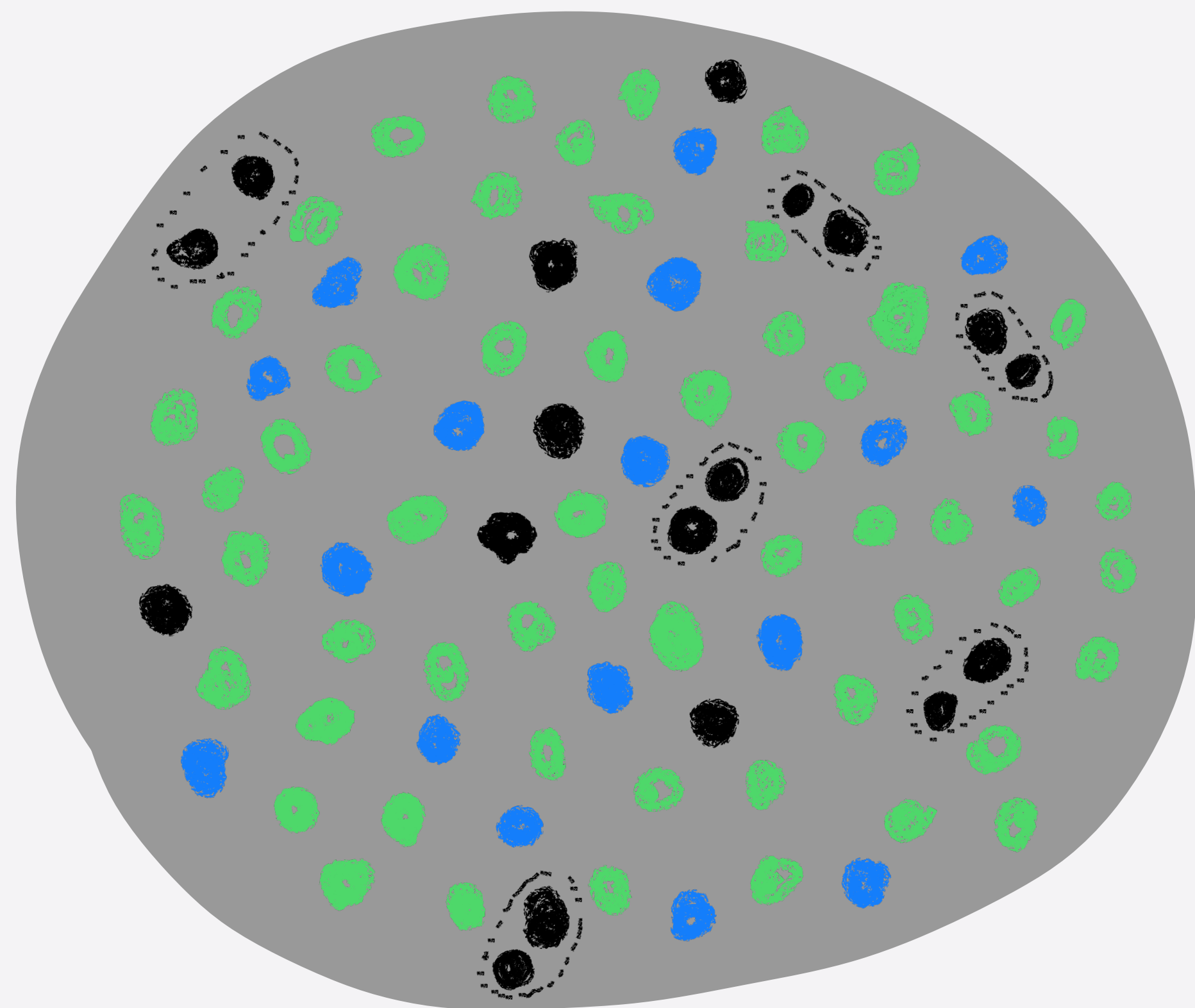


$H \ll \Gamma$

$$s z H \frac{dY_{B_I}}{dx} \Rightarrow \Gamma_{B_I, \text{break}} \left(\frac{Y_{DM}^2}{Y_{eq}^2} - \frac{Y_{B_I}}{Y_{B_I}^{eq}} \right) + \Gamma_{B_I, \text{ann}} \left(1 - \frac{Y_{B_I}}{Y_{B_I}^{eq}} \right) + \sum \Gamma_{I,J} \left(\frac{Y_{B_I}}{Y_{B_I}^{eq}} - \frac{Y_{B_I}}{Y_{B_J}^{eq}} \right)$$



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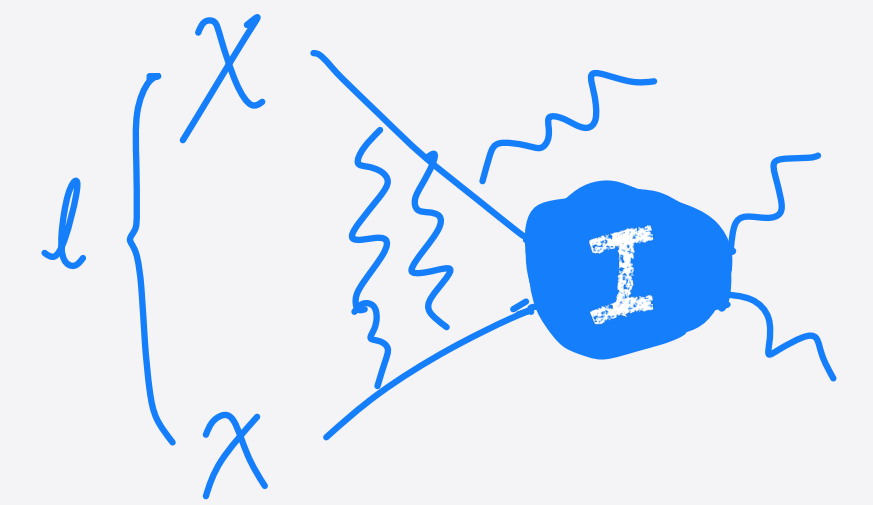
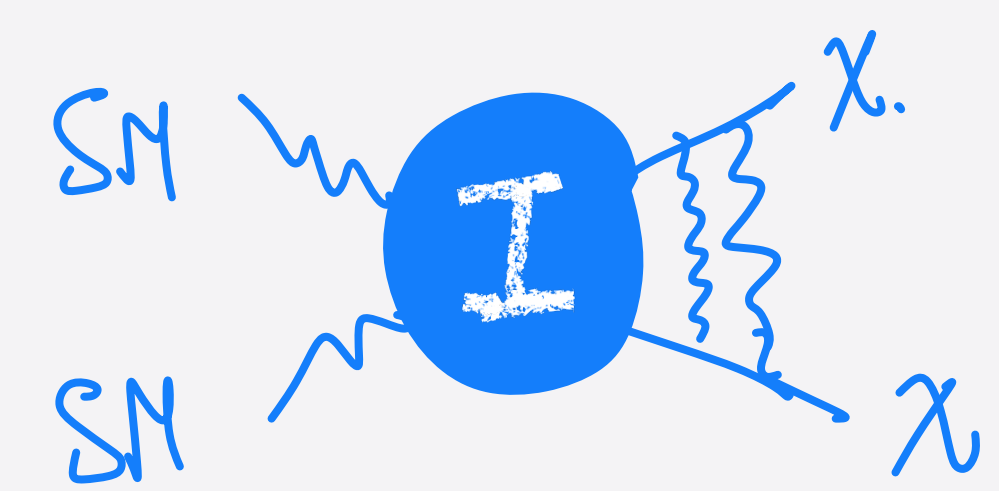
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DARK MATTER BOUND STATES

$$x H \frac{dY}{dx} = - \langle \sigma_{eff} v \rangle s (Y^2 - Y_{eq}^2)$$

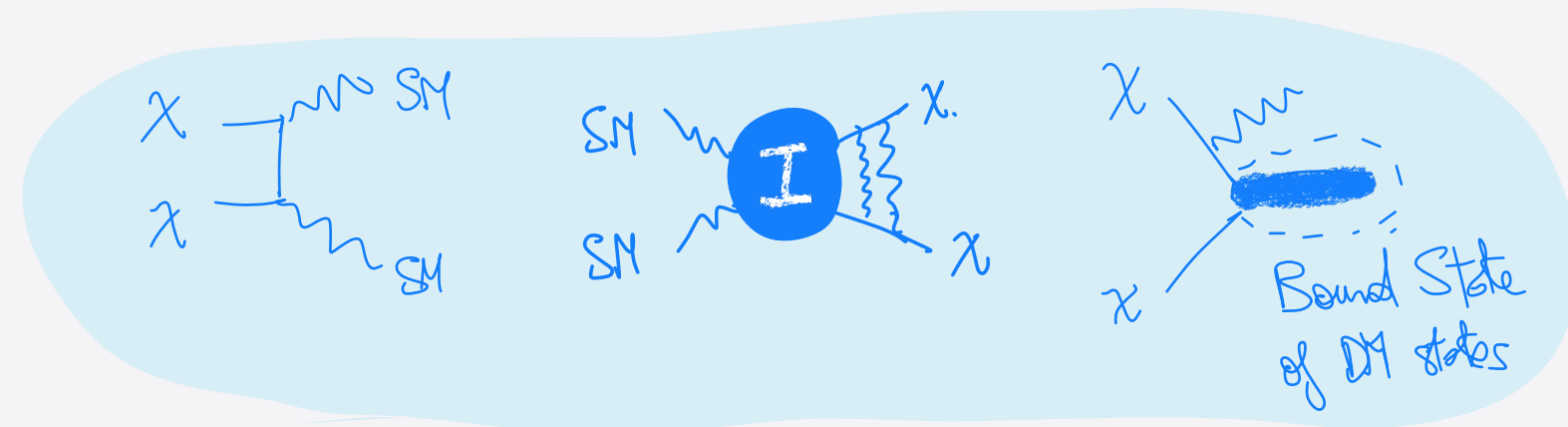
$$\langle \sigma_{eff} v_{rel} \rangle = \sum_I \langle S_E^{(I)} \tilde{\sigma}_{om}^{(I)} v_{rel} \rangle + \sum_{\substack{I, J \\ I \neq J}} S_E^{(I)} S_{B_j}^{(I)} R_{B_j}$$



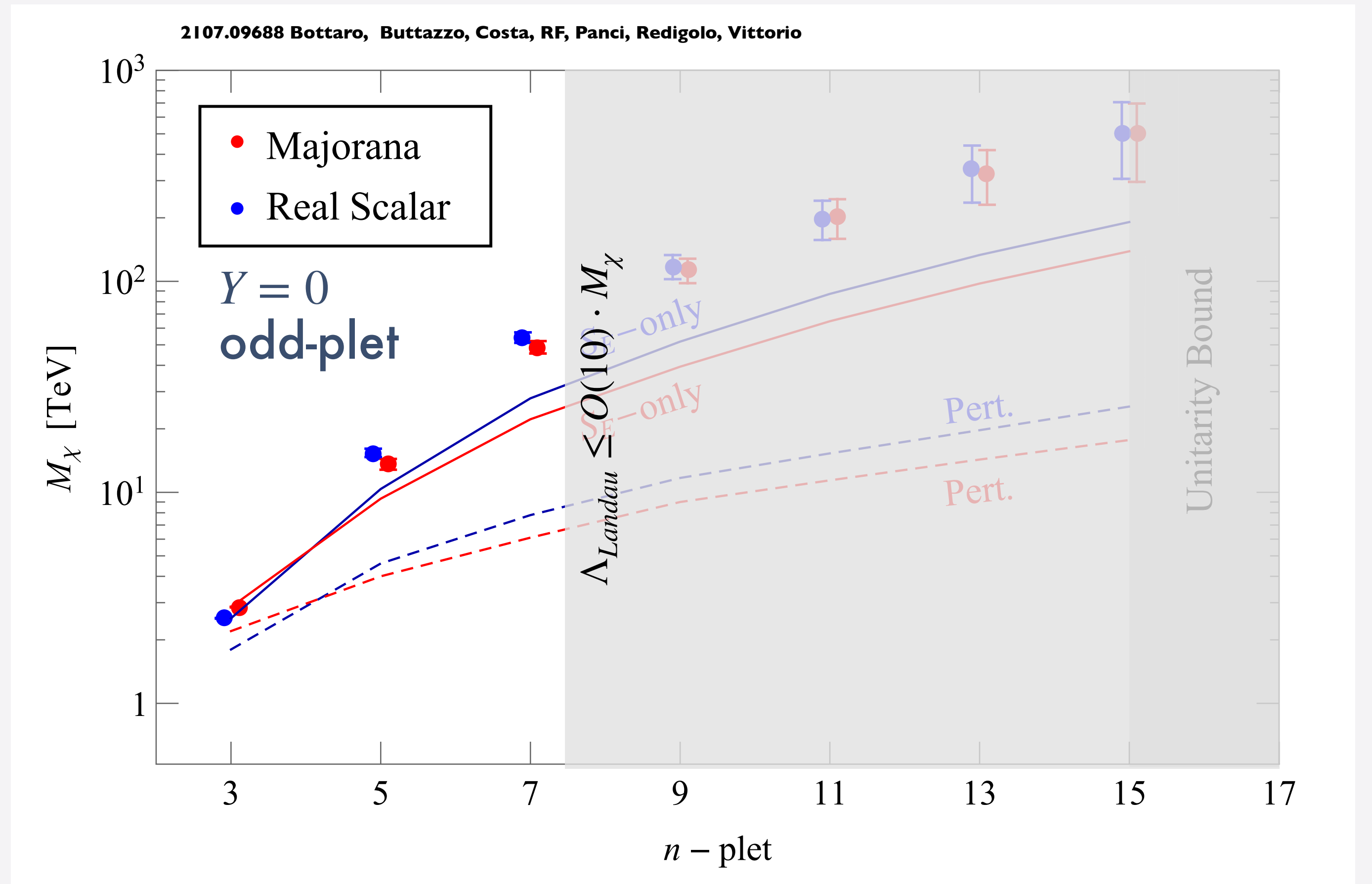
channel-by-channel Sommerfeld enhancement (resummation)

AN "INTERPOLATOR" MODEL

$$\Omega_{nr} \sim \frac{1}{\sigma_{ann}} \sim \frac{M^2}{C_n \cdot g^2}$$



given n the mass is predicted
understood as the maximal mass for that n

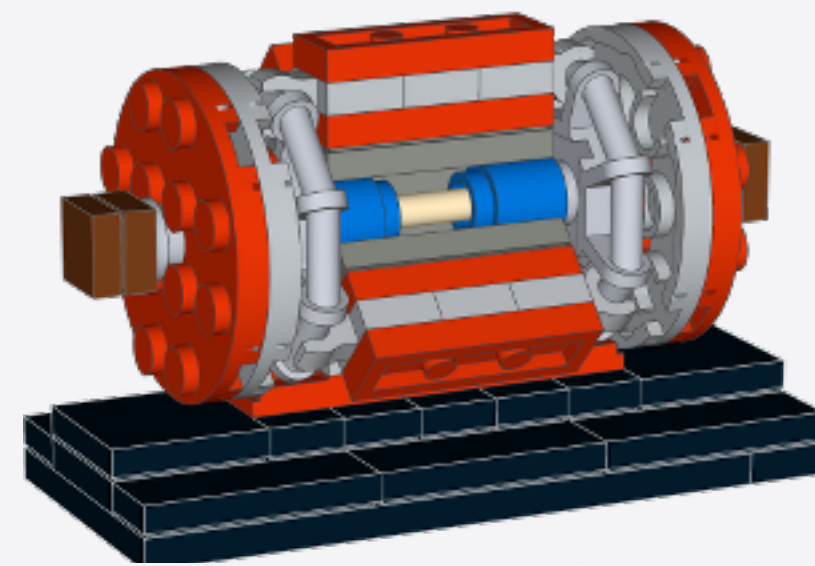


If Dark Matter feels SM weak interactions we can use the general n -plet WIMP to measure how well we are able to test this hypothesis and possibly discover or exclude one or several or the whole category of DM candidates.

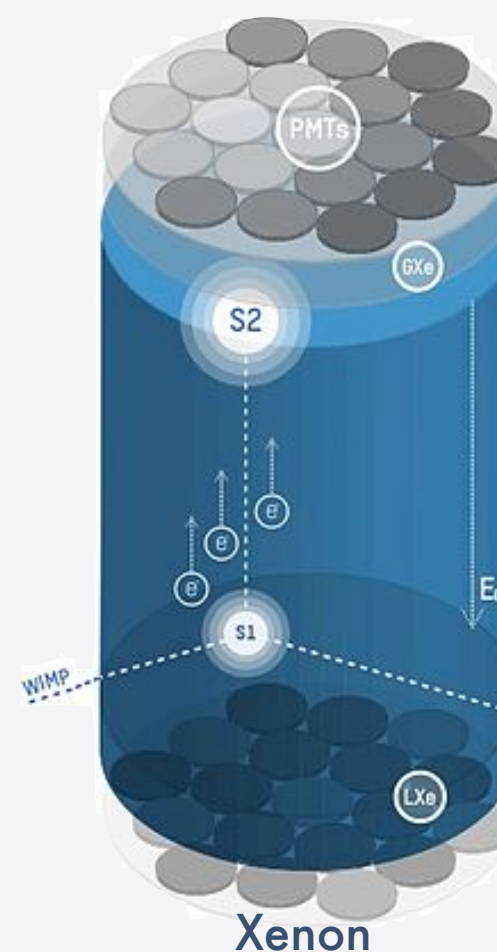
AFTER DECADES OF WIMPs WE MIGHT START TO SEE THE END OF THE WAY (!)

How to thoroughly test it?

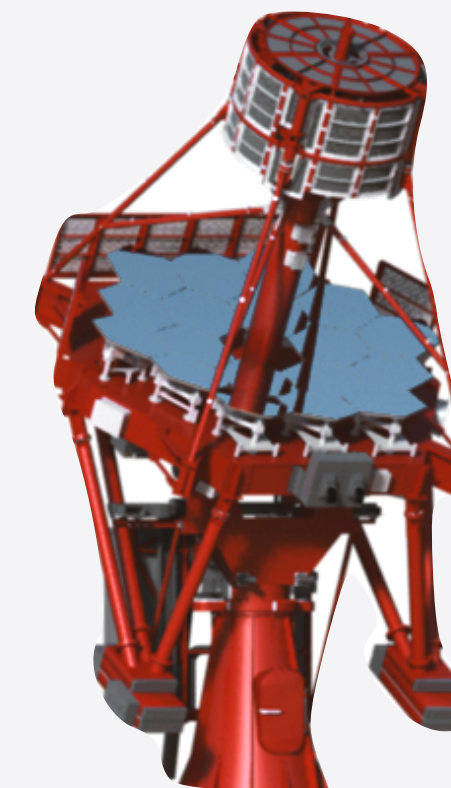
- Produce WIMPs in the lab
- Detect a WIMPs from natural source (big-bang)
- Observe WIMPs interactions (annihilation)
- Future Colliders sensitive to $O(100)$ TeV
- Upcoming nT Xe detectors
- Upcoming Cosmic Rays observatories



Future Collider

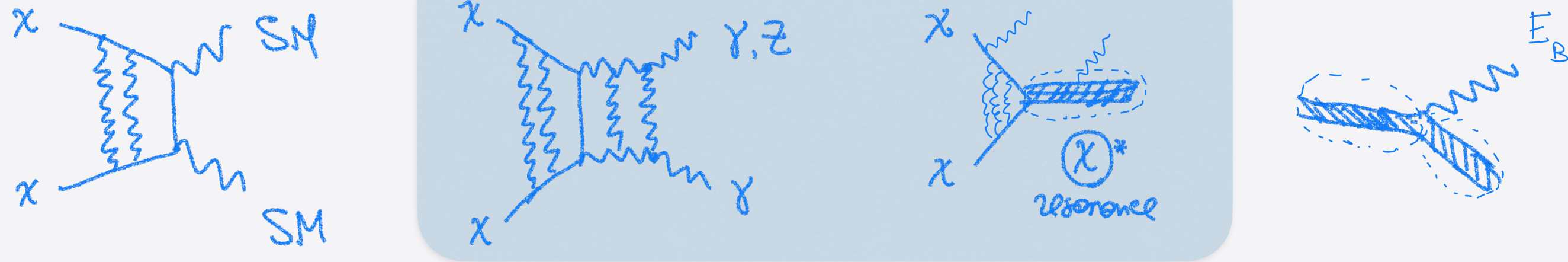


Xenon



CTA

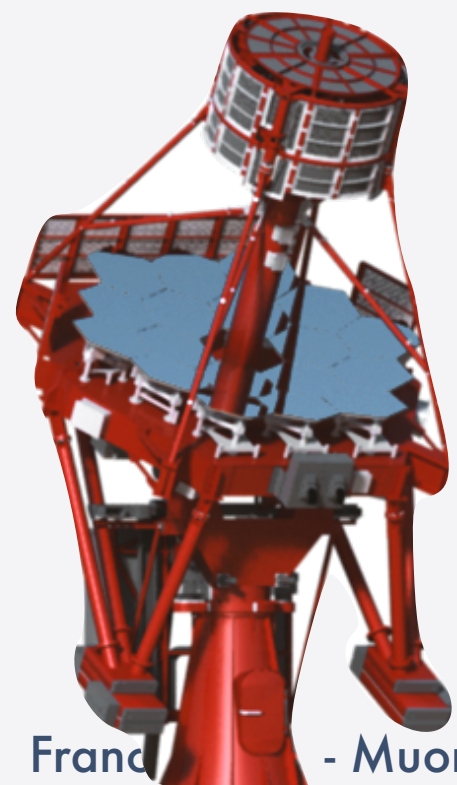
INDIRECT DETECTION



Annihilation in the astrophysical environment result in high-energy SM particle, which can be detector by cosmic rays observatories.

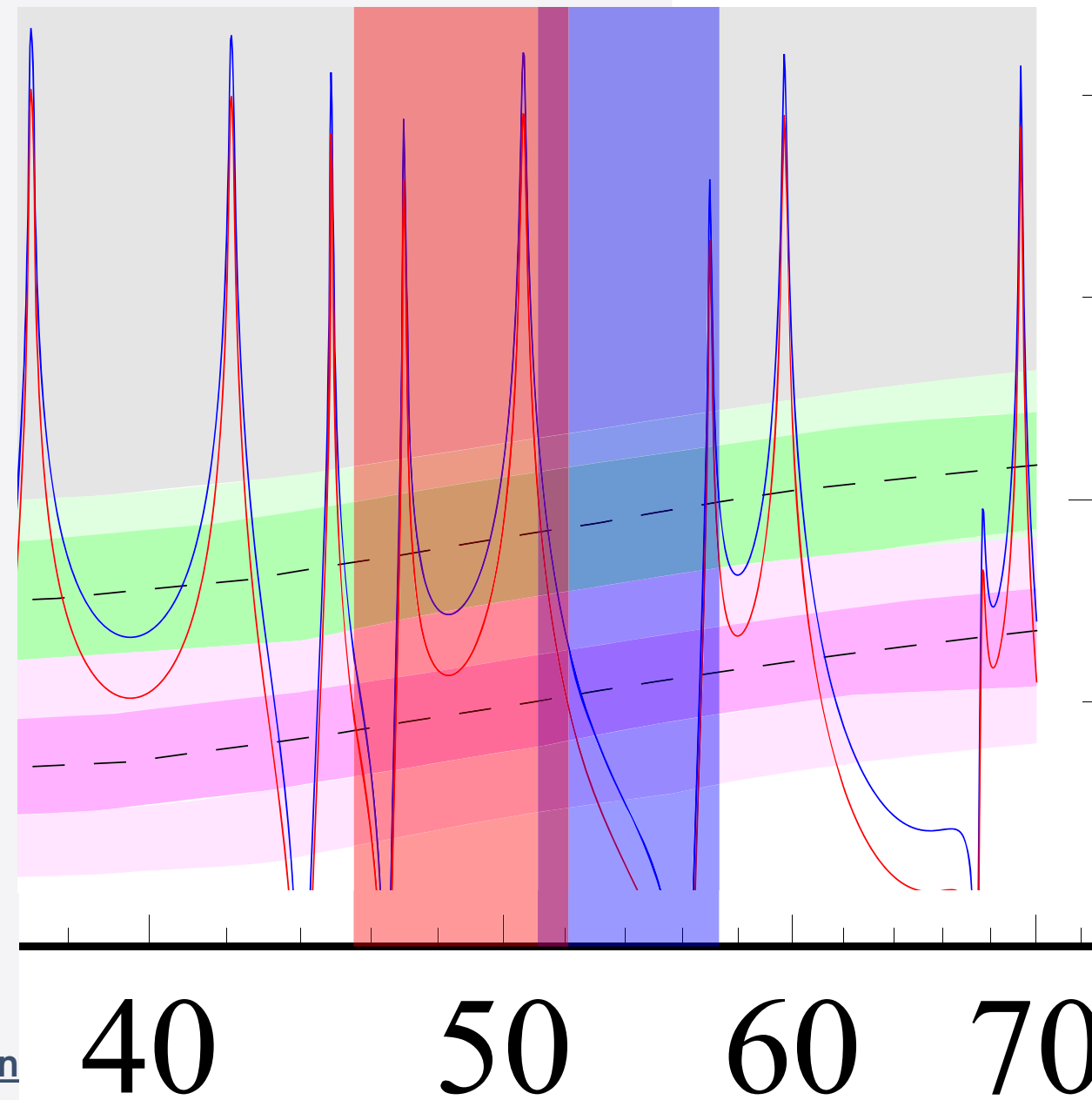
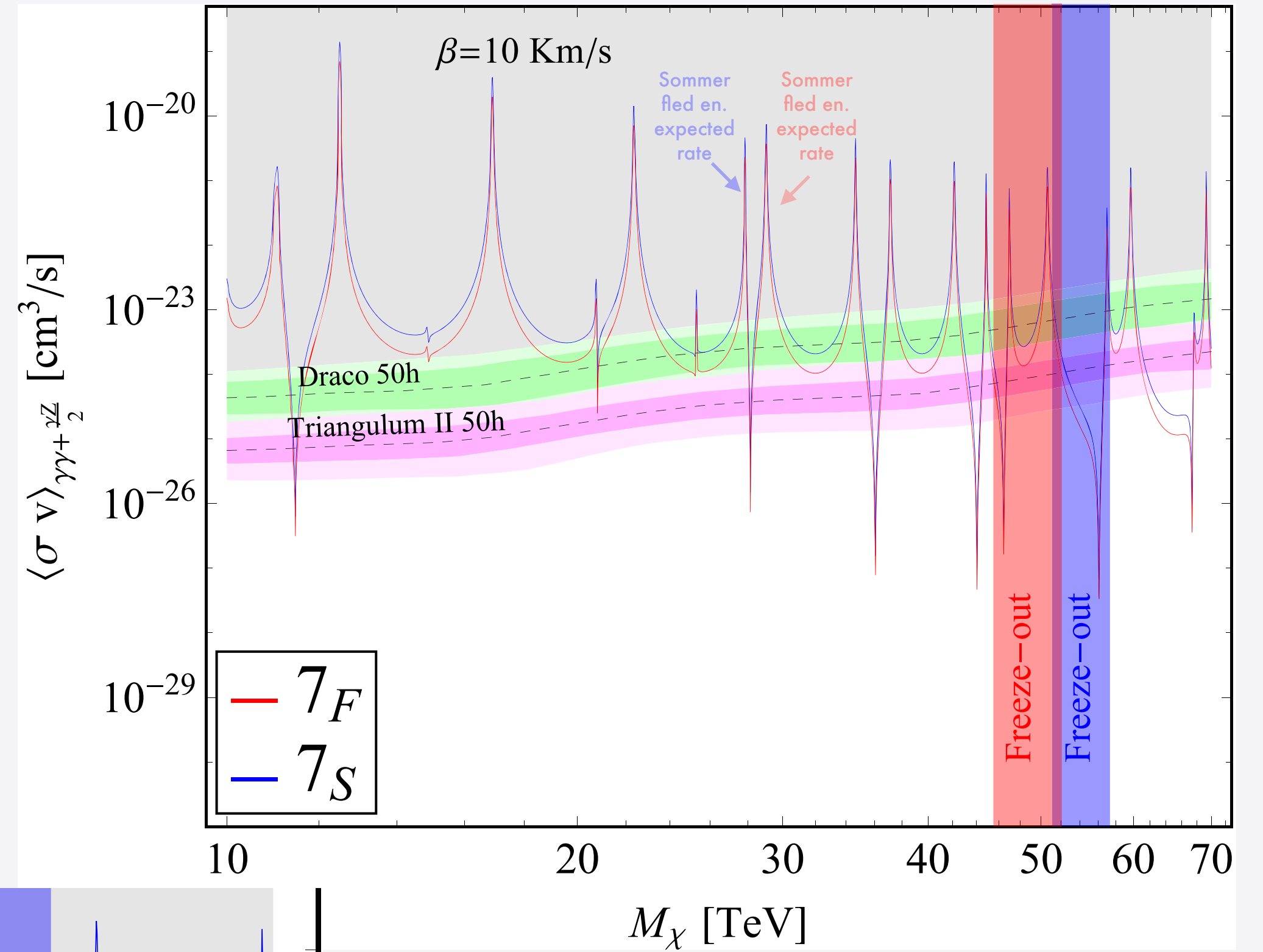
The signature depends on DM mass, possible resonant bound states formation and DM density profile

An excess on monochromatic multi-TeV photons would be quite convincing evidence of DM. The model can be even tested by the presence of multiple "lines" from bound states annihilations and lower energy de-excitation



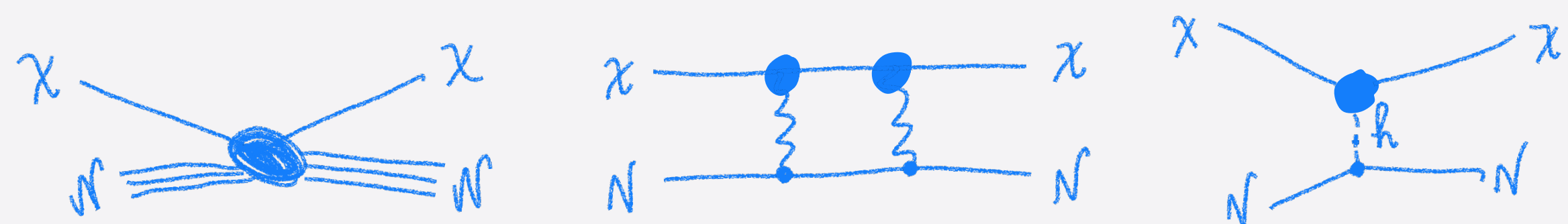
2030s

up to 300 TeV, $\frac{\Delta E}{E} \sim 10\%$



thermal mass "lottery": if the actual mass varies within the current theoretical uncertainty the signal strength changes by orders of magnitude!

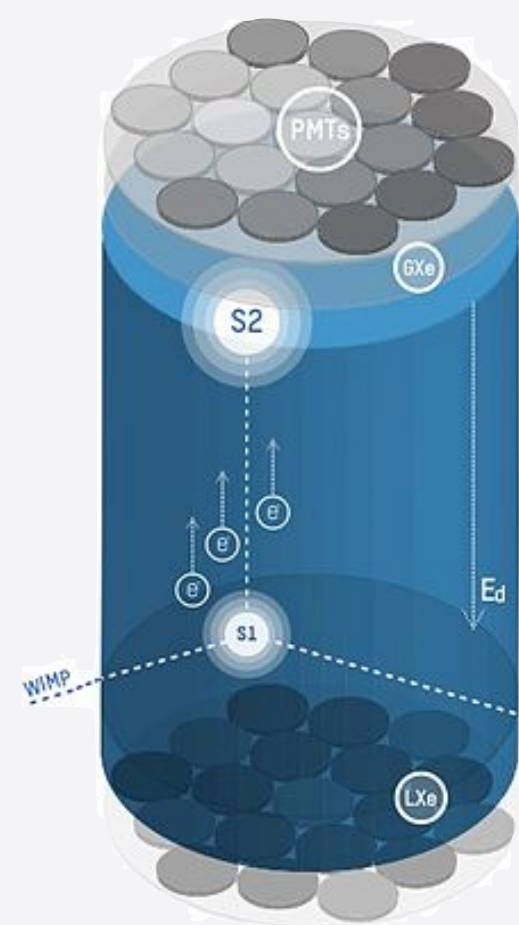
DIRECT DETECTION



Scattering on SM materials can be detected in ultra-low background experiments

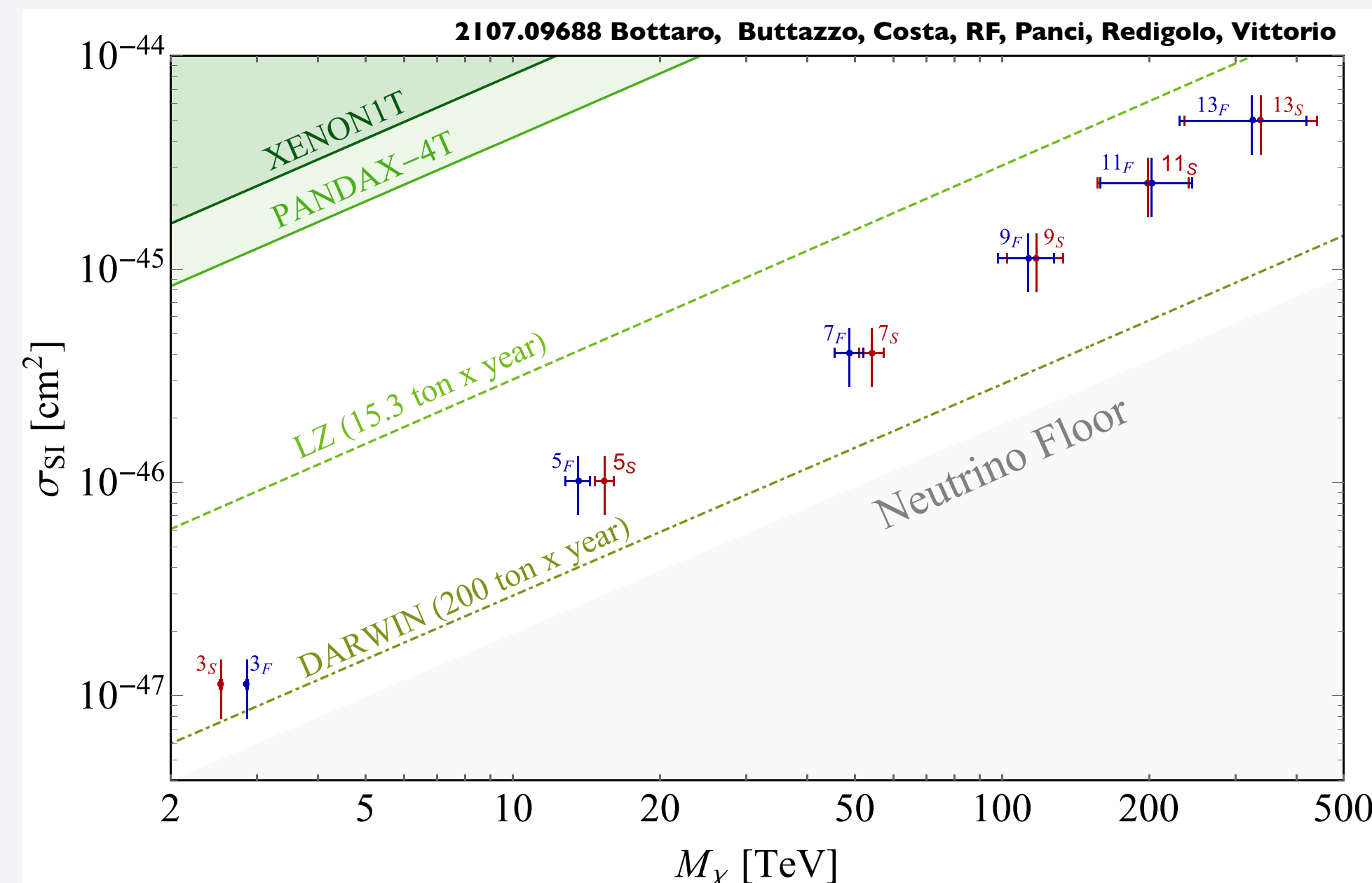
Larger rates for the larger n -plets keep them visible

For such large DM mass the signature does not depend on the DM mass.

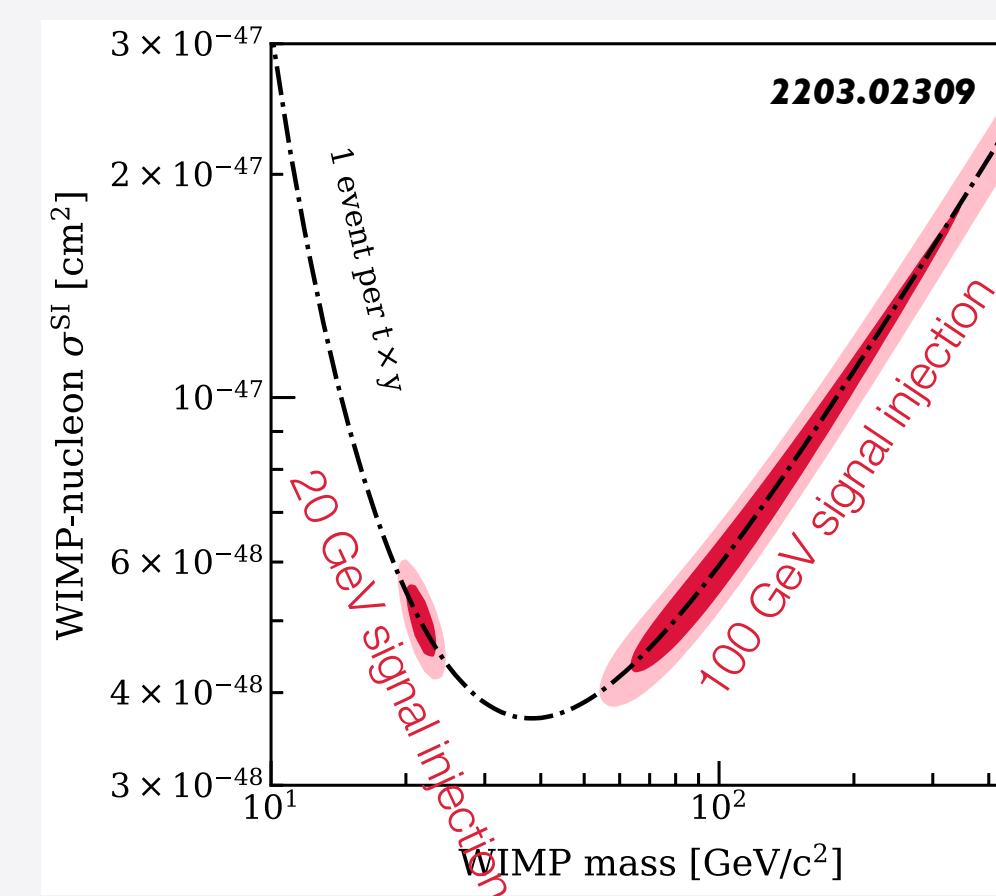


2030s

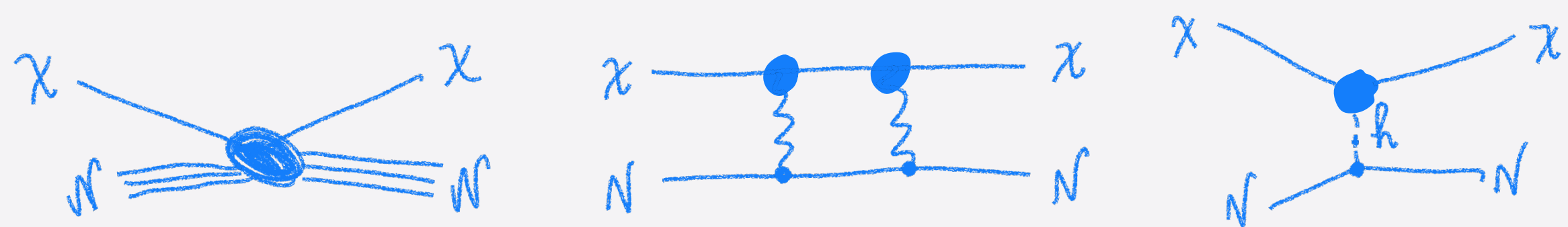
up to $O(\text{PeV})$



An excess would require a "seasonality" check and maybe independent confirmation (many excesses in the past in this type of experiments, though most were at the lowest accessible masses)



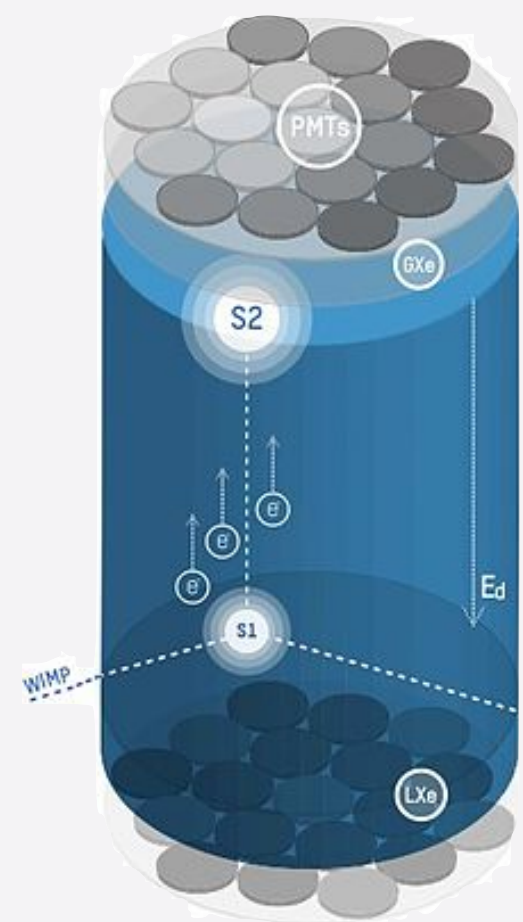
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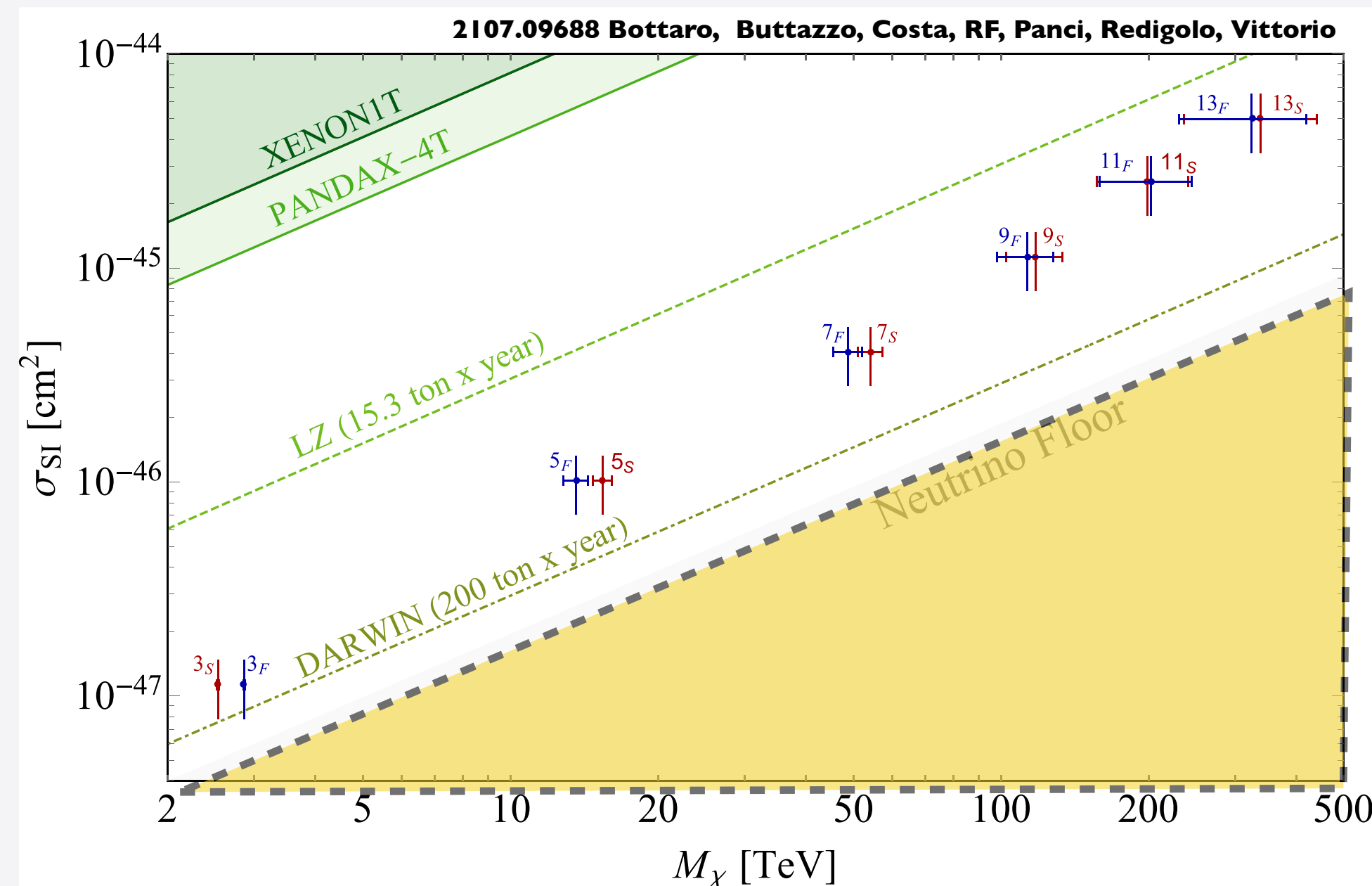
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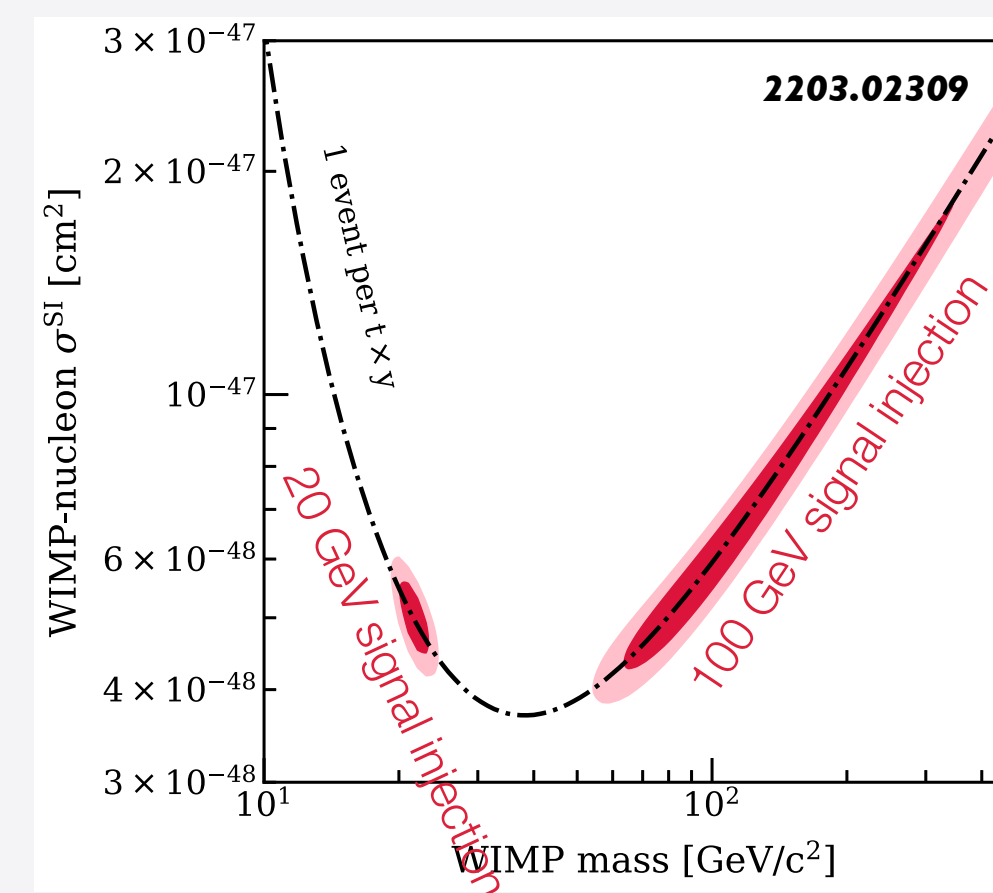


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(IN)DIRECT DETECTION CIRCA 2030s

- Within 10 years we may have a detection of a WIMPs from natural source (big-bang)
- No detection at Darwin may kill the most minimal case ("odd-plet" $Y = 0$)
- Within 10 years we may get indirect observation of WIMPs annihilation
- "No detection" would be harder to interpret, because of possible missing pheno bits (e.g. expected SNR in the astrophysical objects for the actual detector resolution)

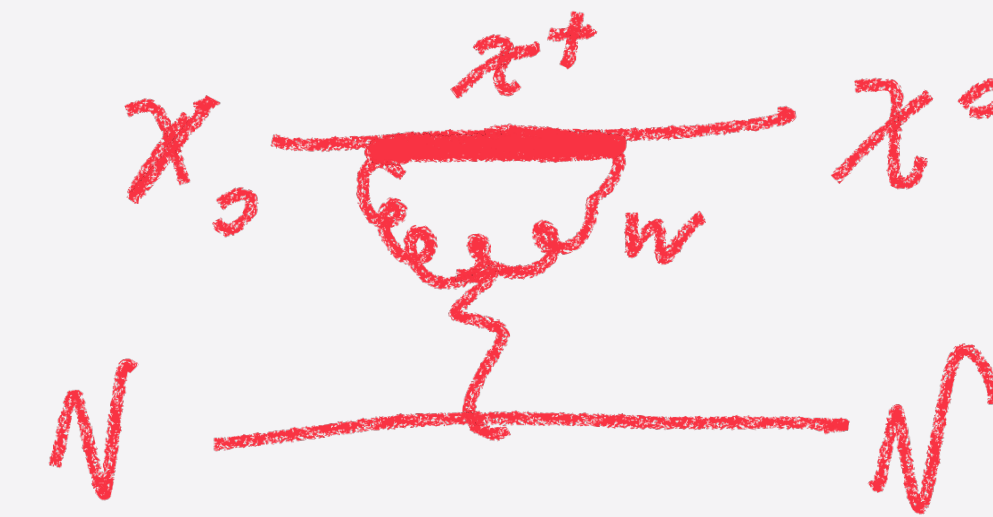
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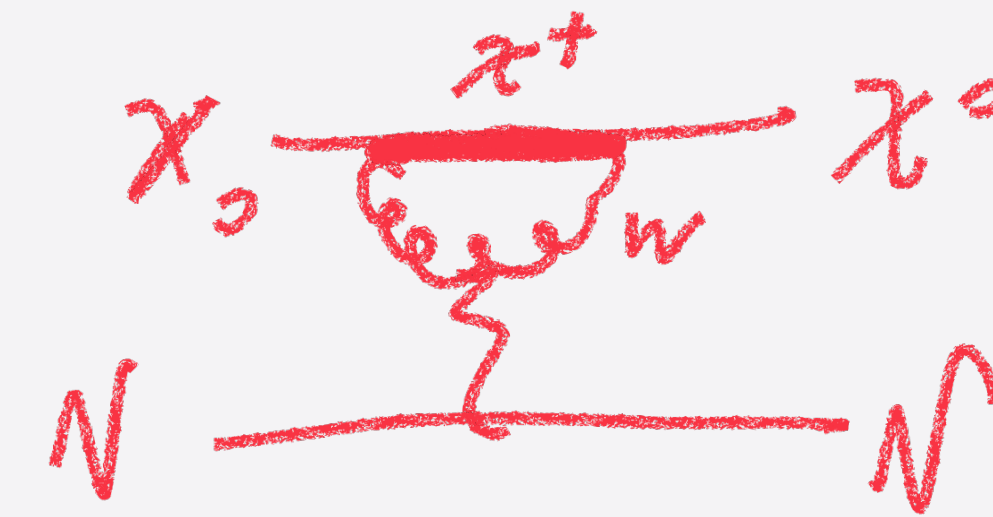
INELASTIC WIMP SCATTERING

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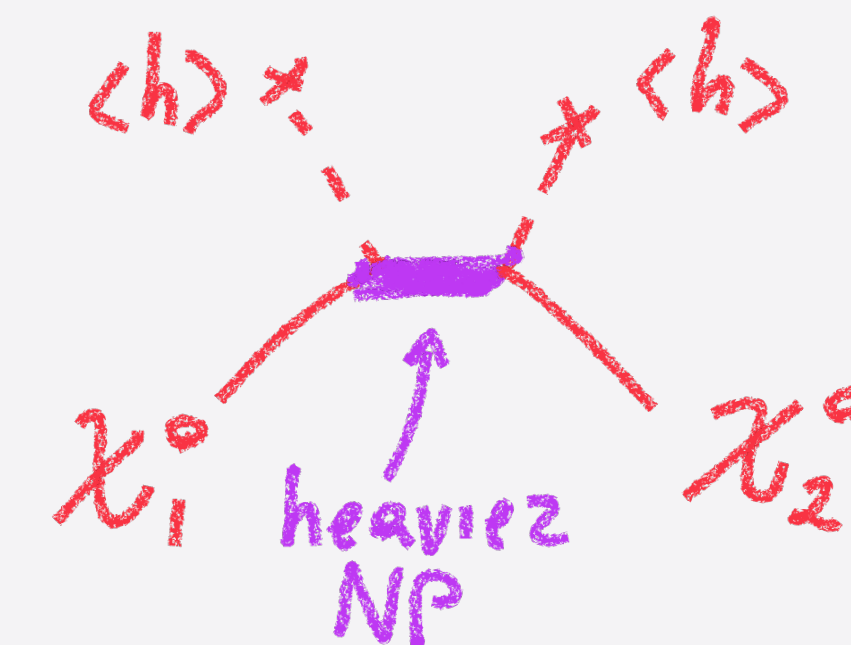
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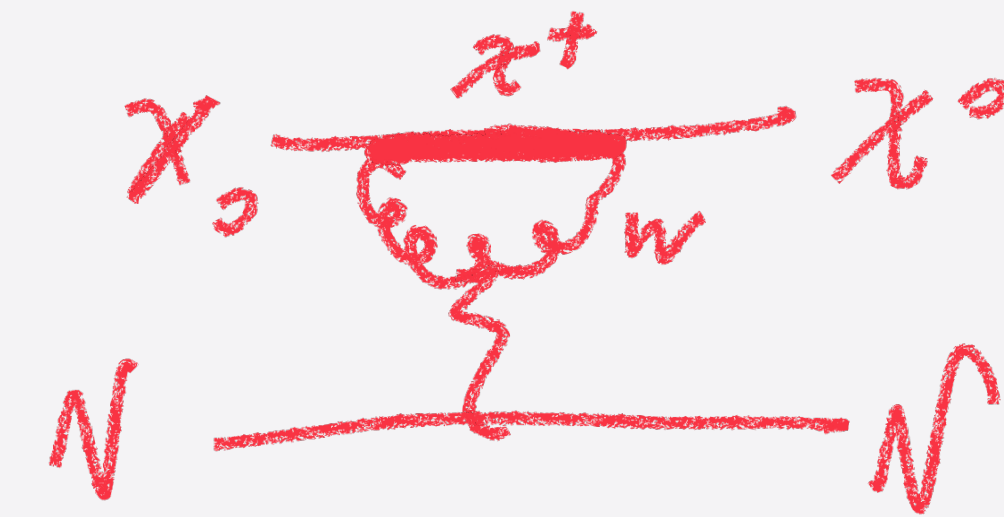
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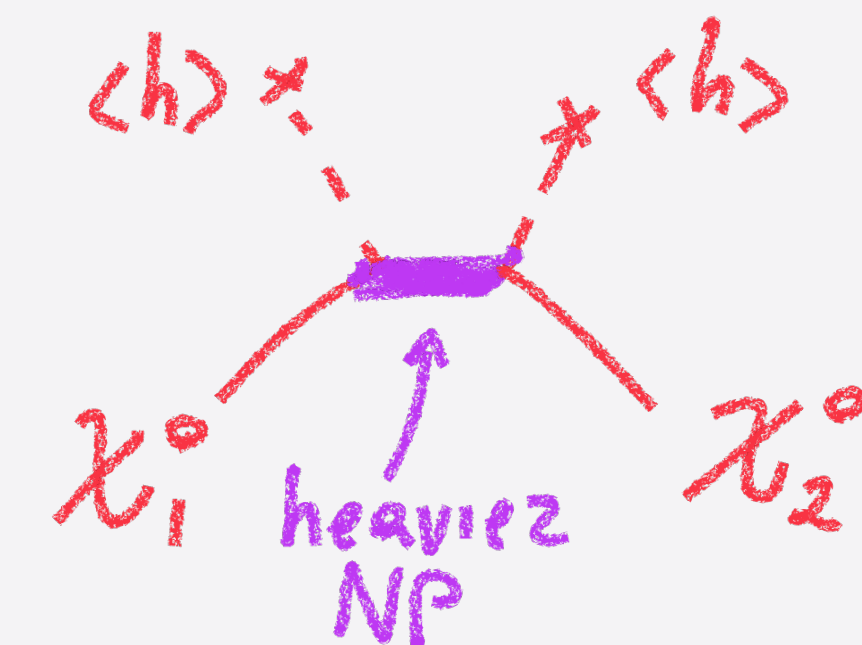
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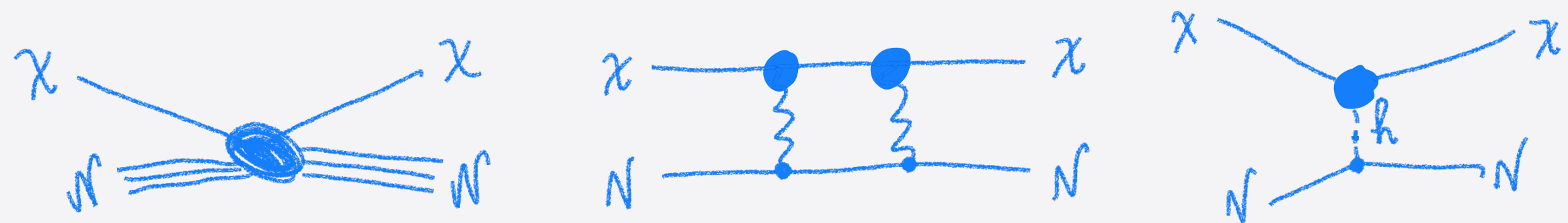
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hypercharge offers one extra handle on the mass splitting

DIRECT DETECTION

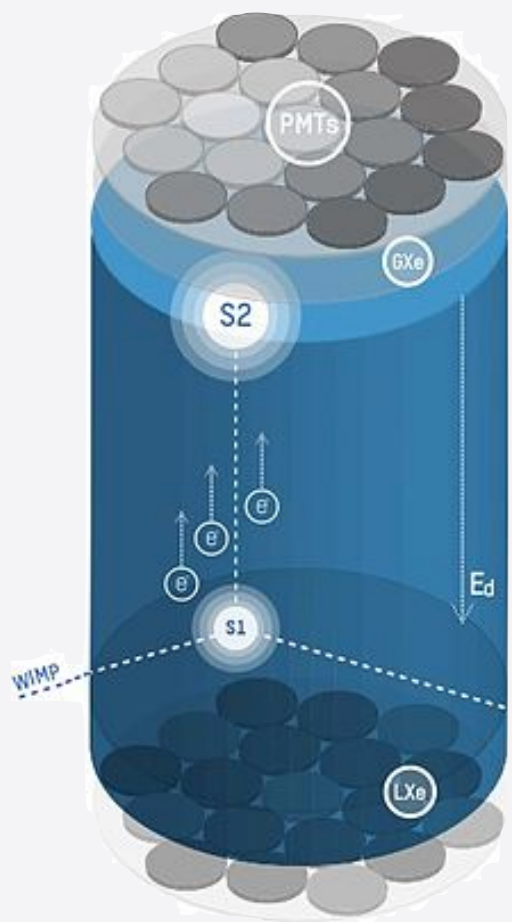
$Y \neq 0$, pure EW Mass-Splitting



Scattering on SM materials can be detected in ultra-low background experiments

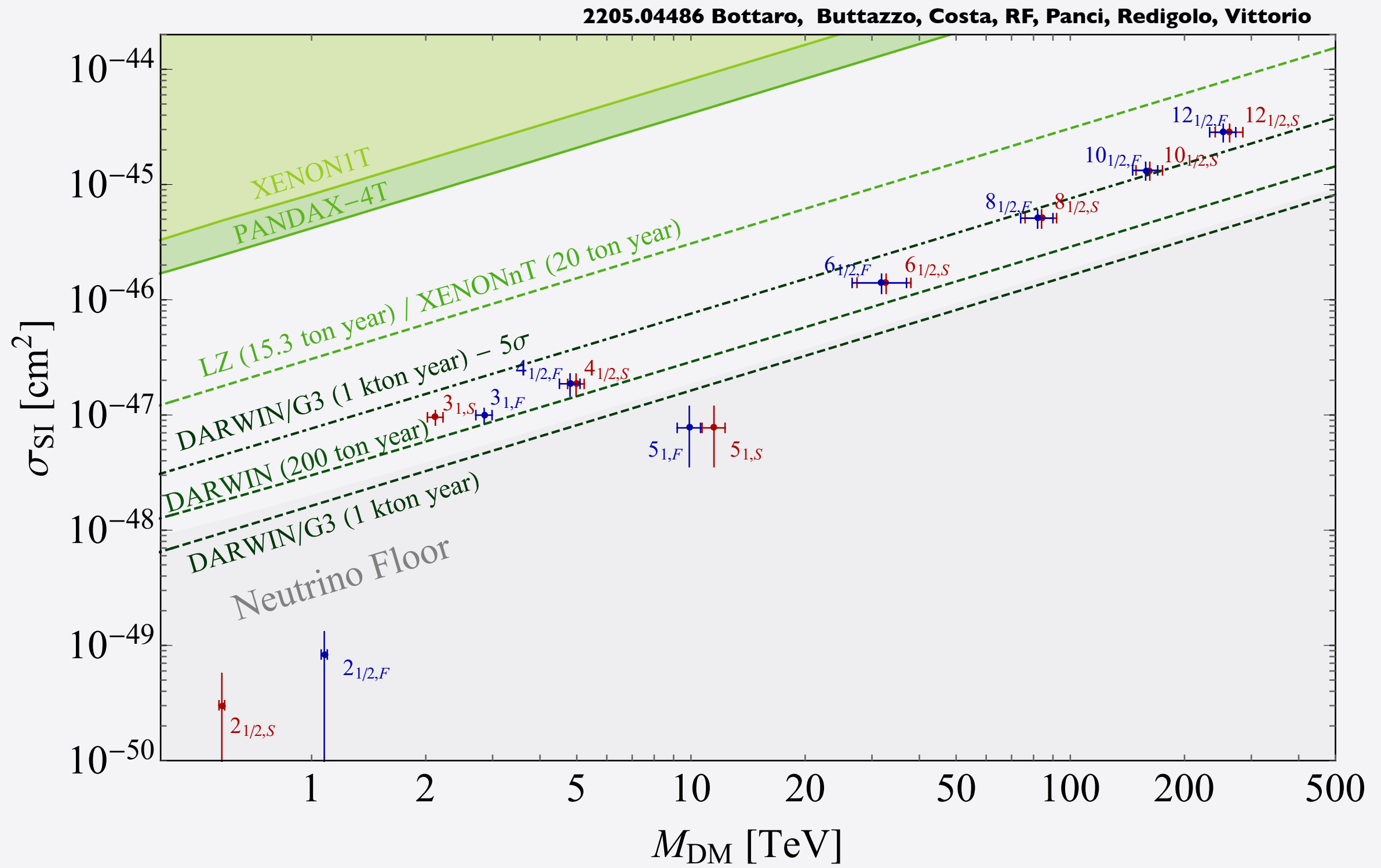
Larger rates for the larger n -plets keep them visible

For such large DM mass the signature does not depend on the DM mass.



2030s

up to $O(\text{PeV})$

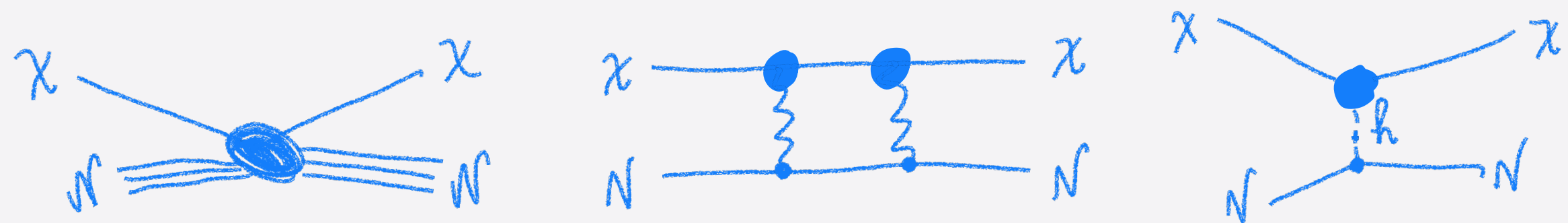


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simple $2n$ -plet scenarios can evade Direct Detection

DIRECT DETECTION

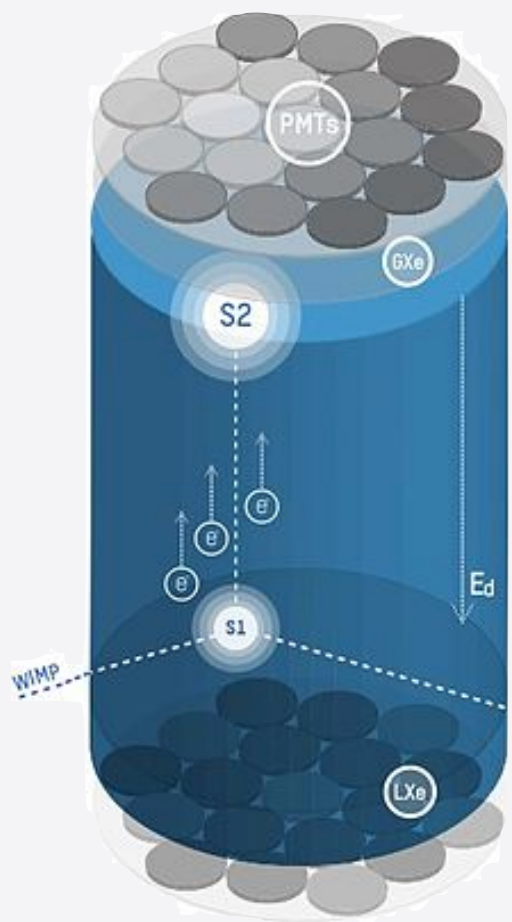
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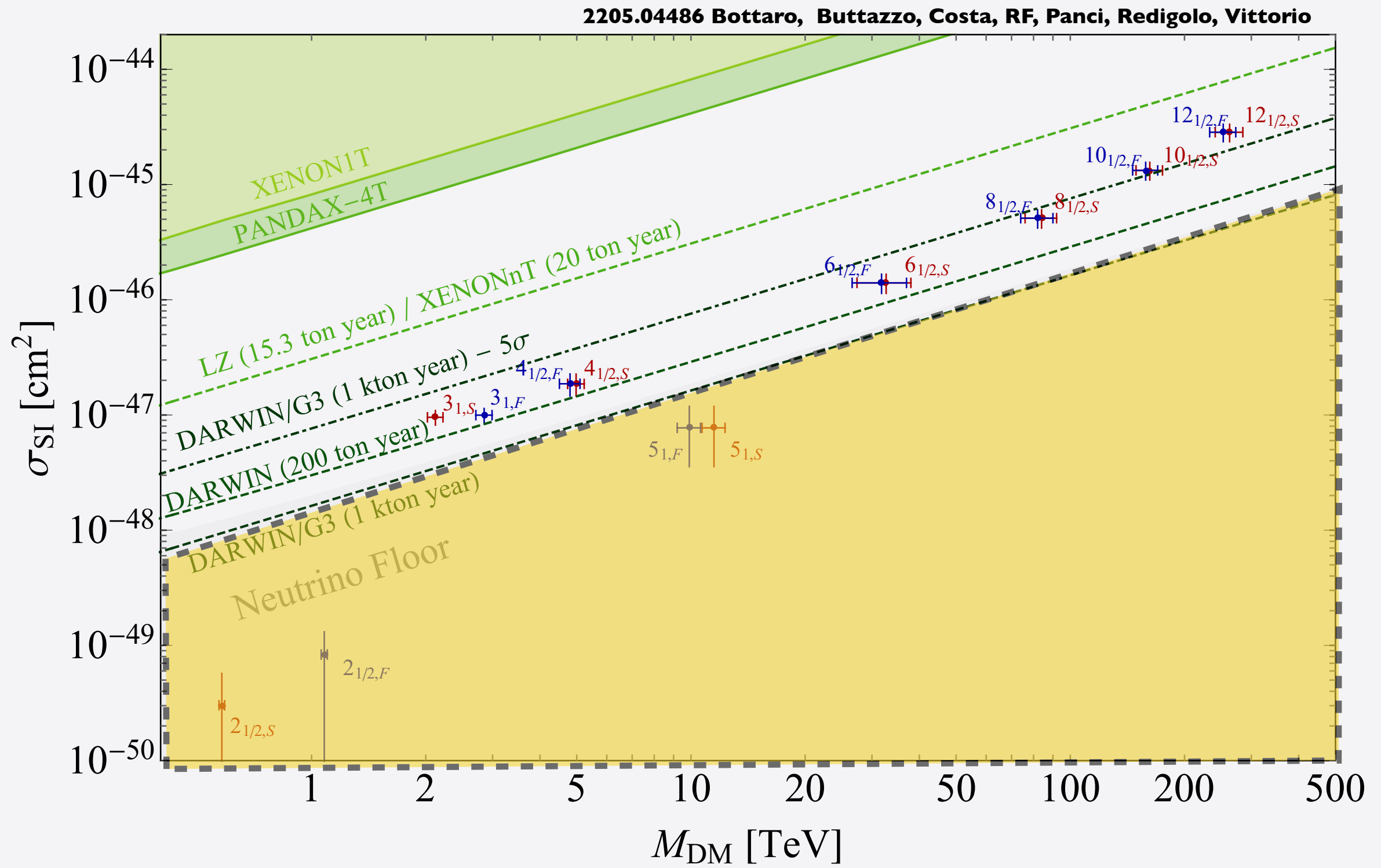
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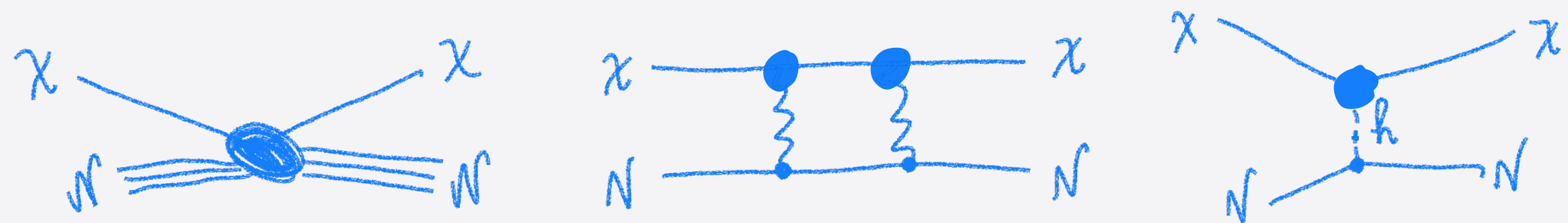
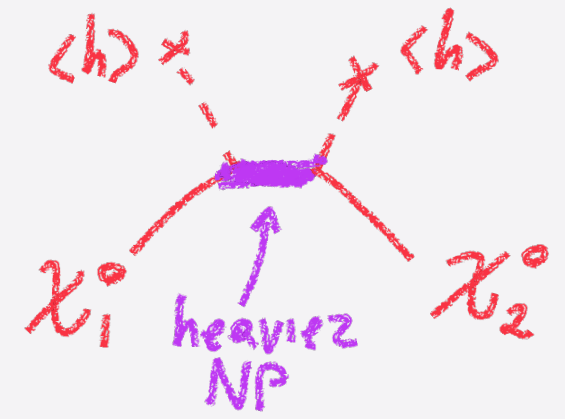


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DIRECT DETECTION

$Y \neq 0$, Mass-Splitting from DIM>4

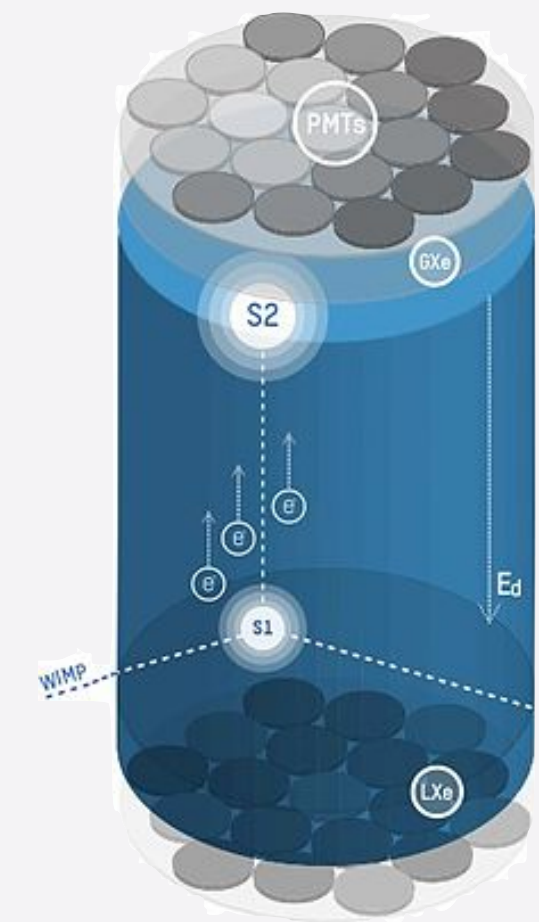
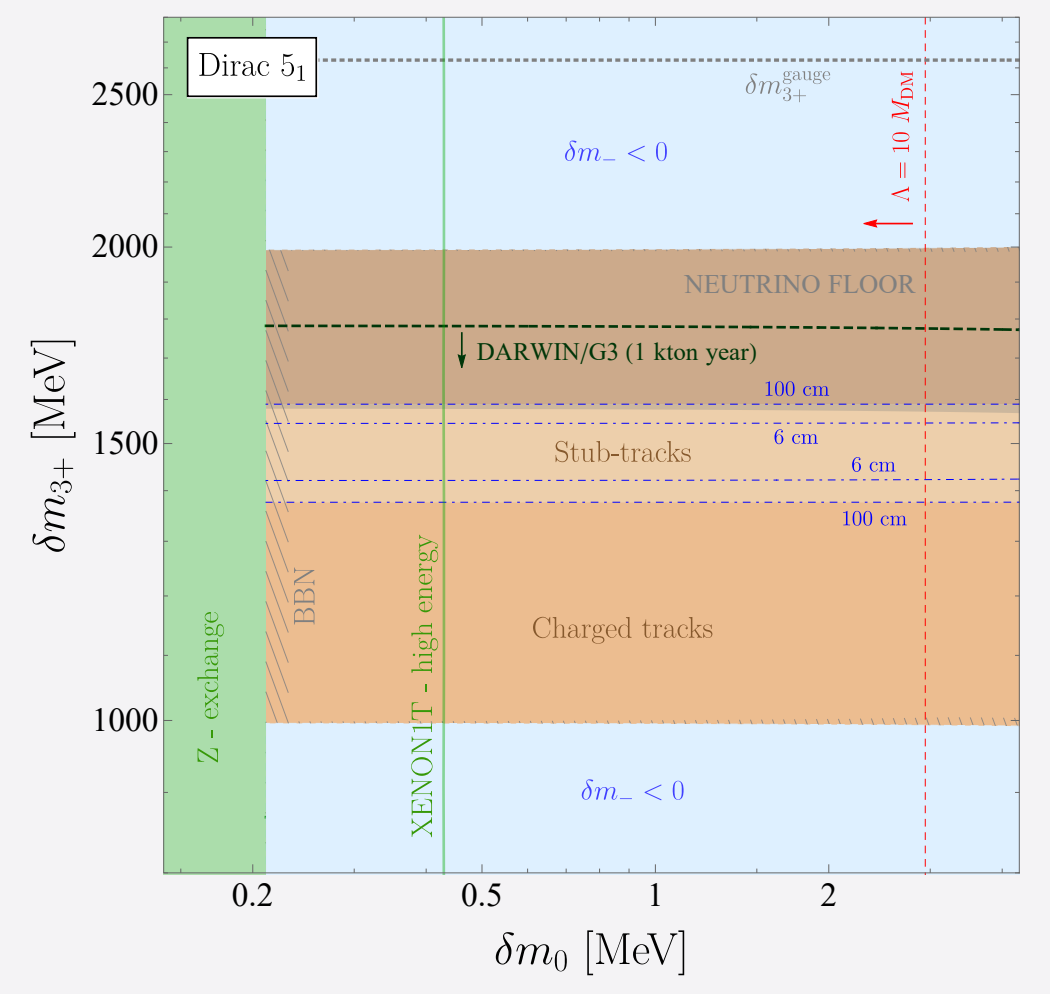
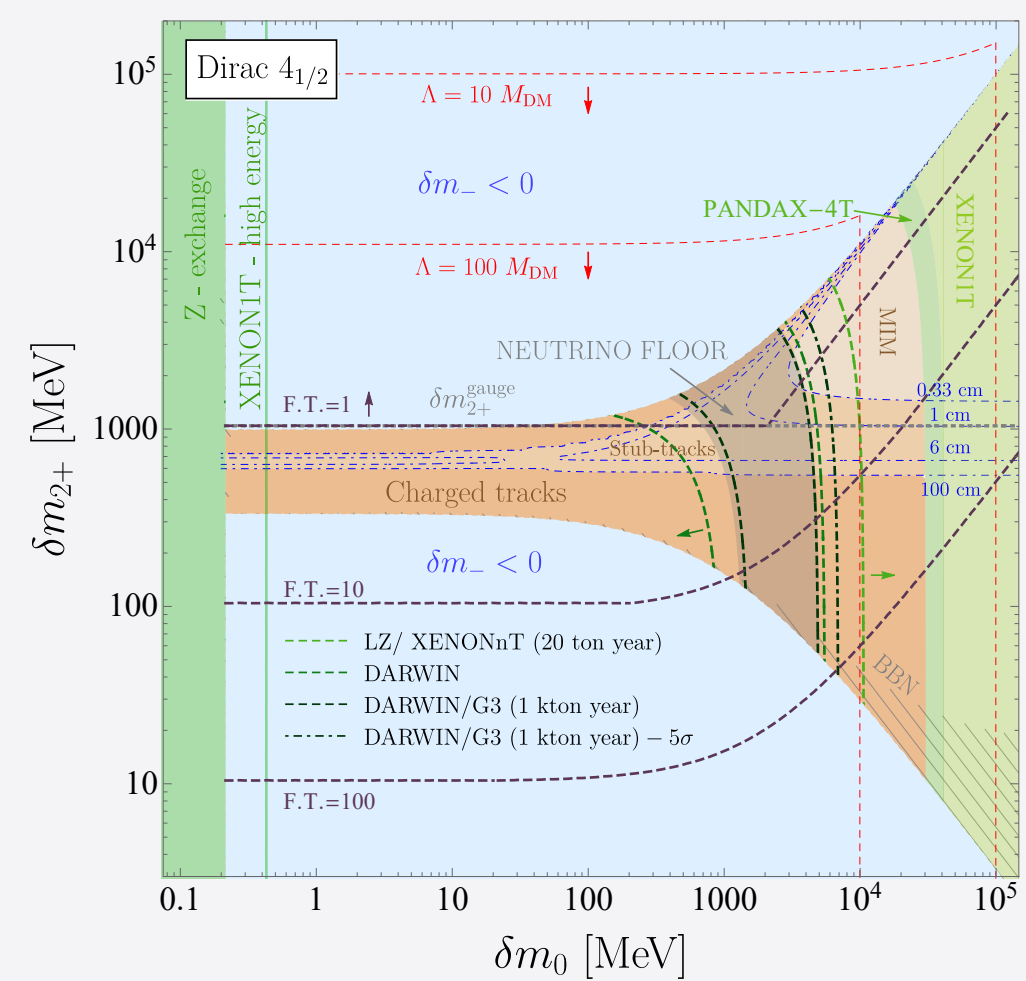
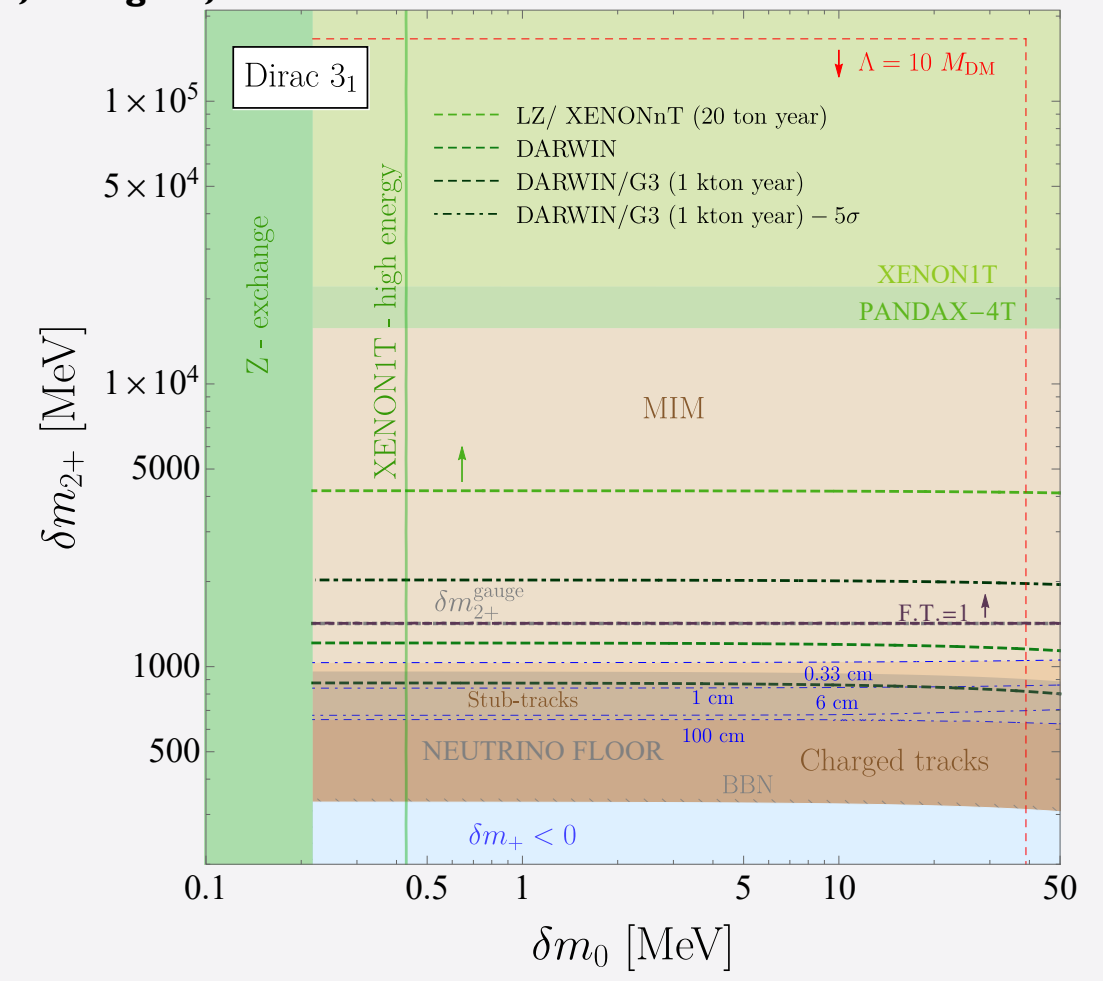
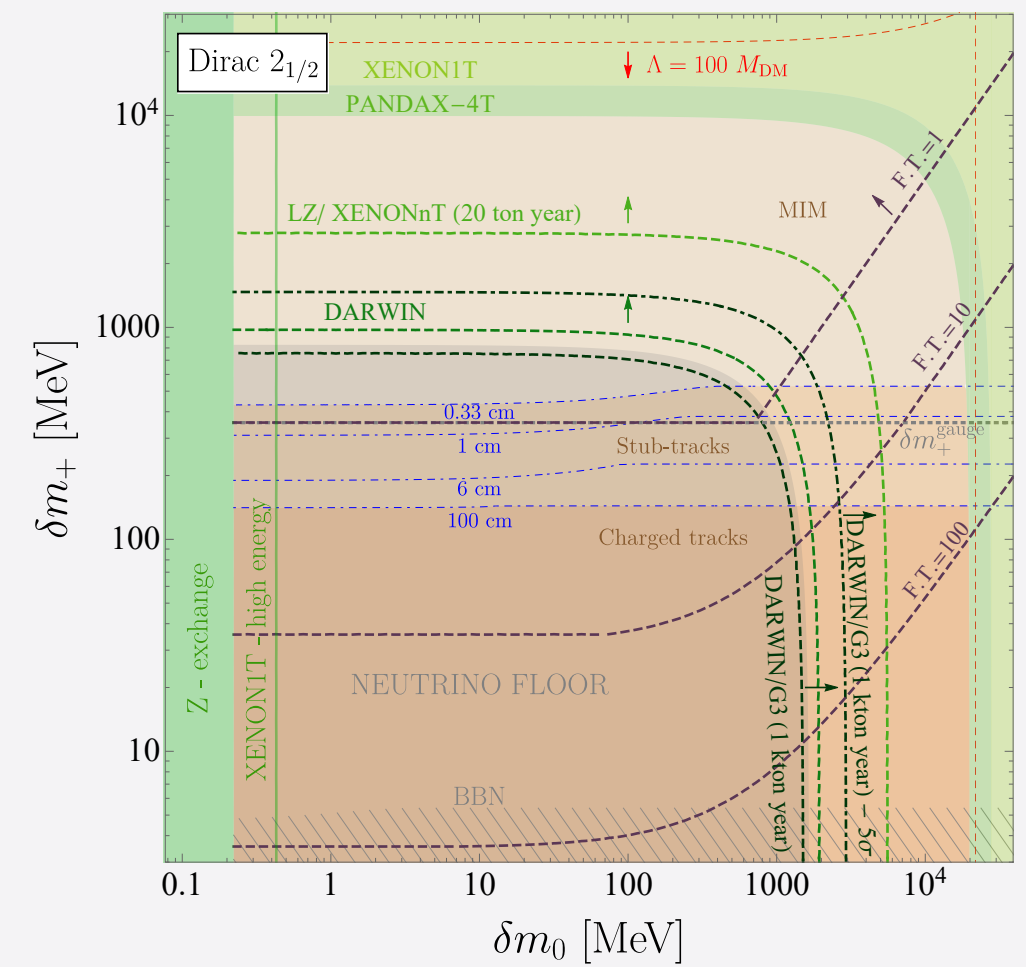


Scattering on SM materials can be detected in ultra-low background experiments

Larger rates for the larger n -plets keep them visible

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2205.04486 Bottaro, Buttazzo, Costa, RF, Panci, Redigolo, Vittorio



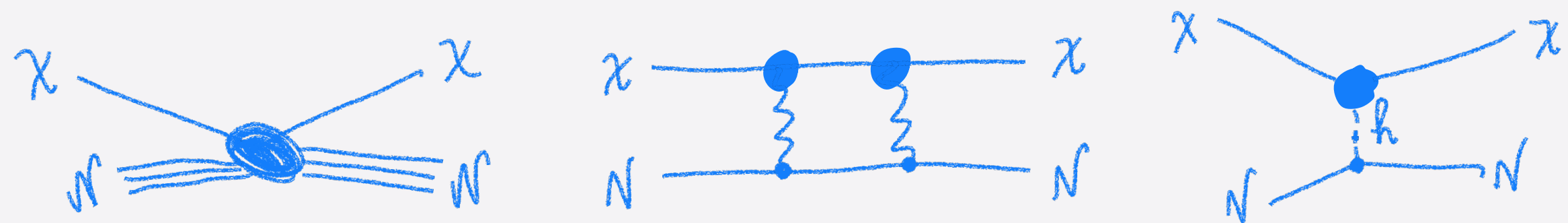
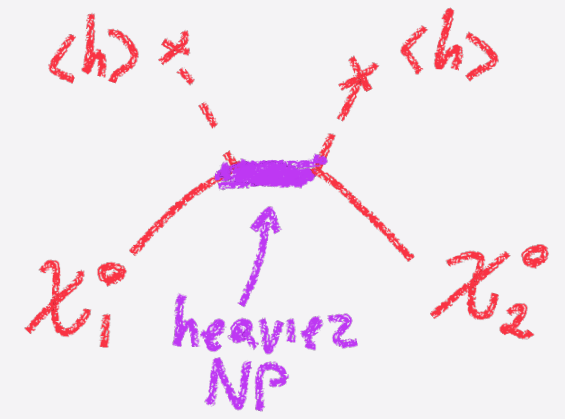
2030s

up to $O(\text{PeV})$

all next-to-simple $2n$ -plet scenarios can evade Direct Detection

DIRECT DETECTION

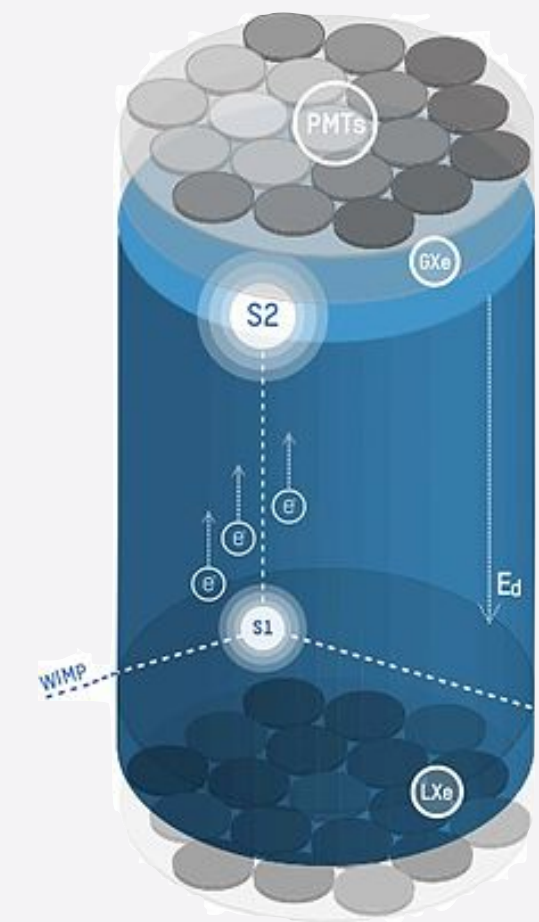
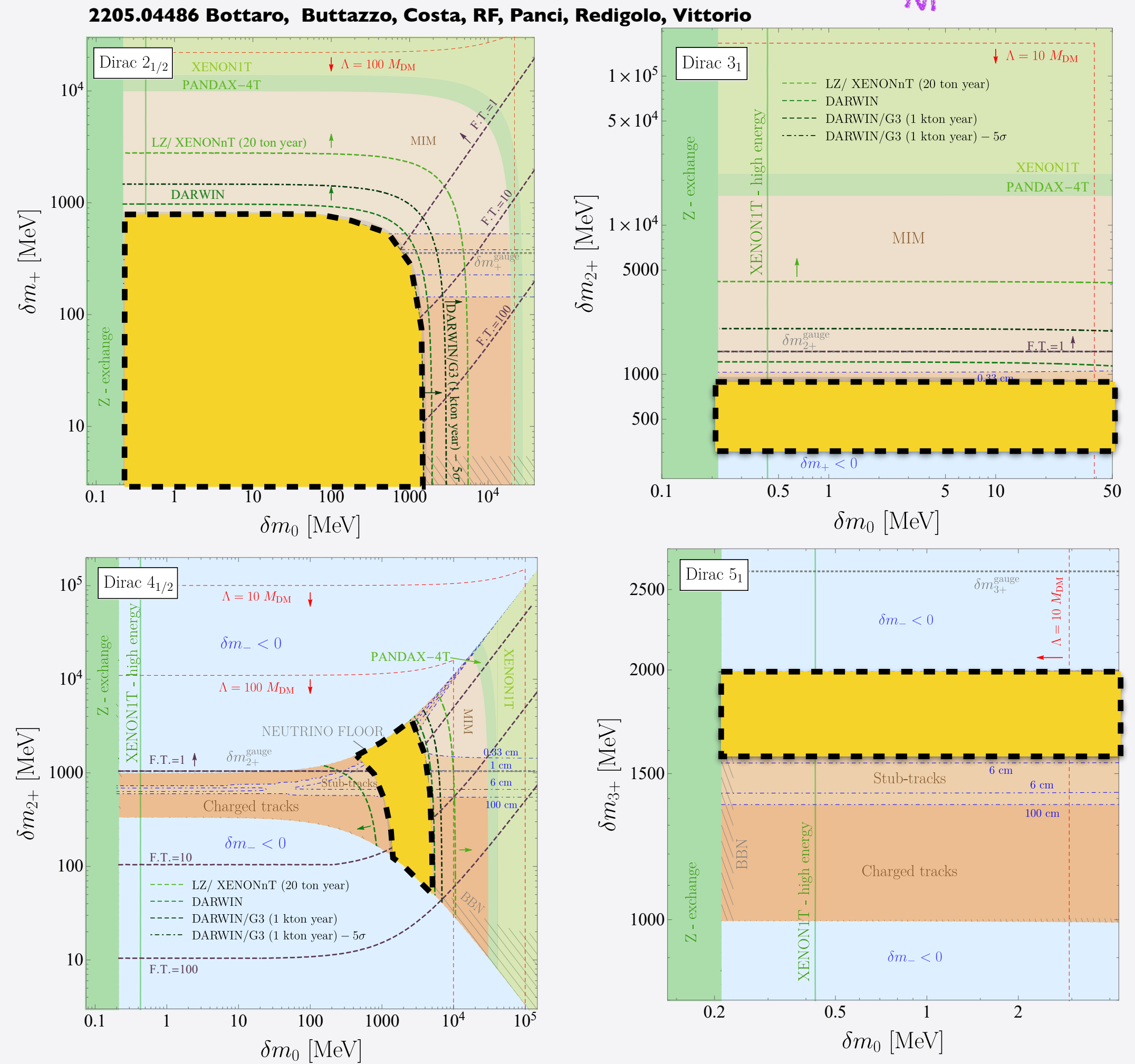
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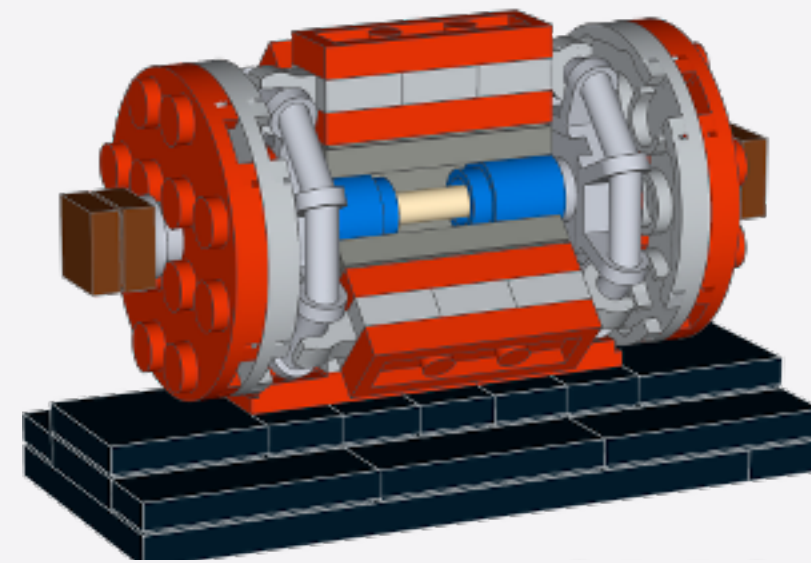
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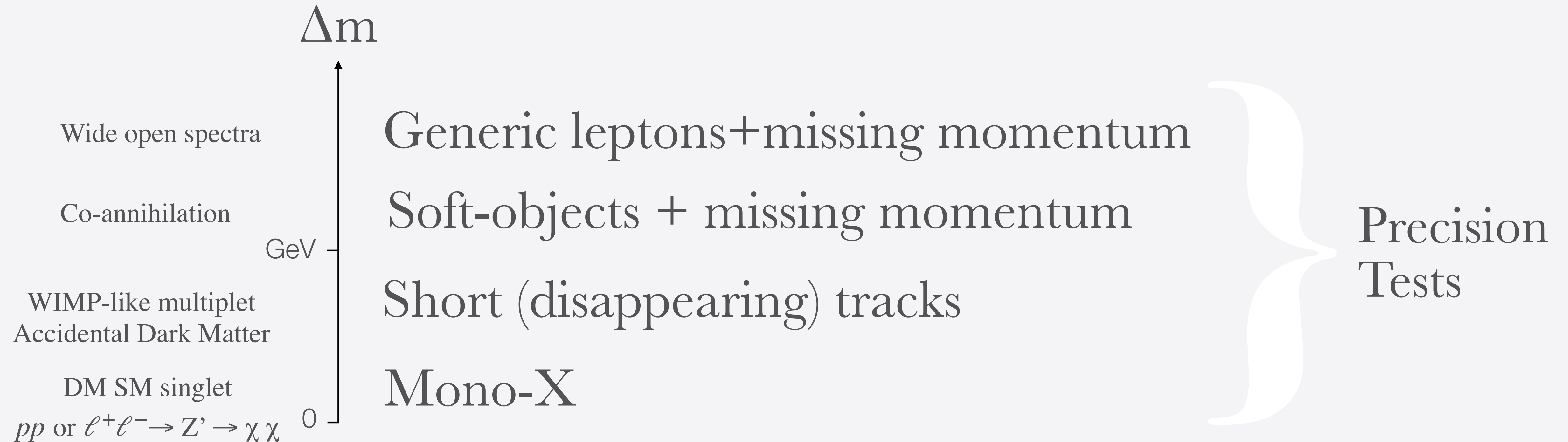
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DIRECT PRODUCTION AT COLLIDERS

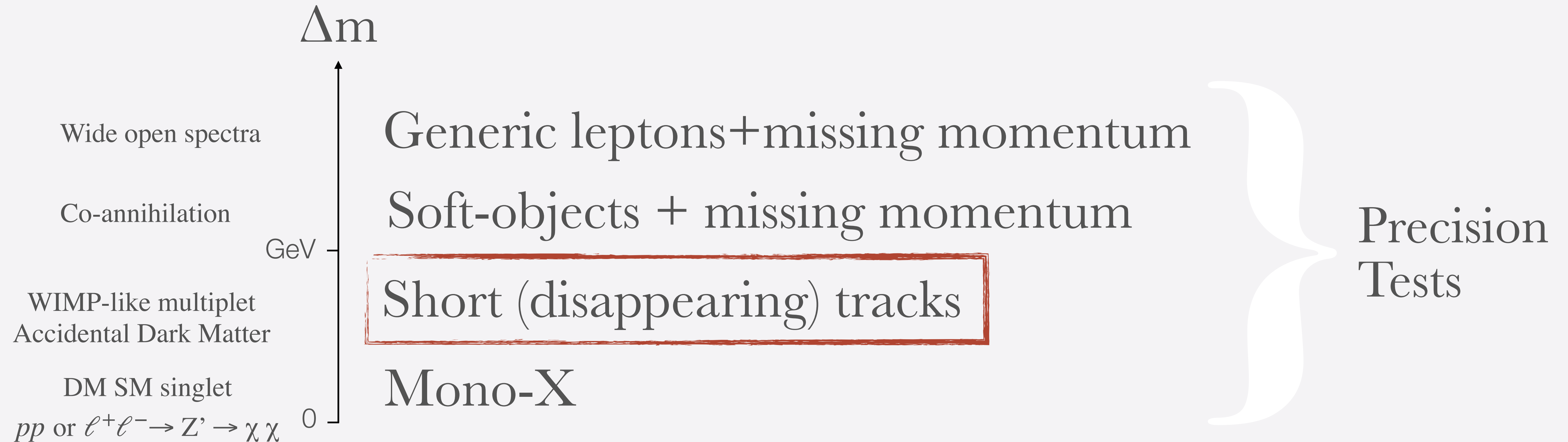


2040s

DIRECT SIGNALS AT COLLIDERS



DIRECT SIGNALS AT COLLIDERS



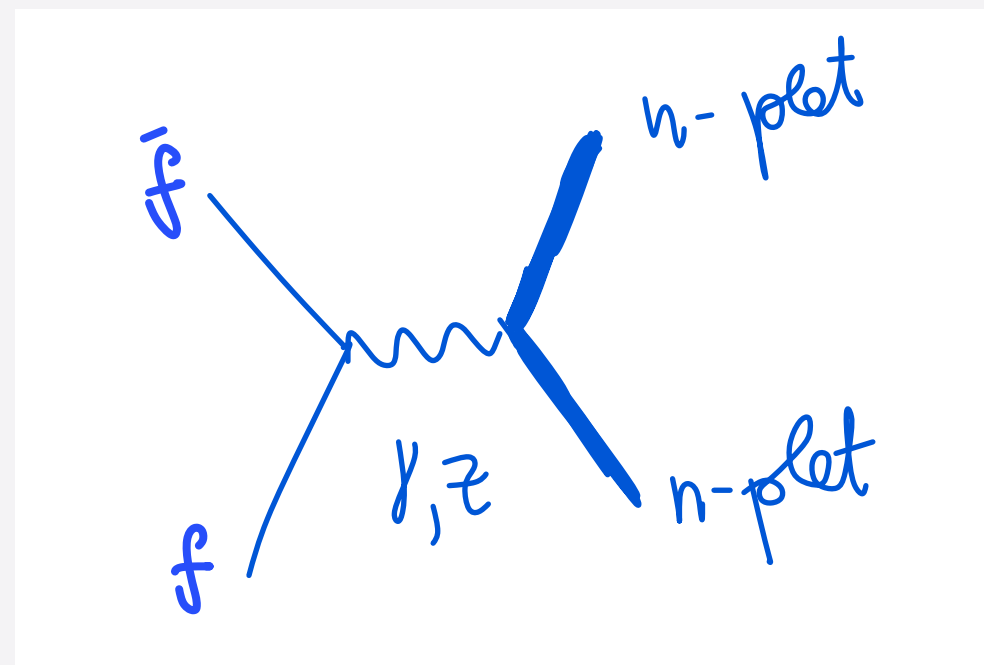
PURE \tilde{h} AND \tilde{W} DM

stub track and soft tracks

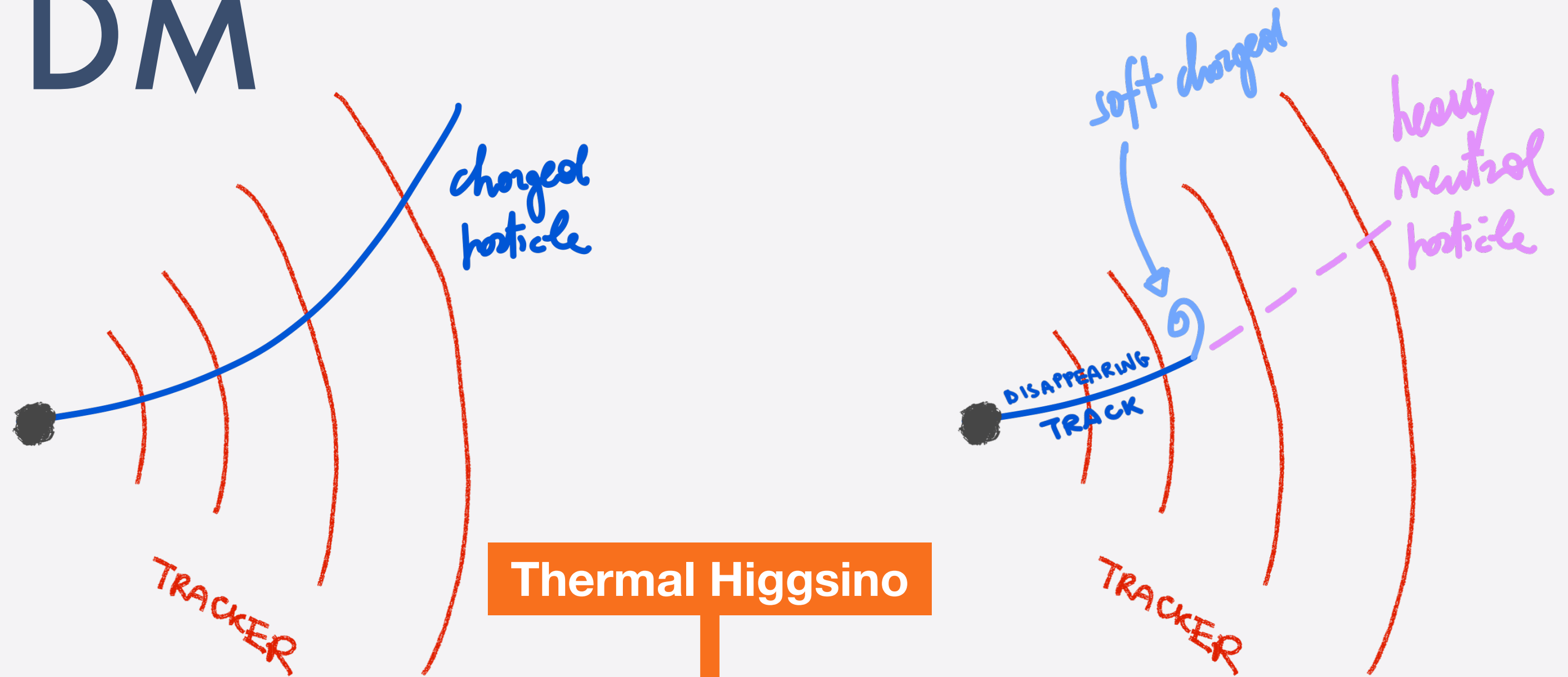
2040s

up to $\mu\mu$ 3-10 TeV

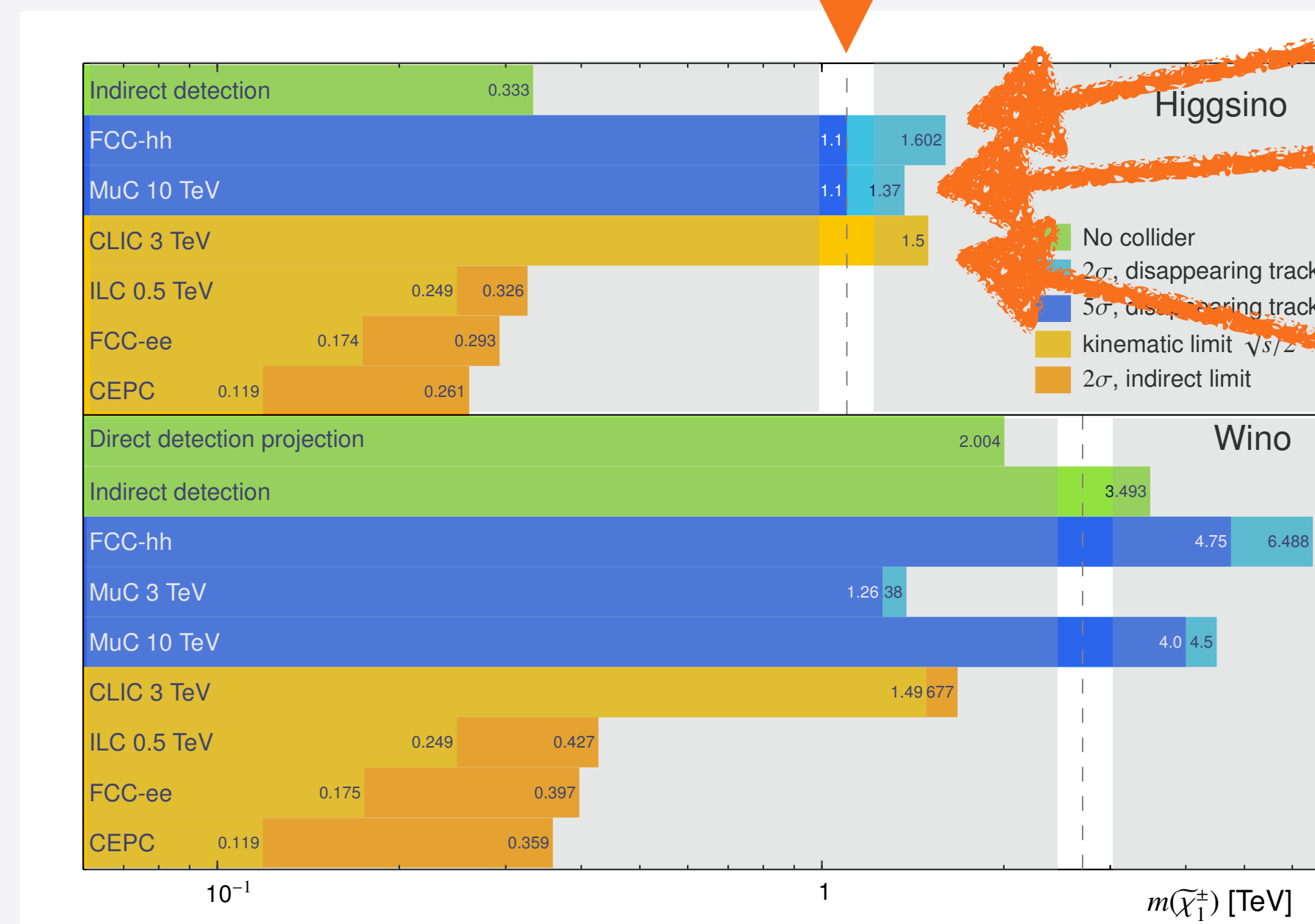
- Heavy n -plet of SU(2)
- Mass splitting $\sim \alpha_W m_W \sim 0.1\text{GeV} - 1\text{GeV}$



Large rates, but needs to light up the detector in a discernible way



Thermal Higgsino



pp 100 TeV 30 ab⁻¹
 $\mu^+\mu^-$ 10 TeV 10 ab⁻¹
 e^+e^- 3 TeV 5 ab⁻¹

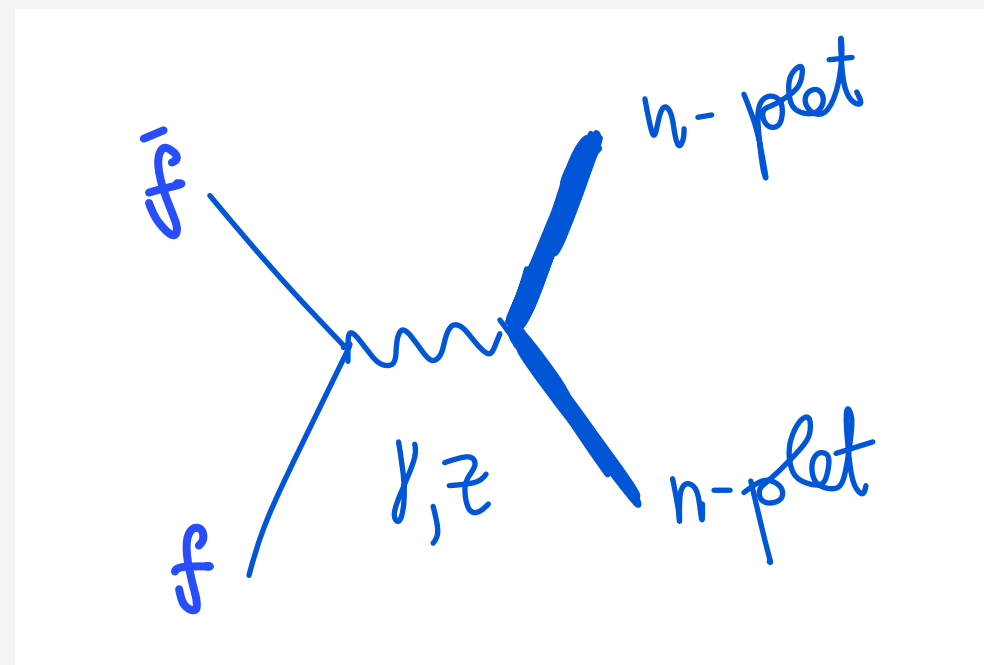
PURE \tilde{h} AND \tilde{W} DM

stub track and soft tracks

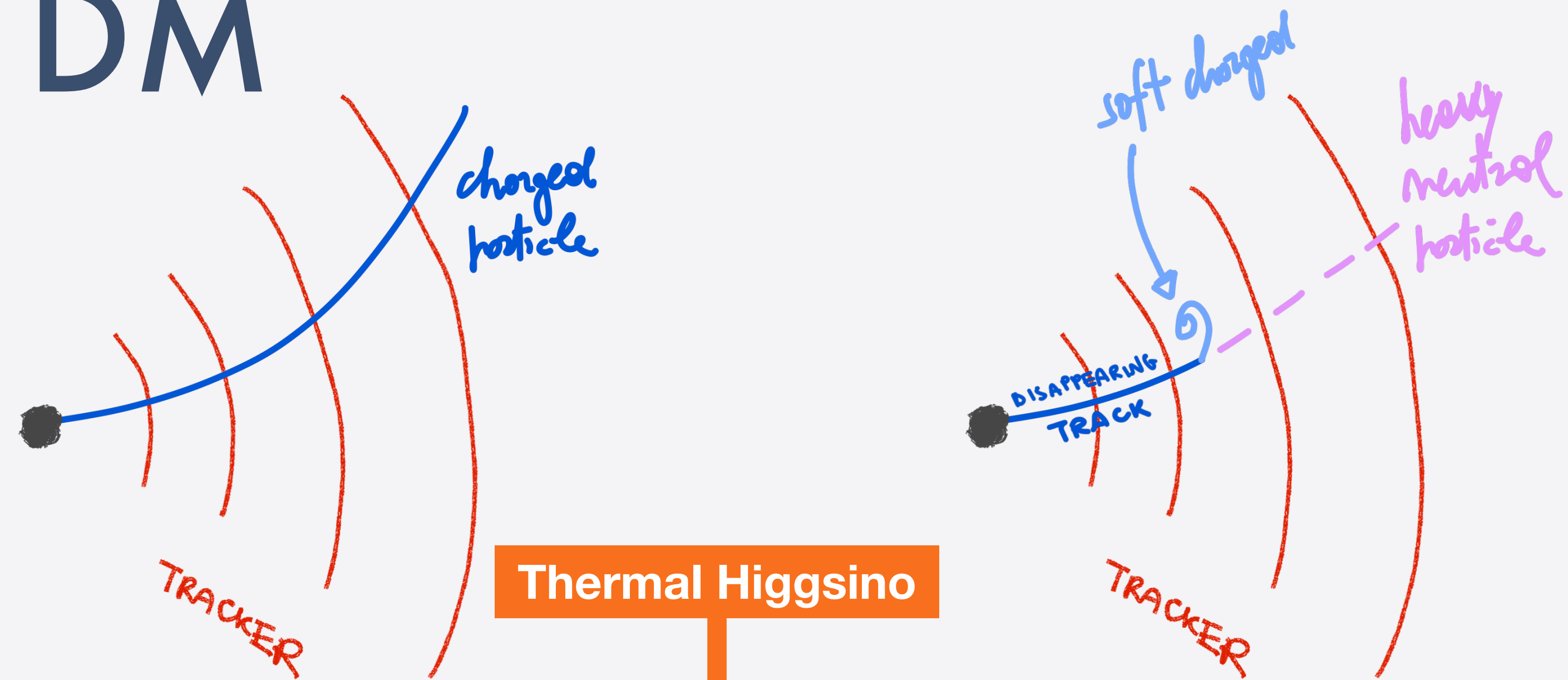
2040s

up to $\mu\mu$ 3-10 TeV

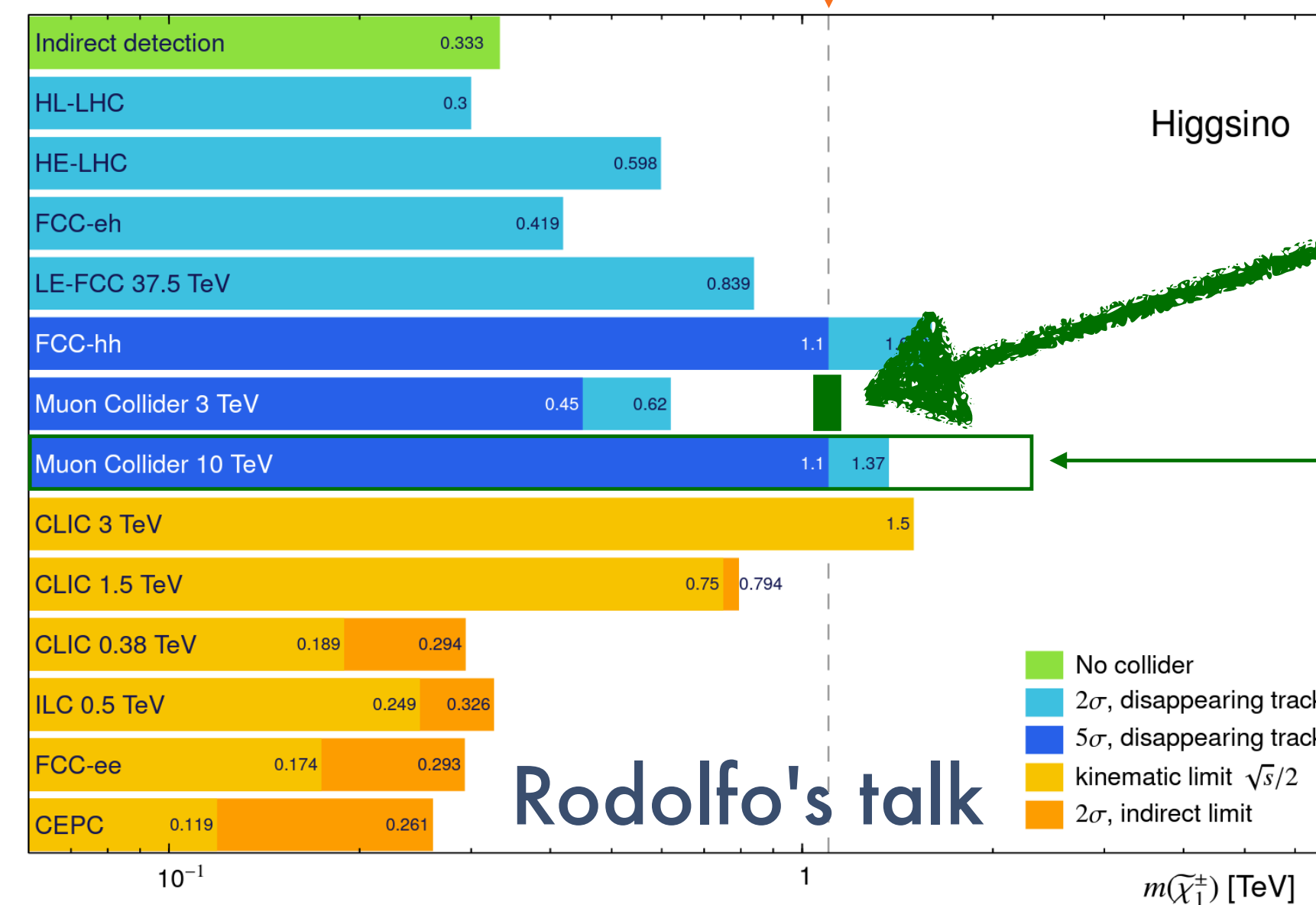
- Heavy n -plet of SU(2)
- Mass splitting $\sim \alpha_W m_W \sim 0.1\text{GeV} - 1\text{GeV}$



Large rates, but needs to light up the detector in a discernible way



Thermal Higgsino



$\mu^+\mu^-$ 3 TeV 1 ab⁻¹
The thermal target will be discovered!

Updated results from Federico Meloni's Disappearing Tracks

Rodolfo's talk

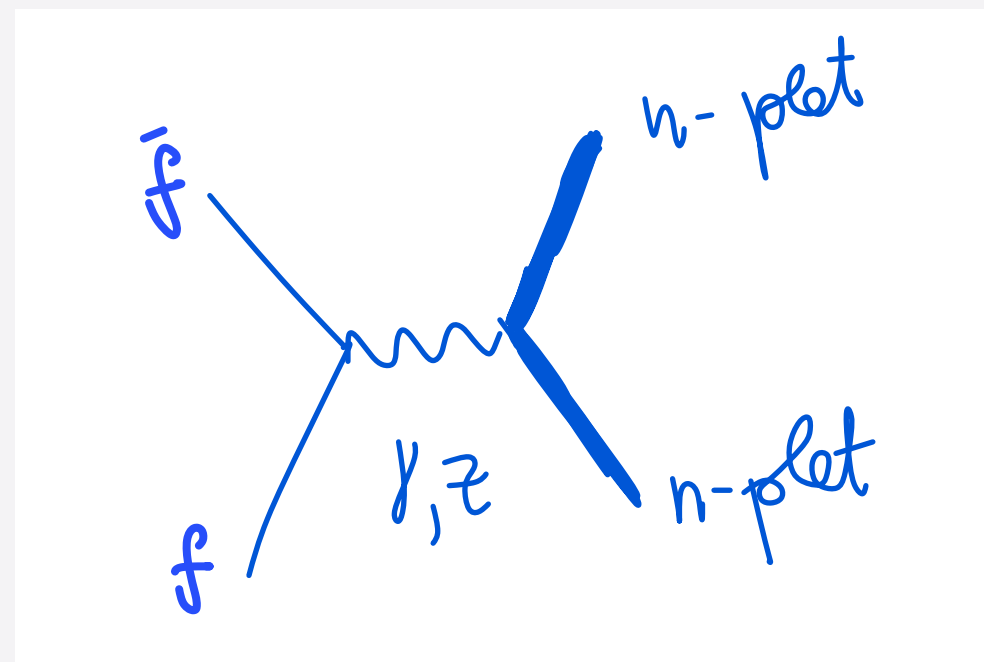
PURE \tilde{h} AND \tilde{W} DM

stub track and soft tracks

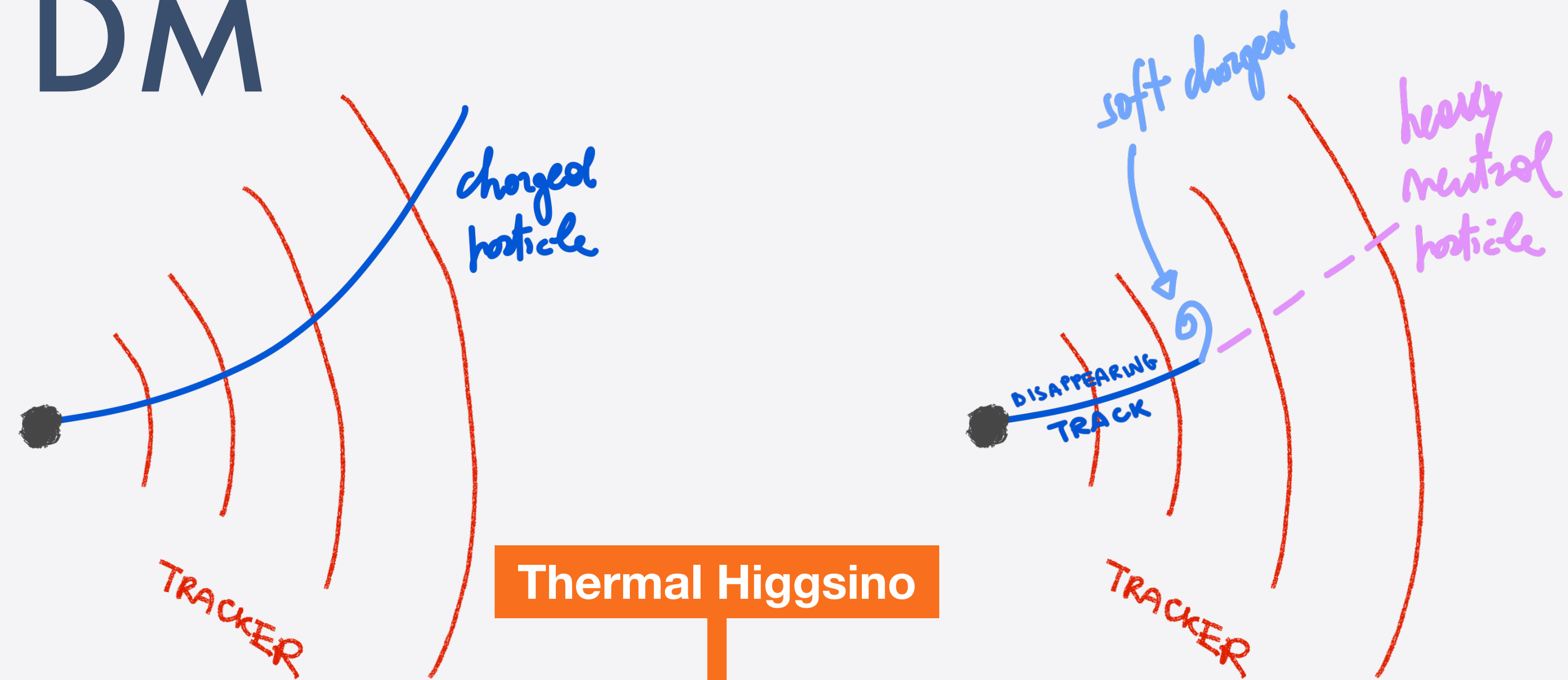
2040s

up to $\mu\mu$ 3-10 TeV

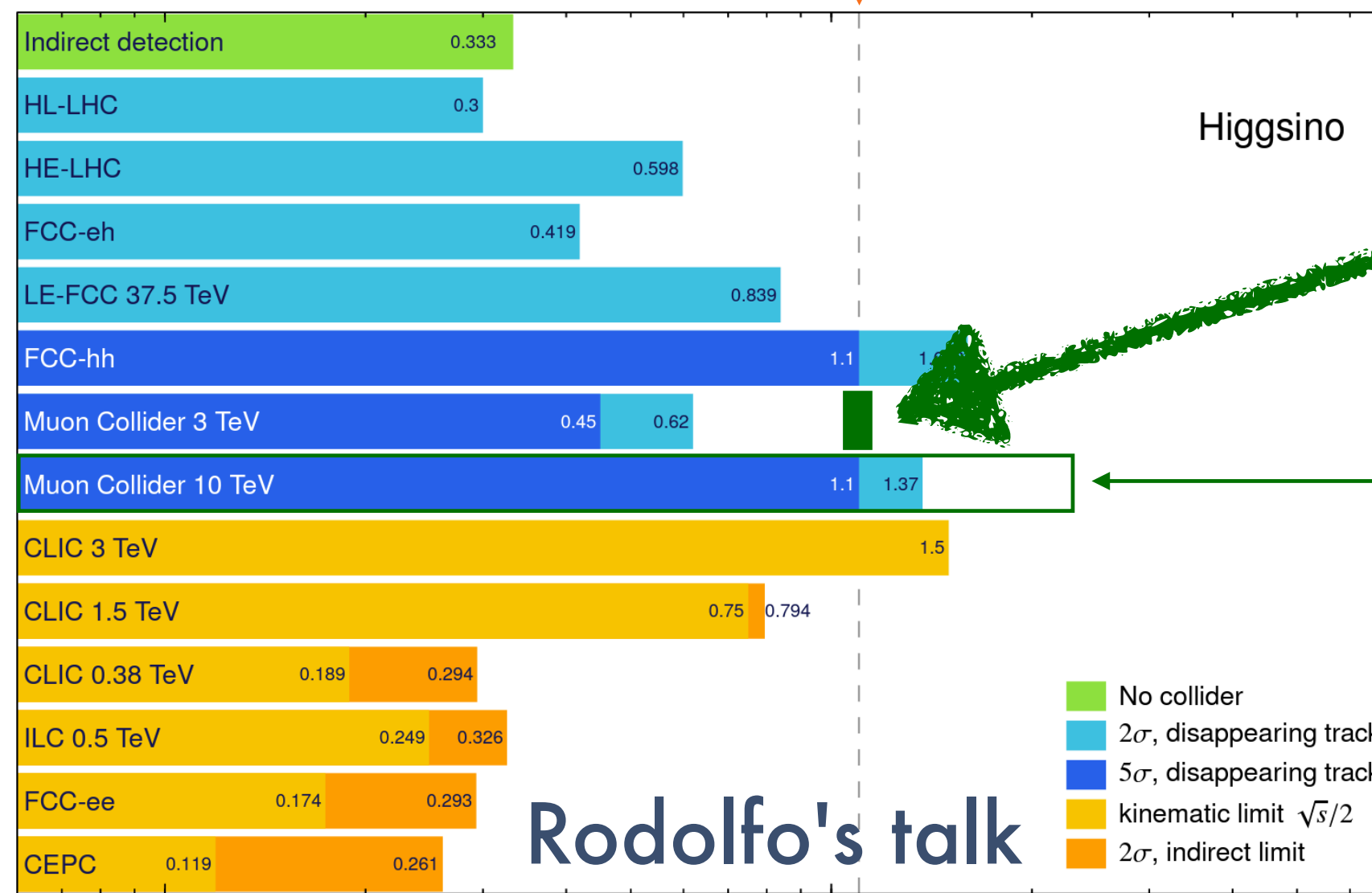
- Heavy n -plet of SU(2)
- Mass splitting $\sim \alpha_W m_W \sim 0.1\text{GeV} - 1\text{GeV}$



Large rates, but needs to light up the detector in a discernible way



Thermal Higgsino



$\mu^+\mu^-$ 3 TeV 1 ab⁻¹
The thermal target will be discovered!

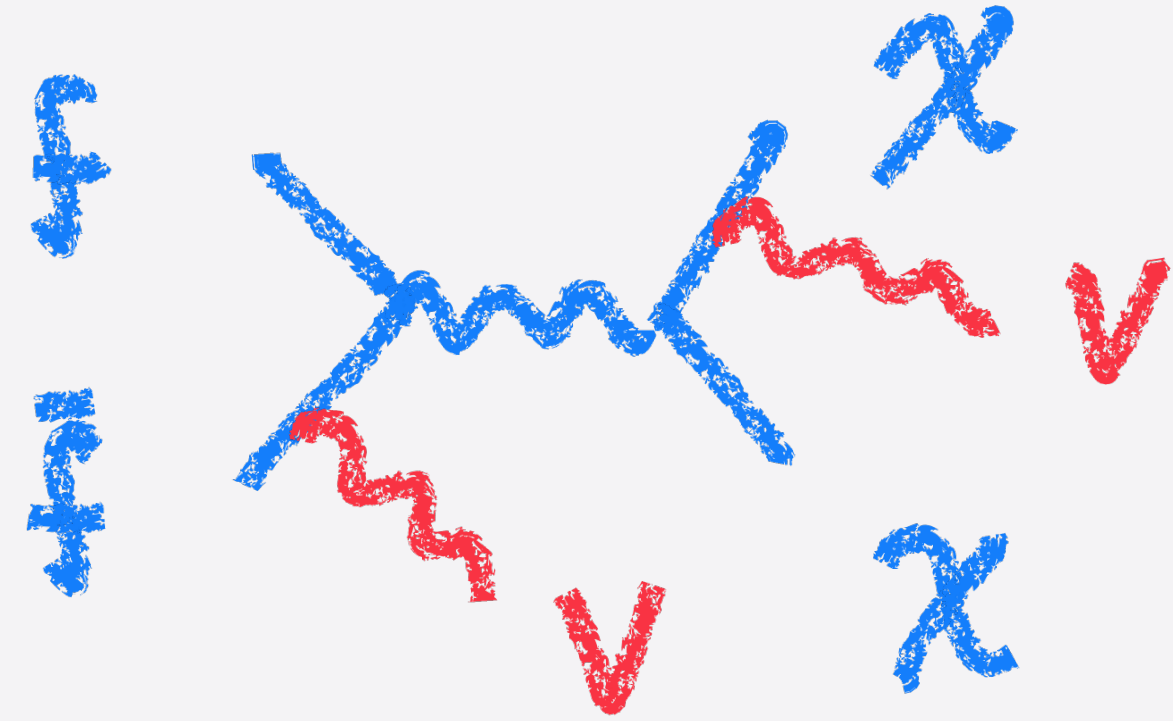
Updated results from Federico Meloni's Disappearing Tracks

Rodolfo's talk

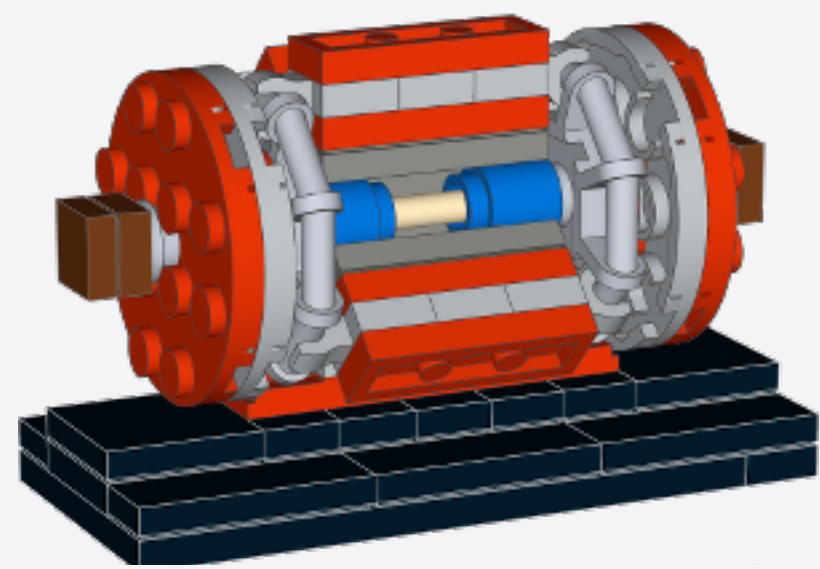
$m(\tilde{\chi}_1^\pm)$ [TeV]

PURE \tilde{h} AND \tilde{W} DM

stub tracks



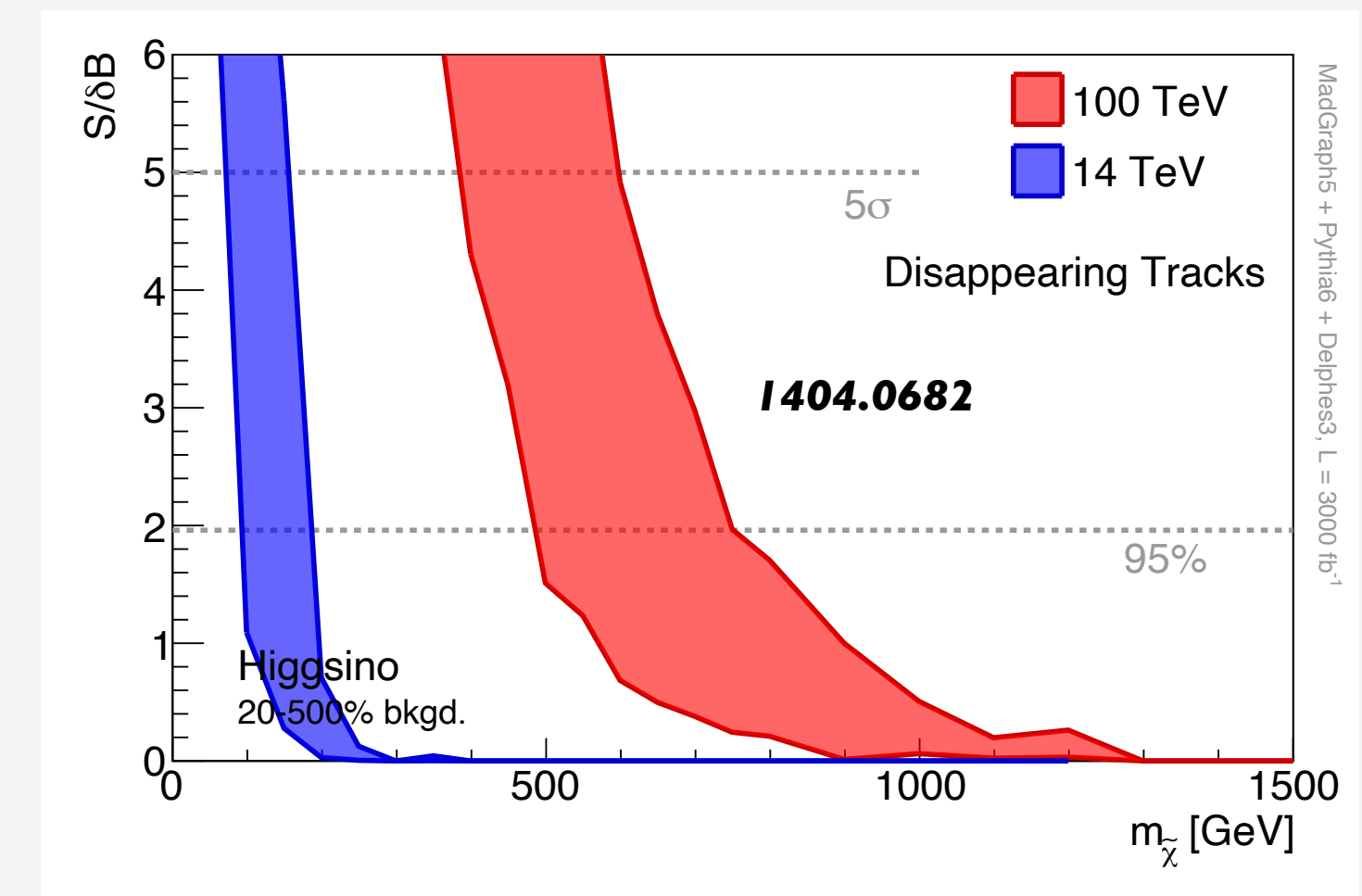
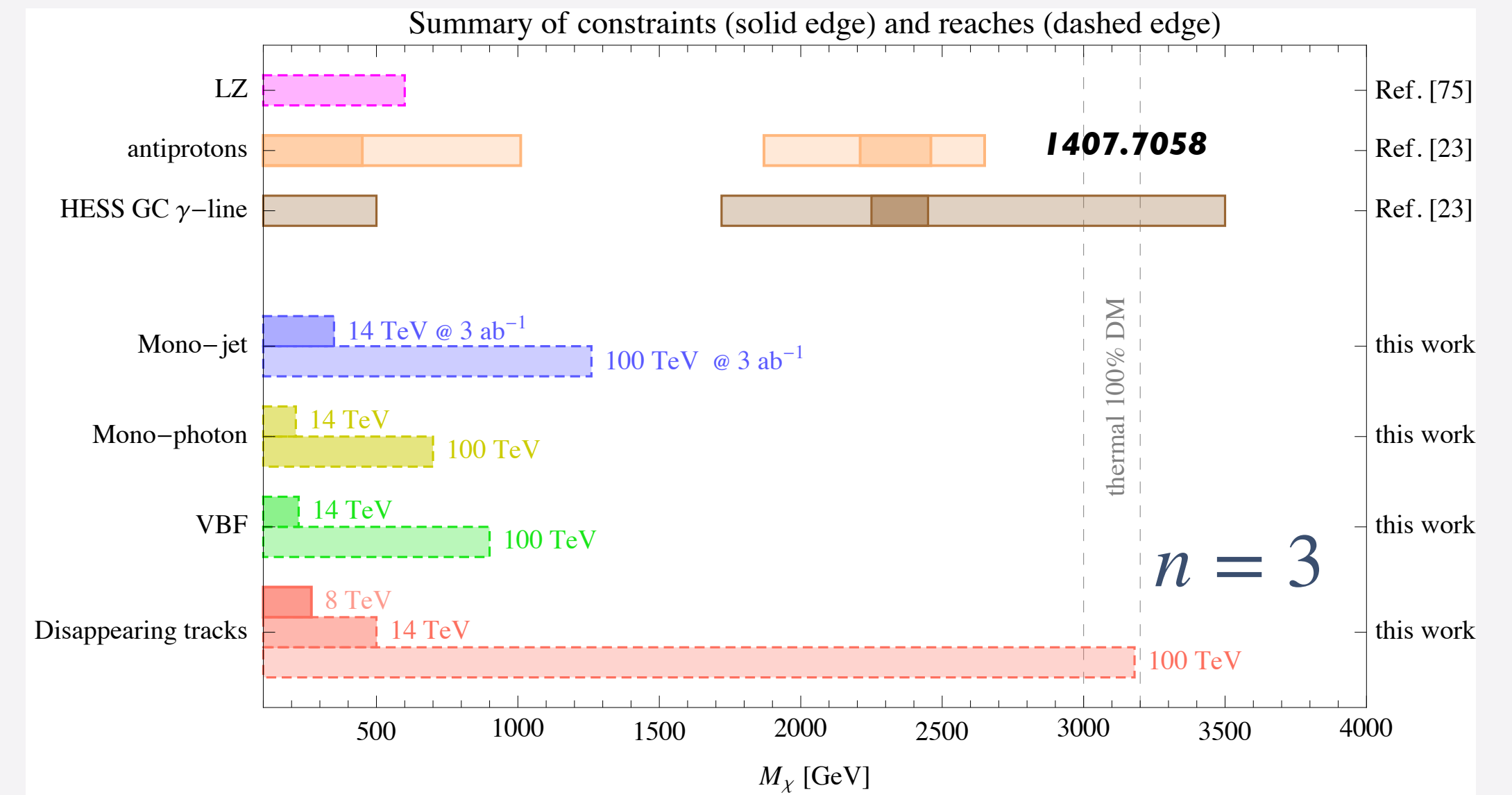
Production of Dark Matter weak multiplet states and observation of the decay products or associated productions



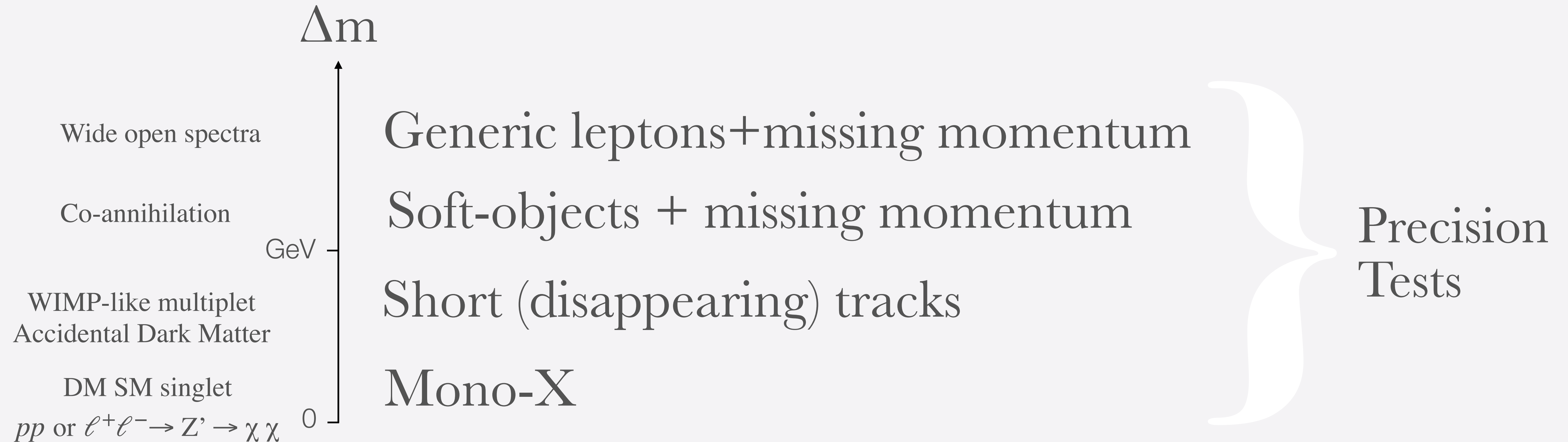
2060s

up to pp 100 TeV

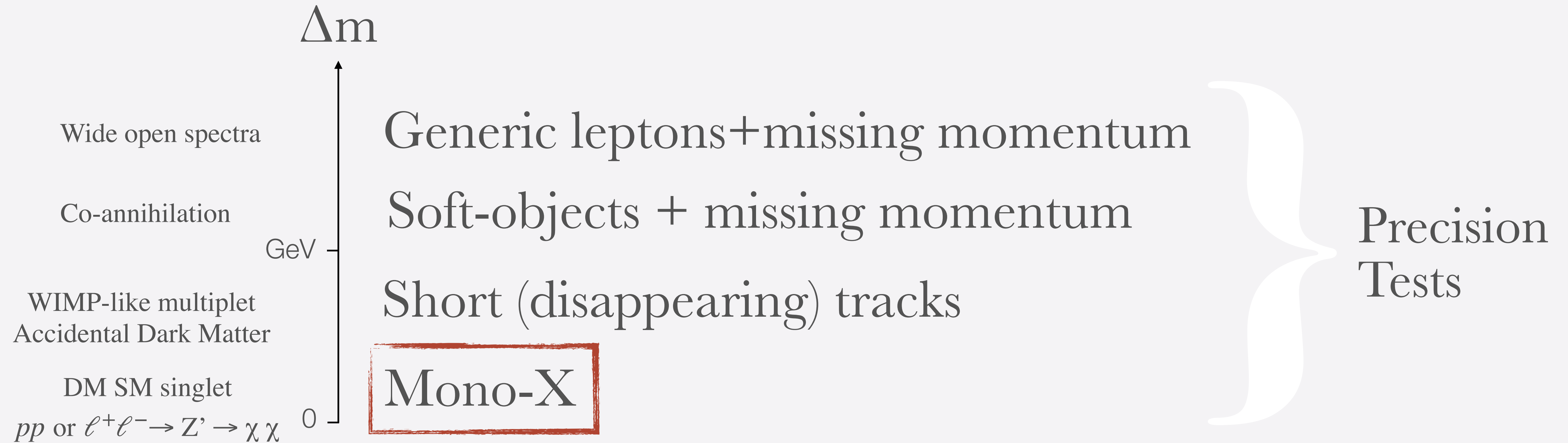
$n = 2$ and $n = 3$ just inside reach of 100 TeV pp collider



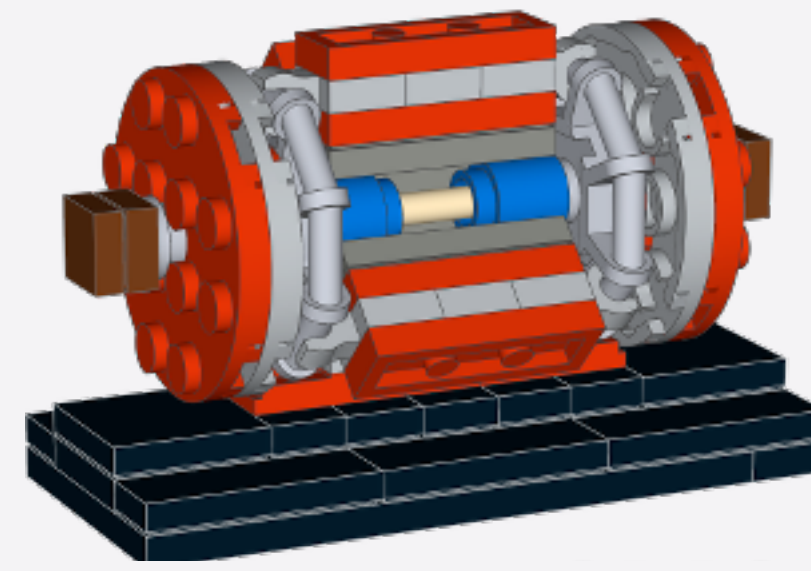
DIRECT SIGNALS AT COLLIDERS



DIRECT SIGNALS AT COLLIDERS



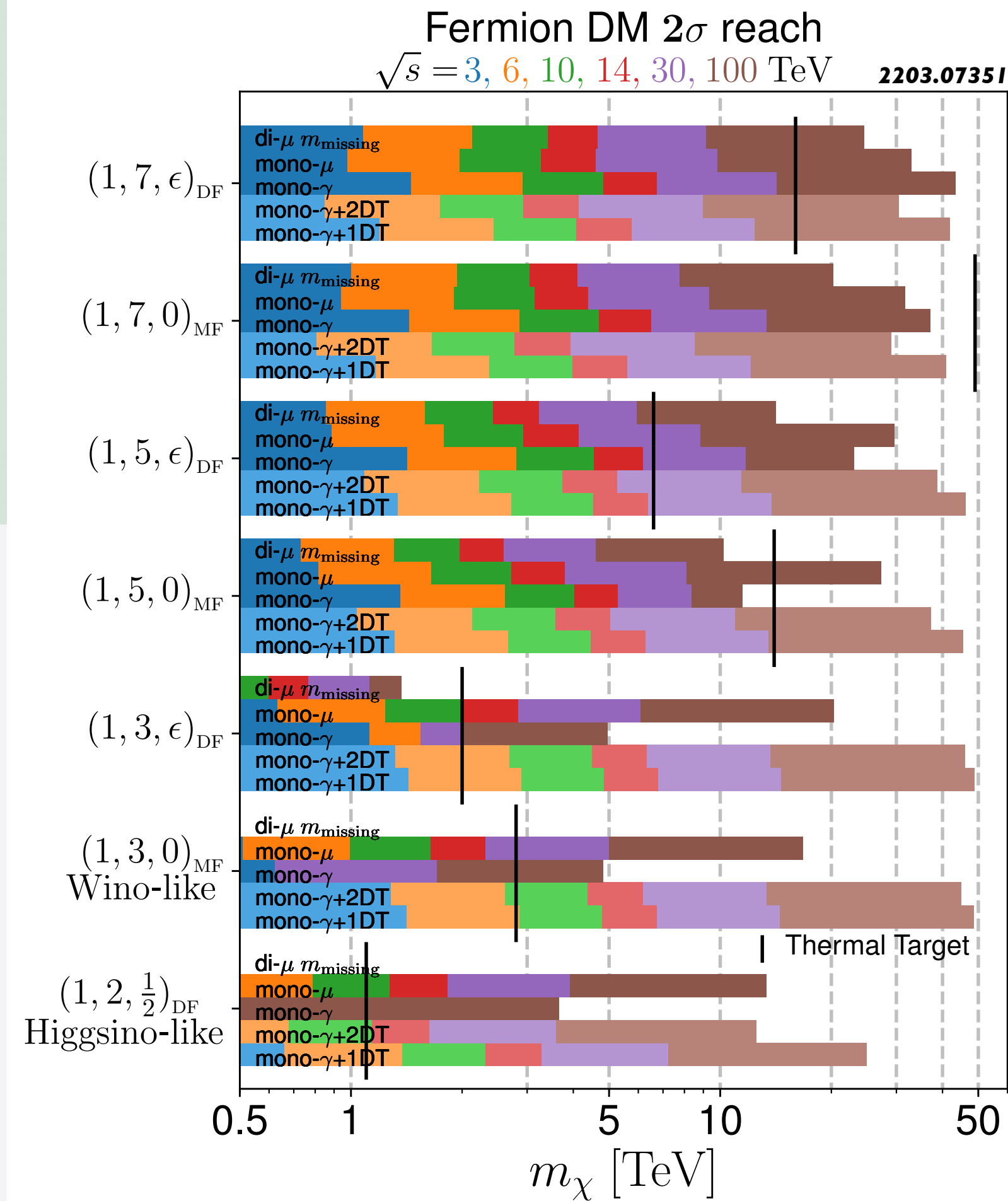
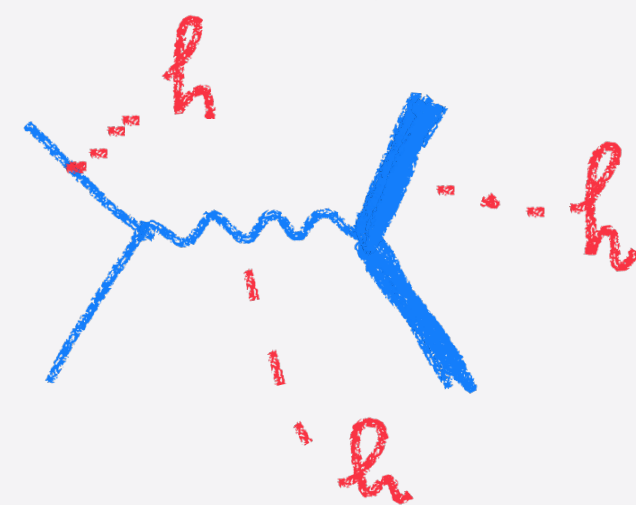
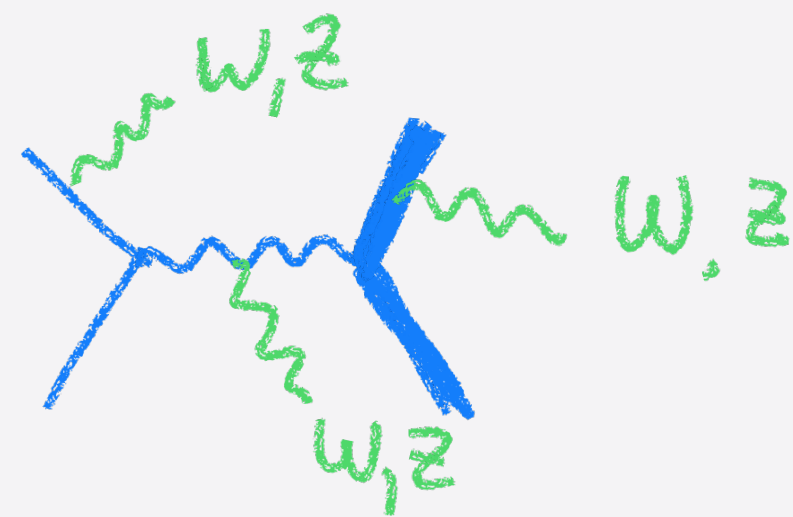
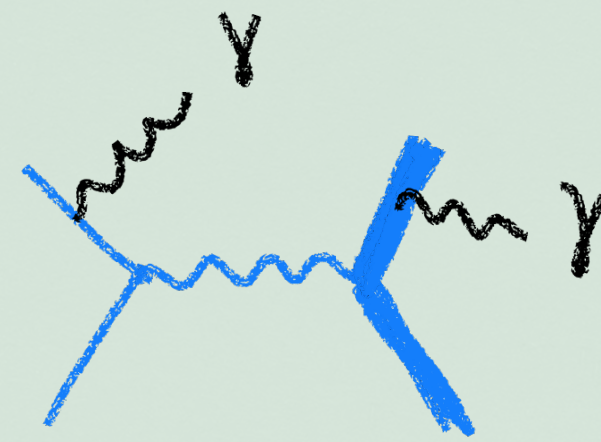
MONO-X



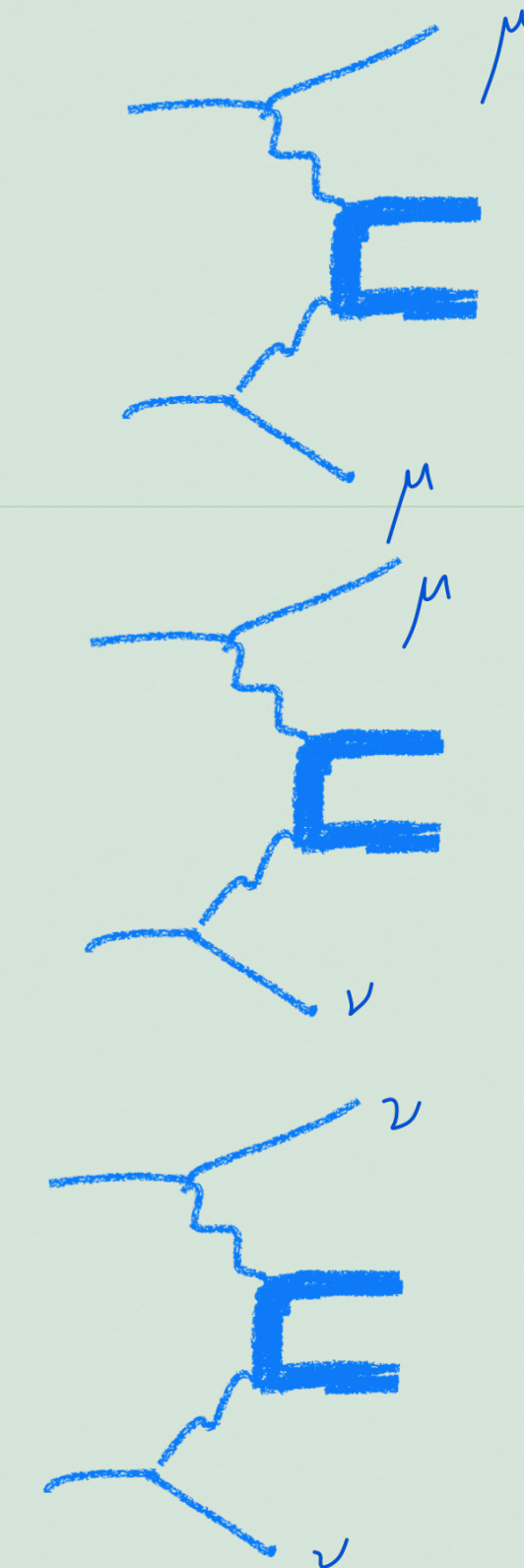
2040s

up to 10+ TeV

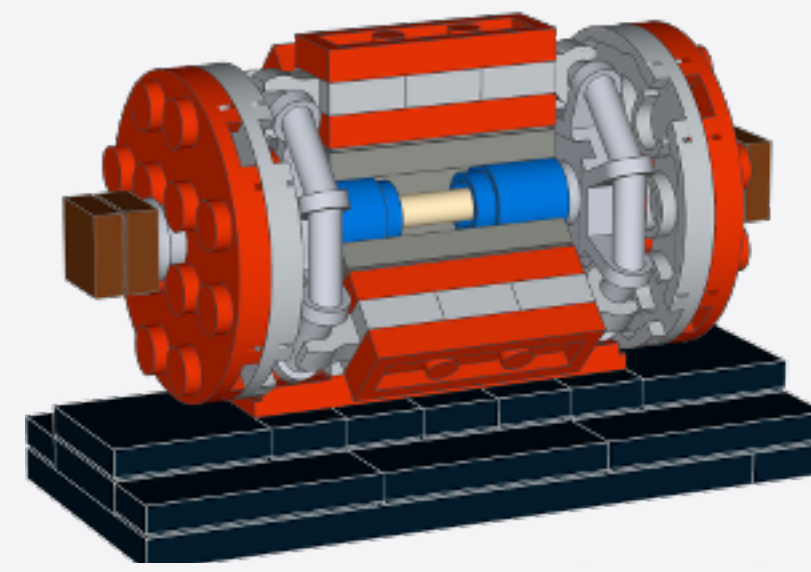
Sensitive up to mass comparable to the center of mass of $\mu^+\mu^-$



Excellent for low mass compared to the center of mass of $\mu^+\mu^-$



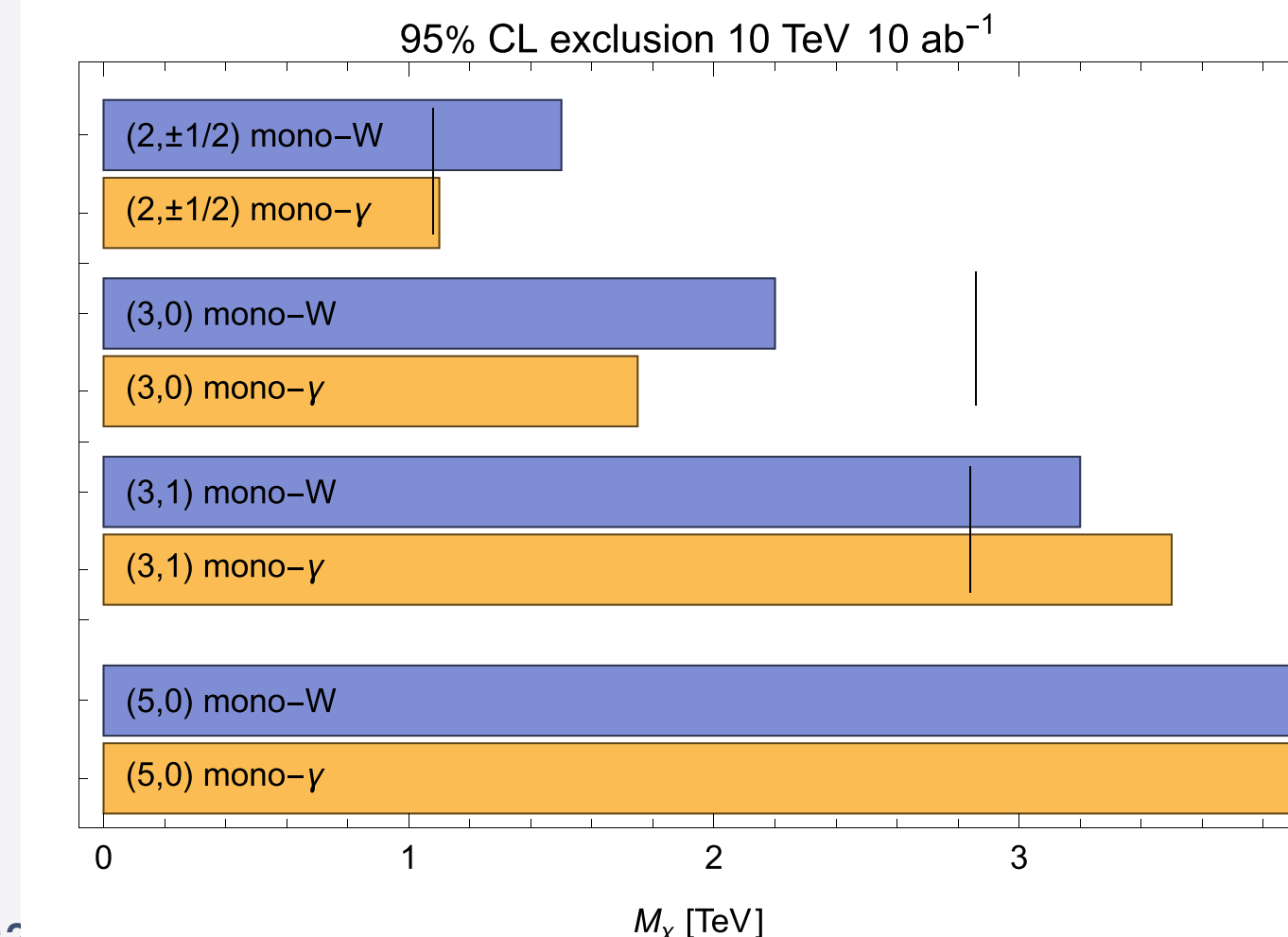
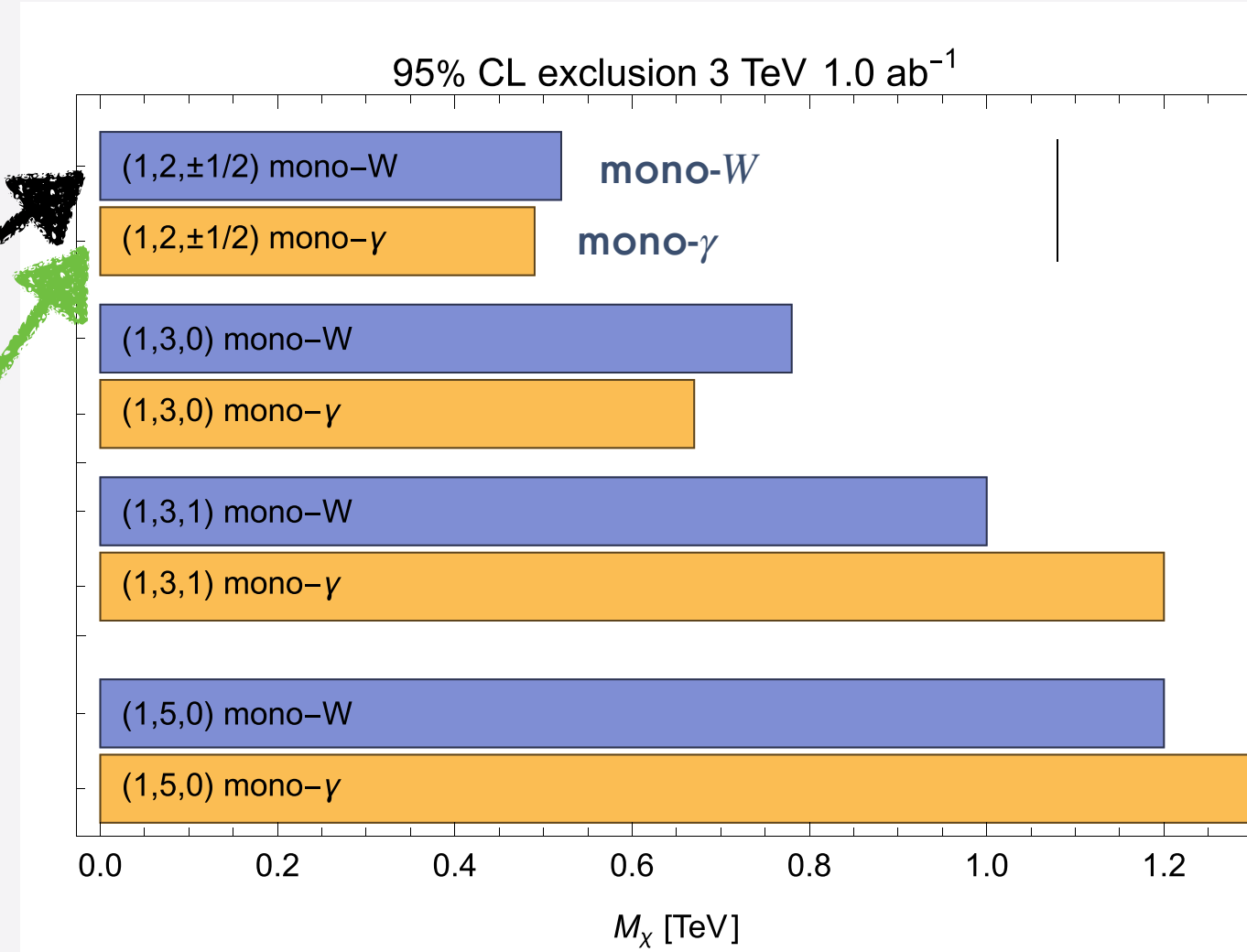
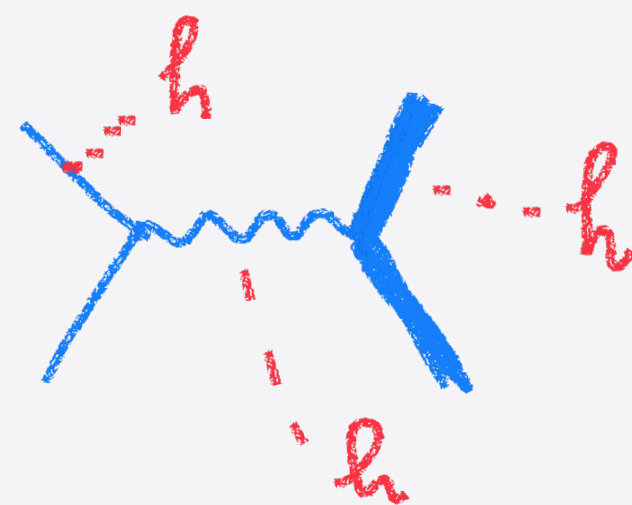
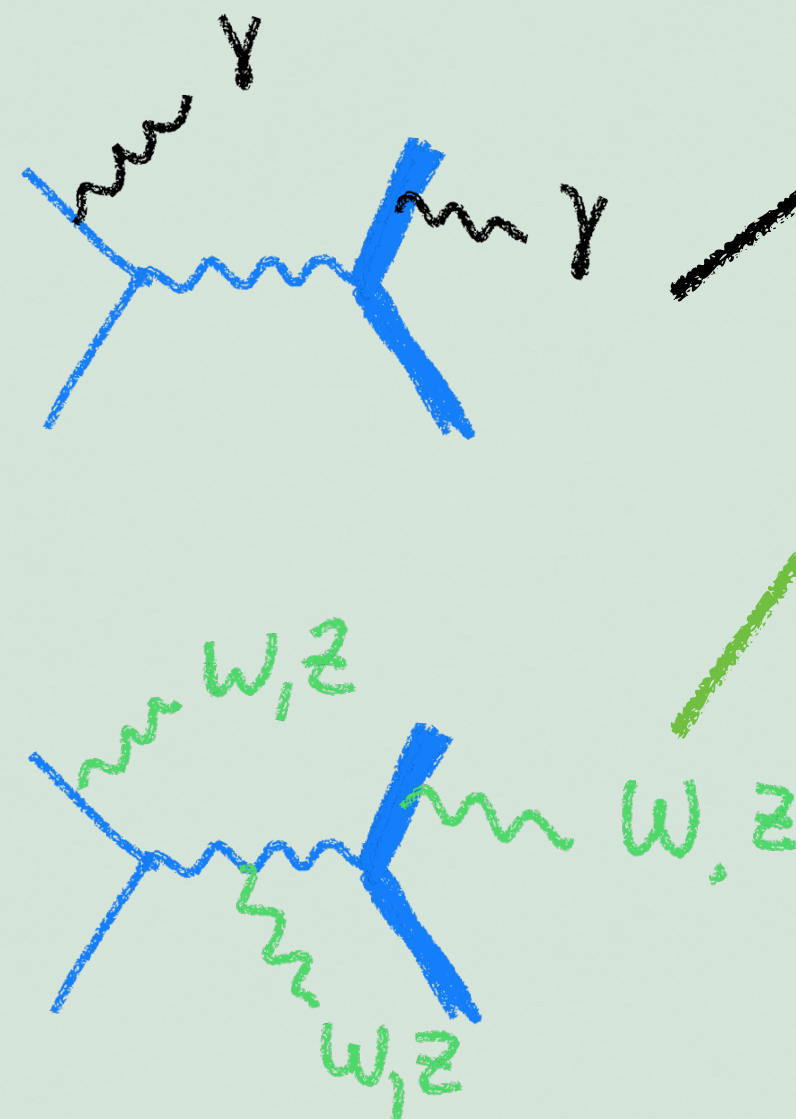
MONO-X



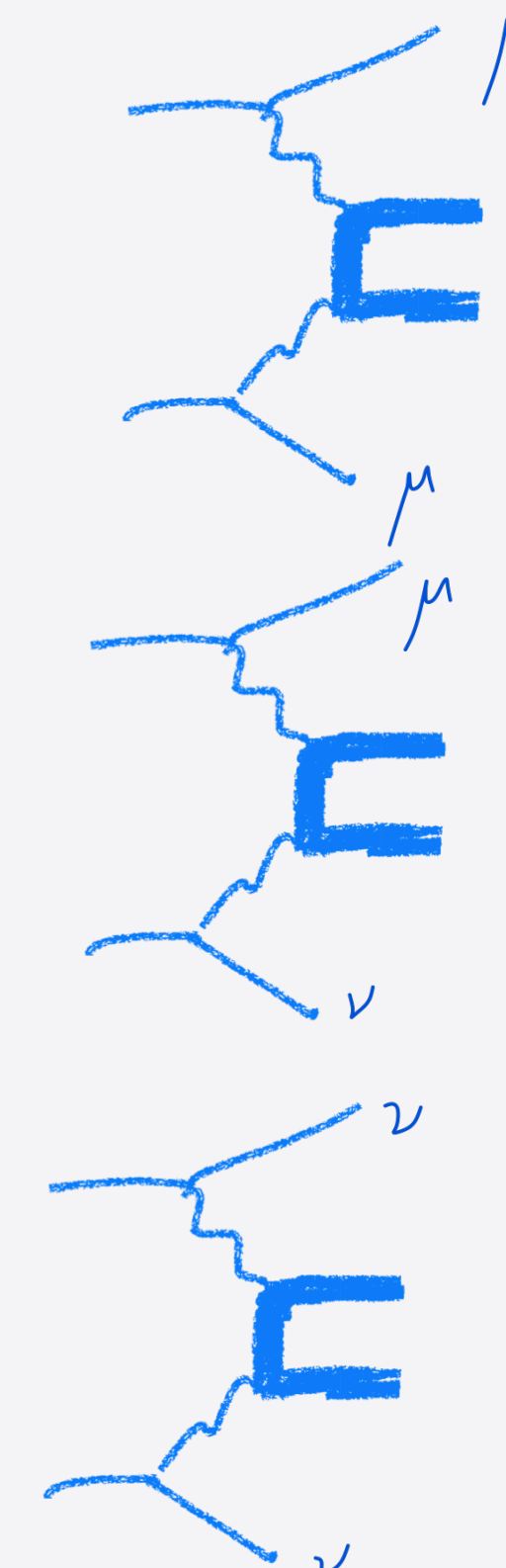
2040s

up to 10+ TeV

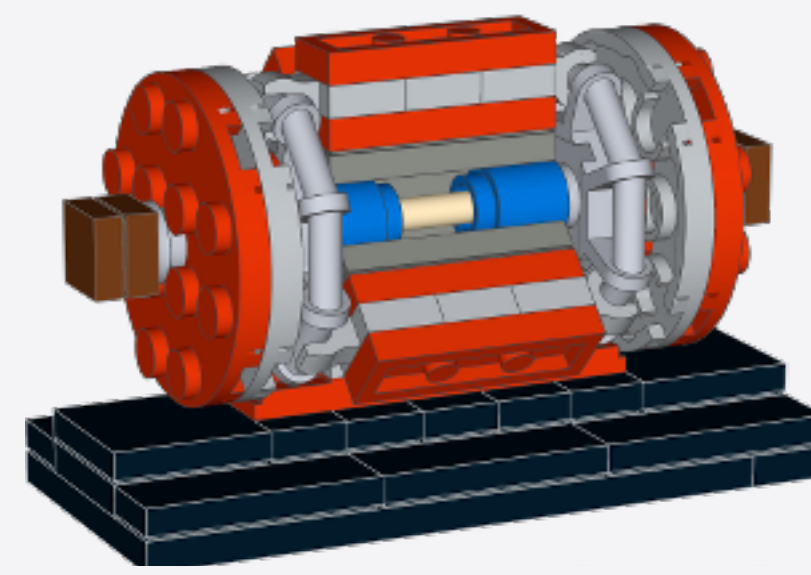
Sensitive up to mass comparable to the center of mass of $\mu^+\mu^-$



Excellent for low mass compared to the center of mass of $\mu^+\mu^-$



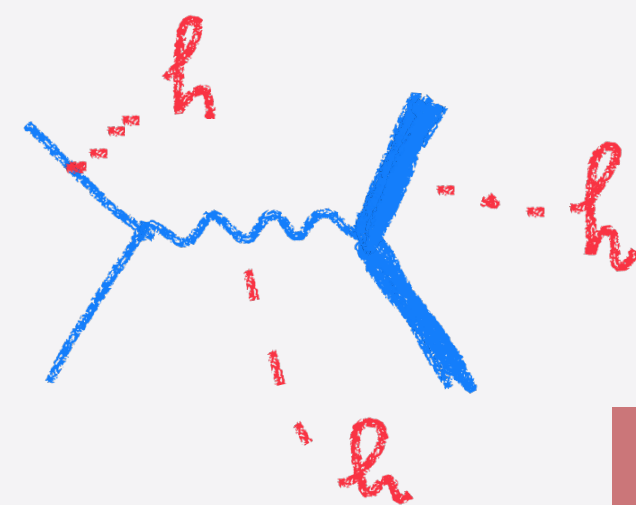
MONO-X



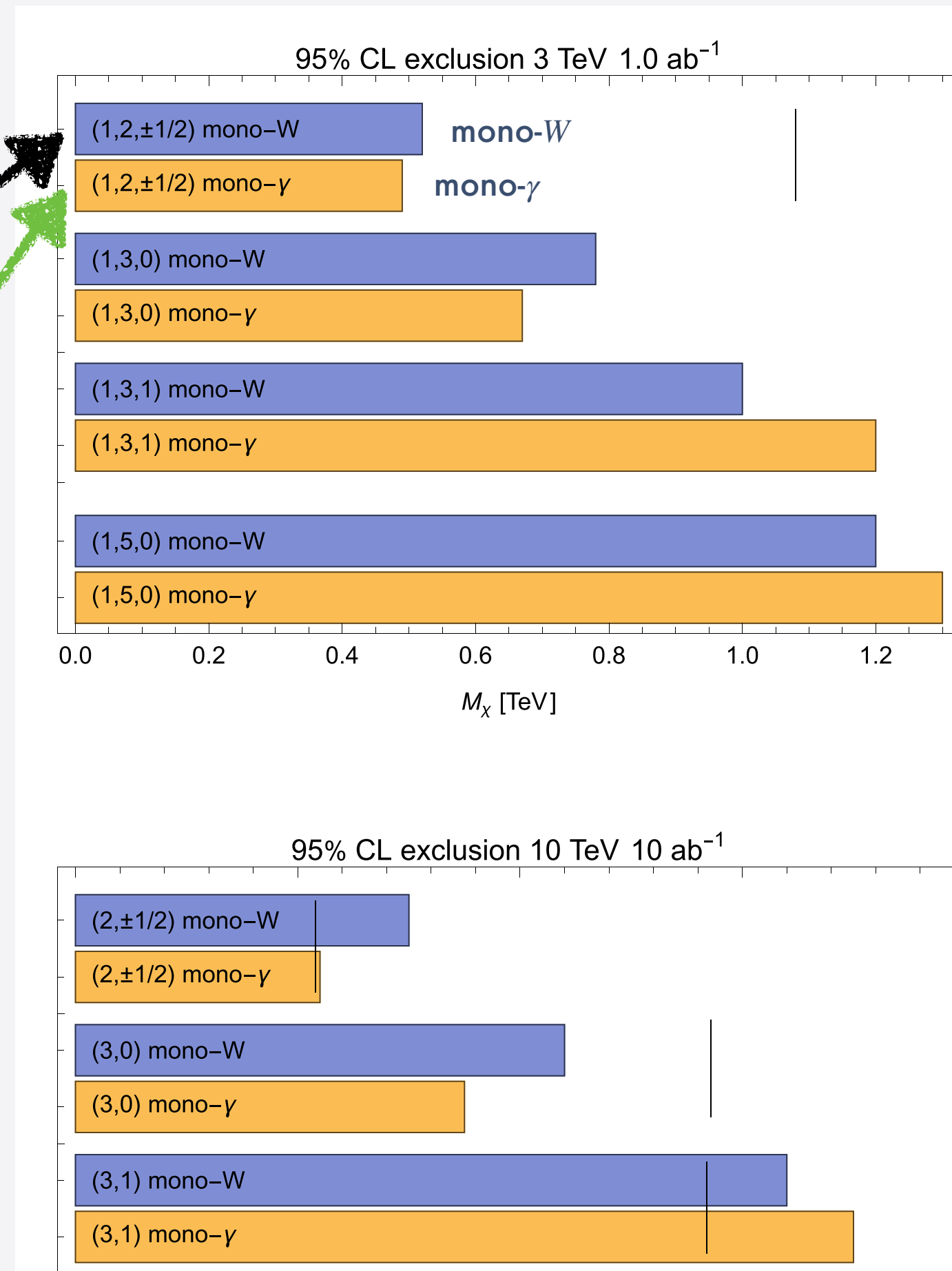
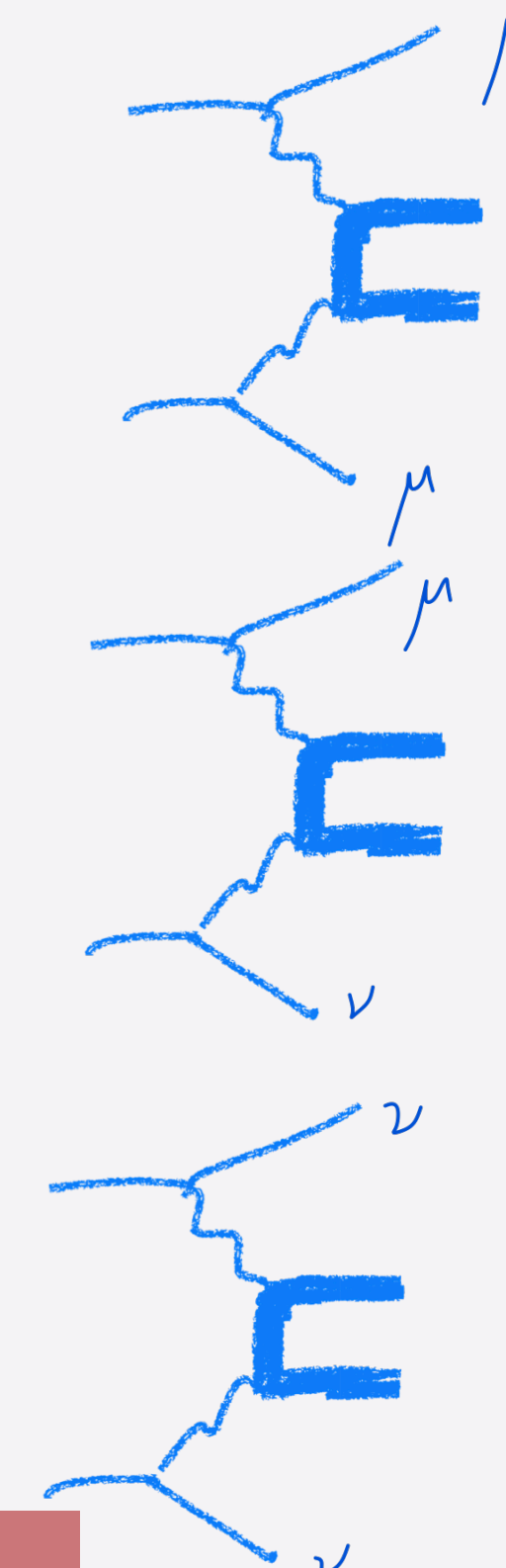
2040s

up to 10+ TeV

Sensitive up to mass comparable to the center of mass of $\mu^+\mu^-$

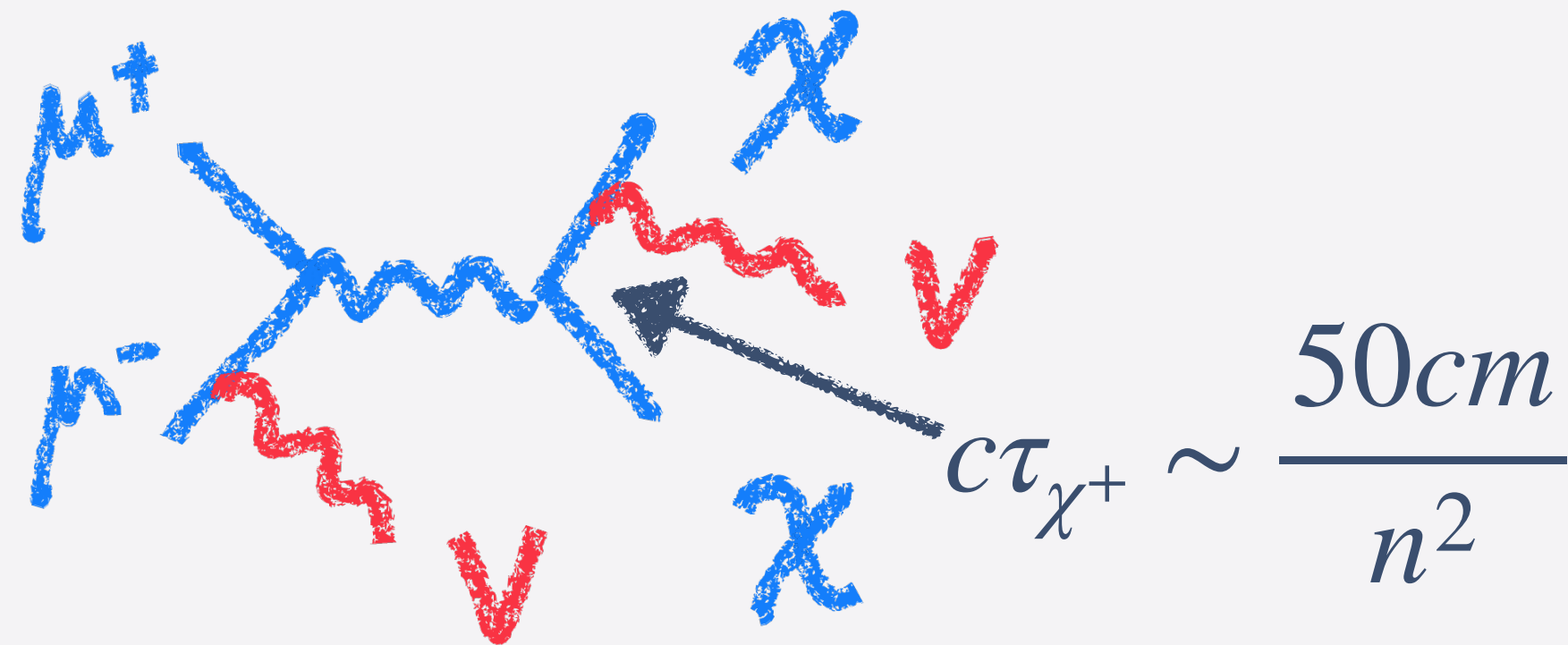


Excellent for low mass compared to the center of mass of $\mu^+\mu^-$

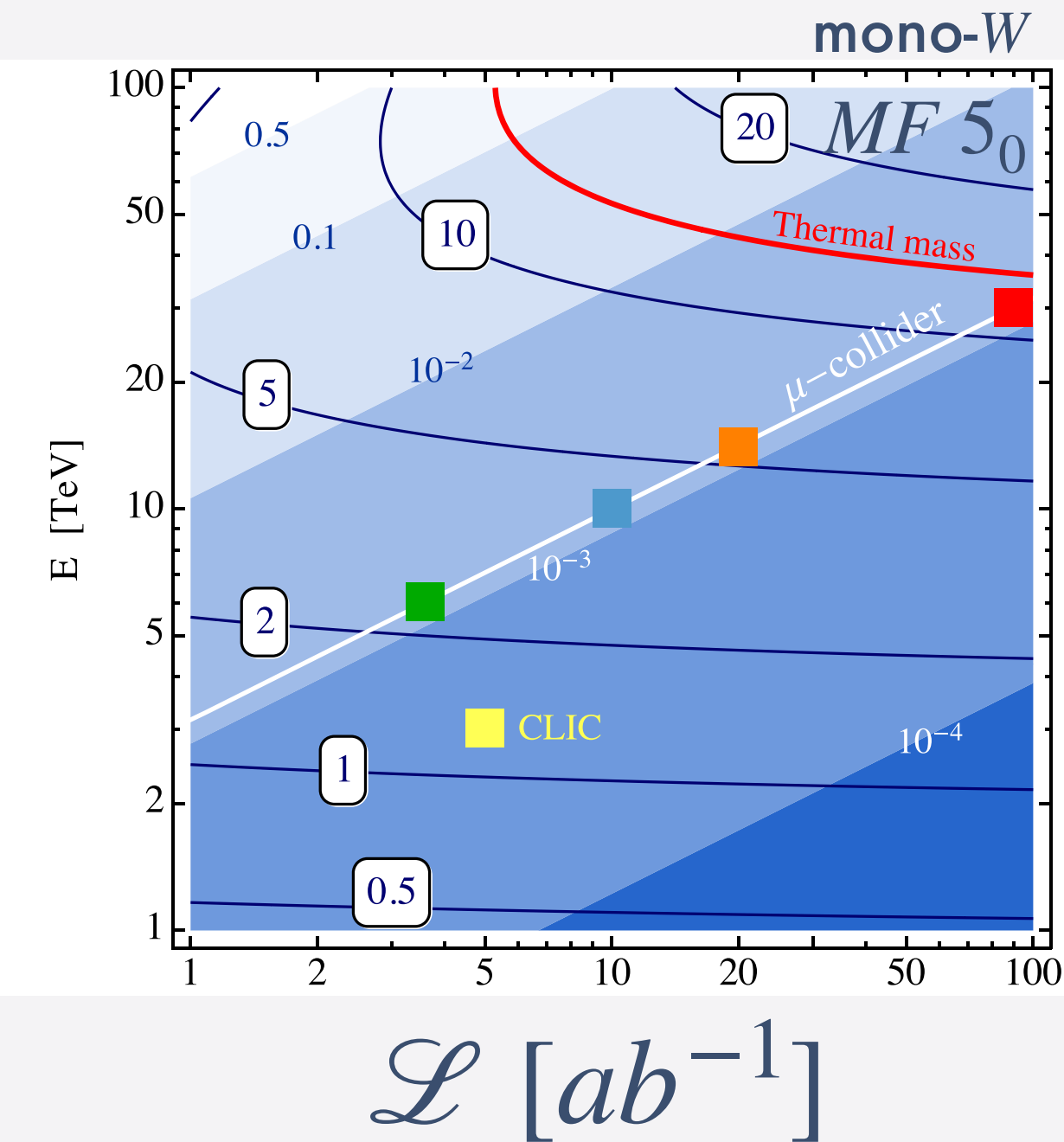
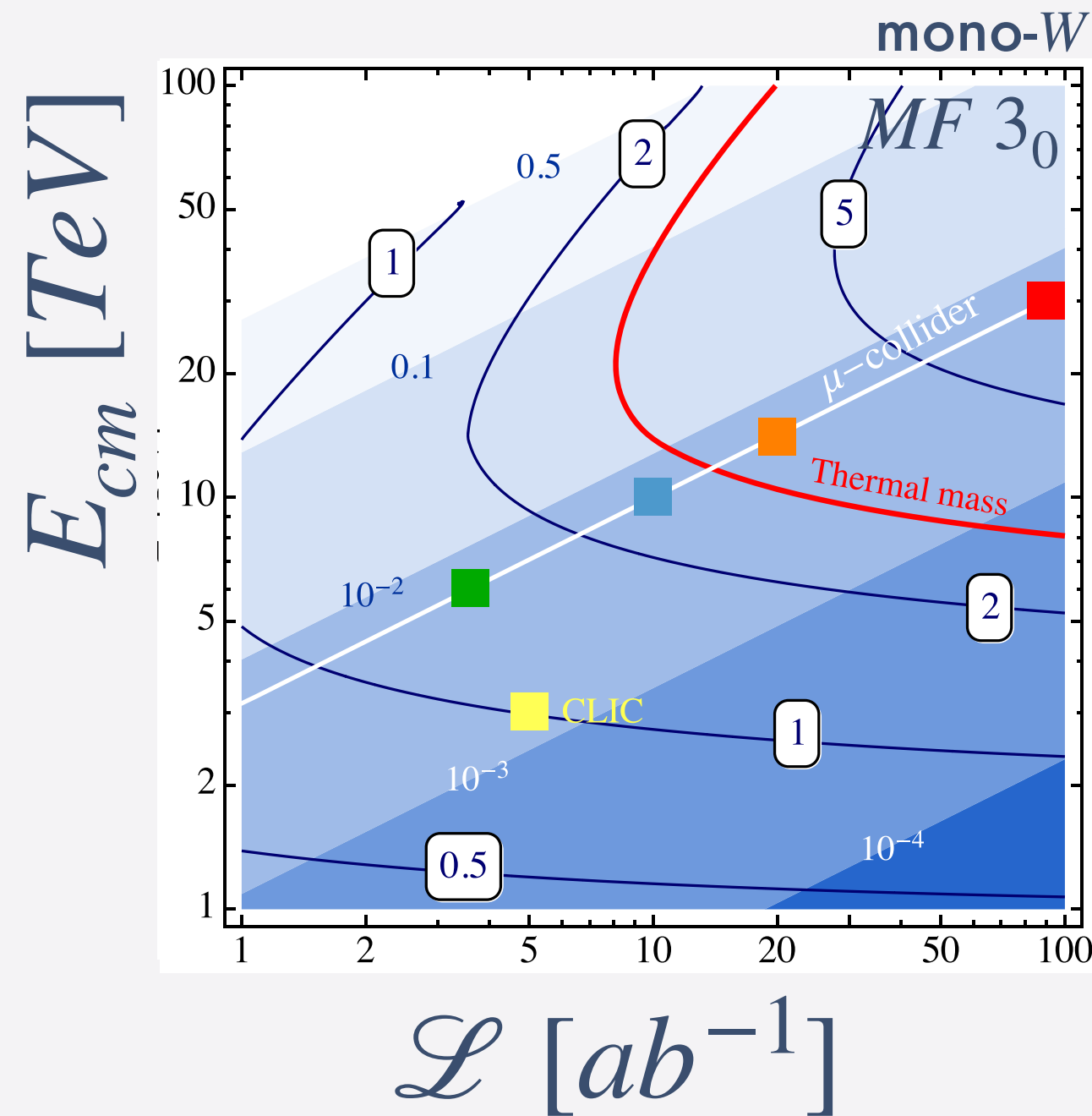


very helpful corroborating evidence multiple signals in several channels expected

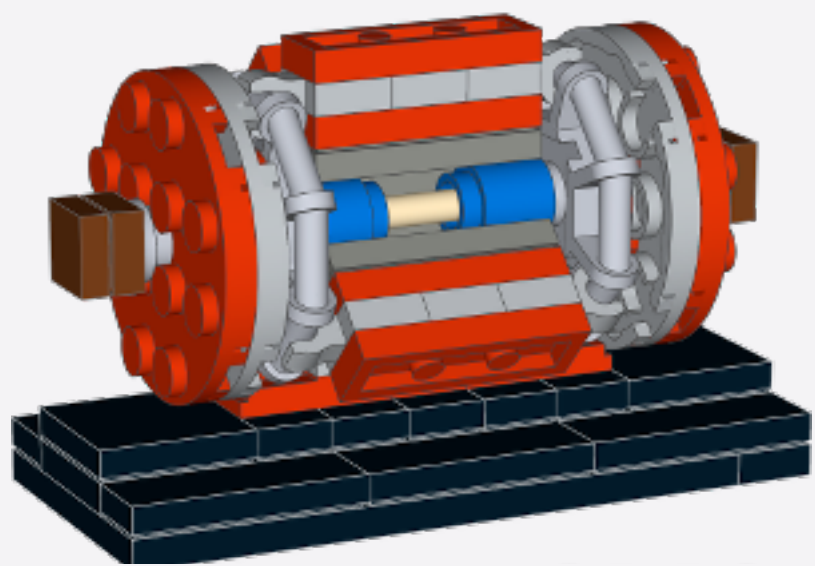
DIRECT PRODUCTION



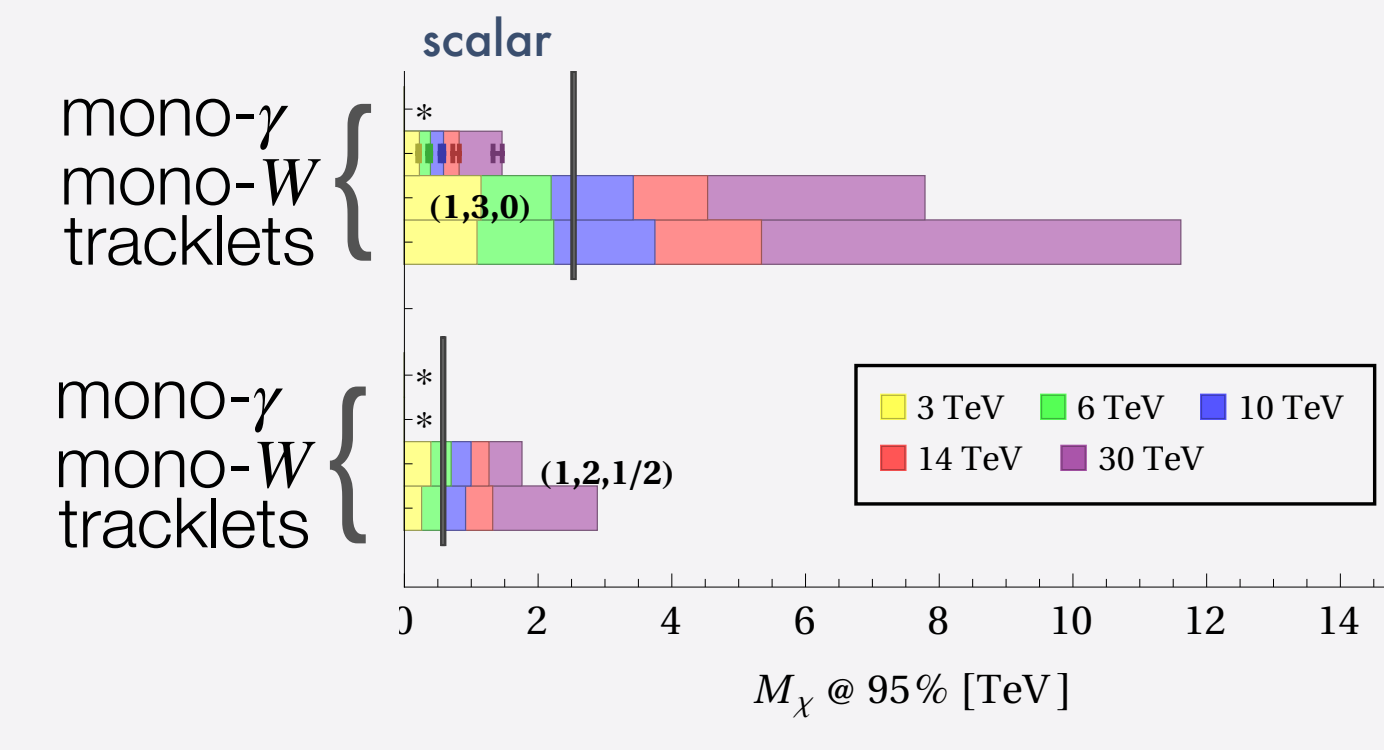
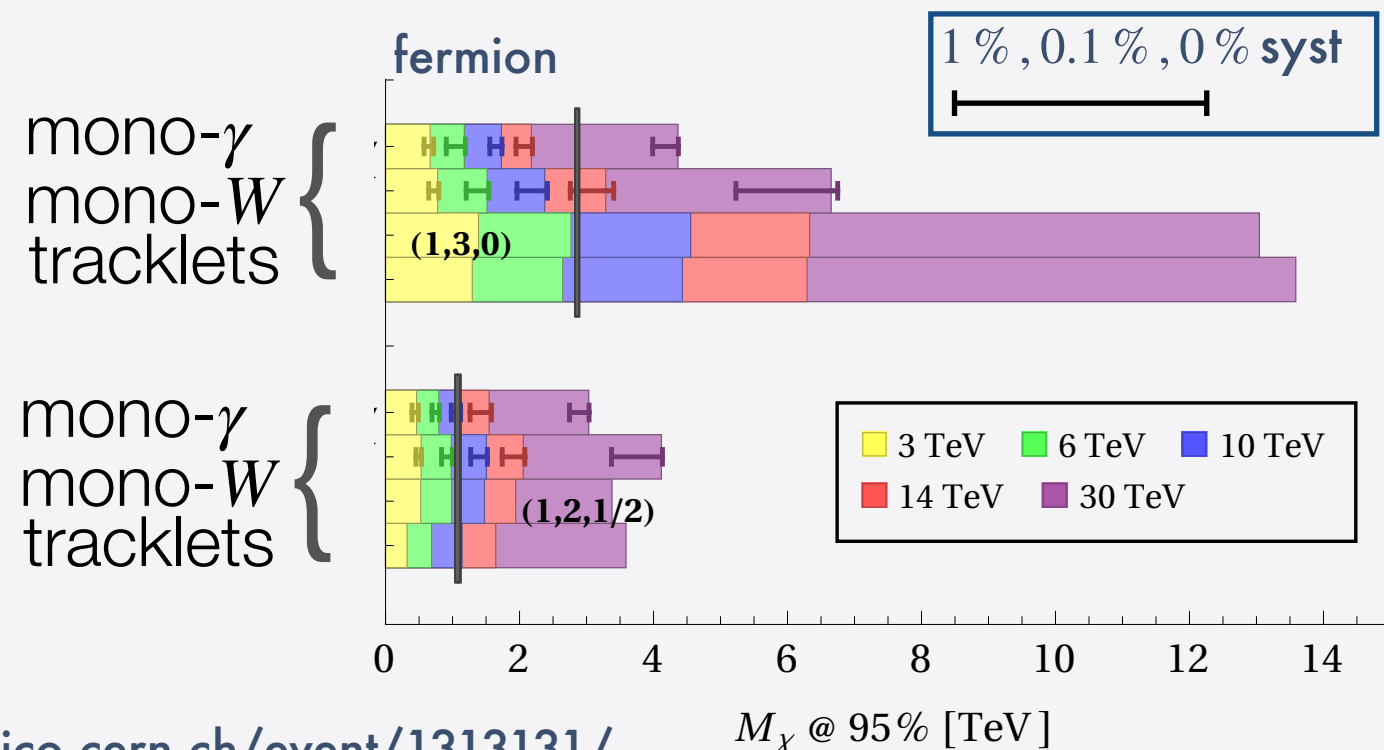
Production of Dark Matter weak multiplet states and observation of the decay products or associated productions



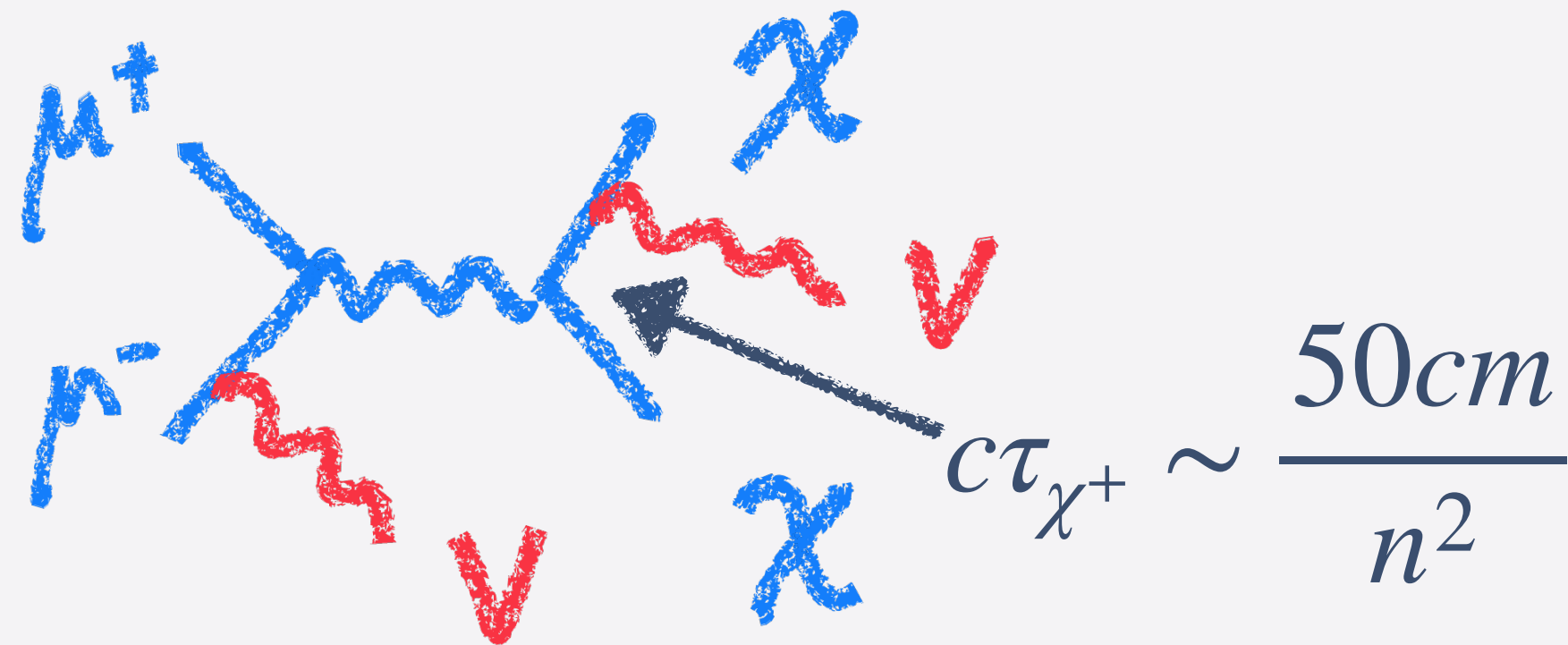
very helpful corroborating evidence multiple signals in several channels expected



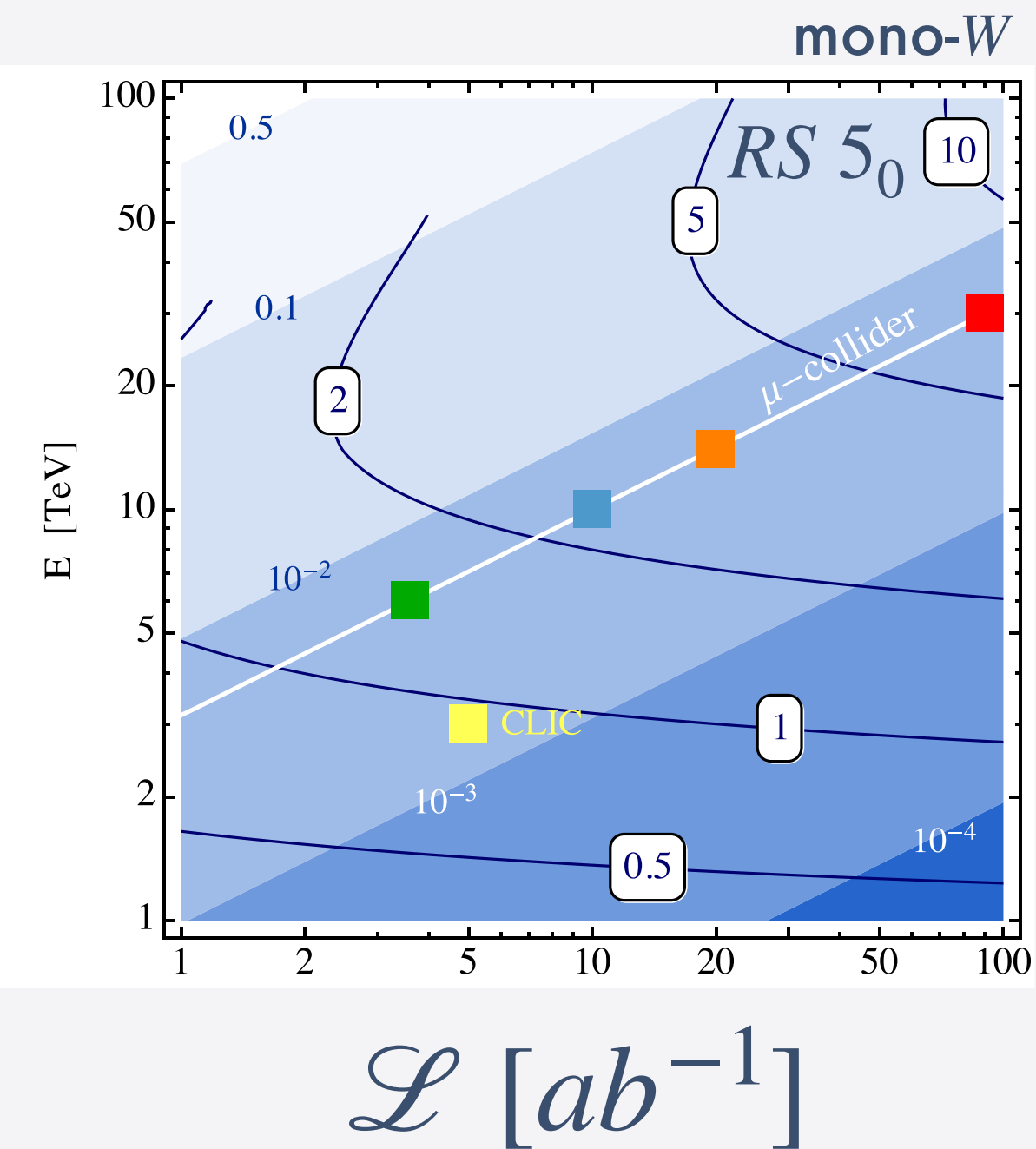
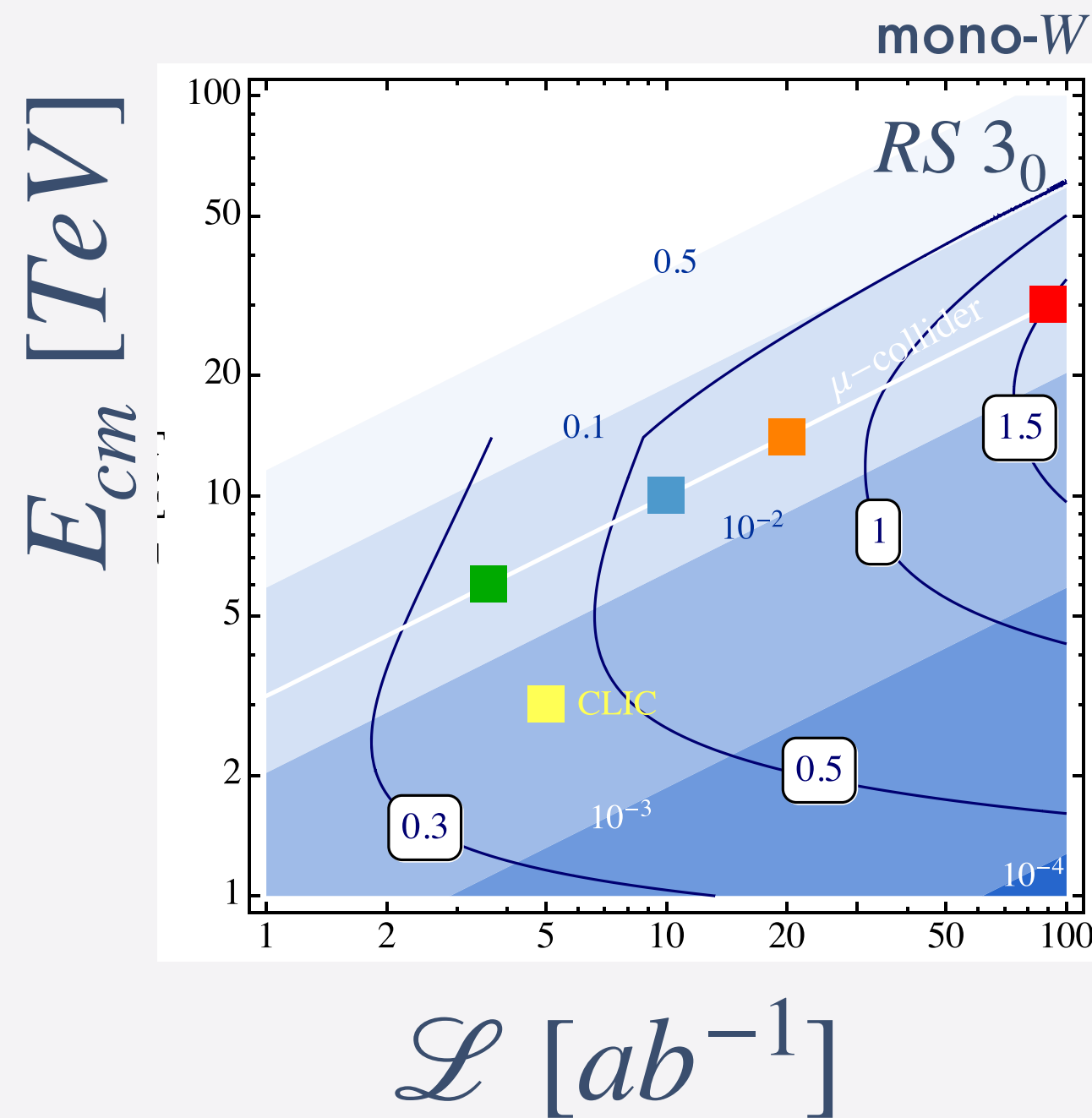
2040s
up to 10+ TeV



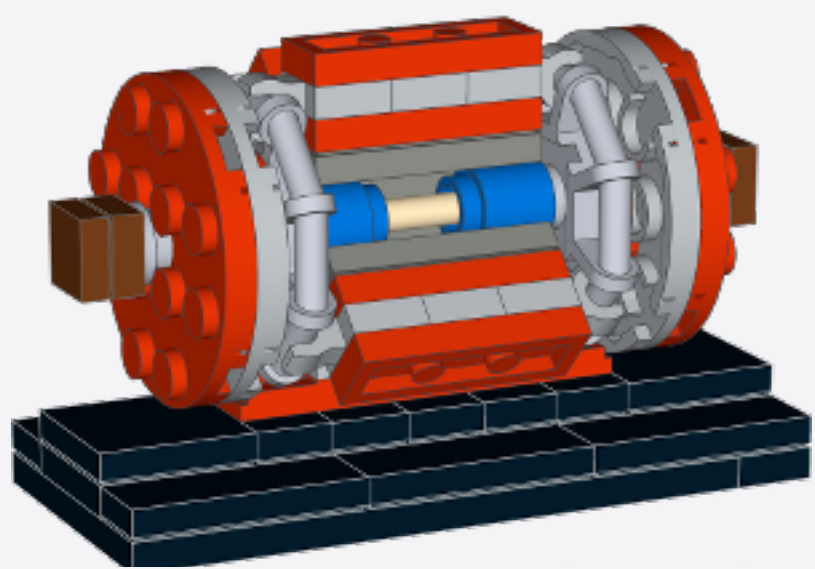
DIRECT PRODUCTION



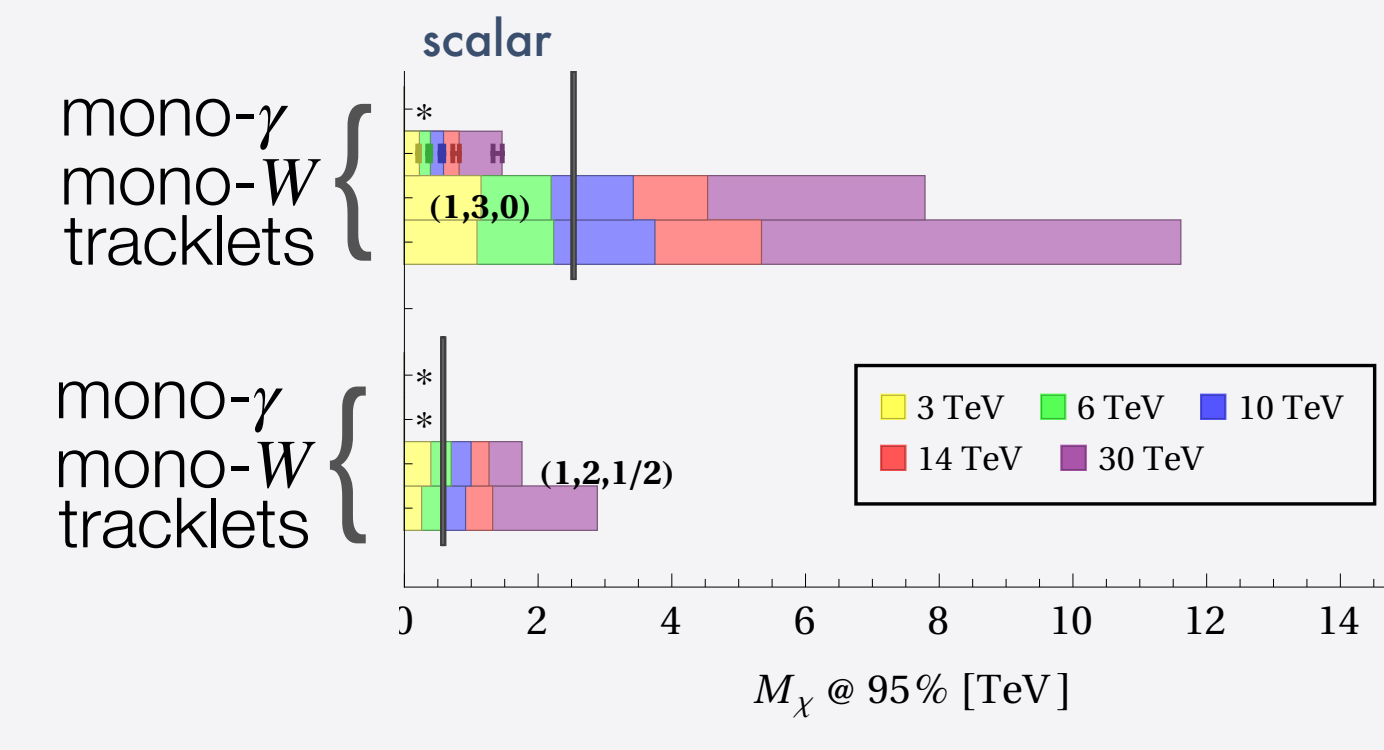
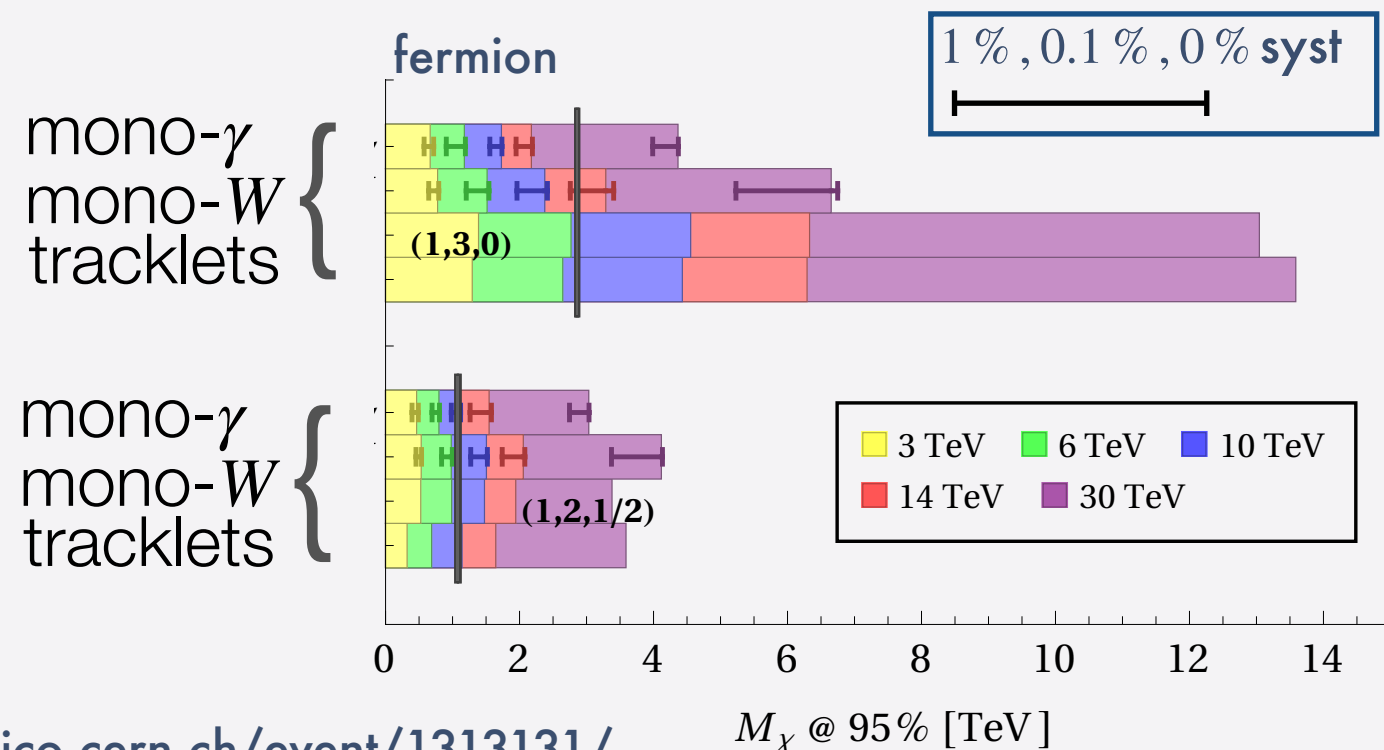
Production of Dark Matter weak multiplet states and observation of the decay products or associated productions



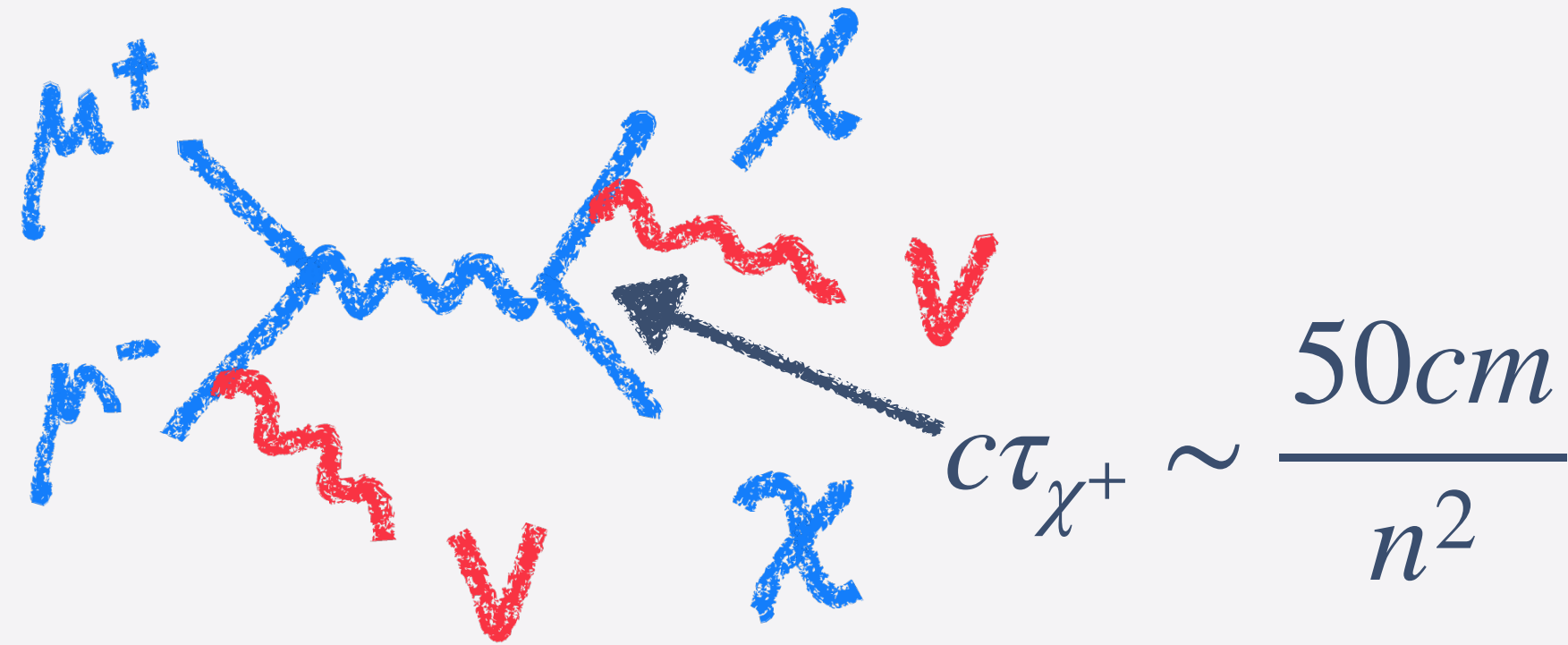
very helpful corroborating evidence multiple signals in several channels expected



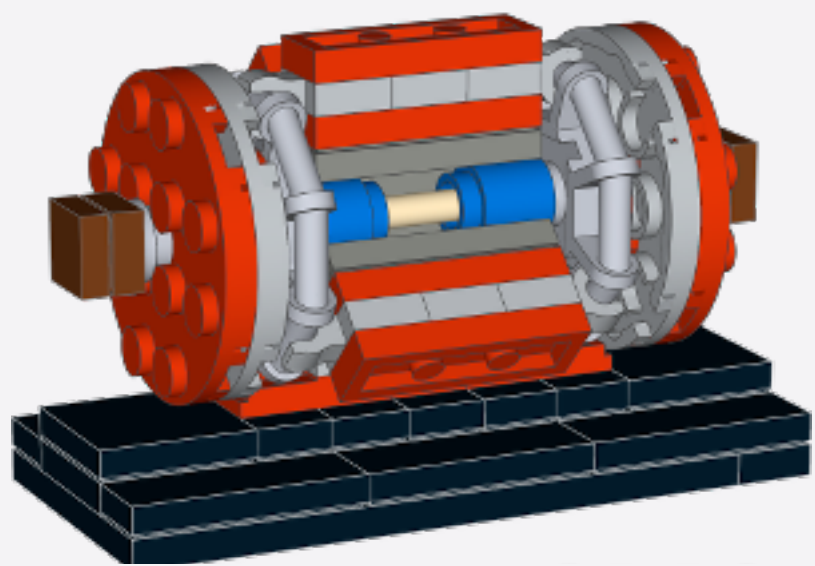
2040s
up to 10+ TeV



DIRECT PRODUCTION



Production of Dark Matter weak multiplet states and observation of the decay products or associated productions

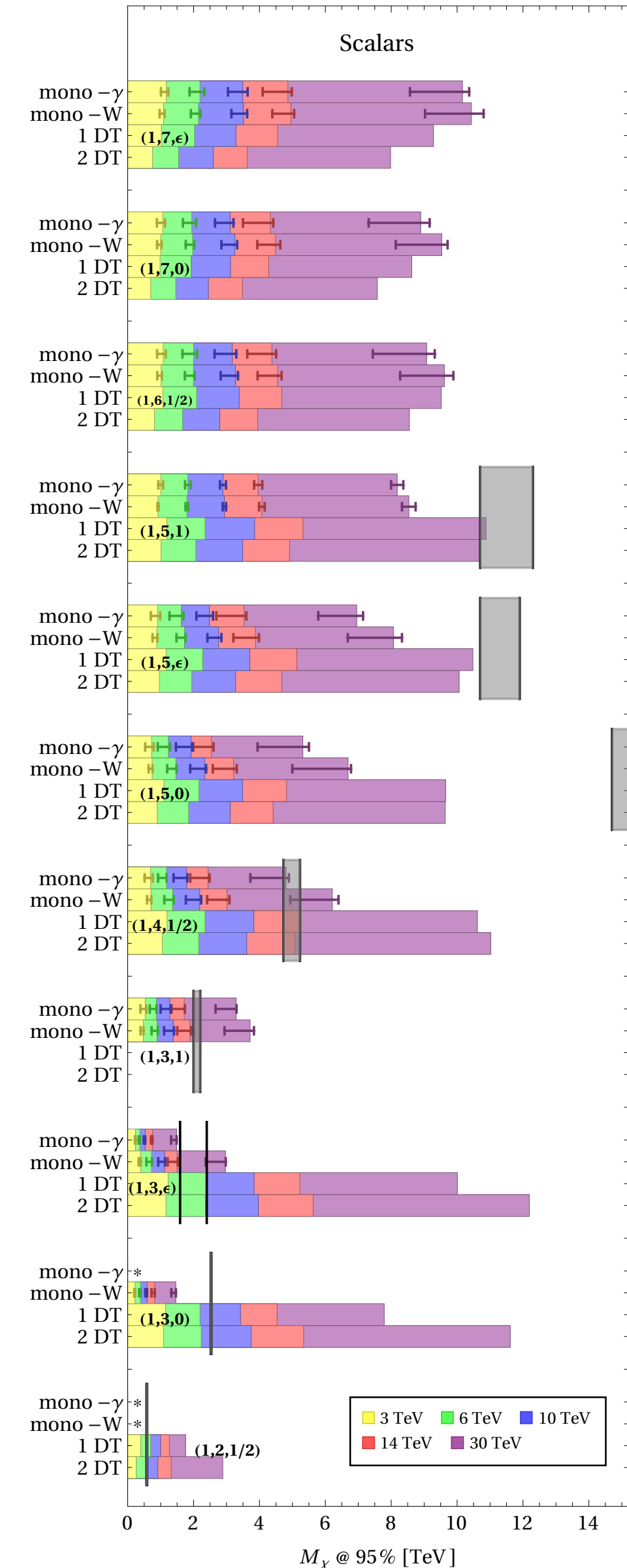
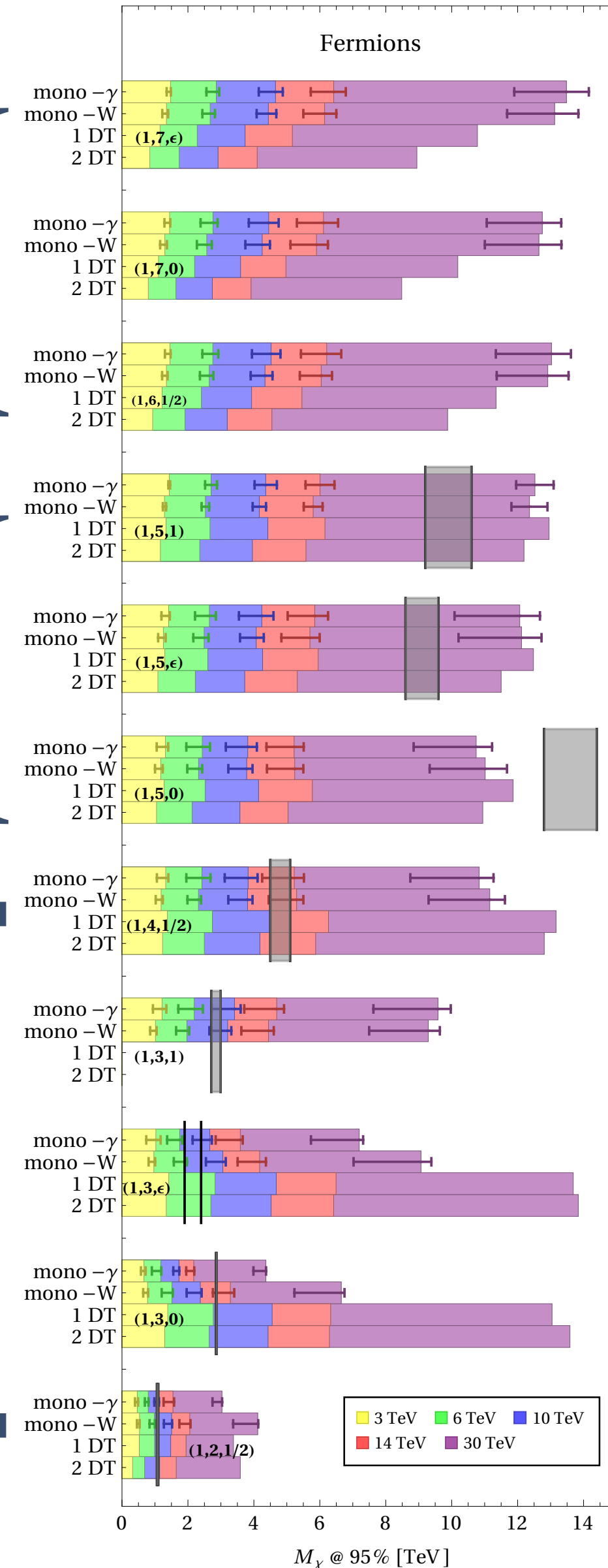


2040s
up to 10+ TeV

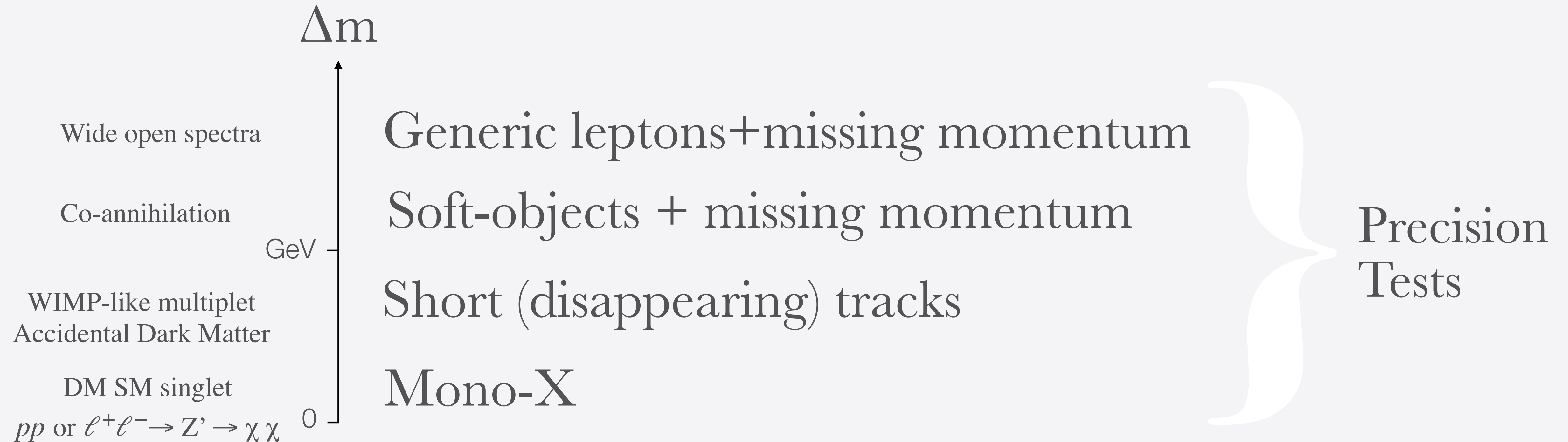
$M_7 \sim 50 \text{ TeV}$

$M_5 \sim 15 \text{ TeV}$

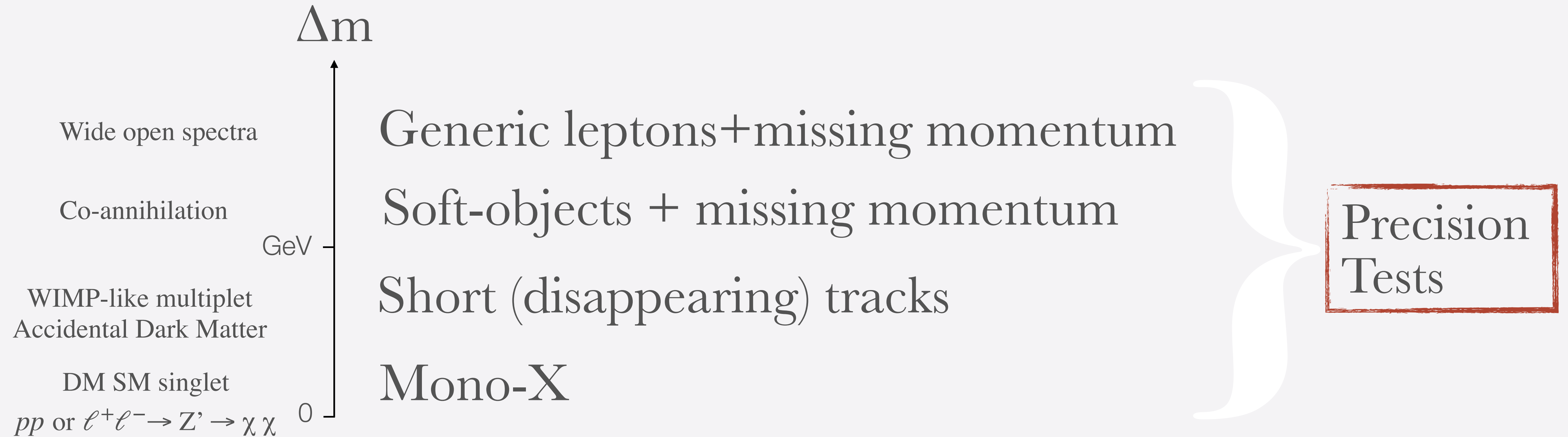
$M_2, M_3, M_4 \leq 5 \text{ TeV}$



DIRECT SIGNALS AT COLLIDERS

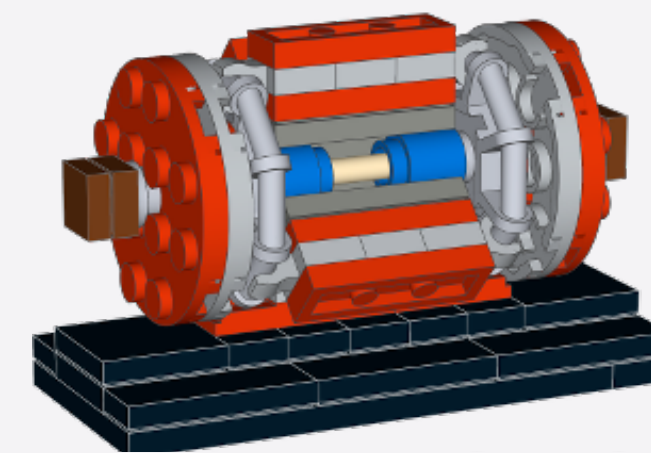


DIRECT SIGNALS AT COLLIDERS



VIRTUAL* PRODUCTION

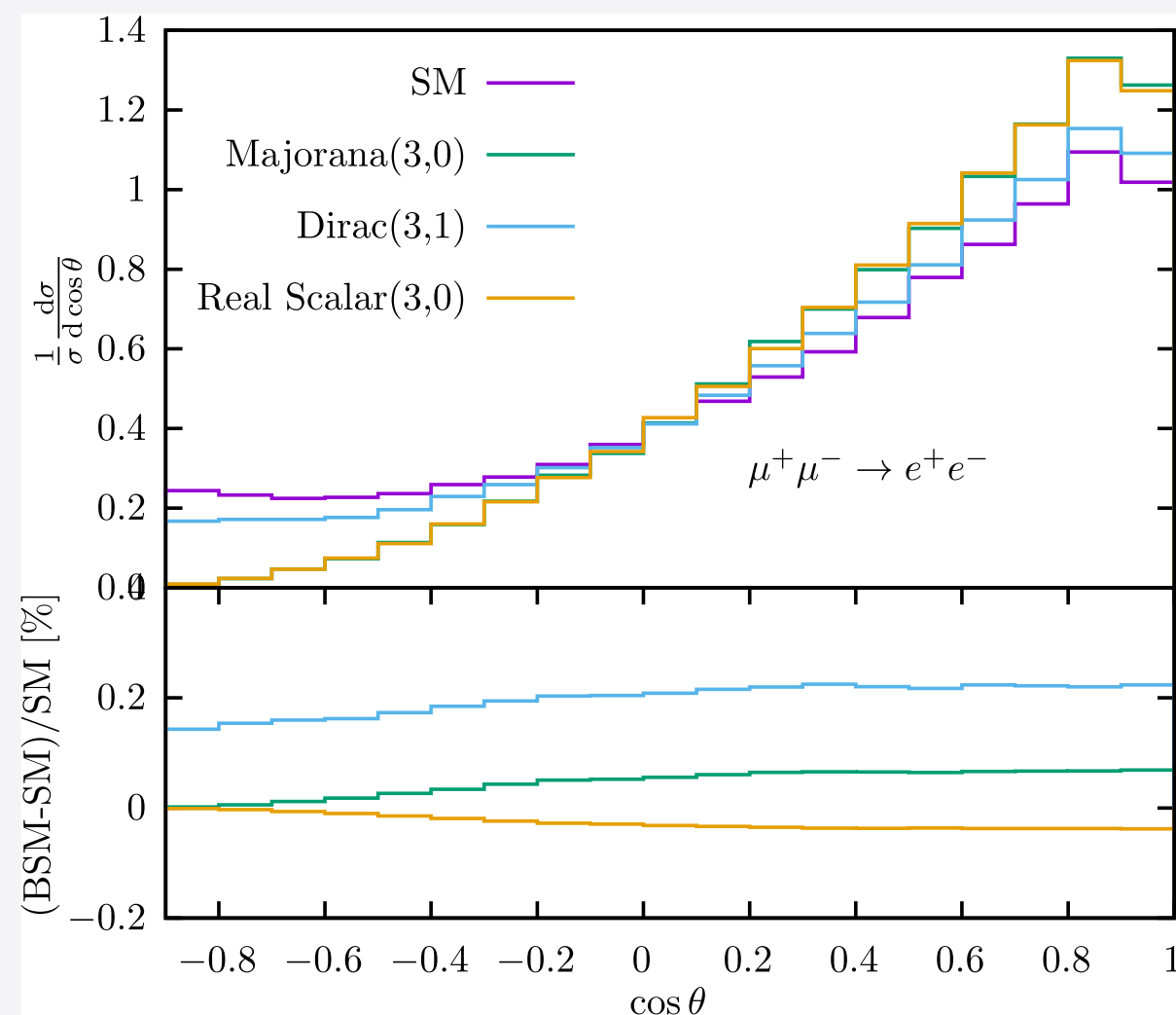
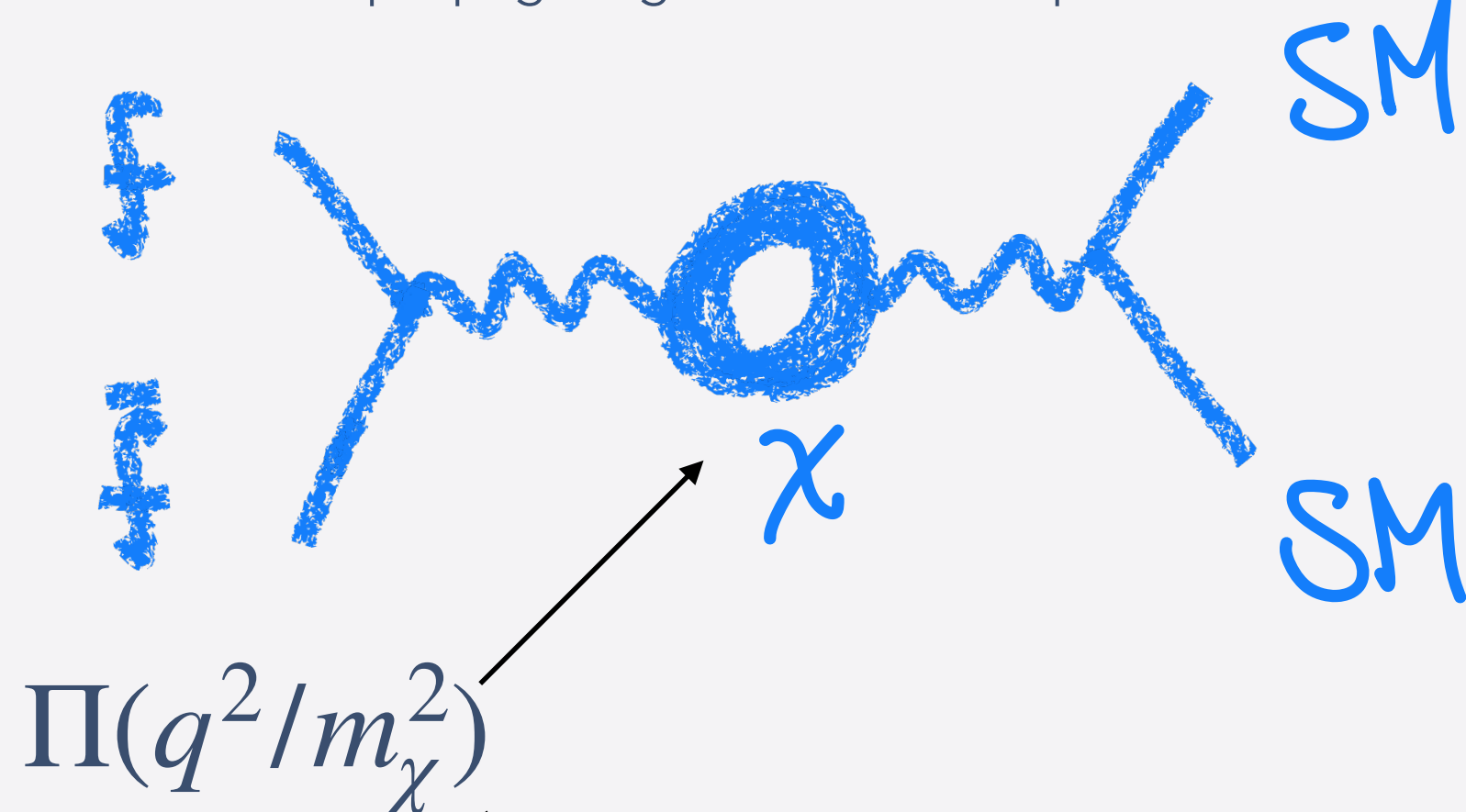
s-channel and *t*-channel



2040s

up to 10+ TeV

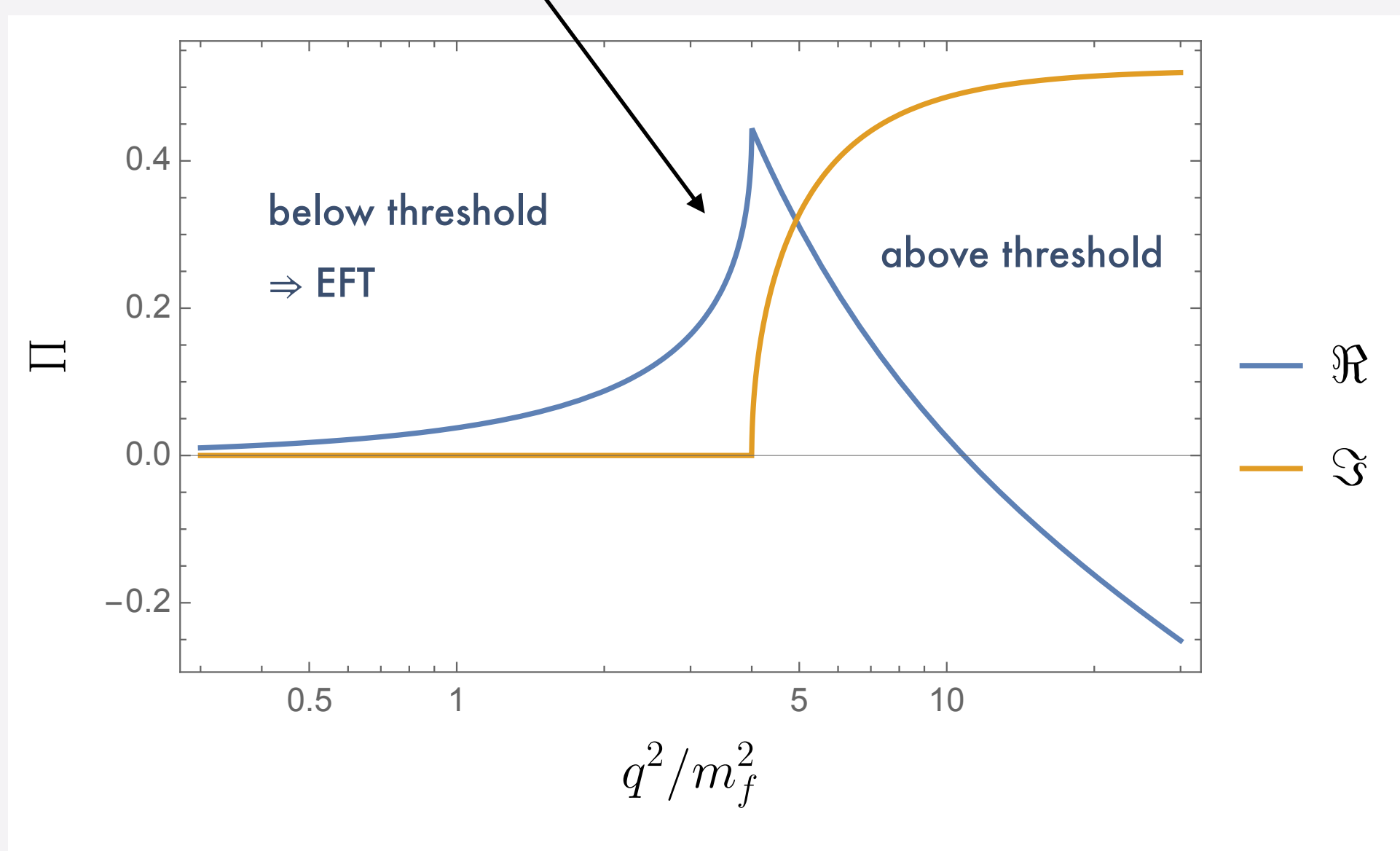
Virtual or propagating DM affects SM production rates



$$SM \subset ff$$

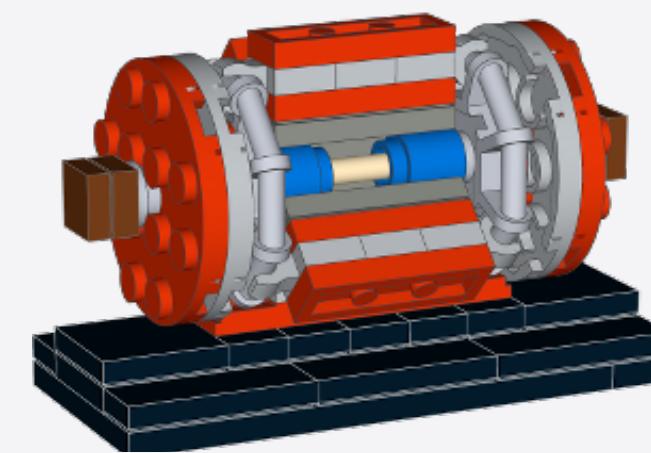
$$\ell^+\ell^- \rightarrow e^+e^-, b\bar{b}, \mu^+\mu^-, c\bar{c}$$

- differential distributions $\frac{d\sigma}{d \cos \theta^*}$
- differential distributions $\frac{d\sigma}{d \cos \theta^*}$



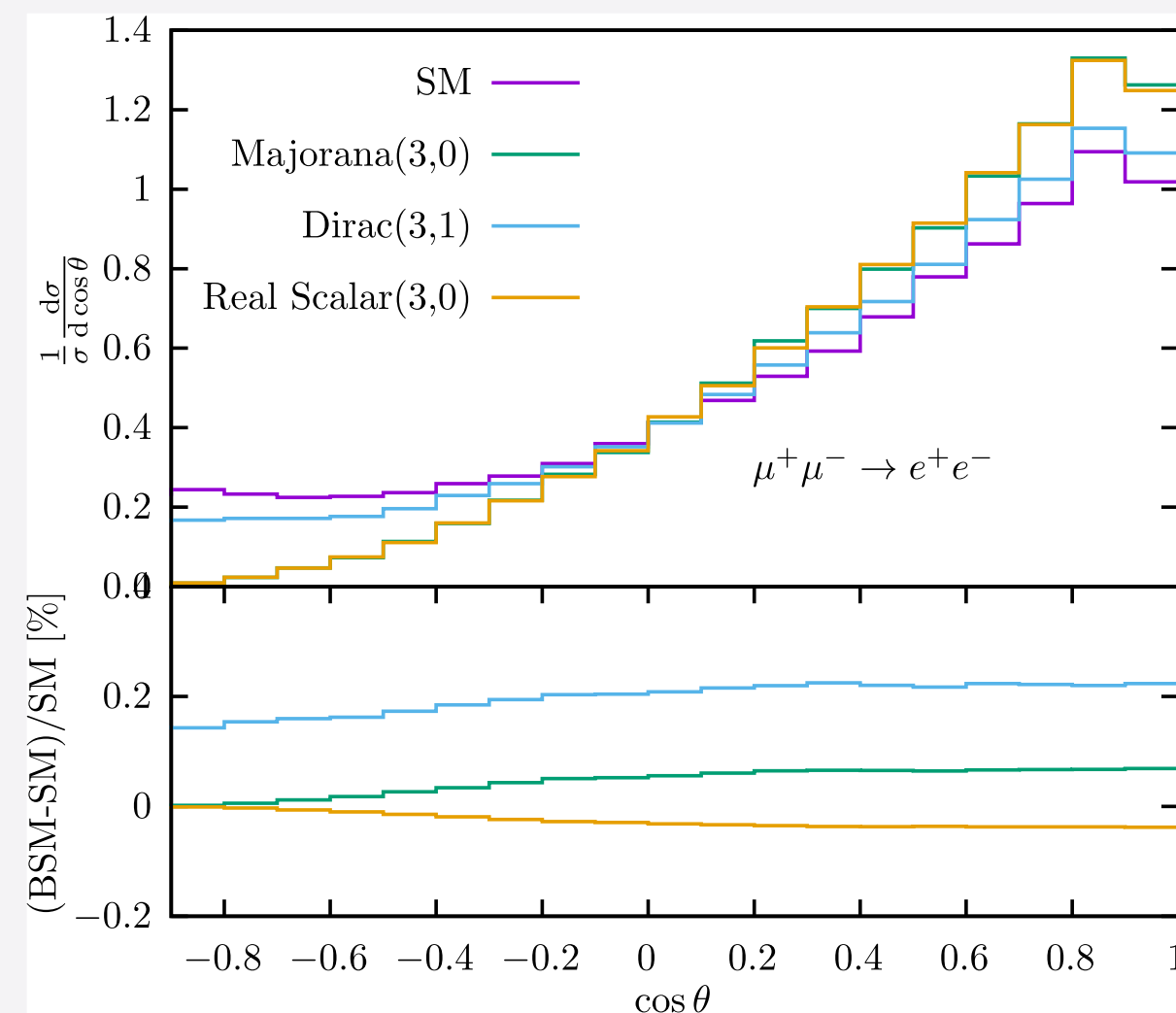
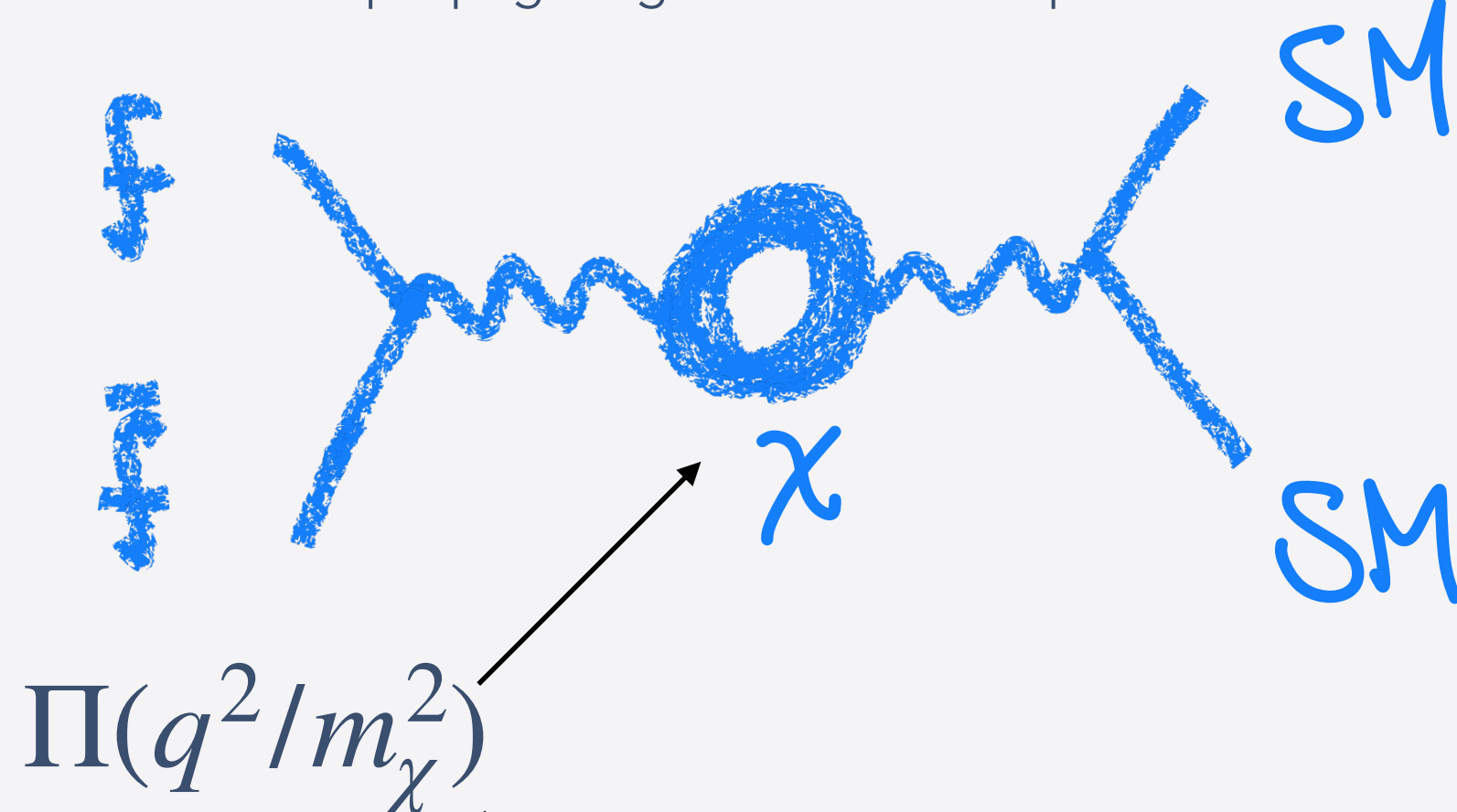
VIRTUAL* PRODUCTION

s-channel and *t*-channel



2040s
up to 10+ TeV

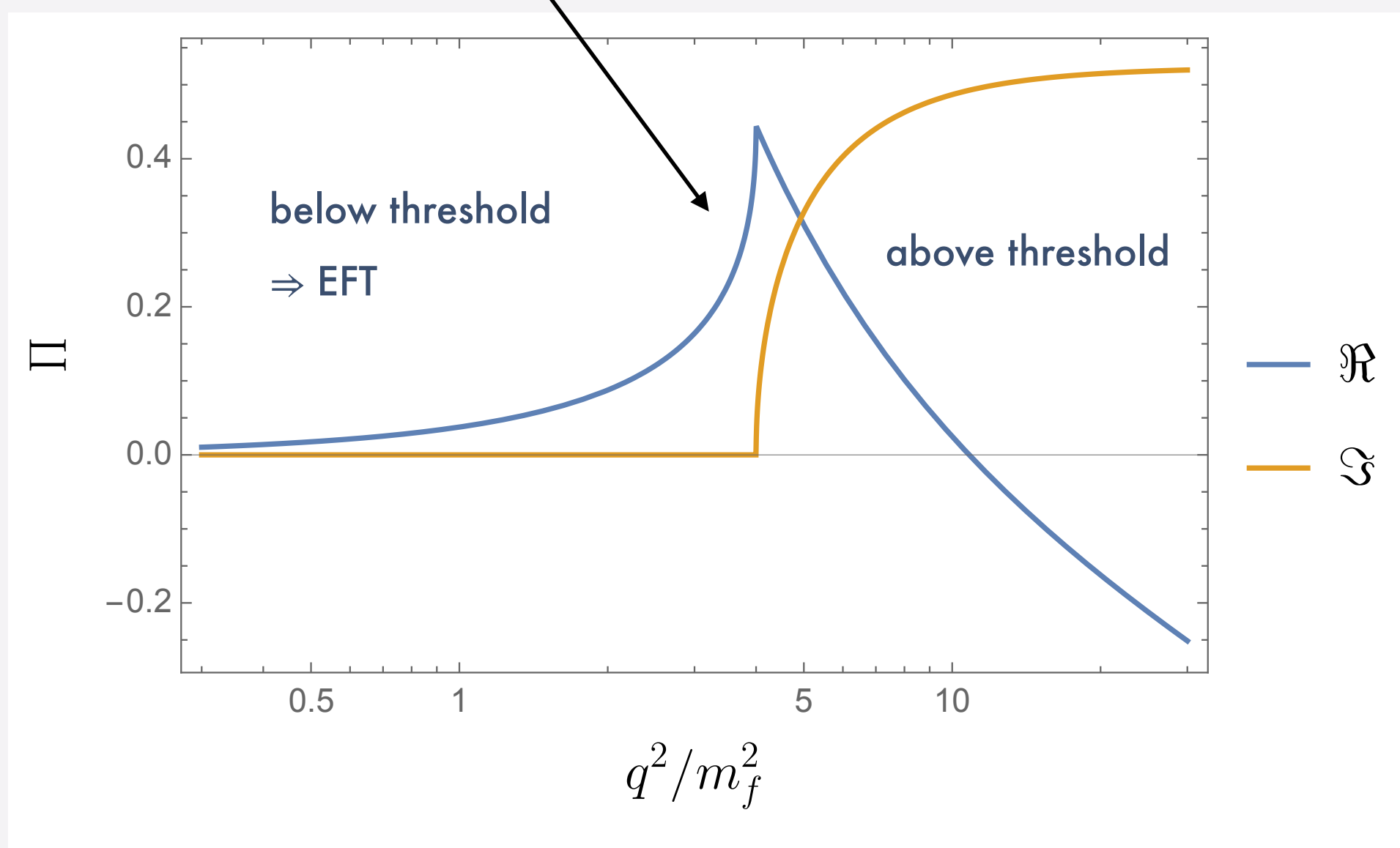
Virtual or propagating DM affects SM production rates



$$SM \subset ff$$

$$\ell^+ \ell^- \rightarrow e^+ e^-, b\bar{b}, \mu^+ \mu^-, c\bar{c}$$

- differential distributions $\frac{d\sigma}{d \cos \theta^*}$
- differential distributions $\frac{d\sigma}{d \cos \theta^*}$



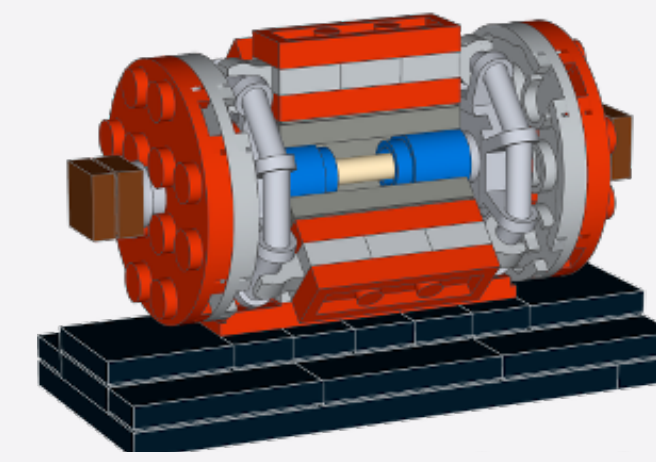
1810.10993

χ / m_χ [TeV]	DM	HL-LHC	HE-LHC	FCC-100	CLIC-3	Muon-14
$(1, 2, 1/2)_{DF}$	1.1	—	—	—	0.4	0.6
$(1, 3, \epsilon)_{CS}$	1.6	—	—	—	0.2	0.2
$(1, 3, \epsilon)_{DF}$	2.0	—	0.6	1.5	0.8 & [1.0, 2.0]	2.2 & [6.3, 7.1]
$(1, 3, 0)_{MF}$	2.8	—	—	0.4	0.6 & [1.2, 1.6]	1.0
$(1, 5, \epsilon)_{CS}$	6.6	0.2	0.4	1.0	0.5 & [0.7, 1.6]	1.6
$(1, 5, \epsilon)_{DF}$	6.6	1.5	2.8	7.1	3.9	11
$(1, 5, 0)_{MF}$	14	0.9	1.8	4.4	2.9	3.5 & [5.1, 8.7]

clear advantage with respect to *pp*

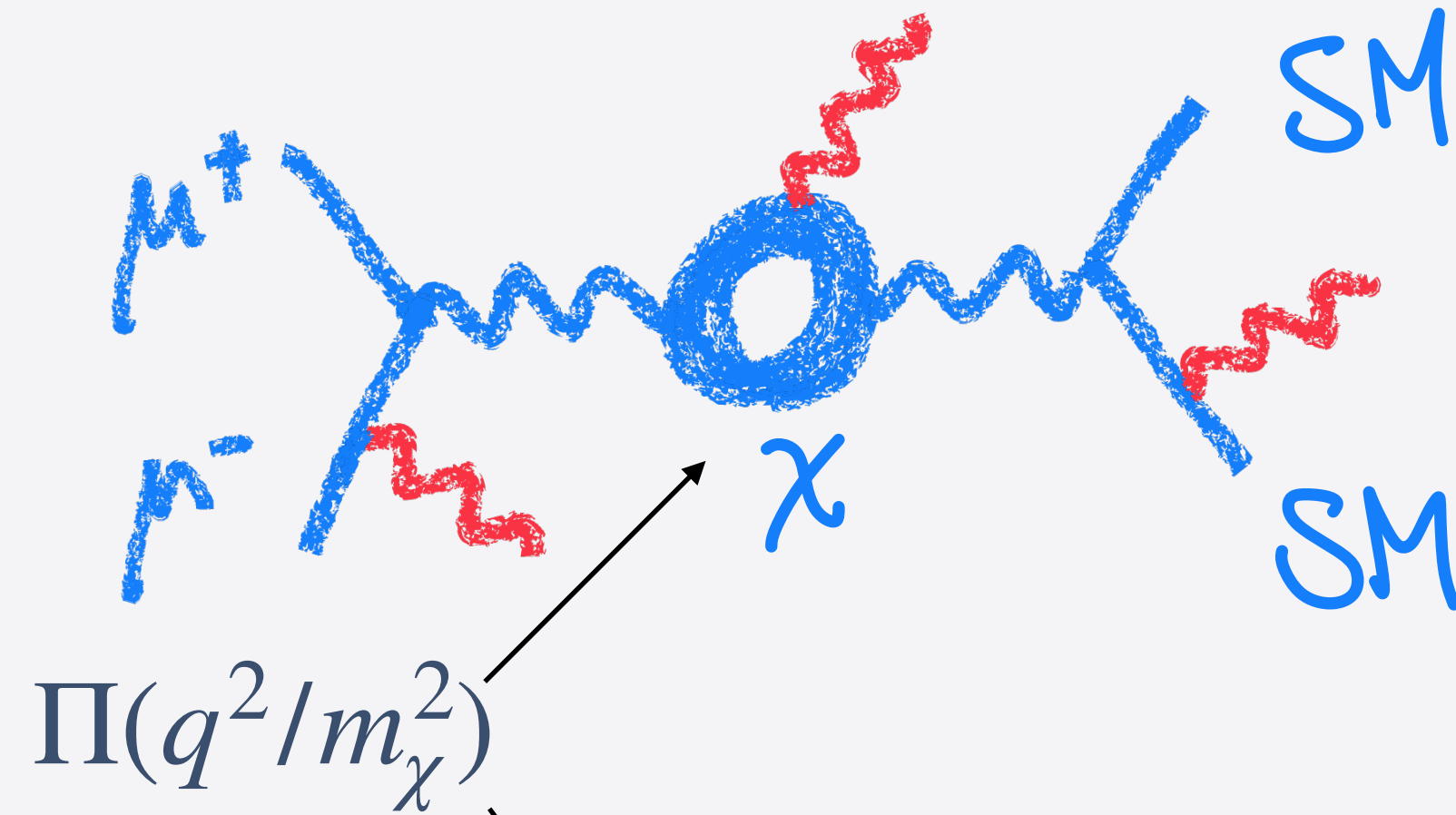
VIRTUAL* PRODUCTION

s-channel and *t*-channel



2040s
up to 10+ TeV

Virtual or propagating DM affects SM production rates



$$SM SM = (ff, VV) + X$$

$$\ell^+ \ell^- \rightarrow e^+ e^-, b\bar{b}, \mu^+ \mu^-, c\bar{c}$$

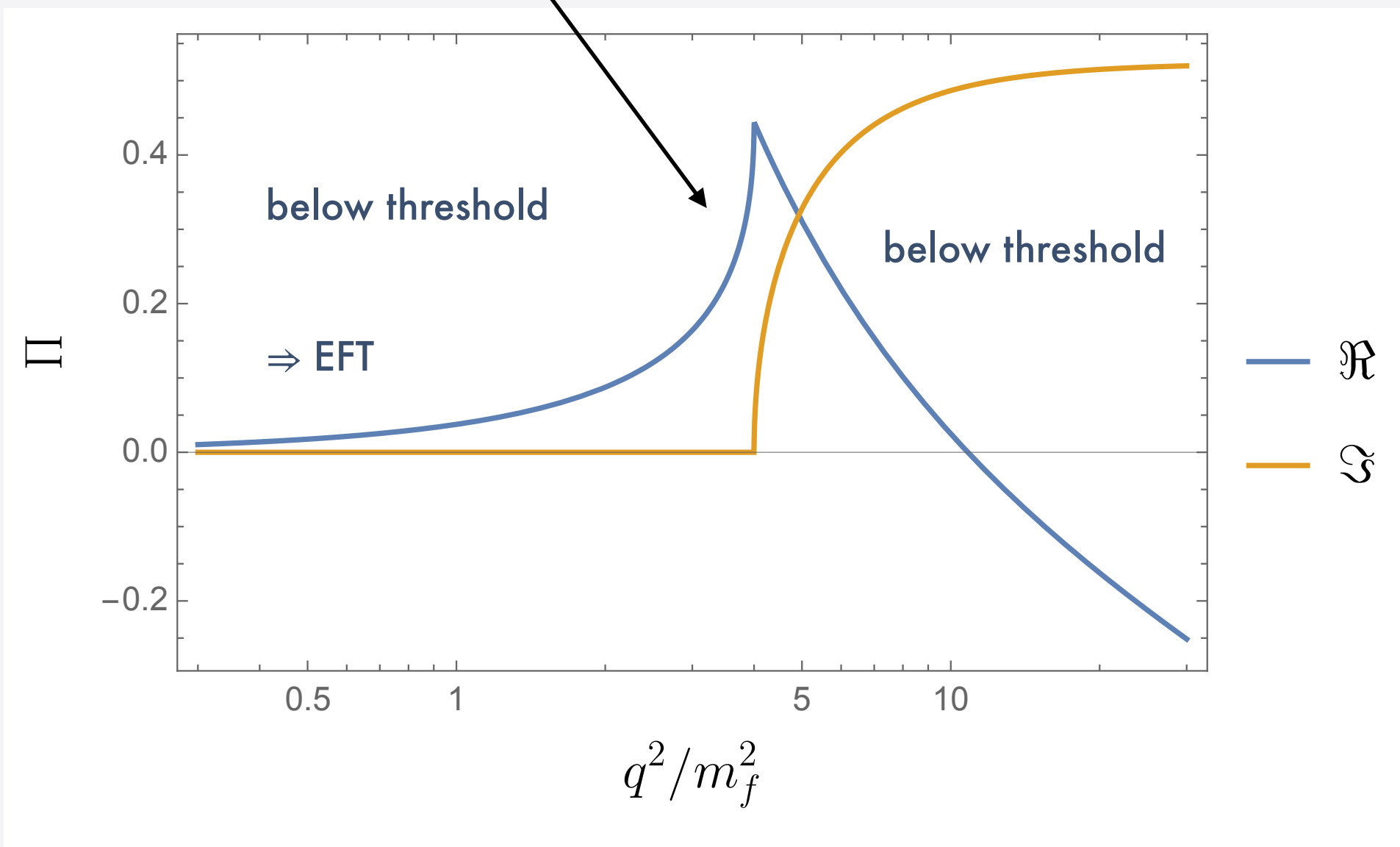
- differential distributions $\frac{d\sigma}{d \cos \theta^*}$
- differential distributions $\frac{d\sigma}{d \cos \theta^*}$

$$\ell^+ \ell^- \rightarrow jj, tt, Zh, W^+ W^-, Wff'$$

- inclusive fiducial rates

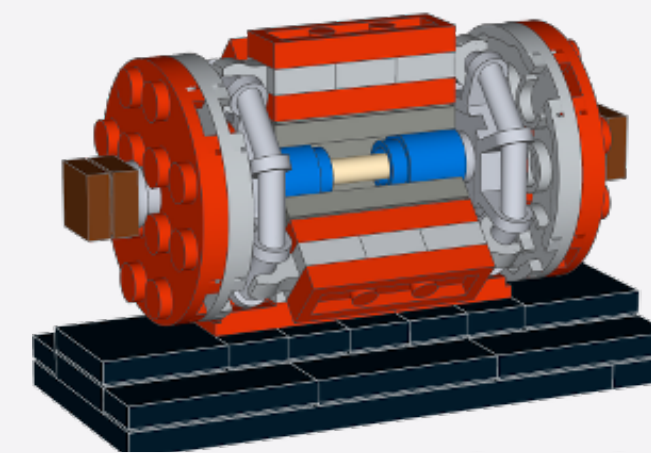
precision SM studies \Rightarrow systematics are the key

- luminosity measurements for inclusive fiducial measurements
 $\mu\text{h}\alpha\mu\text{h}\alpha$ scattering $\Rightarrow \delta\mathcal{L}/\mathcal{L} = 0.2\%$ at 1.5 TeV (ref)
- other systematics affecting SM final states



VIRTUAL* PRODUCTION

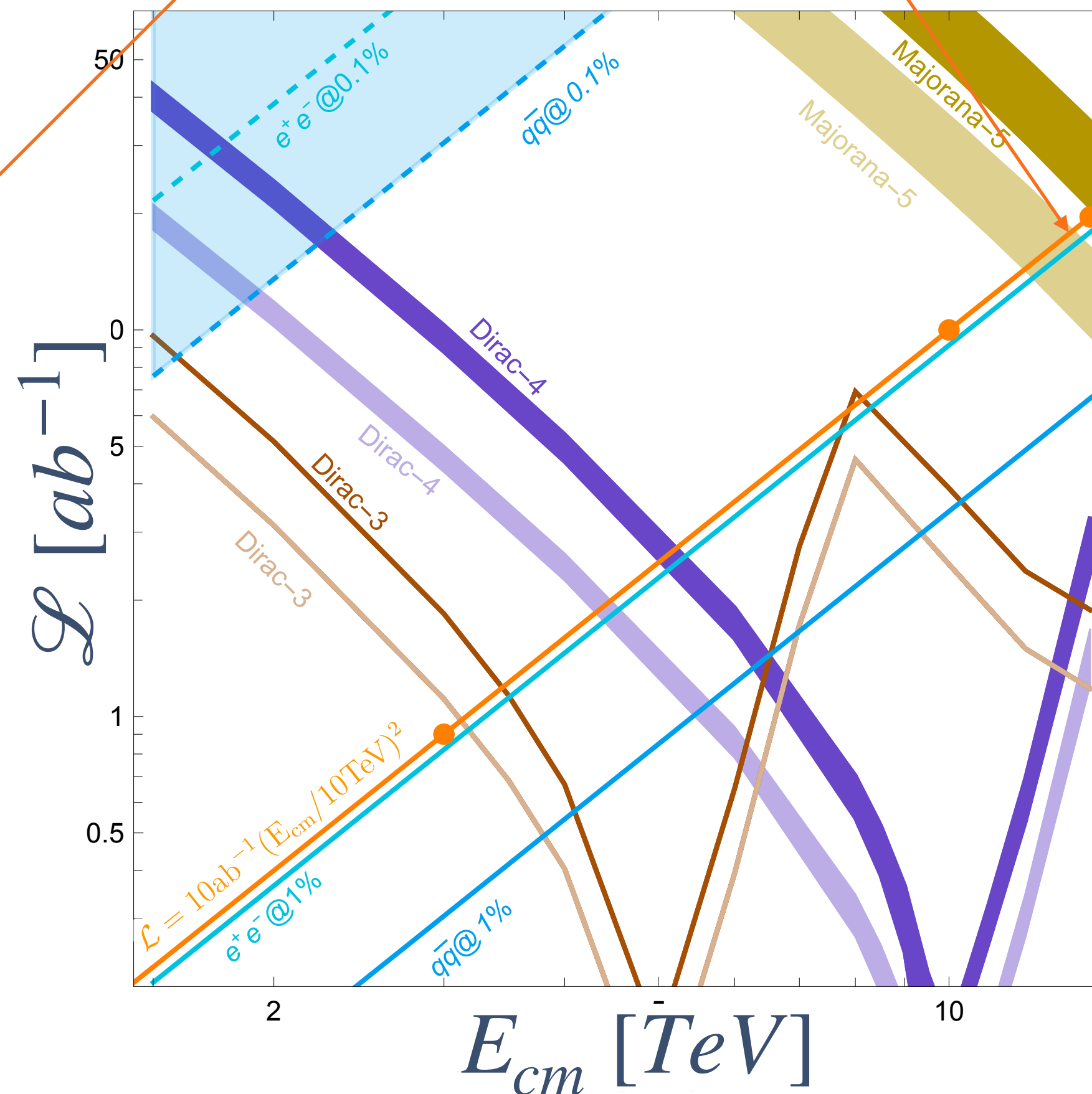
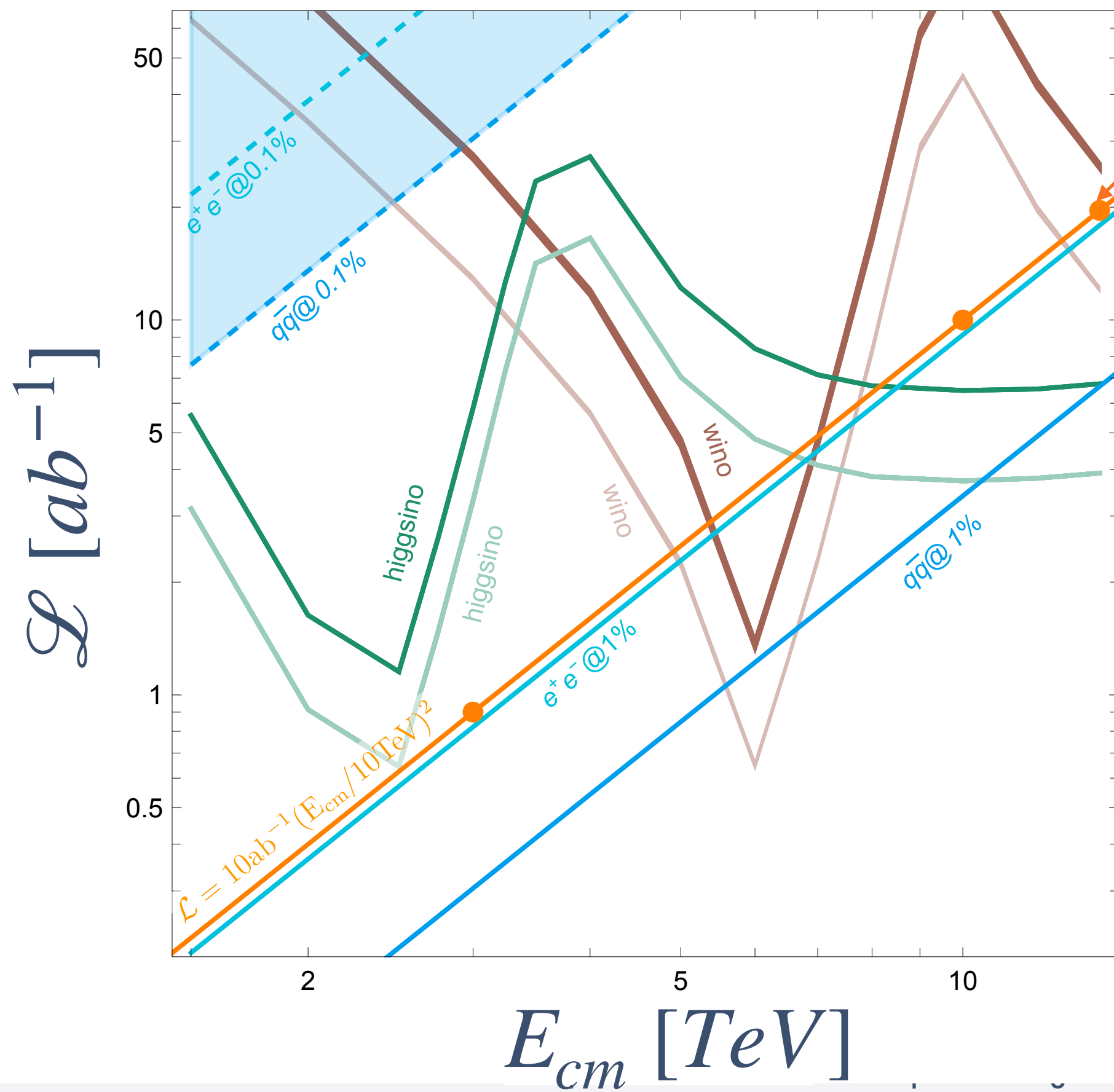
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

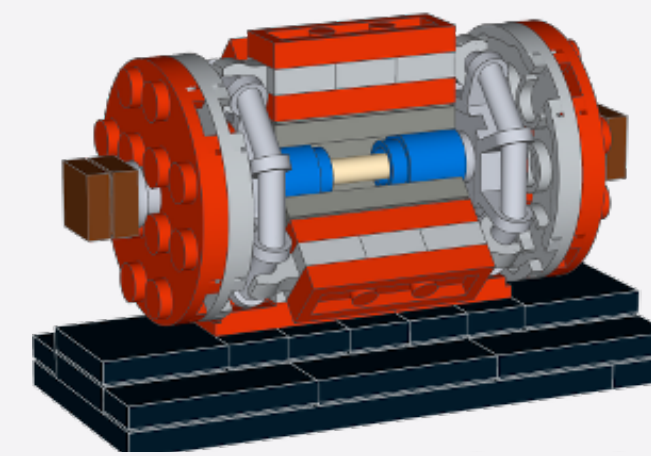
up to 10+ TeV

$$\mathcal{L} = 10 \text{ ab}^{-1} \cdot (E_{com}/10 \text{ TeV})^2$$



VIRTUAL* PRODUCTION

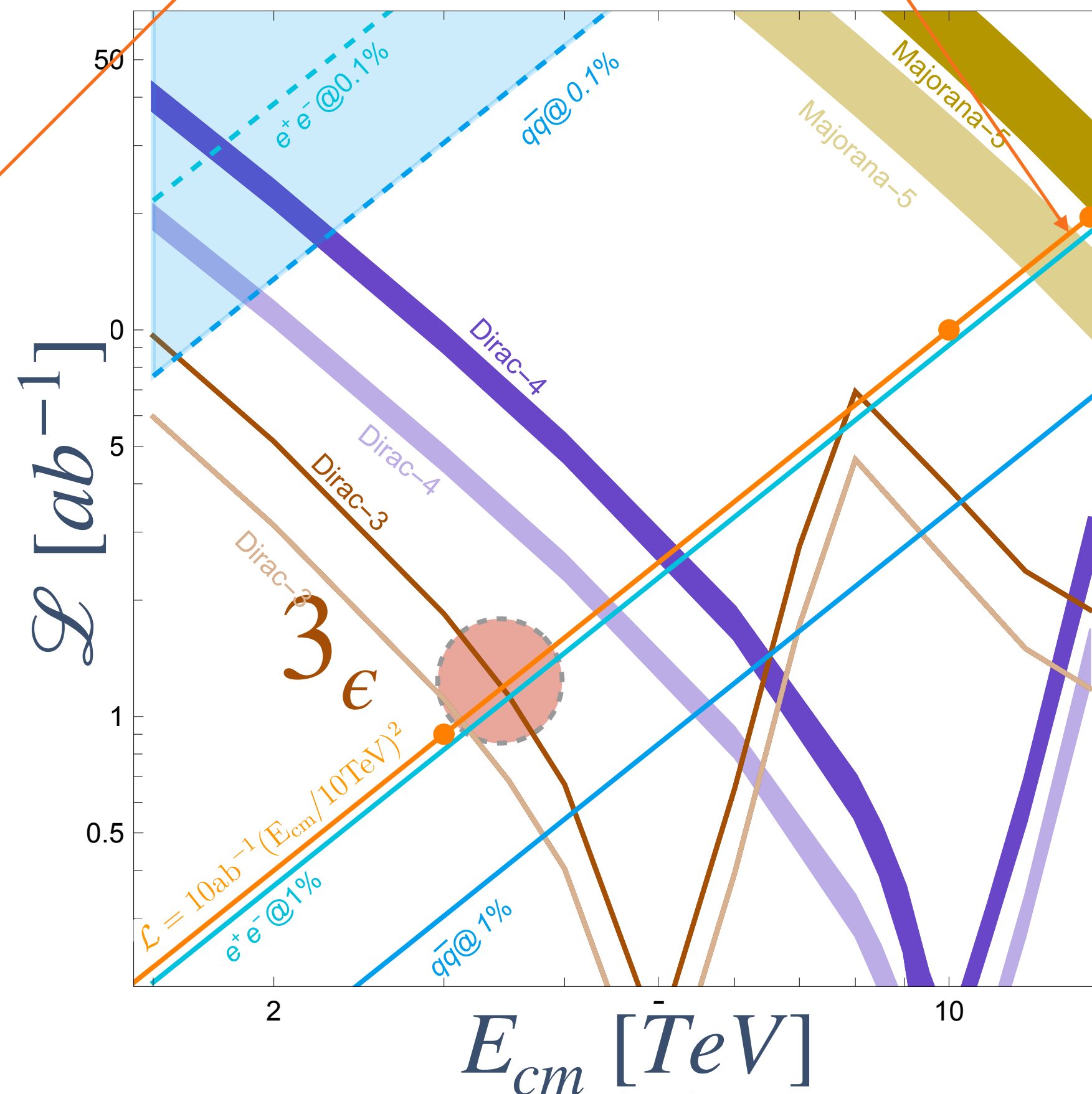
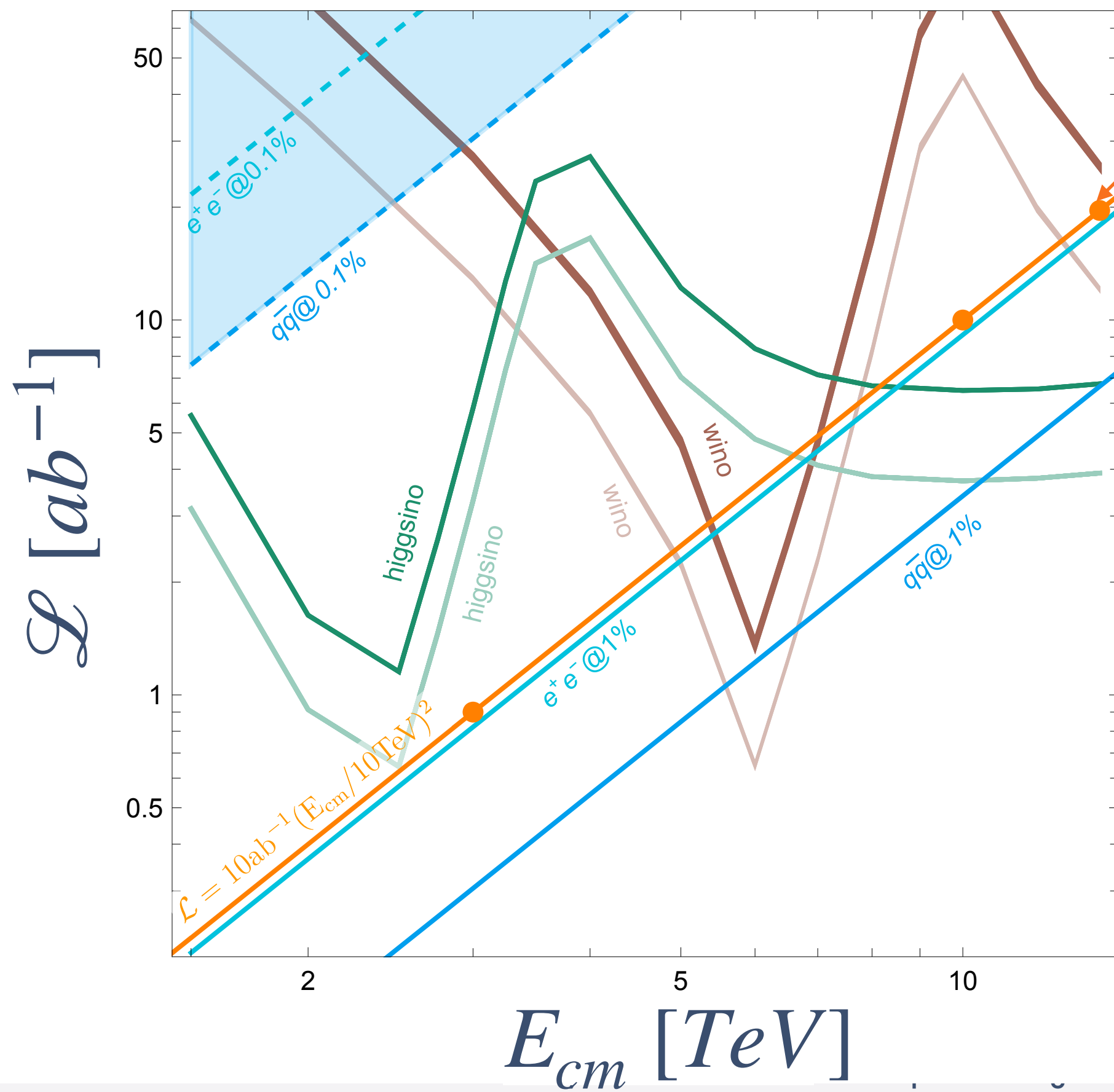
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

up to 10+ TeV

$$\mathcal{L} = 10 \text{ ab}^{-1} \cdot (E_{com}/10 \text{ TeV})^2$$

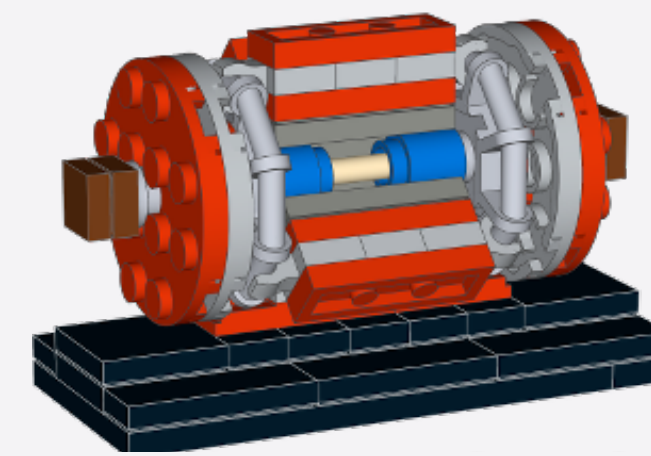


$(3, \epsilon)_{Dirac}$

$\ell^+ \ell^- 3 \text{ TeV } 1 \text{ ab}^{-1}$

VIRTUAL* PRODUCTION

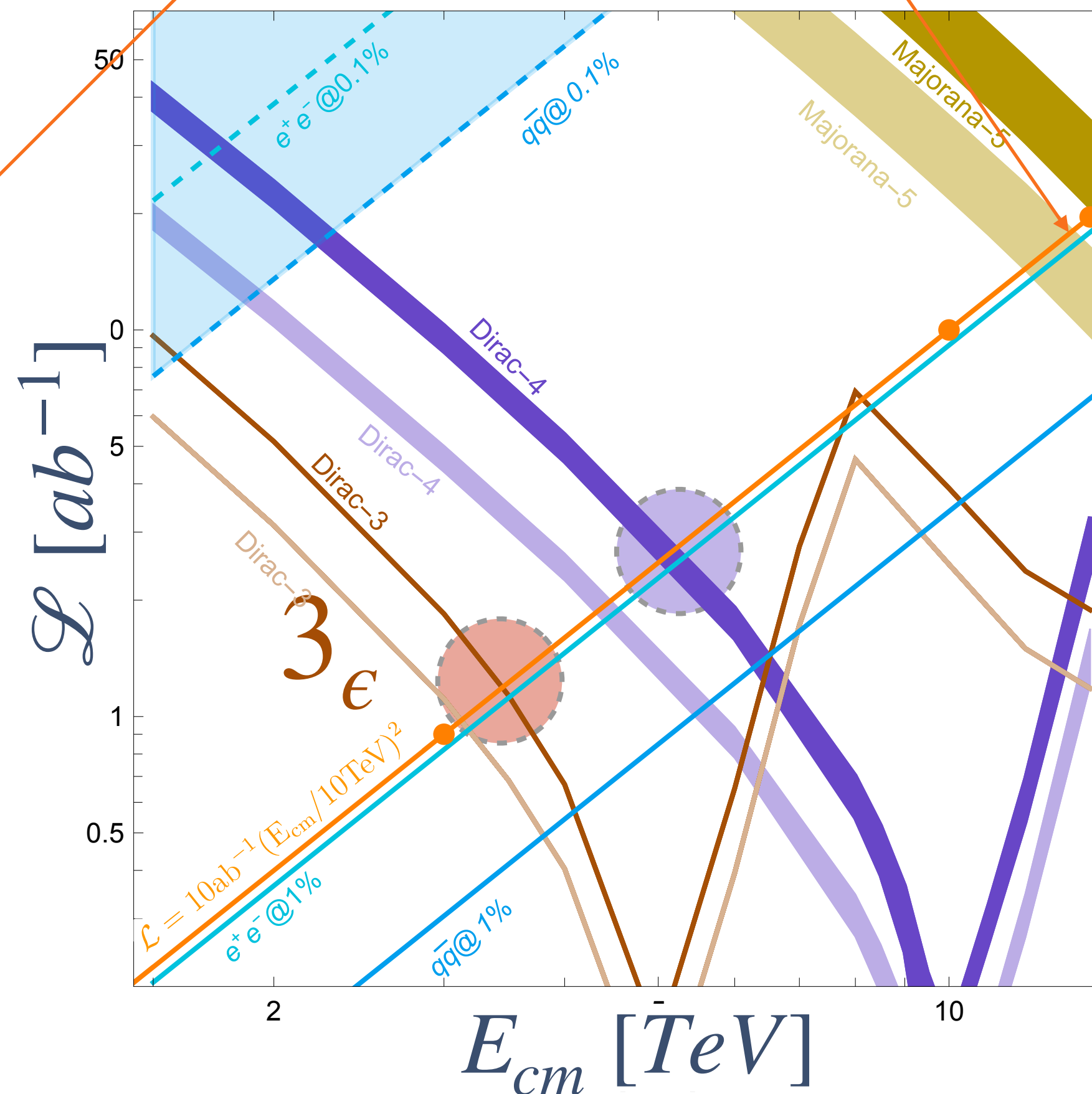
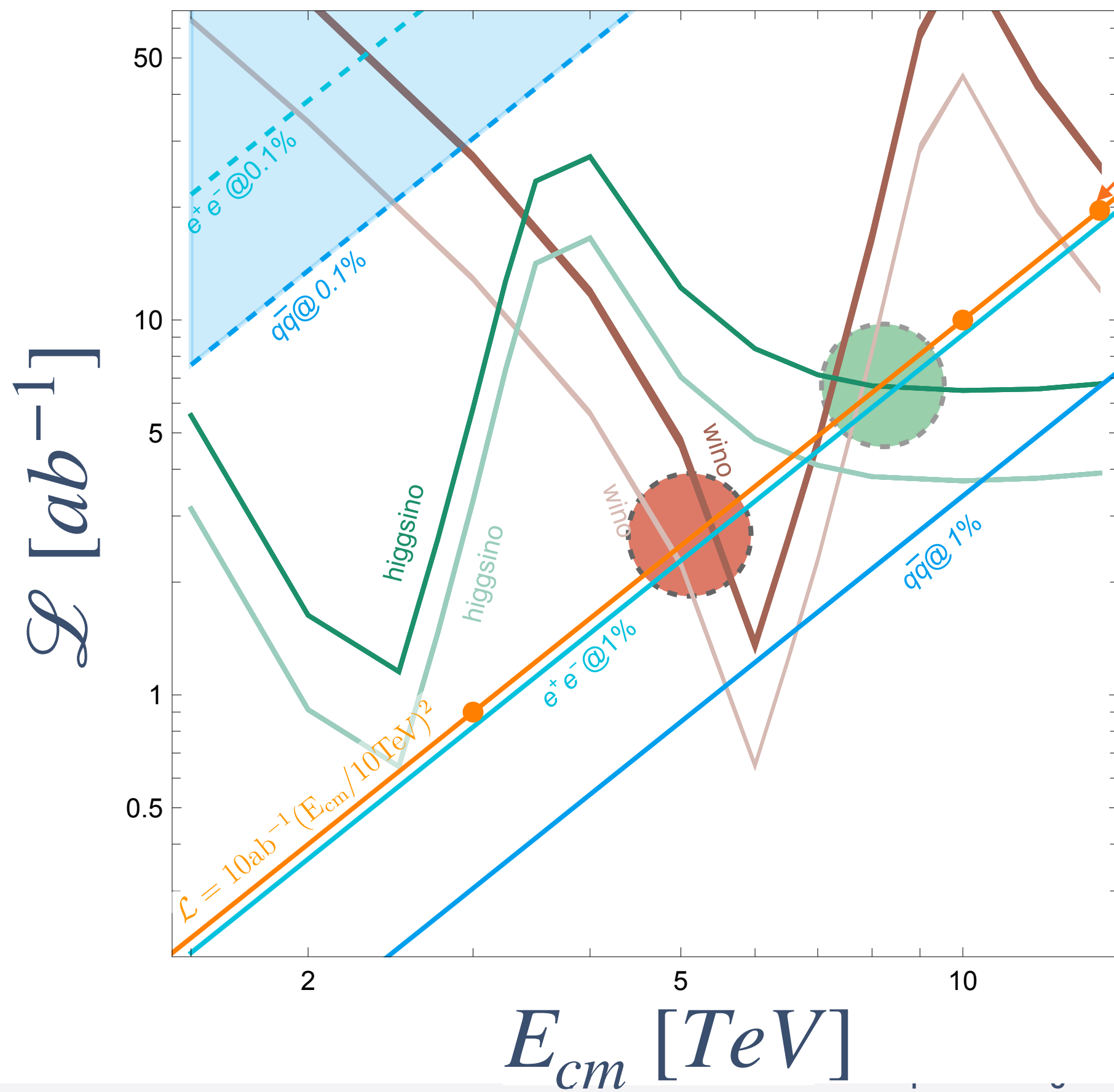
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

up to 10+ TeV

$$\mathcal{L} = 10 \text{ ab}^{-1} \cdot (E_{com}/10 \text{ TeV})^2$$



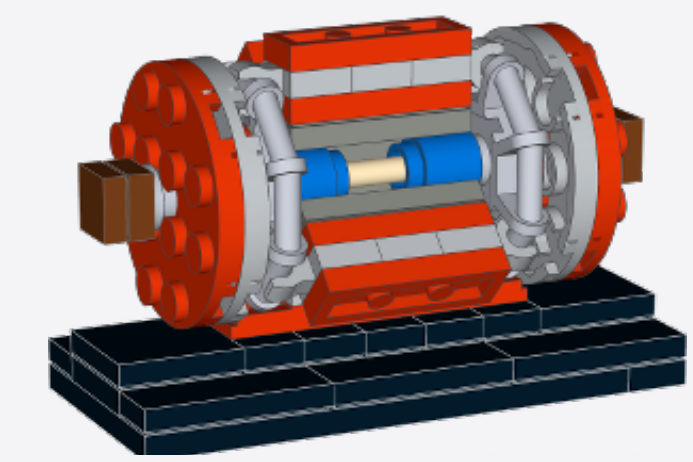
- $\left(4, \frac{1}{2}\right)$ Dirac
- $(3, 0)$ Majorana
- $(3, \epsilon)$ Dirac
- $\left(2, \frac{1}{2}\right)$ Dirac

$$\ell^+ \ell^- \text{ 10 TeV } 10 \text{ ab}^{-1}$$

$$\ell^+ \ell^- \text{ 3 TeV } 1 \text{ ab}^{-1}$$

VIRTUAL* PRODUCTION

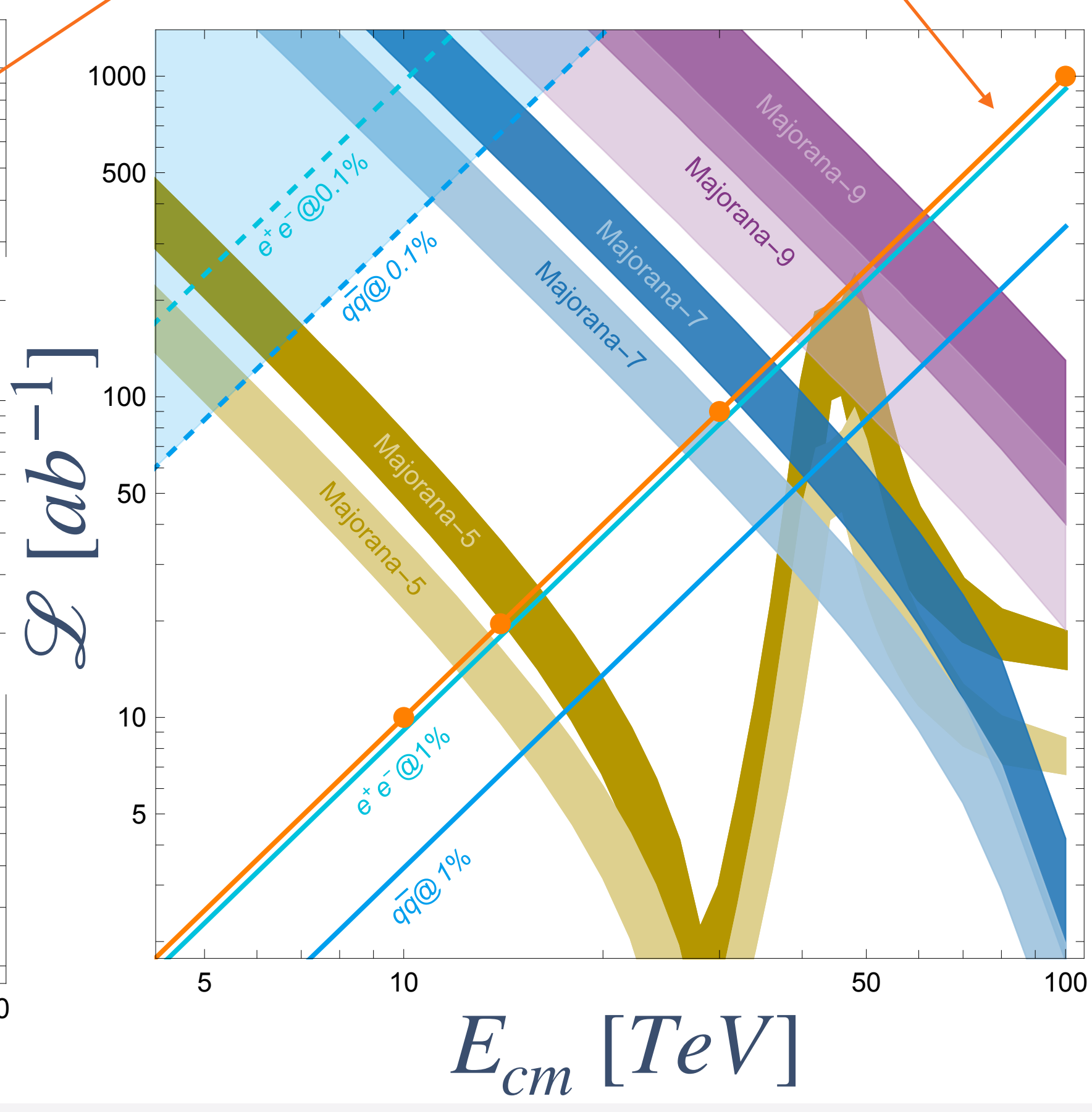
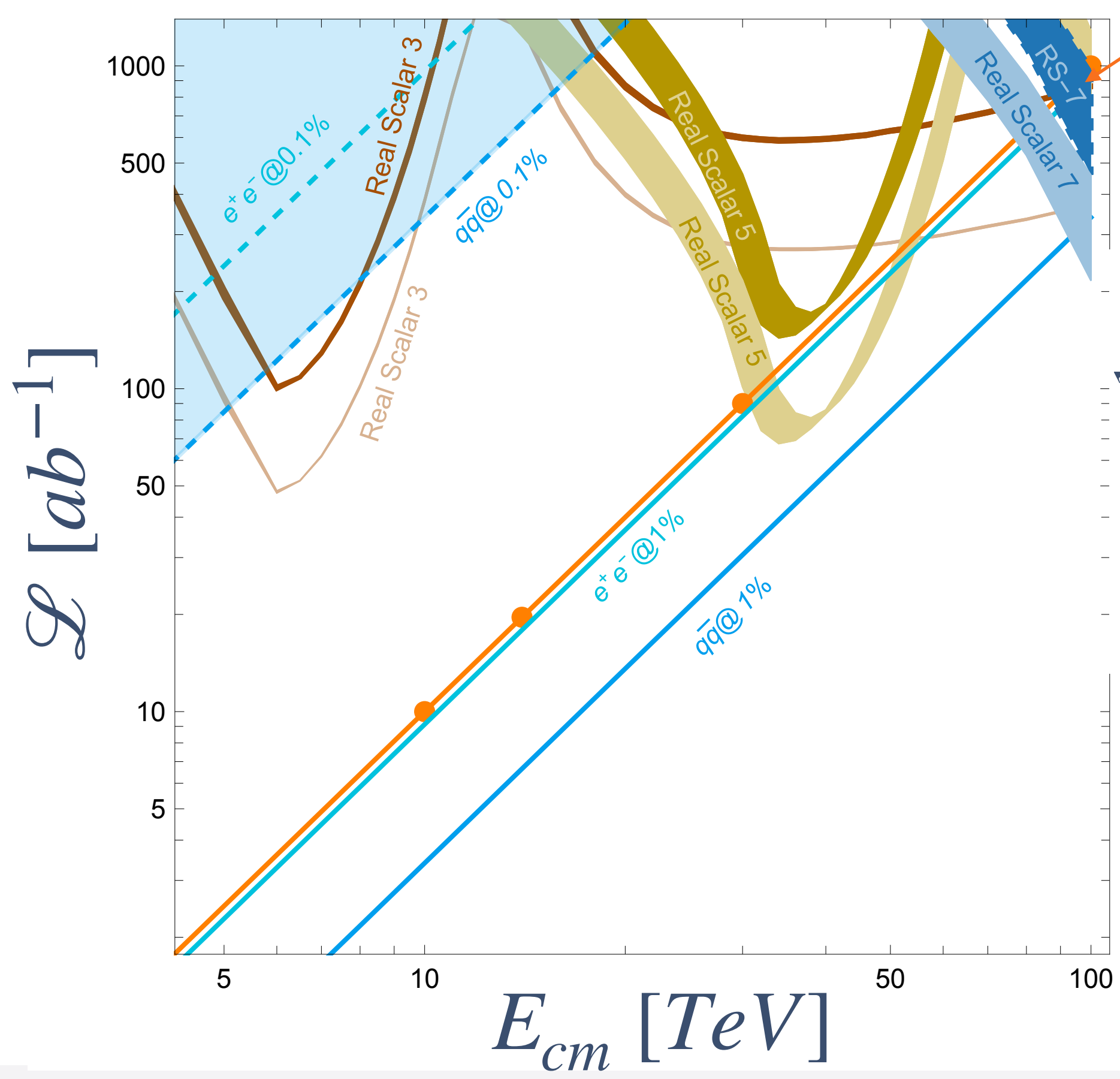
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

up to 10+ TeV

$$\mathcal{L} = 10 \text{ ab}^{-1} \cdot (E_{com}/10 \text{ TeV})^2$$



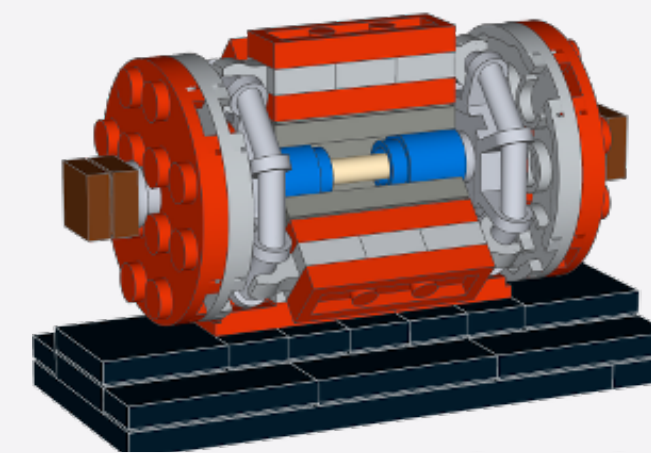
- $\left(4, \frac{1}{2}\right)$ Dirac
- $(3, 0)$ Majorana
- $(3, \epsilon)$ Dirac
- $\left(2, \frac{1}{2}\right)$ Dirac

$\ell^+ \ell^-$ 10 TeV 10 ab^{-1}

$\ell^+ \ell^-$ 3 TeV 1 ab^{-1}

VIRTUAL* PRODUCTION

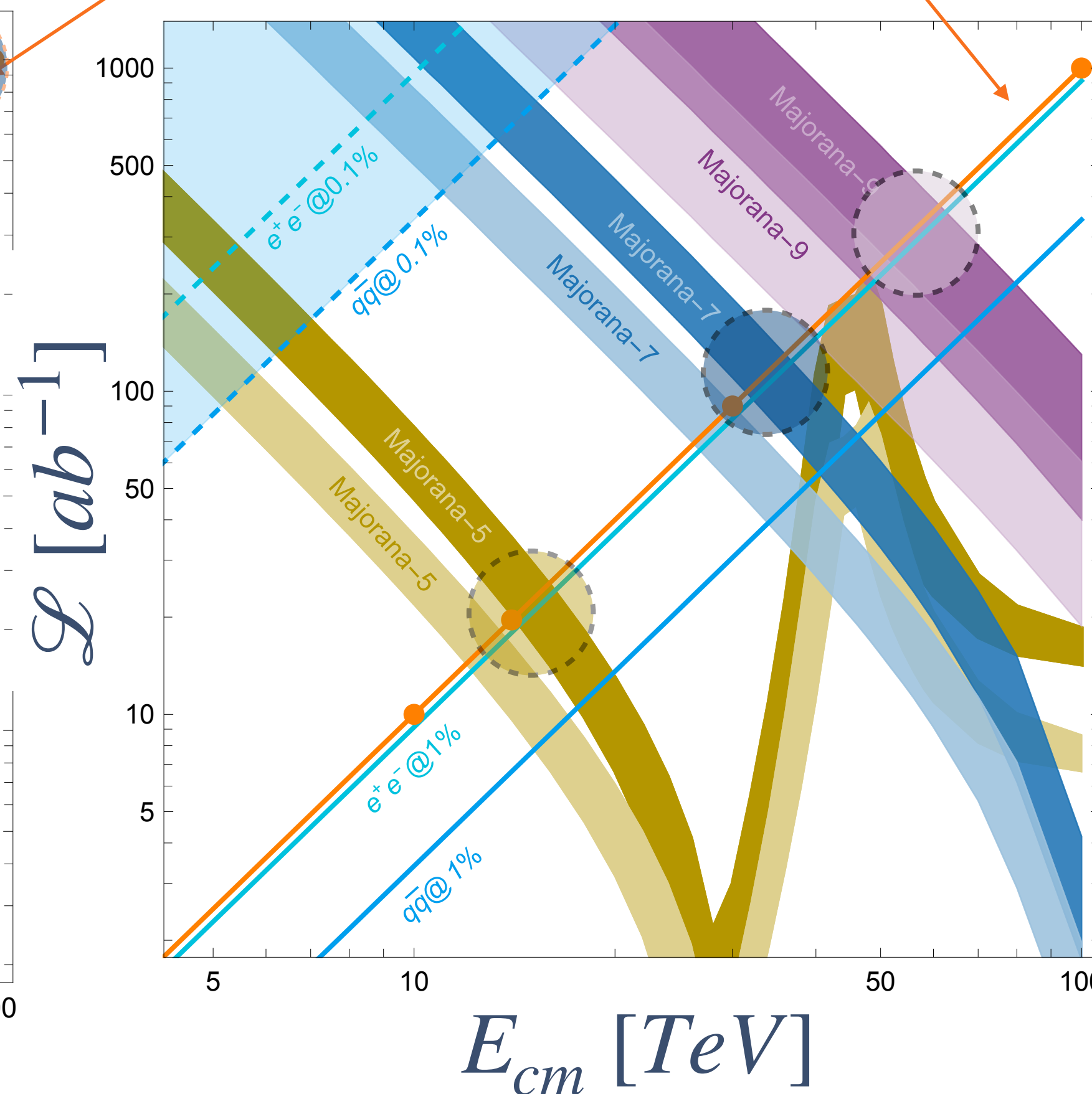
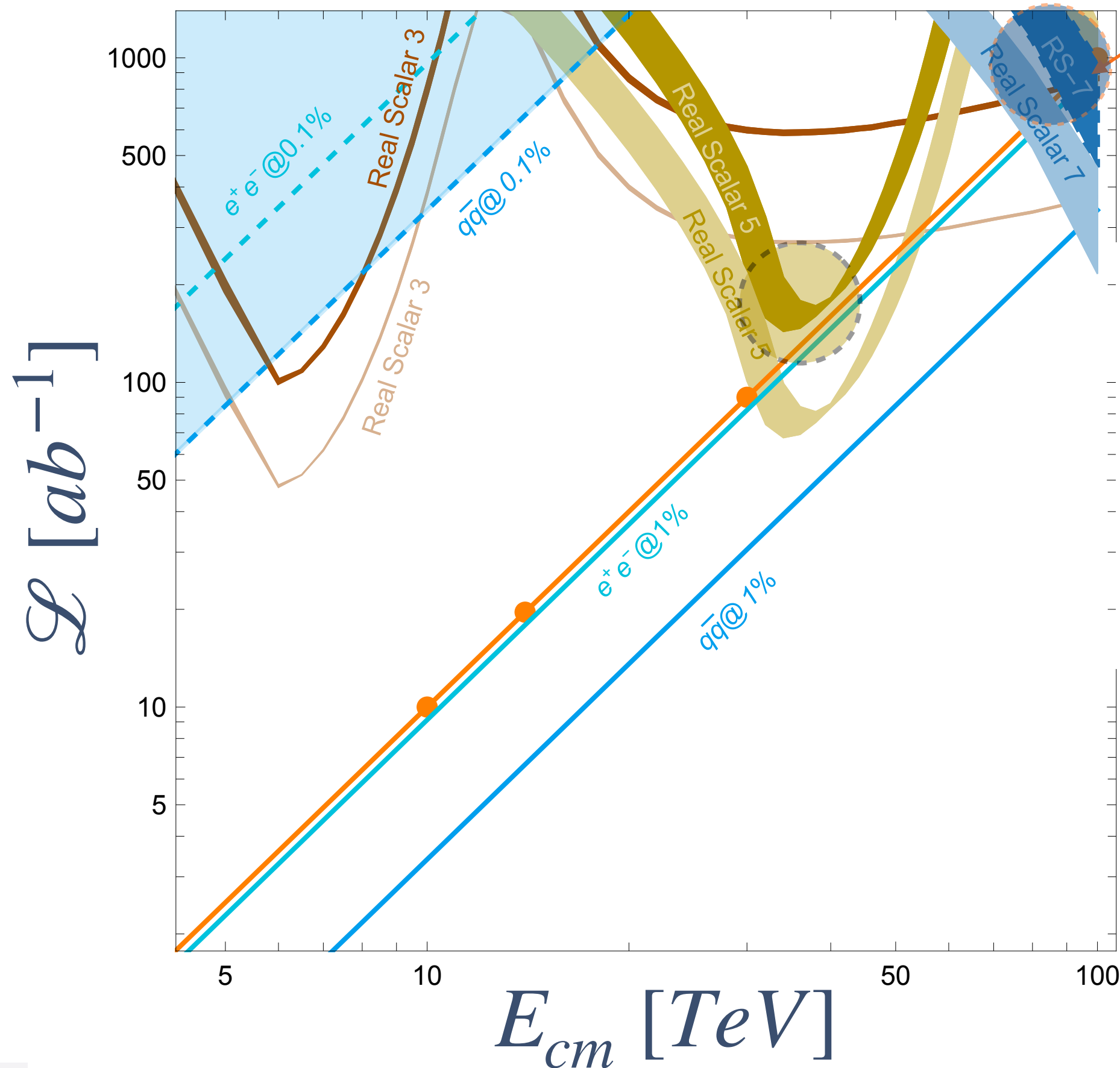
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

up to 10+ TeV

$$\mathcal{L} = 10 \text{ ab}^{-1} \cdot (E_{com}/10 \text{ TeV})^2$$



$(7,0)_{Majorana}$

$(7, \epsilon)_{Dirac}$

$(5,0)_{Majorana}$

$(5, \epsilon)_{Dirac}$

$(4, \frac{1}{2})_{Dirac}$

$(3,0)_{Majorana}$

$(3, \epsilon)_{Dirac}$

$(2, \frac{1}{2})_{Dirac}$

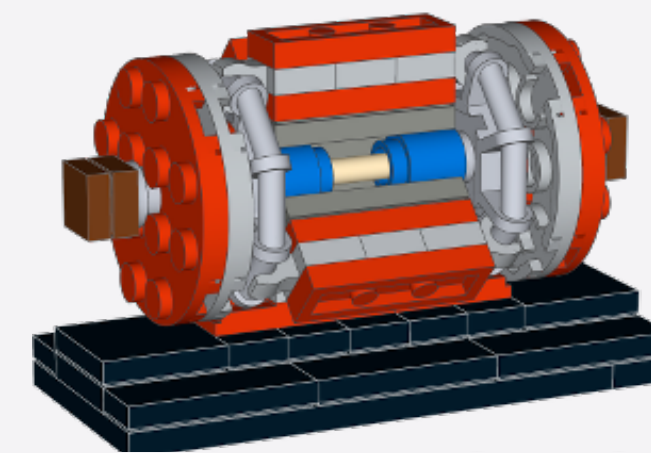
$\ell^+ \ell^-$ 10+ TeV 10+ ab^{-1}

$\ell^+ \ell^-$ 10 TeV 10 ab^{-1}

$\ell^+ \ell^-$ 3 TeV 1 ab^{-1}

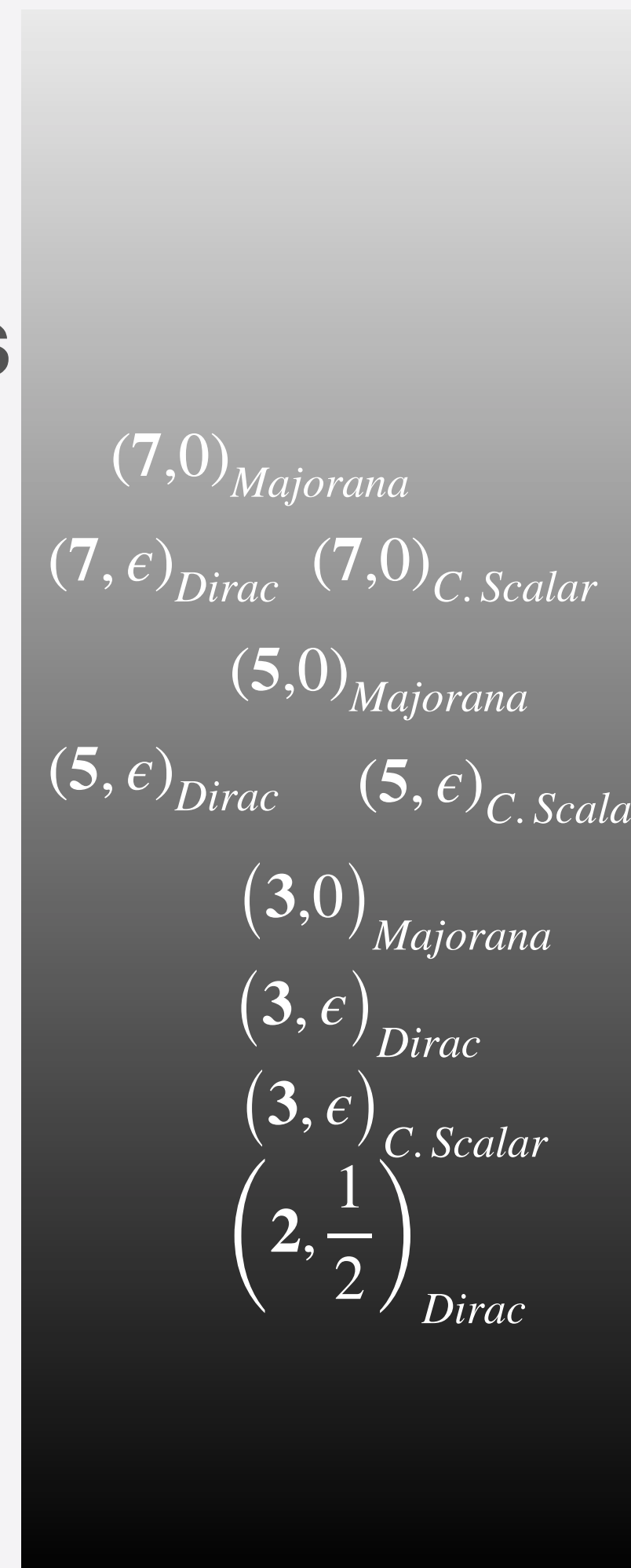
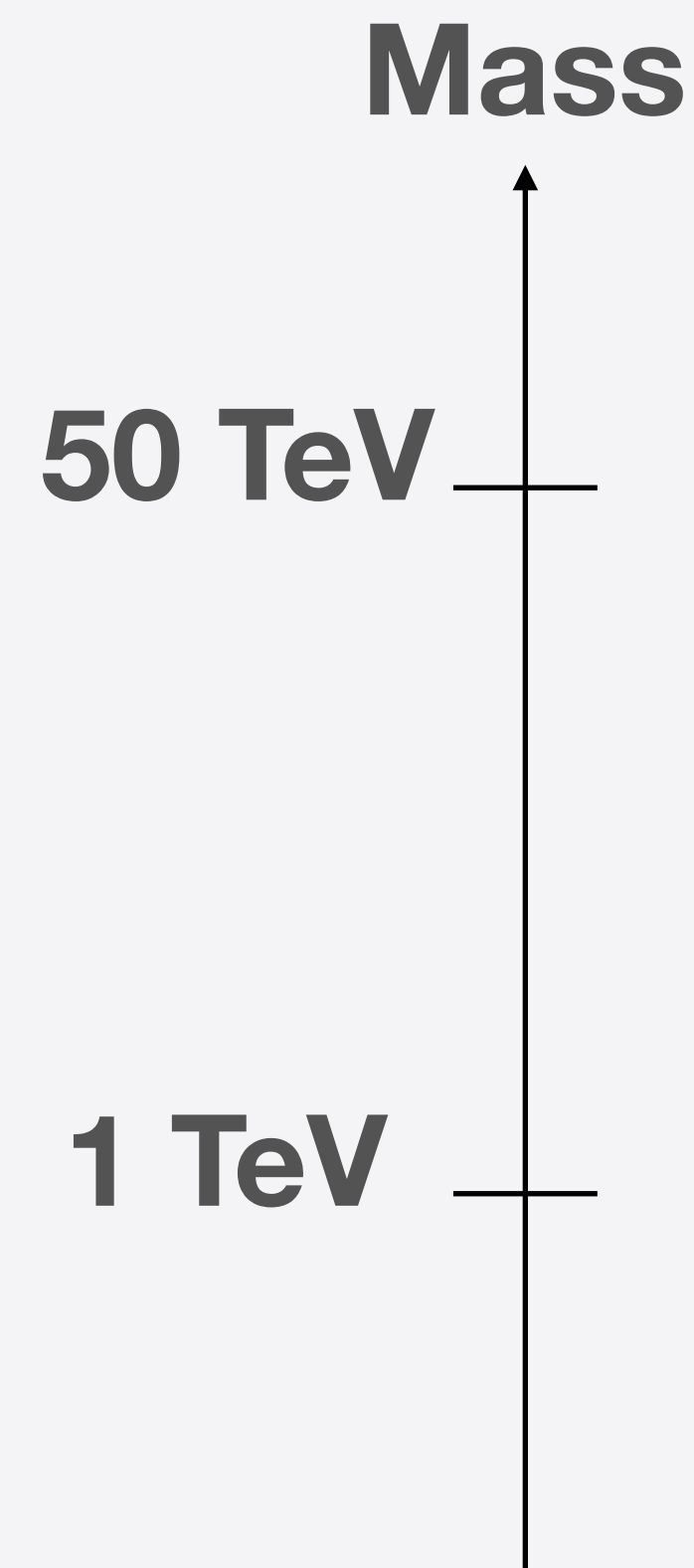
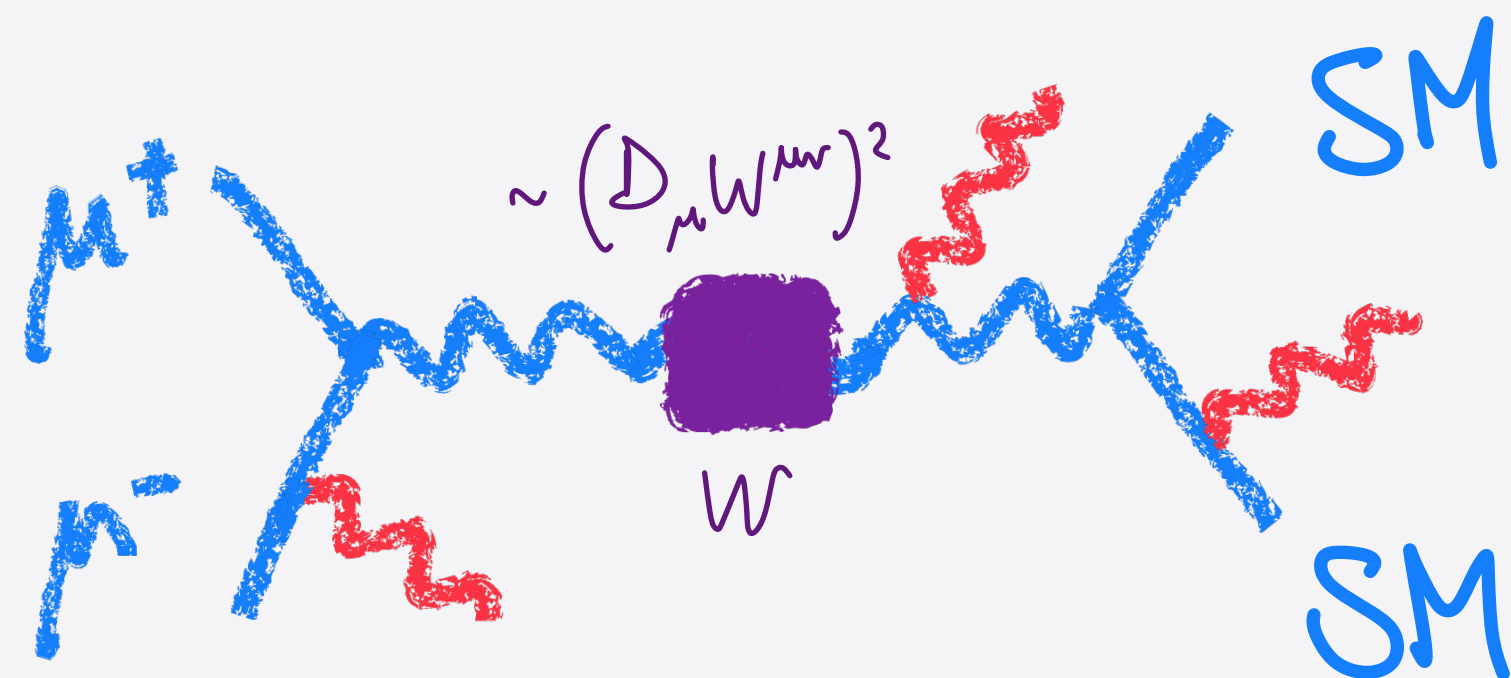
VIRTUAL* PRODUCTION

$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

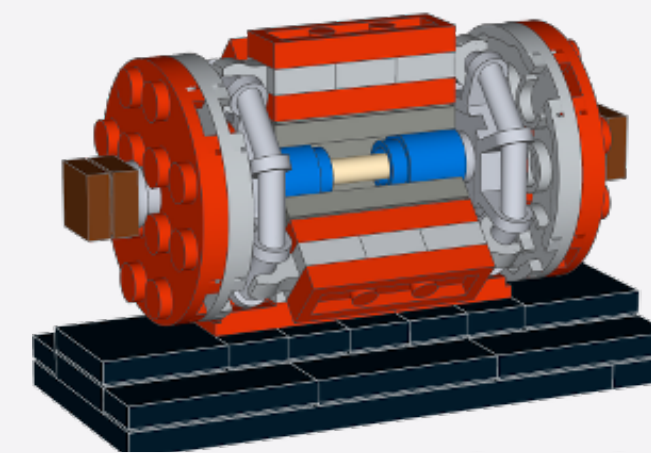
up to 10+ TeV



“WIMP” Dark Matter

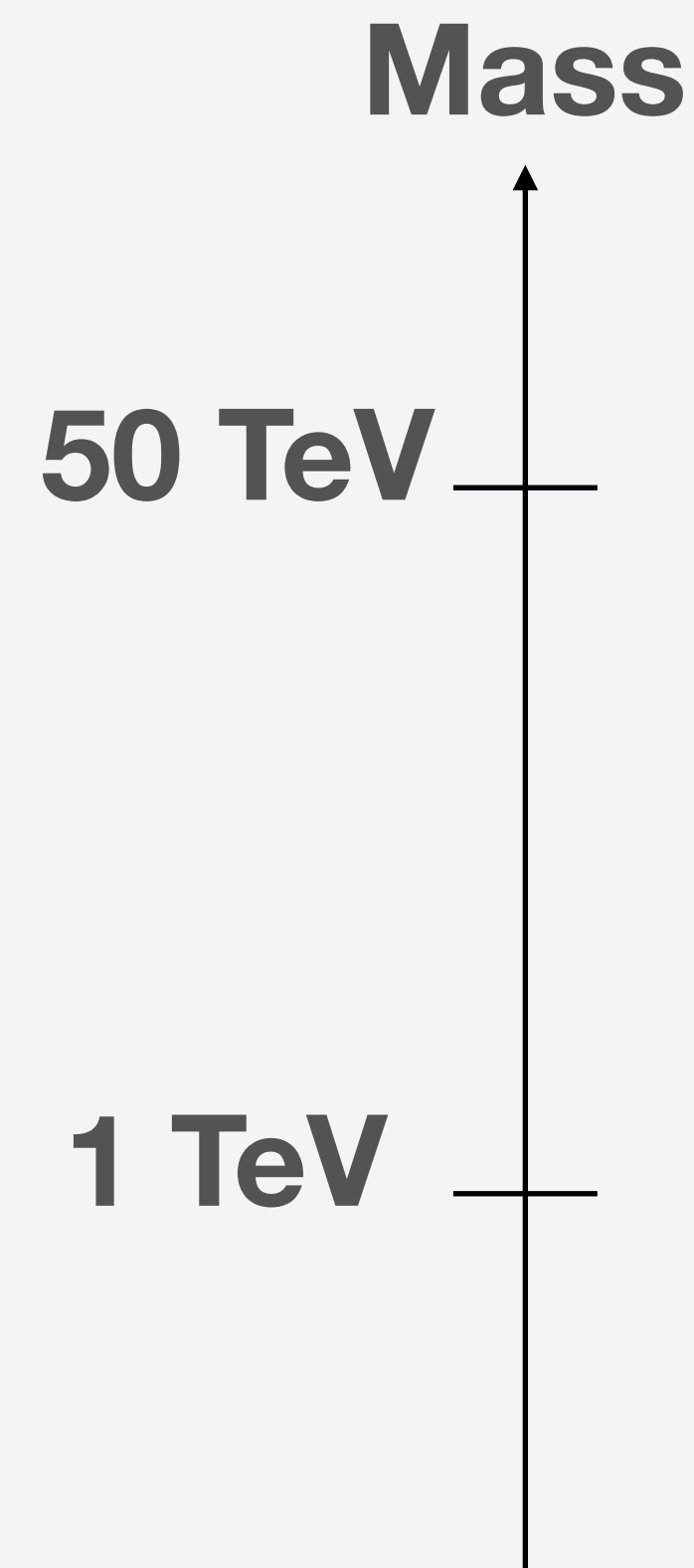
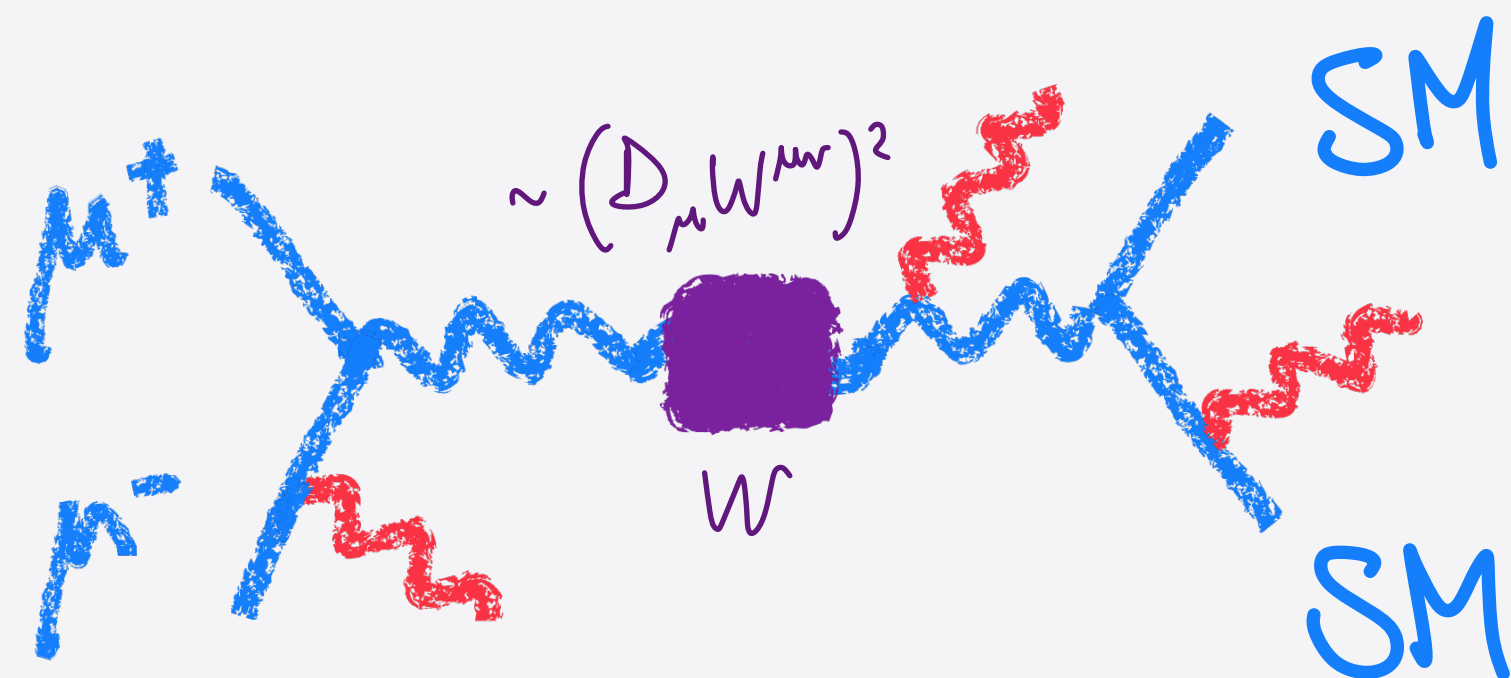
VIRTUAL* PRODUCTION

$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

up to 10+ TeV



$\ell^+ \ell^-$ 10 TeV 10 ab^{-1}

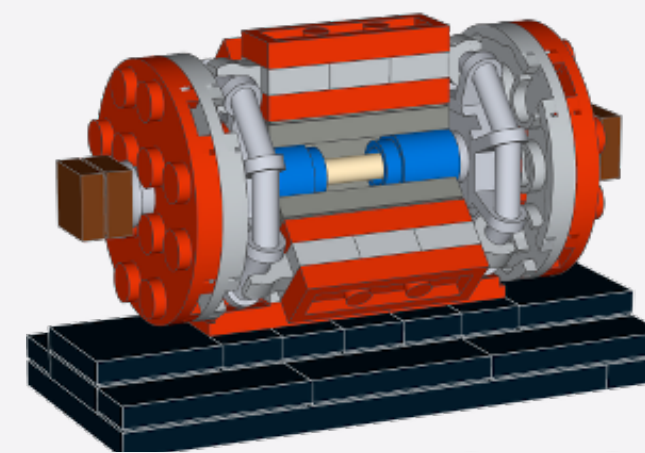
SUSY
WINO

SUSY
HIGGSINO

“WIMP” Dark Matter

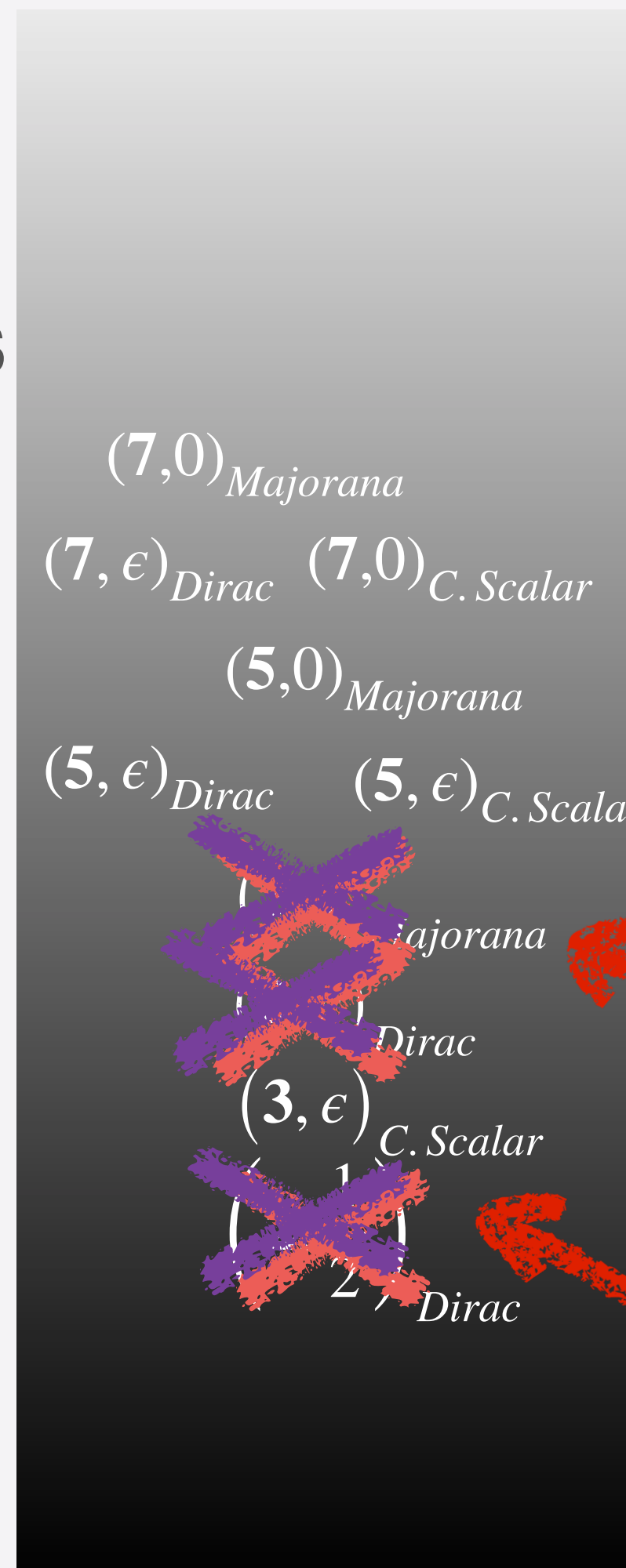
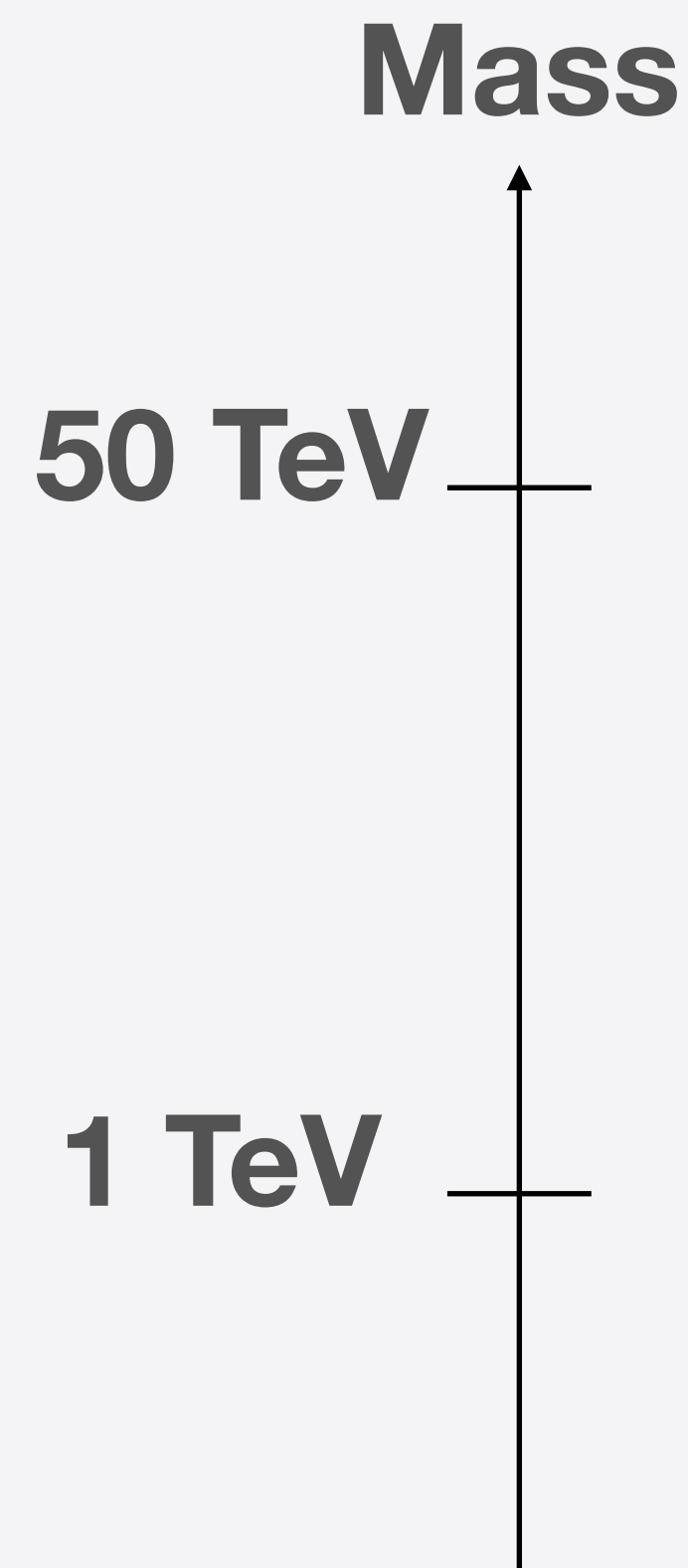
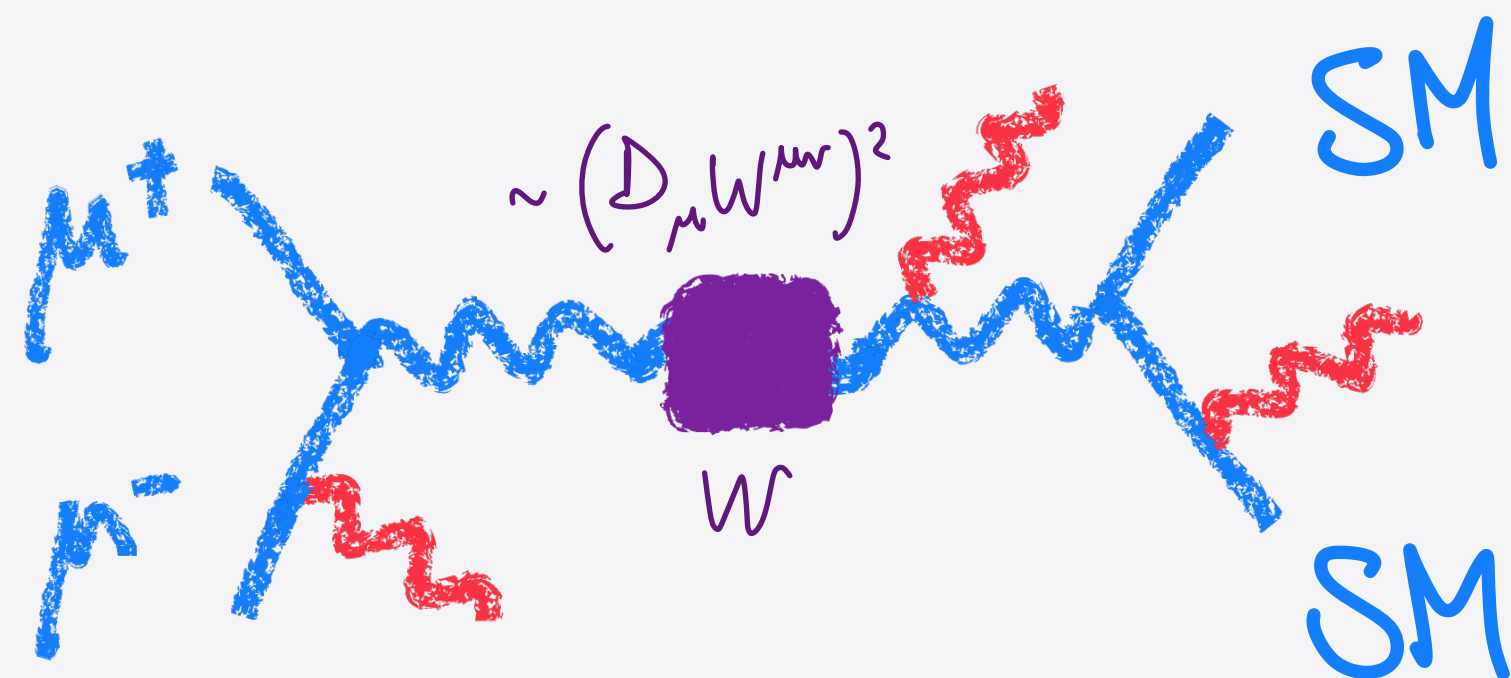
VIRTUAL* PRODUCTION

$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

up to 10+ TeV



$\ell^+ \ell^-$ 10 TeV 10 ab^{-1}
 pp 100 TeV 30 ab^{-1}

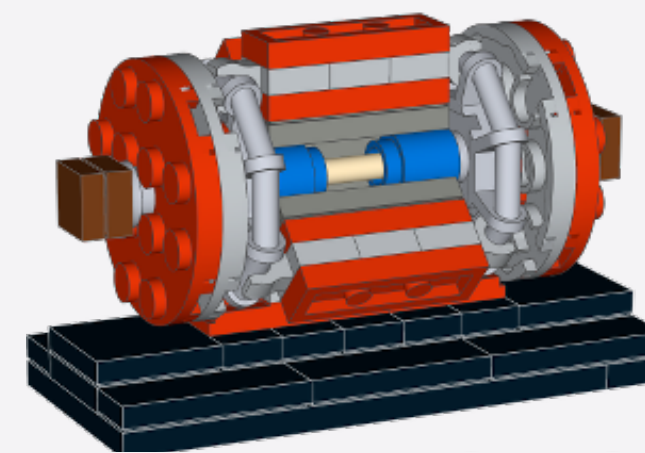
SUSY
WINO

SUSY
HIGGSINO

“WIMP” Dark Matter

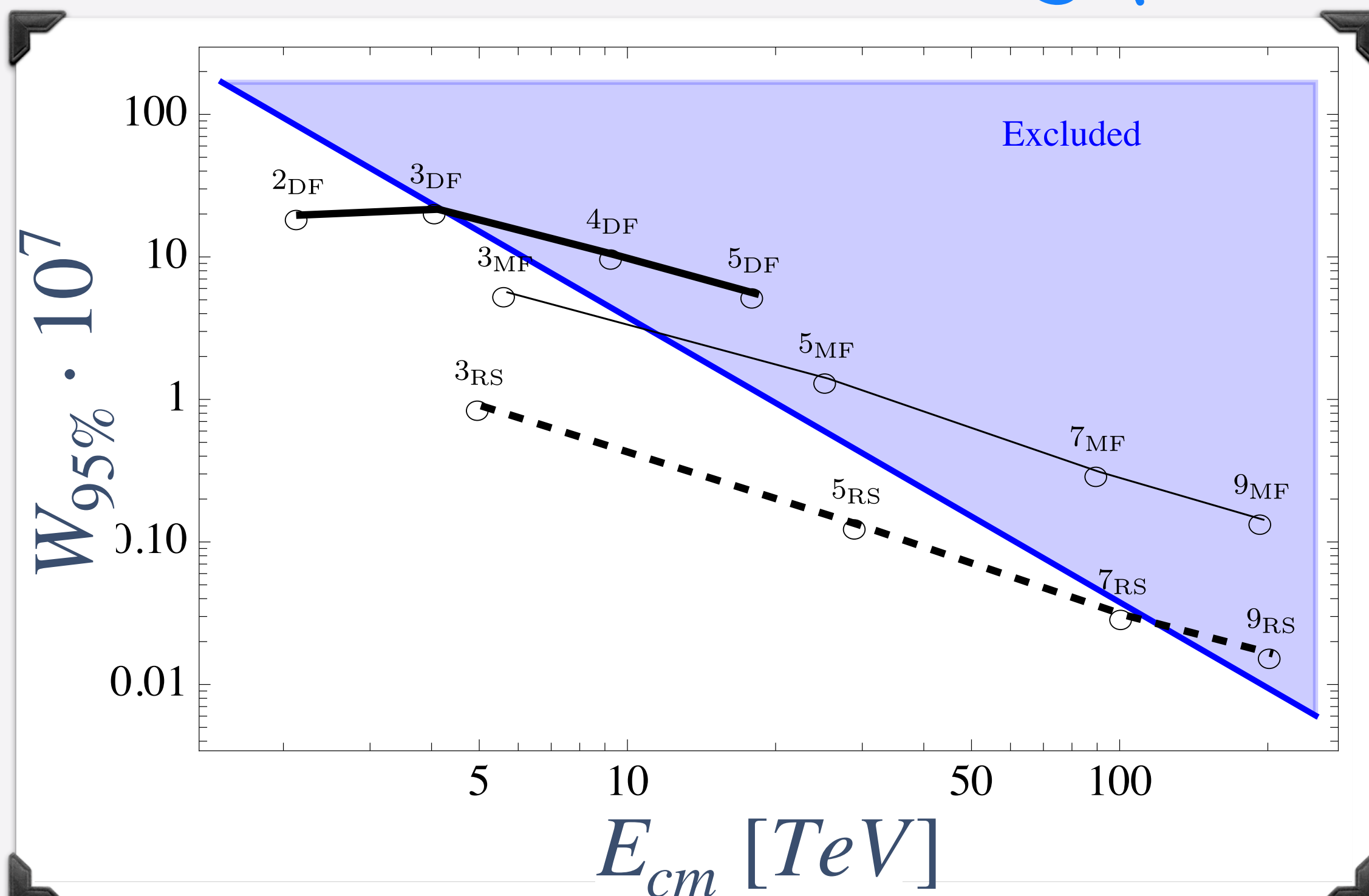
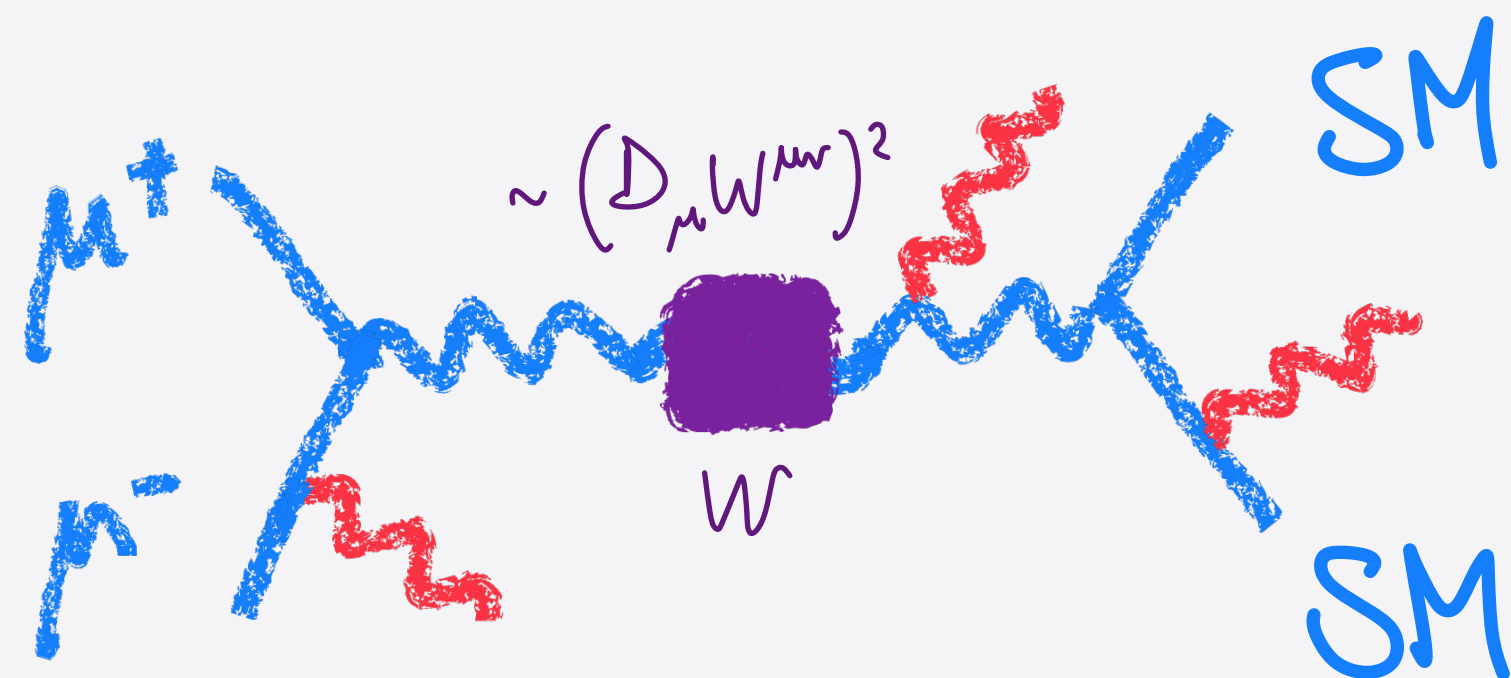
VIRTUAL* PRODUCTION

$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

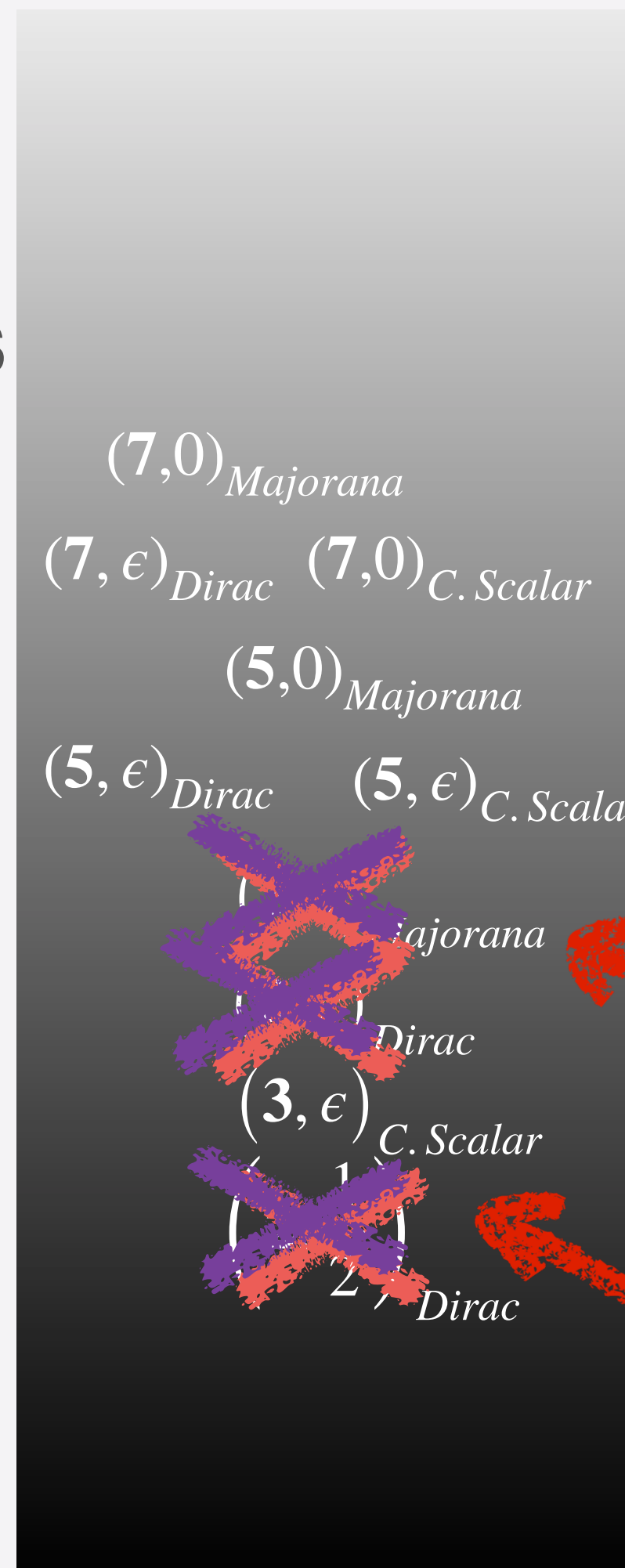
up to 10+ TeV



Mass

50 TeV

1 TeV



$\ell^+ \ell^-$ 10 TeV 10 ab^{-1}
 pp 100 TeV 30 ab^{-1}

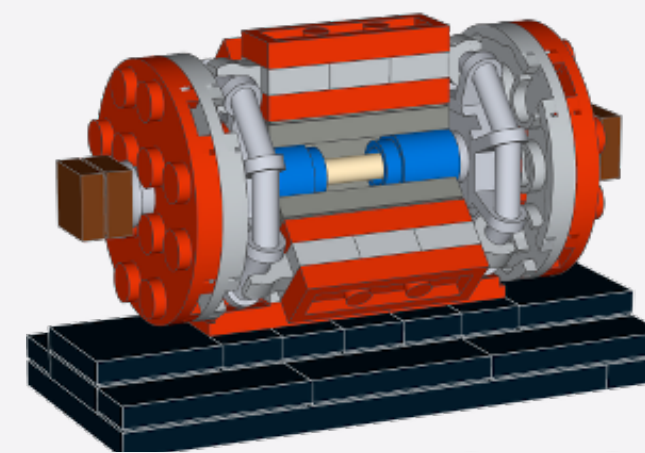
SUSY
WINO

SUSY
HIGGSINO

“WIMP” Dark Matter

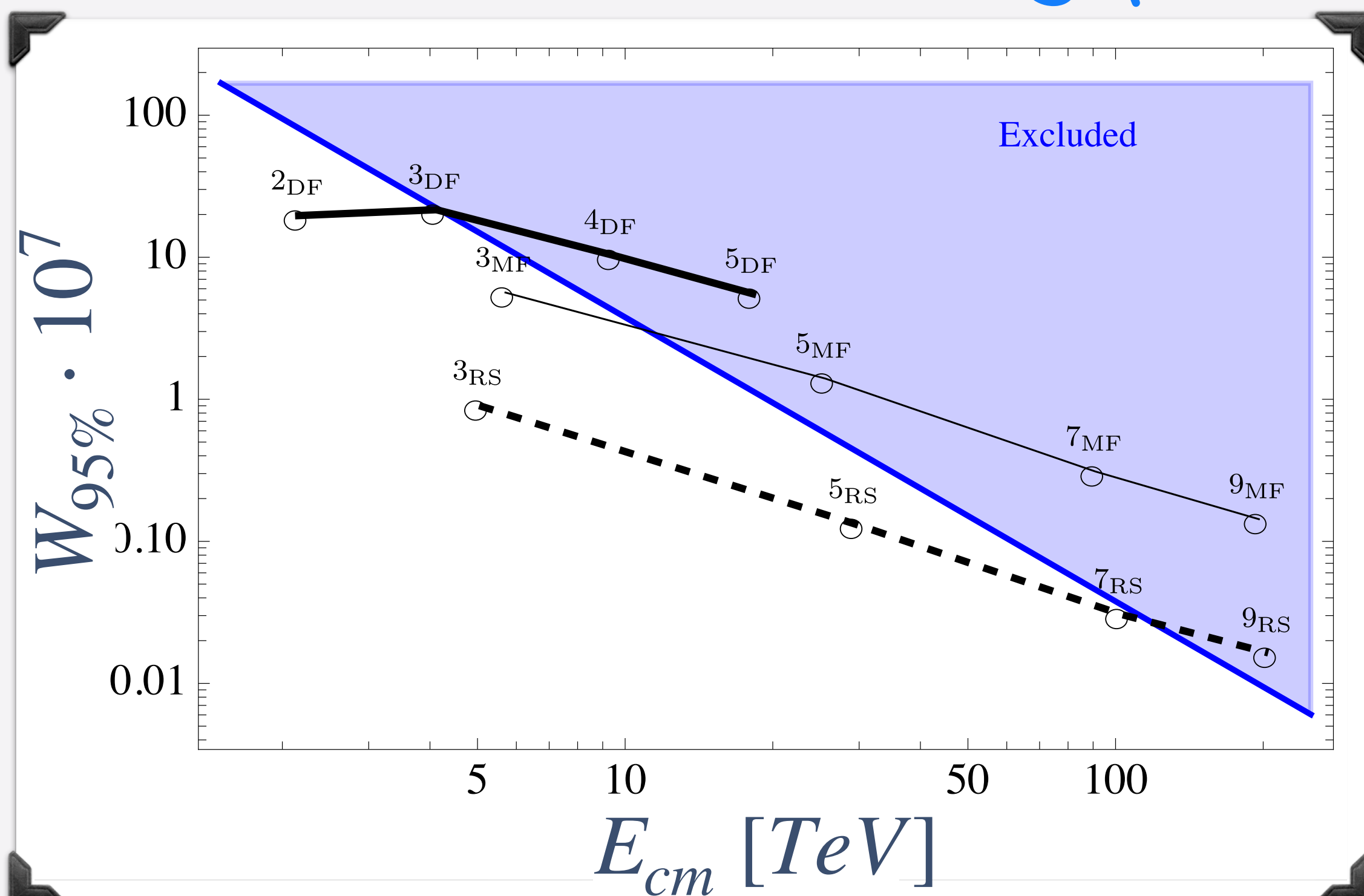
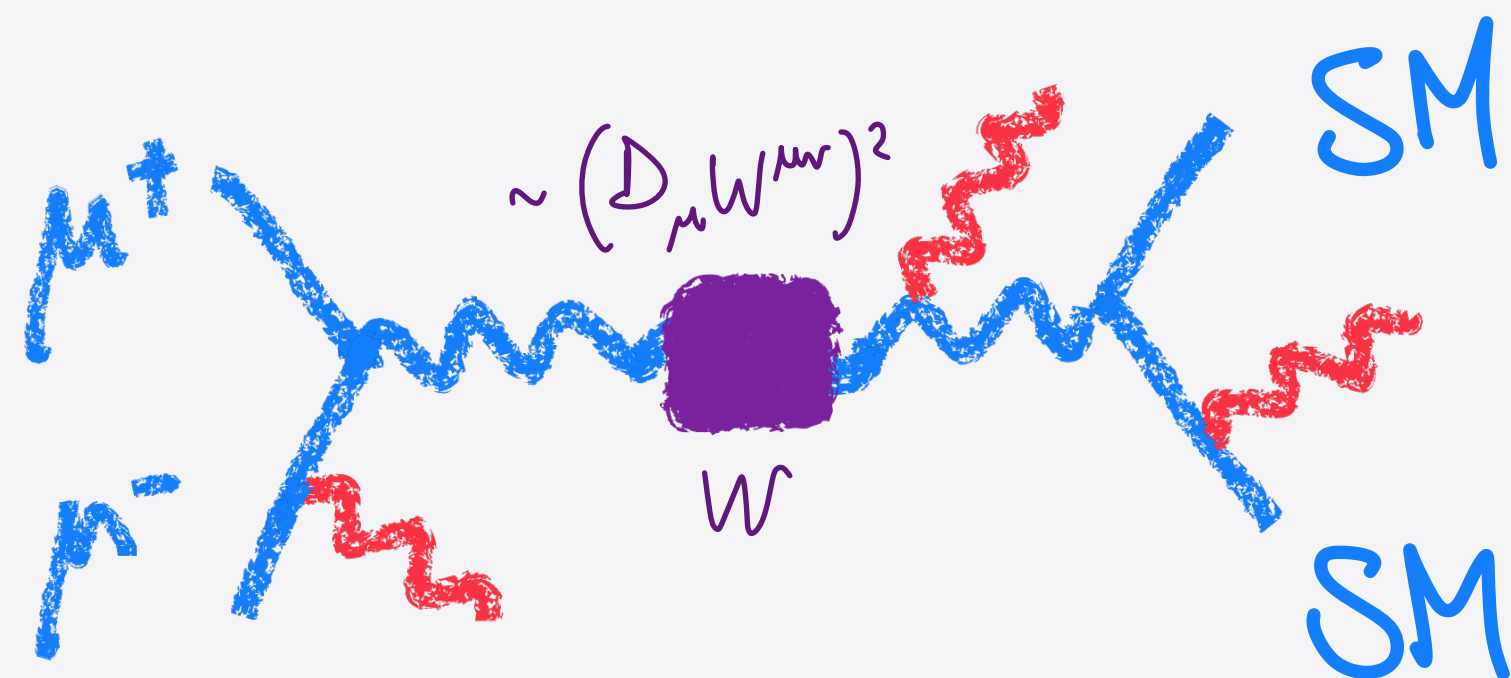
VIRTUAL* PRODUCTION

$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

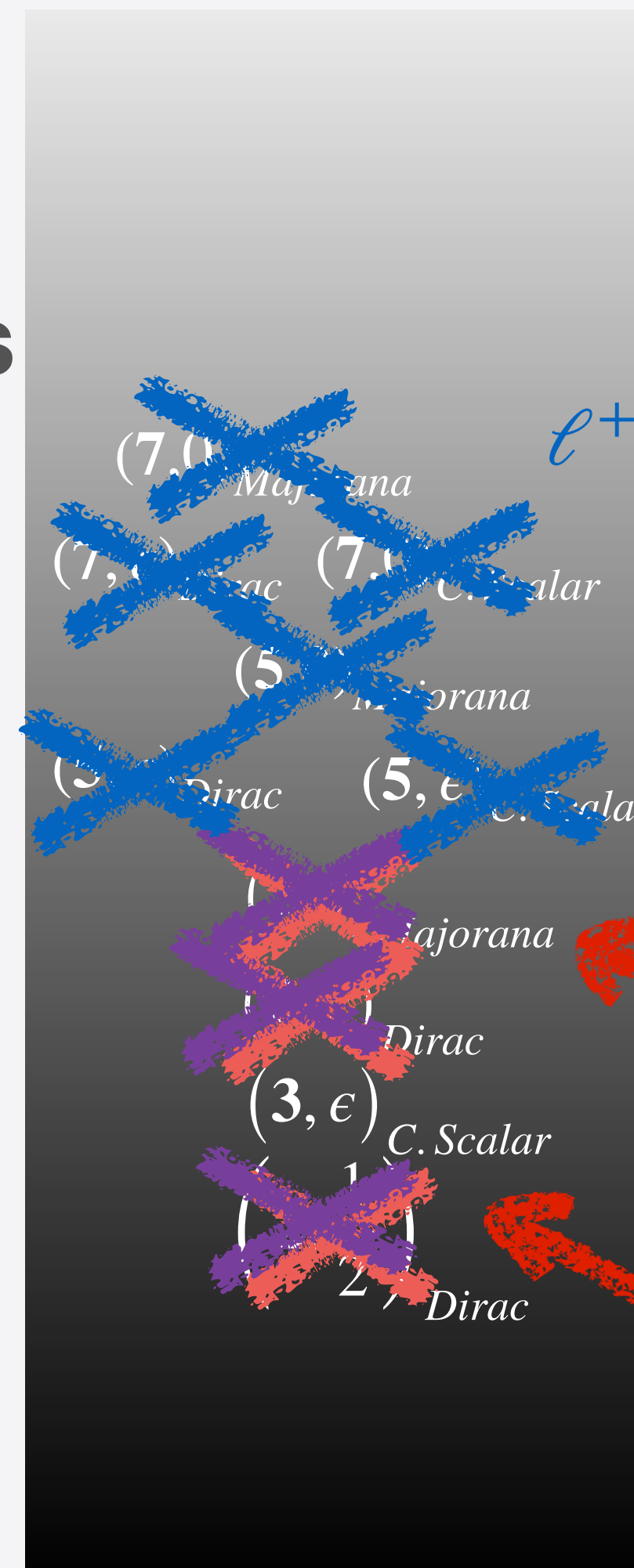
up to 10+ TeV



Mass

50 TeV

1 TeV



$\ell^+ \ell^-$ 10+ TeV 10+ ab^{-1}

$\ell^+ \ell^-$ 10 TeV 10 ab^{-1}

pp 100 TeV 30 ab^{-1}

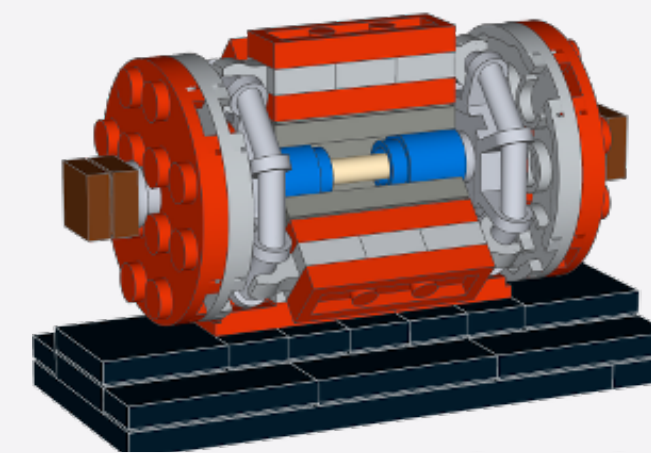
SUSY WINO

SUSY HIGGSINO

“WIMP” Dark Matter

VIRTUAL* PRODUCTION

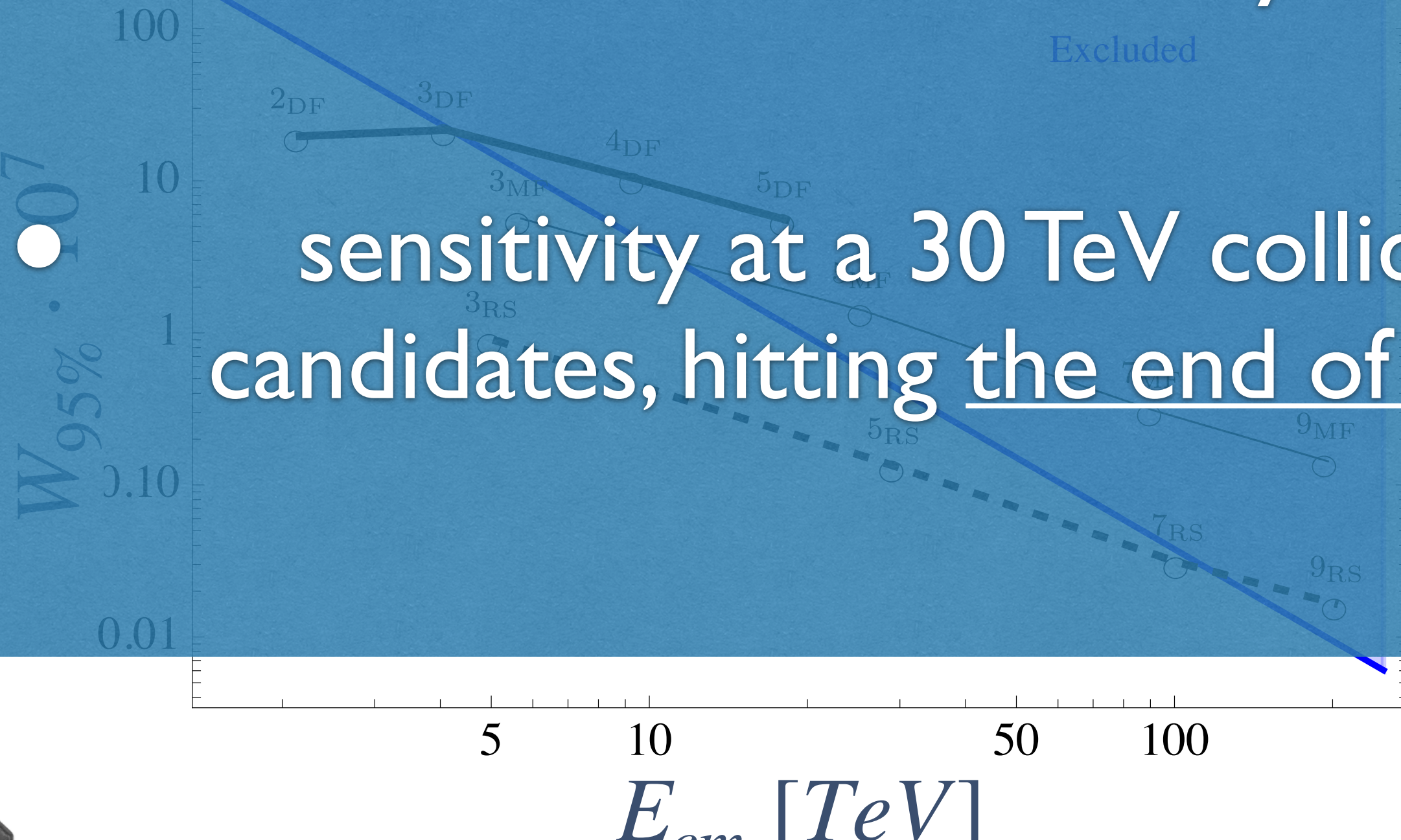
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



2040s

up to 10+ TeV

- muon collider provides a systematic way to probe heavy dark matter candidates even beyond the kinematic reach of the machine



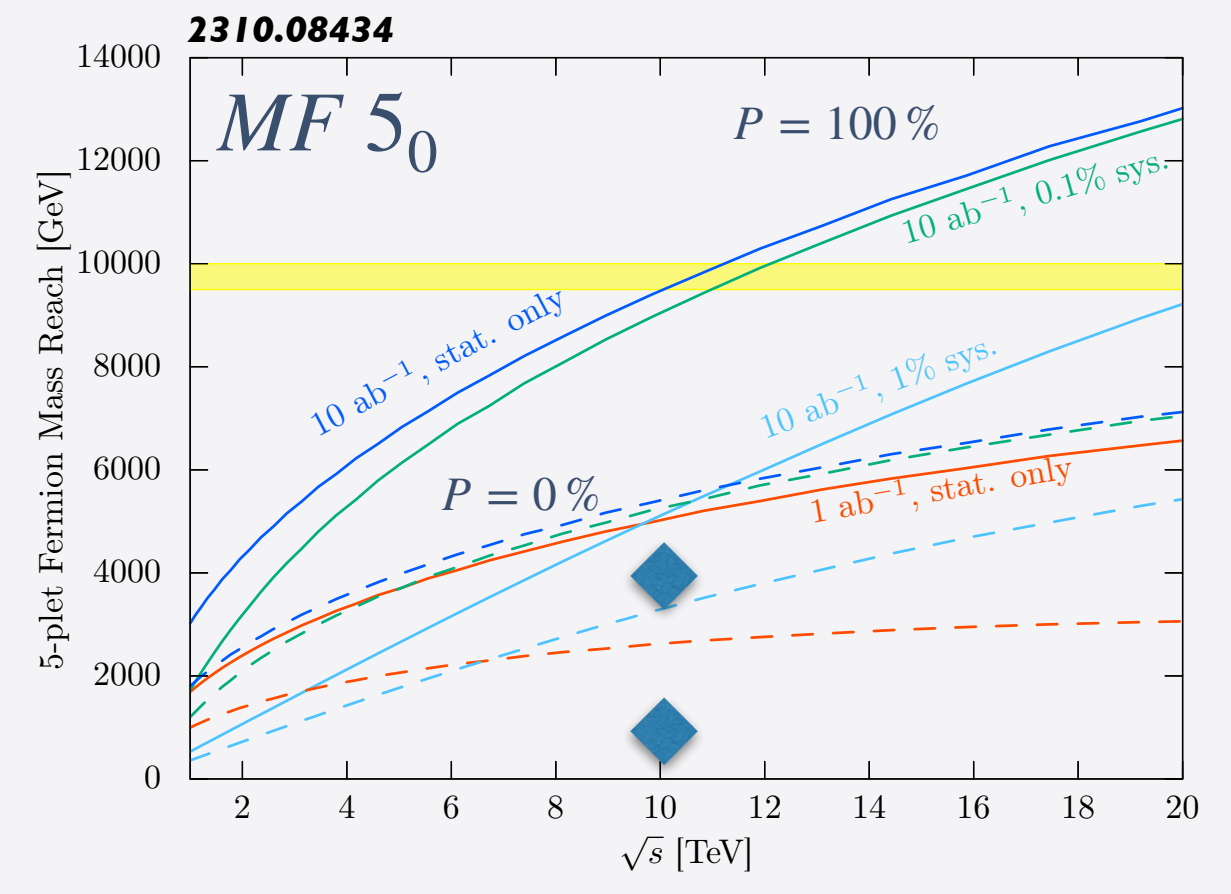
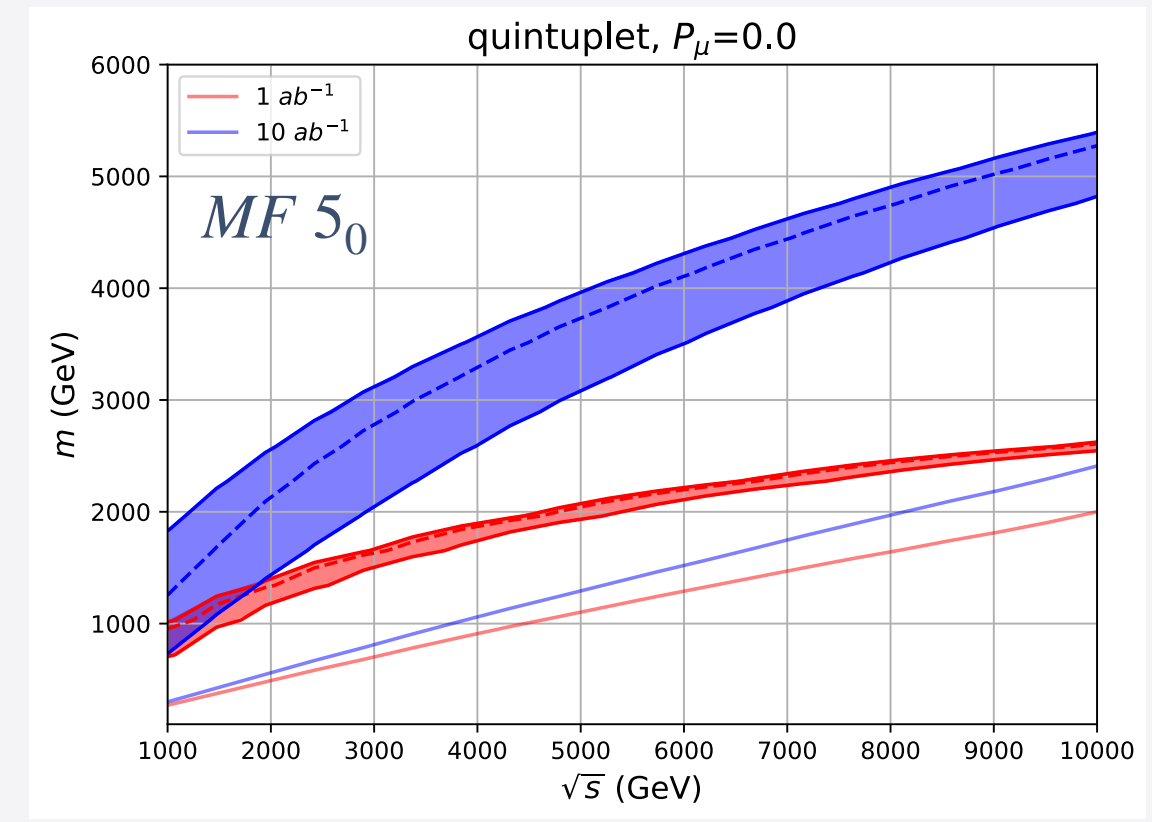
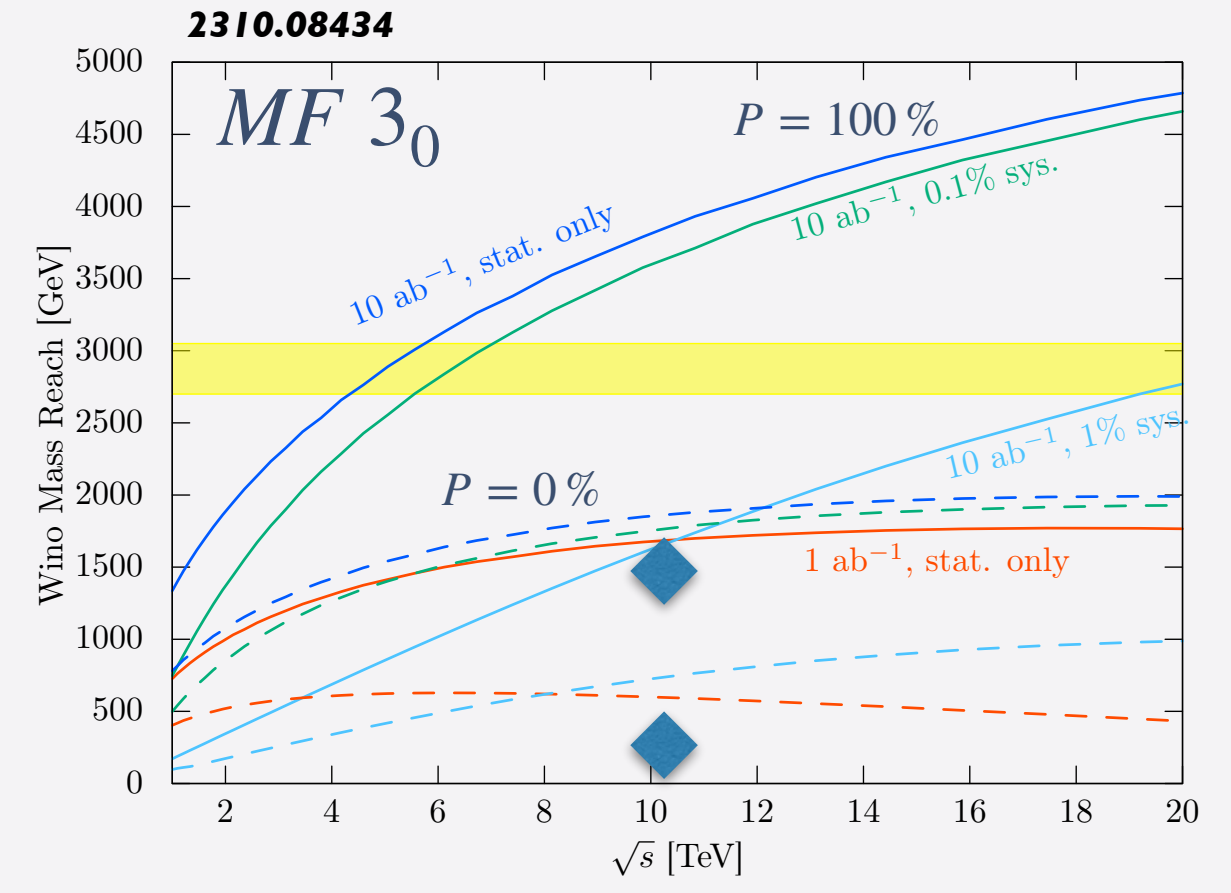
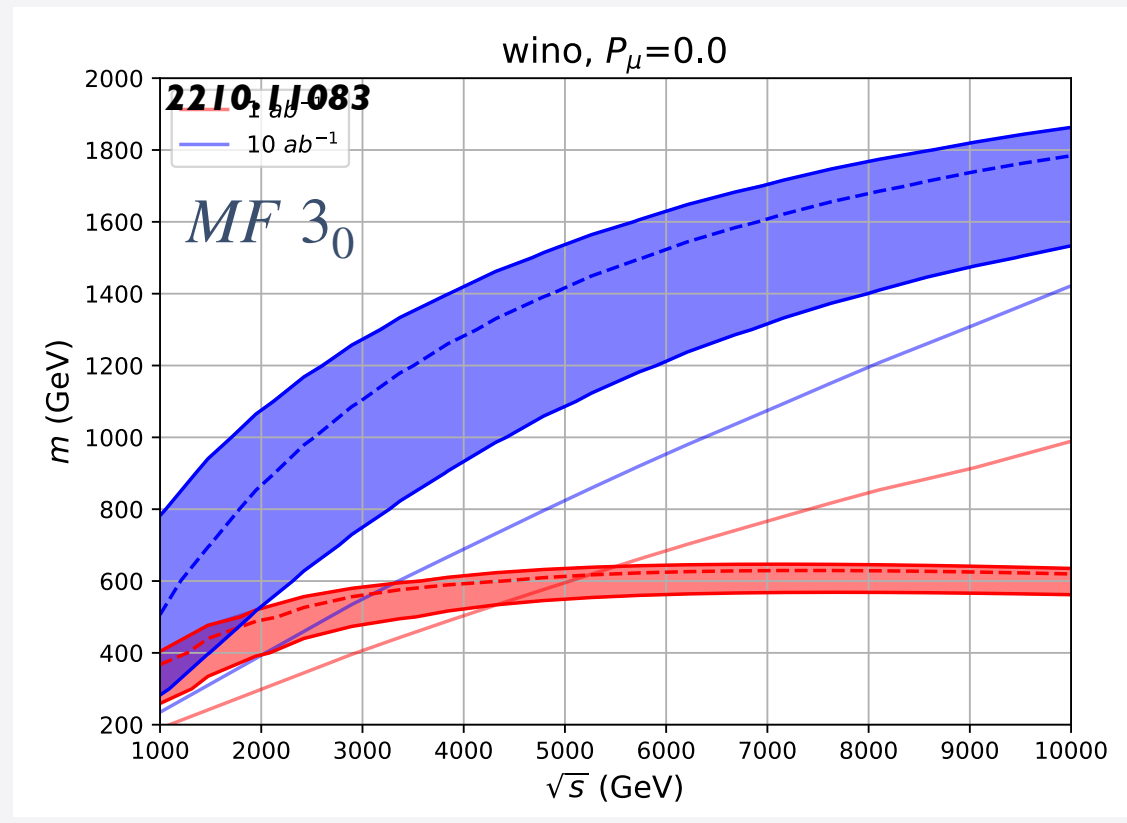
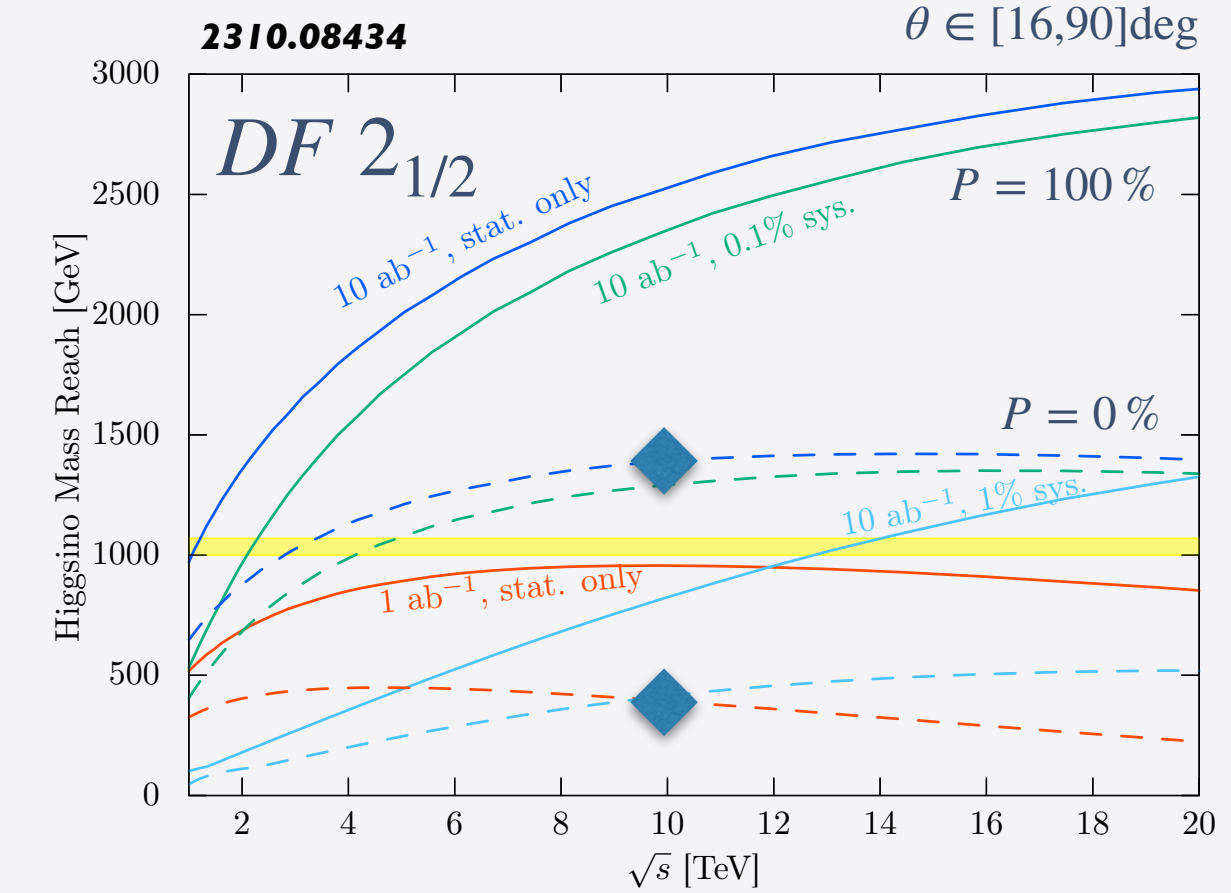
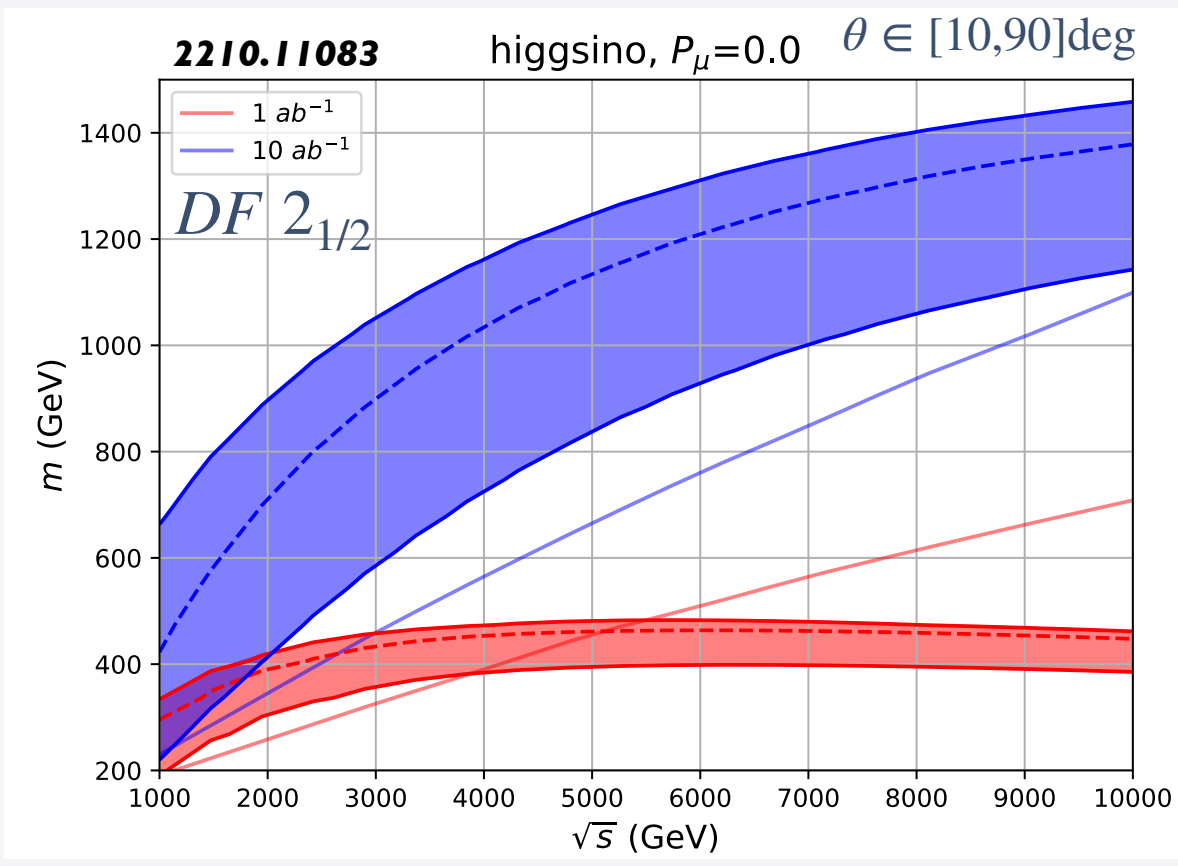
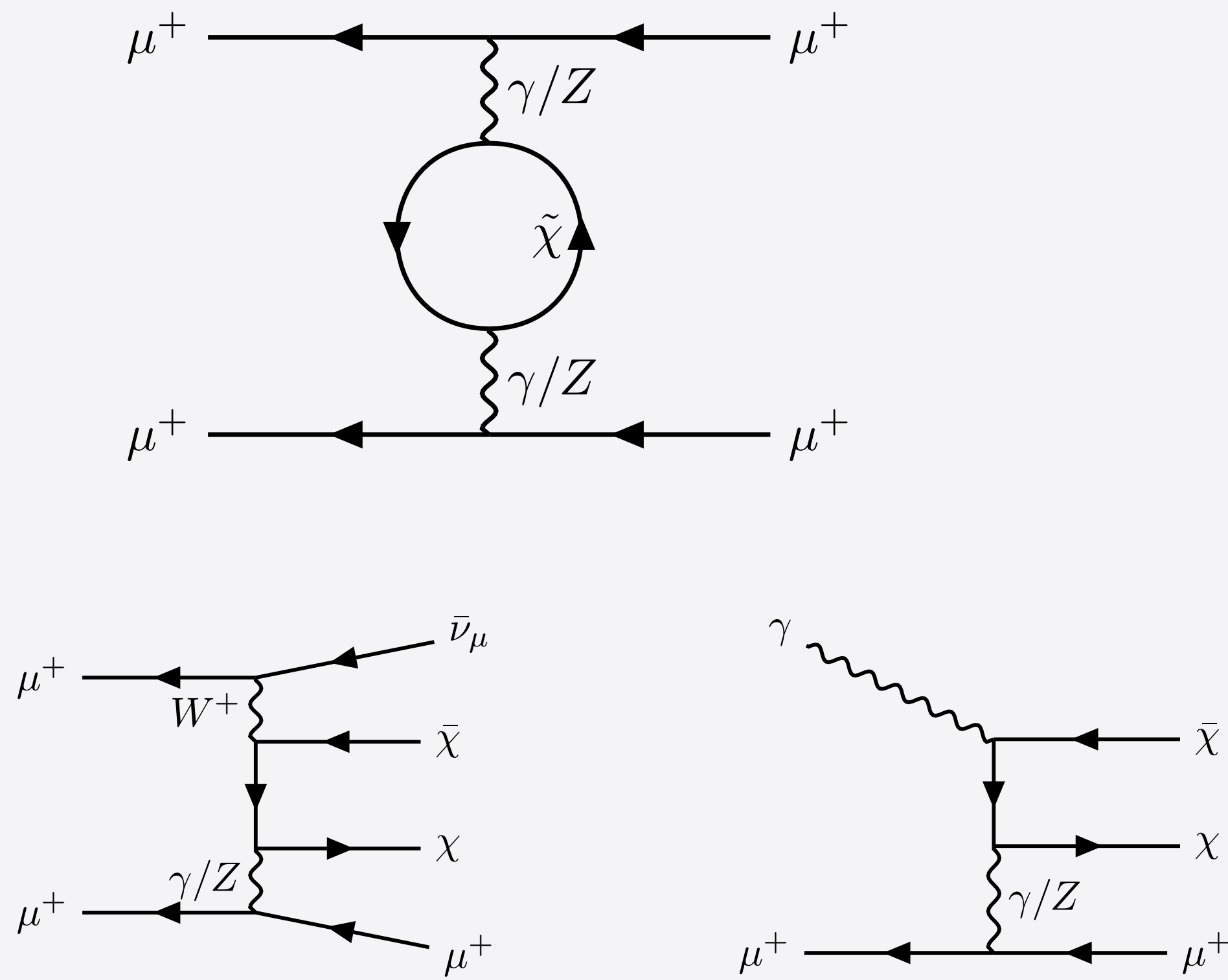
- sensitivity at a 30 TeV collider extends to 50 TeV dark matter candidates, hitting the end of the weakly coupled WIMP catalog(!)

“WIMP” Dark Matter

SUSY
HIGGSINO

VIRTUAL* PRODUCTION

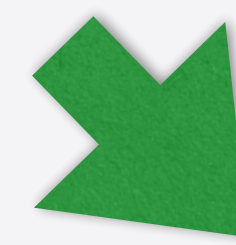
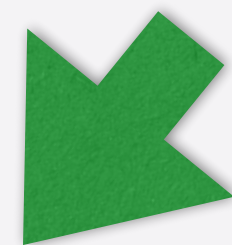
t -channel Ryuichiro's talk



CONCLUSIONS AND OUTLOOK

WIMP dark matter can be challengingly heavy for production at colliders ... still

- We can look for WIMPs in the sky
 - Establishing clear signals from the sky may prove quite hard, due to backgrounds, but are certainly intriguing
 - Signal rates are also subject to uncertainties that can make WIMPs not accessible
- We can try to detect WIMPs from the big-bang
 - Underground ultra-low background experiments can give signals soon, but cannot measure the mass of the WIMP
 - Half or so of the WIMP candidates are easily below the sensitivity of the next generations of Direct Detection experiments



Signals from the sky and from underground laboratories in the next 10-20 years can be a huge motivation for a new collider

Even in absence of signals from the sky and from underground laboratories in the next 10-20 years there is plenty of room left for WIMPs of the most simple kind

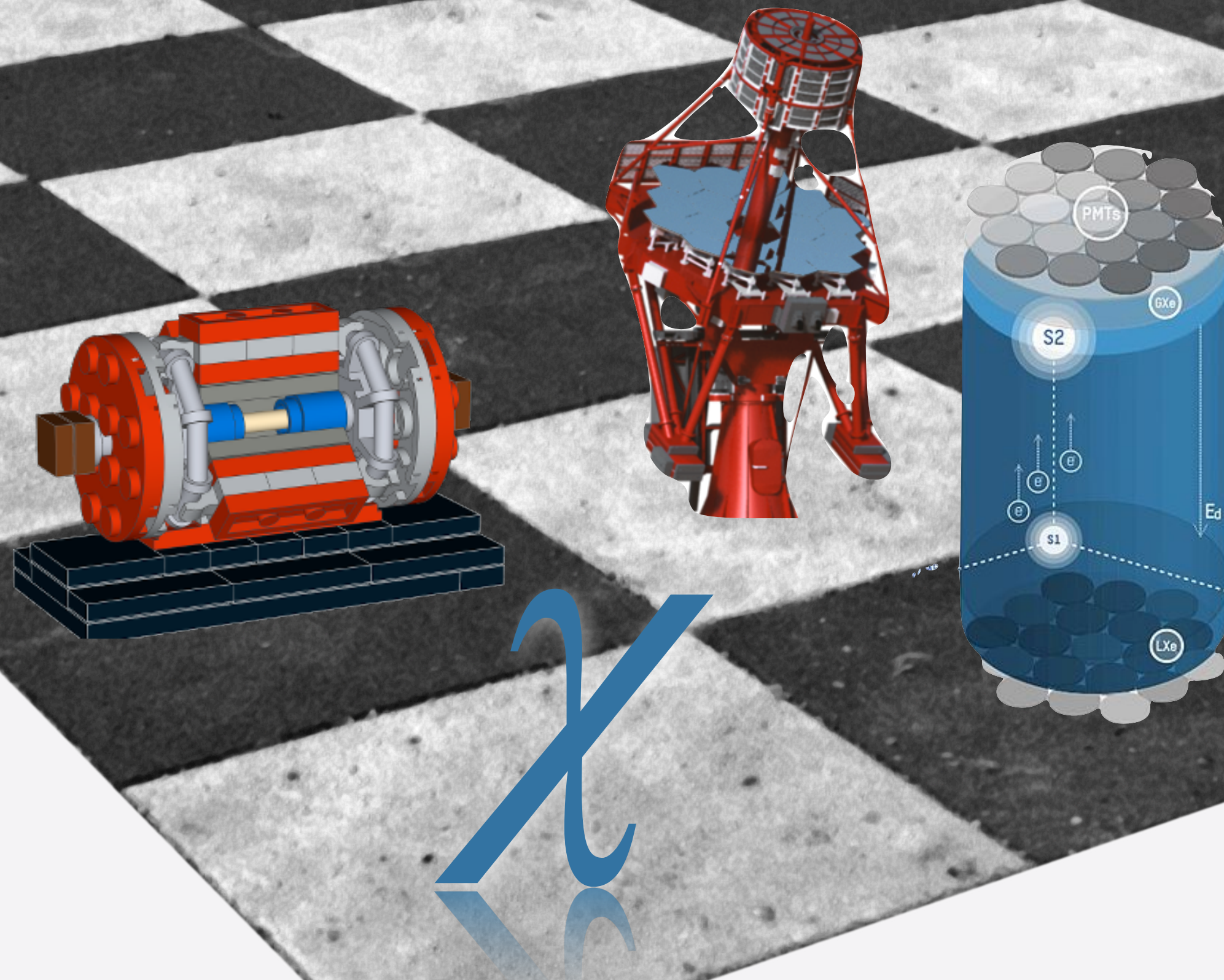
Muon collider can probe it all, up to the perturbative unitarity limit

WIMP DARK MATTER ENDGAME

The 3-10 TeV muon collider can discover Higgsino, Wino and light minimal dark matter ($n=2,3,4$) up to their thermal mass for 100% of Ω_{DM}

$E_{cm} > 10$ TeV is conceivable thanks to the muon beams. Heavier MDM candidates ($n=5,7$) up to their thermal mass for 100% of Ω_{DM} are in reach

In conjunction with direct and indirect detection experiments we have a path forward for the complete and definitive exploration of the idea of WIMPs as Dark Matter



Thank you!

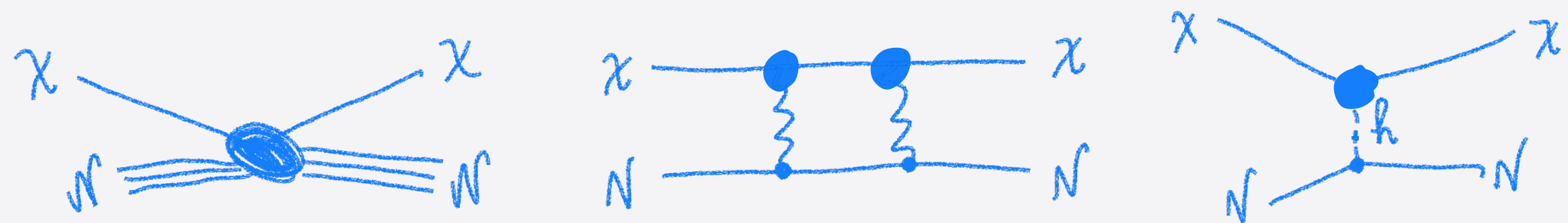
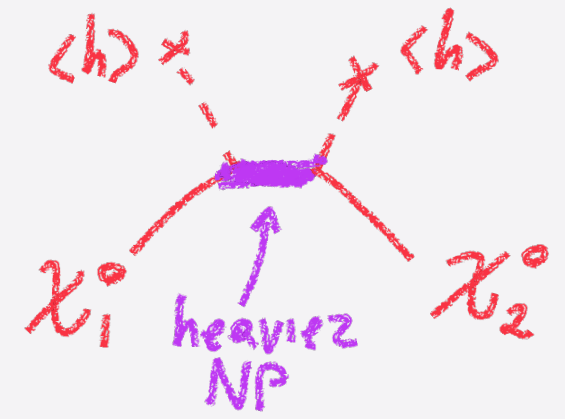
DM spin	EW n-plet	M_χ (TeV)	$\Lambda_{\text{Landau}}/M_\chi$	$(\sigma v)_{\text{tot}}^{J=0}/(\sigma v)_{\text{max}}^{J=0}$	ΔM_0 [MeV]	$\Lambda_{\text{UV}}^{\text{max}}(\Delta M_0^{\text{min}})/M_\chi$	ΔM_- [MeV]
Complex scalar	2	0.58 ± 0.01	$> M_{\text{Pl}}$	-	$0.22 - 4.6 \times 10^4$	-	4.2 - 9600
	4	4.98 ± 0.05	$> M_{\text{Pl}}$	0.004	$0.22 - 10^4$	-	3.2 - 2000
	6	34.9 ± 0.5	$\simeq 6 \times 10^{13}$	0.016	0.54 - 2300	-	280 - 660
	8	88 ± 2	2×10^4	0.12	$0.89 - 1.2 \times 10^3$	-	324 - 507
	10	167 ± 4	20	0.45	1.27 - 800	-	340 - 450
Dirac fermion	2	1.08 ± 0.01	$> M_{\text{Pl}}$	-	0.22 - 5000	2×10^5	4.8 - 7800
	4	4.8 ± 0.1	$\simeq M_{\text{Pl}}$	0.013	0.21 - 2200	$\times 10^5$	3.6 - 2600
	6	31.7 ± 0.5	2×10^4	0.057	0.51 - 510	$\times 10^4$	185 - 780
	8	82 ± 2	14	0.37	0.86 - 800	3000	290 - 550

DM spin	EW n-plet	M_χ (TeV)	$(\sigma v)_{\text{tot}}^{J=0}/(\sigma v)_{\text{max}}^{J=0}$	$\Lambda_{\text{Landau}}/M_{\text{DM}}$	$\Lambda_{\text{UV}}/M_{\text{DM}}$
Real scalar	3	2.53 ± 0.01	-	3×10^{37}	$4 \times 10^{24*}$
	5	15.4 ± 0.7	0.002	5×10^{36}	2×10^{24}
	7	54.2 ± 3.1	0.022	2×10^{19}	2×10^{24}
	9	117.8 ± 15.4	0.088	3×10^3	2×10^{24}
	11	199 ± 42	0.25	20	3×10^{24}
	13	338 ± 102	0.6	3.5	3×10^{24}
Majorana fermion	3	2.86 ± 0.01	-	3×10^{37}	$8 \times 10^{12*}$
	5	13.6 ± 0.8	0.003	3×10^{17}	5×10^{12}
	7	48.8 ± 3.3	0.019	1×10^4	4×10^7
	9	113 ± 15	0.07	30	3×10^7
	11	202 ± 43	0.2	6	3×10^7
	13	324.6 ± 94	0.5	2.6	3×10^7

DM spin	n_Y	M_{DM} (TeV)	DM spin	EW n-plet	M_χ (TeV)	DM spin	n_ϵ	M_{DM} (TeV)		
Dirac fermion	$2_{1/2}$	1.08 ± 0.02	Real scalar	3	2.53 ± 0.01	Complex scalar	3	$1.60 \pm 0.01 - 2.4^*$		
	3_1	2.85 ± 0.14		5	15.4 ± 0.7		5	11.3 ± 0.6		
	$4_{1/2}$	4.8 ± 0.3		7	54.2 ± 3.1		7	47 ± 3		
	5_1	9.9 ± 0.7		9	117.8 ± 15.4		9	118 ± 9		
	$6_{1/2}$	31.8 ± 5.2		11	199 ± 42		11	217 ± 17		
	$8_{1/2}$	82 ± 8		13	338 ± 102		13	352 ± 30		
	$10_{1/2}$	158 ± 12		Majorana fermion	3		2.86 ± 0.01	Dirac fermion	3	$2.0 \pm 0.1 - 2.4^*$
	$12_{1/2}$	253 ± 20			5		13.6 ± 0.8		5	9.1 ± 0.5
Complex scalar	$2_{1/2}$	0.58 ± 0.01	7		48.8 ± 3.3	7	45 ± 3			
	3_1	2.1 ± 0.1	9		113 ± 15	9	115 ± 9			
	$4_{1/2}$	4.98 ± 0.25	11		202 ± 43	11	211 ± 16			
	5_1	11.5 ± 0.8	13		324.6 ± 94	13	340 ± 27			
	$6_{1/2}$	32.7 ± 5.3								
	$8_{1/2}$	84 ± 8								
	$10_{1/2}$	162 ± 13								
	$12_{1/2}$	263 ± 22								

DIRECT DETECTION

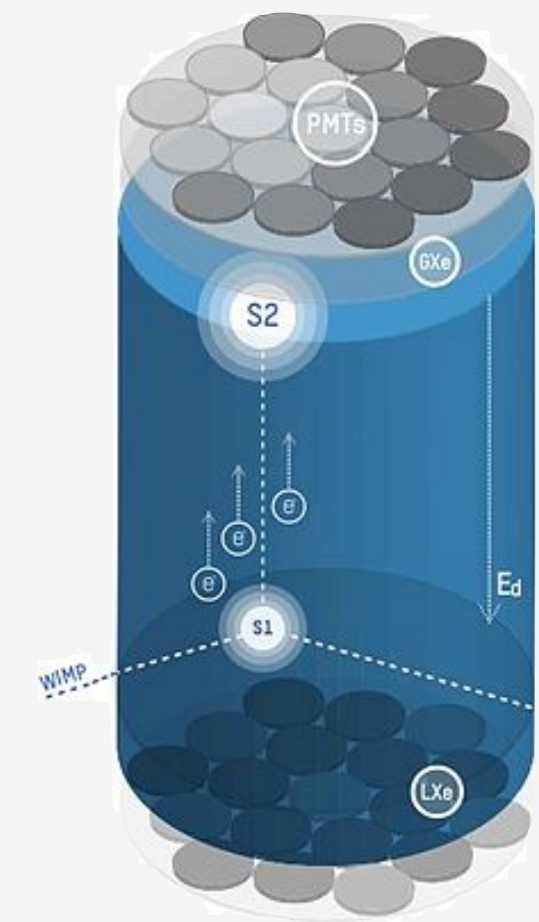
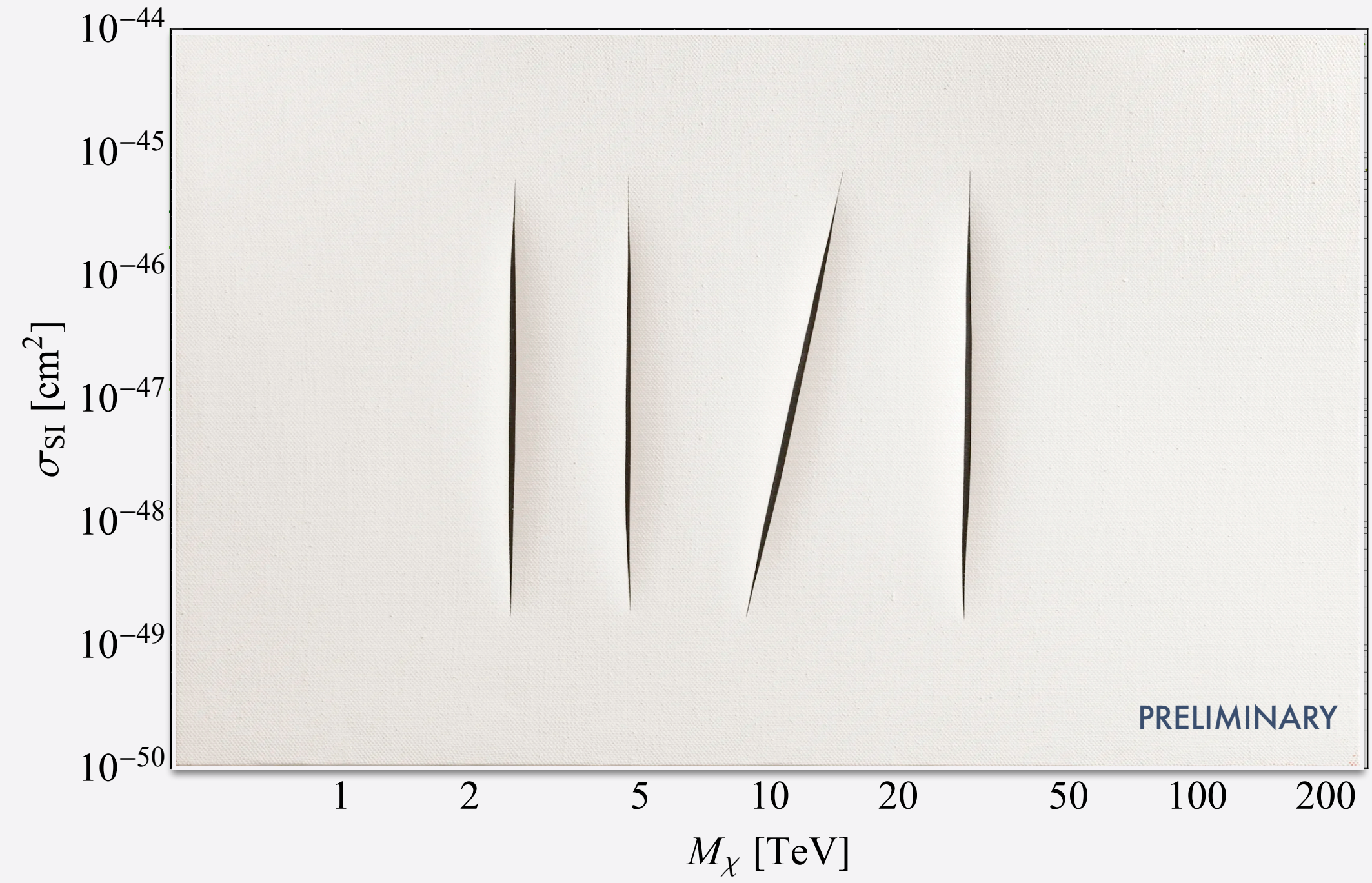
$Y \neq 0$, Mass-Splitting from DIM>4



Scattering on SM materials can be detected in ultra-low background experiments

Larger rates for the larger n -plets keep them visible

For such large DM mass the signature does not depend on the DM mass.



2030s
up to O(PeV)

An excess would require a "seasonality" check and maybe independent confirmation (many excesses in the past in this type of experiments, though most were at the lowest accessible masses)

Wff' PHASE SPACE

$$0.5 \cdot E_{cm} < m(f' \bar{f}) < 0.9 \cdot E_{cm}.$$

$$8^\circ < \theta(W) < 172^\circ,$$

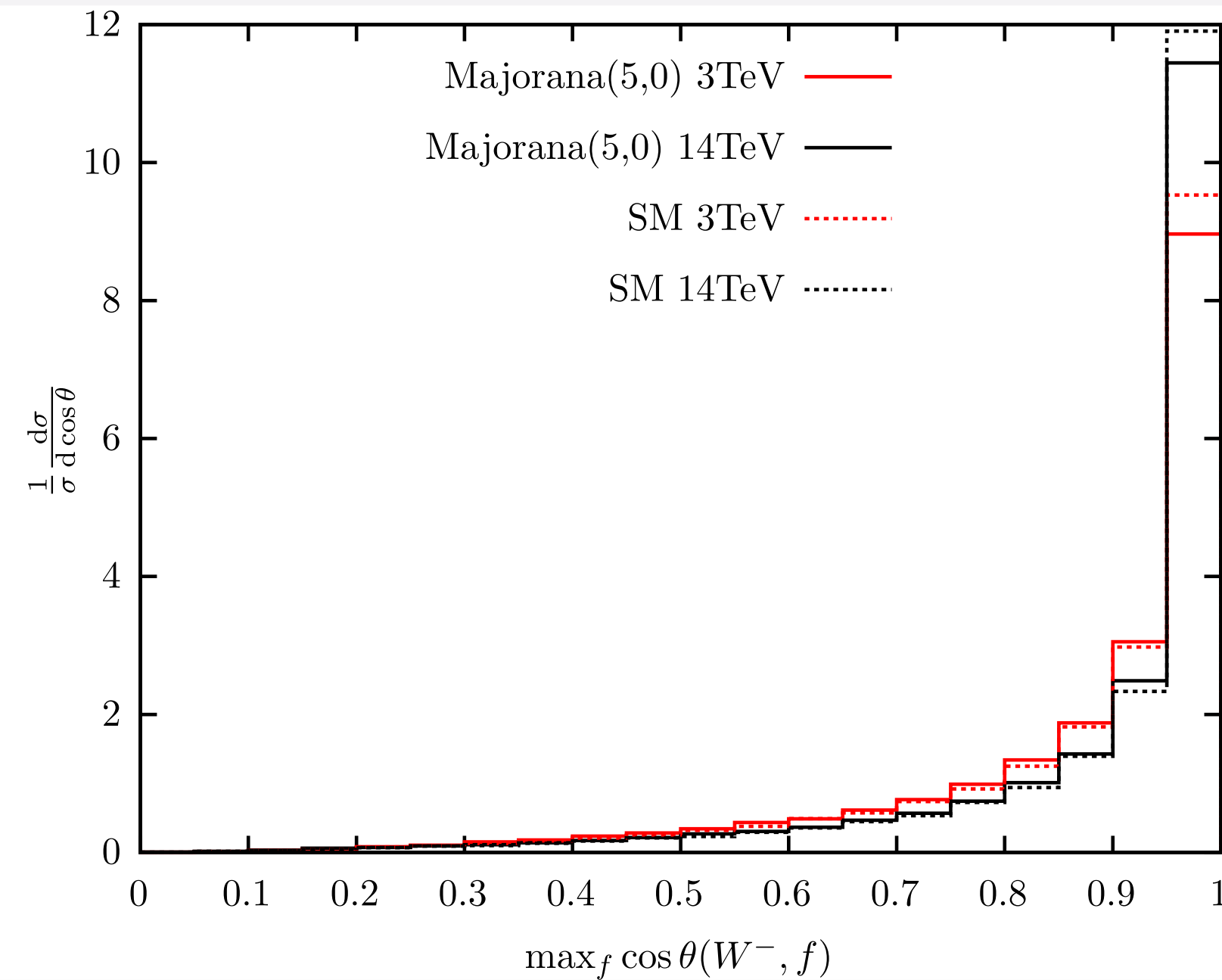
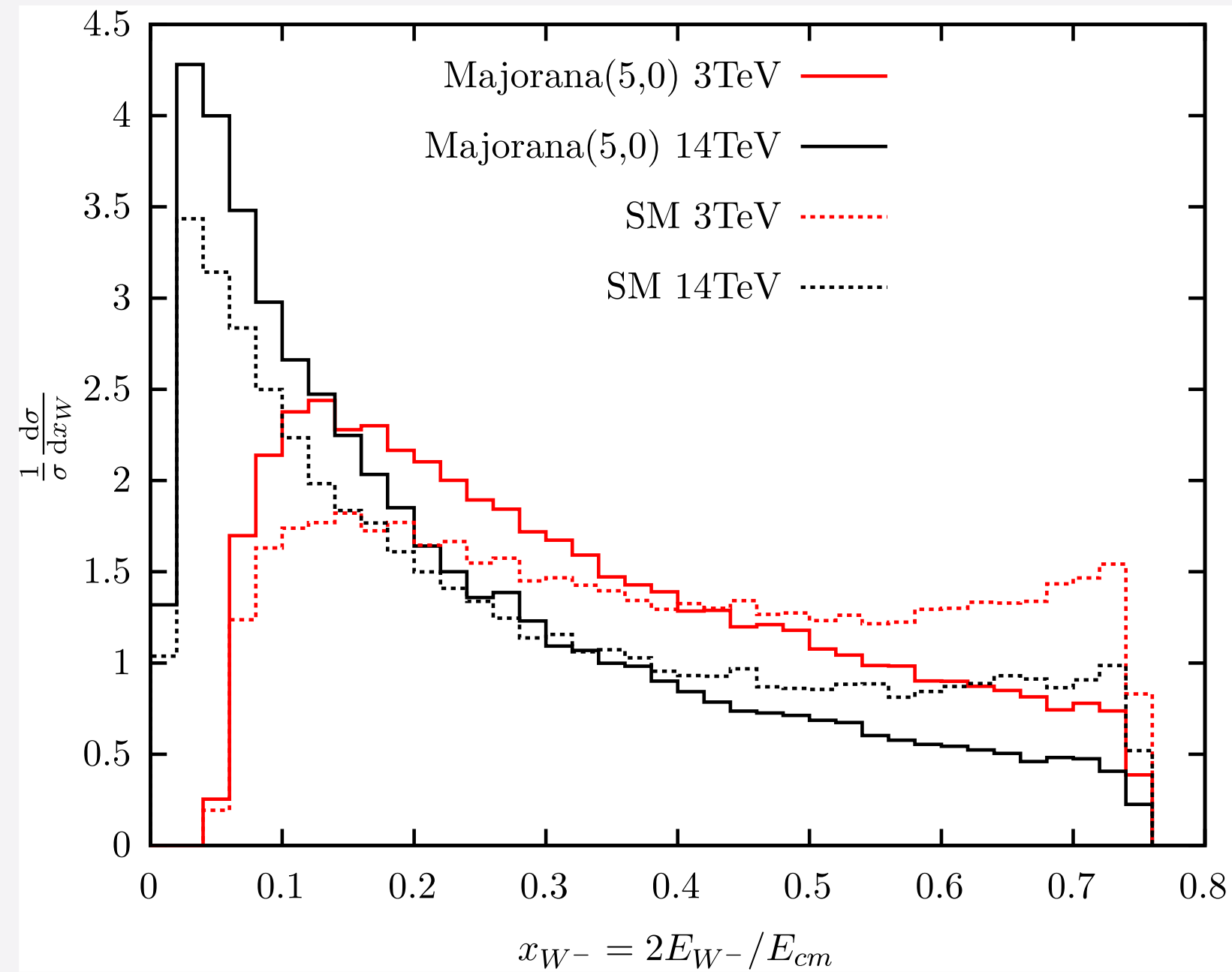
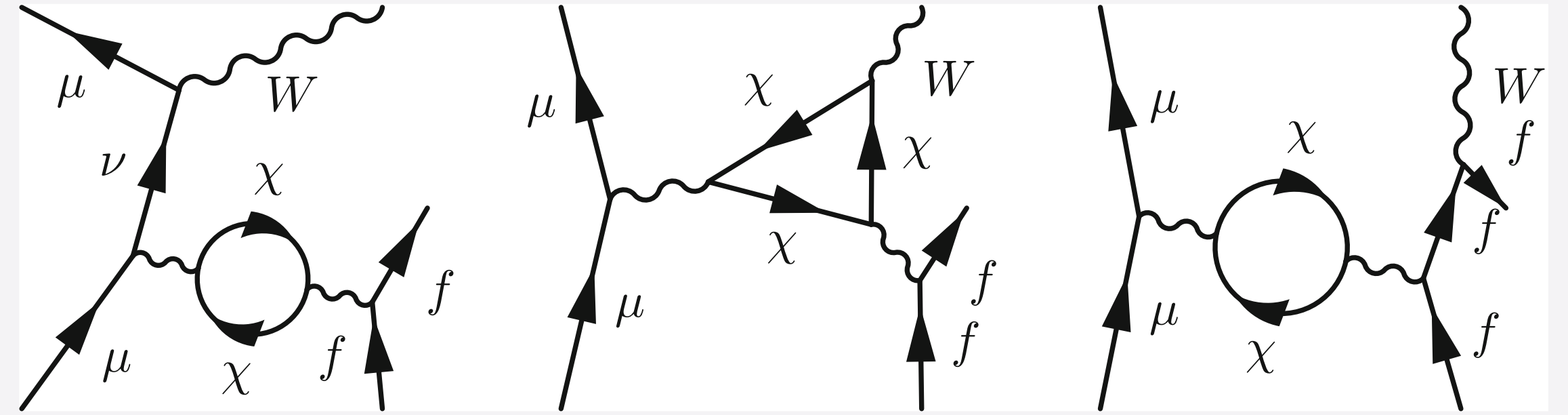


Fig. 5 Differential distribution of the normalized W boson energy ($x_W = 2E_W/E_{cm}$) and maximal $\cos\theta(W, f)$ ($f = \mu^+, \mu^-, u, \bar{d}$) for the $\mu^+\mu^- \rightarrow W^- u\bar{d}$ in the SM and the interference with a Majorana fermion 5-plet at the 3 TeV and 14 TeV muon collider

SOFT AND COLLINEAR W

