

Long-lived particle searches at future colliders

Nivedita Ghosh
Presented in Phoenix



19th December, 2023

Outline

Based on the work:

Light long-lived particles at the FCC-hh with the proposal for a dedicated forward detector FOREHUNT and a transverse detector DELIGHT (Arxiv: 2306.11803), Biplob Bhattacharjee, Herbi K. Dreiner, NG, Shigeki Matsumoto, Rhitaja Sengupta, Prabhat Solanki

Motivation

Model

Validation

Dedicated Detectors

Forward Detectors

Transverse Detectors

Conclusion

Motivation

- Long-lived BSM particles (LLPs) ($c\tau \gtrsim \mathcal{O}(\text{mm})$).

¹Kling et al, Phys. Rev. D 97 (2018) 035001

²Curtin et al, Phys. Rev. D 98 (2018) 115005

³Aielli et al., Eur. Phys. J. C 80 (2020) 1177

⁴Bauer et al., 1909.13022

Motivation

- Long-lived BSM particles (LLPs) ($c\tau \gtrsim \mathcal{O}(\text{mm})$).
- The CMS and ATLAS detectors extend up to $\mathcal{O}(10\text{ m})$.

¹Kling et al, Phys. Rev. D 97 (2018) 035001

²Curtin et al, Phys. Rev. D 98 (2018) 115005

³Aielli et al., Eur. Phys. J. C 80 (2020) 1177

⁴Bauer et al., 1909.13022

Motivation

- Long-lived BSM particles (LLPs) ($c\tau \gtrsim \mathcal{O}(\text{mm})$).
- The CMS and ATLAS detectors extend up to \mathcal{O} (10 m).
- Light LLPs with large decay lengths are more likely to decay outside the LHC main detector volumes due to the high boost values \rightarrow Dedicated detectors needed.

¹Kling et al, Phys. Rev. D 97 (2018) 035001

²Curtin et al, Phys. Rev. D 98 (2018) 115005

³Aielli et al., Eur. Phys. J. C 80 (2020) 1177

⁴Bauer et al., 1909.13022

Motivation

- Long-lived BSM particles (LLPs) ($c\tau \gtrsim \mathcal{O}(\text{mm})$).
- The CMS and ATLAS detectors extend up to \mathcal{O} (10 m).
- Light LLPs with large decay lengths are more likely to decay outside the LHC main detector volumes due to the high boost values \rightarrow Dedicated detectors needed.
- Depending on the production mode, LLP can traverse either in forward or transverse direction.

¹Kling et al, Phys. Rev. D 97 (2018) 035001

²Curtin et al, Phys. Rev. D 98 (2018) 115005

³Aielli et al., Eur. Phys. J. C 80 (2020) 1177

⁴Bauer et al., 1909.13022

Motivation

- Long-lived BSM particles (LLPs) ($c\tau \gtrsim \mathcal{O}(\text{mm})$).
- The CMS and ATLAS detectors extend up to $\mathcal{O}(10\text{ m})$.
- Light LLPs with large decay lengths are more likely to decay outside the LHC main detector volumes due to the high boost values \rightarrow Dedicated detectors needed.
- Depending on the production mode, LLP can traverse either in forward or transverse direction.
- At LHC, FASER (ForwArD Search ExpeRiment) ¹ is one such detector specifically designed to look for light LLPs in the far forward region while there are proposed experiments in the transverse direction, like MATHUSLA ², CODEX-b ³, and ANUBIS ⁴.

¹Kling et al, Phys. Rev. D 97 (2018) 035001

²Curtin et al, Phys. Rev. D 98 (2018) 115005

³Aielli et al., Eur. Phys. J. C 80 (2020) 1177

⁴Bauer et al., 1909.13022

Motivation

- Long-lived BSM particles (LLPs) ($c\tau \gtrsim \mathcal{O}(\text{mm})$).
- The CMS and ATLAS detectors extend up to \mathcal{O} (10 m).
- Light LLPs with large decay lengths are more likely to decay outside the LHC main detector volumes due to the high boost values \rightarrow Dedicated detectors needed.
- Depending on the production mode, LLP can traverse either in forward or transverse direction.
- At LHC, FASER (ForwARD Search ExpeRiment) ¹ is one such detector specifically designed to look for light LLPs in the far forward region while there are proposed experiments in the transverse direction, like MATHUSLA ², CODEX-b ³, and ANUBIS ⁴.
- **Not any proposal for 100 TeV FCC-hh !!**

¹Kling et al, Phys. Rev. D 97 (2018) 035001

²Curtin et al, Phys. Rev. D 98 (2018) 115005

³Aielli et al., Eur. Phys. J. C 80 (2020) 1177

⁴Bauer et al., 1909.13022

Dark Higgs Scalar

The Lagrangian can be written as ⁵

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mu_{\Phi}^2 \Phi^2 - \frac{1}{4} \lambda_{\Phi} \Phi^4 - \epsilon \Phi^2 |H|^2. \quad (1)$$

⁵Li et al, Arxiv:2212.06186

Dark Higgs Scalar

The Lagrangian can be written as ⁵

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mu_{\Phi}^2 \Phi^2 - \frac{1}{4} \lambda_{\Phi} \Phi^4 - \epsilon \Phi^2 |H|^2. \quad (1)$$

$$\begin{aligned} h_{125} &= \Phi \sin \theta + h \cos \theta, \\ \phi &= \Phi \cos \theta - h \sin \theta, \end{aligned} \quad (2)$$

⁵Li et al, Arxiv:2212.06186

Dark Higgs Scalar

The Lagrangian can be written as ⁵

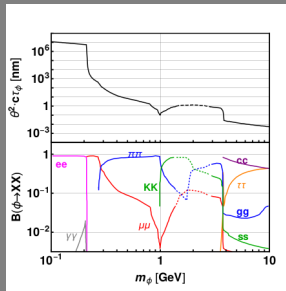
$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mu_{\Phi}^2 \Phi^2 - \frac{1}{4} \lambda_{\Phi} \Phi^4 - \epsilon \Phi^2 |H|^2. \quad (1)$$

$$\begin{aligned} h_{125} &= \Phi \sin \theta + h \cos \theta, \\ \phi &= \Phi \cos \theta - h \sin \theta, \end{aligned} \quad (2)$$

$$\mathcal{L}_{\text{int}} = \phi \sin \theta \sum_f \frac{m_f}{v} \bar{f} f, \quad (3)$$

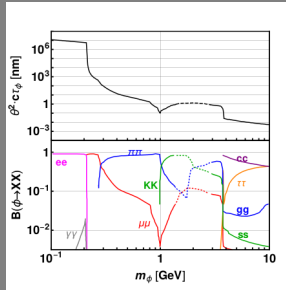
⁵Li et al, Arxiv:2212.06186

Dark Higgs Scalar



$$\Gamma_{\phi \rightarrow f\bar{f}} = \frac{N_c G_F m_\phi m_f^2 \sin^2 \theta}{4\sqrt{2}\pi} \left(1 - \frac{4m_f^2}{m_\phi^2}\right)^{3/2} \quad (4)$$

Dark Higgs Scalar



$$\Gamma_{\phi \rightarrow f\bar{f}} = \frac{N_c G_F m_\phi m_f^2 \sin^2 \theta}{4\sqrt{2}\pi} \left(1 - \frac{4m_f^2}{m_\phi^2}\right)^{3/2} \quad (4)$$

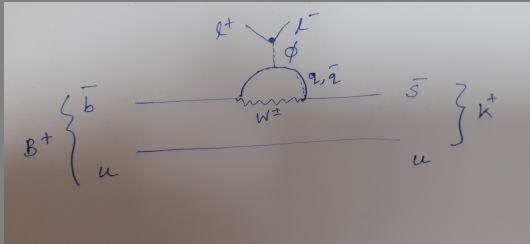
If the mixing angle, $\sin \theta$, is very small, the proper decay length of the dark Higgs scalar is $c\tau \sim$ few mm, making the particle long-lived.

Dark Higgs Scalar

ϕ to be very light, with its mass ranging from ~ 100 MeV to few GeV.

Dark Higgs Scalar

ϕ to be very light, with its mass ranging from ~ 100 MeV to few GeV.
 $B^\pm \rightarrow K^\pm \phi$ ⁶

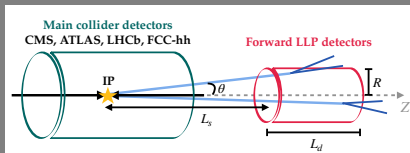


$$Br(B^\pm \rightarrow K^\pm \phi) \approx 5.7 \sin^2 \theta \left(1 - \frac{m_\phi^2}{m_b^2} \right)^2 \quad (5)$$

where $m_B = 5.28$ GeV, $m_K = 0.494$ GeV, and $m_b = 4.75$ GeV .

⁶FASER collaboration, PhysRevD.99.095011

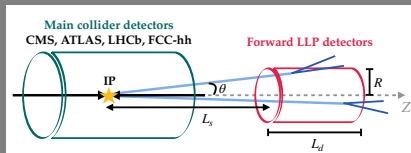
Analysis Setup



FASER R 10 cm and L_d 1.5 m, placed at 480 m in the z-axis from the IP, aiming to collect data during LHC run3 2021-2023 ⁷ for integrated luminosity 150 fb^{-1} .

⁷FASER collaboration, Phys. Rev. D 99 (2019) 095011

Analysis Setup

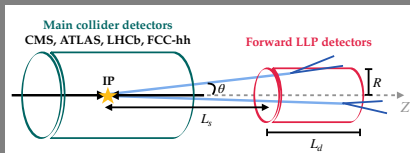


FASER R 10 cm and L_d 1.5 m, placed at 480 m in the z-axis from the IP, aiming to collect data during LHC run3 2021-2023 ⁷ for integrated luminosity 150 fb^{-1} .

FASER2 will possess a radius of 1 m and a length of 5 m, and it is expected to collect data for HL-LHC in the era 2026-2035 with an integrated luminosity of $\mathcal{L} = 3000 \text{ fb}^{-1}$.

⁷FASER collaboration, Phys. Rev. D 99 (2019) 095011

Analysis Setup



FASER R 10 cm and L_d 1.5 m, placed at 480 m in the z-axis from the IP, aiming to collect data during LHC run3 2021-2023 ⁷ for integrated luminosity 150 fb^{-1} .

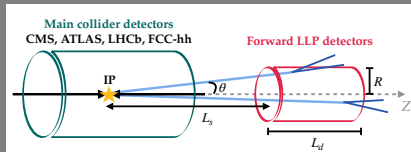
FASER2 will possess a radius of 1 m and a length of 5 m, and it is expected to collect data for HL-LHC in the era 2026-2035 with an integrated luminosity of $\mathcal{L} = 3000 \text{ fb}^{-1}$.

$$P_{\text{decay}} = \frac{(1 - e^{-\frac{L_1}{|D_z|}})}{e^{\frac{L_s}{|D_z|}}}, \quad (6)$$

where $D_z = \frac{p_z}{m} c\tau$.

⁷FASER collaboration, Phys. Rev. D 99 (2019) 095011

Analysis Setup



FASER R 10 cm and L_d 1.5 m, placed at 480 m in the z-axis from the IP, aiming to collect data during LHC run3 2021-2023 ⁷ for integrated luminosity 150 fb^{-1} .

FASER2 will possess a radius of 1 m and a length of 5 m, and it is expected to collect data for HL-LHC in the era 2026-2035 with an integrated luminosity of $\mathcal{L} = 3000 \text{ fb}^{-1}$.

$$P_{\text{decay}} = \frac{(1 - e^{-\frac{L_d}{|D_z|}})}{e^{\frac{L_s}{|D_z|}}}, \quad (6)$$

where $D_z = \frac{p_z}{m} c\tau$.

$$\epsilon_{\text{LLP}} = \frac{\sum_i P_i^{\text{decay}}}{N_{\text{events}}}, \quad (7)$$

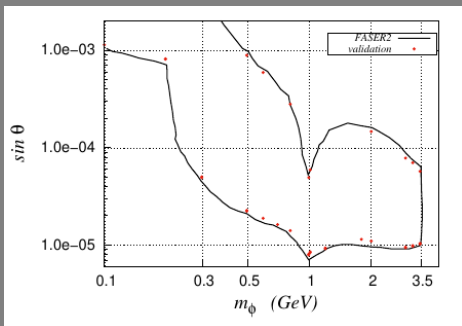
⁷FASER collaboration, Phys. Rev. D 99 (2019) 095011

Analysis Setup

$$N_{\text{detector}} = \sigma_{bb} \times \epsilon_{B^\pm} \times \text{Br}(B^\pm \rightarrow K^\pm \phi) \times \epsilon_{\text{LLP}} \times \mathcal{L} \quad (8)$$

$$\sigma_{bb} = 9.4 \times 10^{11} \text{fb}^8$$

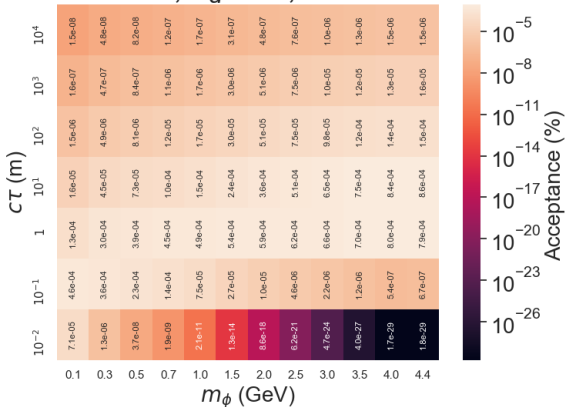
LLP decays to the visible particles with 100% branching ratio and will be detected in the detector only if the momentum $p_\phi > 100 \text{ GeV}$



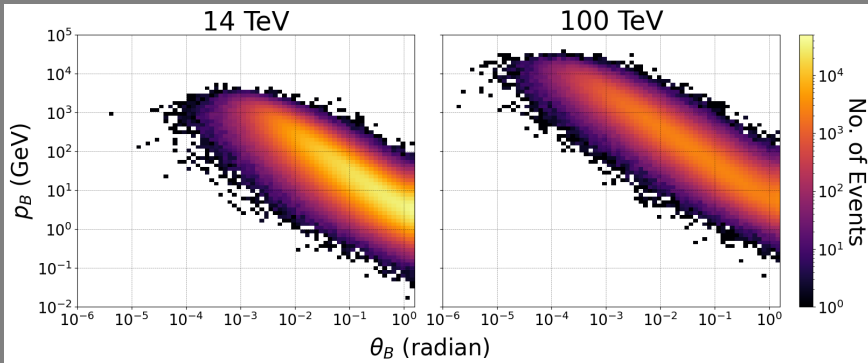
⁸validation done with FORESEE package, Kling et al

Why 100 TeV?

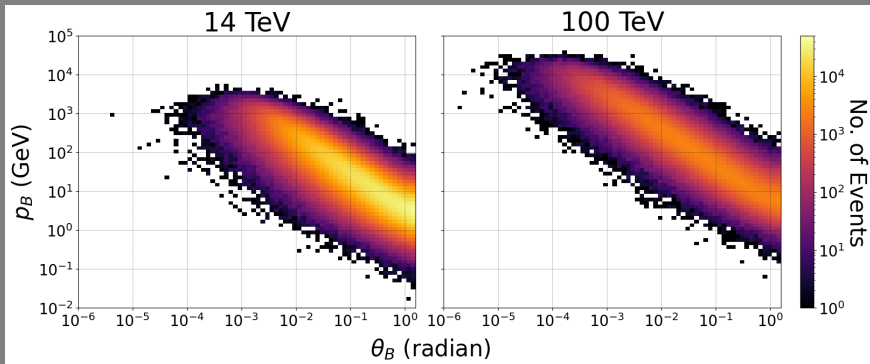
$R=1m, L_d=5m, 14 \text{ TeV}$



Why 100 TeV?

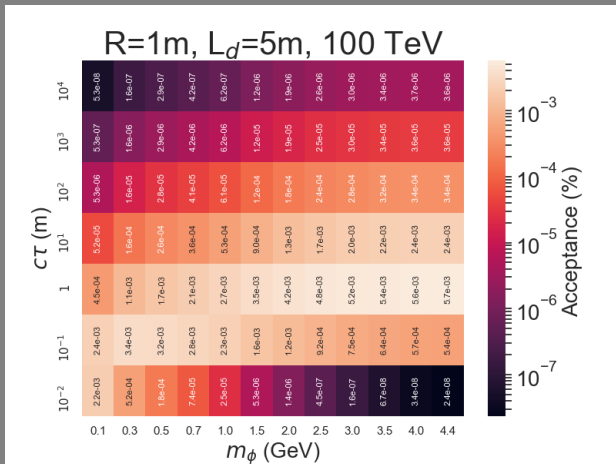


Why 100 TeV?

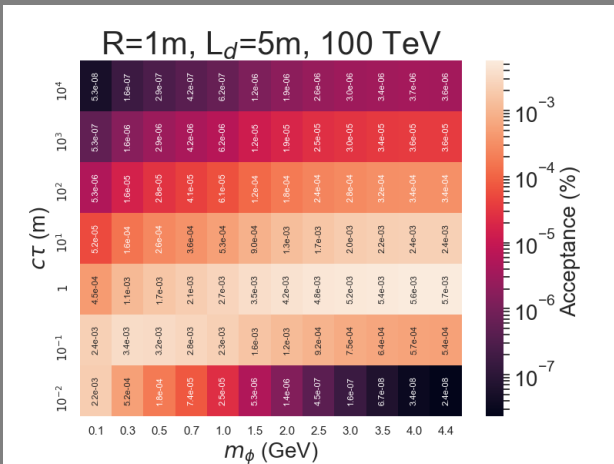


Compared to 14 TeV, at 100 TeV, the B^- mesons are much more forward.

Why 100 TeV?



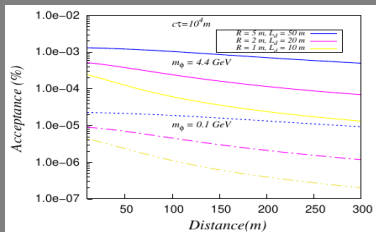
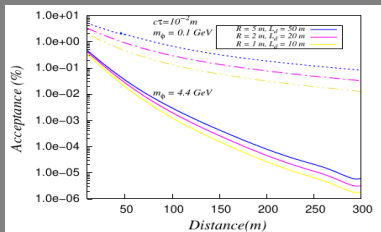
Why 100 TeV?



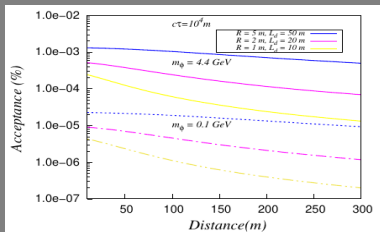
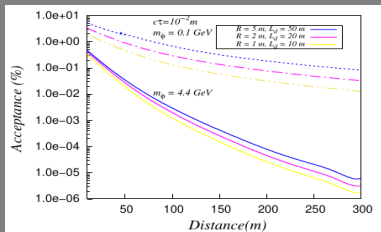
At future colliders like LHC at 100 TeV, we are not limited by the space constraint ⁹

⁹Aleksa et al., CERN-2022-002

Optimizing the detector

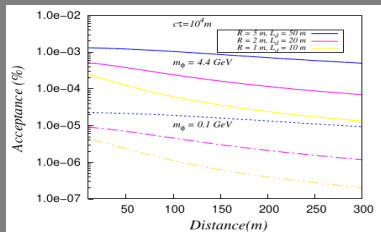
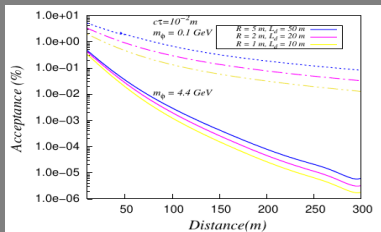


Optimizing the detector



FOREHUNT (FORward Experiment for HUNDred TeV)

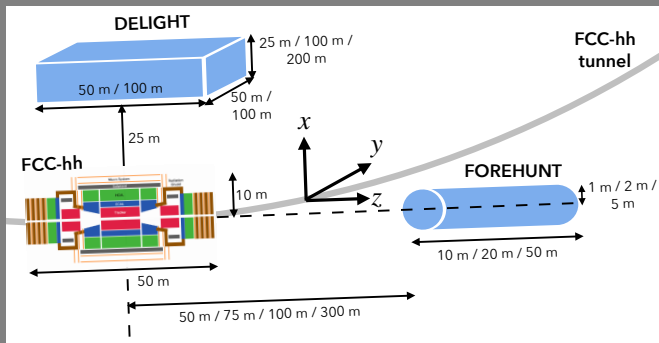
Optimizing the detector



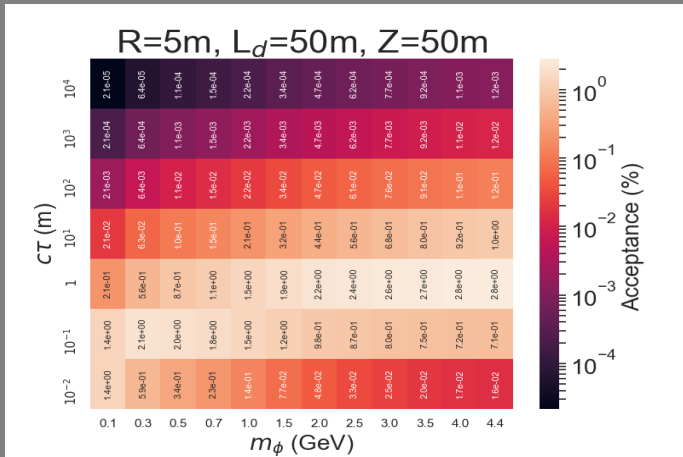
FOREHUNT (FORward Experiment for HUNDred TeV)

Detector Configuration @100 TeV	Radius (R)	Length (L_d)	Position (Z)
FOREHUNT-A	1 m	10 m	50 m
FOREHUNT-B	2 m	20 m	50 m
FOREHUNT-C	5 m	50 m	50 m
FOREHUNT-D	2 m	20 m	75 m
FOREHUNT-E	5 m	50 m	75 m
FOREHUNT-F	5 m	50 m	100 m

Optimizing the detector



Dark Higgs



CODEX-B

CODEX-b (“COmpact Detector for EXotics at LHCb”) is proposed to search for LLPs decaying with $c\tau > 1 \text{ m}^{10}$ with an integrated luminosity of 300 fb^{-1} . This detector is to be installed near the LHCb interaction point.

¹⁰Aielli et al., Arxiv:2203.07316

CODEX-B

CODEX-b (“COmpact Detector for EXotics at LHCb”) is proposed to search for LLPs decaying with $c\tau > 1 \text{ m}^{10}$ with an integrated luminosity of 300 fb^{-1} . This detector is to be installed near the LHCb interaction point.

The considered dimensions for this detector is a $10 \times 10 \times 10 \text{ m}^3$ decay volume and if possible, a bigger size of $20 \times 10 \times 10 \text{ m}^3$, with the following position:

- **CODEX – b** : $26.0 \text{ m} < x < 46.0 \text{ m}$, $-7.0 \text{ m} < y < 3.0 \text{ m}$, $5.0 \text{ m} < z < 15.0 \text{ m}$

¹⁰Aielli et al., Arxiv:2203.07316

MATHUSLA

MATHUSLA(‘MASSive Timing Hodoscope for Ultra-Stable neutral pArticles’) ¹¹ is proposed to detect particle with $c\tau > 100$ m at the 14 TeV HL-LHC with an integrated luminosity of $3ab^{-1}$. MATHUSLA is intended to be positioned near the CMS interaction point at the HL-LHC.

¹¹MATHUSLA collaboration, JINST 15 (2020) C06026

MATHUSLA

MATHUSLA (“MASSive Timing Hodoscope for Ultra-Stable neutral pArticles”) ¹¹ is proposed to detect particle with $c\tau > 100$ m at the 14 TeV HL-LHC with an integrated luminosity of $3ab^{-1}$. MATHUSLA is intended to be positioned near the CMS interaction point at the HL-LHC.

- **MATHUSLA** : $60.0 \text{ m} < x < 85.0 \text{ m}$, $-50.0 \text{ m} < y < 50.0 \text{ m}$, $68.0 \text{ m} < z < 168.0 \text{ m}$

¹¹MATHUSLA collaboration, JINST 15 (2020) C06026

DELIGHT

DELIGHT(“Detector for long-lived particles at high energy of 100 TeV”) is a transverse detector that is proposed to detect LLPs at the 100 TeV LHC, as discussed in ¹².

¹²Bhattacharjee et al., Phys. Rev. D 106 (2022) 095018

DELIGHT

DELIGHT(“Detector for long-lived particles at high energy of 100 TeV”) is a transverse detector that is proposed to detect LLPs at the 100 TeV LHC, as discussed in ¹².

- **DELIGHT – A** : $25.0 \text{ m} < x < 50.0 \text{ m}$, $0.0 \text{ m} < y < 100.0 \text{ m}$, $-50.0 \text{ m} < z < 50.0 \text{ m}$
- **DELIGHT – B** : $25.0 \text{ m} < x < 125.0 \text{ m}$, $0.0 \text{ m} < y < 100.0 \text{ m}$, $-50.0 \text{ m} < z < 50.0 \text{ m}$
- **DELIGHT – C** : $25.0 \text{ m} < x < 225.0 \text{ m}$, $0.0 \text{ m} < y < 50.0 \text{ m}$, $-25.0 \text{ m} < z < 25.0 \text{ m}$

¹²Bhattacharjee et al., Phys. Rev. D 106 (2022) 095018

Comparison

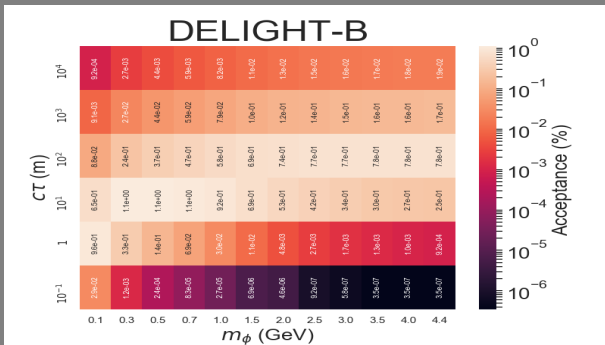
m_ϕ (GeV)	$c\tau$ (m)	FASEER2 ($p_\phi > 100\text{GeV}$)	CODEX-b ($E_\phi > 1\text{GeV}$)	MATHUSLA ($E_\phi > 1\text{GeV}$)	FOREHUNT-C ($p_\phi > 100\text{GeV}$)	DELIGHT-B ($E_\phi > 1\text{GeV}$)
0.1	10^1	$1.6 \times 10^{-5}\%$	$1.0 \times 10^{-2}\%$	$1.3 \times 10^{-1}\%$	$2.1 \times 10^{-2}\%$	$6.5 \times 10^{-1}\%$
0.1	10^4	$1.5 \times 10^{-8}\%$	$1.1 \times 10^{-5}\%$	$2.1 \times 10^{-4}\%$	$2.1 \times 10^{-5}\%$	$9.2 \times 10^{-4}\%$
2.0	10^1	$3.6 \times 10^{-4}\%$	$1.8 \times 10^{-2}\%$	$4.4 \times 10^{-2}\%$	$4.4 \times 10^{-1}\%$	$5.3 \times 10^{-1}\%$
2.0	10^4	$4.8 \times 10^{-7}\%$	$1.9 \times 10^{-4}\%$	$3.4 \times 10^{-3}\%$	$4.7 \times 10^{-4}\%$	$1.5 \times 10^{-2}\%$
4.4	10^1	$8.6 \times 10^{-4}\%$	$9.2 \times 10^{-3}\%$	$1.3 \times 10^{-2}\%$	1.0%	$2.5 \times 10^{-1}\%$
4.4	10^4	$1.5 \times 10^{-6}\%$	$2.3 \times 10^{-4}\%$	$5.0\% \times 10^{-3}\%$	$1.2 \times 10^{-3}\%$	$1.9 \times 10^{-2}\%$

Comparison

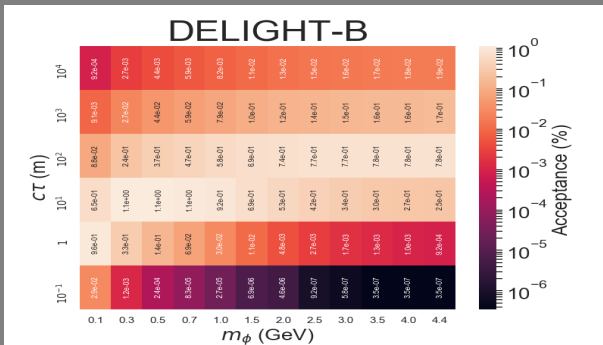
m_ϕ (GeV)	c_T (m)	FASER2 ($p_\phi > 100\text{GeV}$)	CODEX-b ($E_\phi > 1\text{GeV}$)	MATHUSLA ($E_\phi > 1\text{GeV}$)	FOREHUNT-C ($p_\phi > 100\text{GeV}$)	DELIGHT-B ($E_\phi > 1\text{GeV}$)
0.1	10^1	$1.6 \times 10^{-5}\%$	$1.0 \times 10^{-2}\%$	$1.3 \times 10^{-1}\%$	$2.1 \times 10^{-2}\%$	$6.5 \times 10^{-1}\%$
0.1	10^4	$1.5 \times 10^{-8}\%$	$1.1 \times 10^{-5}\%$	$2.1 \times 10^{-4}\%$	$2.1 \times 10^{-5}\%$	$9.2 \times 10^{-4}\%$
2.0	10^1	$3.6 \times 10^{-4}\%$	$1.8 \times 10^{-2}\%$	$4.4 \times 10^{-2}\%$	$4.4 \times 10^{-1}\%$	$5.3 \times 10^{-1}\%$
2.0	10^4	$4.8 \times 10^{-7}\%$	$1.9 \times 10^{-4}\%$	$3.4 \times 10^{-3}\%$	$4.7 \times 10^{-4}\%$	$1.5 \times 10^{-2}\%$
4.4	10^1	$8.6 \times 10^{-4}\%$	$9.2 \times 10^{-3}\%$	$1.3 \times 10^{-2}\%$	1.0%	$2.5 \times 10^{-1}\%$
4.4	10^4	$1.5 \times 10^{-6}\%$	$2.3 \times 10^{-4}\%$	$5.0\% \times 10^{-3}\%$	$1.2 \times 10^{-3}\%$	$1.9 \times 10^{-2}\%$

DELIGHT performs very well for most of the benchmark points with $c_T > 10^1$ m.

DELIGHT for Dark-Higgs

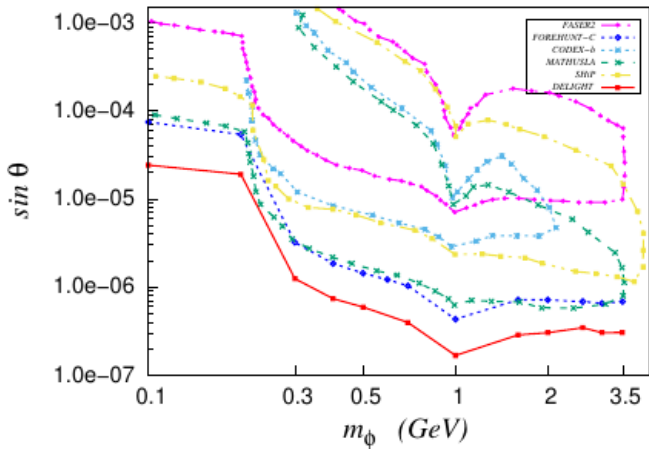


DELIGHT for Dark-Higgs



- $m_\phi = 4.4$ GeV and $cT = 1$ m, FOREHUNT-C outperforms DELIGHT-B by a factor of $\mathcal{O}(3 \times 10^3)$.
- DELIGHT-B superior performance for decay lengths $\geq 10^2$ m.
- For $cT \approx 10$ m, DELIGHT-B performs better than FOREHUNT-C for LLPs with masses < 2.5 GeV.

Final Result



Conclusion

- Detection prospect of light LLPs coming from B -meson decays at the FCC-hh for dark Higgs boson.

Conclusion

- Detection prospect of light LLPs coming from B -meson decays at the FCC-hh for dark Higgs boson.
- Compared to FASER2, enhance the sensitivity by a factor of 20 for the dark Higgs model. → **DELIGHT** performs even well.

Conclusion

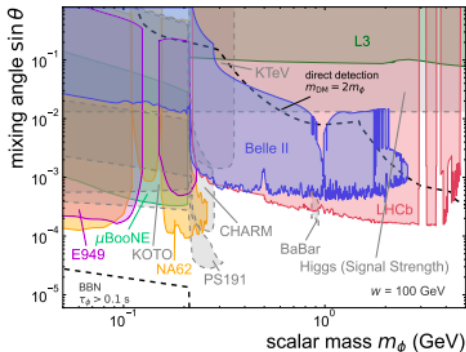
- Detection prospect of light LLPs coming from B -meson decays at the FCC-hh for dark Higgs boson.
- Compared to FASER2, enhance the sensitivity by a factor of 20 for the dark Higgs model. → **DELIGHT** performs even well.
- For model-independent analysis, our analysis reveals that if the LLP has low decay length < 10 m, a forward detector like FOREHUNT is the best option to look for the decaying LLP, while DELIGHT is preferable for higher decay lengths.

Conclusion

- Detection prospect of light LLPs coming from B -meson decays at the FCC-hh for dark Higgs boson.
- Compared to FASER2, enhance the sensitivity by a factor of 20 for the dark Higgs model. → **DELIGHT** performs even well.
- For model-independent analysis, our analysis reveals that if the LLP has low decay length < 10 m, a forward detector like FOREHUNT is the best option to look for the decaying LLP, while DELIGHT is preferable for higher decay lengths.



Dark Higgs



E949: $K^+ \rightarrow \pi^+ \phi (\rightarrow \text{inv.})$

Phys. Rev. D 79 (2009) 082004

KOTO: $K_S^0 \rightarrow \pi^0 \phi (\rightarrow \text{inv.})$

Phys. Rev. Lett. 126 (12) (2021) 121801

μ BooNE: $K^+ \rightarrow \pi^+ \phi (\rightarrow e^+ e^-)$

Phys. Rev. Lett. 127 (15) (2021) 151803

NA62: $K^+ \rightarrow \pi^+ \phi (\rightarrow \text{inv.})$

JHEP 02 (2021) 051, JHEP 08 (2021) 098

PS191: $K^{\pm} \rightarrow \pi^{\pm} \phi (\rightarrow e^+ e^-, \mu^+ \mu^-)$

Phys. Lett. B 203 (1990) 333-334, Phys. Lett. B 320 (2021) 136024

CHARM: $K^{\pm} \rightarrow \pi^{\pm} \phi (\rightarrow e^+ e^-, \mu^+ \mu^-)$

Phys. Lett. B 203 (1990) 332-334, Phys. Lett. B 320 (2021) 136024

Belle II: $B \rightarrow K^{(*)} \phi (\rightarrow e^+ e^-, \mu^+ \mu^-, \pi^+ \pi^-, K^+ K^-)$

Morise 2023

KTeV: $K_S^0 \rightarrow \pi^0 \phi (\rightarrow \mu^+ \mu^-)$

Phys. Rev. Lett. 84 (2000) 5270-5282, Phys. Rev. D 99 (1) (2019) 015018

BaBar: $B \rightarrow X_S \phi (\rightarrow e^+ e^-, \mu^+ \mu^-, \pi^+ \pi^-, K^+ K^-)$

Phys. Rev. Lett. 114 (17) (2015) 171801, Phys. Rev. D 89 (1) (2019) 015018

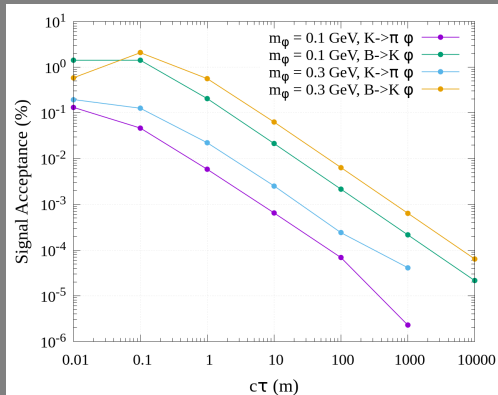
L3: $e^+ e^- \rightarrow Z^* \phi$

Phys. Lett. B 365 (1996) 454-470

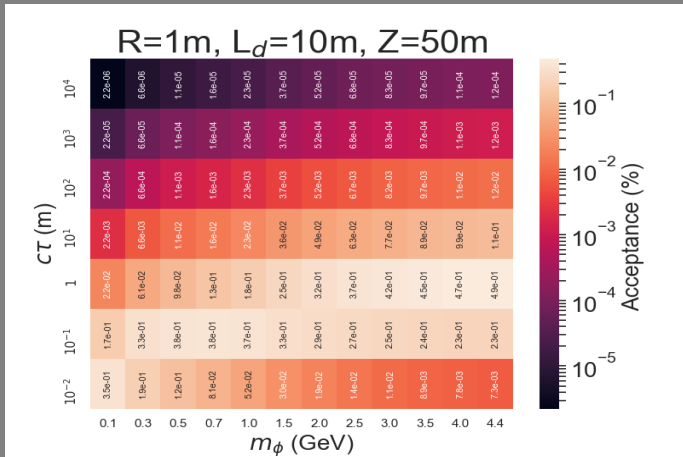
LHCb: $B \rightarrow K^{(*)} \phi (\rightarrow \mu^+ \mu^-)$

Phys. Rev. Lett. 115 (6) (2015) 061802, Phys. Rev. D 95 (7) (2017) 071101, Phys. Rev. D 98 (11) (2018) 115009

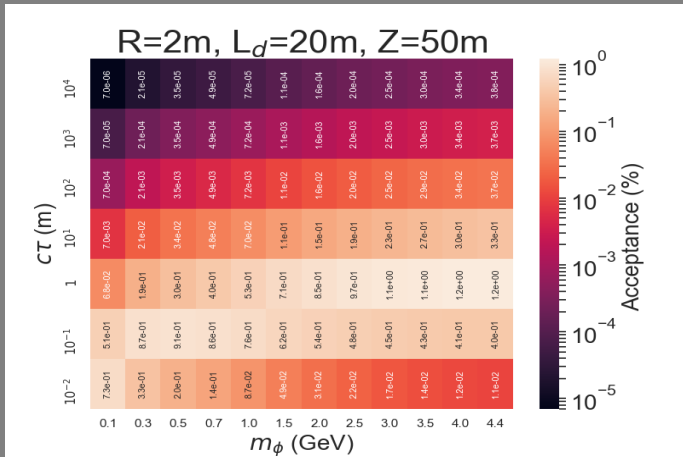
Dark Higgs



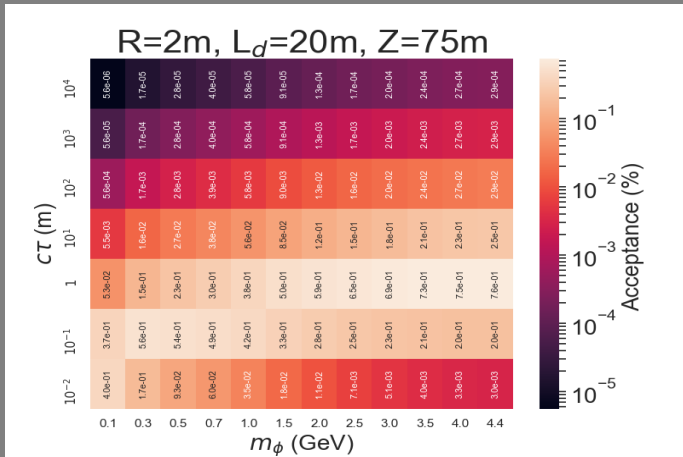
Dark Higgs



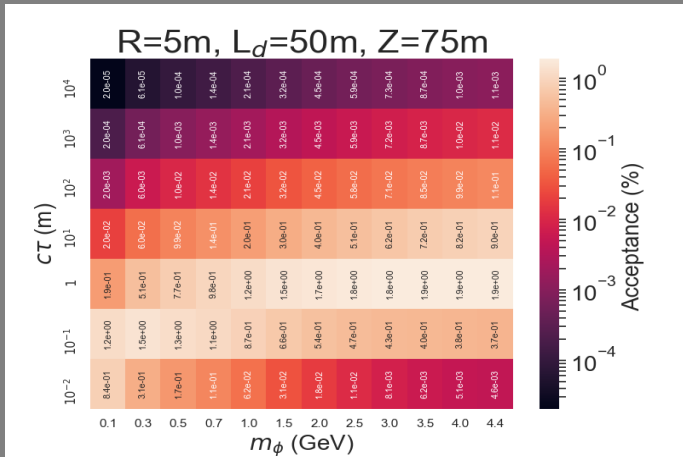
Dark Higgs



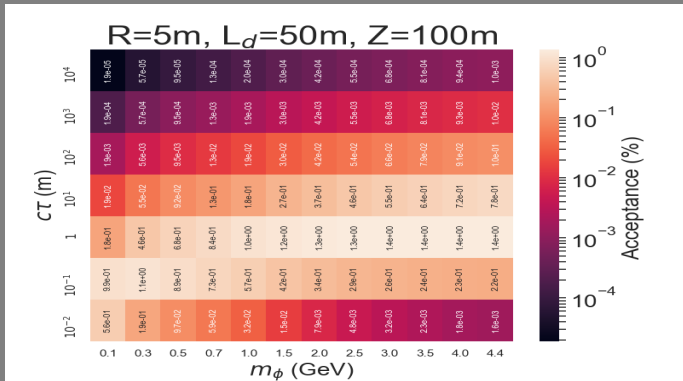
Dark Higgs



Dark Higgs



Dark Higgs

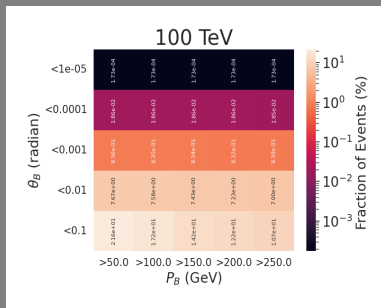
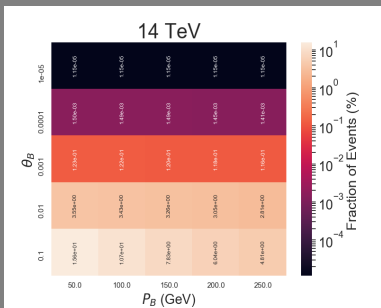


m_ϕ (GeV)	$c\tau$ (m)	acceptance for first detector at $z=50$ m	acceptance for second detector at $z=100$ (150) m	acceptance for second detector at $z=300$ m
0.1	10^{-1}	1.4×10^{-2}	9.9×10^{-3} (7.0×10^{-3})	2.9×10^{-3}
4.4	10^{-1}	7.0×10^{-3}	2.2×10^{-3} (1.0×10^{-3})	1.9×10^{-4}
0.1	10^4	2.1×10^{-7}	1.9×10^{-7} (1.6×10^{-7})	9.3×10^{-8}
4.4	10^4	1.2×10^{-5}	1.0×10^{-5} (8.5×10^{-6})	4.9×10^{-6}

m_ϕ (GeV)	$c\tau$ (m)	acceptance for first detector at $z=50$ m	acceptance for second detector at $z=100$ (150) m	acceptance for second detector at $z=300$ m
0.1	10^{-1}	1.4×10^{-2}	9.9×10^{-3} (7.0×10^{-3})	2.9×10^{-3}
4.4	10^{-1}	7.0×10^{-3}	2.2×10^{-3} (1.0×10^{-3})	1.9×10^{-4}
0.1	10^4	2.1×10^{-7}	1.9×10^{-7} (1.6×10^{-7})	9.3×10^{-8}
4.4	10^4	1.2×10^{-5}	1.0×10^{-5} (8.5×10^{-6})	4.9×10^{-6}

m_ϕ (GeV)	$c\tau$ (m)	1 m off-axis ($p_\phi > 100$ GeV)	5 m off-axis ($p_\phi > 100$ GeV)
0.1	10^{-1}	0.83%	$5.5 \times 10^{-2}\%$
4.4	10^{-1}	$1.53 \times 10^{-2}\%$	$1.2 \times 10^{-4}\%$
0.1	10^4	$1.5 \times 10^{-5}\%$	$8.7 \times 10^{-7}\%$
4.4	10^4	$8.4 \times 10^{-4}\%$	$1.7 \times 10^{-4}\%$

m_ϕ (GeV)	$c\tau$ (m)	FOREHUNT-C ($p_\phi > 50$ GeV, $z=100$ m)	FOREHUNT-C ($p_\phi > 50$ GeV, $z=200$ m)	FOREHUNT-C ($p_\phi > 50$ GeV, $z=300$ m)
0.1	10^1	$3.3 \times 10^{-2}\%$	$1.8 \times 10^{-2}\%$	$1.1 \times 10^{-2}\%$
0.1	10^4	$3.3 \times 10^{-5}\%$	$1.8 \times 10^{-5}\%$	$1.2 \times 10^{-5}\%$
2.0	10^1	$6.0 \times 10^{-1}\%$	$3.0 \times 10^{-1}\%$	$2.0 \times 10^{-1}\%$
2.0	10^4	$7.4 \times 10^{-4}\%$	$4.4 \times 10^{-4}\%$	$3.0 \times 10^{-4}\%$
4.4	10^1	1.1%	$5.0 \times 10^{-1}\%$	$3.0 \times 10^{-1}\%$
4.4	10^4	$1.6 \times 10^{-3}\%$	$9.0 \times 10^{-4}\%$	$5.9 \times 10^{-4}\%$



Cost Estimation

- The typical cost of BIS78 RPCs are around $3.1 \text{ k€}/\text{m}^2$ ¹³.
- We propose to place several circular layers of RPCs transverse to the length of the cylindrical decay volume.
- For FOREHUNT-C, the estimated cost per layer of RPC would be around 245 k€.

¹³Bauer et al., Arxiv:1909.13022