

Gravitational wave imprints of the doublet left-right symmetric model^a

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^a arxiv: 2309.12023, with Siddhartha Karmakar (TIFR, IITB)

Motivation

Gravitational Wave Astronomy

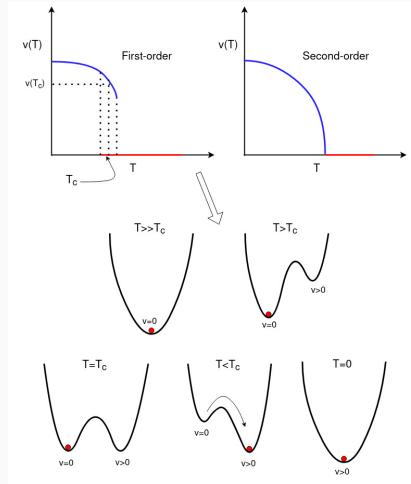
- 1st direct detection: BH-BH merger by LIGO/VIRGO in 2015, ~ 50 detections as of December 2019.
- 2023, (possible) detection of nanoHz GW background by PTAs.
- Cosmological sources of GW background: inflation, domain walls, cosmic strings, **first-order phase transitions**.
- Planned: aLIGO, LISA, ET, BBO, DECIGO, CE, SKA.
- Fresh look at the universe!

Phase transitions in particle physics

- Particle physics model featuring spontaneous symmetry breaking:

$$G \xrightarrow{v \neq 0} H.$$

- At temperature T , the vev ($v \equiv \langle \phi \rangle$) lies at the minimum of the effective potential, $V_{\text{eff}}(\phi, T)$.
- Usually at high T , $v \rightarrow 0$ due to thermal effects [Kirzhnitz, 1972] (symmetry restoration).
- As the universe cools, there is a phase transition from $v = 0$ to $v \neq 0$.
- Order parameter: $v(T)$.

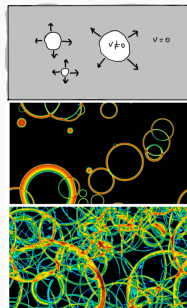


FOPT and GWs

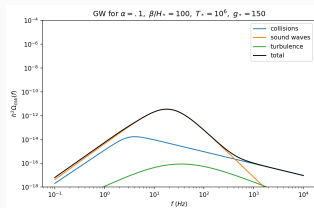
- FOPT \implies bubbles of true phase nucleate in a sea of false phase.
- Tunneling probability [Callan-Coleman 1977; Linde, 1977], $\Gamma(T) \approx T^4 \left(\frac{S_3}{2\pi T} \right)^{3/2} e^{-\frac{S_3}{T}}$.
- Strength of FOPT characterized by,
 - T_n : $\Gamma(T_n) \sim \mathcal{O}(1)$,
 - Ratio of latent heat and radiation density, α ,
 - Rate of PT,

$$\beta \equiv - \left. \frac{dS}{dt} \right|_{t=t_*} = TH_* \left. \frac{dS}{dT} \right|_{T=T_*}.$$
- Bubbles expand rapidly, collide with each other.
- GWs are produced by: bubble collisions, sound waves in the plasma, and MHD turbulence.

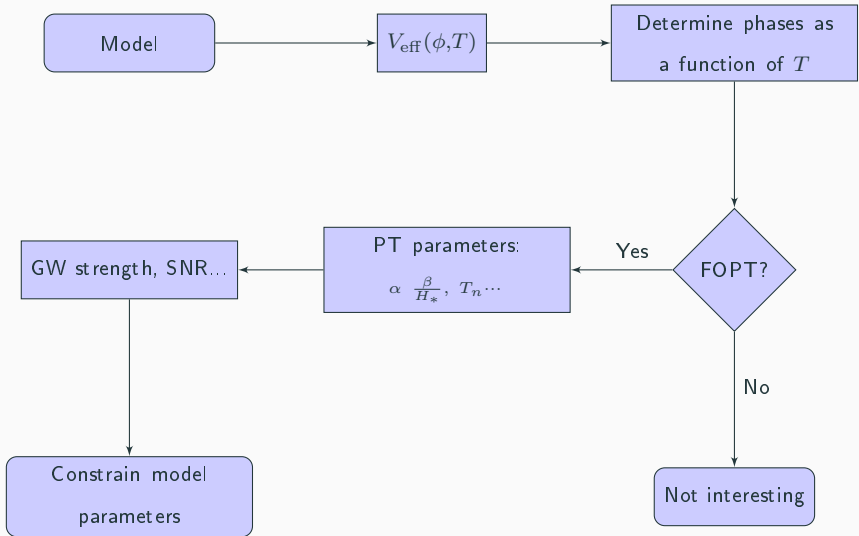
$$h^2 \Omega_{\text{GW}} \approx h^2 \Omega_{\text{coll}} + h^2 \Omega_{\text{sw}} + h^2 \Omega_{\text{turb}}.$$
- Large α , small β/H_* \implies strong FOPT \implies strong GW background.
- $f_{\text{peak}} \propto T_n$.



[D. Weir, 2017]



Constraining models with GWs from FOPT



The model

Left-right symmetric model

- LRSM gauge group:

$$\mathcal{G}_{\text{LRSM}} = SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

- Breaking pattern: $\mathcal{G}_{\text{LRSM}} \xrightarrow{v_R} \mathcal{G}_{\text{SM}} \xrightarrow{v_L, \kappa_1, \kappa_2} U(1)_{\text{em}}$
- Scalars for SSB: a bidoublet + 2 triplets (TLRSM), or a bidoublet and 2 doublets (DLRSM).
- Higgs and EWPO data: electroweak symmetry breaking in DLRSM can be much different from that in TLRSM.¹
- For $v_R \sim \mathcal{O}(10)$ TeV, the GW background can be detected at observatories like BBO and DECIGO.

¹Bernard et. al. 2020; Karmakar, Uma et.al. 2022

Doublet left-right symmetric model

- Fermions:

$$Q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix} \sim (3, 2, 1, 1/3), \quad Q_R = \begin{pmatrix} u_R \\ d_R \end{pmatrix} \sim (3, 1, 2, 1/3),$$
$$L_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \sim (1, 2, 1, -1), \quad L_R = \begin{pmatrix} \nu_R \\ e_R \end{pmatrix} \sim (1, 1, 2, -1).$$

- Scalars:

$$\Phi = \begin{pmatrix} \phi_1^0 & \phi_2^+ \\ \phi_1^- & \phi_2^0 \end{pmatrix} \sim (1, 2, 2, 0),$$
$$\chi_L = \begin{pmatrix} \chi_L^+ \\ \chi_L^0 \end{pmatrix} \sim (1, 2, 1, 1), \quad \text{and} \quad \chi_R = \begin{pmatrix} \chi_R^+ \\ \chi_R^0 \end{pmatrix} \sim (1, 1, 2, 1).$$

- Yukawa lagrangian:

$$\mathcal{L}_Y \supset -\bar{Q}_{Li}(y_{ij}\Phi + \tilde{y}_{ij}\tilde{\Phi})Q_{Rj} + \text{h.c.}$$

- Parity-symmetric scalar potential:

$$\begin{aligned}
V &= V_2 + V_3 + V_4, \\
V_2 &= -\mu_1^2 \text{Tr}(\Phi^\dagger \Phi) - \mu_2^2 [\text{Tr}(\tilde{\Phi} \Phi^\dagger) + \text{Tr}(\tilde{\Phi}^\dagger \Phi)] - \mu_3^2 [\chi_L^\dagger \chi_L + \chi_R^\dagger \chi_R], \\
V_3 &= \mu_4 [\chi_L^\dagger \Phi \chi_R + \chi_R^\dagger \Phi^\dagger \chi_L] + \mu_5 [\chi_L^\dagger \tilde{\Phi} \chi_R + \chi_R^\dagger \tilde{\Phi}^\dagger \chi_L], \\
V_4 &= \lambda_1 \text{Tr}(\Phi^\dagger \Phi)^2 + \lambda_2 [\text{Tr}(\tilde{\Phi} \Phi^\dagger)^2 + \text{Tr}(\tilde{\Phi}^\dagger \Phi)^2] + \lambda_3 \text{Tr}(\tilde{\Phi} \Phi^\dagger) \text{Tr}(\tilde{\Phi}^\dagger \Phi) \\
&\quad + \lambda_4 \text{Tr}(\Phi^\dagger \Phi) [\text{Tr}(\tilde{\Phi} \Phi^\dagger) + \text{Tr}(\tilde{\Phi}^\dagger \Phi)] + \rho_1 [(\chi_L^\dagger \chi_L)^2 + (\chi_R^\dagger \chi_R)^2] + \rho_2 \chi_L^\dagger \chi_L \chi_R^\dagger \chi_R \\
&\quad + \alpha_1 \text{Tr}(\Phi^\dagger \Phi) [\chi_L^\dagger \chi_L + \chi_R^\dagger \chi_R] + \left\{ \alpha_2 [\chi_L^\dagger \chi_L \text{Tr}(\tilde{\Phi} \Phi^\dagger) + \chi_R^\dagger \chi_R \text{Tr}(\tilde{\Phi}^\dagger \Phi)] + \text{h.c.} \right\} \\
&\quad + \alpha_3 [\chi_L^\dagger \Phi \Phi^\dagger \chi_L + \chi_R^\dagger \Phi^\dagger \Phi \chi_R] + \alpha_4 [\chi_L^\dagger \tilde{\Phi} \tilde{\Phi}^\dagger \chi_L + \chi_R^\dagger \tilde{\Phi}^\dagger \tilde{\Phi} \chi_R],
\end{aligned}$$

- $\langle \Phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} \kappa_1 & 0 \\ 0 & \kappa_2 \end{pmatrix}$, $\langle \chi_L \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_L \end{pmatrix}$, $\langle \chi_R \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_R \end{pmatrix}$.
- Introduce: $r \equiv \frac{\kappa_2}{\kappa_1}$, $w \equiv \frac{v_L}{\kappa_1}$.
- Parameter set: $\{\lambda_{1,2,3,4}, \alpha_{1,2,3,4}, \rho_{1,2}, \mu_4, r, w, v_R\}$.

Particle spectrum

Sector	Label
CP-even scalars	h, H_1, H_2, H_3
CP-odd scalars	A_1, A_2
Charged scalars	H_1^\pm, H_2^\pm
Charged gauge bosons	$W_{1\mu}^\pm, W_{2\mu}^\pm$
Neutral gauge bosons	$A_\mu, Z_{1\mu}, Z_{2\mu}$

- SM Higgs: $m_{h,\text{analytic}}^2 \approx v^2 \left(2\lambda_1 - \frac{(\alpha_1 + \alpha_4)^2}{2\rho_1} \right)$.
- Other scalars:

$$m_{H_1}^2 \simeq m_{A_1}^2 \simeq m_{H_1^\pm}^2 \approx \frac{1}{2}(\alpha_3 - \alpha_4)v_R^2,$$

$$m_{H_2}^2 \simeq m_{A_2}^2 \simeq m_{H_2^\pm}^2 \approx \frac{1}{2}(\rho_2 - 2\rho_1)v_R^2,$$

$$m_{H_3}^2 = 2\rho_1 v_R^2, \quad m_{H_2}^2 > m_{H_1}^2.$$

- Gauge bosons: $m_{W_1} = m_W$, $m_{Z_1} = m_Z$, and $m_{W_2, Z_2} \sim \mathcal{O}(v_R)$.

Phenomenological constraints

- Theoretical bounds: perturbativity, unitarity, bounded from below.
- Recent bound on W_2 mass: $m_{W_2} > 5.1 \text{ TeV}$. [Pich et. al. 2023]
- This gives² $v_R > \frac{2m_{W_2}}{g} = 15.7 \text{ TeV}$.
- $hb\bar{b}$ coupling rules out large parameter space, $\kappa_b = 0.98_{-0.13}^{+0.14}$.
- Neutral meson mixing constraint: $m_{H_1} > 15 \text{ TeV}$. [Zhang et. al. 2008]
- Trilinear higgs coupling: ATLAS bound, $\kappa_h = \frac{c_h^3}{c_h^{SM^3}} \in [-2.3, 10.3]$ at 95% CL.

²we take $g_L = g_R = g$

$SU(2)_R \times U(1)_{B-L}$ **breaking phase transition**

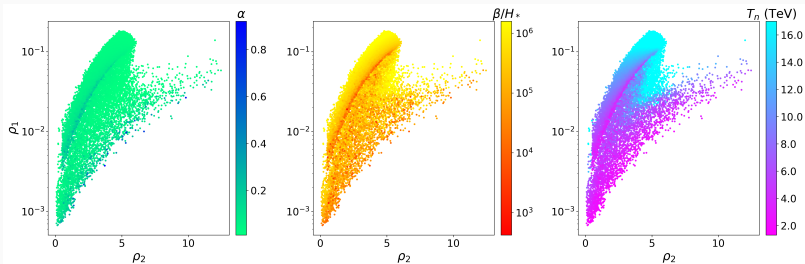
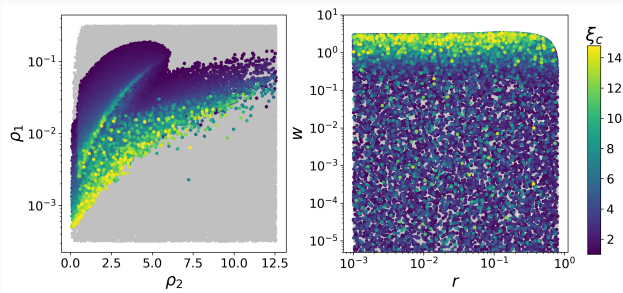
Parameter scan

- For $SU(2)_R \times U(1)_{B-L}$ breaking PT, $V_{\text{eff}} \equiv V_{\text{eff}}(R, T)$.
- $V_{\text{eff}}(R, T) = V_0 + V_{\text{CW}} + V_{\text{c.t.}} + V_{1T} + V_{\text{Daisy}}$
- 'Simple basis': $\lambda_0 \equiv \lambda_1 = \lambda_3 = \lambda_4$, λ_2 , $\alpha_0 \equiv \alpha_1 = \alpha_2 = \alpha_4$.
- Parameter set: $\{\lambda_0, \alpha_0, \rho_1, \rho_2, r, w, v_R\}$.

$$\begin{aligned} \log \alpha_0 &\in [-3, 0], \quad \log \alpha_3 \in [-3, 0], \quad \log \rho_1 \in [-3.5, -0.5], \\ \rho_2 &\in [0, 4\pi], \quad x \equiv \frac{\lambda_2}{\lambda_0} \in [0.25, 0.85], \quad \log r \in [-3, 0], \\ \log w &\in [-6, 1], \quad v_R = 20, 30, 50 \text{ TeV}. \end{aligned}$$

- Filter points using theoretical and experimental bounds.
- Look for FOPT.³ SFOPT condition: $\xi_c \equiv \frac{v_c}{T_c} > 1$.
- For points with SFOPT, compute: α , β/H_* , T_n .

³We used a modified version of CosmoTransitions.

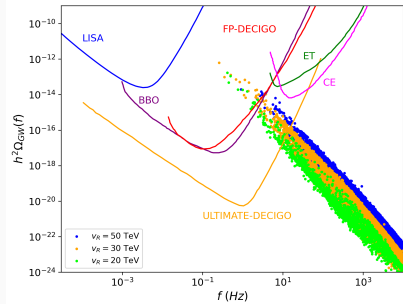
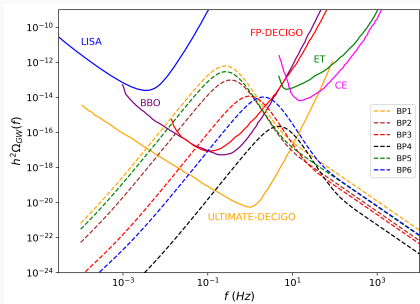


Variation of PT parameters, $v_R = 30$ TeV. SFOPT is for small ρ_1 , and $w \sim \mathcal{O}(1)$.

Gravitational wave background

GW spectra

- Non-runaway scenario: $h^2\Omega_{\text{GW}} \approx h^2\Omega_{\text{sw}} + h^2\Omega_{\text{turb}}$.
- Terminal bubble wall velocity, $v_w \approx 1$.
- $\Omega_{\text{GW}}(f_{\text{peak}}) \propto v_w \left(\frac{H_*}{\beta}\right)^x \left(\frac{\kappa\alpha}{1+\alpha}\right)^y \left(\frac{100}{g_*}\right)^{1/3}$, where $x, y > 0$, κ efficiency factor.



Left: GW spectra for 6 benchmark points. Right: $v_R = 20, 30,$ and 50 TeV.

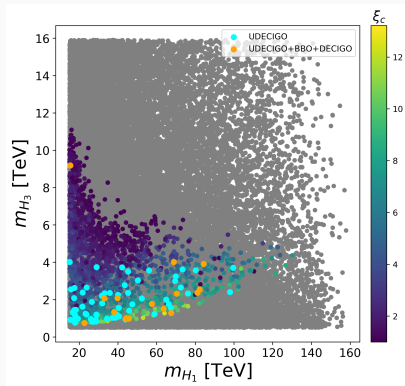
Outlook

Collider signatures

- GW favours $\rho_1 \lesssim \mathcal{O}(10^{-1})$, i.e. light H_3 .
- FCC-hh at $\sqrt{s} = 100$ TeV with $\sigma \sim \mathcal{O}(fb)$ can rule out m_{H_3} upto 2 TeV. [DeV, 2016]
- HE-LHC, CLIC₃₀₀₀, and FCC-hh will improve sensitivity of κ_h to $\sim 20\%$, 10% , and 5% respectively.

$\delta\kappa_h$	20 TeV	30 TeV	50 TeV
> 5%	52%	58%	50%
> 10%	21%	34%	33%
> 20%	8%	20%	25%

Percentage of points detectable at
Ultimate-DECIGO



Detectable points for $v_R = 20$ TeV

Conclusions

- GWs are a promising window to the early universe.
- GWs from $SU(2)_R \times U(1)_{B-L}$ PT, possibly detectable at BBO, FP-DECIGO, Ultimate-DECIGO, for $v_R = 20, 30, 50$ TeV.
- Preference for a light H_3 . Future colliders will be able to rule out m_{H_3} upto a few TeV.
- Preference for $w \sim \mathcal{O}(1) \implies$ pattern of EWSB is different from TLRSB.
- Complementary collider probes for light H_3 , and $\delta\kappa_h$.

Thank You!

Effective potential

- Background field value of the neutral CP-even field, $\chi_{Rr}^0: R$.
- For $SU(2)_R \times U(1)_{B-L}$ breaking PT, $V_{\text{eff}} \equiv V_{\text{eff}}(R, T)$.
- The effective potential is,

$$V_{\text{eff}}(R, T) = V_0 + V_{\text{CW}} + V_{\text{c.t.}} + V_{1T} + V_{\text{Daisy}}$$

$$V_0(R) = -\frac{\mu_3^2}{2} R^2 + \frac{\rho_1}{4} R^4,$$

$$V_{\text{CW}}(R) = \frac{1}{64\pi^2} \sum_i (-1)^{f_i} n_i m_i^4(R) \left[\log \left(\frac{m_i^2(R)}{\mu^2} \right) - c_i \right],$$

$$V_{1T}(R, T) = \frac{T^4}{2\pi^2} \sum_i (-1)^{f_i} n_i J_{b/f} \left(\frac{m_i^2}{T^2} \right),$$

$$V_{\text{Daisy}} = -\frac{T}{12\pi} \sum_i n_i \left((m_i^2(R) + \Pi_i(T))^{3/2} - (m_i^2(R))^{3/2} \right).$$

- $V_{\text{c.t.}}$ is chosen such that the one-loop vev and mass coincide with the tree-level values.

Large T expansion of V_{1T}

$$J_{b/f}(x^2) = \pm \int_0^\infty dy y^2 \log(1 \mp e^{-\sqrt{x^2+y^2}}).$$

For small x^2 ,

$$\begin{aligned} J_f(x^2, n) &= - \frac{7\pi^4}{360} + \frac{\pi^2}{24}x^2 + \frac{1}{32}x^4(\log x^2 - c_f) \\ &\quad - \pi^2 x^2 \sum_{l=2}^n \left(-\frac{1}{4\pi^2}x^2\right)^l \frac{(2l-3)!!\zeta(2l-1)}{(2l)!!(l+1)} \left(2^{2l-1} - 1\right), \\ J_b(x^2, n) &= - \frac{\pi^4}{45} + \frac{\pi^2}{12}x^2 - \frac{\pi}{6}(x^2)^{3/2} - \frac{1}{32}x^4(\log x^2 - c_b) \\ &\quad + \pi^2 x^2 \sum_{l=2}^n \left(-\frac{1}{4\pi^2}x^2\right)^l \frac{(2l-3)!!\zeta(2l-1)}{(2l)!!(l+1)}. \end{aligned}$$

Small T expansion of V_{1T}

For large x^2 , both fermions and bosons have the same expansion,

$$J_{b/f}(x^2, n) = -\exp\left(-x^2\right) \left(\frac{\pi}{2} x^2\right)^{1/2} \sum_{l=0}^n \frac{1}{2^l l!} \frac{\Gamma(5/2+l)}{\Gamma(5/2-l)} (x^2)^{-l/2}.$$

Daisy Resummation

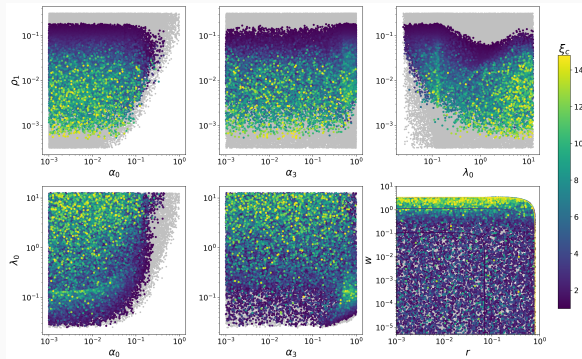
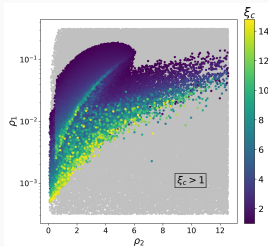
- Particles receive thermal (Debye mass) due to 'hard loops'⁴. Scalars, longitudinal component of gauge bosons and fermions get thermal mass. For $SU(N)$,

$$\Pi^L = g_N^2 T^2 \left[\frac{N}{3} + \frac{1}{6} \sum_s n_s C(r_s) + \frac{1}{12} \sum_f n_f C(r_f) \right].$$

- For N -loop diagrams with $N - 1$ petals, $\Pi_{\text{daisy}} \sim \lambda^N \frac{T^{2N-1}}{\mu^{2N-3}}$.
- Breakdown of perturbativity: At $T_c \sim \frac{\mu}{\sqrt{\lambda}}$, parameter $\alpha \equiv \lambda \frac{T^2}{\mu^2} \sim 1$.
- Resummed contribution from daisy diagrams $\implies m^2 \rightarrow m^2 + \Pi(T)$.
- Effect is to shift $V_T \rightarrow V_T + V_{\text{daisy}}$.
- Generally, perturbation theory can be applied is $\frac{\phi_c}{T_c} \gtrsim 1$.

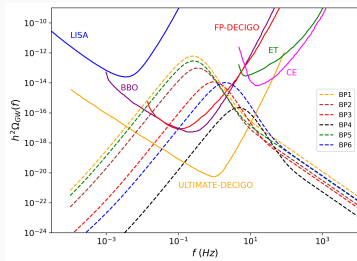
⁴Thesis-Breitbach, 2018

Other projections



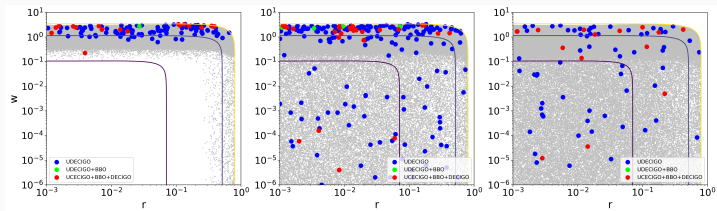
GW Detection

- For detection time t , $\text{SNR} = \sqrt{\tau \int_{f_{\min}}^{f_{\max}} df \left[\frac{\Omega_{\text{GW}}(f)h^2}{\Omega_{\text{sens}}(f)h^2} \right]^2}$
- Signal is detectable if $\text{SNR} > \text{SNR}_{\text{thr}}$.
- Six BPs were identified with high SNR at BBO, FP-DECIGO and Ultimate DECIGO.



GW spectra for the benchmark points

Detectable points in the $r - w$ plane



GW spectra for the benchmark points

H_3 production channels:

1. H_1 -decay, $pp \rightarrow H_1 \rightarrow hH_3$,
2. decay of boosted h , $pp \rightarrow h^* \rightarrow hH_3, H_3H_3$,
3. Higgsstrahlung, $pp \rightarrow V_R^* \rightarrow V_R H_3$,
4. $V_R V_R$ fusion, $pp \rightarrow H_3 jj$.