



Is light neutralino thermal DM ruled out in the PMSSM?

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- Introduction.
 - Low mass ($m_{LSP} < m_{h_{SM}}/2$) DM in SUSY.

1 $\tilde{\chi}_1^0$ LSP: pMSSM

2 If time permits some comments on $\tilde{\chi}_1^0$ LSP in NMSSM

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Credit: I have stolen freely from a very nice set of slides made by Rhitaja Sengupta for a talk.

Talk today is based on these papers focus on $2m_{\tilde{\chi}_1^0} \leq m_h(125)$. :

1) B. Banerjee, R. K. Barman, G. Bélanger, R. Godbole, **R. Sengupta** Phys.Rev.Lett. 131 (2023) 1, 011802 .

2) B. Banerjee, R. K. Barman, G. Bélanger, R. Godbole, **R. Sengupta** e-print: 2312.XXXXXX.

This is the 'final' result. Facilitated by newer data both from the colliders and the direct detection experiments.

But this talk is in some sense an analytic continuation of the earlier talks at Anomalies.

-3) R. K. Barman, G. Belanger, B. Bhattacharjee, R. Godbole, G. Mendiratta and D. Sengupta, [Phys. Rev. D 95 \(2017\) no.9, 095018; 1703.03838](#);

-2) R. K. Barman, G. Belanger, B. Bhattacharjee, R. Godbole, D. Sengupta and X. Tata, [2006.07854, Phys. Rev. D 103, \(2021\) 015029](#);

Talk at the first Anomalies conference.

-1) R. K. Barman, G. Bélanger, R. Godbole, 'Low mass LSP in SUSY' , Review : [Eur.Phys.J.ST 229 \(2020\) 21, 3159-3185](#),

Talk at the second Anomalies conference.

This whole work is an analytic continuation of sorts of work which I had started around 2000/2001.

G. Belanger, F. Boudjema, F. Donato R. M. Godbole and S. Rosier-Lees, Nucl. Phys. B **581**, 3 (2000) [hep-ph/0002039]

G. Belanger, F. Boudjema, A. Cottrant, R. M. Godbole and A. Semenov, Phys. Lett. B **519**, 93 (2001) [hep-ph/0106275]

D. Albornoz Vasquez, G. Belanger, R. M. Godbole and A. Pukhov, Phys. Rev. D **85** (2012) 115013,[arXiv:1112.2200 [hep-ph]].

G. Belanger, G. D. La Rochelle, B. Dumont, R. M. Godbole, S. Kraml and S. Kulkarni, Phys. Lett. B **726** 773 (2013) [arXiv:1308.3735 [hep-ph]]

Many of us grew up in the period where SUSY was the 'standard BSM' and the Lightest Supersymmetric Particle (LSP) was the most attractive, Weakly Interacting Massive Particle as the candidate for the DM. .

But [LHC](#) results have put the idea of 'natural' SUSY under stress and the [XENON-1T](#), [PandaX \(4T\)](#), [LZ](#) results have put the WIMP paradigm under stress.

Experimental constraints on masses of various sparticles from the LHC

These then translate into constraints on parameters of the SUSY models : most of the parameters are related to SUSY breaking!

Many SUSY breaking mass parameters are constrained to have very high values.

One mass that is still allowed to be 'low' is the lightest neutralino $\tilde{\chi}_1^0$

Lightest Neutralino in the MSSM

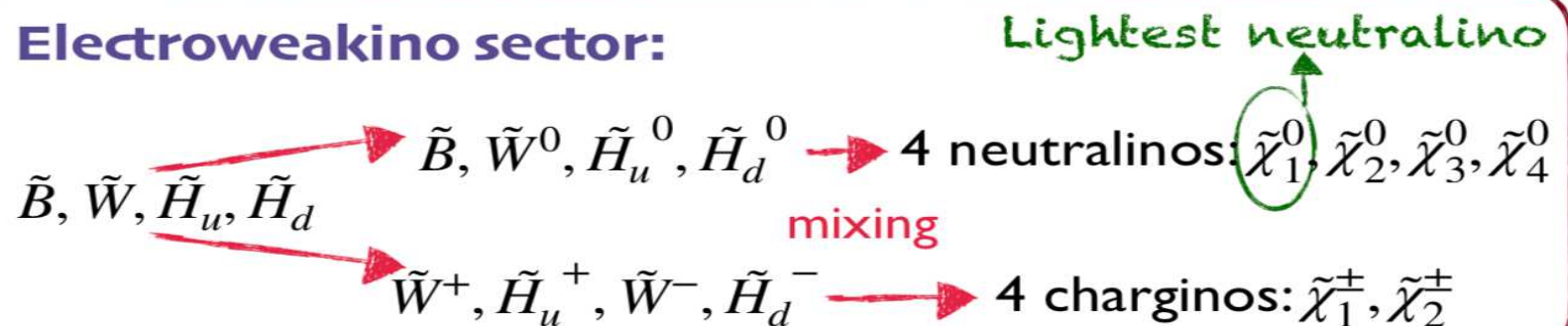
**Extending SM
to MSSM**

Higgs sector: 2 Higgs doublets in MSSM: H_u, H_d
5 Higgs bosons: h, H, A, H^\pm

Supersymmetry (SUSY):

Weyl fermion \leftrightarrow complex scalar fermions \leftrightarrow sfermions
 complex scalar \leftrightarrow Weyl fermion Higgs bosons \leftrightarrow higgsinos
 gauge bosons \leftrightarrow Weyl fermion gauge bosons \leftrightarrow gauginos

Electroweakino sector:



Among the multitude of SUSY breaking parameters only four are relevant for determining the masses and the couplings of the $\tilde{\chi}$ (ElectroWeakino sector) at tree level:

SUSY breaking gaugino masses M_1, M_2 and Higgs sector parameters (supersymmetric) μ and $\tan \beta$. At loop levels some of the parameters of the t, \tilde{t} sector as well become relevant.

For the neutralino sector it is diagonalisation of a four by four matrix and for the chargino sector that of a two by two matrix.

In general LHC constraints on the Electro Weakinos are the weakest.

Run-II data $35fb^{-1}$.

Higgsino upto 390 GeV ruled out. G. Pozzo et al. Phys. Lett. B, 789:582–591, 2019. arXiv: 1807.01476 : Pure Wino upto 650 GeV ruled out (CMS data). These used W/Z 's decaying into leptons Leptonic final states

Latest from analysis of hadronically decaying boosted bosons ATLAS, Phys. Rev. D, 104 (2021) 112010. with Wino mass limits going upto 1060 GeV (Higgsino upto 900 GeV), for LSP lighter than 400 (200) GeV. Need large mass difference with the LSP.

Critically evaluate the case of a light LSP (in general light EW sector). That is the subject of my talk: A light LSP ($2m_{\tilde{\chi}_1^0} < m_{h125}$)

Why does a theorist find the idea of a light $\tilde{\chi}_1^0$ attractive?

In a world where there might be some underlying high scale relations between SUSY breaking parameters, the sparticles in the EW sector are generally among the lightest because of the smaller strength of the couplings which affect their running.

Even with all the strong sparticles at very high scale, it is possible to have a light EW sector and 'have natural' SUSY in the sense of Tata and Baer.

Essentially boils down to 'small' values of μ , which is after all NOT a SUSY breaking parameter.

Is there a cosmological limit on how light a CDM particle can be?

C. Boehm et al. J. Phys. G, 30:279–286, 2004. arXiv: astro-ph/0208458; C. Boehm, T.A. Ensslin, and J. Silk, J. Phys. G, 30:279–286, 2004, C. Boehm et al. JCAP, 08:041, 2013. arXiv: 1303.6270

Using PLANCK limit on N_{eff} ; effective number of ν species: masses for CDM as small as \sim MeV and less than a few GeV $\tilde{\chi}_1^0$ (neutralino in SUSY) can be allowed.

For latest constraints from 511 KeV line, see for example:

P. De la Torre Luque, S. Balaji and J. Silk, “New 511 keV line data provides strongest sub-GeV dark matter constraints,” [arXiv:2312.04907 [hep-ph]].

We summarised the situation in:

"Status of low mass LSP in SUSY"

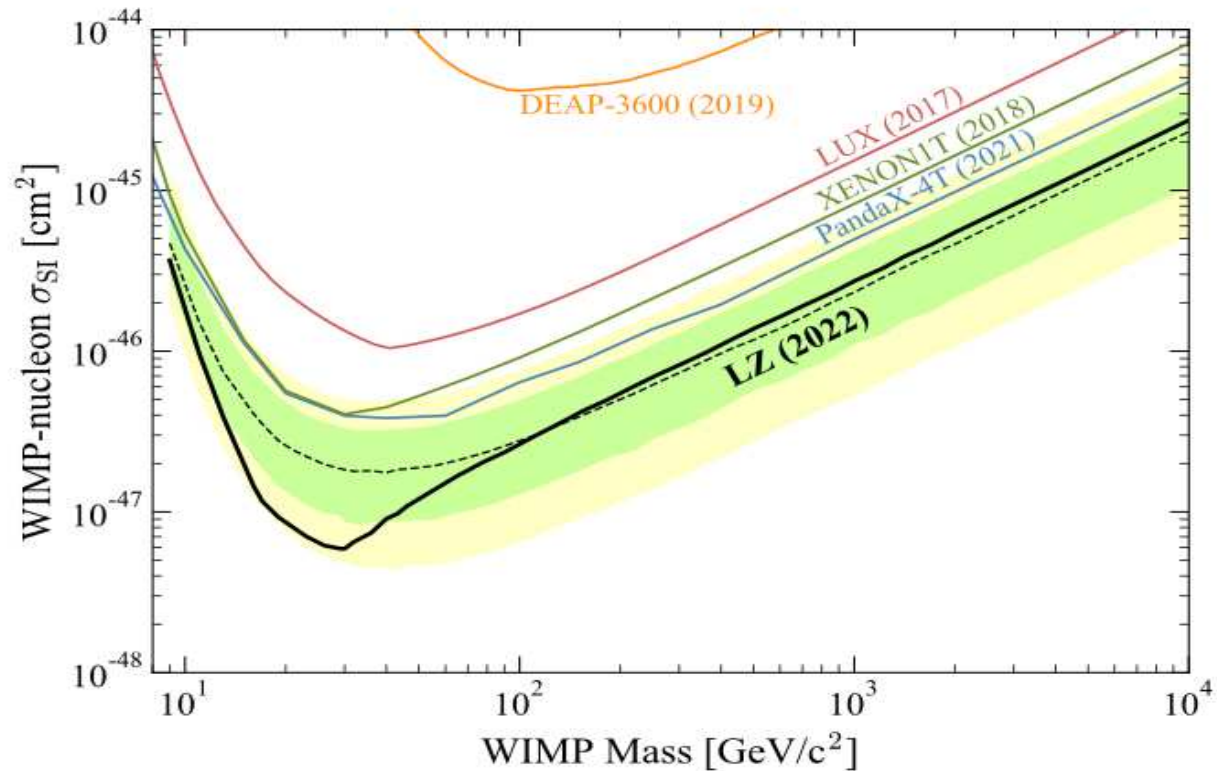
Eur. Phys. J. ST **229**, no.21, 3159-3185 (2020), [arXiv:2010.11674 [hep-ph]] **and references therein**

Question to ask:

How light can a SUSY LSP candidate be and still be a viable DM candidate?

What is meant by that?

- It should not over close the Universe. (If we assume standard cosmology and hence thermal relic)
- Should be allowed the Direct/Indirect detection constraints.



This is data from only the first 60 days of exposure for LZ. It is the most stringent limit is set for spin-independent scattering at **30 GeV**, excluding cross sections above $5.9 \times 10^{-48} \text{ cm}^2$ at the 90% confidence level.

The relic density calculations and also the DM detection cross-sections in a model will depend on the couplings of the DM with the SM particles!

In pMSSM the $\tilde{\chi}_1^0$ is a mixture of Higgsino and Gauginos .

The extent of this mixing decides couplings of the $\tilde{\chi}_1^0$ with all the SM and MSSM particles.

The mixing depends on relative values of M_1, M_2 and μ .

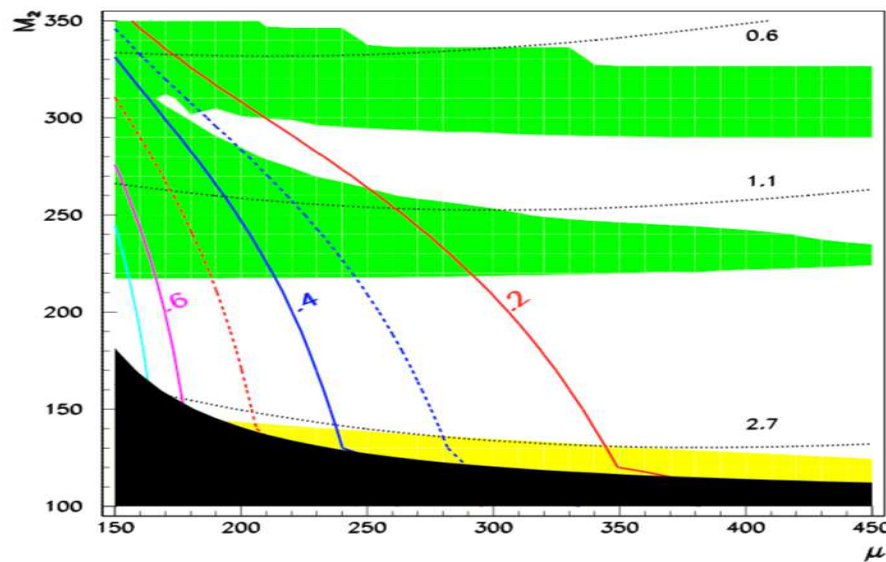
Limits on Wino masses force M_2 to be higher. A light, mixed $\tilde{\chi}_1^0$ means similar order of magnitude for M_1 and μ .

A Wino like or Higgsino like $\tilde{\chi}_1^0$ will have to be heavy (\sim TeV) to explain the observed relic due to the high cross-sections. How a model can produce a wino like LSP is a different question.

A bino-like $\tilde{\chi}_1^0$ means too high a relic density unless additional annihilation possibilities exist because of its smaller couplings!

t-channel light slepton OR a resonant annihilation via Higgs/A/Z. The Z exchange requires a nontrivial Higgsino fraction too in the neutralino! The so called 'well tempered neutralino'.

For the Higgsino-Bino well tempered relic, h_{125} can have appreciable branching fraction into invisible neutralino pair. In fact this was the focus of our early papers! G. Belanger, F. Boudjema, F. Donato R. M. Godbole and S. Rosier-Lees, Nucl. Phys. B **581**, 3 (2000)



Green : Relic < 0.1 , White:
 $0.1 < \text{relic} < 0.3$, yellow :
 relic > 0.3

Phys. Lett. B 519 (2001) 93-102 "The MSSM invisible Higgs in the light of dark matter and $g-2$ "

Till the DM detection experiments came in full swing the collider bounds dominated the story. In cMSSM the LEP constraint on $m_{\tilde{\chi}_1^\pm}$ and universal gaugino mass would rule out light $\tilde{\chi}_1^0$. So a light $\tilde{\chi}_1^0$ necessarily means **non universal gaugino masses**. Focus moved to the **pMSSM**

G. Belanger, F. Boudjema, F. Donato R. M. Godbole and S. Rosier-Lees, Nucl. Phys. B **581**, 3 (2000), Phys. Lett. B 519 (2001) 93-102.

Before Xenon 1T and LHC results, older relic measurements:
Lower limit of 30 GeV on the mass of the $\tilde{\chi}_1^0$.

L. Calibbi, T. Ota, Y. Takanishi, JHEP 07, 013 (2011), D.A. Vasquez, G. Belanger, C. Boehm, Phys. Rev. D 84, 095015 (2011), G. Belanger, G. D. La Rochelle, B. Dumont, R. M. Godbole, S. Kraml and S. Kulkarni, Phys. Lett. B **726** 773 (2013)

A light LSP can contribute to the 'invisible' decay of the Higgs.

Invisible decay of the Higgs can also be searched for at the LHC:

E.g. : R. M. Godbole, M. Guchait, K. Mazumdar, S. Moretti and D. P. Roy (2003), Phys. Lett. B **571**; D. Ghosh, R. Godbole, M. Guchait, K. Mohan and D. Sengupta, Phys. Lett. B **725**, arXiv:1211.7015 [hep-ph] (2013)

Current best limit from the LHC is $\tilde{13}\%$. [ATLAS-CONF-2020-008](#) and $\tilde{14.5}\%$
[ATLAS: submitted to JHEP, 2202.07953](#)

Future for looking for this 'dark' higgs is 'bright'.

LHC can reach 'invisible' BR upto 3.8%

ILC/CLIC/FCC can reach upto 0.2-0.4 %

In the current situation different possibilities to look for light $\tilde{\chi}_1^0$ in SUSY:

1) Look for Mono events or LLP. Not effective for light LSP.

2) Look for invisibly decaying Higgs.

3) Direct production of the heavier Electroweakino states ($\tilde{\chi}_1^\pm \tilde{\chi}_2^0$ etc) and their decays. WZ mediated and WH mediated decays of heavier charginos and neutralinos.

Now we have

- 1) precise determination of relic,
- 2) strong constraints from Direct Detection
- 3) LEP/LHC searches for electroweakinos
- 4) **Measurements of Higgs X-sections and branching ratios.**
- 5) precision calculations of the Higgs mass.
- 6) measurements of the invisible width of the Higgs.

What is the situation now?

How low a mass can a viable DM candidate have in SUSY consistent with all the current exclusions? Can the future colliders probe these 'light' LSP's? Ie. can we rule out this region from collider experiments? Using phenomenology of the heavier electro weakinos.

Can models and observed relic density support a light SUSY DM particle if reported in either Direct or Indirect detection experiment? If yes what can the LHC (current, HL/LHC and HE/LHC) say about it?

Will discuss:

pMSSM : The weakest LHC constraints from non observation are on the mass of the $\tilde{\chi}_1^0$. The important parameters are μ, M_1, M_2 and $\tan \beta$. Radiative corrections bring in dependence on A_t, m_t . and even M_3 .

Results from

B. Bhattcharjee, R. Barman, Rhitaja Sengupta, RG Phys.Rev.Lett. 131 (2023) 1, 011802, e-Print: 2207.06238 [hep-ph]; e-print 2312.XXXXX

1) Make sure given point is allowed by a variety of current constraints: LHC constraints, LEP constraints, flavour constraints coming from B sector, Higgs sector constraints.

2) Calculate the invisible branching ratio for the Higgs.

3) Calculate the expected 'direct detection cross-sections.

4) Calculate the relic density for the given point.

Calculate $\xi = \Omega_{cal} h^2 / \Omega_{obs} h^2 = \Omega_{cal} h^2 / 0.122$

$\xi \leq 1$: Thermal DM

The pMSSM Parameter Space

10 parameters scanned

Slepton masses fixed at 2 TeV

1st and 2nd generation squark masses fixed at 5 TeV

M_1 bino mass
 M_2 wino mass
 μ higgsino mass
 $\tan\beta$ ratio of vevs
 M_A pseudoscalar mass

$$\begin{aligned}
 &30 \text{ GeV} < M_1 < 100 \text{ GeV}, \quad 1 \text{ TeV} < M_2 < 3 \text{ TeV}, \\
 &100 \text{ GeV} < |\mu| < 2 \text{ TeV}, \quad 2 < \tan\beta < 50, \\
 &100 \text{ GeV} < M_A < 5 \text{ TeV}, \quad 3 \text{ TeV} < M_{\tilde{Q}_{3L}} < 20 \text{ TeV}, \\
 &3 \text{ TeV} < M_{\tilde{t}_R} < 20 \text{ TeV}, \quad 3 \text{ TeV} < M_{\tilde{b}_R} < 20 \text{ TeV}, \\
 &-20 \text{ TeV} < A_t < 20 \text{ TeV}, \quad 2 \text{ TeV} < M_3 < 5 \text{ TeV}, \\
 &M_{\tilde{Q}_{1,2L}} = M_{\tilde{u}_{1,2R}} = M_{\tilde{d}_{1,2R}} = 5 \text{ TeV}, \quad A_{u/d/c/s/b} = 0, \\
 &M_{\tilde{L}_{1,2,3L}} = M_{\tilde{e}_{1,2,3R}} = 2 \text{ TeV}, \quad A_{e/\mu/\tau} = 0.
 \end{aligned}$$

$M_{\tilde{Q}_{3L}}, M_{\tilde{t}_R}, M_{\tilde{b}_R}$
 3rd generation squark mass
 A_t stop trilinear coupling
 M_3 gluino mass

Both $\mu > 0$ and $\mu < 0$ scenarios studied separately

Particle spectrum generated using FeynHiggs 2.18.1

LEP constraints.

invisible decay of Z-boson
from new physics

$$\Gamma_{\text{inv}}^{\text{new}} < 2 \text{ MeV}$$

ALEPH, DELPHI, L3, OPAL, [Phys. Rept. 427 \(2006\) 257–454](#)

chargino mass

$$m_{\chi_1^\pm} > 103 \text{ GeV}$$

OPAL, [EPJC 35, 1–20 \(2004\)](#)

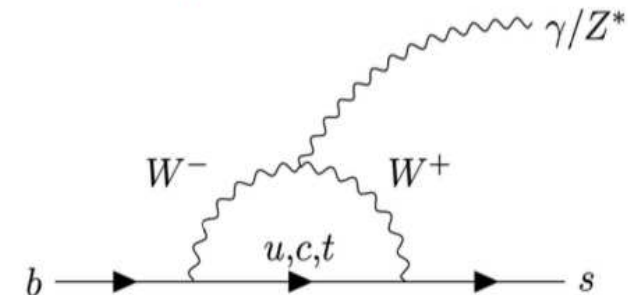
cross-section of associated production
of neutralinos in final states with jets

$$\sigma(e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0) \times \text{Br}(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 + \text{jets}) \\ + \sigma(e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_3^0) \times \text{Br}(\tilde{\chi}_3^0 \rightarrow \tilde{\chi}_1^0 + \text{jets}) < 0.1 \text{ pb}$$

OPAL, [EPJC 35, 1–20 \(2004\)](#)

Flavour constraints.

- ***** Rare processes in SM
- ***** Might receive contribution from MSSM
- ***** Precise measurement of the branching of these processes constrain the MSSM parameter space



$$3.00 \times 10^{-4} < \text{Br}(b \rightarrow s\gamma) < 3.64 \times 10^{-4}$$

HFLAV, [Eur. Phys. J. C 77, 895 \(2017\)](#)

$$1.66 \times 10^{-9} < \text{Br}(B_s \rightarrow \mu^+ \mu^-) < 4.34 \times 10^{-9}$$

CMS & LHCb, [Nature 522, 68–72 \(2015\)](#)

$$0.78 < (\text{Br}(B \rightarrow \tau\nu))_{\text{obs}} / (\text{Br}(B \rightarrow \tau\nu))_{\text{SM}} < 1.78$$

Belle, [PRD 82, 071101\(R\)](#)

Current Constraints on the Parameter Space

Higgs constraints

Observed Higgs mass

$$122 \text{ GeV} < m_h < 128 \text{ GeV}$$

FeynHiggs 2.18.1

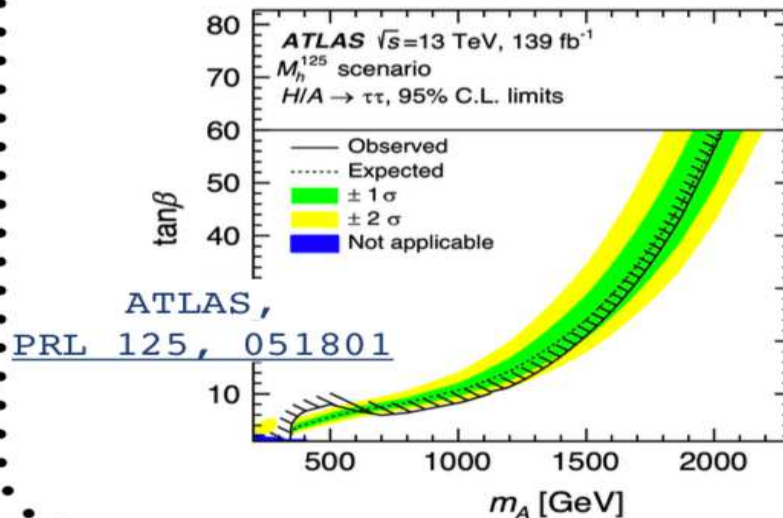
Higgs signal strength

$$\mu = \frac{(\text{Production}_{\text{mode}} \times \text{Branching}_{\text{mode}})_{\text{obs}}}{(\text{Production}_{\text{mode}} \times \text{Branching}_{\text{mode}})_{\text{SM}}}$$

HiggsSignal 2.6.2

Heavy Higgs searches

HiggsBounds 5.10.0



Invisible decay of the Higgs Boson

$$\text{Br}(h \rightarrow \text{invisible}) < 0.11$$

ATLAS, [ATLAS-CONF-2020-052](#)

Current Constraints on the Parameter Space

Electroweakino constraints

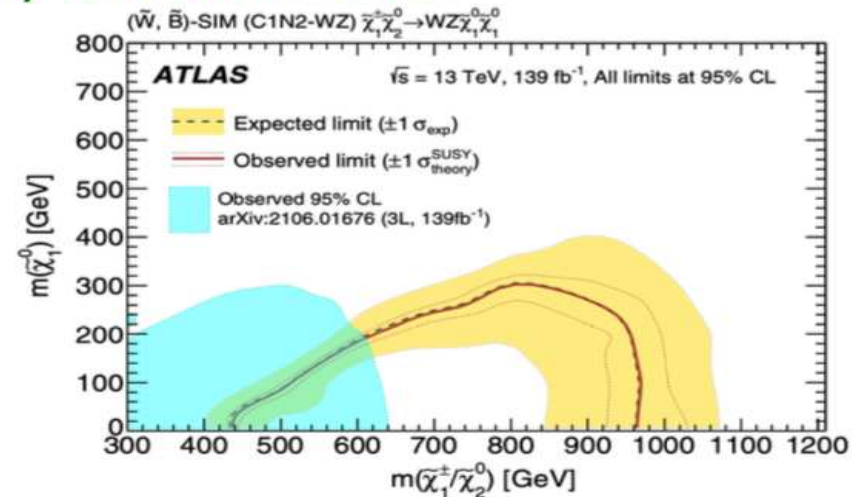
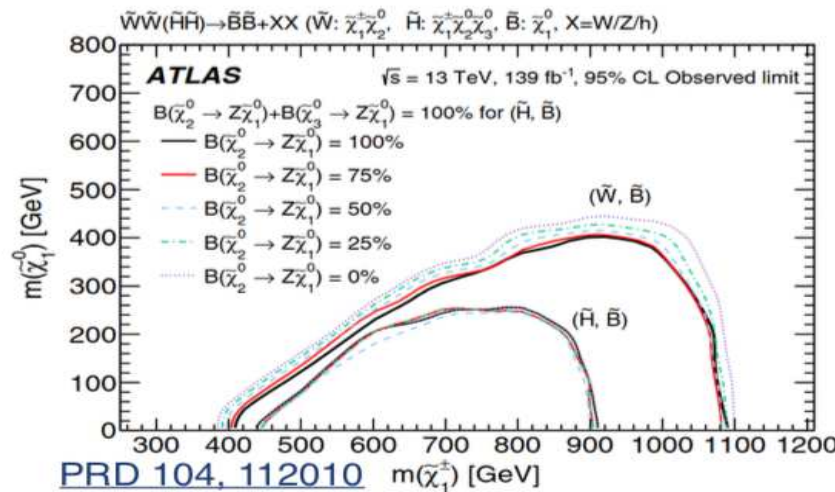
results of direct searches for chargino and neutralino at the ATLAS and CMS experiments of the LHC

$$\begin{aligned}
 PP &\rightarrow \tilde{\chi}_1^\pm \tilde{\chi}_2^0 / \tilde{\chi}_1^\pm \tilde{\chi}_3^0 \\
 \tilde{\chi}_1^\pm &\rightarrow W^\pm \tilde{\chi}_1^0 \\
 \tilde{\chi}_2^0 / \tilde{\chi}_3^0 &\rightarrow (Z/h) \tilde{\chi}_1^0
 \end{aligned}$$

Leptonic decay modes of $W/Z/h$: being cleaner have been used in the past, like $3l + MET$ analysis
 Low branching - sensitive to lighter NLSPs

Recently, hadronic final states are also being analysed

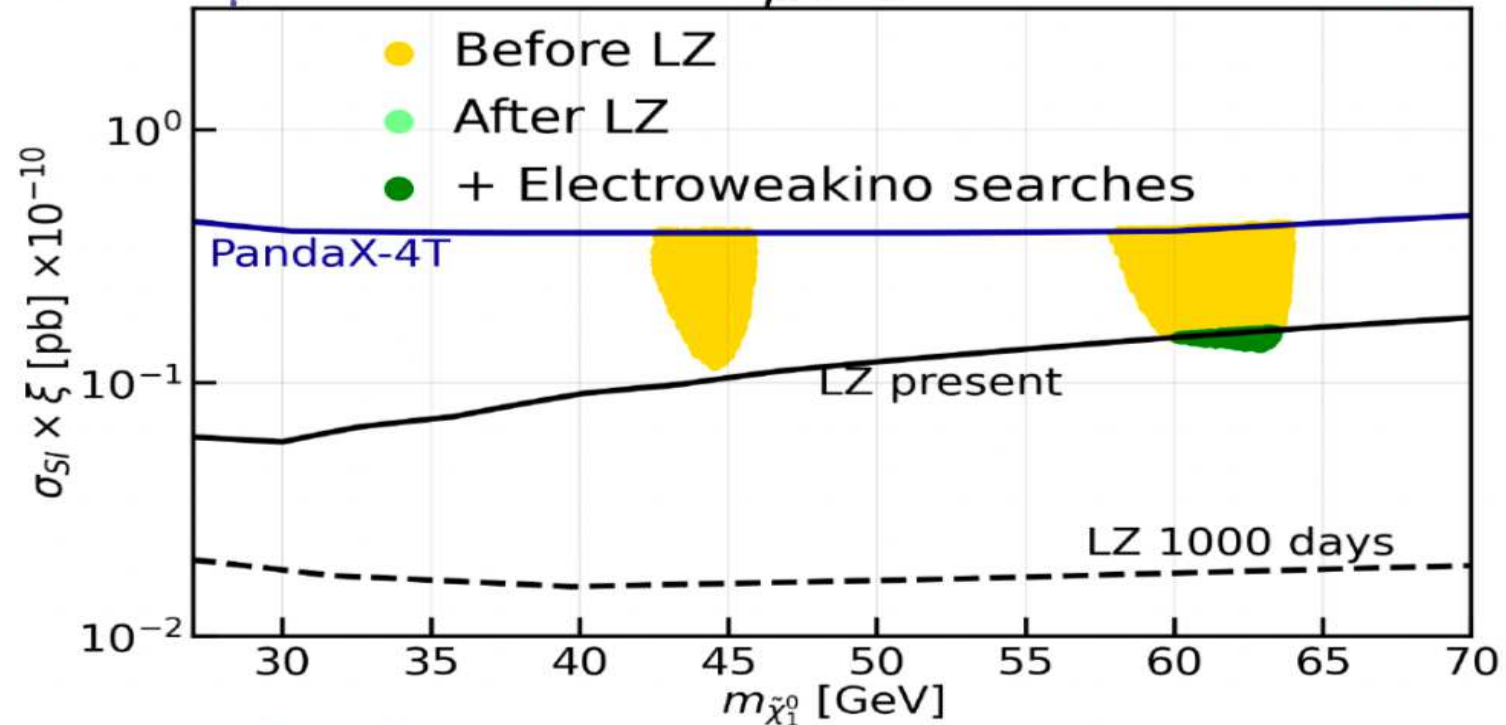
⇒ increase sensitivity to heavier NLSPs



The Positive μ Scenario

Rahool K. Barman, Genevieve Belanger, Biplob Bhattacharjee, Rohini M. Godbole, RS, [arXiv: 2207.06238 \[hep-ph\]](https://arxiv.org/abs/2207.06238), PRL 131 (2023) 1, 011802

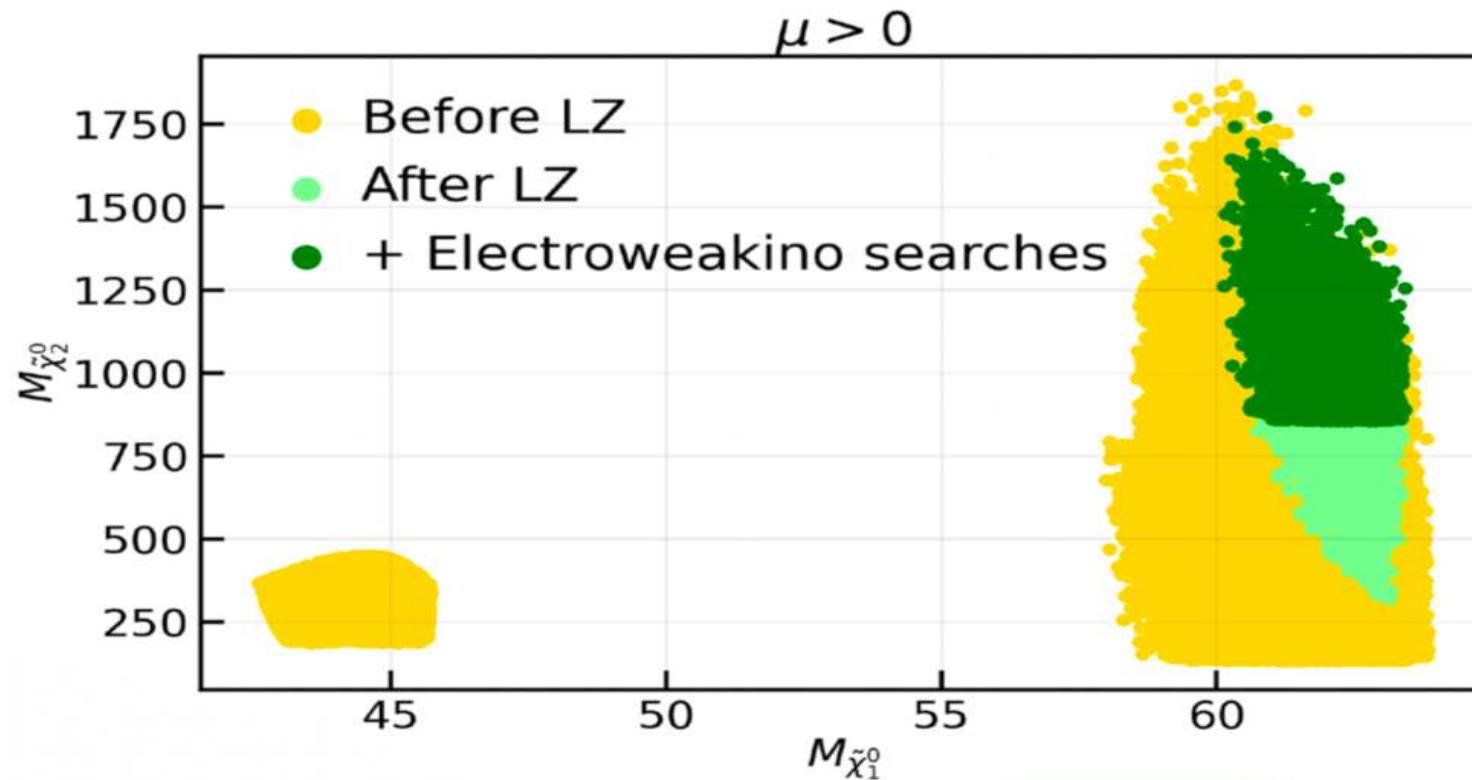
Spin-independent DD Limit $\mu > 0$



DD limits restrict allowed parameter space to Z and h funnel regions since here relic density can be satisfied even with smaller coupling due to resonance enhancement

Before LZ: constraints from LEP, flavor, Higgs constraints, relic density and the DD experiments **XENON-1T**, **PICO-60** and **PandaX-4T**

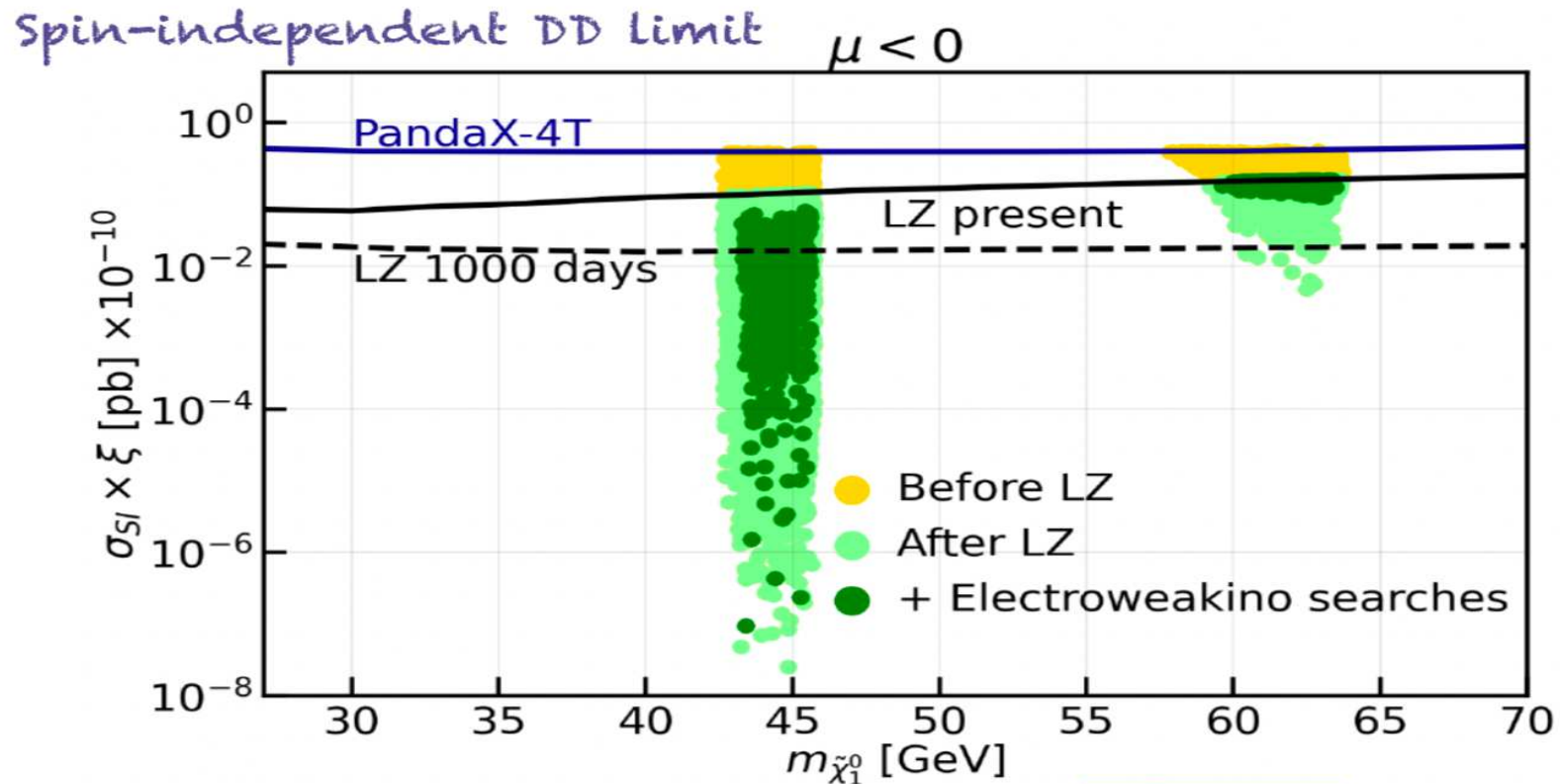
The Positive μ Scenario



Higgsinos heavier than
 ~ 850 GeV allowed from
 electroweakino searches

Before LZ: constraints from LEP,
 flavor, Higgs constraints, relic density
 and the DD experiments **XENON-1T**,
PICO-60 and **PandaX-4T**

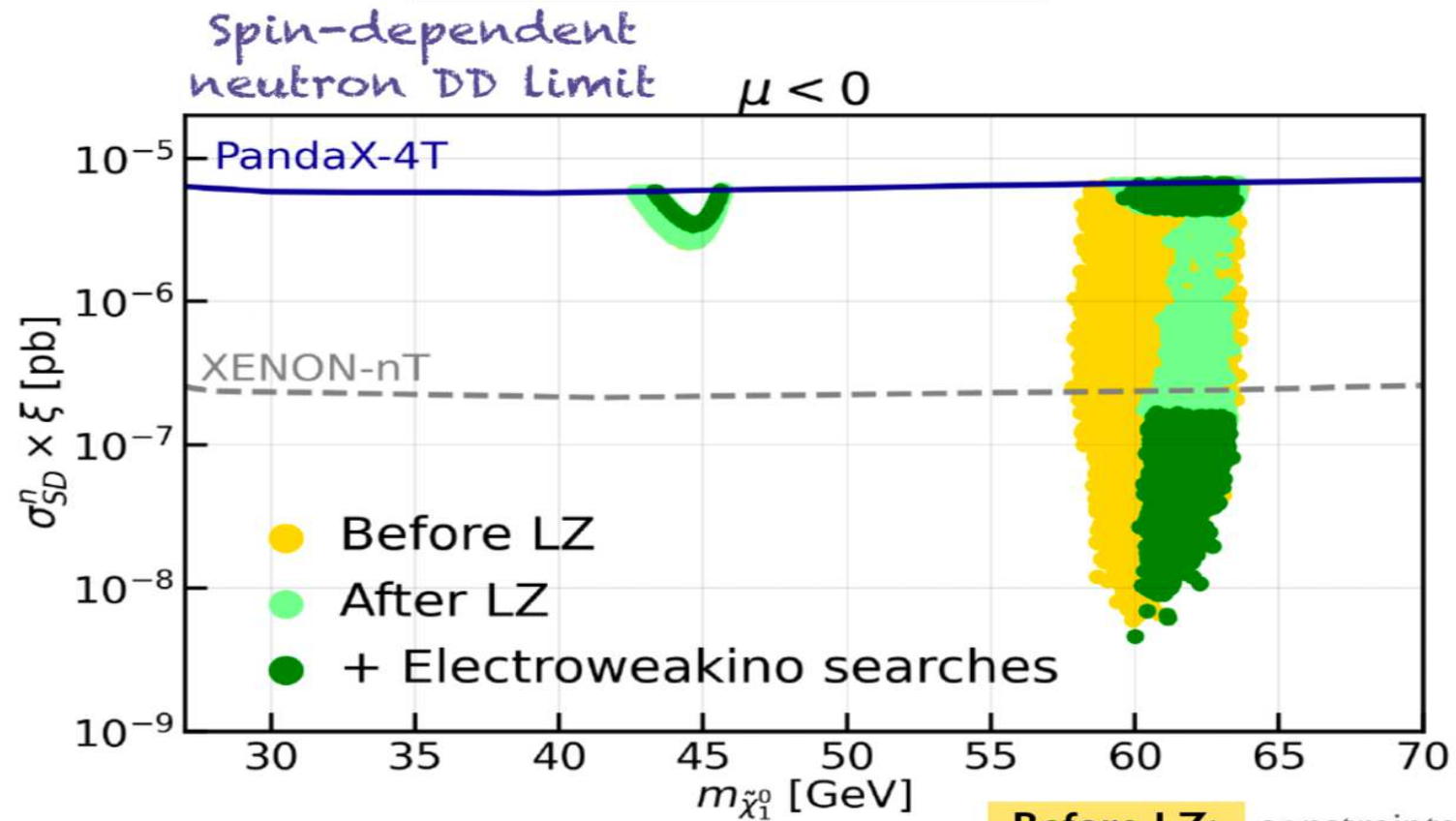
The Negative μ Scenario



Allowed regions in both Z and h funnels
 h -funnel well within the reach of the full
 LZ data

Before LZ: constraints from LEP, flavor, Higgs constraints, relic density and the DD experiments **XENON-1T**, **PICO-60** and **PandaX-4T**

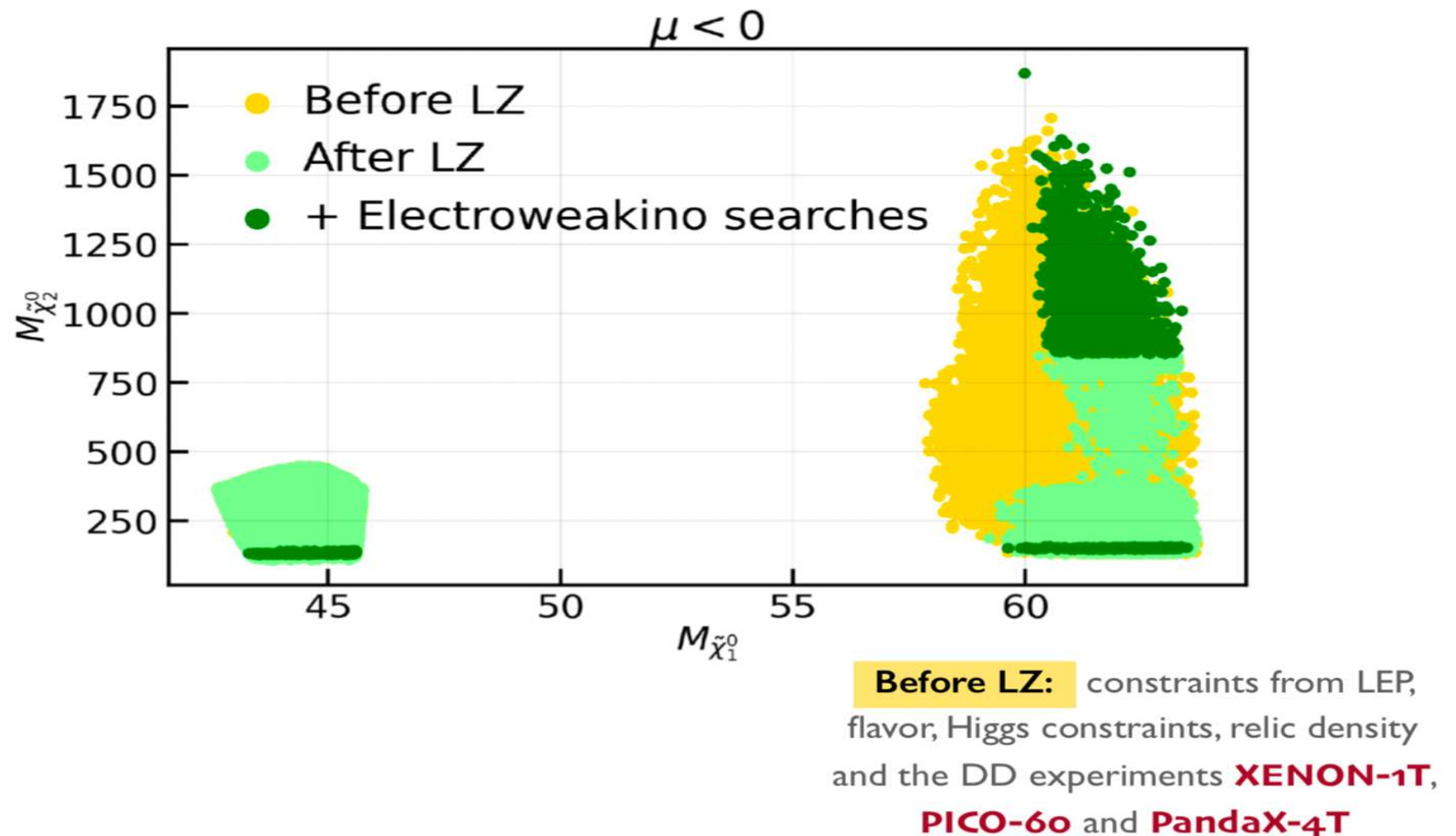
The Negative μ Scenario



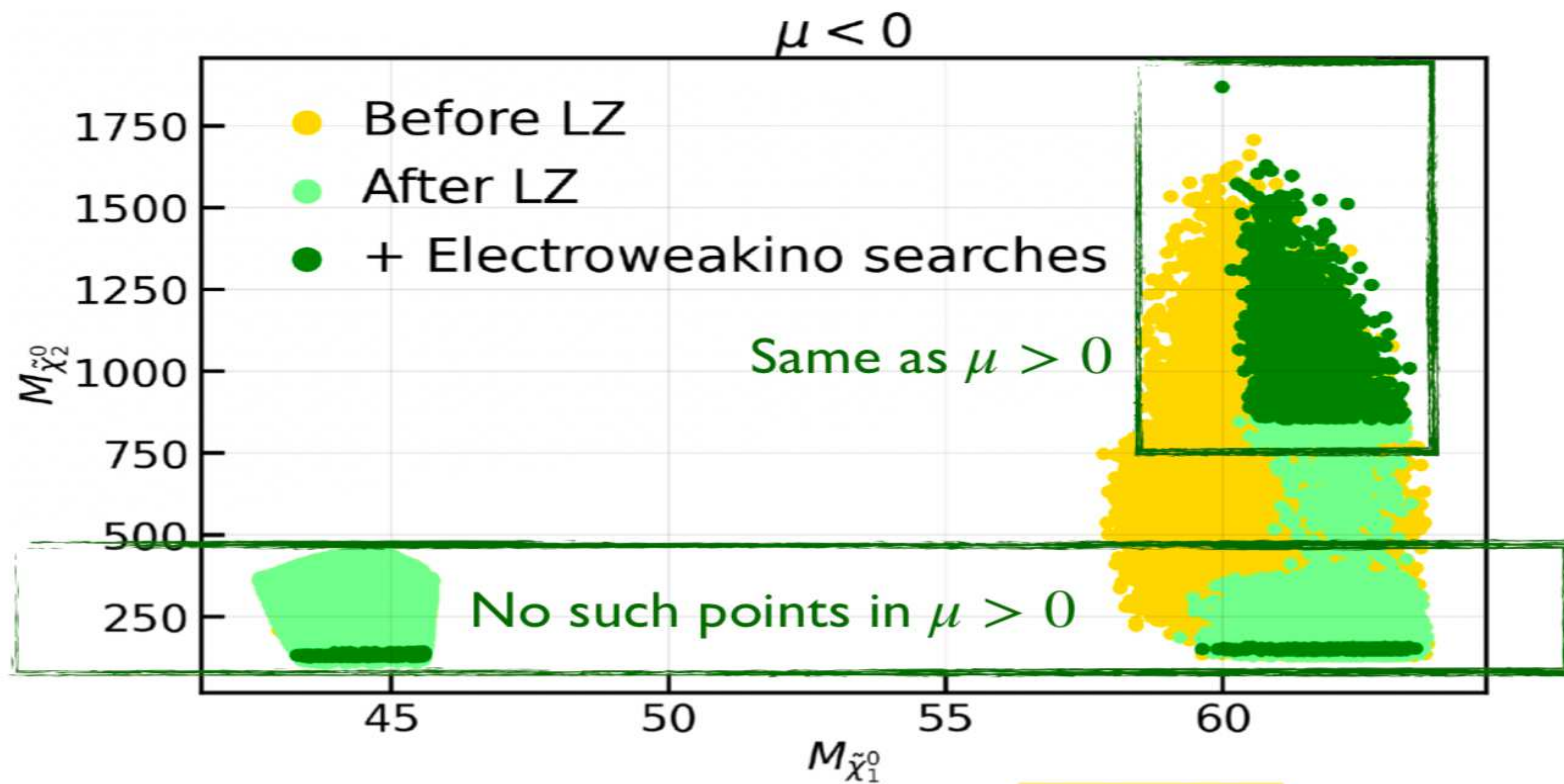
Z-funnel well within the reach of
XENON-nT data

Before LZ: constraints from LEP, flavor, Higgs constraints, relic density and the DD experiments **XENON-1T**, **PICO-60** and **PandaX-4T**

The Negative μ Scenario



The Negative μ Scenario



Before LZ: constraints from LEP, flavor, Higgs constraints, relic density and the DD experiments **XENON-1T**, **PICO-60** and **PandaX-4T**

Light higgsinos still allowed by electroweakino searches?

Light higgsinos survive in the region where

$$M_{\tilde{\chi}_1^\pm/\tilde{\chi}_2^0/\tilde{\chi}_3^0} - M_{\tilde{\chi}_1^0} \approx M_Z$$

Performed an analysis with leptonic final states using **XGBOOST**

Signal significance of 3.6 (1.5) with 20% (50%)
systematic uncertainty with 137 fb^{-1} of data at 14 TeV

Could be probed with upcoming analyses of the Run-2 data
which have not yet been implemented in **SModelS**
or in the **Run-3 of LHC**

Experimental collaborations need to focus on this region of
light higgsinos to **provide a conclusive statement about
their present status.**

Light higgsinos: impact of LZ dependent on the sign of μ

LZ limits the SI DD cross-section

Both h and H contribute to this

$\mu > 0$

 $\tan\beta$ enhanced

 $\mu < 0$
when $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0} < 0$

These contributions **constructively interfere** for down type quarks

These contributions **destructively interfere** for down type quarks

Even for same $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0}$ coupling, the SI DD cross-section increases for $\mu > 0$ and decreases for $\mu < 0$ for high $\tan\beta$

(scaled with the relic density)

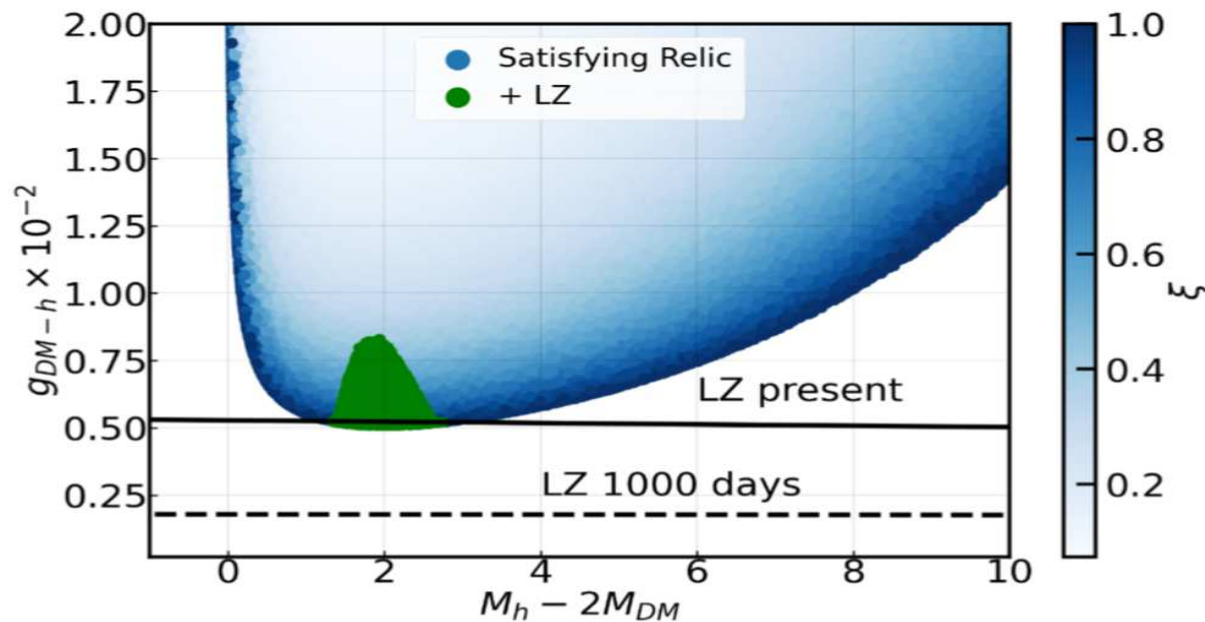
Relic density depends on $g_{Z\tilde{\chi}_1^0\tilde{\chi}_1^0}$ in Z -funnel and $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0}$ in h -funnel

ALLOWED POINTS IN $\mu < 0$ WITH LIGHT HIGGSINOS

Heavy higgsinos in the h -funnel

- Heavy higgsino have low values of couplings of LSP with Z and h
 - relic density condition not satisfied
- In h -funnel, extra handle of $\tan\beta$
 - relic satisfied only for low $\tan\beta$ where coupling is high
- Effect of H not important

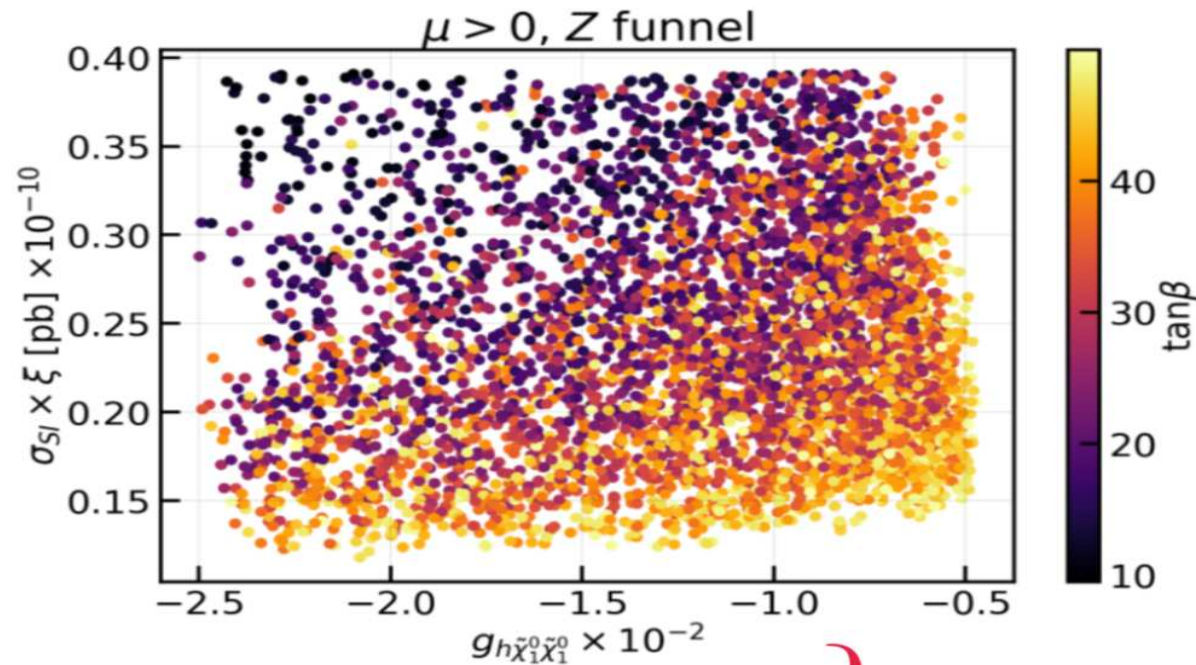
Similar to any Majorana fermion coupled to only h



**ALSO STRONGLY
CONSTRAINED**

Can be probed with few
more days of LZ data

The Z-funnel for $\mu > 0$



Low $\tan\beta$: High magnitude of $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0}$

High $\tan\beta$: Low magnitude of $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0}$,

but added contribution from $g_{H\tilde{\chi}_1^0\tilde{\chi}_1^0}$

Taking into account 20% theoretical uncertainty in relic density - a small allowed region opens up after LZ

Z-FUNNEL
EXCLUDED BY LZ

EXCLUDED BY
ELECTROWEAKINO SEARCHES

1) What is the impact of theoretical uncertainties on the calculation of relic density.

Small additional allowed region opens up but still within the reach of future runs of LZ, Xenon-nT and LHC-run3.

2) Impact of lighter sparticles? The only one which can be light and can impact the results is a light $\tilde{\tau}$. Affects the relic results by about 25% and also the branching ratios of the Higgsinos in our XGBOOST analysis at the LHC.

The analysis of allowed regions is nontrivial. But we have just finished it. Again very small region at low masses is allowed and LHC-run3 should be able to cover it.

ii) NMSSM (Additional singlet higgs superfield) : In addition to above additional parameters related to this extra field. Additional light (pseudo)scalars. $\kappa, \lambda, A_\kappa, A_\lambda$.

iii) PMSSM + $\tilde{\nu}_R$

iv) NMSSM + $\tilde{\nu}_R$

Will tell mainly about (ii).

For NMSSM it is a mixture of higgsinos and gauginos as well as a singlino. The scalars are also doublet-singlet mixtures.

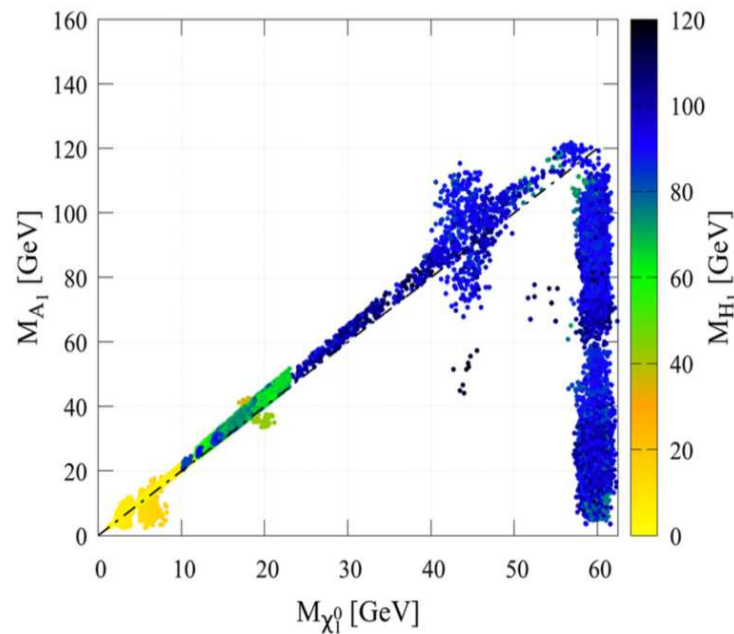
The extent of this mixing decides couplings of the $\tilde{\chi}_1^0$ with all the SM and NMSSM particles.

For case of $\tilde{\nu}_R$ LSP additional Yukawa couplings may come into play.

NMSSM superpotential extended from MSSM by adding terms $\lambda \hat{S} \hat{H}_u \cdot \hat{H}_d + \frac{\kappa}{3} \hat{S}^3$

Now the neutralino mass matrix is five dimensional. There is one more neutral fermion : the singlino. The LSP is a superposition of all the five.

Has one more pseudoscalar and scalar in addition to the MSSM Higgses. Thus in principle two 'lighter states A_1, H_1 become available for resonant annihilation. Thus additional annihilation channels become possible.



h_2 identified with the observed SM-like Higgs. Possibility of a light singlet dominated h_1, a_1 lighter than 122 GeV.

$\tilde{\chi}_1^0$ Singlino or Bino dominated. Anihilations through a_1, h_1 provide the right relic No co-annihilations for our choice . Only resonance annihilations.

Along the line $2M_{\tilde{\chi}_1^0} = m_{a_1}$. Away from this it is the h_1 which provides efficient annihilation.

R. K. Barman, G. Bélanger, B. Bhattacharjee, R. Godbole, D. Sengupta and X. Tata, Phys. Rev. D **103**, no.1, 015029 (2021)

So in NMSSM a light LSP is easily accommodated.

Question: Light A_1, H_1 obtained with low values of κ, λ . Is that natural?

Our LSP is mostly singlino. Difficulty to search for a mixed, light LSP region.

Plan to do first a simplified model analysis and then perhaps go back to NMSSM again to understand it.

The current experiments, especially the recent results from the electroweakino searches at the LHC and the LZ dark matter DD experiment have squeezed the allowed parameter space.

1) regions of heavy higgsinos very close to being probed by few days of LZ data

OR

2) very low mass higgsinos (and low mass right handed stau) which can be targeted at the Run-3 of LHC with dedicated analyses to be sensitive in this narrow gap.

How much further up can we extend the limit of 62.5 GeV on the mass of the LSP in pMSSM?

In NMSSM a light LSP is allowed. Only thermal scenario studied. Direct detection, LHC searches and invisible branching ratio of the Higgs all offer probes of the scenario. (The analysis needs to be redone with LZ limits!)

pMSSM extended with a $\tilde{\nu}_R$: a light $\tilde{\nu}_R$ still possible. Characteristic signals. (Detailed recent analyses are not available)

We can see that this WIMP paradigm for a light LSP in pMSSM and NMSSM can be tested at the HL/HE LHC, ILC/CEPC and DD experiments.