

# Inclusive decay of $\tau$ into hadrons

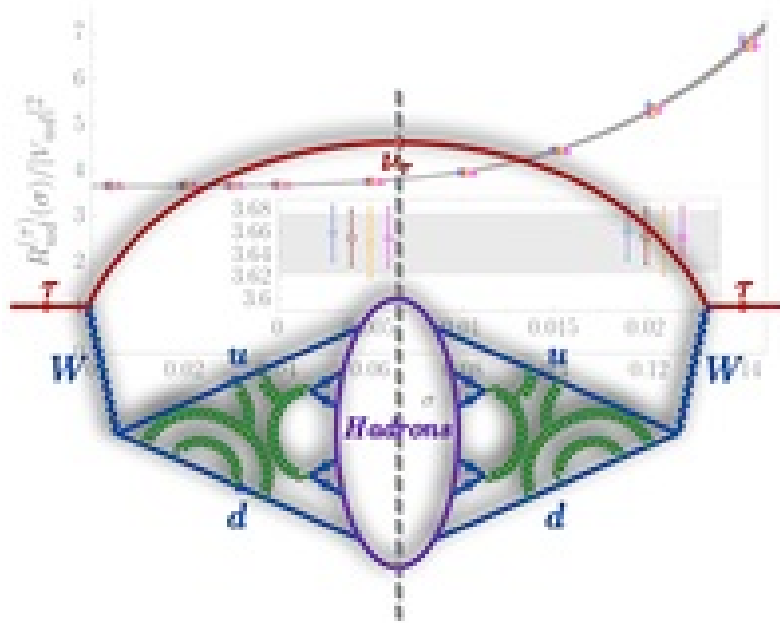
## EDITORS' SUGGESTION

### Inclusive hadronic decay rate of the $\tau$ lepton from lattice QCD

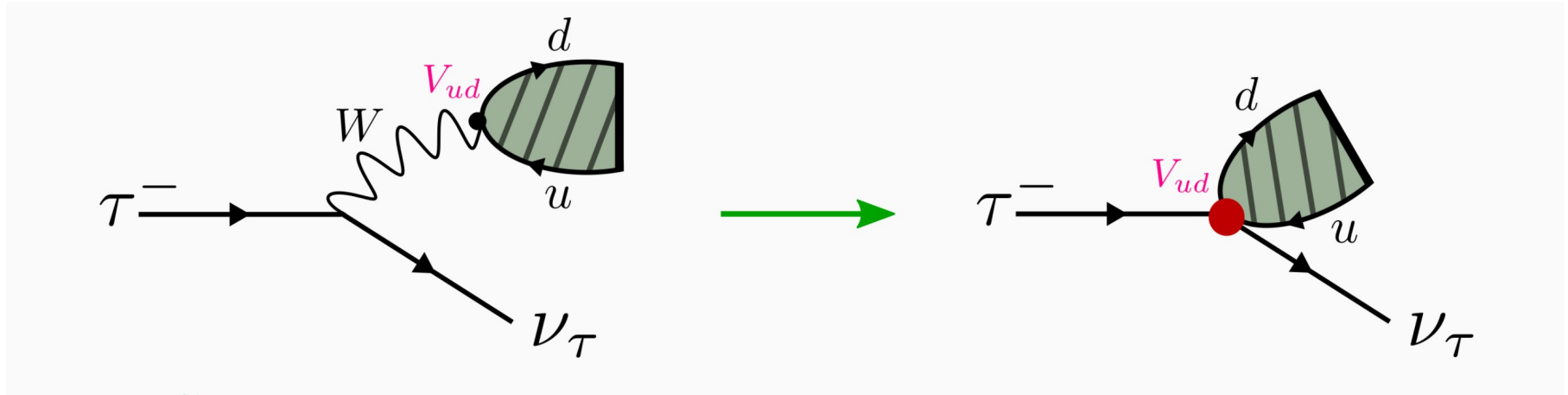
The authors express the inclusive hadronic decay rate of the tau lepton as an integral over the spectral density of the two-point correlator of the weak  $V - A$  hadronic current which they compute fully nonperturbatively in lattice QCD. In a lattice QCD computation with all systematic errors except for isospin breaking effects under control, they then obtain the CKM matrix element  $V_{ud}$  with subpercent errors showing that their nonperturbative method can become a viable alternative to superallowed nuclear beta decays for obtaining  $V_{ud}$ .

A. Evangelista *et al.*

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# The process at LO in electroweak theory



We go directly for the rate

$$\sum X_{ud} \left| \tau^- \xrightarrow{p_\tau} \nu_\tau \xrightarrow{p_\nu} \begin{array}{c} d \\ \text{---} \\ u \end{array} \xrightarrow{V_{ud}} q \right|_2 = \frac{1}{2m_\tau} 2\text{Im} \tau^- \xrightarrow{p_\tau} \begin{array}{c} d \\ \text{---} \\ u \end{array} \xrightarrow{V_{ud}} q \xrightarrow{p_\nu} \begin{array}{c} d \\ \text{---} \\ u \end{array} \xrightarrow{V_{ud}} q \xrightarrow{p_\tau} \tau^-$$

The equation shows the sum of the squared amplitudes for the LO process,  $\sum X_{ud} \left| \tau^- \xrightarrow{p_\tau} \nu_\tau \xrightarrow{p_\nu} \begin{array}{c} d \\ \text{---} \\ u \end{array} \xrightarrow{V_{ud}} q \right|_2$ , is equal to  $\frac{1}{2m_\tau} 2\text{Im} \tau^- \xrightarrow{p_\tau} \begin{array}{c} d \\ \text{---} \\ u \end{array} \xrightarrow{V_{ud}} q \xrightarrow{p_\nu} \begin{array}{c} d \\ \text{---} \\ u \end{array} \xrightarrow{V_{ud}} q \xrightarrow{p_\tau} \tau^-$ . The diagrams show the tau minus decaying into a neutrino tau and a quark  $q$ , and the neutrino tau decaying into a quark  $q$  and a tau minus. The quark  $q$  is shown as a loop of  $d$  and  $u$  quarks, with vertices labeled  $V_{ud}$ .

The rate involves two form factors

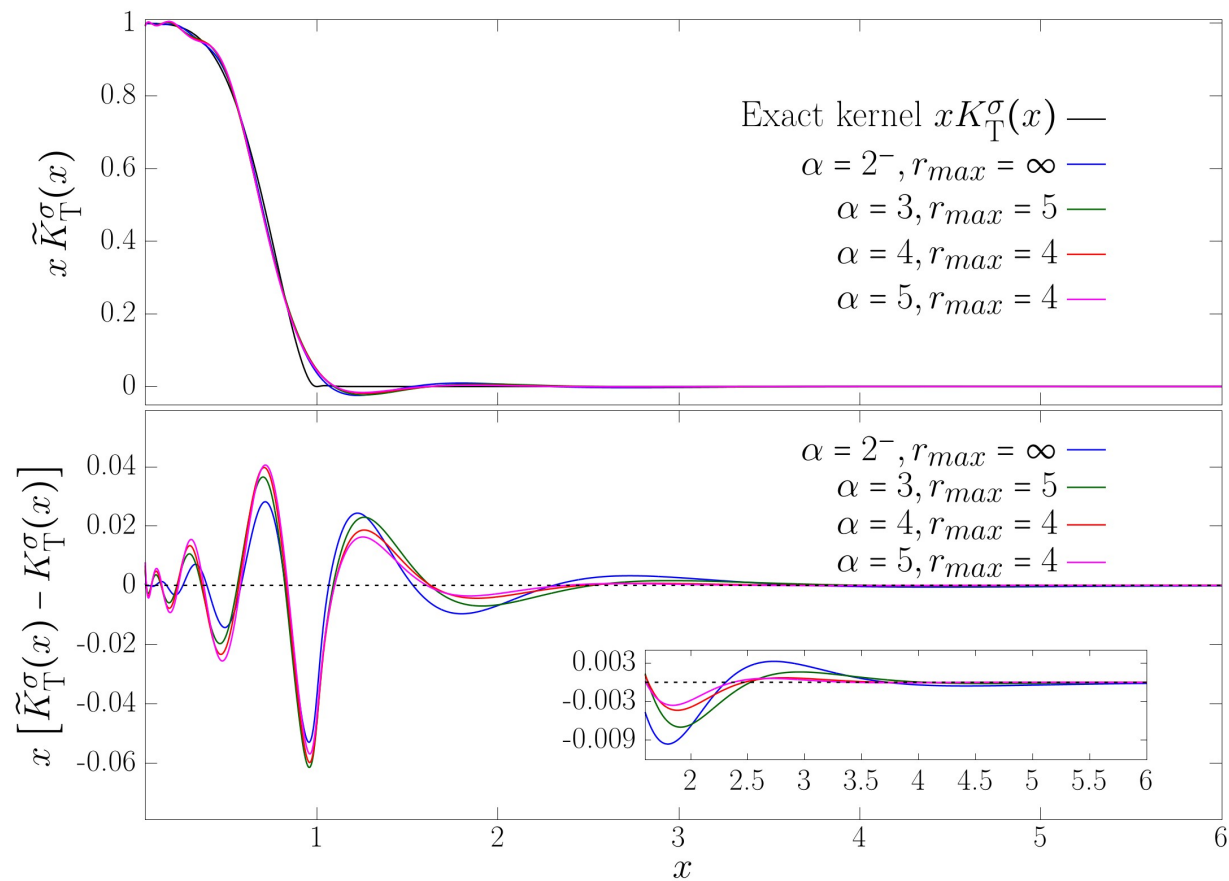
$$\begin{aligned} R_{ud}^{(\tau)} &= 6\pi S_{EW} |V_{ud}|^2 \int_0^1 ds (1-s)^2 \left[ (1+2s) \rho_T(s) + \rho_L(s) \right] \\ &= 12\pi S_{EW} \frac{|V_{ud}|^2}{m_\tau^3} \int_0^\infty dE \left[ K_T \left( \frac{E}{m_\tau} \right) E^2 \rho_T(E^2) + K_L \left( \frac{E}{m_\tau} \right) E^2 \rho_L(E^2) \right] \end{aligned}$$

To be extracted from longitudinal/transverse correlation function of EW currents

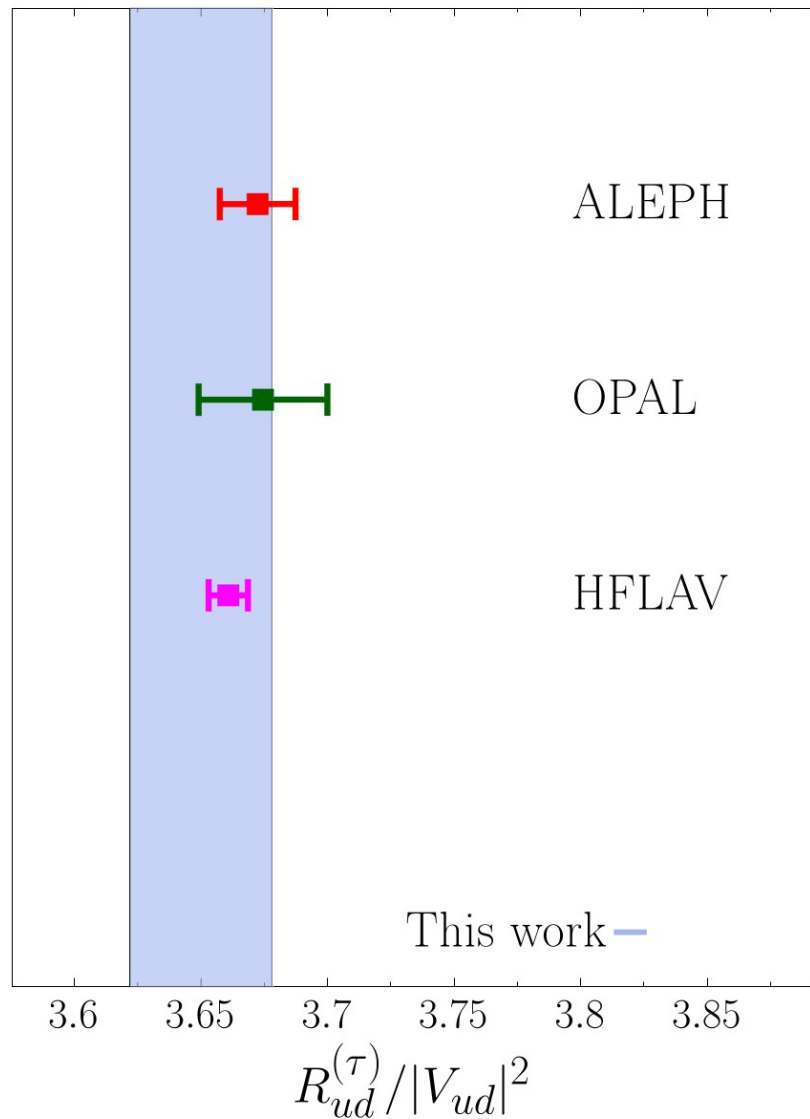
$$C_L(t) \equiv C^{00}(t, \mathbf{0}) = \int_0^\infty \frac{dE}{2\pi} e^{-Et} \rho_L(E^2) E^2$$

$$C_T(t) \equiv \frac{1}{3} C^{ii}(t, \mathbf{0}) = \int_0^\infty \frac{dE}{2\pi} e^{-Et} \rho_T(E^2) E^2$$

# Transverse kernel reconstructed via HLT



Allows to extract  $V_{ud}$   
Not competitive with  
nuclear decay  
approach  
But ok, independent



# Novelty: the $us$ channel

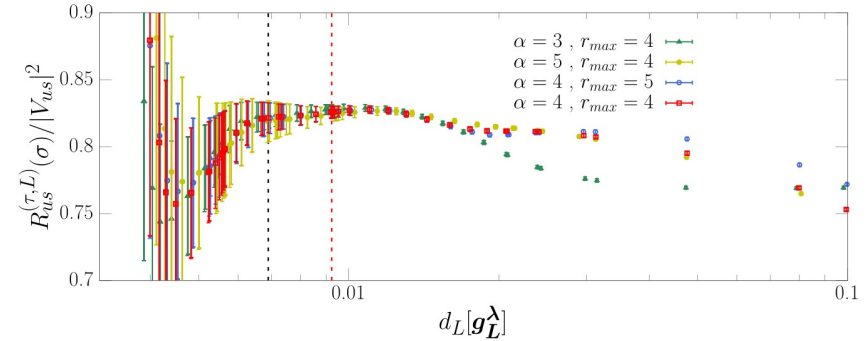
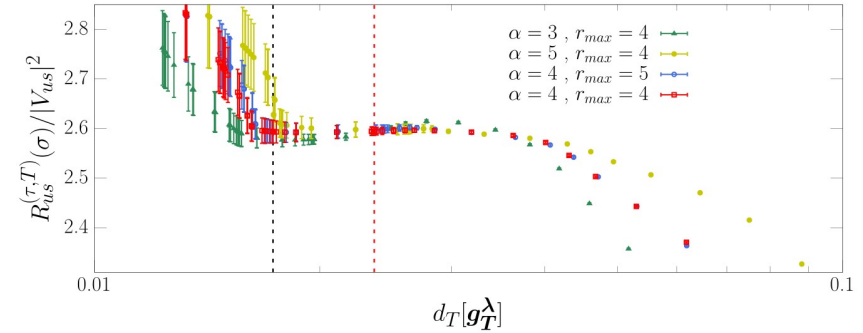
$$R_{us}(\sigma) = 12\pi S_{EW} |V_{ud}|^2 \int_0^\infty \frac{dE E^2}{m_\tau^3} \left\{ K_T^\sigma \left( \frac{E}{m_\tau} \right) \rho_T(E^2) + K_L^\sigma \left( \frac{E}{m_\tau} \right) \rho_L(E^2) \right\}$$

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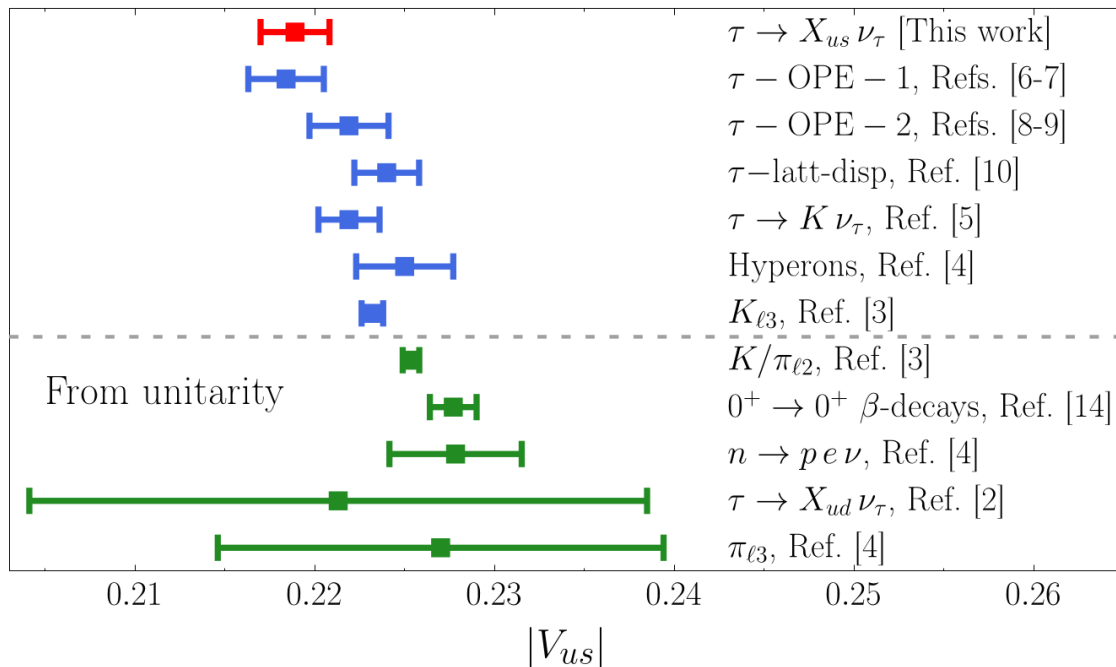
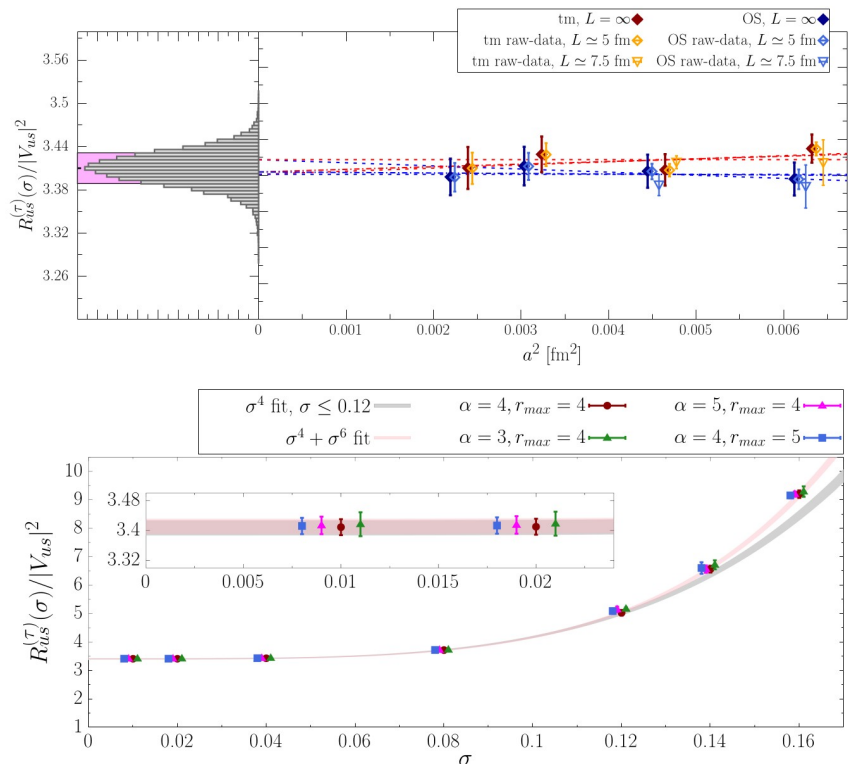
## Inclusive Hadronic Decay Rate of the $\tau$ Lepton from Lattice QCD: The $\bar{u}s$ Flavor Channel and the Cabibbo Angle

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(Extended Twisted Mass Collaboration)



# Two regularizations, four lattice spacings, yeah, a complete work!



DONE

*Thank  
you!*