

# Discussion on the future of form factor computations

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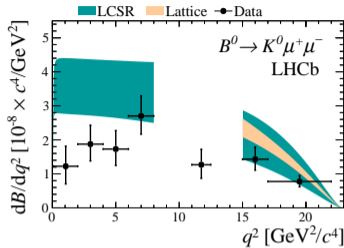
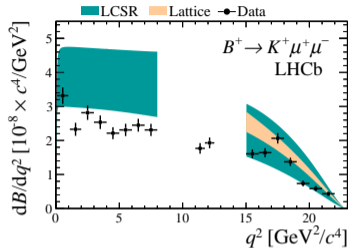


Lattice@CERN 2024  
19/7/2024

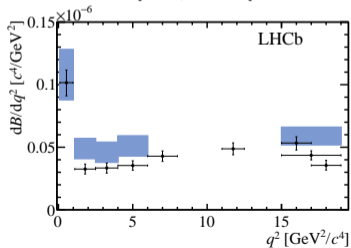


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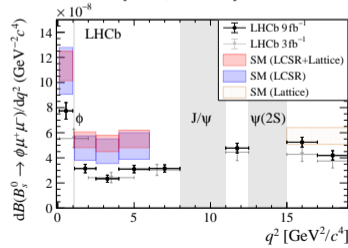
# B-ANOMALIES



$B^+ \rightarrow K^+$  [LHCb, JHEP 14]



$B^0 \rightarrow K^0$  [LHCb, JHEP 14]



$B^0 \rightarrow K^{*0}$  [LHCb, JHEP 16]

$B_s \rightarrow \phi$  [LHCb, PRL 21]

- most recent LHCb measurements of  $b \rightarrow s l^+ l^-$  branching fractions
- low- $q^2$ : LCSR
- high- $q^2$ : lattice
- experiment consistently lower than theory, particularly at low  $q^2$
- can we improve this picture with lattice?

EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH (CERN)



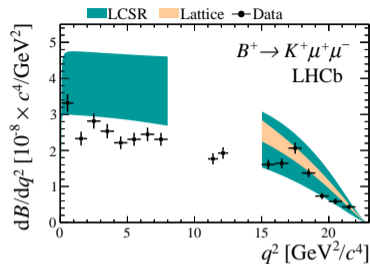
CERN-PH-EP-2013-137  
LHCb-PAPER-2013-039  
4 September 2013

Observation of a resonance in  
 $B^+ \rightarrow K^+ \mu^+ \mu^-$  decays at low recoil

[LHCb, PRL 13]

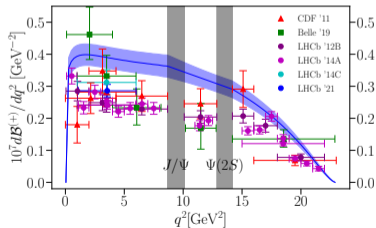
The contribution of the  $\psi(4160)$  resonance in the low recoil region, taking into account interference with the non-resonant  $B^+ \rightarrow K^+ \mu^+ \mu^-$  decay, is about 20% of the total signal. This value is larger than theoretical estimates, where the  $c\bar{c}$  contribution is  $\sim 10\%$  of the vector amplitude, with a small correction from quark-hadron duality violation [23]. Results presented in this Letter will play an important role in controlling charmonium effects in future inclusive and exclusive  $b \rightarrow s \mu^+ \mu^-$  measurements.

# B-ANOMALIES

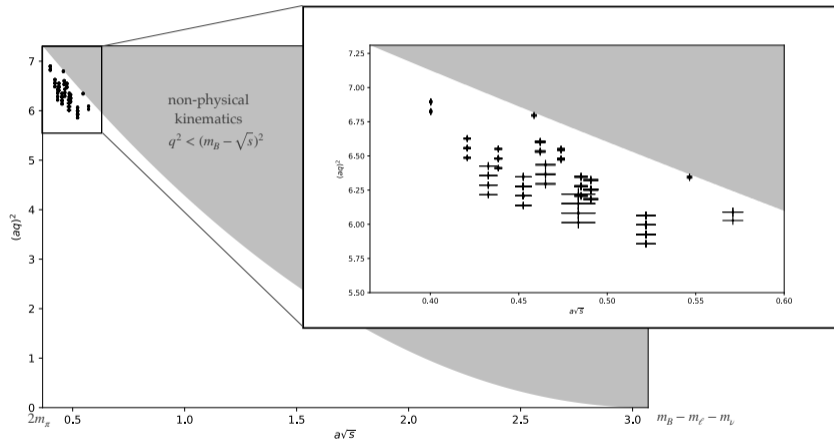


- progress with pseudoscalar final states
- 2021 HPQCD lattice calculation  $B \rightarrow K \ell^+ \ell^-$
- Results down to  $q^2 = 0$
- tensions with LHCb  $B^+ \rightarrow K^+ \mu^+ \mu^-$  in the low- $q^2$  region as high as  $4.2\sigma$

$B^+ \rightarrow K^+$  [LHCb, JHEP 14]

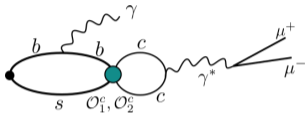


$B^0 \rightarrow K^+$  [Parrot, Bouchard, Davies, PRD 21]



- FV energies for Luka's  $B \rightarrow \pi\pi\ell\nu$  calculation
- no 4-quark  $H_W$ , no charmonium resonances like in  $B \rightarrow K^*\ell^+\ell^-$
- reach to  $q^2 = 0$  significantly harder

## Other Contributions - Charming Penguins



- Of the contributions we have not computed directly, the most significant one at large  $q^2$  is expected to be that from the operators  $O_{1,2}^c$  (charming penguins) and we are working on developing methods to overcome this.

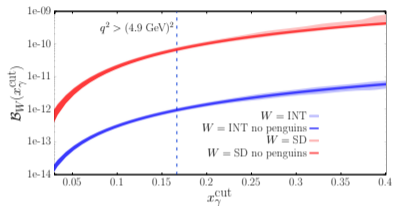
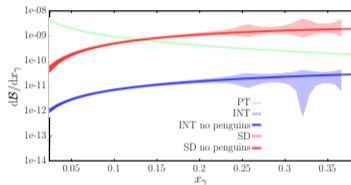
There are a number of new theoretical issues to be understood.

- In the meantime we follow previous ideas and estimate the contribution based on VMD inserting all  $c\bar{c}$  resonances from the  $J/\Psi$  to the  $\Psi(4660)$ . It can be viewed as a shift in  $C_9 \rightarrow C_9^{\text{eff}}(q^2) = C_9 + \Delta C_9(q^2)$ :

$$\Delta C_9(q^2) = -\frac{9\pi}{\alpha_{\text{em}}^2} \left( C_1 + \frac{C_2}{3} \right) \sum_V |k_V| e^{i\delta_V} \frac{m_V \Gamma_V B(V \rightarrow \mu^+ \mu^-)}{q^2 - m_V^2 + im_V \Gamma_V}.$$

- $k_V$  and  $\delta_V$  parametrise the deviation from the factorisation approximation (in which  $\delta_V = k_V - 1 = 0$ ). We allow  $\delta_V$  to vary over  $(0, 2\pi)$  and  $|k_V|$  to vary in the range  $1.75 \pm 0.75$ .

## Branching Fractions



$$\mathcal{B}(x_\gamma^{\text{cut}}) = \int_0^{x_\gamma^{\text{cut}}} dx_\gamma \frac{d\mathcal{B}(x_\gamma)}{dx_\gamma}$$

- Structure Dependent (SD) contribution dominated by  $F_V$ .
- The error from the charming penguins increases with  $x_\gamma$  (at  $x_\gamma = 0.4$  it is about 30 %).
- Our Result -  $\mathcal{B}_{\text{SD}}(0.166) = 6.9(9) \times 10^{-11}$ ; LHCb -  $\mathcal{B}_{\text{SD}}(0.166) < 2 \times 10^{-9}$ .

# CHARMONIUM RESONANCES, B ANOMALIES

- B anomalies
- can lattice contribute?
- how to deal with charmonium resonances?




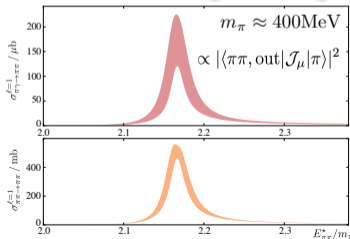
## Transition amplitudes

$$|\langle n, L | \mathcal{J} | \pi, L \rangle|^2 = \langle \pi | \mathcal{J} | \beta, \text{in} \rangle \mathcal{R}_{\alpha\beta}(P, L) \langle \beta, \text{out} | \mathcal{J} | \pi \rangle$$

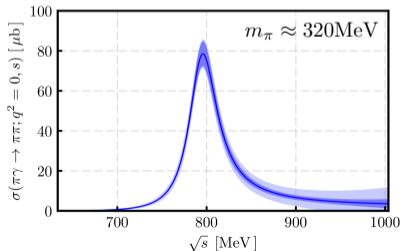
$$\mathcal{R}(P, L) = - \lim_{E \rightarrow E_n(L)} \frac{E - E_n(L)}{\mathcal{M}(s) + F^{ie}(P, L)^{-1}} = \frac{1}{\mu'(E)} \mathbf{v}^T \mathbf{v}$$

Briceño, Dudek, Leskovec

$$\langle \pi\pi, \text{out} | \mathcal{J}_\mu | \pi \rangle \equiv$$




Briceño et. al., Phys. Rev. D93, 114508 (2016)



Alexandrou et. al., Phys. Rev. D98, 074502 (2018)

- Formalisms are understood and applied in calculations already

⇒ Large toolkit available

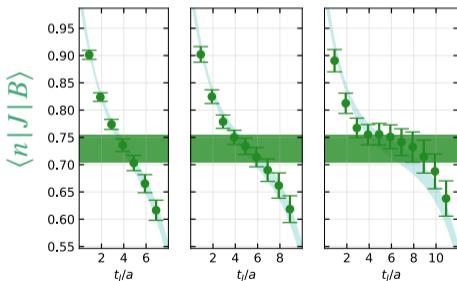
## state projection

$$C_{3,i} = \sum_{n \in [\pi\pi]} Z_i^n \langle n | J | B \rangle Z_B \frac{e^{-E_n(\Delta t - t_f)} e^{-E_B t_f}}{2E_n 2E_B}$$

$$C_3^n = u_i^n C_{3,i}$$

weights from GEVP

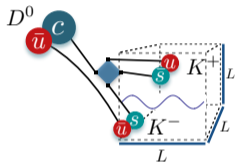
$$C_3^n = \langle n | J | B \rangle Z_B \frac{e^{-E_n(\Delta t - t_f)} e^{-E_B t_f}}{2E_B}$$



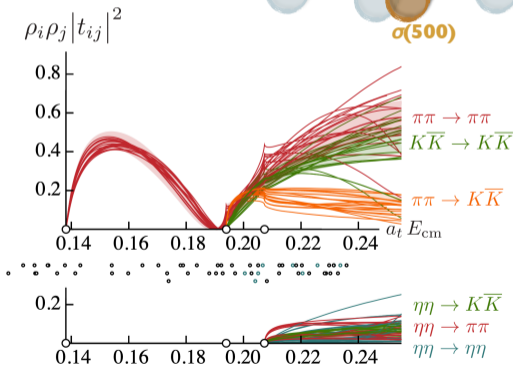
- same recipe works for B decays
- overall computation more costly, b-quark parametrization, etc

Dreaming of the future...

$$I^G(J^{PC}) = 0^+(0^{++})$$



dreaming of the future



- We have the toolkit to do very involved calculations
- can we think of realistic dreams for the foreseeable future?

□ Biggest problem is >2 hadron states!

# PERSPECTIVES FOR SCATTERING CALCULATIONS IN FLAG

- currently, there are no scattering calculations in FLAG
- should we invest more effort into fulfilling relevant criteria?
  - continuum extrapolation
  - chiral extrapolation
  - full systematic error budget
- maybe the opposing dream: how do we ensure we can control what we know well?
- Which quantities would we like to see?
  - Resonance pole positions
  - form factors of e.g.  $B \rightarrow \pi\pi\ell\nu$

- is it more tempting to keep exploring the massive toolbox we have been provided with?

## Landscape of amplitudes

✓ Two-to-two scattering:  $2 \rightarrow 2$



✓ Decays with an external current:  $1 \rightarrow 2$



✓ Transitions with an external current:  $2 \rightarrow 2$



✓ Three-to-three scattering:  $3 \rightarrow 3$



✓ Long distance matrix elements



- If we want to allow re-analysis, we could share all our correlator data & analysis code
- Arguably, if all 3  $B \rightarrow D^*$  calculations [Monday discussions] would have done this, a lot of good phenomenological work could have come out of it
- certainly, at least as much bad phenomenological work would have come out of it!
- is that a problem?
- Not impossible! We did it recently for  $K^*, \rho$  resonance work [FE et al., arXiv:2406.19193] [FE et al., arXiv:2406.19194]
- Correlator data published on CERN Document Server [FE et al.; CDS 2024]
- 800 GB of data - admittedly easier if at least one author has a CERN affiliation
- European grants often pay for cost
- If at least one author is living in Germany, PUNCH4NFDI [www.punch4nfdi.de]

- Ambitious lattice QCD physics programmes take years and people power
  - development of general formalisms
  - adaption of formalisms for specific processes
  - grant / computing time applications
  - gauge field generation
  - production runs
  - maintaining HPC clusters
  - data analysis
- Science / academia is a relatively precarious career path
- How do we ensure researchers at all career stages are
  - visible in the community? See a perspective for research jobs?
  - see a perspective for research jobs?
  - are motivated to have their work reproducible for future re-analysis / extensions?
  - Suggestion in yesterday's discussion to involve phenomenologists in author list

# LAST SLIDE OF LATTICE@CERN 24



Thanks for participating!