

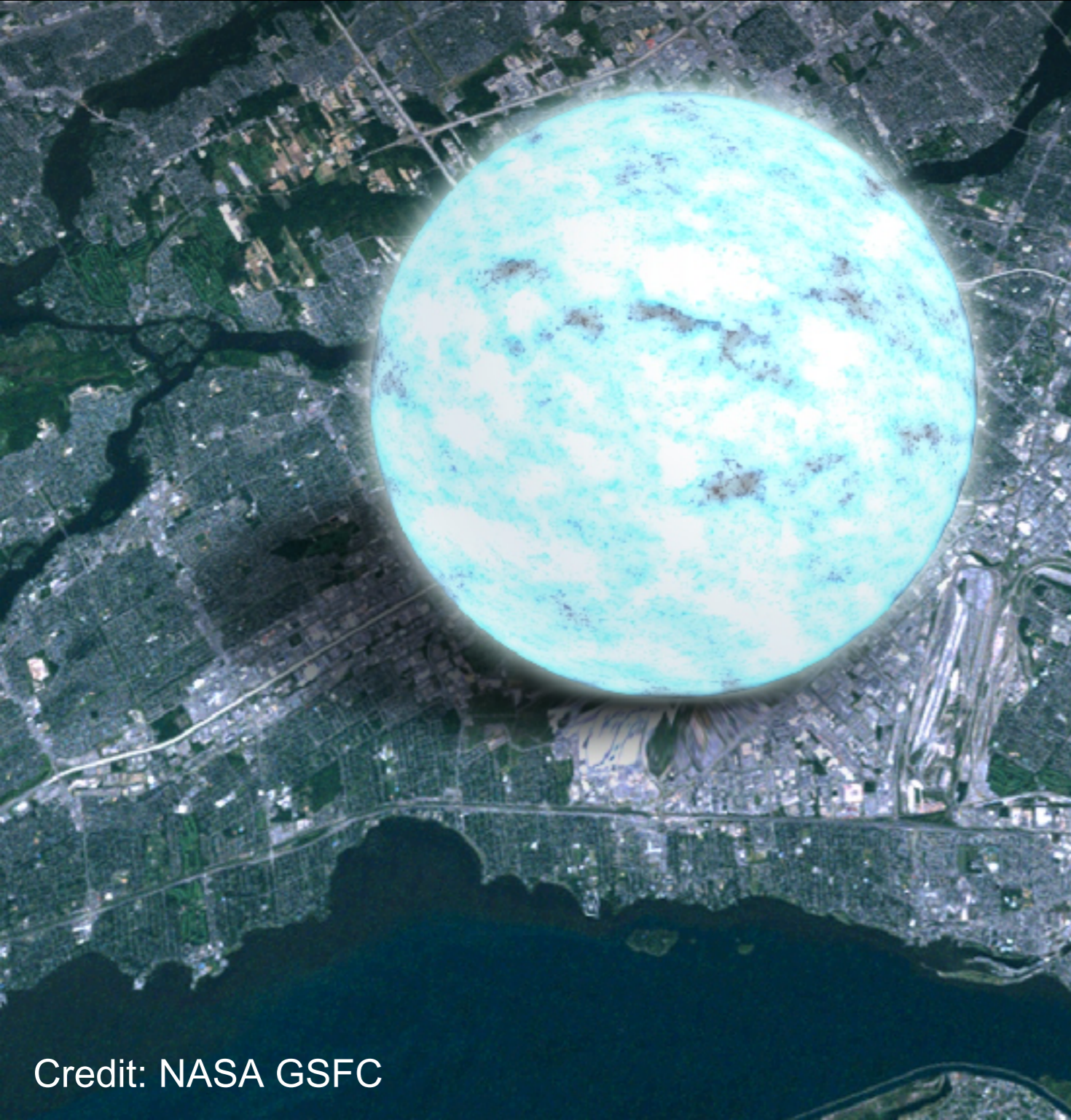


Probing the Neutron-star Equation of State with Radio Pulsars

Emmanuel Fonseca
(on behalf of NANOGrav)
West Virginia University
01 December 2023



Credit: NASA GSFC

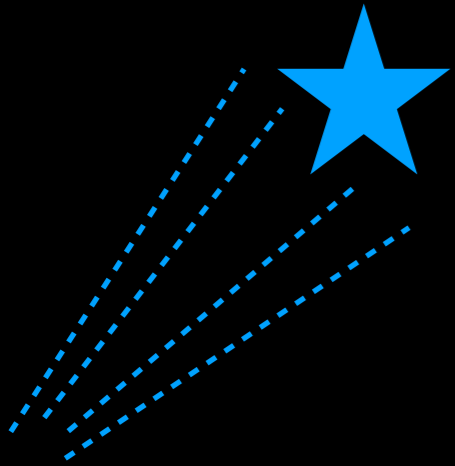


NANOGrav fundamentally relies on “**pulsar timing**” for its GW project.

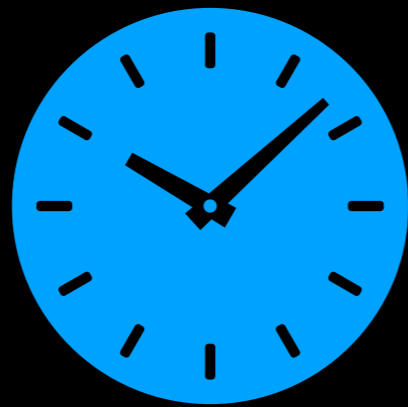
Pulsar timing is “so good” that you can (and must!) study:

- astrometry
- irregularities in spin
- dispersion variations
- pulsar-based timescales
- strong-field gravity
- variations in radio polarization
- **mass and geometric information**

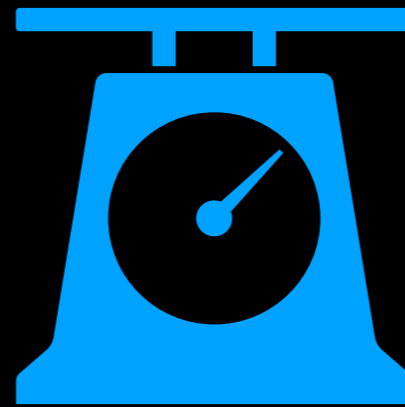
History



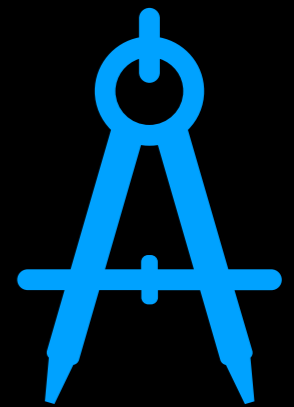
Techniques



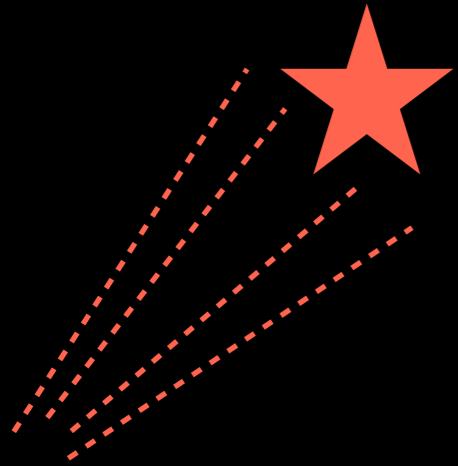
Measurements



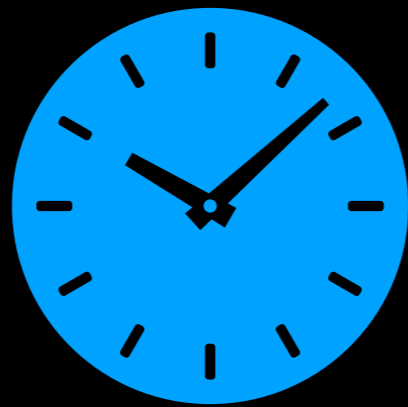
Applications



History



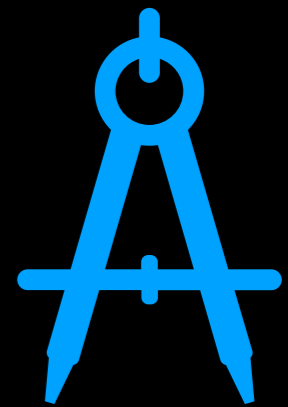
Techniques



Measurements



Applications



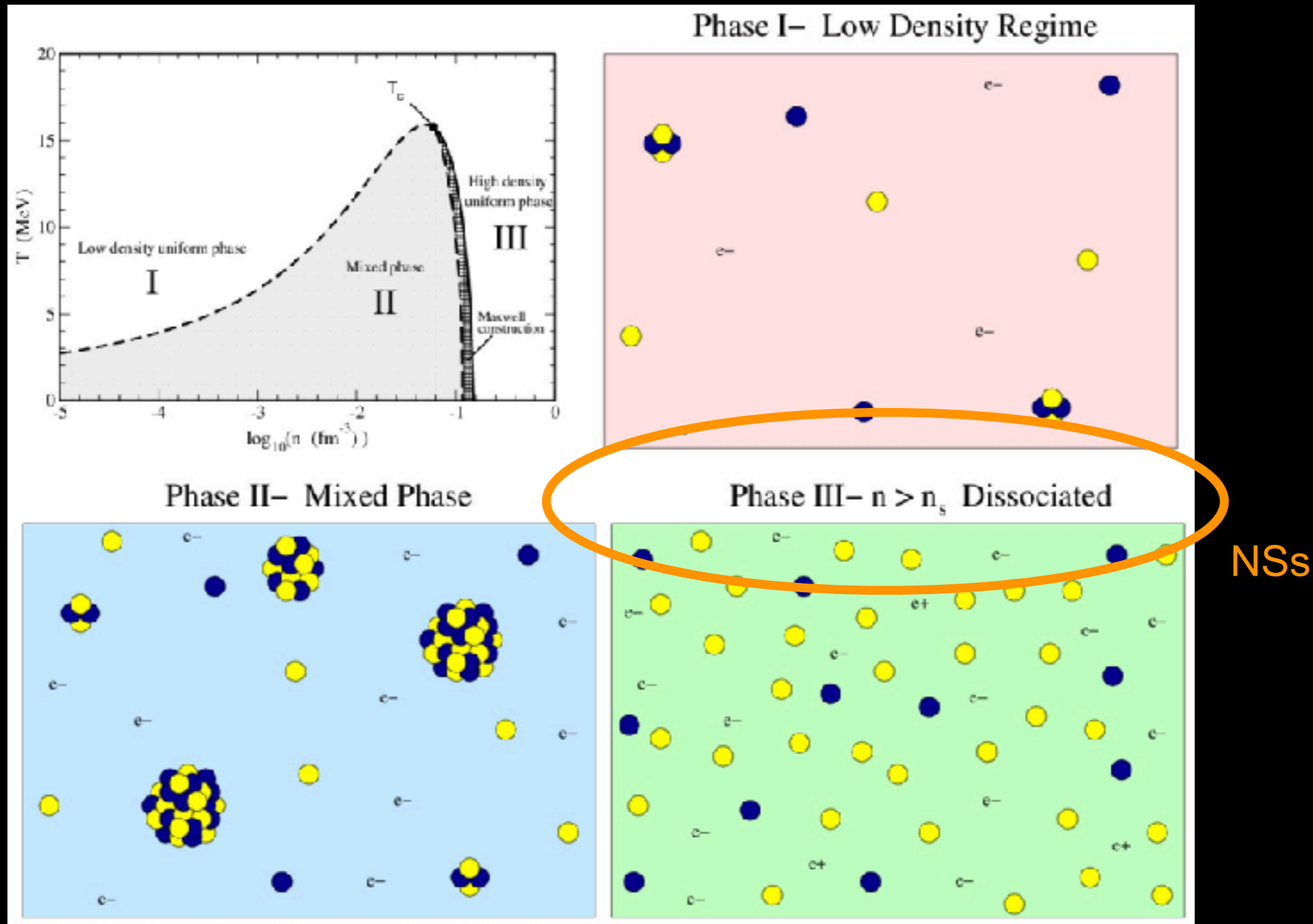
A Brief History of Neutron Stars

- Milestones for our understanding of neutron stars and their interiors:
 - 1933: neutron discovered (J. Chadwick)
 - 1934: neutron stars (NSs) proposed (W. Baade, F. Zwicky)
 - 1939: first **equation of state (EoS)** proposed (R. C. Tolman; J. R. Oppenheimer & G. M. Volkoff)
 - 1966: pre-observation summary of nuclear physics relevant to neutron stars (J. A. Wheeler)
 - 1967: **first pulsar discovered!** (J. Bell-Burnell, A. Hewish)



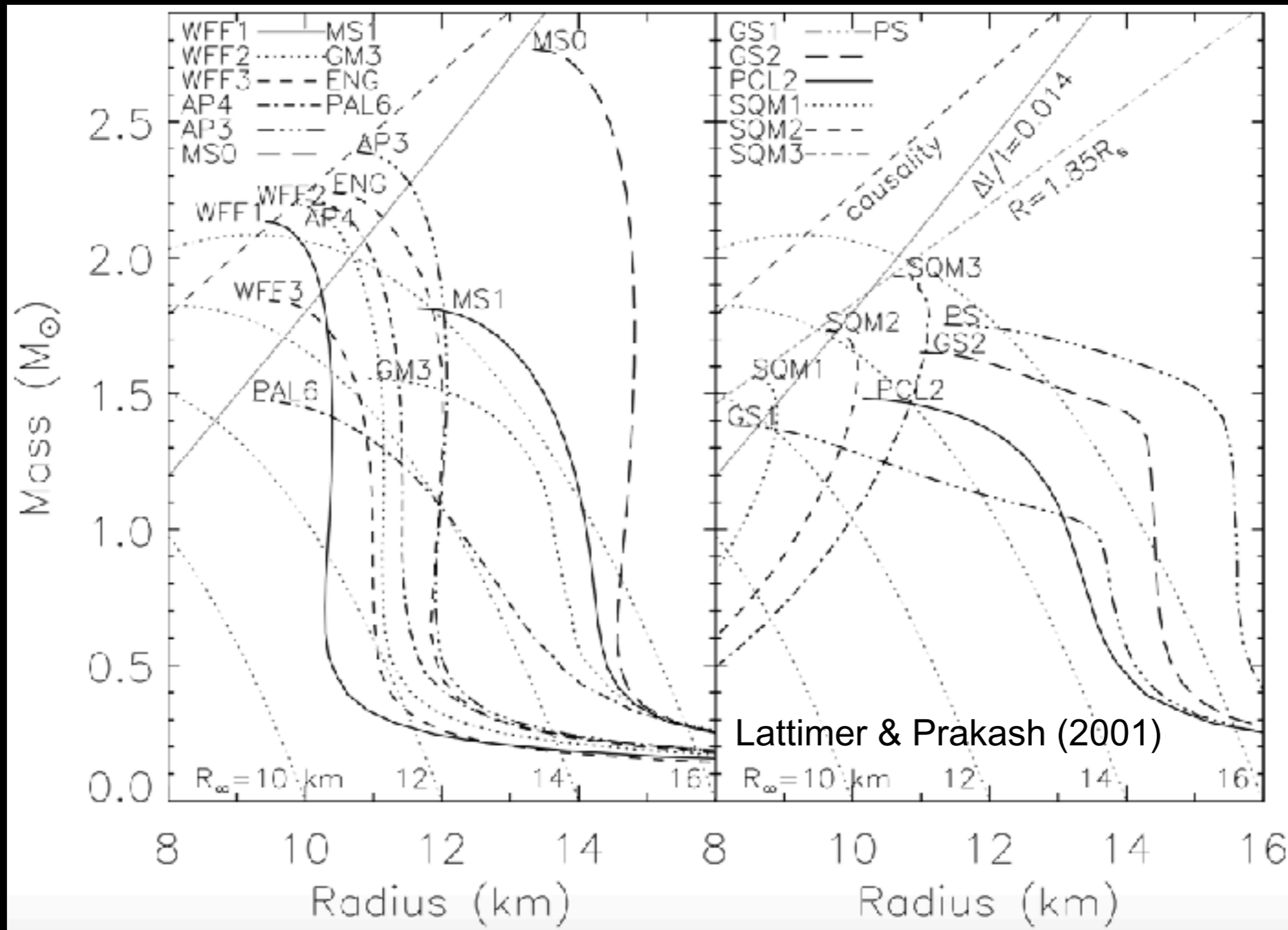
Supernova in NGC4157, discovered by
F. Zwicky in 1937
(Credit: CalTech / Palomar)

History of NS-EoS Theory, I



At supra-nuclear densities (III above), NSs are believed to consist of: unbound nucleons, strange-carrying baryons (e.g., hyperons), quarks, Bose-Einstein condensates, etc. (Credit: M. Carmell.)

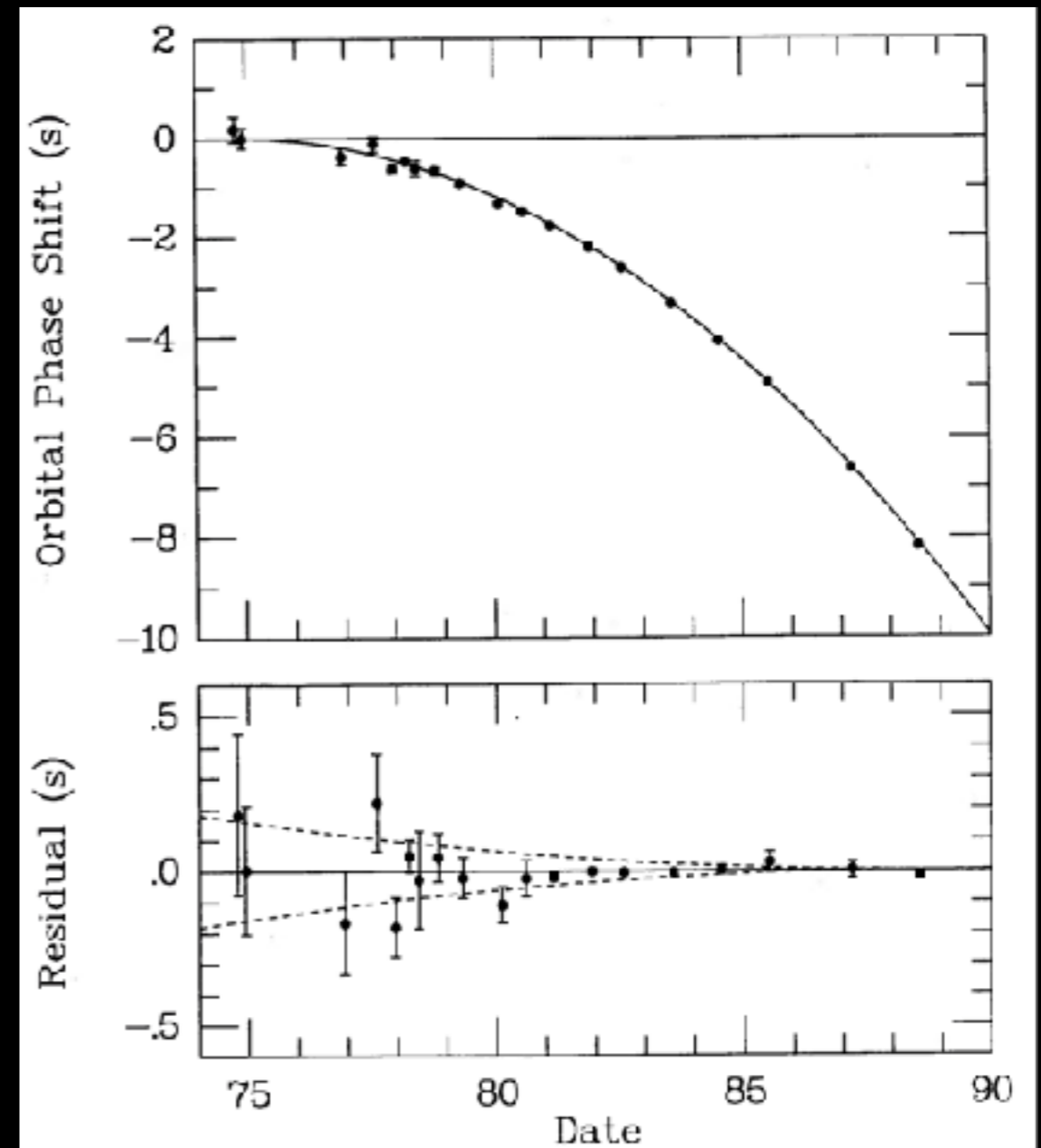
History of NS-EoS Theory, II



Development of particle physics and QCD led to a diverse range of possibilities for NS compositions, due to uncertainties in strong, many-body interactions.

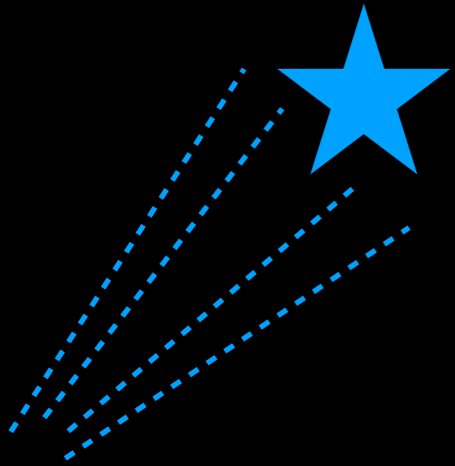
History of NS Observations

- The first binary pulsar, PSR **B1913+16**, found by Hulse & Taylor (1975) to orbit another NS.
- Timing measurements yielded orbital deviations explained by general relativity (Taylor & Weisberg, 1982).
- Masses of both neutron stars determined down to **0.003 solar masses**.



Orbital decay in PSR B1913+16
(Taylor & Weisberg, 1982)

History



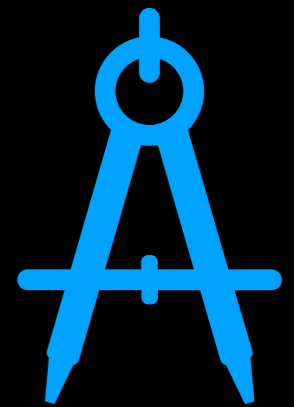
Techniques



Measurements

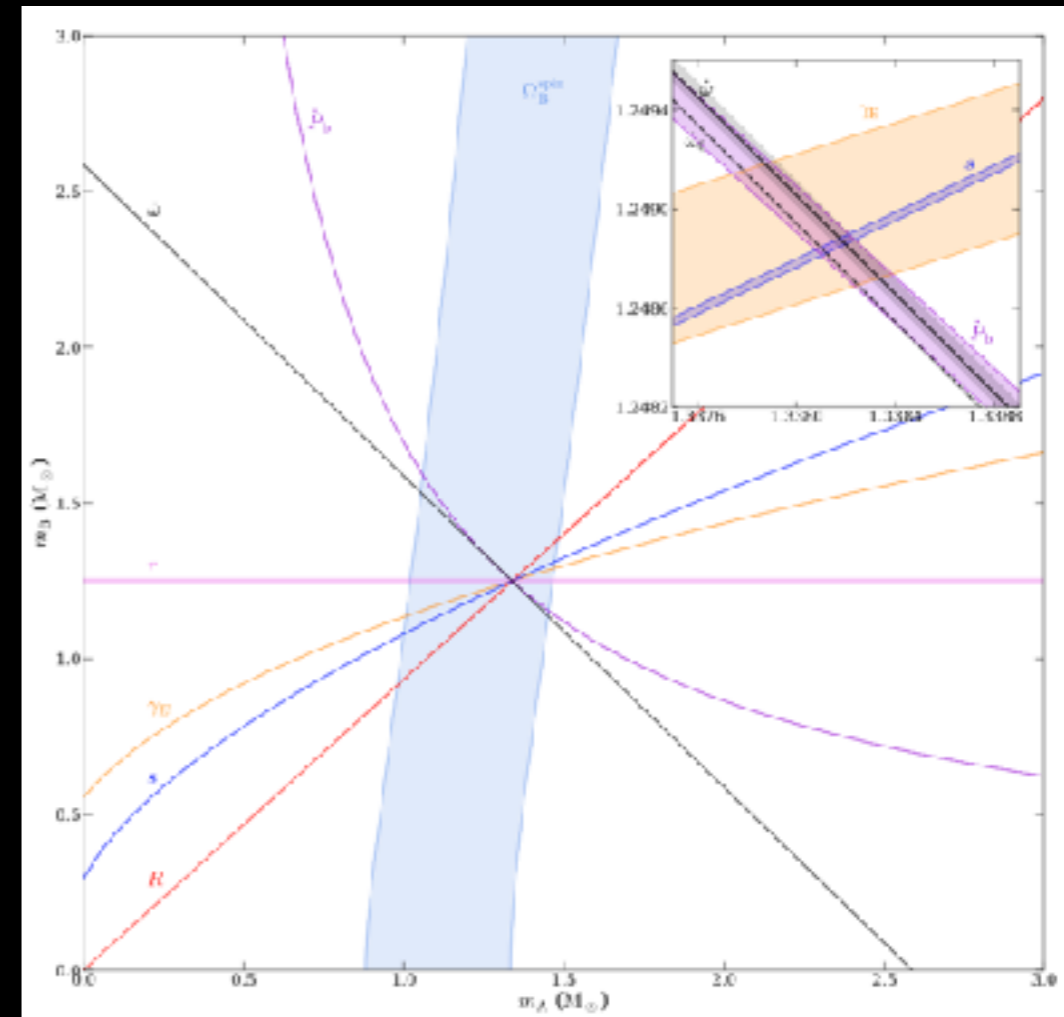


Applications

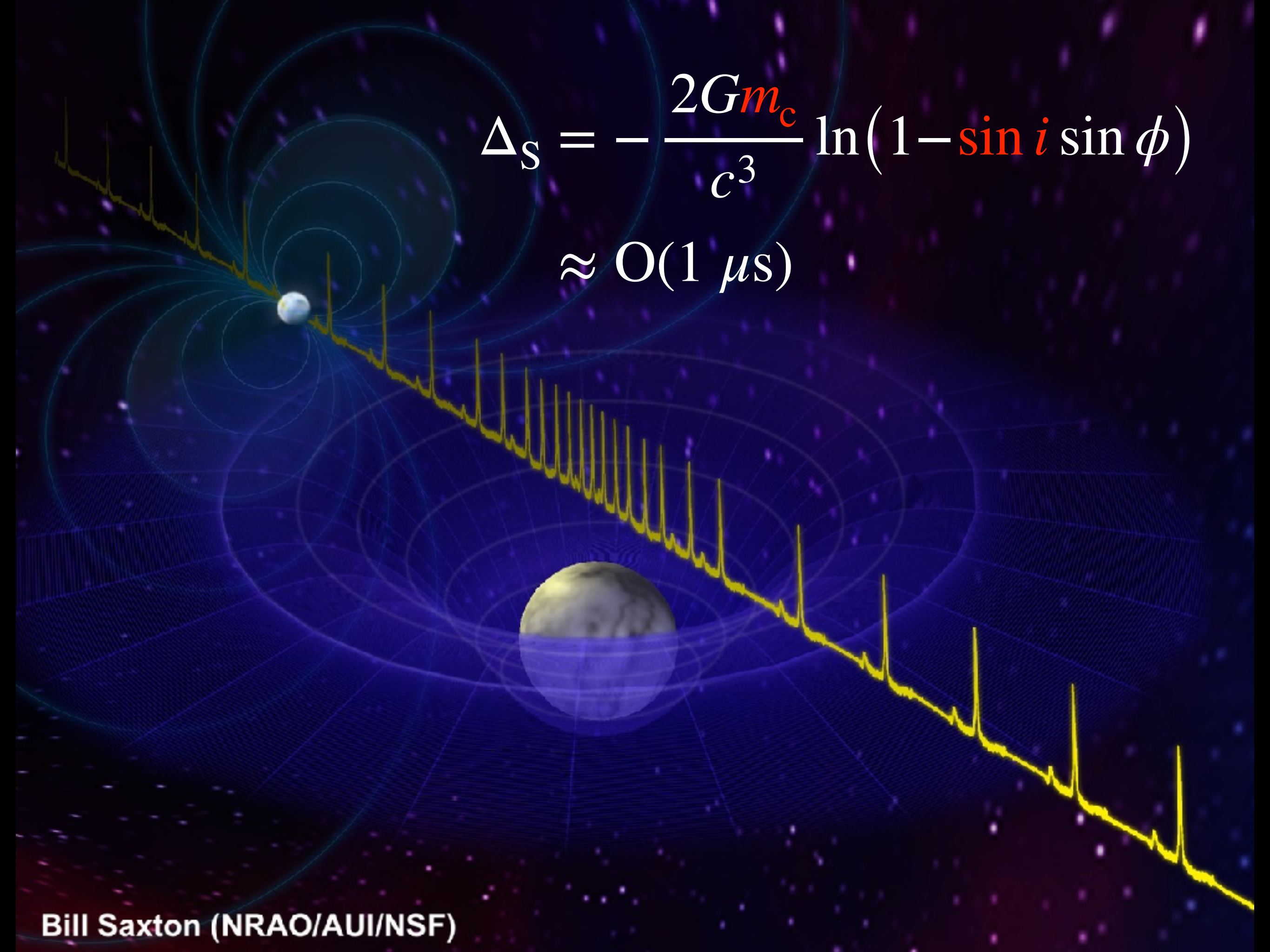


Radio Timing of Binary Pulsars

- **Pulsar timing**: see talk by R. Jennings!
- “Most robust” method of obtaining macroscopic NS parameters.
- mass uncertainties ~ 0.00001 — 0.1 solar masses.
- Common **post-Keplerian** effects:
 - ★ orbital decay
 - ★ apsidal motion
 - ★ time dilation + gravitational redshift
 - ★ the Shapiro time delay

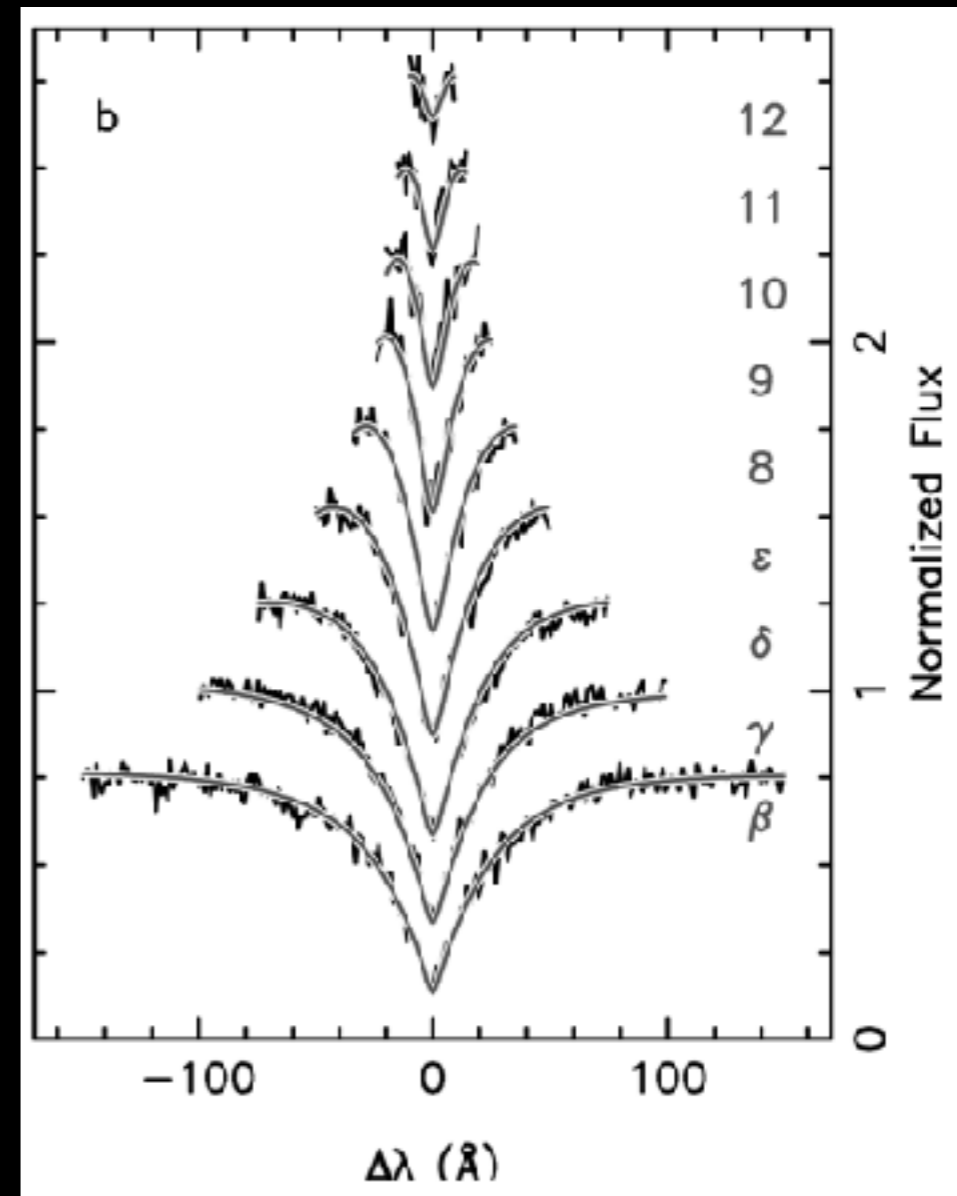


Measurement of 6 PK effects in the double-pulsar system (Kramer et al., 2021)

A visualization of gravitational waves. A large, grey, cratered sphere (representing a black hole or neutron star) is at the bottom center. A smaller, blue and white sphere (representing a planet or star) is at the top left. A yellow line with sharp peaks, representing a gravitational wave signal, travels from the top left towards the bottom right. Concentric blue circles represent the wavefronts of the gravitational waves emanating from the source. The background is a dark blue space filled with purple and white stars.
$$\Delta_S = -\frac{2Gm_c}{c^3} \ln(1 - \sin i \sin \phi)$$
$$\approx O(1 \mu\text{s})$$

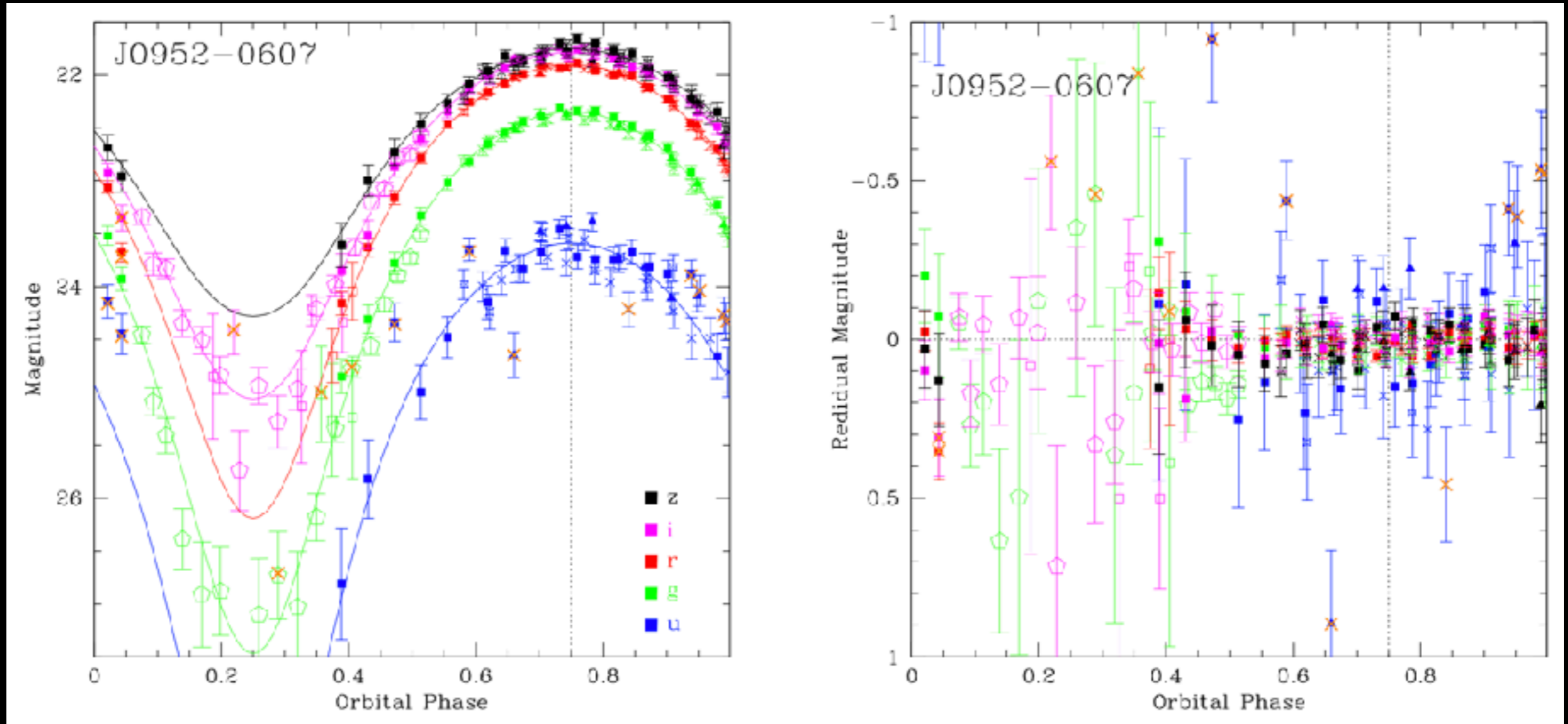
Optical Spectroscopy of WD Companions to Binary Pulsars

- White dwarfs (WDs) that are bright enough (magnitude < 23) can be observed with spectrographs.
- Doppler shift of emission lines \rightarrow projected radial velocity \rightarrow **mass ratio** (when combined with radio timing).
- Additional WD parameters (e.g., surface gravity and temperature from shape of spectral features, radius from WD-EoS models) can be obtained, **but these are model-dependent**.
- NS mass uncertainties $\sim 0.1 M_{\text{sun}}$ or larger.



Observed and models hydrogen Balmer lines in the WD companion to PSR J1911-5958A (Bassa et al., 2006c)

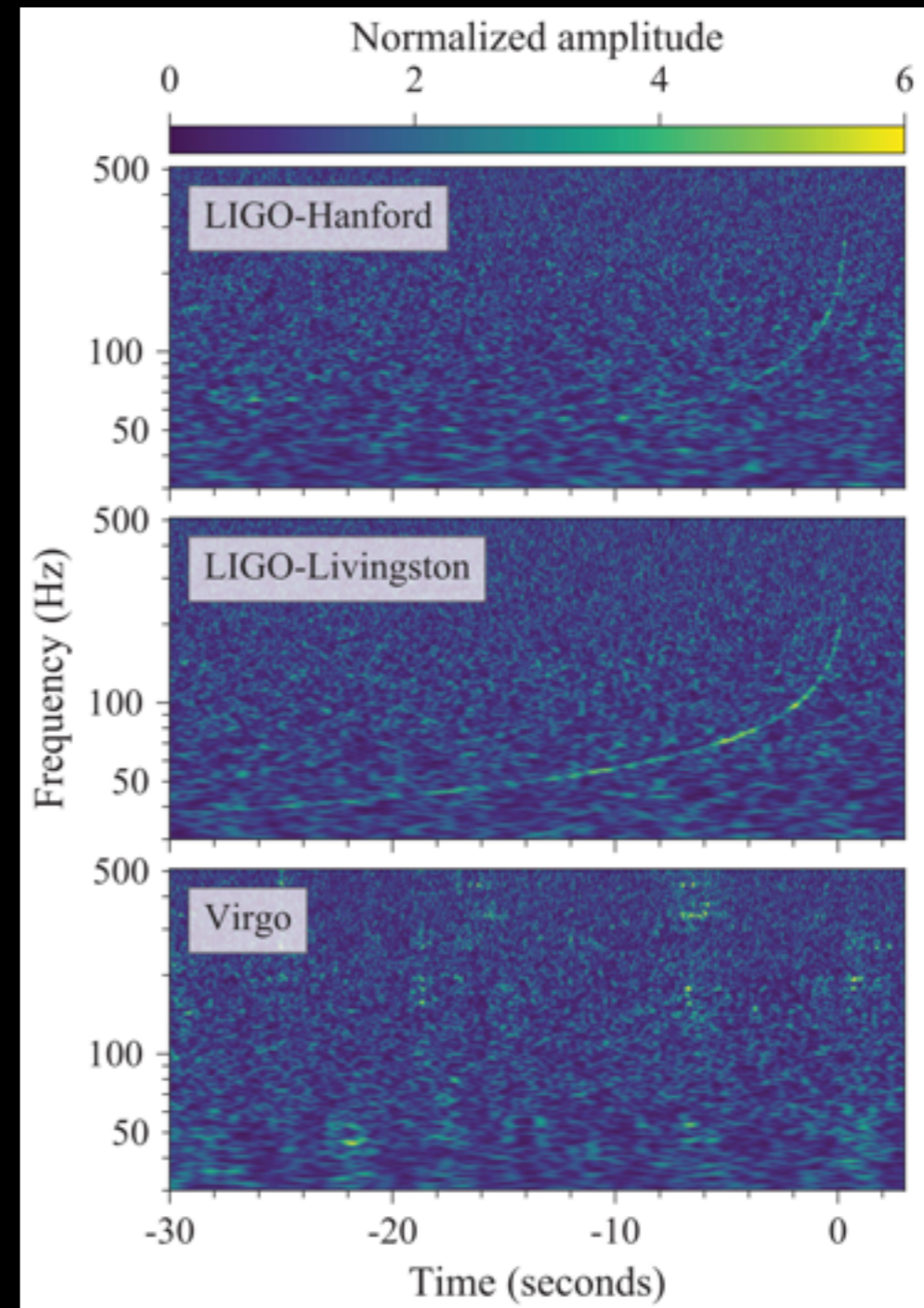
Optical Modeling of “Black Widow” Pulsars



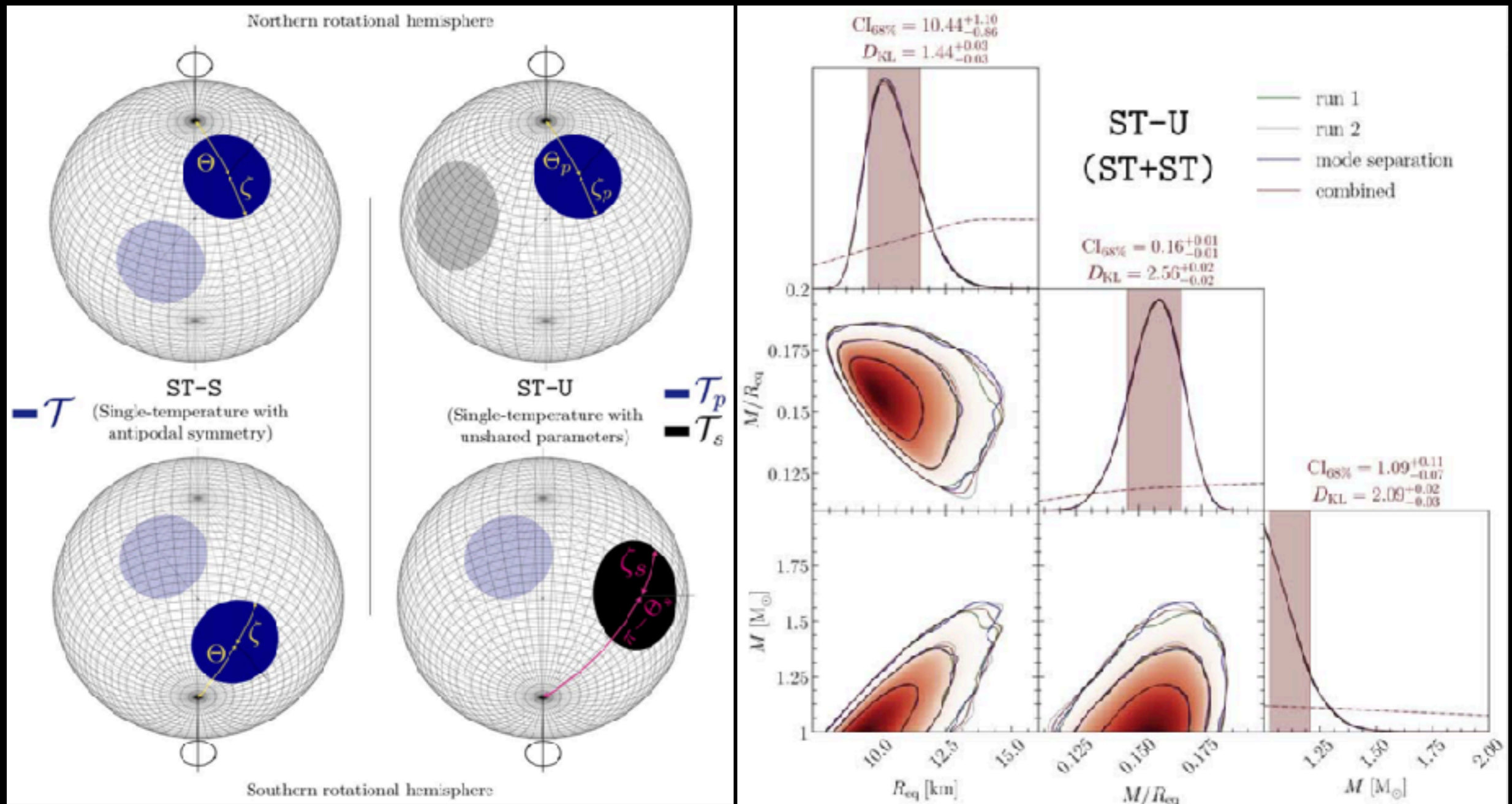
Similar observations can be conducted for “black-widow” pulsars, where modeling of spectral features and light-curve variations (the latter being model-dependent) have been shown to yield mass and geometric information. (Above: Romani et al., 2022.)

Modeling GW Waveforms

- **Gravitational waves (GWs)** have been detectable with LVK as of 2015.
- Waveform modeling can account for point-particle and spin effects to measure component masses.
- **Tidal deformability** can be observed as departure in late-time orbital decay of inspiral \rightarrow direct constraint on radius.

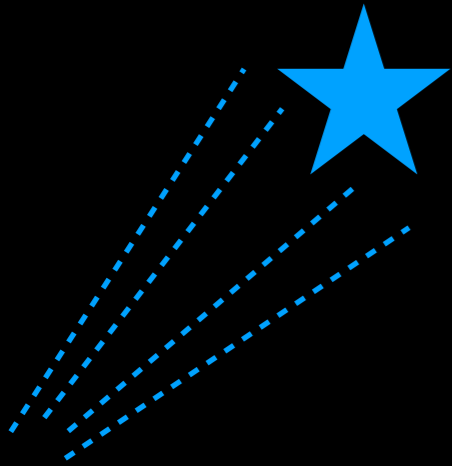


X-ray Measurement of NS Radii

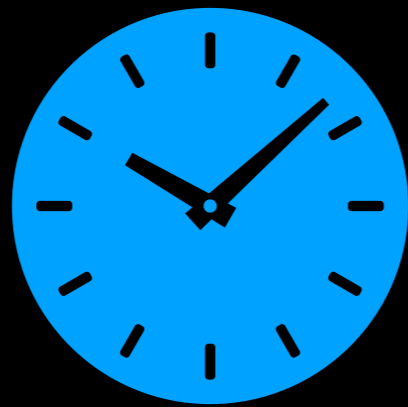


The Neutron Star Interior Composition Explorer (**NICER**) recently measured the mass and radius of PSR J0030+0451 - [an isolated pulsar!](#) - through X-ray lightcurve modeling (e.g., Miller et al., 2019; Riley et al., 2019).

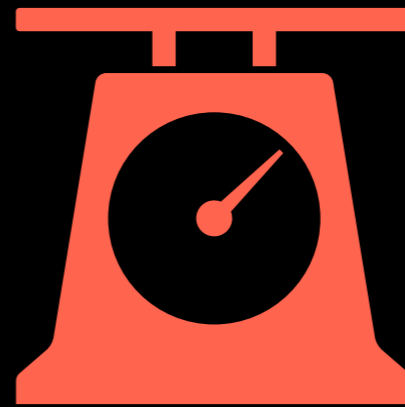
History



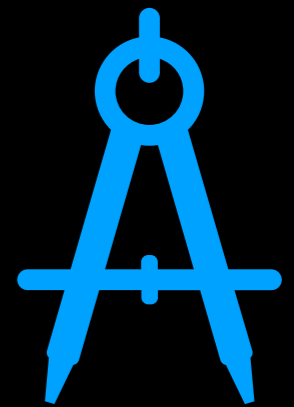
Techniques



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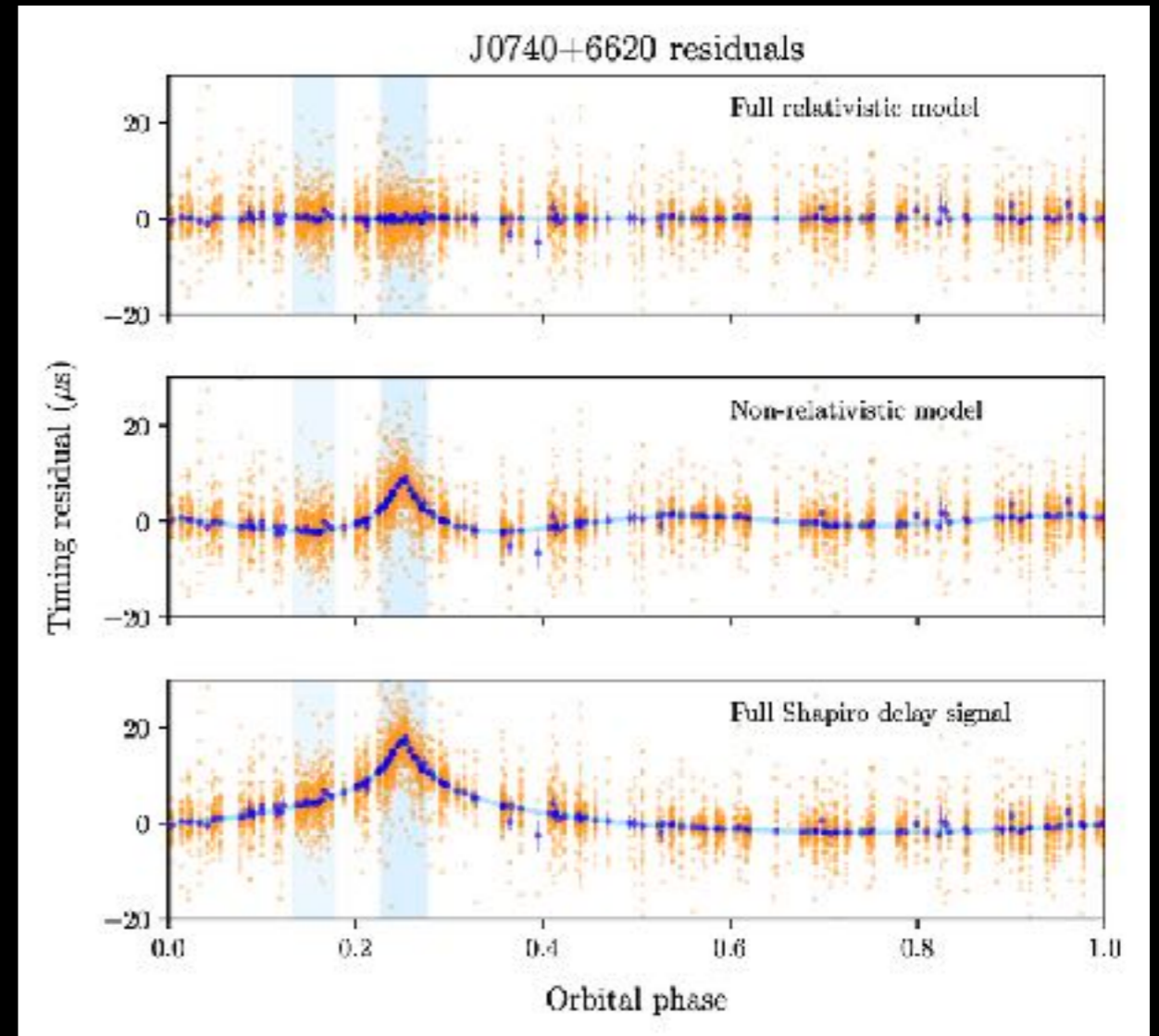


Applications



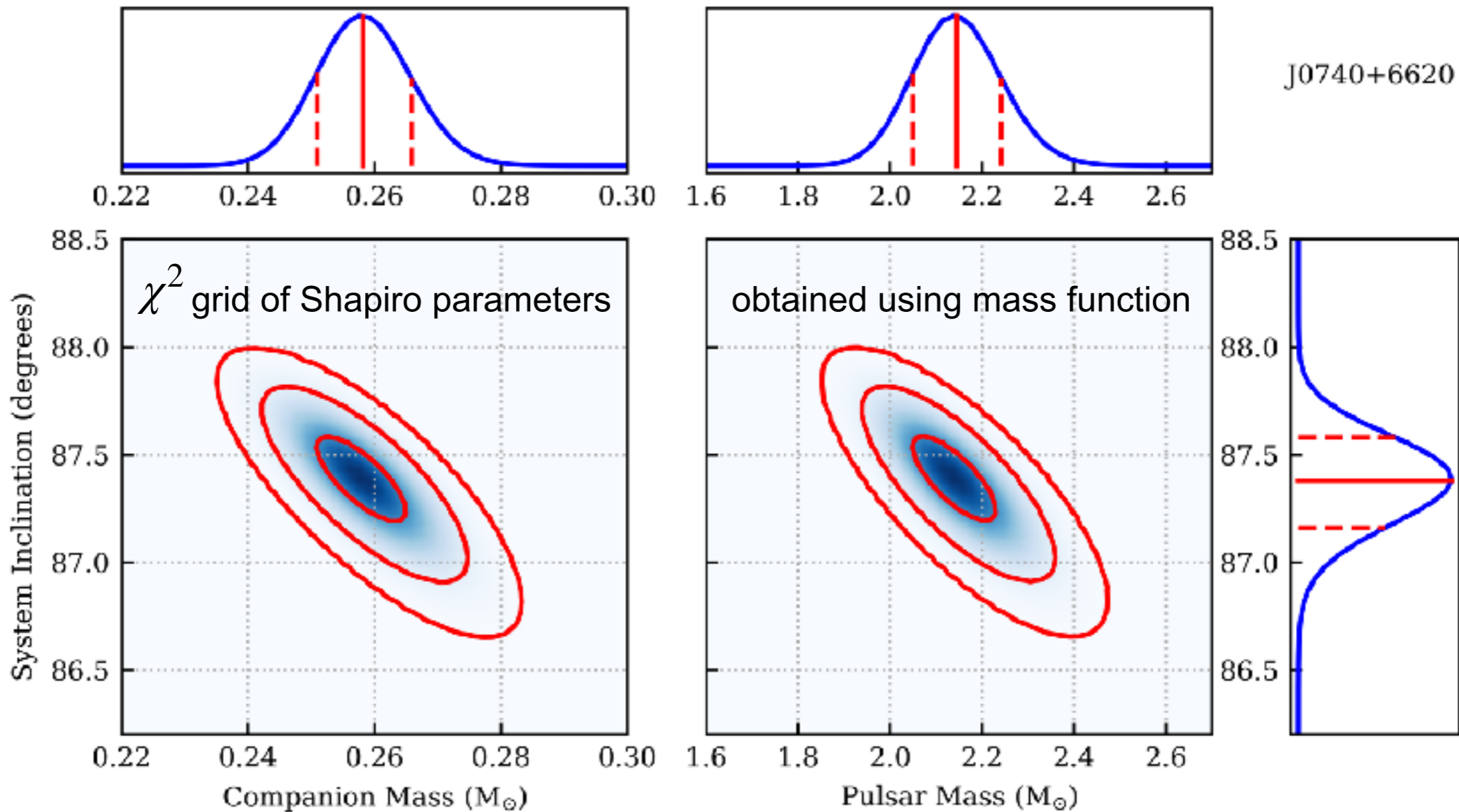
NS-Mass Summary & Statistics

- There are ~60 NS masses measured (53 come from radio-timing / WD modeling).
- All precise measurements (5% or better) come from timing.
 - ★ majority of these come from the Shapiro time delay.
- There are clear trends that correlate with companion types (and therefore *evolutionary history*).



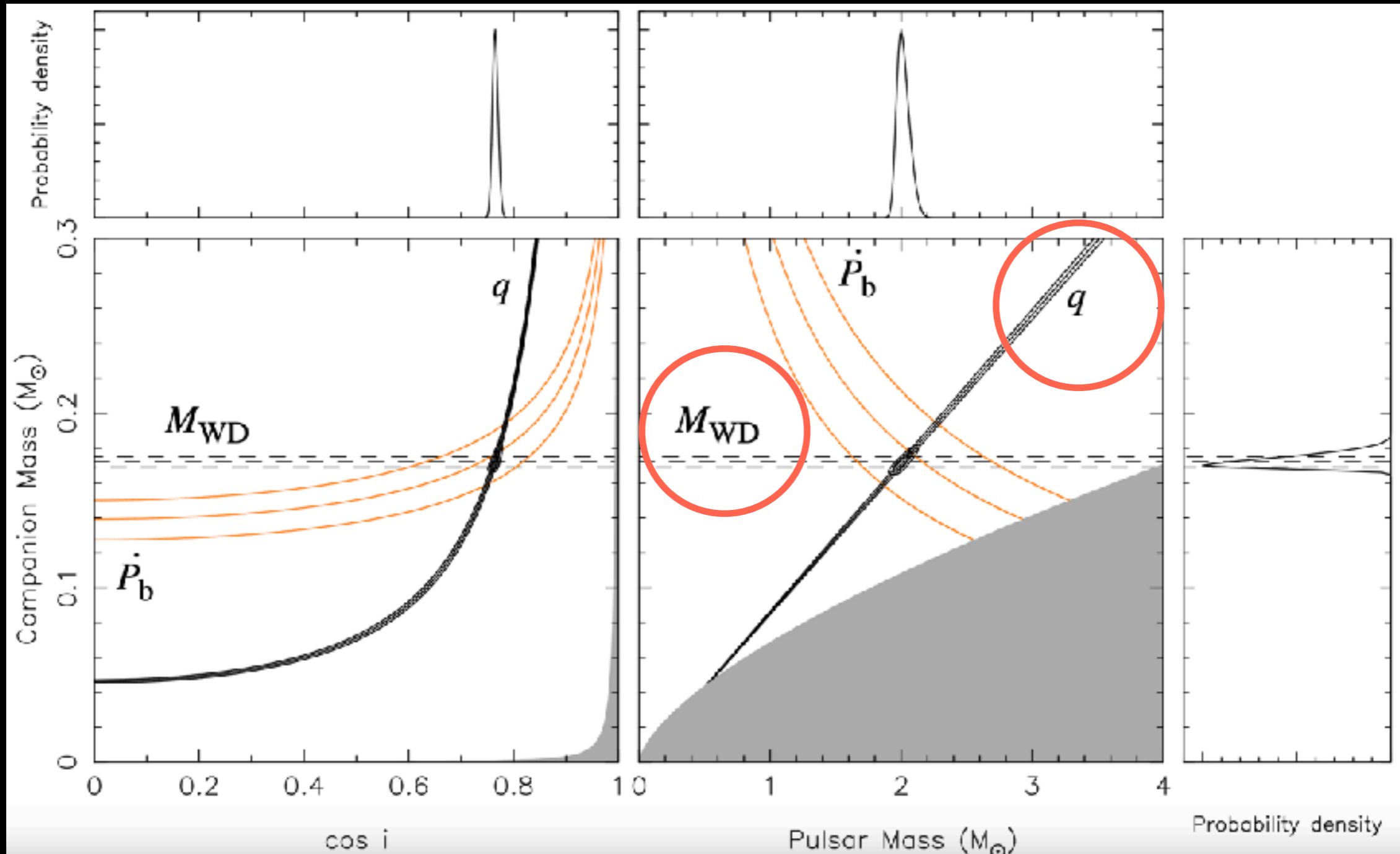
Shapiro delay in the PSR J0740+6620 binary system (Cromartie et al., 2020; Fonseca et al., 2021).

NS Masses from Timing



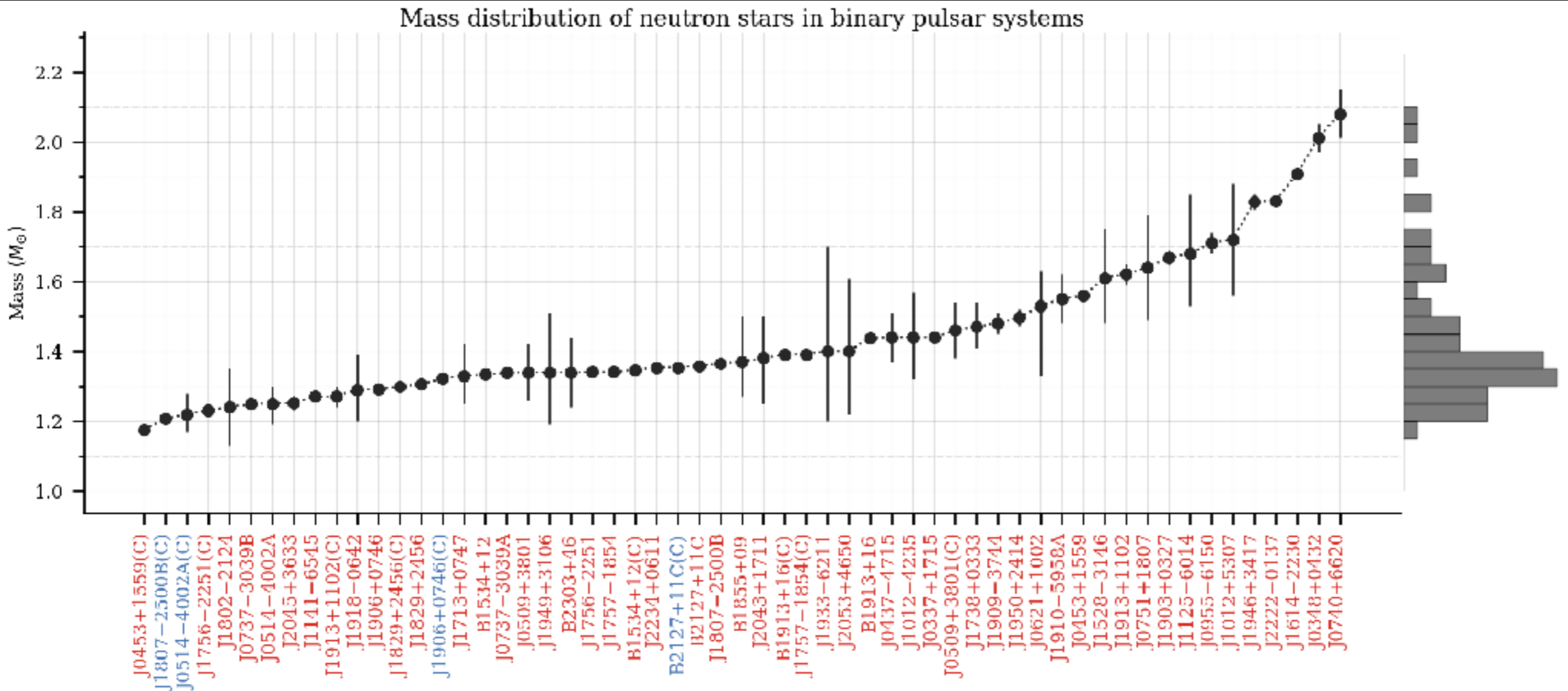
Mass and geometry from the Shapiro time delay in PSR J0747+6620
(Cromartie et al., 2020)

NS Masses from Optical Modeling of WD Companions



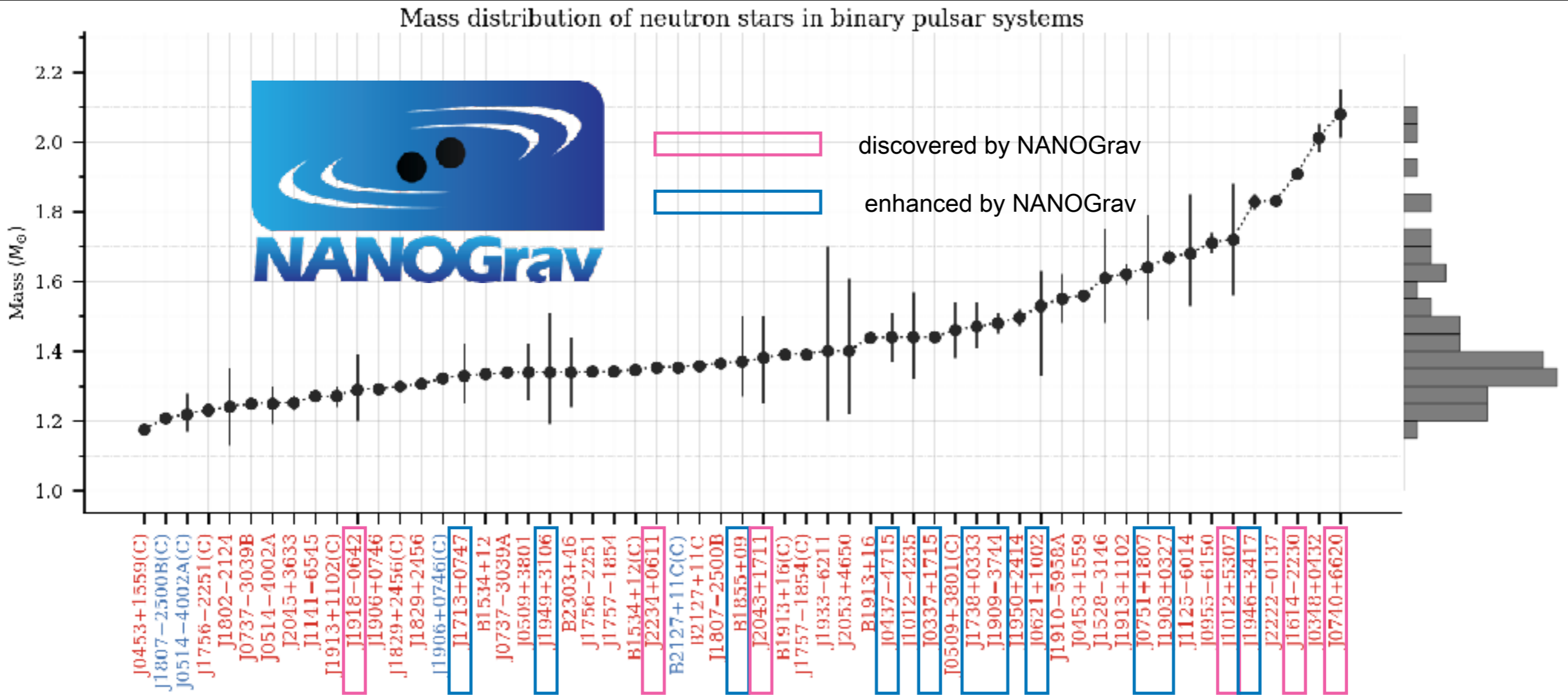
Constraints from spectroscopic measurements (red circles) for WD companion to PSR J0348+0432 (Antoniadis et al., 2013)

Pulsar Mass Summary



Credit: V. V. Krishnan, P. C. C. Freire

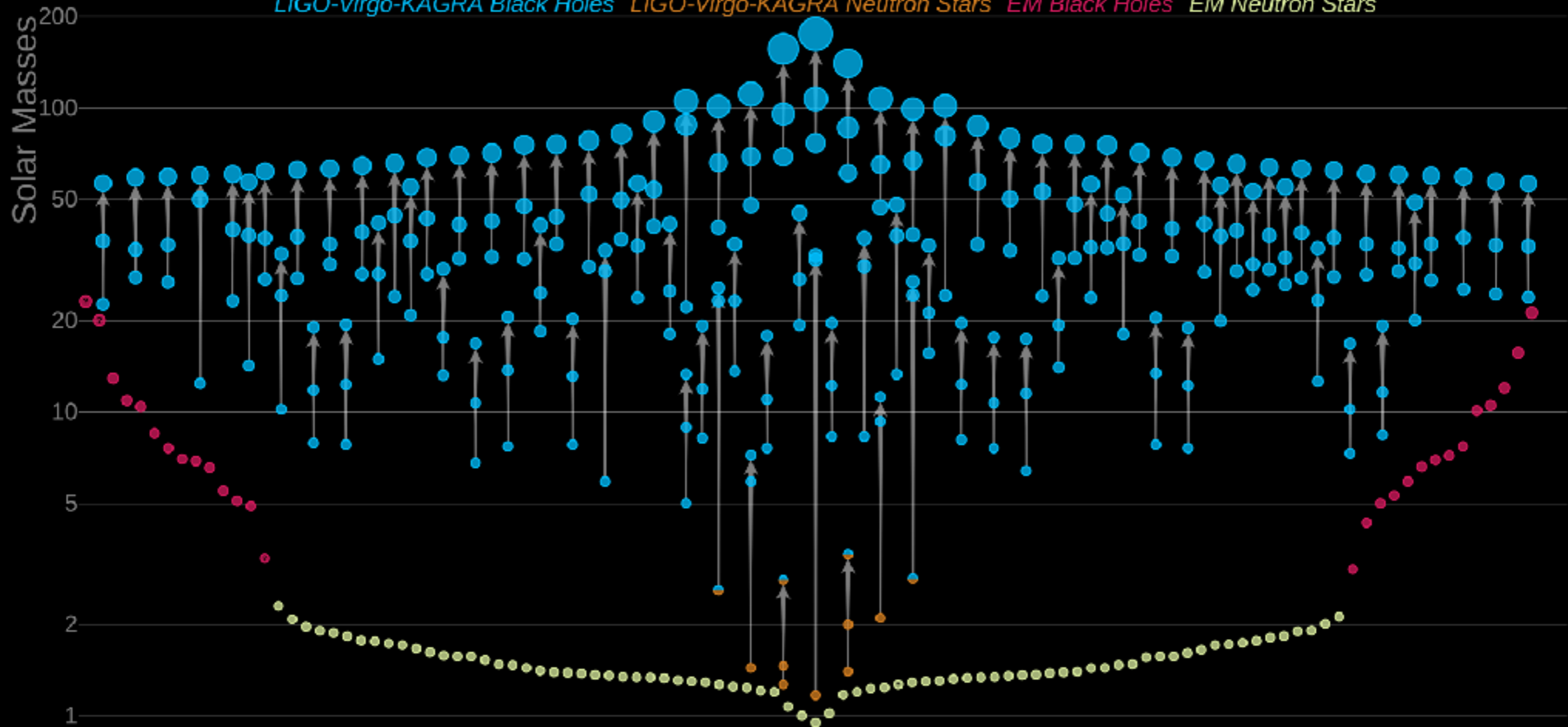
Pulsar Mass Summary



Credit: V. V. Krishnan, P. C. C. Freire

Masses in the Stellar Graveyard

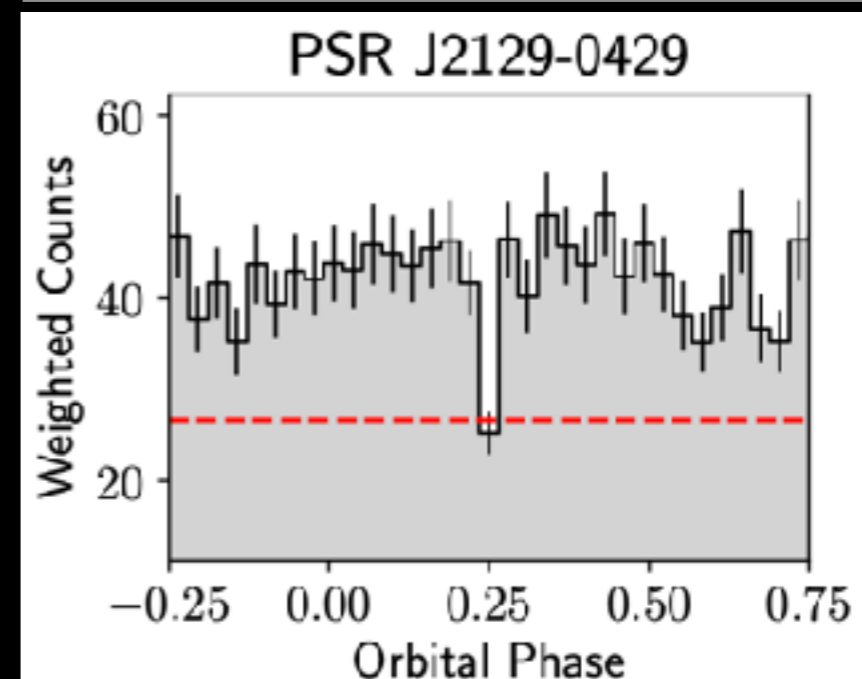
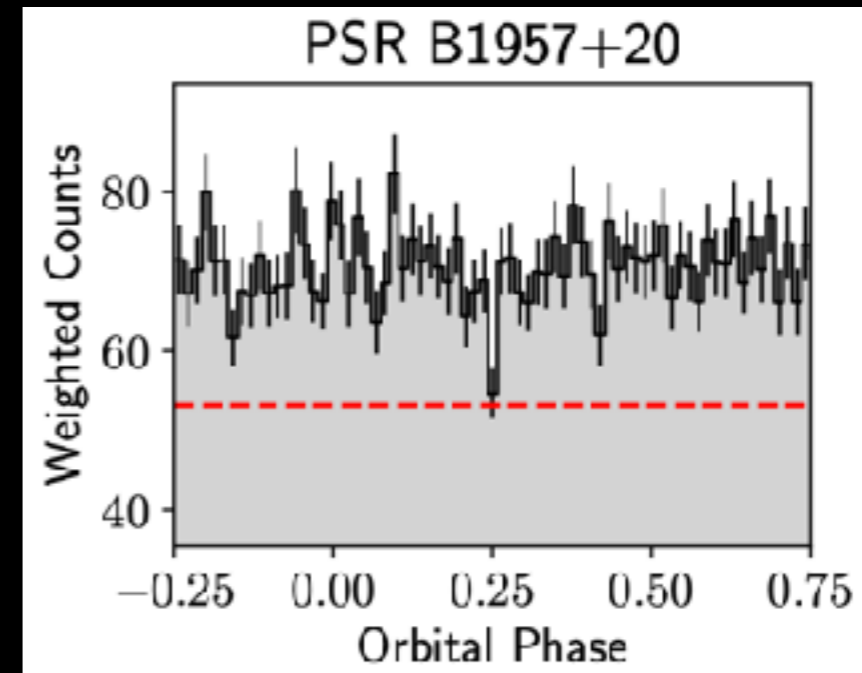
LIGO-Virgo-KAGRA Black Holes *LIGO-Virgo-KAGRA Neutron Stars* *EM Black Holes* *EM Neutron Stars*



LIGO-Virgo-KAGRA | Aaron Geller | Northwestern

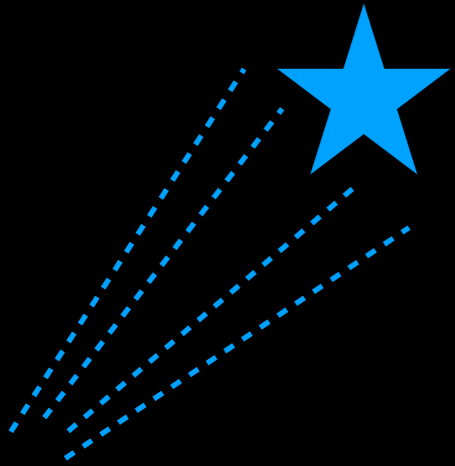
Black-Widow Masses

- Black-widow masses from radio+optical measurements:
 - B1957+20: $(2.4 \pm 0.1) M_{\odot}$
[van Kerkwijk et al., 2011]
 - J2215+5135: $(2.3 \pm 0.15) M_{\odot}$
[Linares et al., 2018]
- Recent work indicates that gamma-ray constraints on inclination in these systems **produce inconsistent results**:
 - B1957+20: $(1.81 \pm 0.04) M_{\odot}$

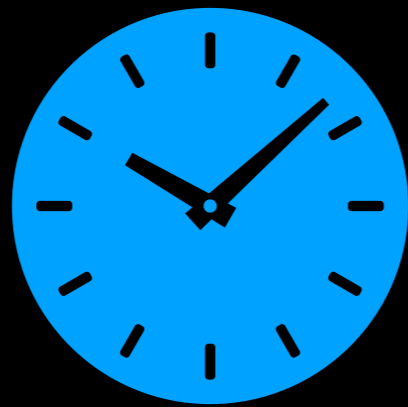


Clark et al. (2023)

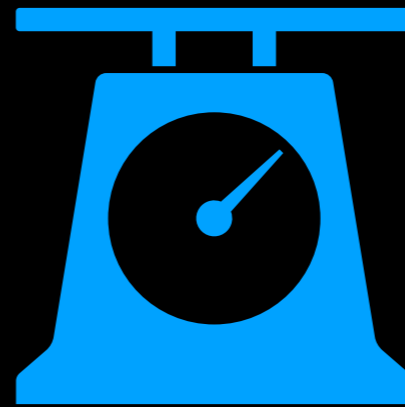
History



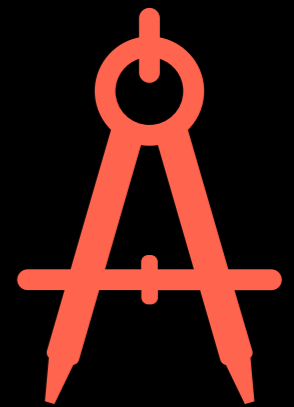
Techniques



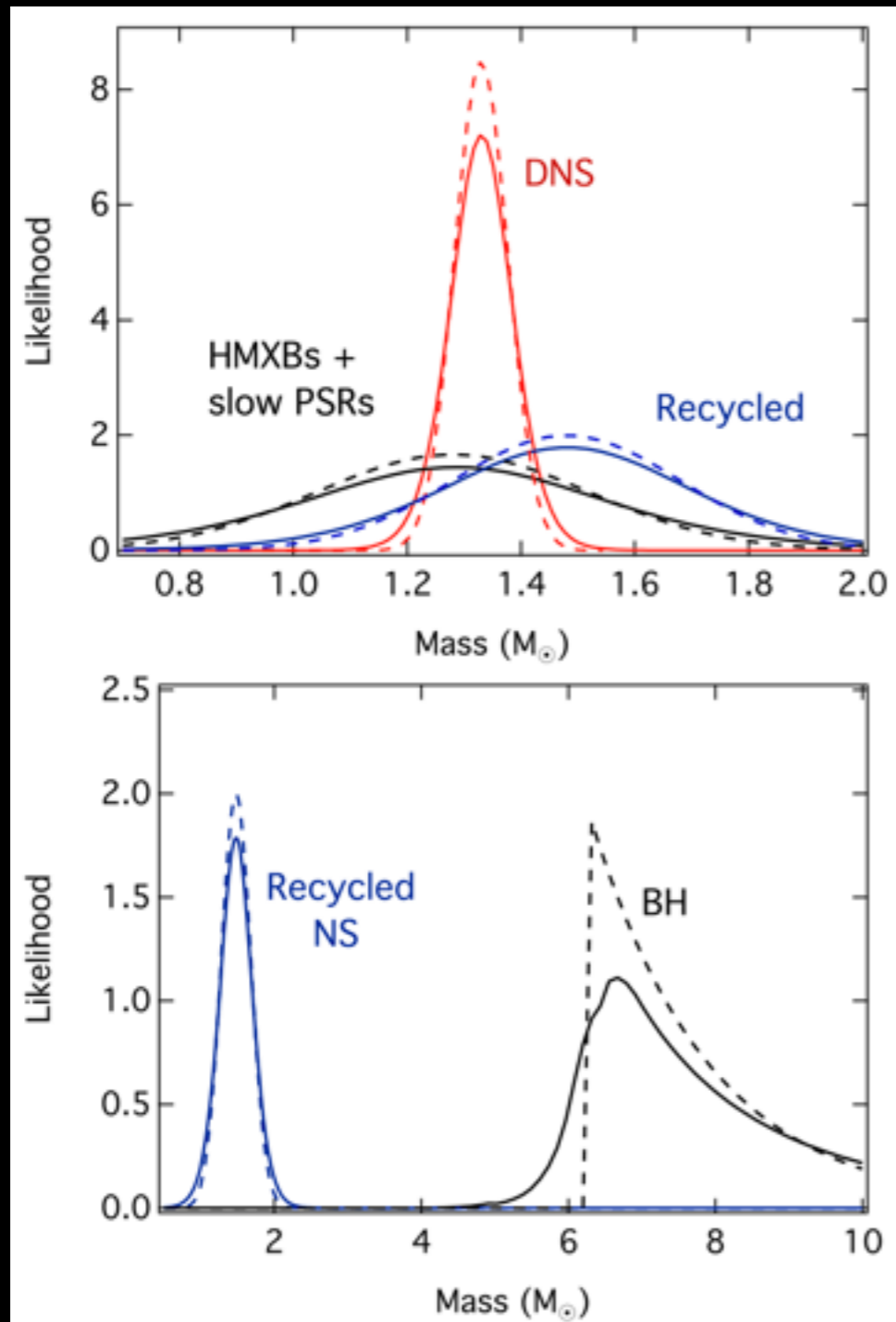
Measurements



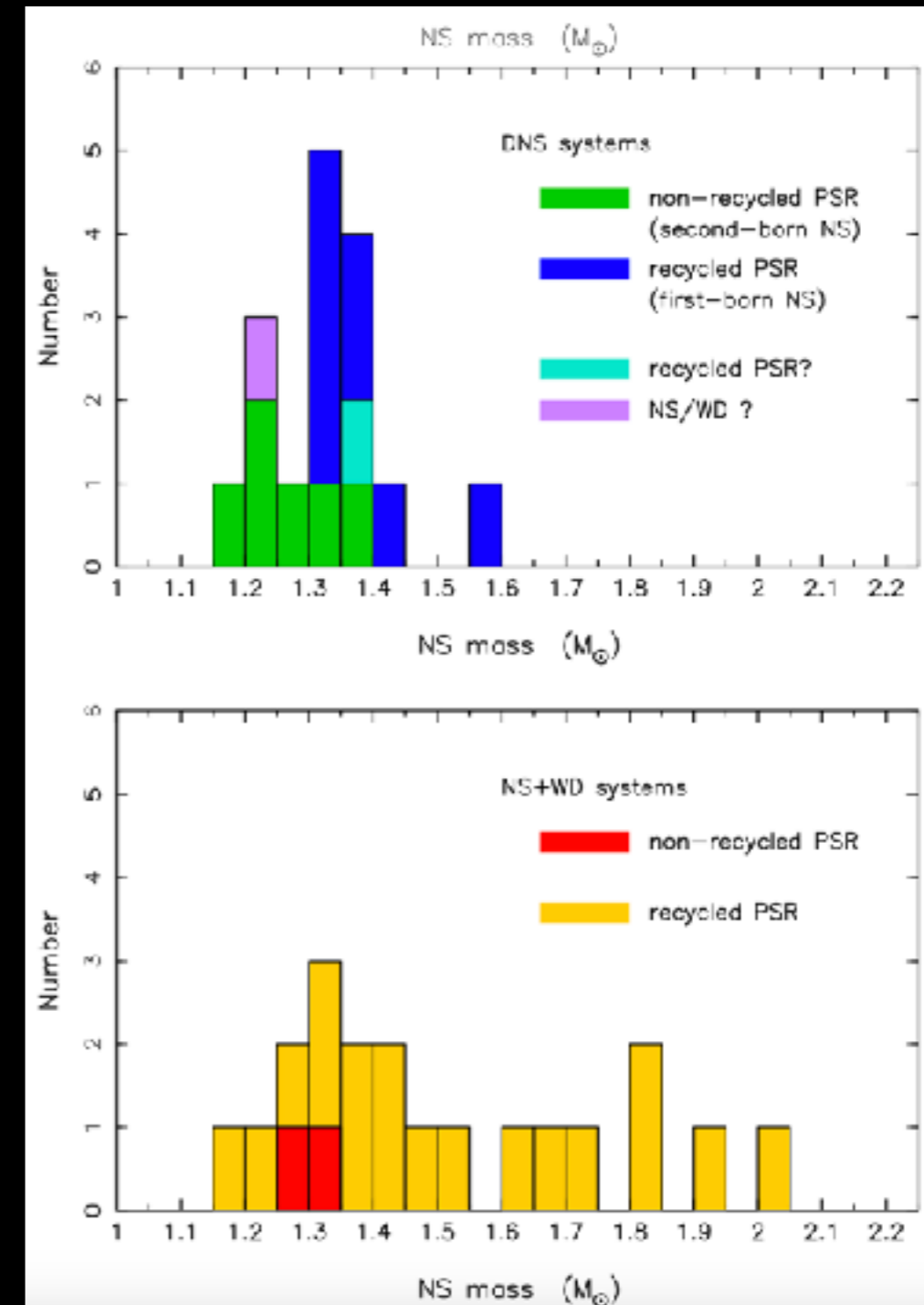
Applications



Census of Pulsar Masses

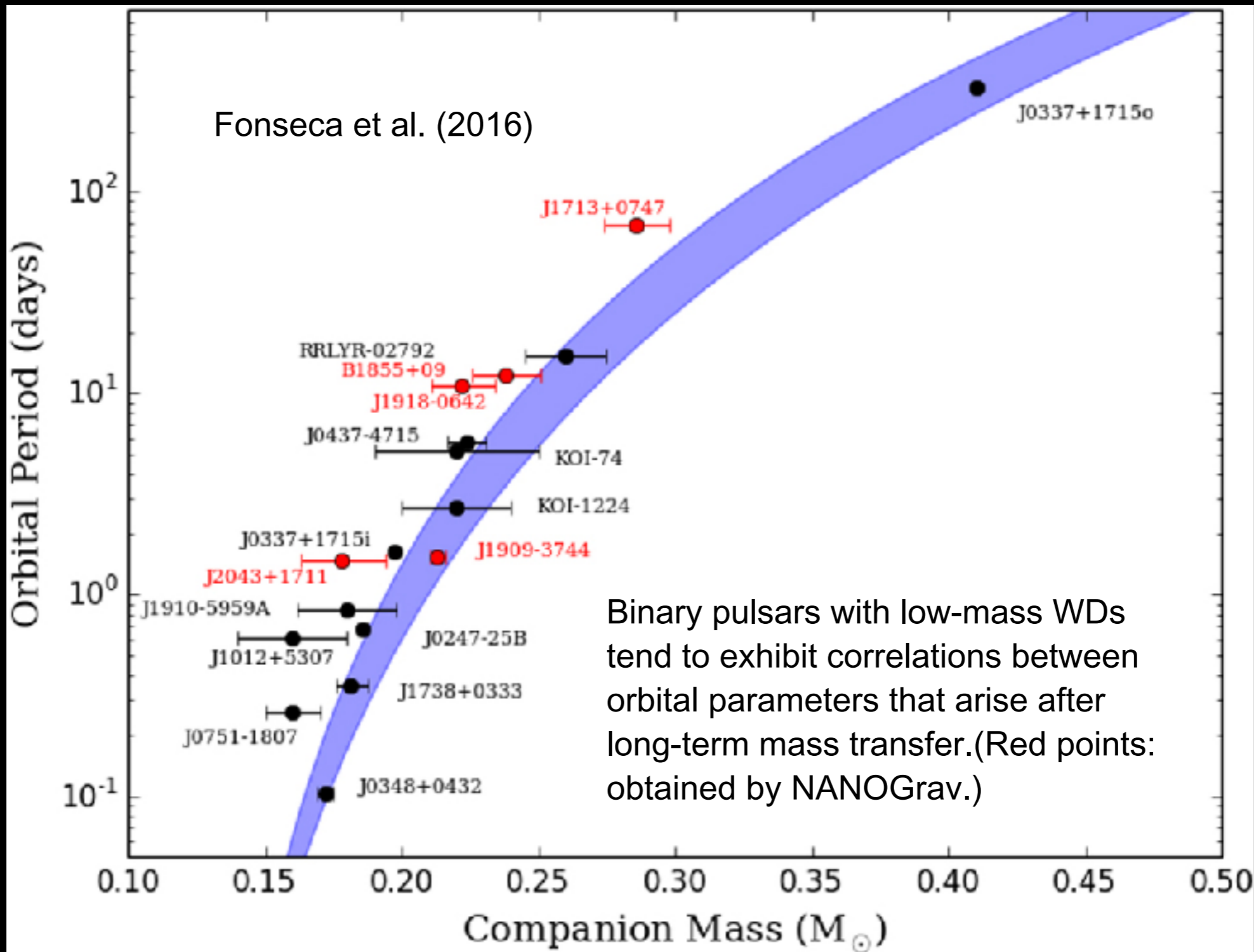


Özel et al. (2012)

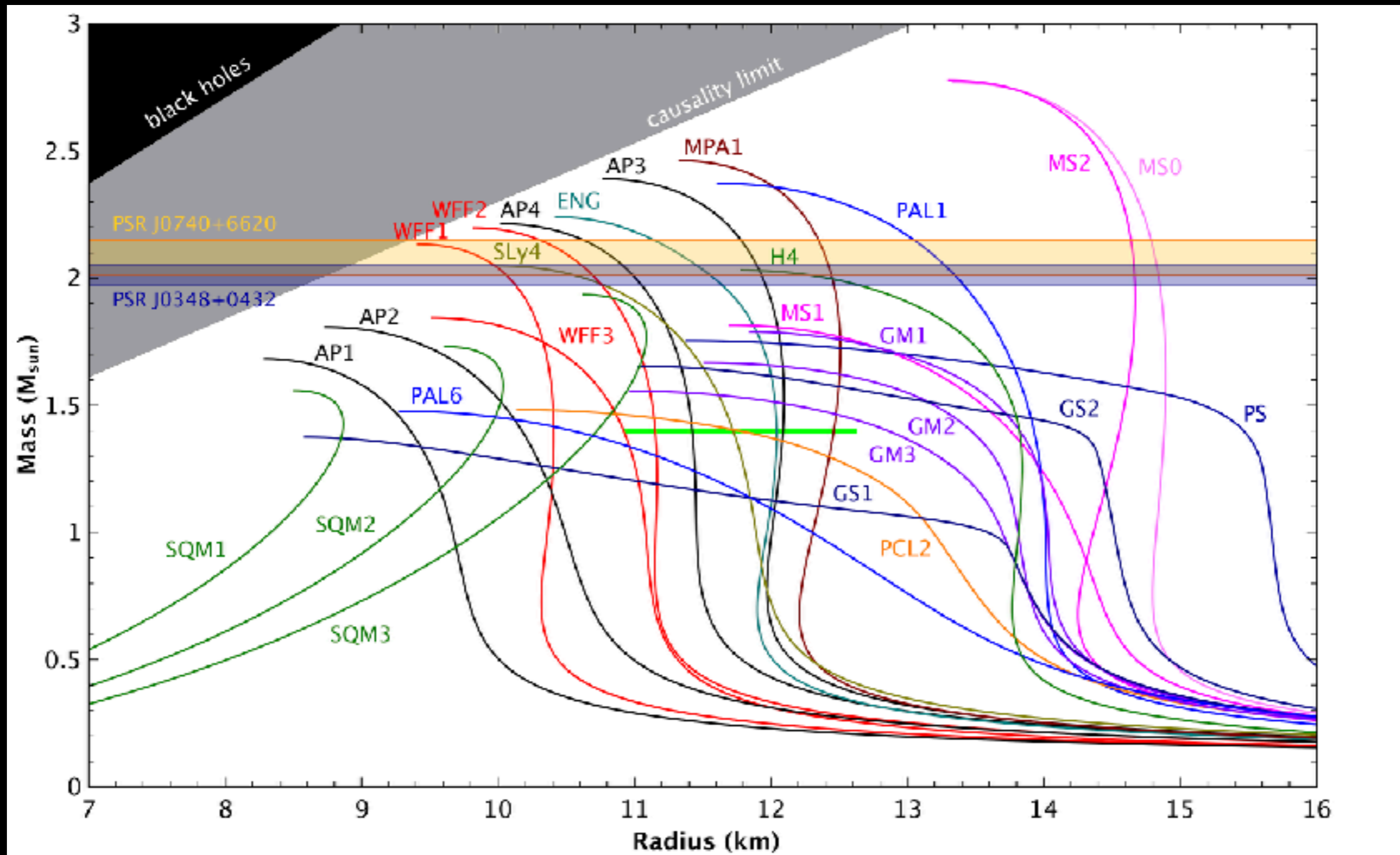


Tauris et al. (2017)

NS/WD Masses & Correlations

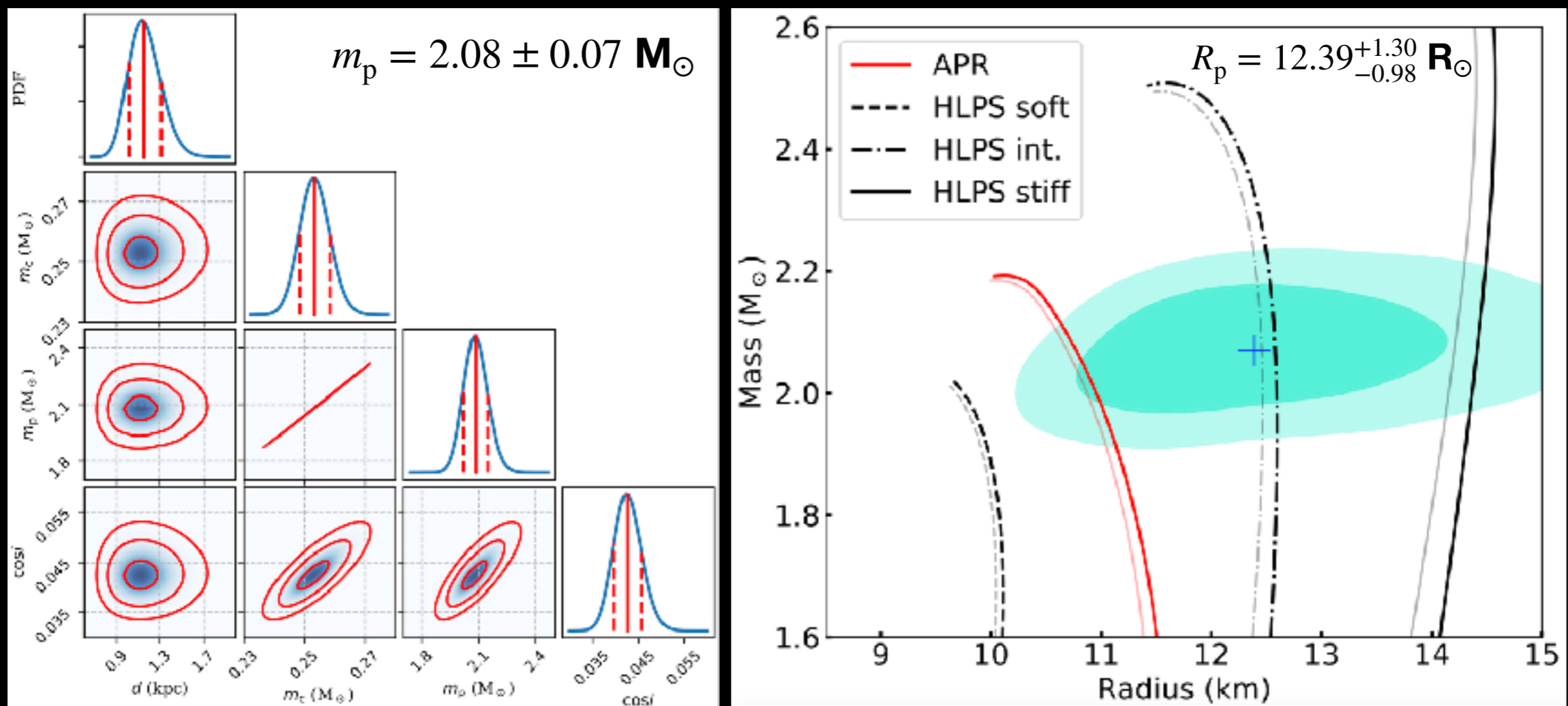


High-mass NSs Constrain EoSs



High-mass NSs are most valuable for EoS science since all EoSs terminate at a specific, **maximum NS mass**. (Credit: N. Wex, P. C. C. Freire.)

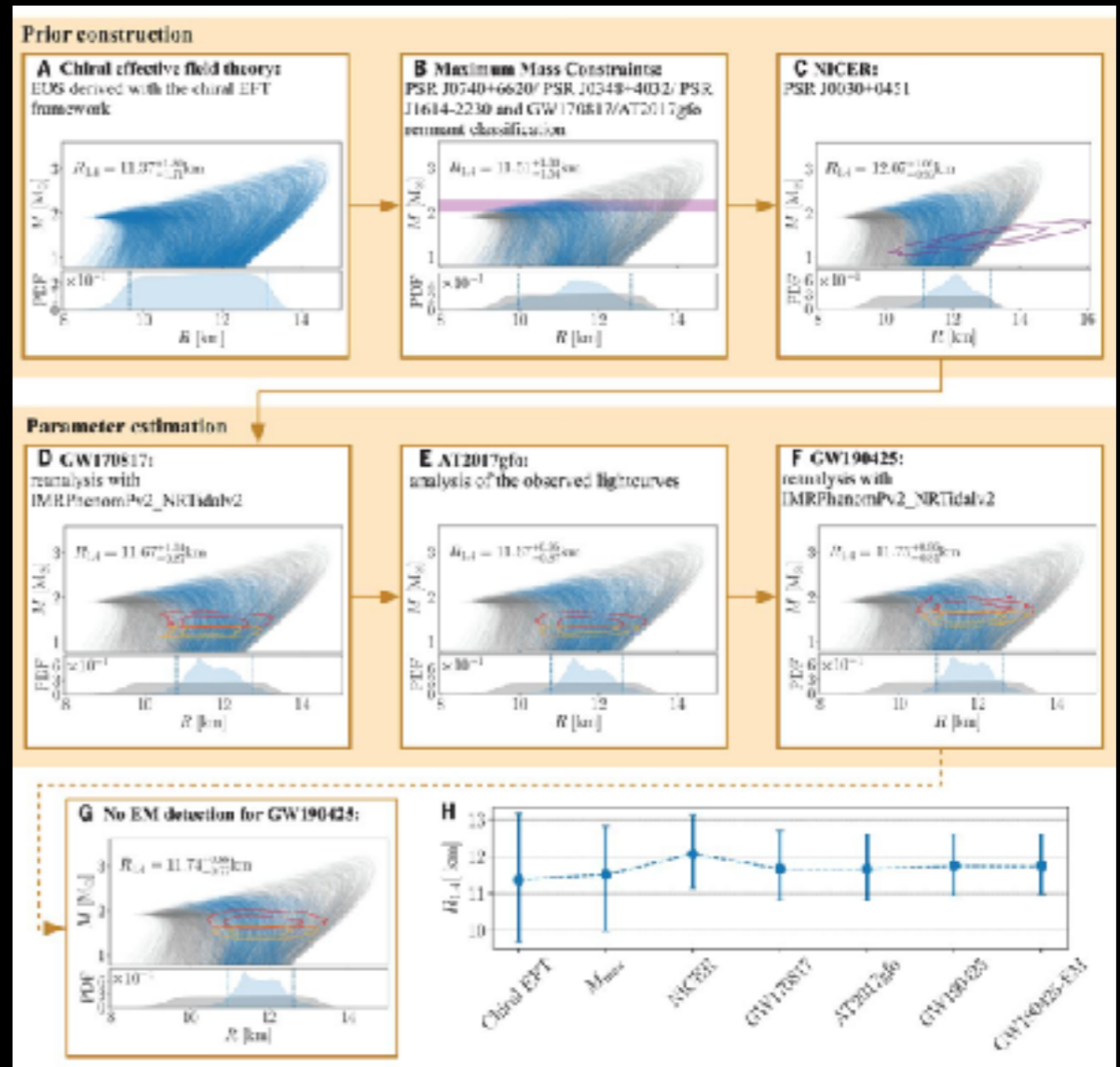
NANOGrav+NICER Constraint on the Radius for PSR J0740+6620



NANOGrav measured the mass of PSR J0740+6620 to $\sim 4\%$ (left; Fonseca et al., 2021), which was then used by NICER to directly measure the radius to $\sim 10\%$ (right; Riley et al., 2021).

Multi-Messenger EoS Constraints

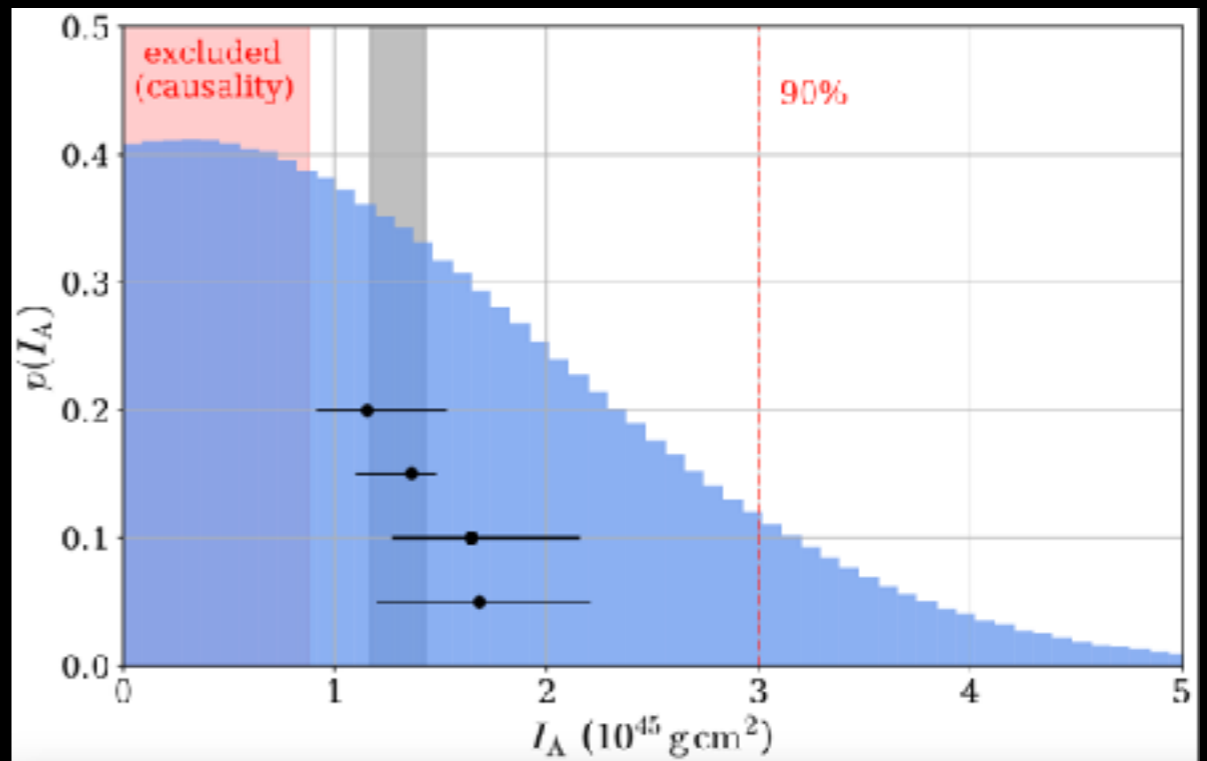
- NS-mass measurements are growing in number due to **multi-messenger opportunities**.
- The union of high-mass outliers and radii measurements allow for unprecedented EoS tests (see right).



Use of radio-timing/X-ray/GW measurements or limits on NS mass/radius to constrain EoS (Dietrich et al., 2020)

Conclusion & Future Prospects

- NANOGrav will produce more Shapiro-delay measurements, fold in non-timing constraints on companion mass and inclination (e.g., **scintillation**).
- Next-generation radio observatories will yield **50-100 more Shapiro-delay measurements**.
- Long-term timing of DNS systems will yield **first measurement of NS moment of inertia** (e.g., Kramer et al., 2021).
- Next-generation X-ray observatories expected to yield **~20 NS radii**.



Constraint on the moment of inertia for PSR J0737-3039A (Kramer et al., 2021).