

Update on DA studies

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- Optics for Collapse and Start of Levelling
- DA tune scans for flat and round optics (v1.6 Optics)
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Collapse process

Collapse process is defined by the target lumi in the range of 1-2.5e34

L-Nb [10^34]	Energy	beta sep	beta cross	MO	Emit [um]	ppb	Crab	sep	crossing	Q'	LHCb - 1.5m / Alice 10m [10^34]	ATS Factor	f _{MO} /g _{MO}	Optics
2.5 - 2200	7	0.7	0.7	450	2.3	2.3	0	0	250	15	0.2/0.014	1	1/1	700 thick, 700 thin
2.5 - 2200	7	0.6	1.2	450	2.3	2.3	0	0	250	15	0.2/0.014	0.83/0.42	1.50/1.21	600 1200 thick, 600 1200 thin
2.5 - 2200	7	0.45	1.8	450	2.3	2.3	0	0	250	15	0.2/0.014	1.1 / 0.28	2.36/1.47	450 1800 thick, 450 1800 thin
2.3 - 2200 or 2.0 - 1960	7	0.5	2	450	2.3	2.3	0	0	250	15	0.2/0.014	1/0.25	2.76/1.56	500 2000 thin
2.5 - 2748 or 1.8 - 1960	7	1.1	1.1	450	2.3	2.3	0	0	250	15	0.2/0.014	1	1/1	1100 thick
2.5 - 2748 or 1.8 - 1960	7	0.9	1.8	450	2.3	2.3	0	0	250	15	0.2/0.014	0.55/0.28	2.56/1.64	900 1800 thick, 900 1800 thin
2.5 - 2748 or 1.8 - 1960	7	0.7	2.8	450	2.3	2.3	0	0	250	15	0.2/0.014	0.71/0.18	4.67/2.02	700 2800 thick, 700 2800 thin
	7	1.0	1.0	450	2.3	2.3	0	0	250	15	0.2/0.014	1	1/1	1000 thick, 1000 thin

$$\begin{cases} \frac{\partial Q_x}{\partial J_x} = \frac{\partial Q_y}{\partial J_y} \propto \frac{I_{MO}}{\gamma} \times \beta_{max}^2 \times f_{MO}(r_X^{Tele}, r_{||}^{Tele}) + \mathcal{O}(\beta_{min}^2) \\ \frac{\partial Q_x}{\partial J_y} = \frac{\partial Q_y}{\partial J_x} \propto \frac{I_{MO}}{\gamma} \times \beta_{min} \times \beta_{max} \times g_{MO}(r_X^{Tele}, r_{||}^{Tele}) \end{cases} \quad \text{with } \begin{cases} f_{MO}(r_x, r_y) \stackrel{def}{=} \frac{1}{8} \left[4 + \left(r_x^2 + \frac{1}{r_x^2} \right) + \left(r_y^2 + \frac{1}{r_y^2} \right) \right] = \frac{1}{8} \left[\left(r_x + \frac{1}{r_x} \right)^2 + \left(r_y + \frac{1}{r_y} \right)^2 \right] \\ g_{MO}(r_x, r_y) \stackrel{def}{=} \frac{1}{2} \left[1 + \frac{1}{4} \left(r_x + \frac{1}{r_x} \right) \left(r_y + \frac{1}{r_y} \right) \right] \end{cases}$$

<https://cds.cern.ch/record/2622595/files/CERN-ACC-2018-0018.pdf>

Tune scan on the bunch with max of long range

Start of levelling

Start of leveling is defined by pile-up e.g. 140

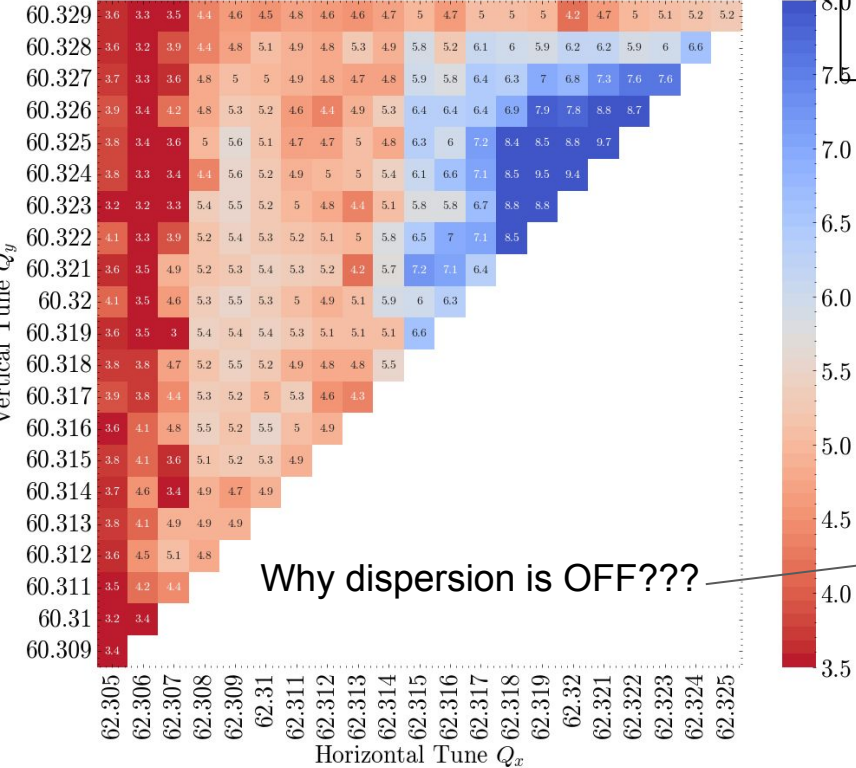
Bunch scheme	Pile up	Energy	beta cross	beta sep	MO	emit	ppb	Crab	sep	crossing	ATS Factor	f_{MO}/g_{MO}	Q'	LHCb - 1.5m / Alice 10m [10 ³⁴]	Optics
hybrid	140	7	0.58	0.58	60	2.5	2.2	190	0	250	1	1/1	15	0.2/0.014	580 1500 thick , 580 1500 thin
hybrid	140	7	0.42	0.84	60	2.5	2.2	190	0	250	0.59/1.19	1.51/1.25	15	0.2/0.014	420 840 thick , 420 840 thin
hybrid	140	7	0.3	1.2	60	2.5	2.2	190	0	250	0.417/1.67	1.74/1.34	15	0.2/0.014	300 1200 thick , 300 1200 thin
8b4e	140	7	0.58	0.58	60	2.5	2.2	190	0	250	1	1/1	5	0.2/0.014	580 thick , 580 thin
8b4e	140	7	0.42	0.84	60	2.5	2.2	190	0	250	0.59/1.19	1.51/1.25	5	0.2/0.014	420 840 thick , 420 840 thin
8b4e	140	7	0.3	1.2	60	2.5	2.2	190	0	250	0.417/1.67	1.74/1.34	5	0.2/0.014	300 1200 thick , 300 1200 thin

Tune scan on the bunch with max of long range

First test scan with 0.5/2.0m flat optics

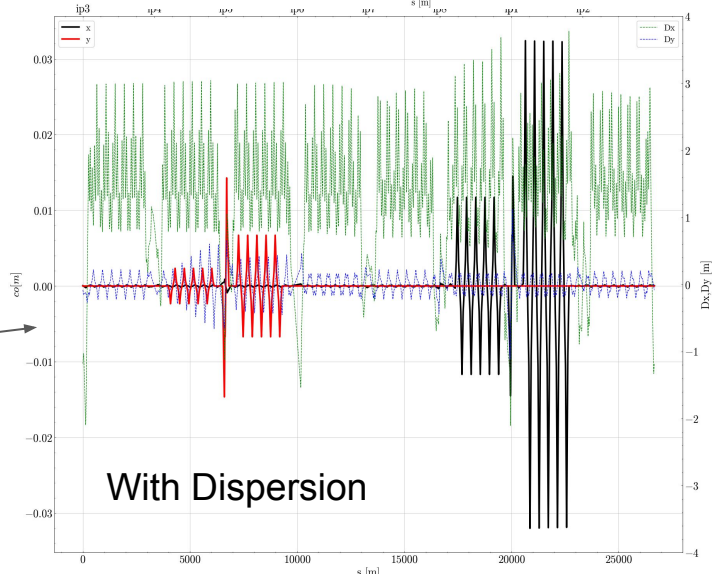
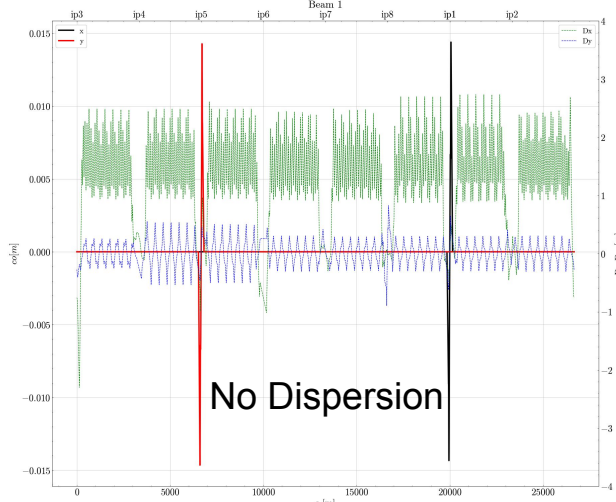
HL-LHC v1.6. Flat Optics. . Bunch 89
 $N_b = 2.3 \cdot 10^{11}$ ppb. $\beta_{y,IP1}^* = 0.5m$, $\beta_{x,IP1}^* = 2.0m$, $\Phi/2_{1,5} = 250\mu rad$
 $\Phi/2_8 = 170\mu rad$, $\epsilon = 2.5\mu m$, $Q' = 5.0$, $I_{MO} = 60A$
 Dispersion = OFF

F.Scheme: 8b4e_1972b_1960_1178_1886_224bpi_12inj_800ns_bs200ns



Dispersion knobs are not optimal for this optics, causes, due to

- sextupoles strength optimized also for off-momentum beta-beating in point 8
- beta function too low to make it effective



Collapse DA tune scans

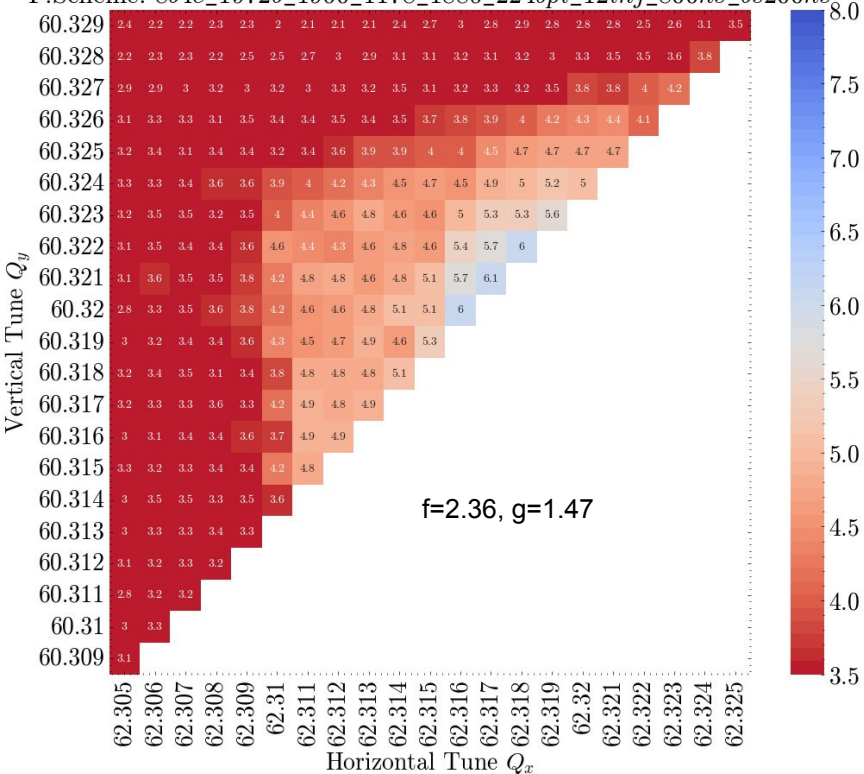
HL-LHC v1.6. Flat Optics. Collapse. Bunch 89

$N_b = 2.3 \cdot 10^{11}$ ppb. $\beta_{y,IP1}^* = 0.45m$, $\beta_{x,IP1}^* = 1.8m$, $\Phi/2_{1,5} = 250\mu rad$

$\Phi/2_8 = 170\mu rad$, $\epsilon = 2.3\mu m$, $Q' = 15.0$, $I_{MO} = 450A$

Dispersion = OFF

F.Scheme: 8b4e_1972b_1960_1178_1886_224bpi_12inj_800ns_bs200ns



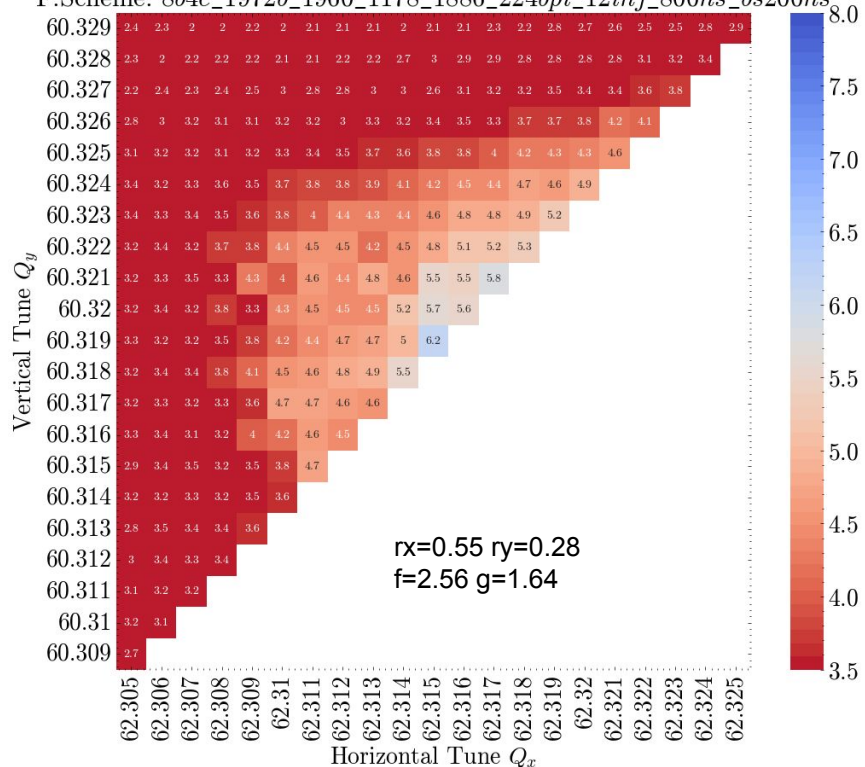
HL-LHC v1.6. Flat Optics. Collapse. Bunch 89

$N_b = 2.3 \cdot 10^{11}$ ppb. $\beta_{y,IP1}^* = 0.9m$, $\beta_{x,IP1}^* = 1.8m$, $\Phi/2_{1,5} = 250\mu rad$

$\Phi/2_8 = 170\mu rad$, $\epsilon = 2.3\mu m$, $Q' = 15.0$, $I_{MO} = 450A$

Dispersion = OFF

F.Scheme: 8b4e_1972b_1960_1178_1886_224bpi_12inj_800ns_bs200ns



Collapse DA tune scans

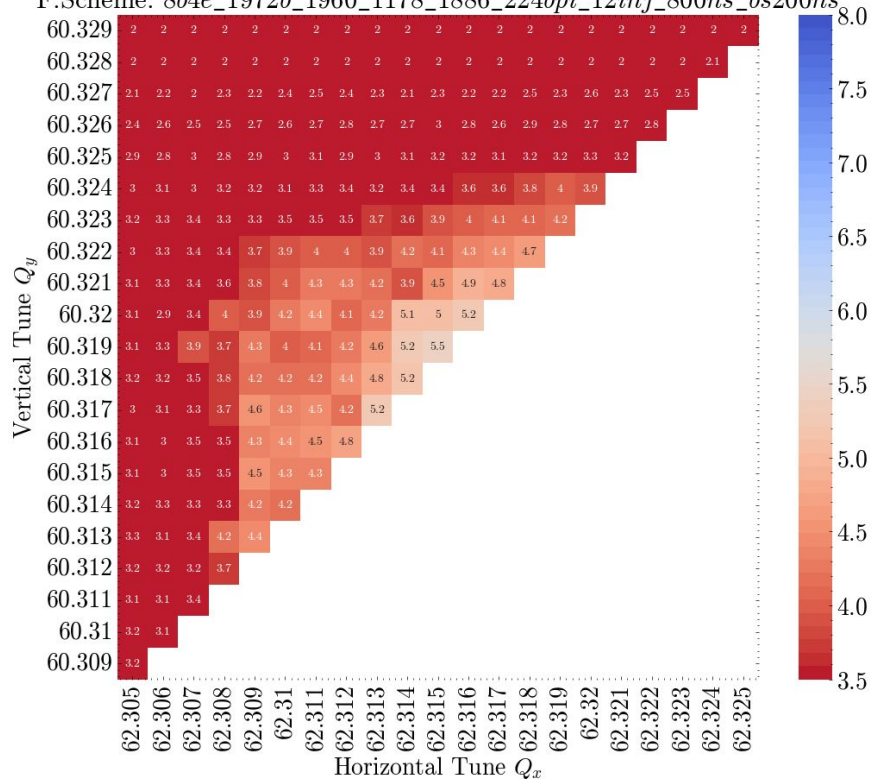
HL-LHC v1.6. Flat Optics. Collapse. Bunch 89

$N_b = 2.3 \cdot 10^{11}$ ppb. $\beta_{y,IP1}^* = 0.7m$, $\beta_{x,IP1}^* = 2.8m$, $\Phi/2_{1,5} = 250\mu rad$

$\Phi/2_8 = 170\mu rad$, $\epsilon = 2.3\mu m$, $Q' = 15.0$, $I_{MO} = 450A$

Dispersion = OFF

F.Scheme: 8b4e_1972b_1960_1178_1886_224bpi_12inj_800ns_bs200ns



Start of Levelling

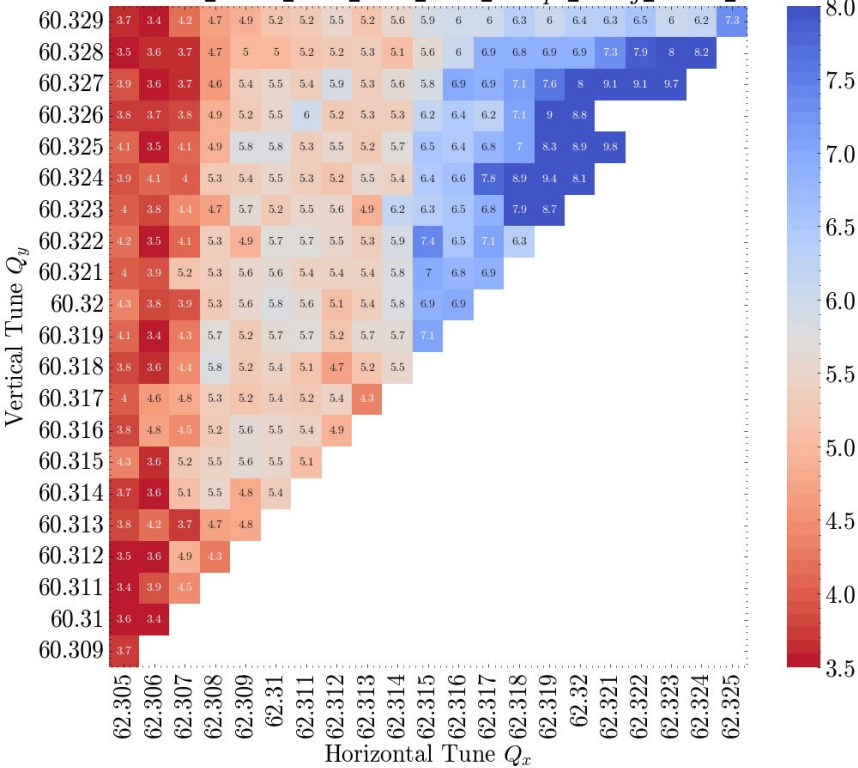
HL-LHC v1.6. Flat Optics. Start of Levelling. Bunch 89

$N_b = 2.2 \cdot 10^{11}$ ppb. $\beta_{y,IP1}^* = 0.3m$, $\beta_{x,IP1}^* = 1.2m$, $\Phi/2_{1,5} = 250\mu rad$

$\Phi/2_8 = 170\mu rad$, $\epsilon = 2.5\mu m$, $Q' = 5.0$, $I_{MO} = 60A$

Dispersion = OFF

F.Scheme: 8b4e_1972b_1960_1178_1886_224bpi_12inj_800ns_bs200ns



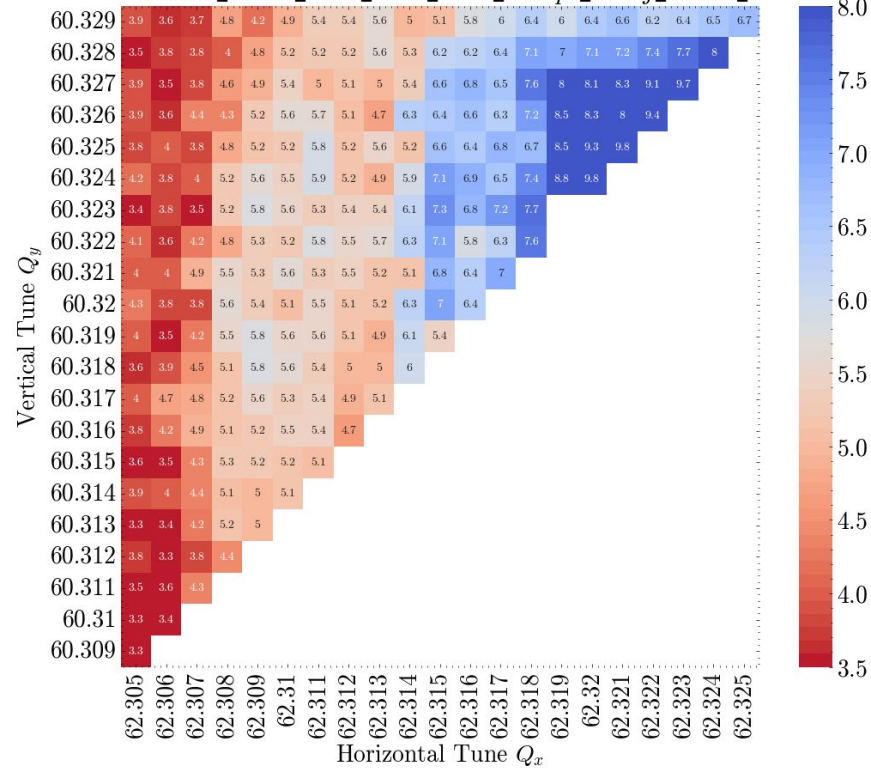
HL-LHC v1.6. Flat Optics. Start of Levelling. Bunch 89

$N_b = 2.2 \cdot 10^{11}$ ppb. $\beta_{y,IP1}^* = 0.3m$, $\beta_{x,IP1}^* = 1.2m$, $\Phi/2_{1,5} = 250\mu rad$

$\Phi/2_8 = 170\mu rad$, $\epsilon = 2.5\mu m$, $Q' = 5.0$, $I_{MO} = 60A$

Dispersion = ON

F.Scheme: 8b4e_1972b_1960_1178_1886_224bpi_12inj_800ns_bs200ns



MO scans

Keeping $Q_y=60.32$

Instead of scanning the diagonal

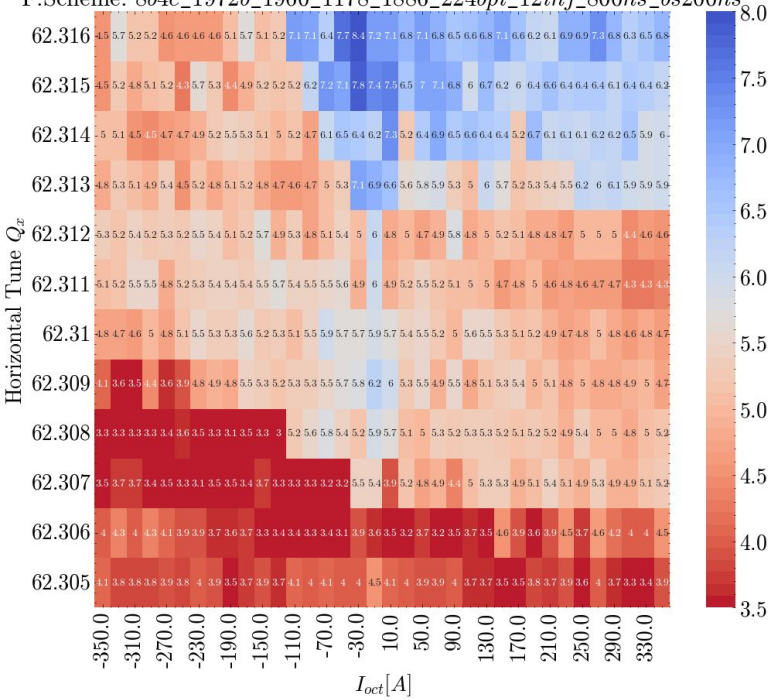
HL-LHC v1.6. Flat Optics. . Bunch 89

$N_b = 2.2 \cdot 10^{11}$ ppb. $\beta_{y,IP1}^* = 0.5m$, $\beta_{x,IP1}^* = 2.0m$, $\Phi/2_{1,5} = 250\mu rad$

$\Phi/2_8 = 170\mu rad$, $\epsilon = 2.5\mu m$, $Q' = 5.0$

Dispersion = OFF

F.Scheme: *8b4e_1972b_1960_1178_1886_224bpi_12inj_800ns_bs200ns*



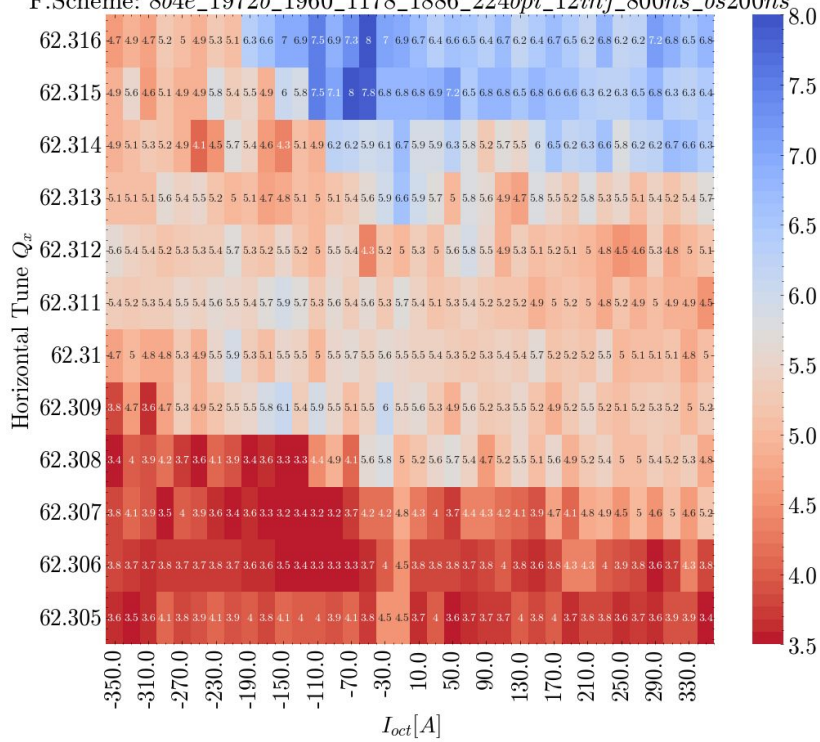
HL-LHC v1.6. Flat Optics. . Bunch 89

$N_b = 2.2 \cdot 10^{11}$ ppb. $\beta_{y,IP1}^* = 0.5m$, $\beta_{x,IP1}^* = 2.0m$, $\Phi/2_{1,5} = 250\mu rad$

$\Phi/2_8 = 170\mu rad$, $\epsilon = 2.5\mu m$, $Q' = 5.0$

Dispersion = ON

F.Scheme: *8b4e_1972b_1960_1178_1886_224bpi_12inj_800ns_bs200ns*



Conclusions and next steps:

- Optics for collapse and start of levelling
- Scans for collapse and SoL can be done without dispersion
- Dispersion knobs not working correctly for all the optics shown

Amp'
detuningSingle
kicksAC-
dipoleOther
method

Summary

Amplitude detuning from an octupole

$$H_n = \frac{1}{B\rho} \operatorname{Re} \left[\frac{1}{n} [B_n(s) + iA_n(s)] (x + iy)^n \right]$$

$$\text{Normal octupole} \rightarrow H_4 = \frac{1}{4!} K_4 L (x^4 - 6x^2y^2 + y^4)$$

In action-angle coordinates $(x, y = \sqrt{2J_{x,y}\beta_{x,y}} \cos \phi_{x,y})$

$$H_4 = \frac{1}{4!} K_4 L (4J_x^2\beta_x^2 \cos^4 \phi_x - 24J_xJ_y \cos^2 \phi_x \cos^2 \phi_y + 4J_y^2\beta_y^2 \cos^4 \phi_y)$$

$$Q_x = \frac{1}{2\pi} \frac{\partial \langle H \rangle}{\partial J_x} = \frac{1}{16\pi} K_4 L (J_x\beta_x^2 - 2J_y\beta_x\beta_y)$$

$$\frac{\partial Q_x}{\partial \epsilon_x} = \frac{1}{32\pi} \beta_x^2 K_4 L \quad \frac{\partial Q_x}{\partial \epsilon_y} = -\frac{1}{16\pi} \beta_x\beta_y K_4 L \quad \frac{\partial Q_y}{\partial \epsilon_y} = \frac{1}{32\pi} \beta_y^2 K_4 L$$