



# Nuclear DFT electromagnetic moments in heavy deformed open-shell odd nuclei

Jacek Dobaczewski, University of York & University of Warsaw

In collaboration with B.C.T. Backes, M. Bender, J. Bonnard, G. Danneaux,  
R.F. Garcia Ruiz, R.P. de Groote, M. Kortelainen, D. Muir, A. Nagpal, W. Nazarewicz,  
A. Sánchez-Fernández, P.L. Sassarini, W. Satuła, X. Sun, J. Wood, H. Wibowo

ISOLDE Workshop and Users meeting 2023  
29 November to 1 December 2023 at CERN, Geneva, Switzerland



Jacek Dobaczewski

UNIVERSITY of York



UK Research  
and Innovation



# Outline

1. Methodology\*
2. Gd-Pb\*
3. Dy
4. Sn-Gd
5. In\*
6. Ag\*
7. Sn\*
8. Sb
9. What next?

\*published



Jacek Dobaczewski

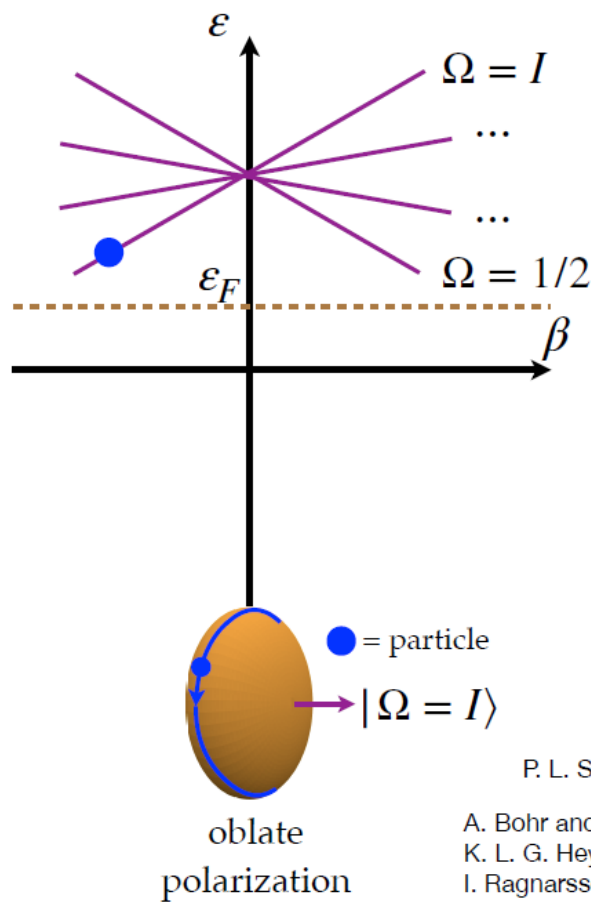
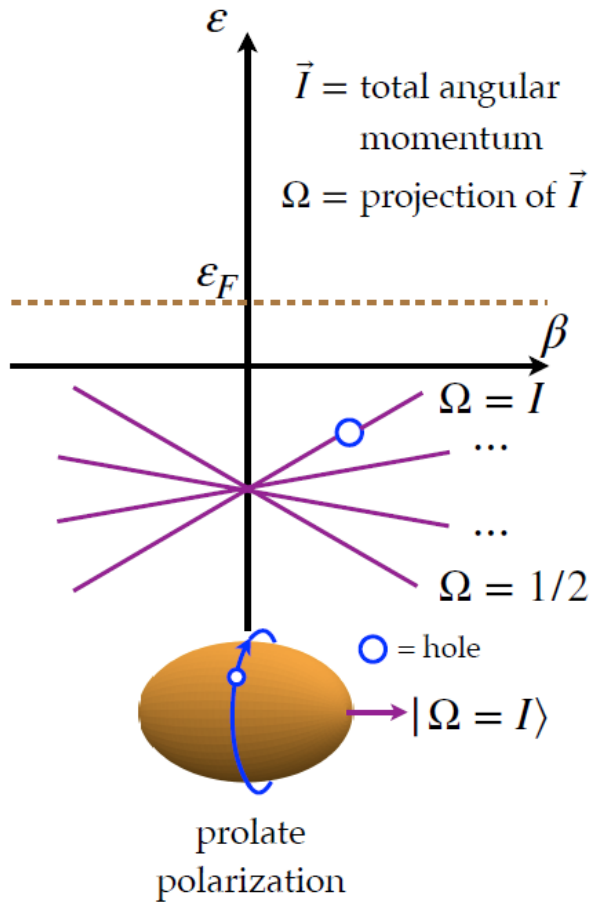
UNIVERSITY *of* York



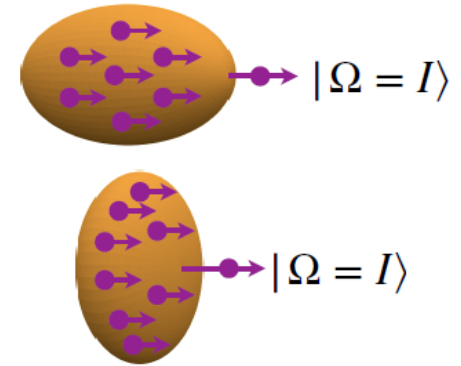
UK Research  
and Innovation



# Shape and spin polarization



Spin polarization



Landau parameter  $g'_0$  ( $g'_0 = 1.7$ )

$$g'_0 = N_0 (2C_1^S + 2C_1^T (3\pi^2 \rho_0 / 2)^{2/3})$$

$$\frac{1}{N_0} \approx 150 \frac{m}{m^*} \text{ MeV} \cdot \text{fm}^3$$

P. L. Sassarini et al., J. Phys. G: Nucl. Part. Phys. **49**, 11LT01 (2022)

A. Bohr and B. R. Mottelson, *Nuclear Structure* Vol. 1

K. L. G. Heyde, *The Nuclear Shell Model*

I. Ragnarsson and S. G. Nilsson, *Shapes and Shells in Nuclear Structure*

Picture: courtesy H. Wibowo



Jacek Dobaczewski

UNIVERSITY of York

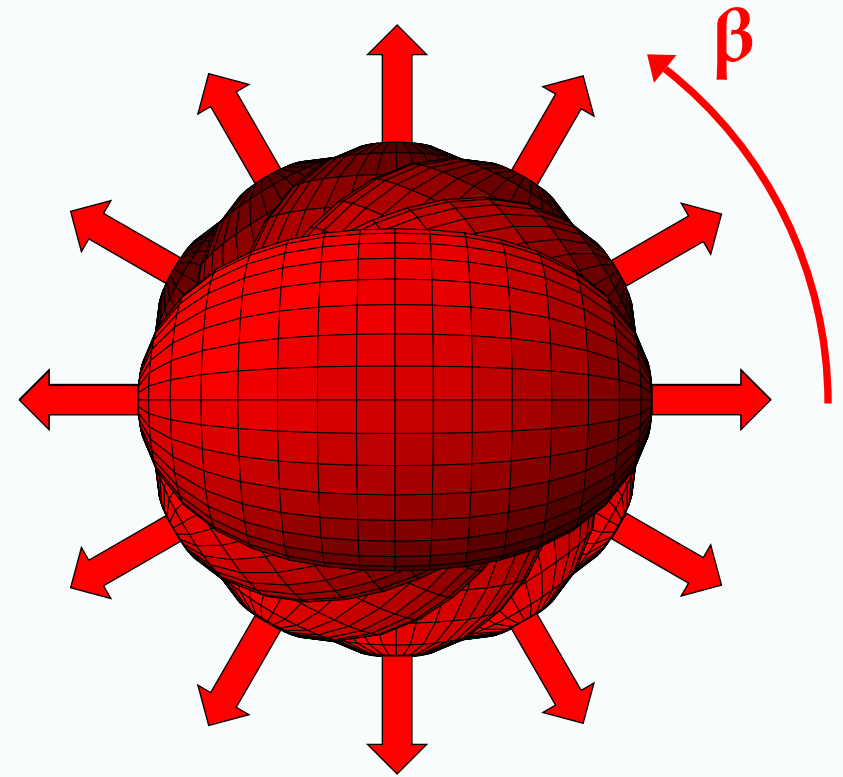
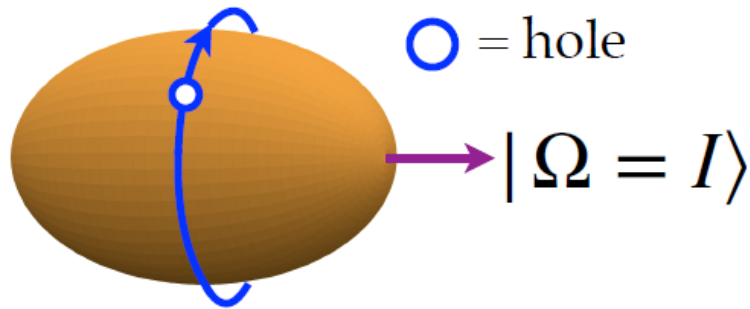
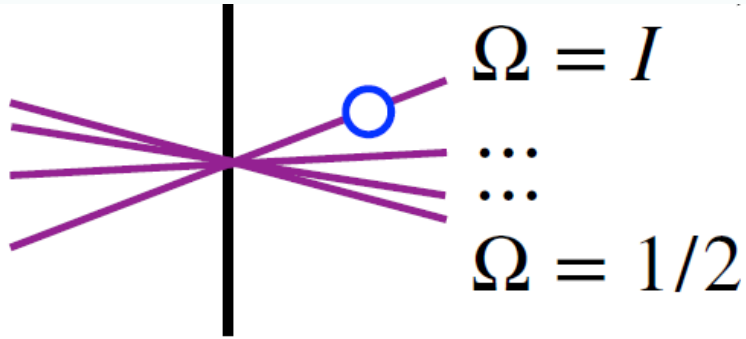
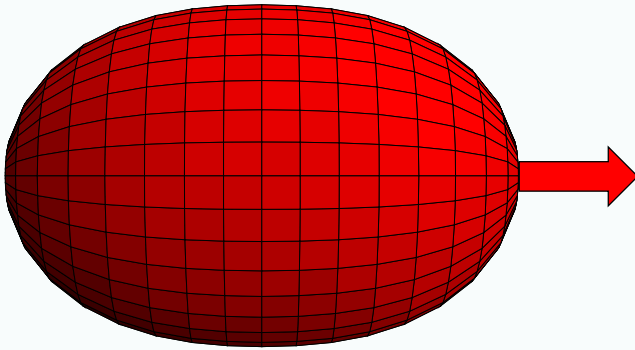


UK Research and Innovation



# Time-odd spin alignment & symmetry restoration

**“Intrinsic”  
Symmetry broken**



**“Laboratory”  
Symmetry restored**

$$|IM\rangle = \mathcal{N}_I \int_{\beta=0}^{\pi} d\beta d_{M\Omega}^I(\beta) |\Omega, \beta\rangle$$

J. A. Sheikh et al., J. Phys. G48, 123001 (2021)



Jacek Dobaczewski

UNIVERSITY of York



UK Research  
and Innovation



# Nuclear quadrupole & dipole moments

Spectroscopic electric quadrupole  $Q$  and magnetic dipole  $\mu$  moments are :

$$Q = \sqrt{\frac{16\pi}{5}} \langle II | \hat{Q}_{20} | II \rangle \quad \text{and} \quad \mu = \sqrt{\frac{4\pi}{3}} \langle II | \hat{M}_{10} | II \rangle .$$

P. Ring and P. Schuck, *The Nuclear Many-Body Problem*

$$\hat{Q}_{20} = \sqrt{\frac{5}{16\pi}} e \sum_{i=1}^A \left( \frac{1}{2} - t_3^{(i)} \right) \{ 3z_i^2 - r_i^2 \}; \quad \hat{M}_{10} = \sqrt{\frac{3}{4\pi}} \mu_N \sum_{i=1}^A \left\{ g_s^{(i)} s_{zi} + g_\ell^{(i)} \ell_{zi} \right\};$$

$$g_s^{(i)} = g_p(g_n) = 5.59(-3.83) \quad g_\ell^{(i)} = 1(0)$$

**Intrinsic moments = moments of the symmetry-broken state**  
**Spectroscopic moments = moments of the symmetry-restored state**

**Spectroscopic moments = moments measured experimentally**



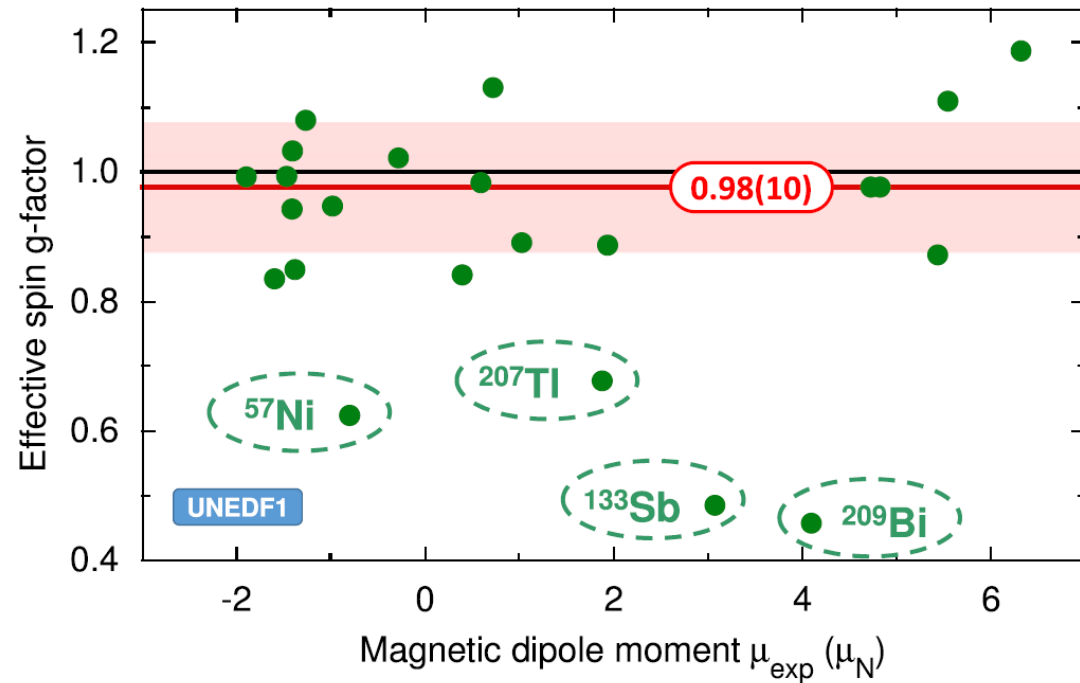
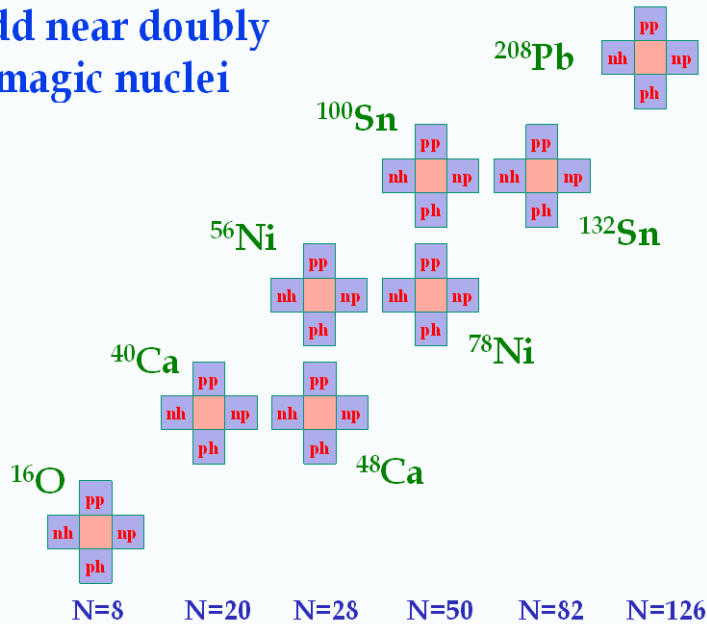
# Effective spin g-factor? Who ordered that?

P. Sassarini et al., J. Phys. G49 (2022) 11LT01

$$g_s^{(i)} = g_p(g_n) = 5.59(-3.83) \times g^{\text{eff}} ???$$

$$g_\ell^{(i)} = 1(0)$$

Odd near doubly  
magic nuclei



Jacek Dobaczewski

UNIVERSITY of York



UK Research and Innovation



# The bottom line

**The nuclear electromagnetic moments of odd nuclei are all about:**

- 1. Polarization**
- 2. Self-consistency**
- 3. Symmetry restoration**



Jacek Dobaczewski

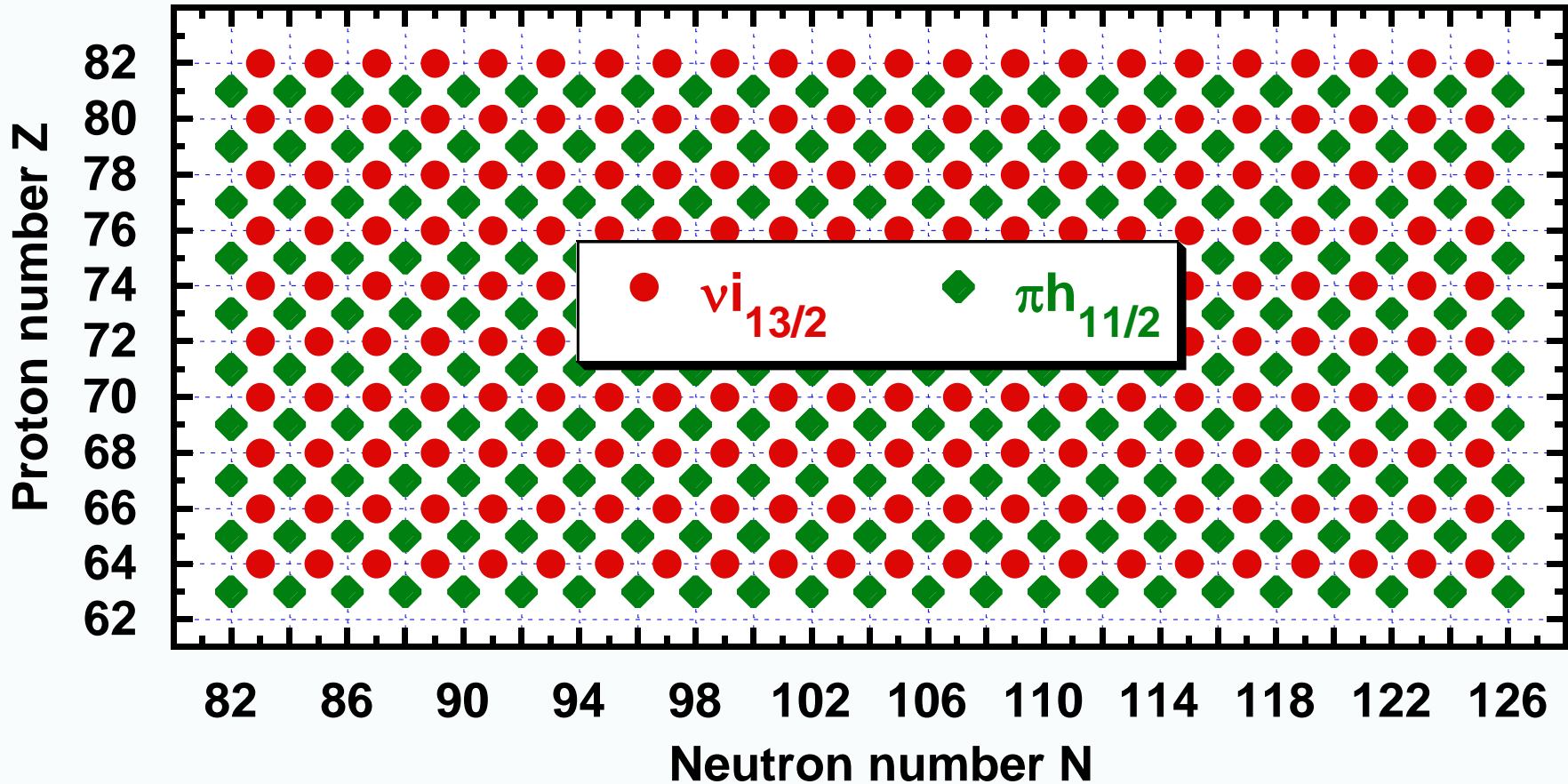
UNIVERSITY *of* York



UK Research  
and Innovation



# The first systematic nuclear-DFT analysis of the electromagnetic moments in heavy deformed open-shell odd nuclei



Blocked quasiparticles were tagged by the neutron  $i_{13/2}$  ( $\Omega=+13/2$ ) or proton  $h_{11/2}$  ( $\Omega=+11/2$ ) single-particle orbitals

J. Bonnard *et al.*, Phys. Lett. B 843 (2023) 138014



Jacek Dobaczewski

UNIVERSITY of York

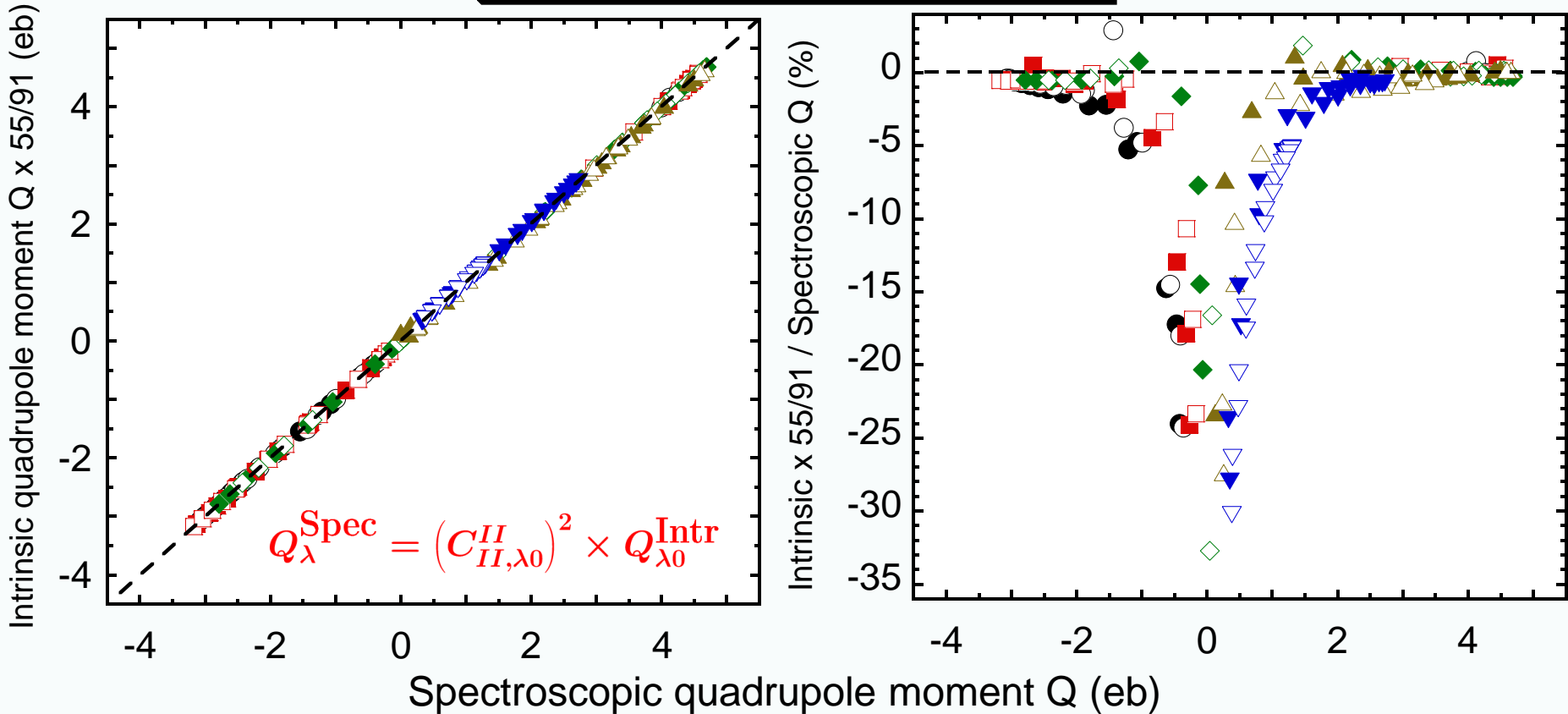


UK Research and Innovation





# Heavy deformed $\pi 11/2^-$ odd-Z nuclei



## Conclusion:

Spectroscopic electric quadrupole moments can be inferred from the intrinsic ones at  $\sim 5\%$  precision only at  $|Q| > 1b$ )

J. Bonnard *et al.*, Phys. Lett. B 843 (2023) 138014



Jacek Dobaczewski

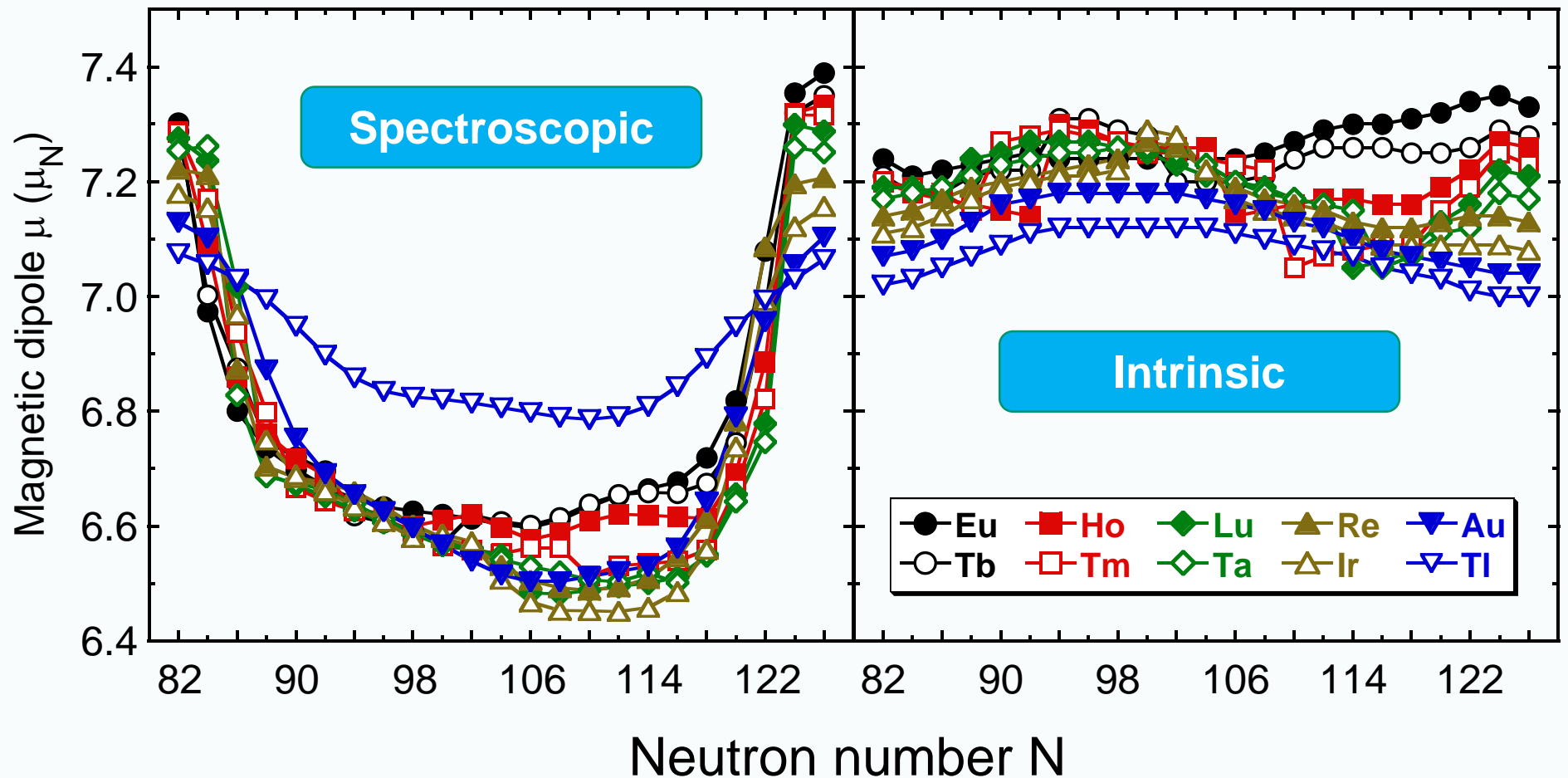
UNIVERSITY of York



UK Research and Innovation



# Heavy deformed $\pi 11/2^-$ odd-Z nuclei



**Conclusion:**  
Spectroscopic magnetic dipole moments  
cannot be inferred from the intrinsic ones

J. Bonnard *et al.*, Phys. Lett. B 843 (2023) 138014



Jacek Dobaczewski

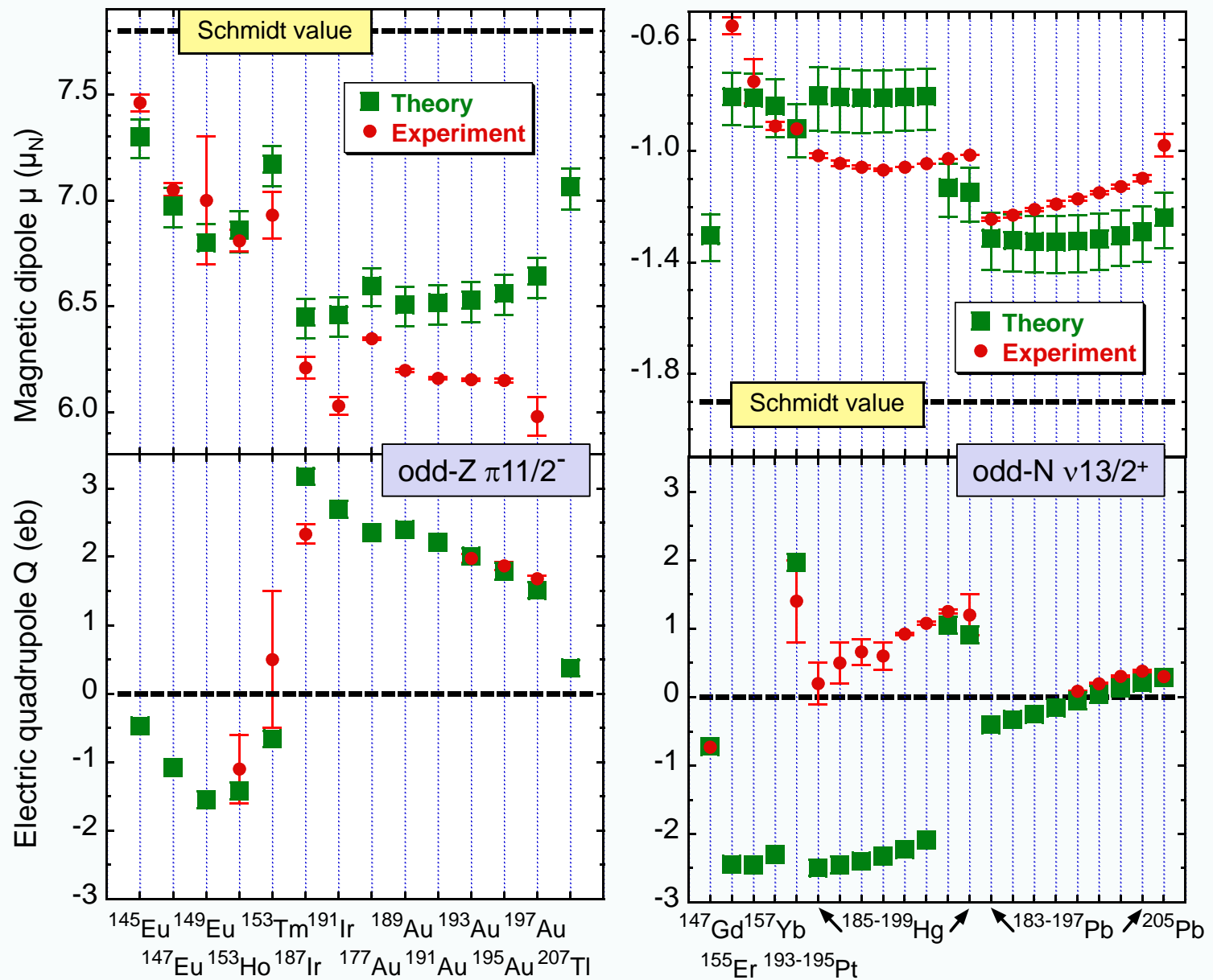
UNIVERSITY of York



UK Research  
and Innovation



# Spectroscopic moments: theory vs. experiment



J. Bonnard *et al.*, Phys. Lett. B 843 (2023) 138014



Jacek Dobaczewski

UNIVERSITY of York

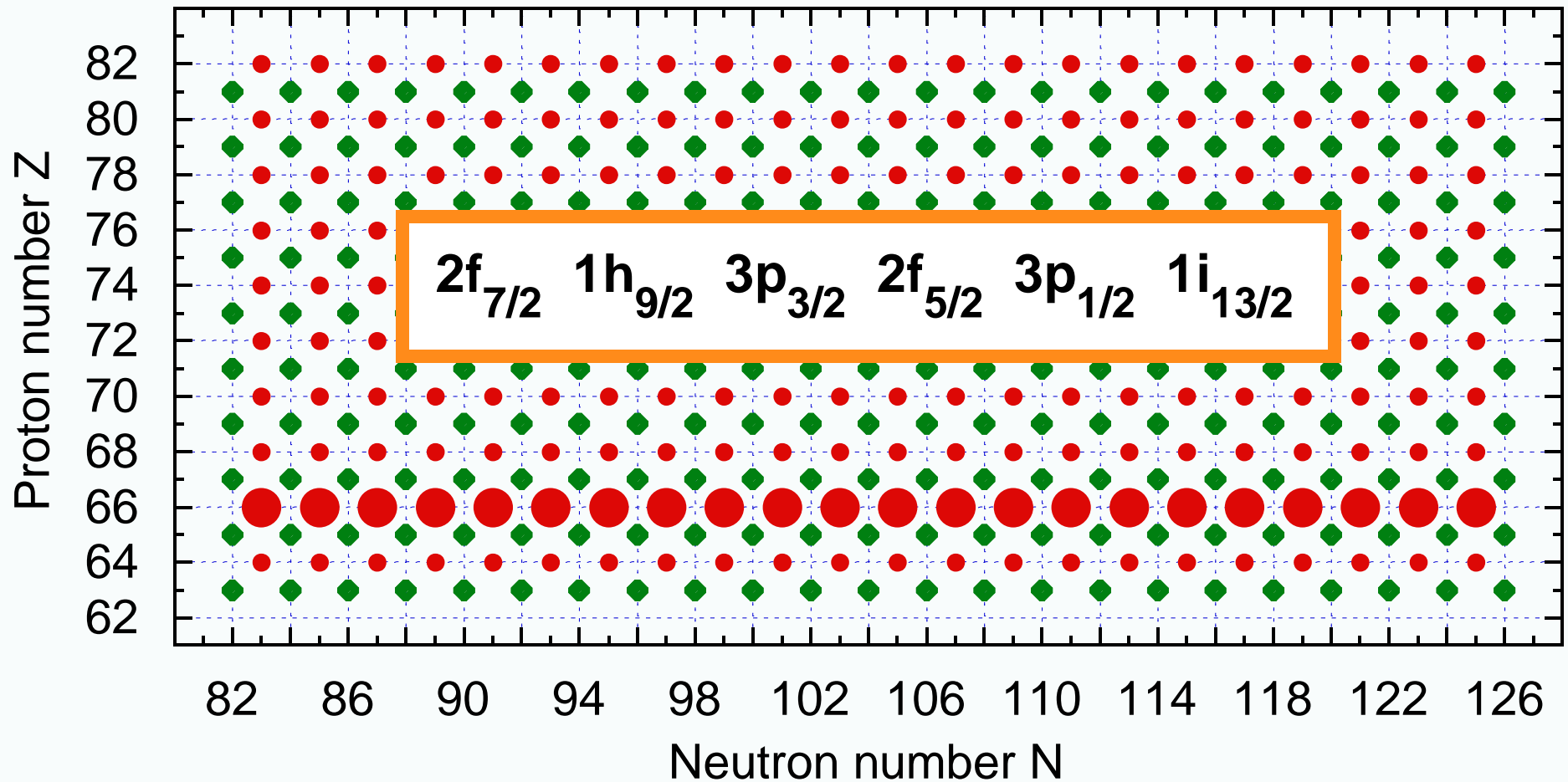


UK Research and Innovation



# The first systematic nuclear-DFT analysis of the electromagnetic moments in excited quasiparticle states

J. Dobaczewski *et al.*, to be published



Jacek Dobaczewski

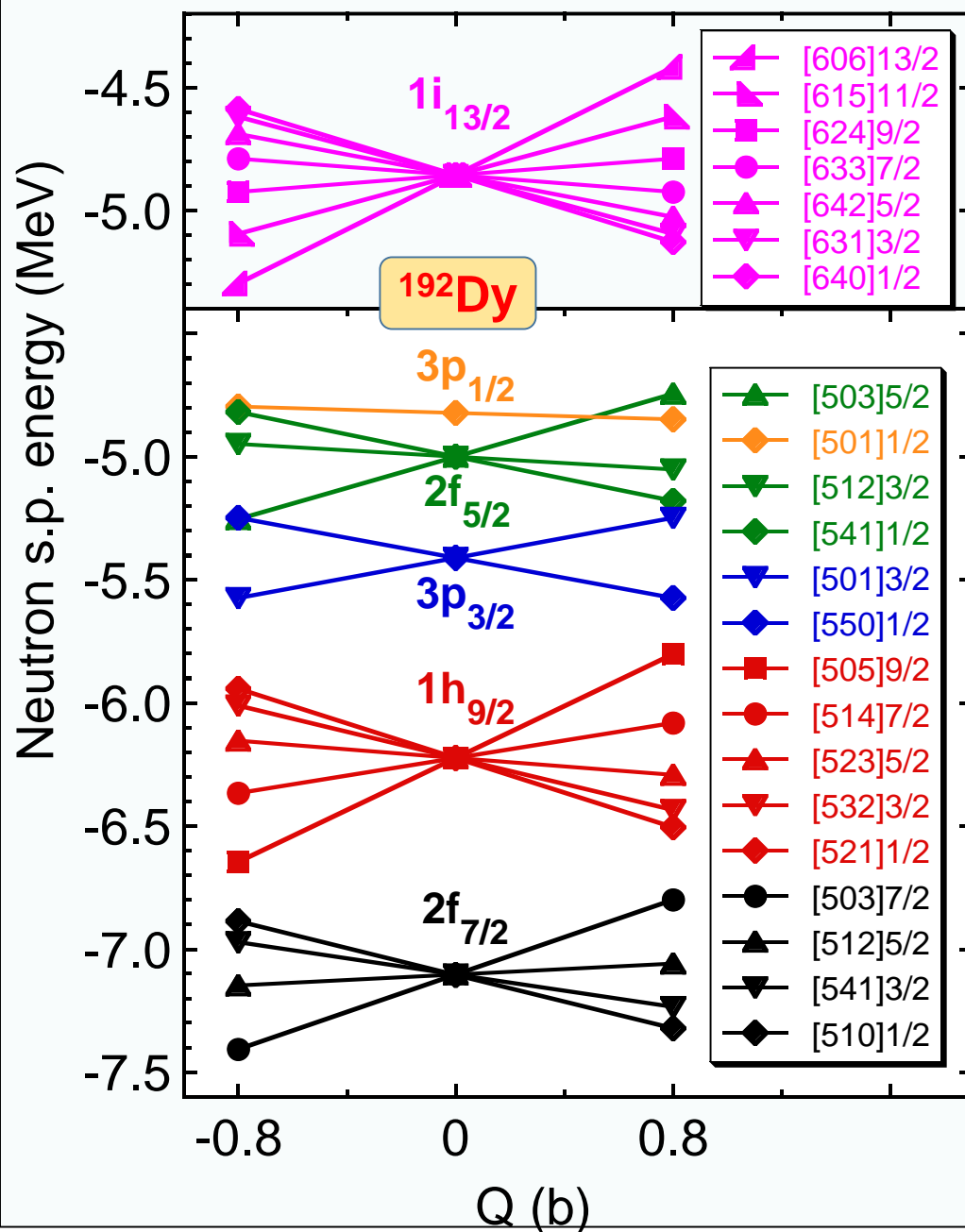
UNIVERSITY of York



UK Research and Innovation



# How to calculate odd nuclei in nuclear DFT?



without pairing

$A$  even,  $p > A$ ,  $h \leq A$

$$|\Psi\rangle_{\text{HF}}^{\text{even}} = a_A^+ \dots a_2^+ a_1^+ |0\rangle$$

$$|\Psi\rangle_{\text{HF}}^{\text{odd}} = \begin{cases} a_p^+ |\Psi\rangle_{\text{HF}}^{\text{even}} \\ a_h |\Psi\rangle_{\text{HF}}^{\text{even}} \end{cases}$$

with pairing

$$|\Psi\rangle_{\text{HFB}}^{\text{even}} = \prod_{\mu>0} (u_\mu + v_\mu a_\mu^+ a_\mu^+) |0\rangle$$

$$|\Psi\rangle_{\text{HFB}}^{\text{odd}} = \beta_\nu^+ |\Psi\rangle_{\text{HFB}}^{\text{even}}$$

$$= a_\nu^+ \prod_{\nu \neq \mu > 0} (u_\mu + v_\mu a_\mu^+ a_\mu^+) |0\rangle$$

tagging quasiparticle states

$$\max_\mu \{ \langle \varphi_\nu | \phi_\mu^{\text{upper}} \rangle, \langle \varphi_\nu | \phi_\mu^{\text{lower}} \rangle \}$$



Jacek Dobaczewski

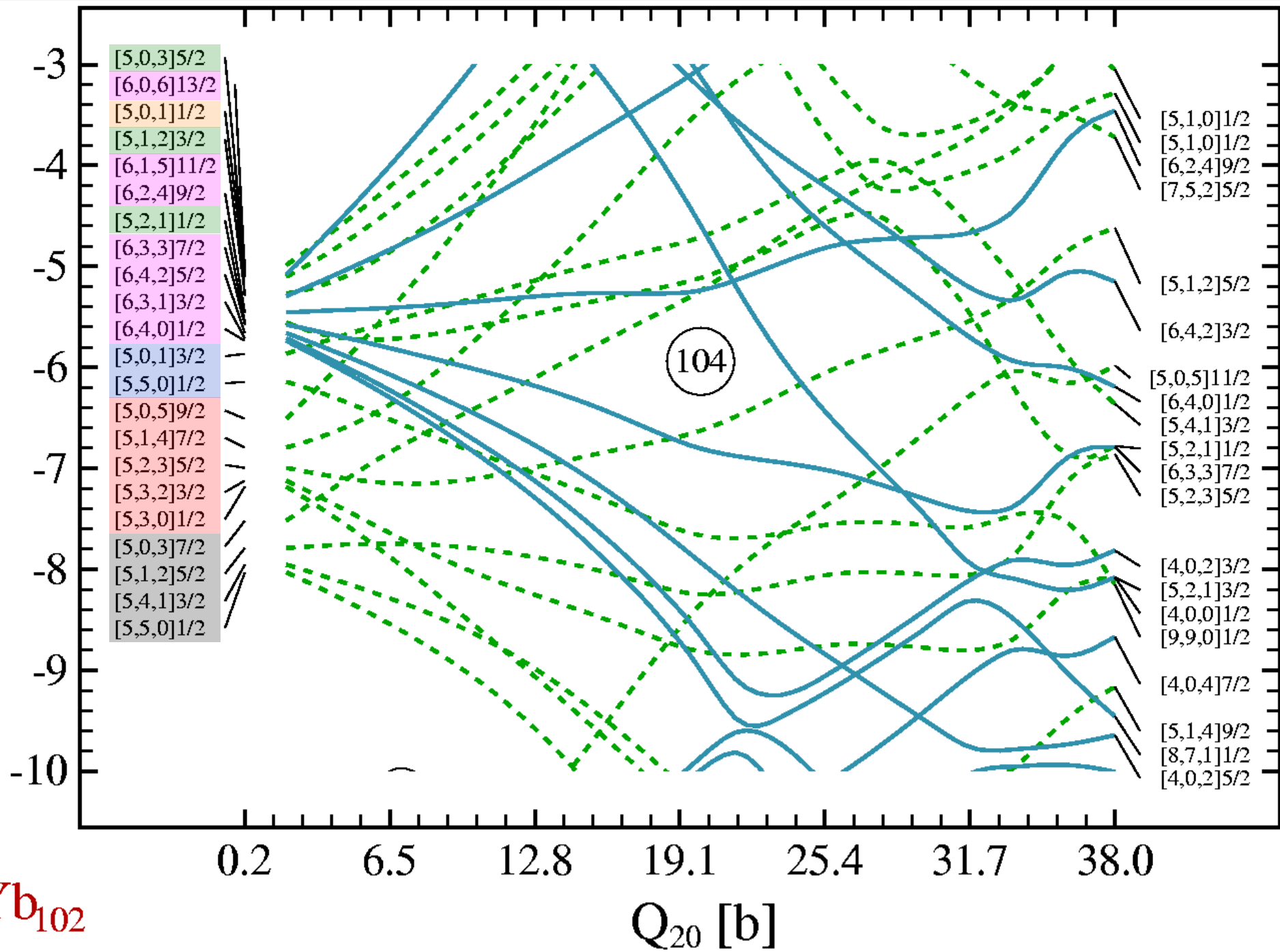
UNIVERSITY of York



UK Research and Innovation



Single-neutron Energies [MeV]



$^{172}_{70}\text{Yb}_{102}$



Jacek Dobaczewski

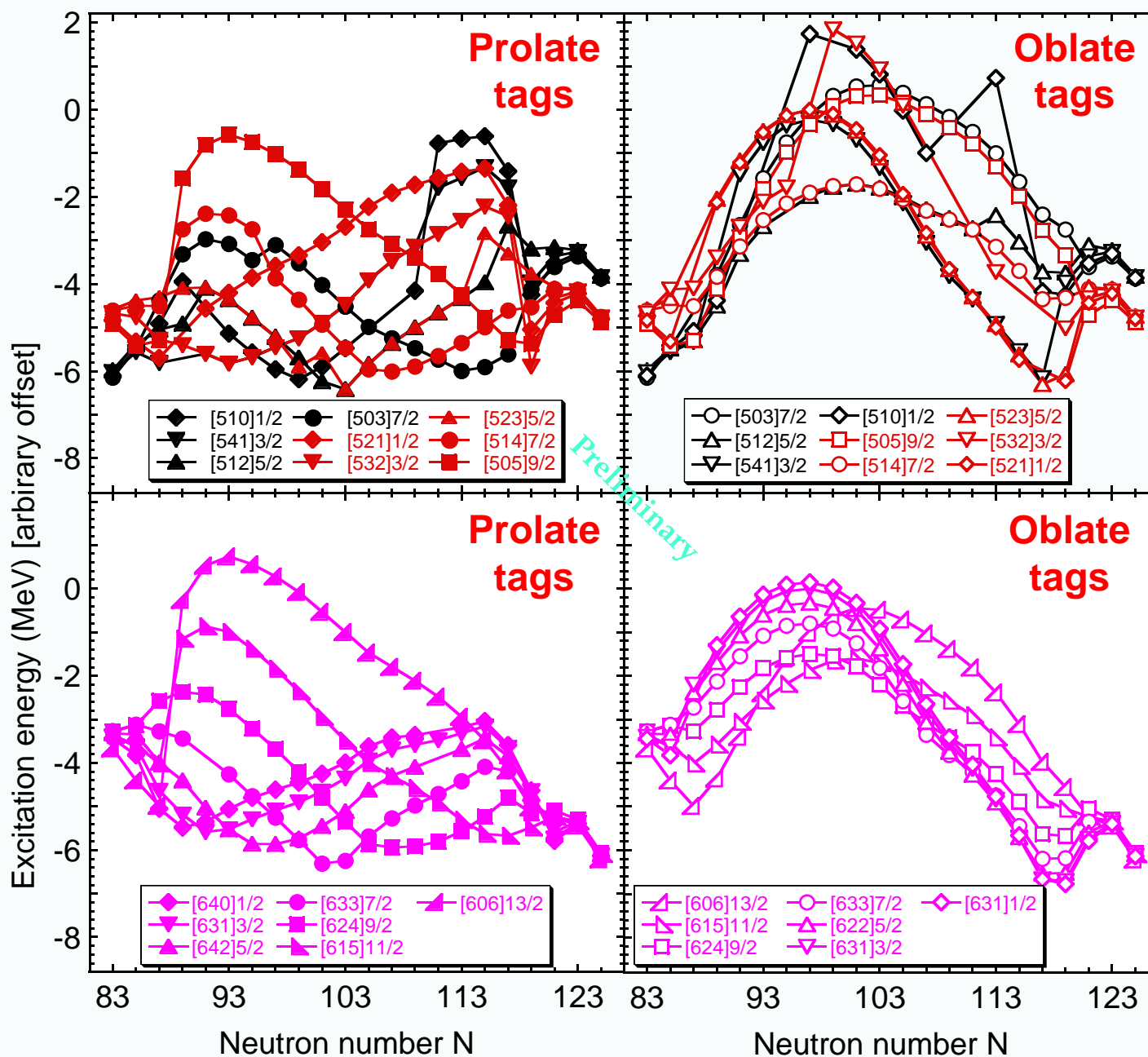
UNIVERSITY of York



UK Research and Innovation



# Excitation energies of odd dysprosium isotopes



Jacek Dobaczewski

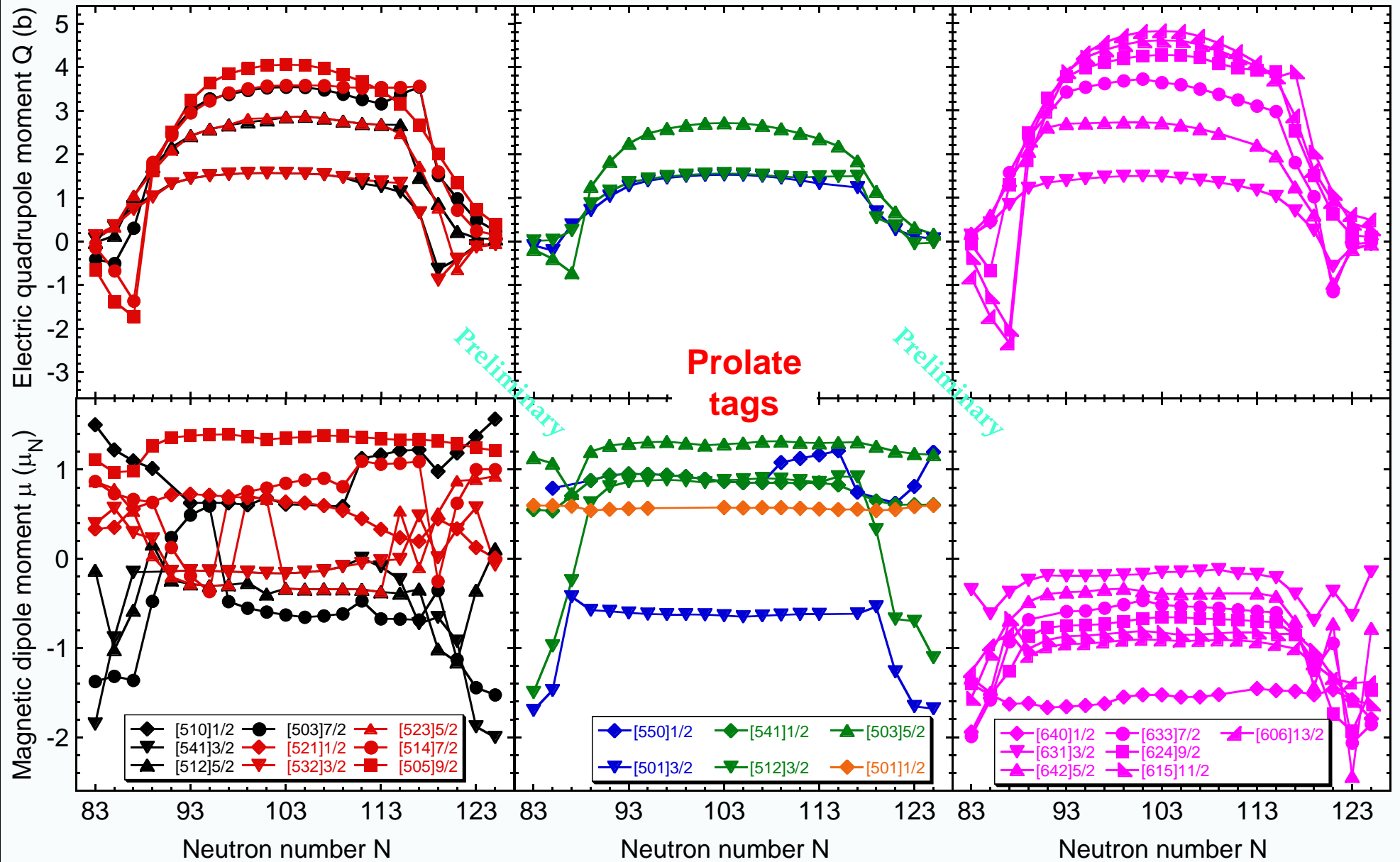
UNIVERSITY of York



UK Research and Innovation



# Electromagnetic moments of odd dysprosium isotopes



Jacek Dobaczewski

UNIVERSITY of York

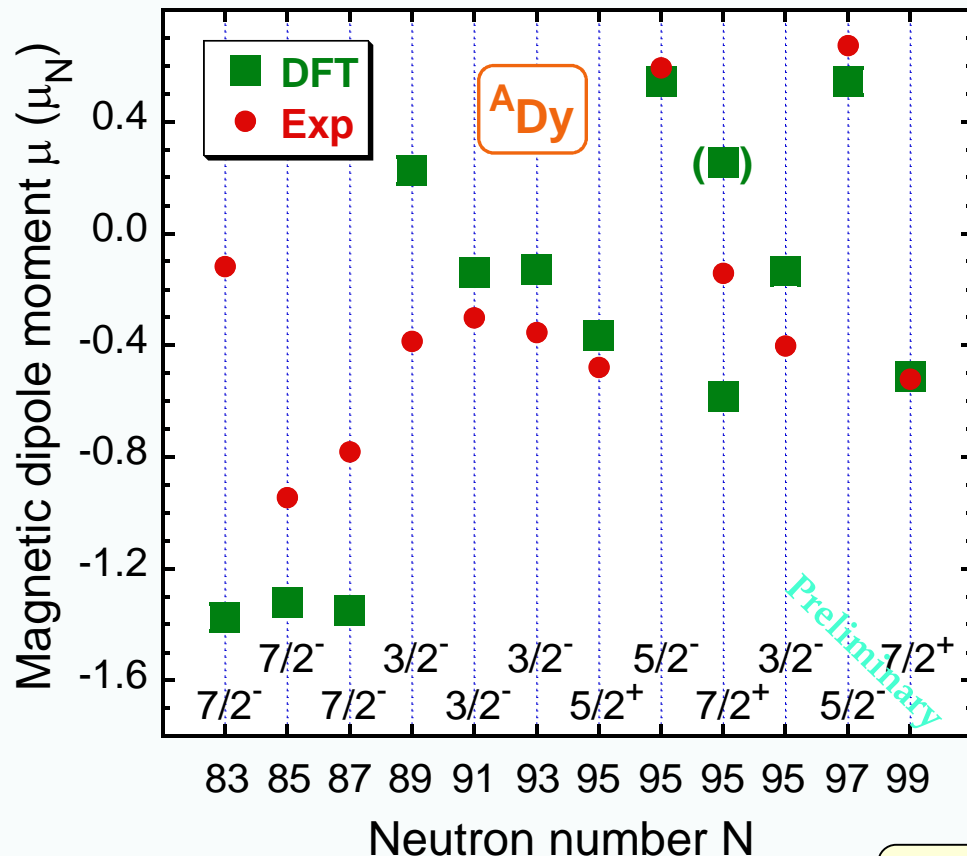
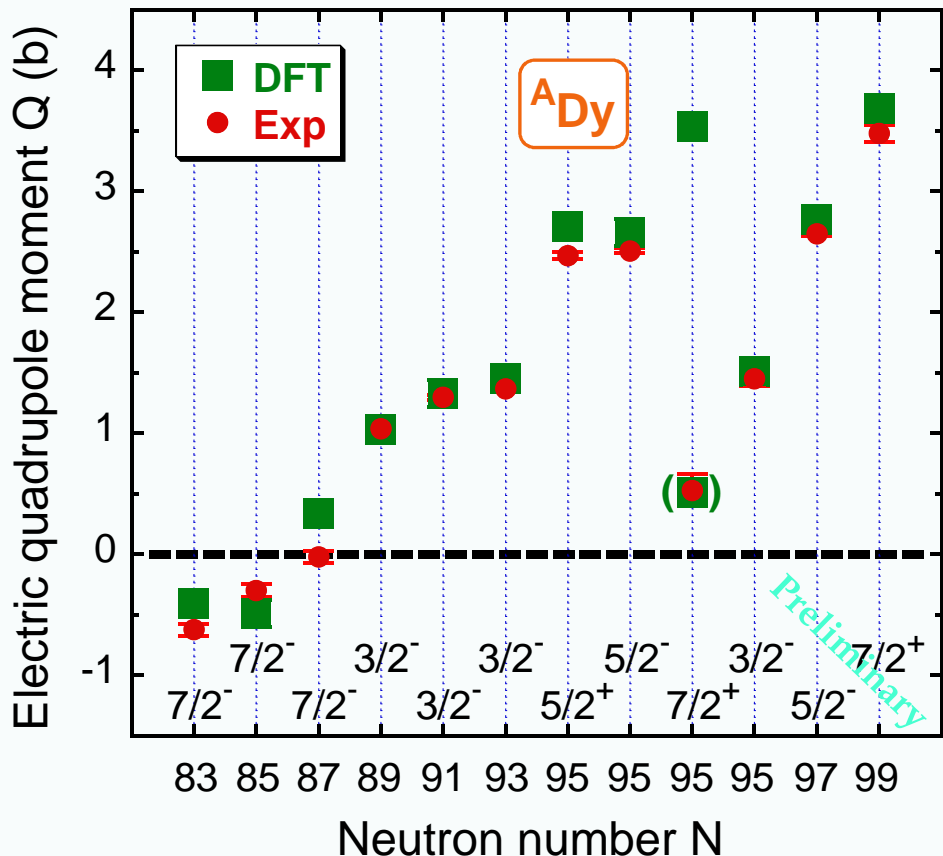


UK Research and Innovation





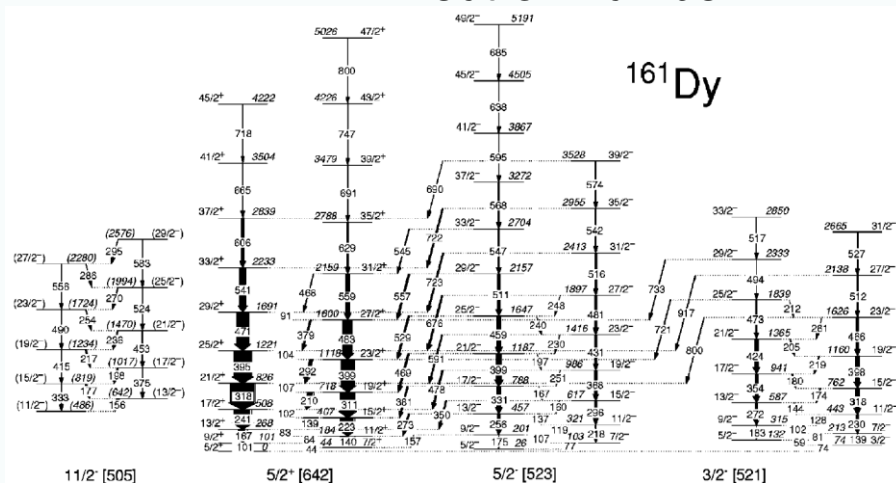
# Electromagnetic moments of odd dysprosium isotopes



$9/2+$	100.4	$7/2-$	103.0	$5/2-$	131.7
	*			$3/2-$	74.6
$7/2+$	43.8				*
	*	$5/2-$	25.7		
$5/2+$	0		*		
	*				

**$^{161}Dy$**

S. J. Margraf et al.,  
Phys. Rev. C52, 2429 (1995)



A. Junglauss et al.,  
Phys. Rev. C67, 034302 (2003)



Jacek Dobaczewski

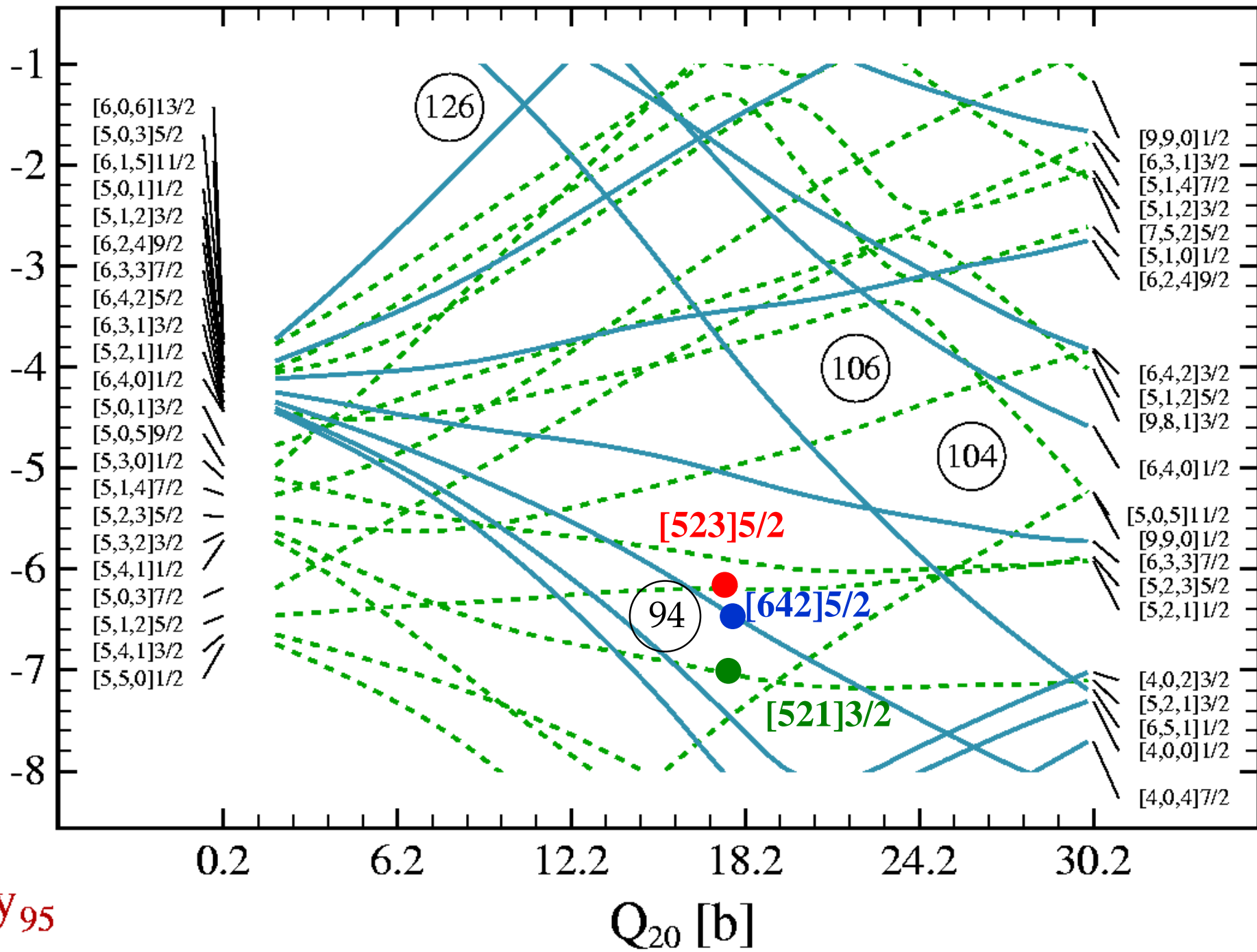
UNIVERSITY of York



UK Research and Innovation



# Single-neutron Energies [MeV]



Jacek Dobaczewski

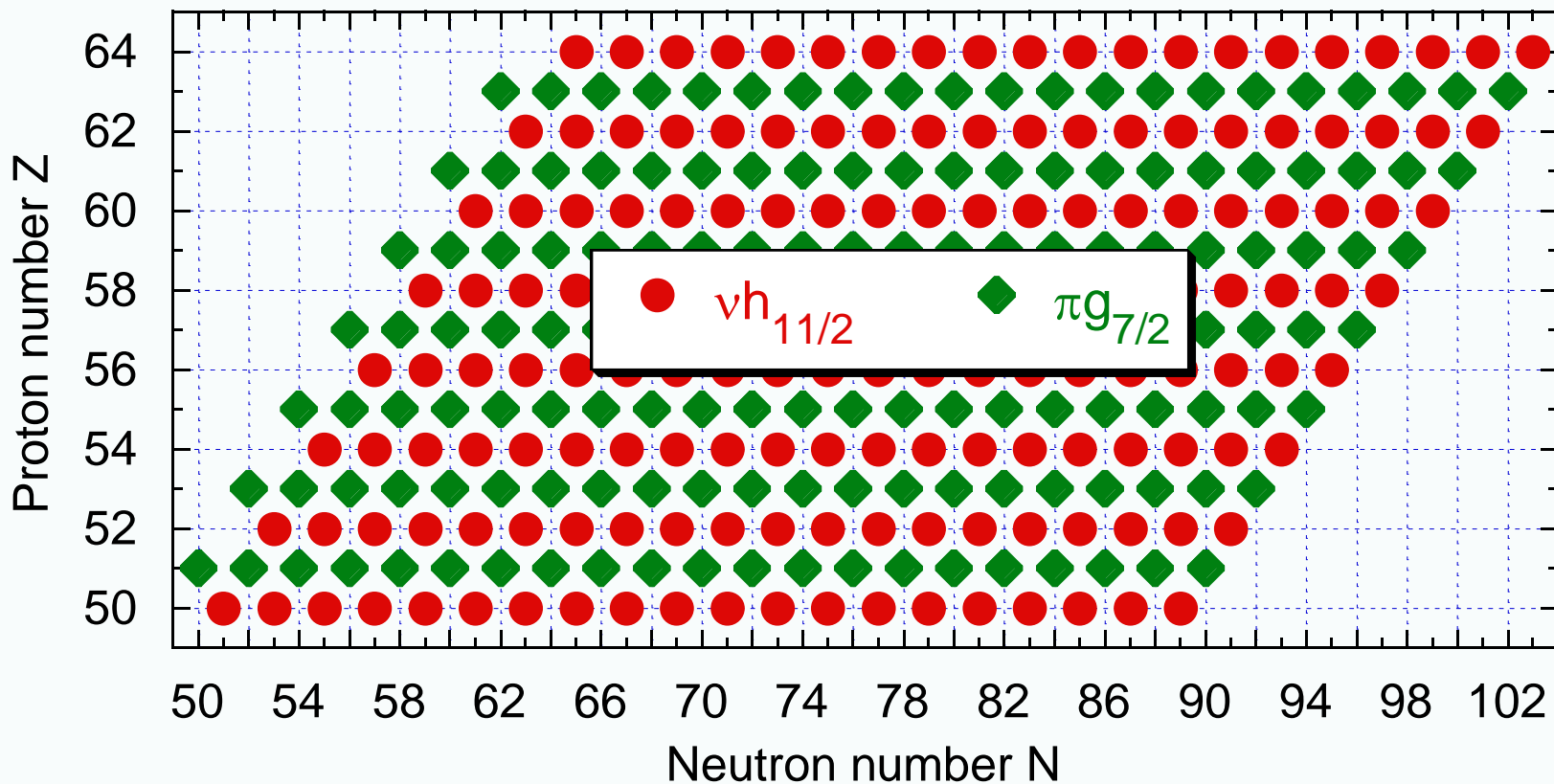
UNIVERSITY of York



UK Research and Innovation



# Nuclear-DFT analysis of electromagnetic moments between the Sn and Gd isotopes



H. Wibowo *et al.*, to be published



Jacek Dobaczewski

UNIVERSITY of York

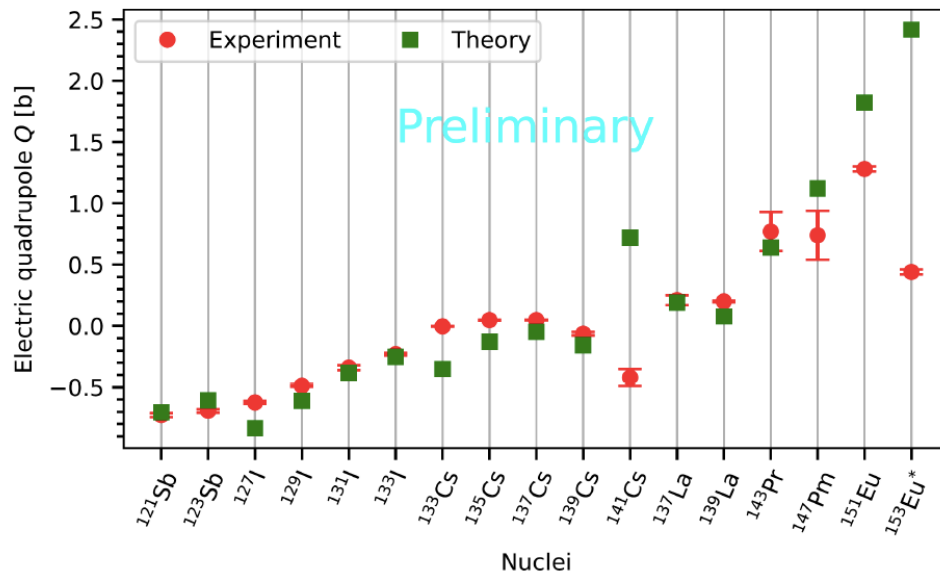


UK Research and Innovation



# Quadrupole moments: theory vs. experiment

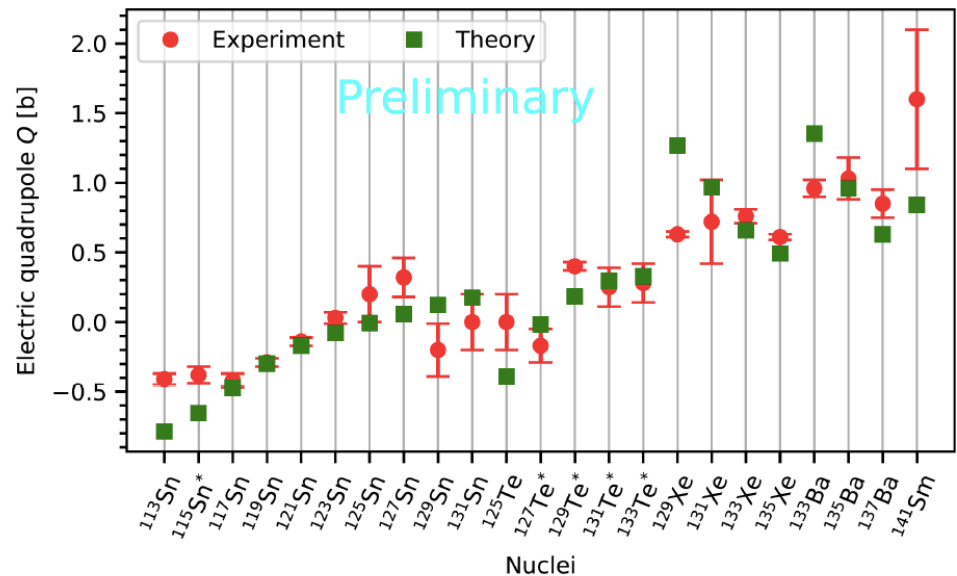
Odd-Z  $\pi 7/2^+$



N. J. Stone, *Table of nuclear magnetic dipole and electric quadrupole moments* (2014), INDC, report INDC(NDS)-0658

N. J. Stone, *Table of nuclear electric quadrupole moments*, ADNDT 111-112, 1 (2016)

Odd-N  $\nu 11/2^-$



Picture: courtesy H. Wibowo

**H. Wibowo et al., to be published**



Jacek Dobaczewski

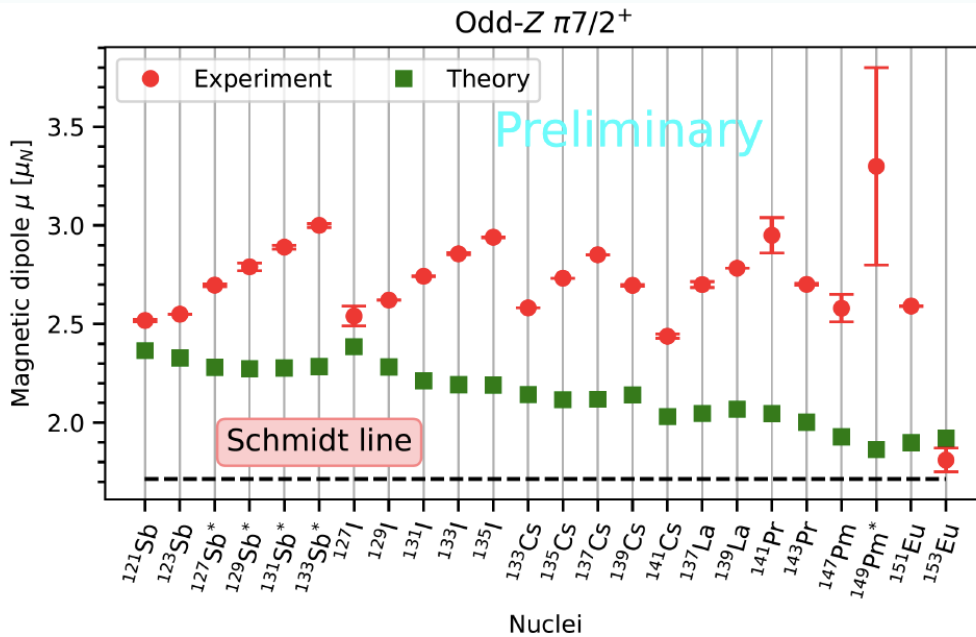
UNIVERSITY of York



UK Research and Innovation

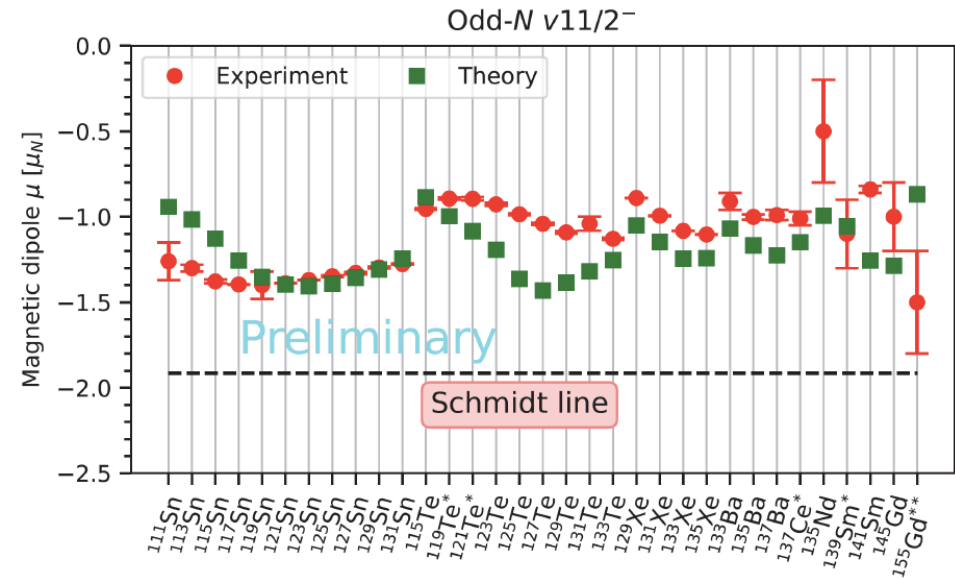


# Magnetic dipole moments: theory vs. experiment



N. J. Stone, *Table of nuclear magnetic dipole and electric quadrupole moments* (2014), INDC, report INDC(NDS)-0658

Schmidt lines represent the value of magnetic dipole moment of an odd-mass nucleus which is completely determined by the  $\ell$  and  $j$  values of the unpaired nucleon (single-particle model).



Picture: courtesy H. Wibowo

H. Wibowo *et al.*, to be published



Jacek Dobaczewski

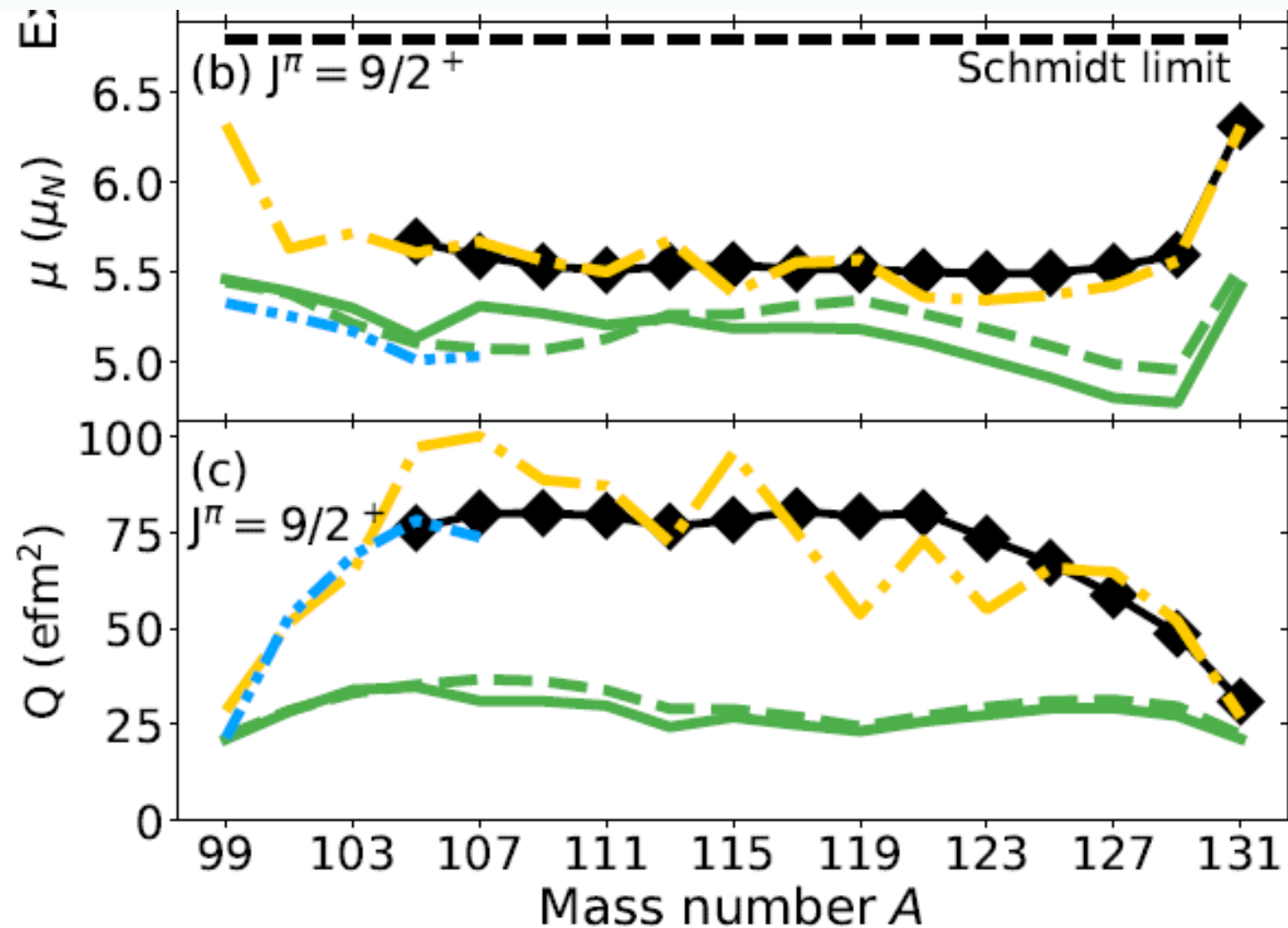
UNIVERSITY of York



UK Research and Innovation



# Moments of the 9/2 states in In



A.R. Vernon *et al.*, Nature 607, 260 (2022)

L. Nies *et al.*, Phys. Rev. Lett. 131, 022502 (2023)



Jacek Dobaczewski

UNIVERSITY of York

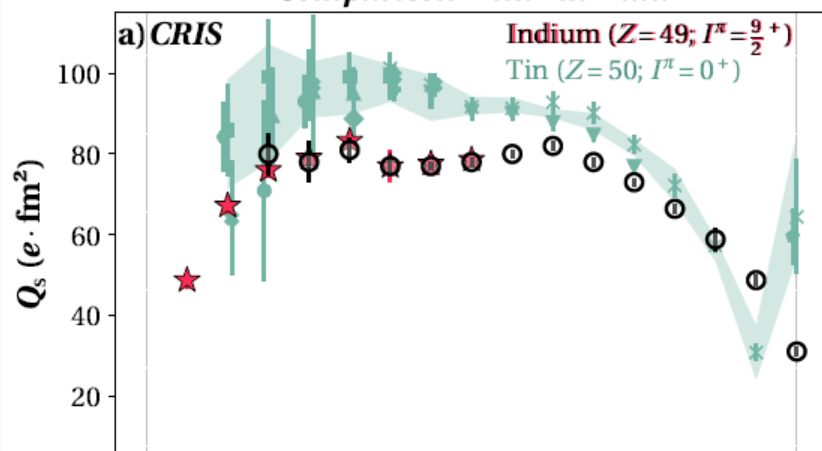


UK Research and Innovation

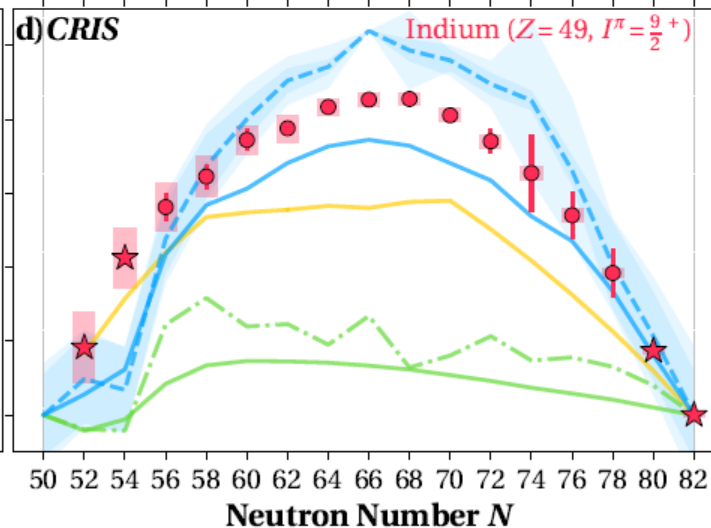
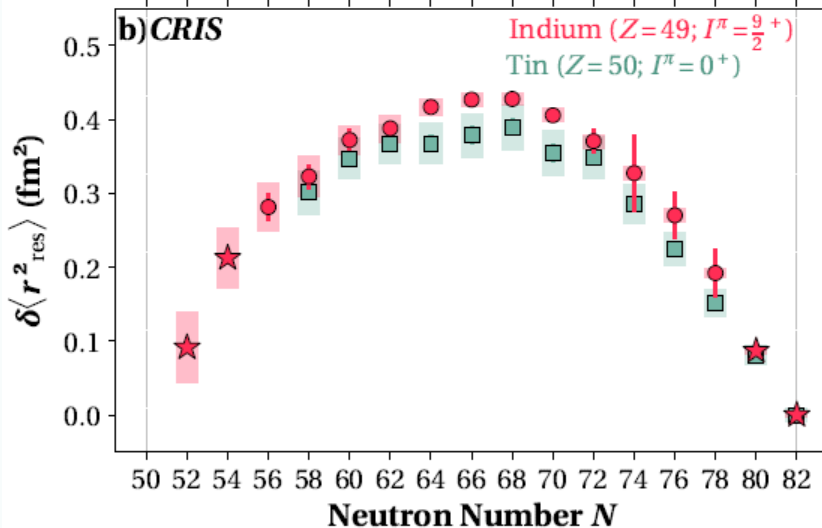
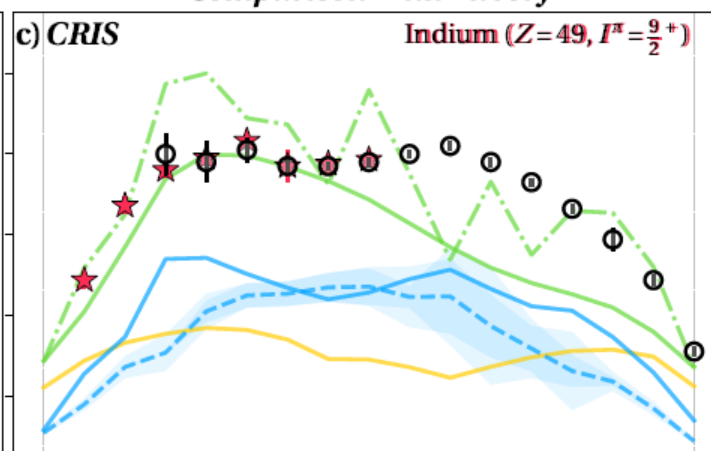


# Quadrupole moments and radii of In and Sn

Comparison With Tin Data



Comparison With Theory



- Data**
- ★ Indium: this work
  - Indium: this work + lit.
  - Indium: laser spec. lit.
  - Tin: laser spec. lit.
  - Tin: NNDC via  $B(E2)$
  - ◆ Tin:  $B(E2)$  from RIKEN
  - ◆ Tin:  $B(E2)$  from GSI
  - ▲ Tin:  $B(E2)$  from ISOLDE
  - Tin:  $B(E2)$  from NSCL
  - ◆ Tin:  $B(E2)$  from TUD
  - ◆ Tin:  $B(E2)$  from ORNL
  - ◆ Tin:  $B(E2)$  from LBNL
  - ◆ Tin:  $B(E2)$  from IUAC
  - ◆ Tin:  $B(E2)$  from Köln
  - ◆ Tin:  $B(E2)$  from AGATA
- Theory (Indium)**
- DFT: Sky(HFB)
  - - DFT: Sky(HF)
  - - DFT: Fy(HFB,  $\Delta r$ )
  - DFT: Fy(HFB, IVP)
  - VS-IMSRG: EM1.8/2.0



J. Karthein *et al.*, arXiv:2310.15093



Jacek Dobaczewski

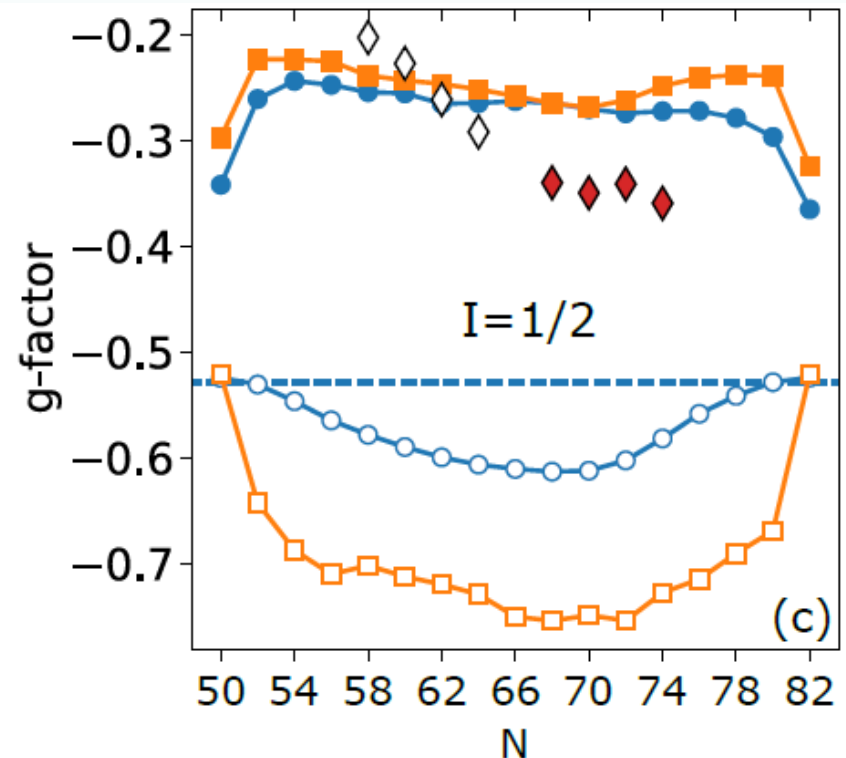
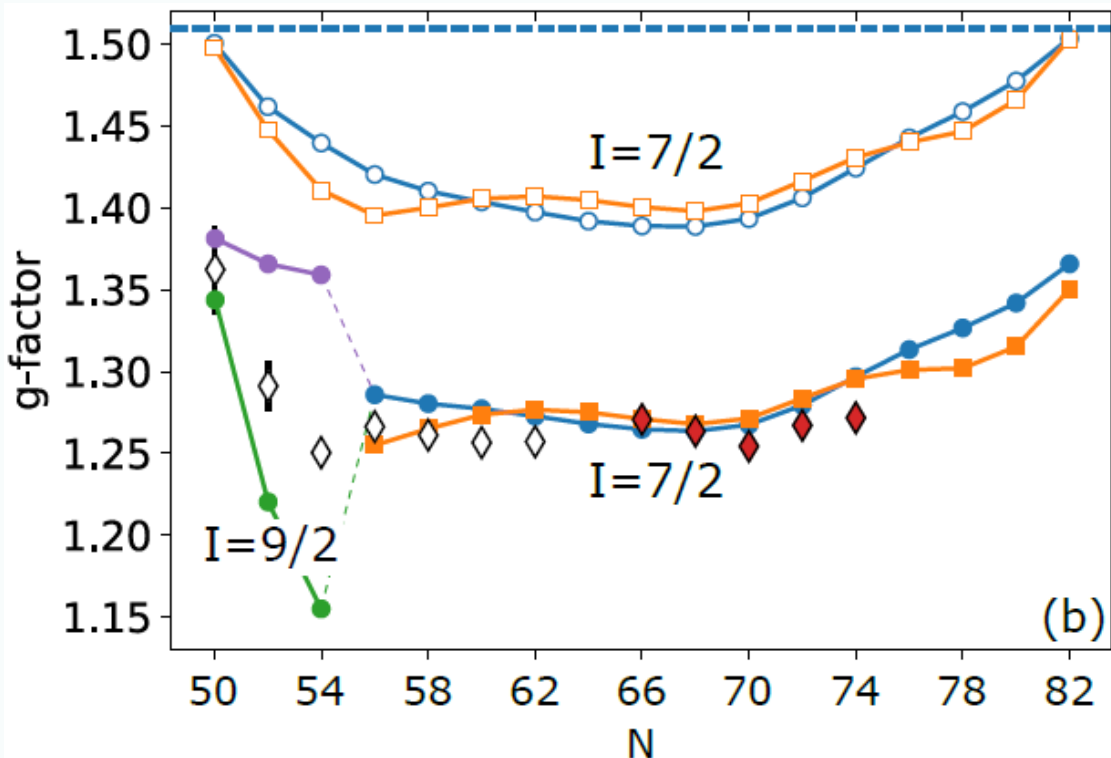
UNIVERSITY of York



UK Research and Innovation



# Moments of the 1/2, 7/2 & 9/2 states in Ag



Experiment ◆ This work  
◆ Literature

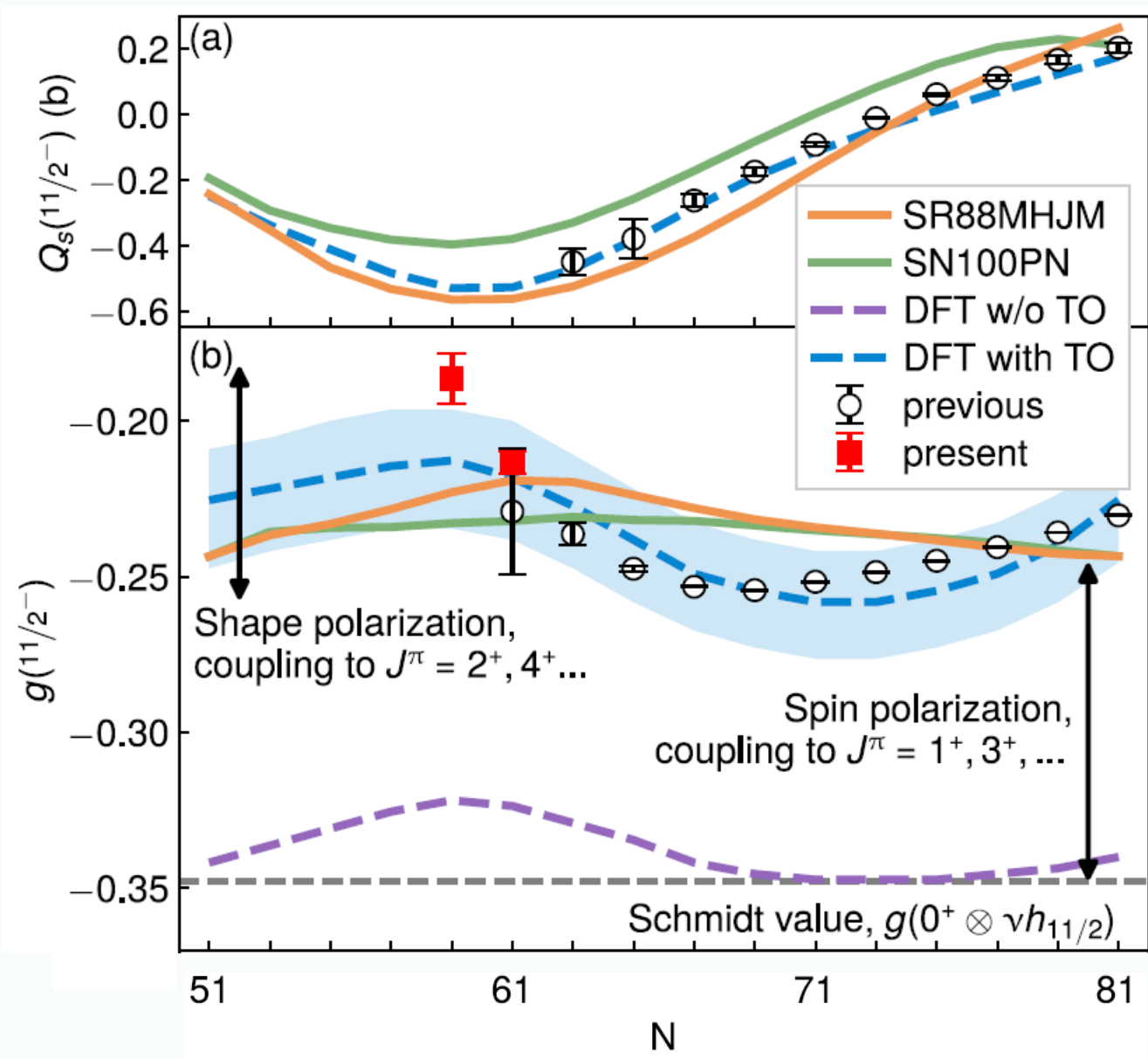
UNEDF1 □  $g'_0 = 0$       UNEDF1<sub>so</sub> ○  $g'_0 = 0$       ●  $g'_0 = 1.7$   $I = 9/2$  (7/2)  
■  $g'_0 = 1.7$       ●  $g'_0 = 1.7$       ●  $g'_0 = 1.7$   $I = 9/2$

**R. P. de Groote *et al.*, Phys. Lett. B 848 (2024) 138352**





# Moments of the $\nu h_{11/2}$ isomers in Sn

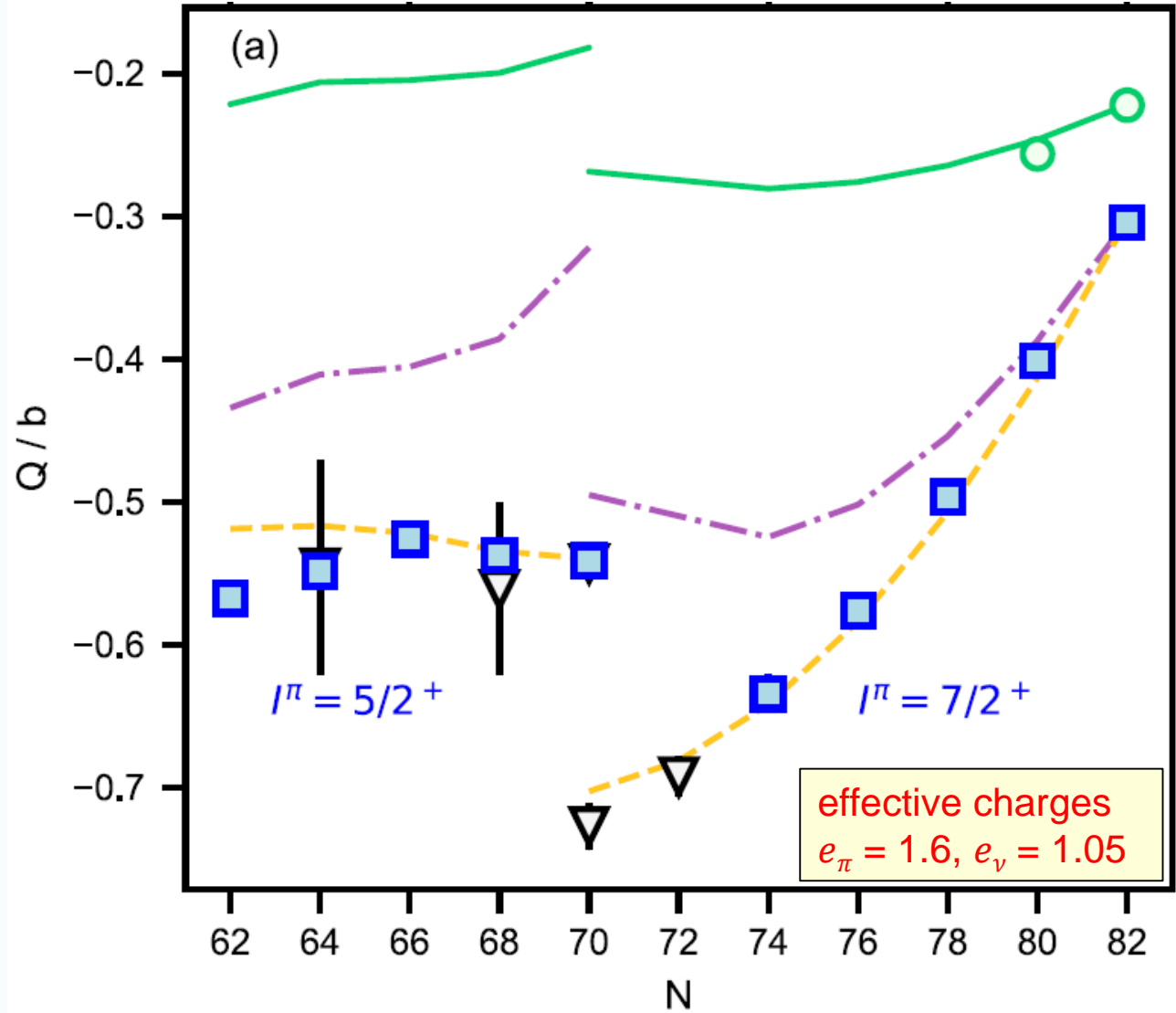
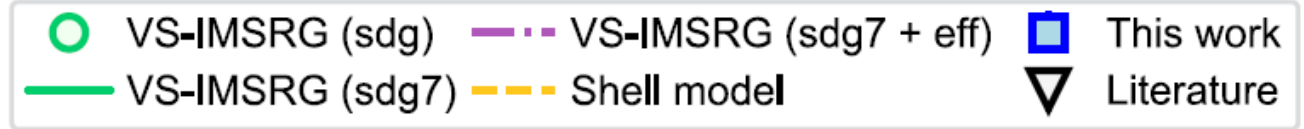


$g = \mu/I$

T.J. Gray et al., Phys. Lett. B 847 (2023) 138268



# Quadrupole moments in Sb



S. Lechner *et al.*, Phys. Lett. B 847 (2023) 138278



Jacek Dobaczewski

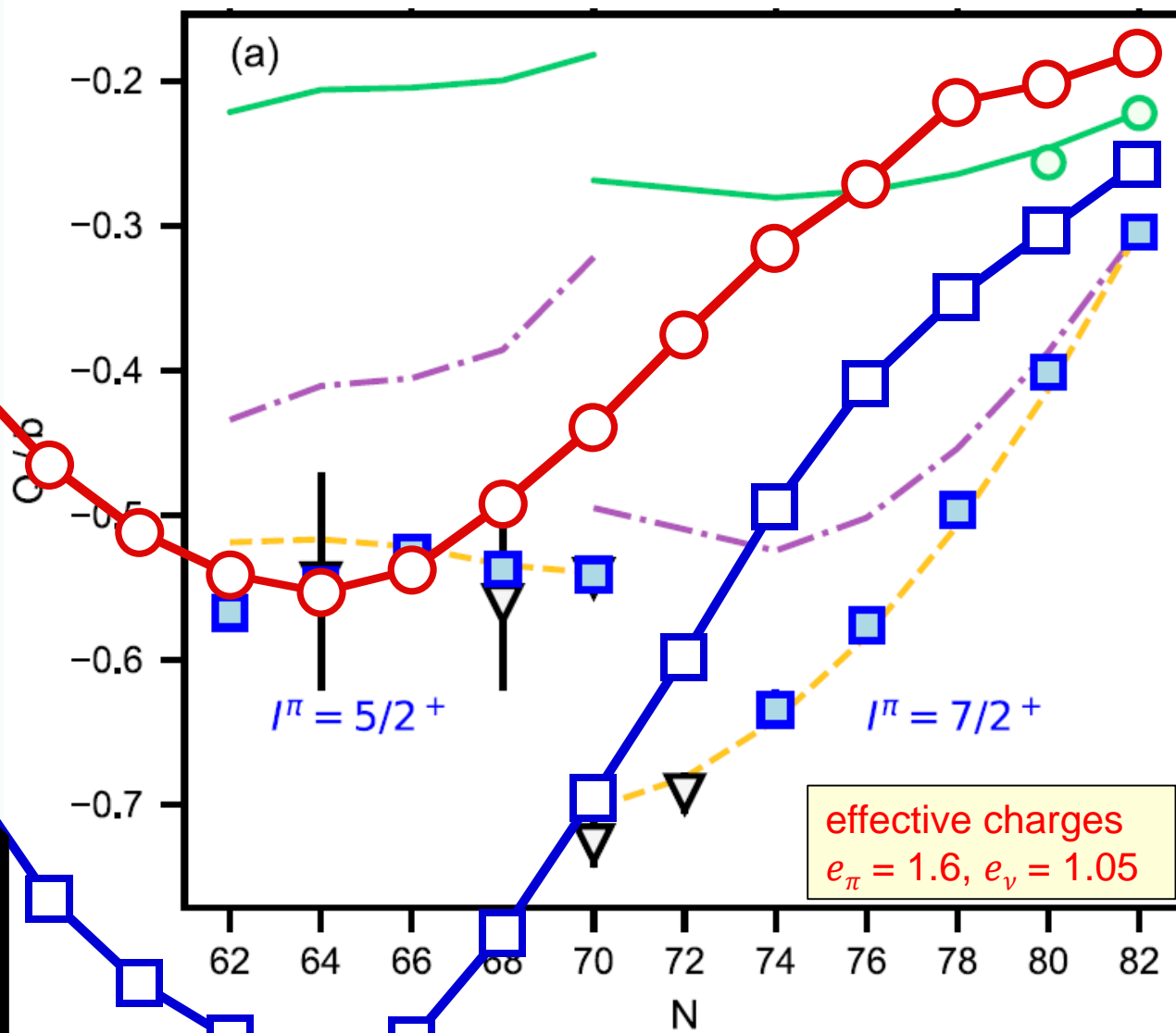
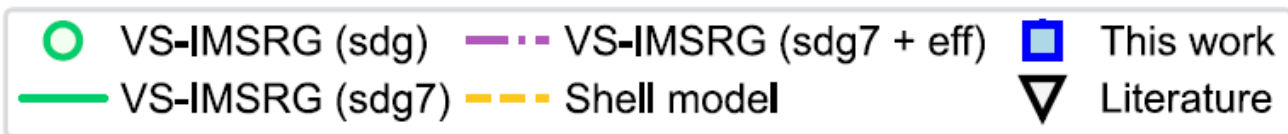
UNIVERSITY of York



UK Research and Innovation



# Quadrupole moments in Sb



no effective charges !!!

—□— DFT  $g_{7/2}$   
—○— DFT  $d_{5/2}$

effective charges  
 $e_\pi = 1.6, e_\nu = 1.05$

S. Lechner *et al.*, Phys. Lett. B 847 (2023) 138278



Jacek Dobaczewski

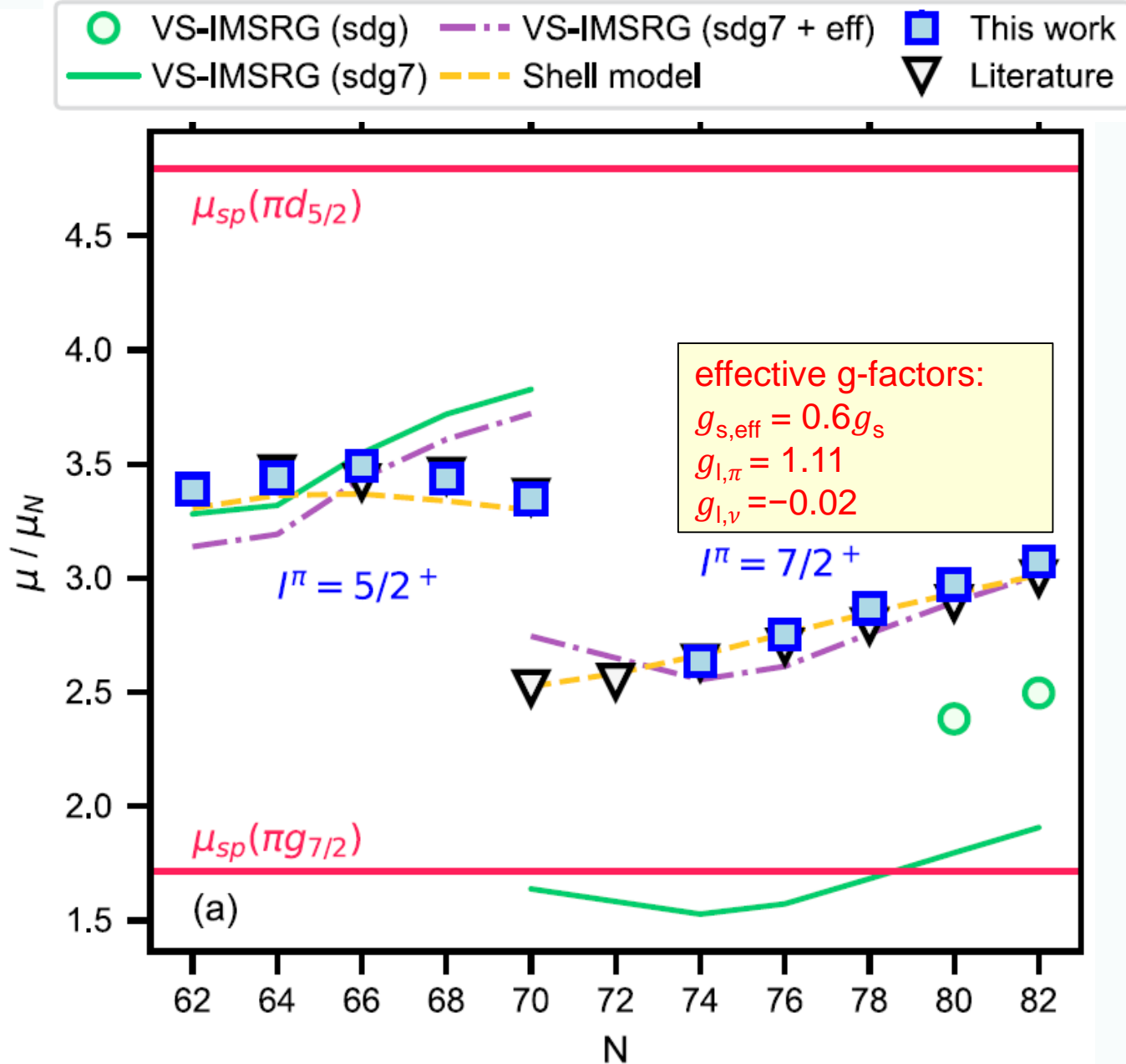
UNIVERSITY of York



UK Research and Innovation



# Magnetic dipole moments in Sb



S. Lechner et al., Phys. Lett. B 847 (2023) 138278



Jacek Dobaczewski

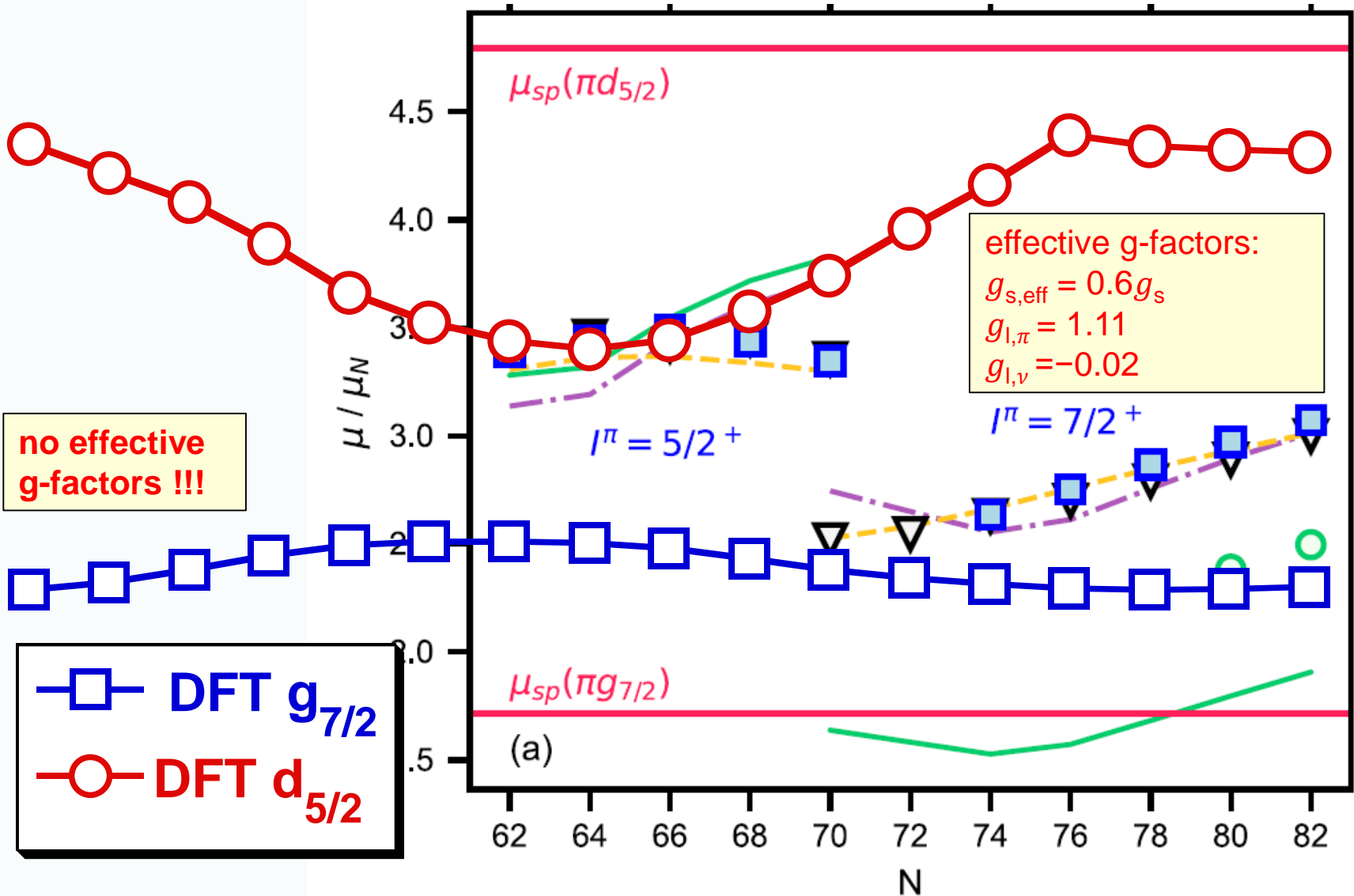
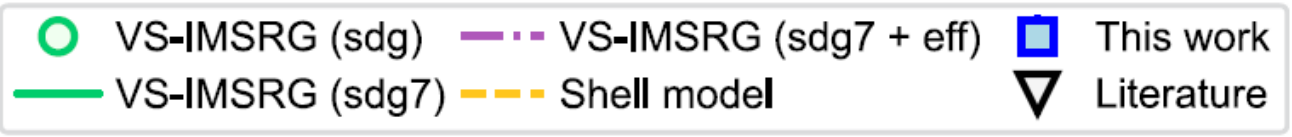
UNIVERSITY of York



UK Research and Innovation



# Magnetic dipole moments in Sb



S. Lechner et al., Phys. Lett. B 847 (2023) 138278



## What's next to consider

**Segré chart of electromagnetic moments**

**Electromagnetic moments of odd-odd nuclei**

**More advanced functionals**

**Octupole deformation**

**Triaxiality**

**Configuration interaction**

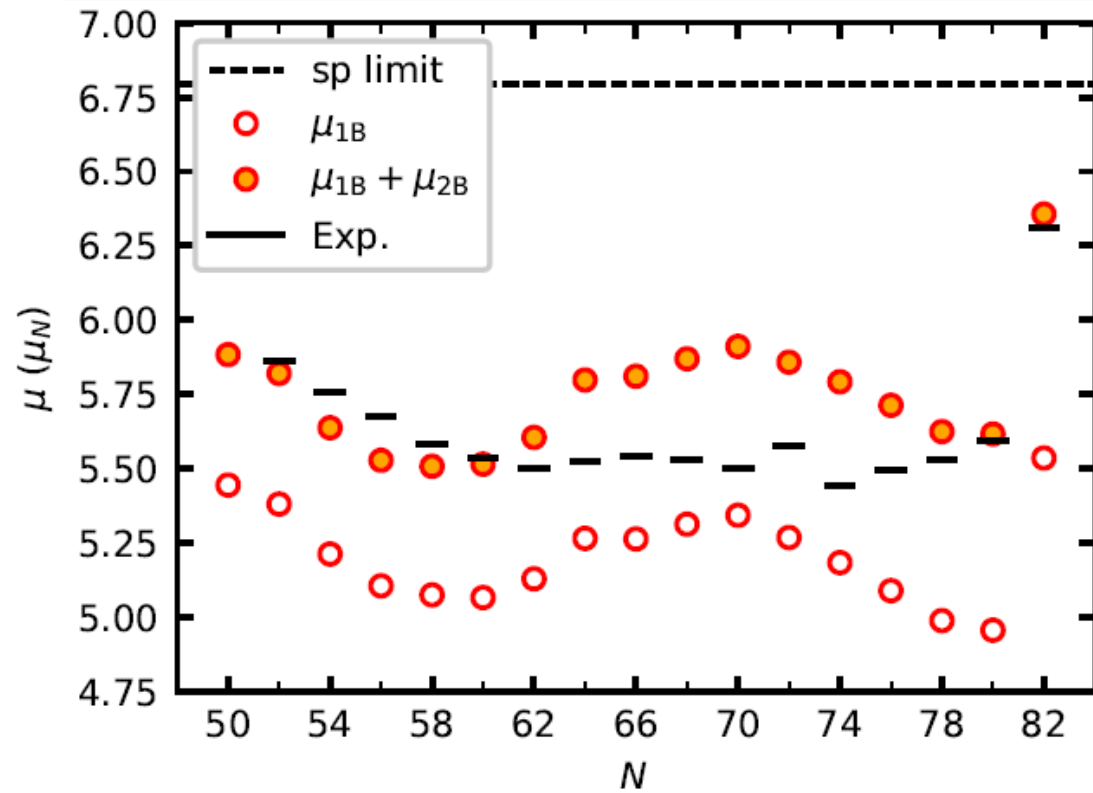
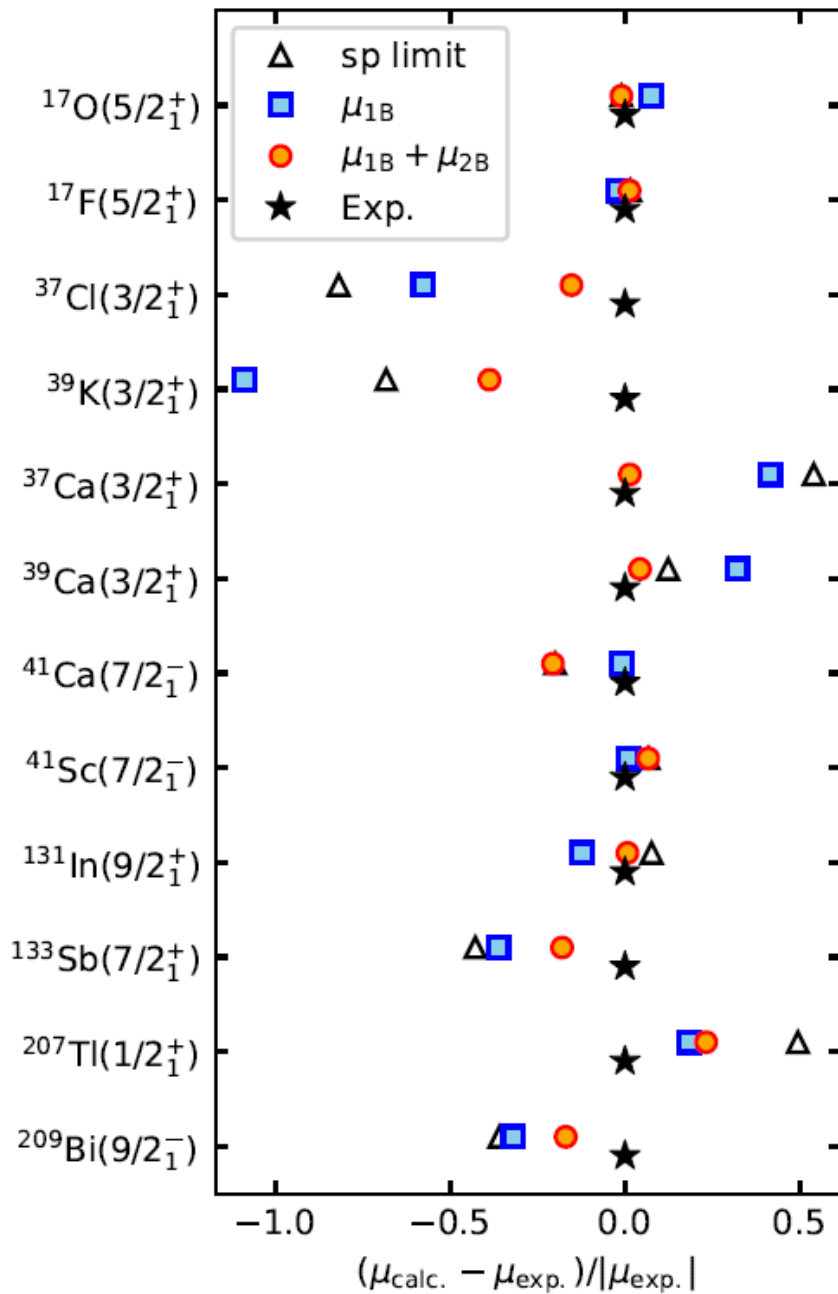
**K-mixing**

**Quadrupole/octupole collectivity**

**Two-body meson-exchange currents**



# Two-body-current corrections to magnetic moments



T. Miyagi *et al.*, arXiv:2311.14383



Jacek Dobaczewski

UNIVERSITY of York



UK Research and Innovation



# Thank you



Jacek Dobaczewski

UNIVERSITY *of York*



UK Research  
and Innovation

