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in collaboration with
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and

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Workshop on SM and Beyond 2024 / 3rd Gordon Godfrey

Exploring Light Dark Matter Boosted by Supernova Neutrinos in the Past and Present Universe

Based on

- Phys. Rev. Lett.* **133**, 111004 (2024)
Phys. Rev. D **108**, 083013 (2023)
Phys. Rev. Lett. **130**, 111002 (2023)



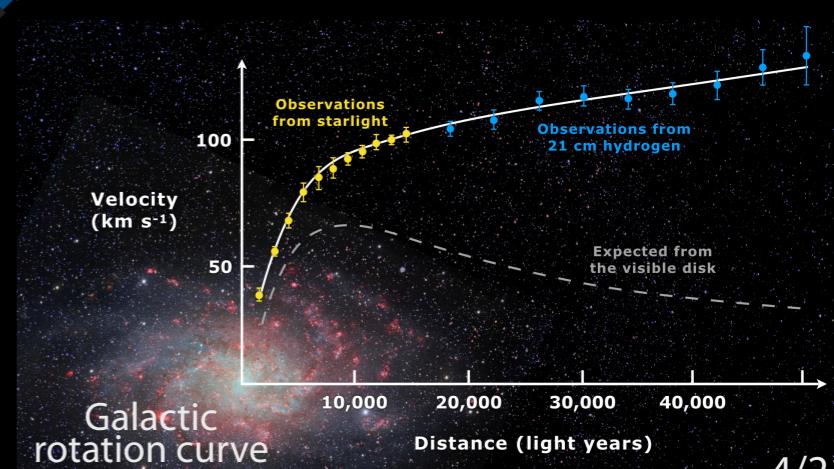
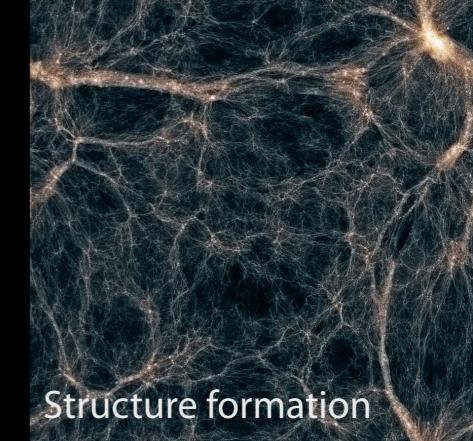
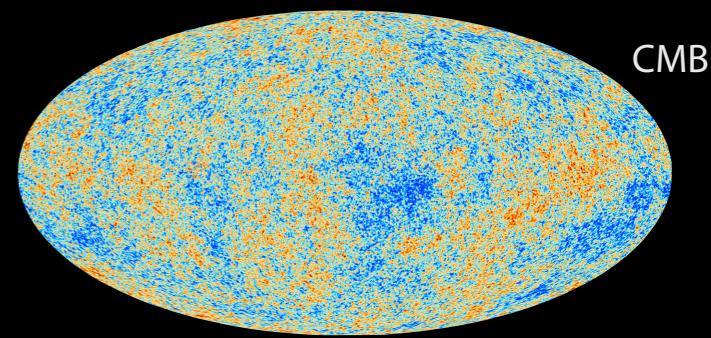
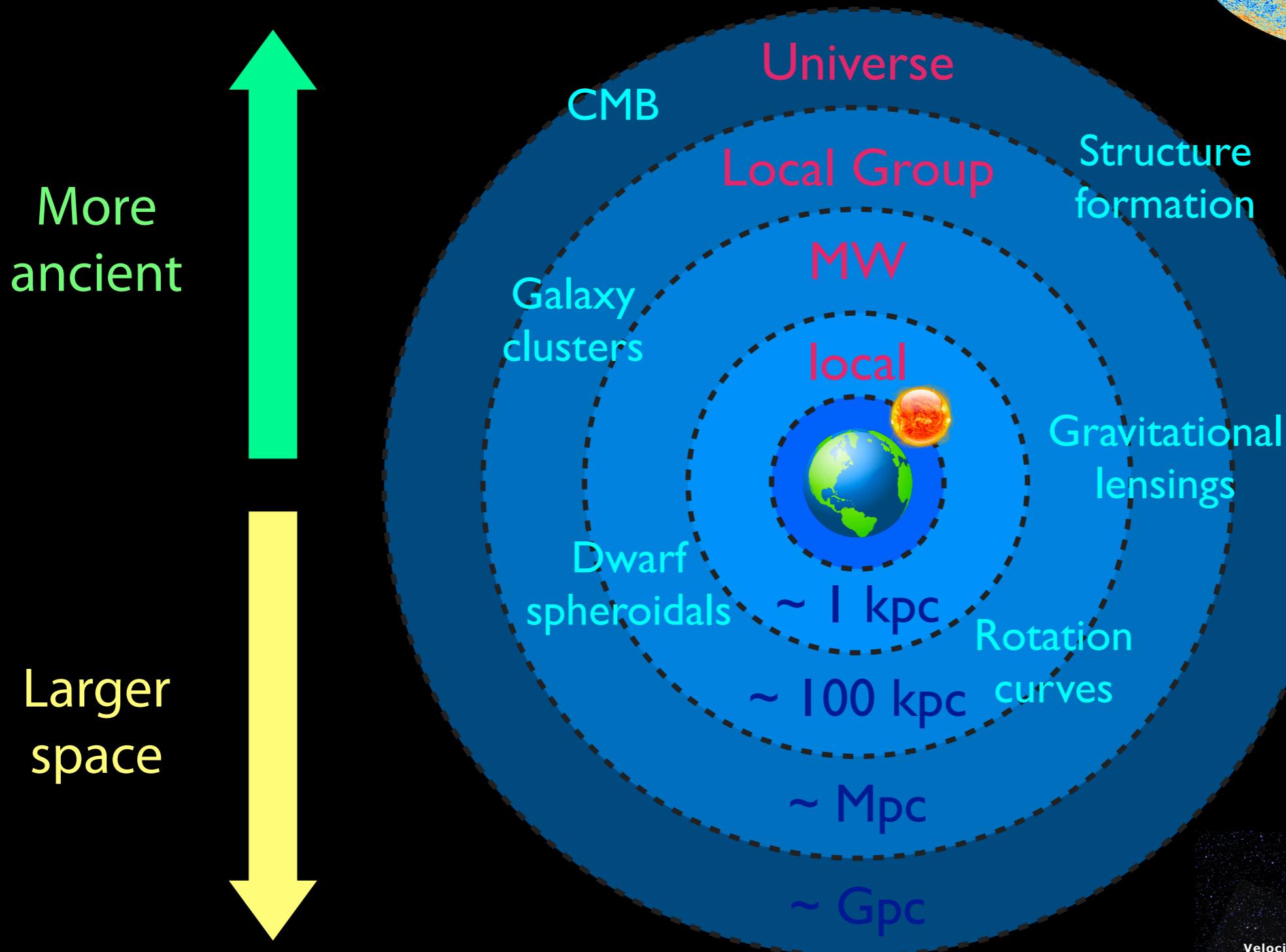
Outline

- Introduction to dark matter (DM)
- Supernova-neutrino-boosted DM (SN ν BDM) and time-of-flight (ToF) for direct mass differentiation
- Diffuse SN ν BDM flux from the high redshift to the present
- Constraints and sensitivities on DM- ν/e^- cross sections
- Summary

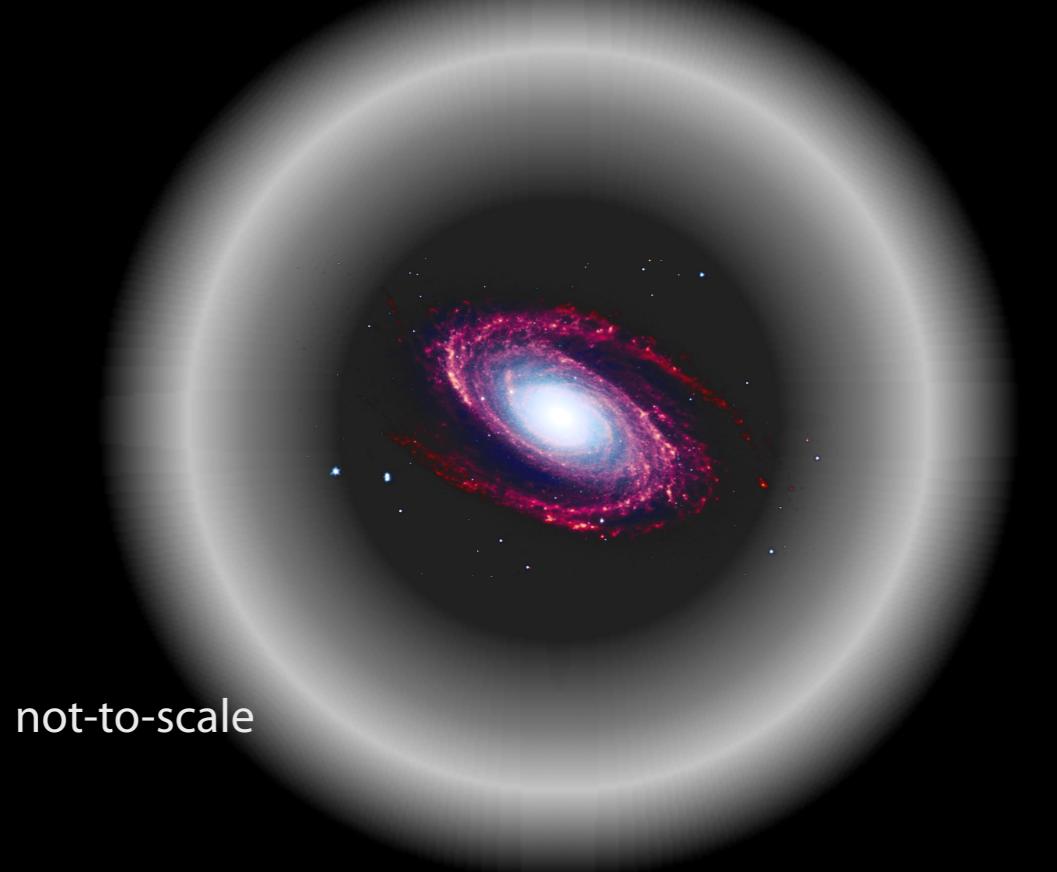


Introduction

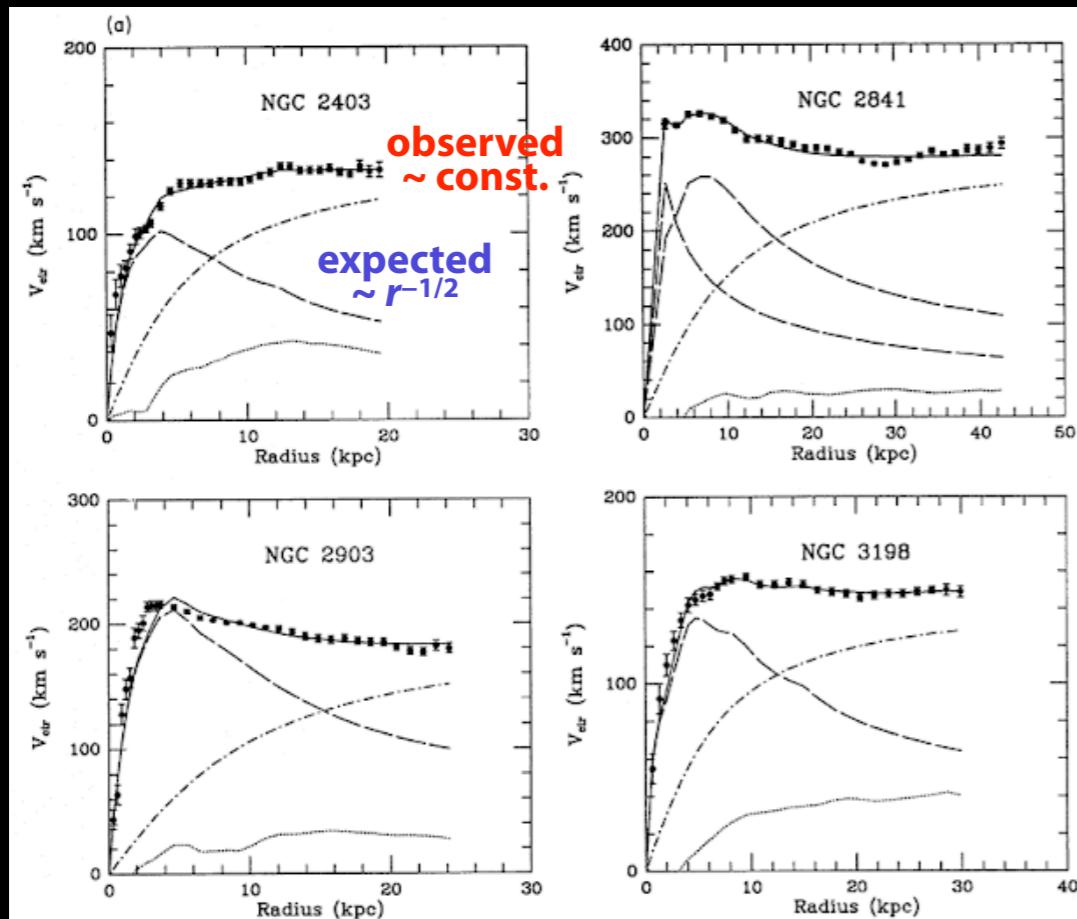
Dark matter is *ubiquitous* in the Universe!



DM halo



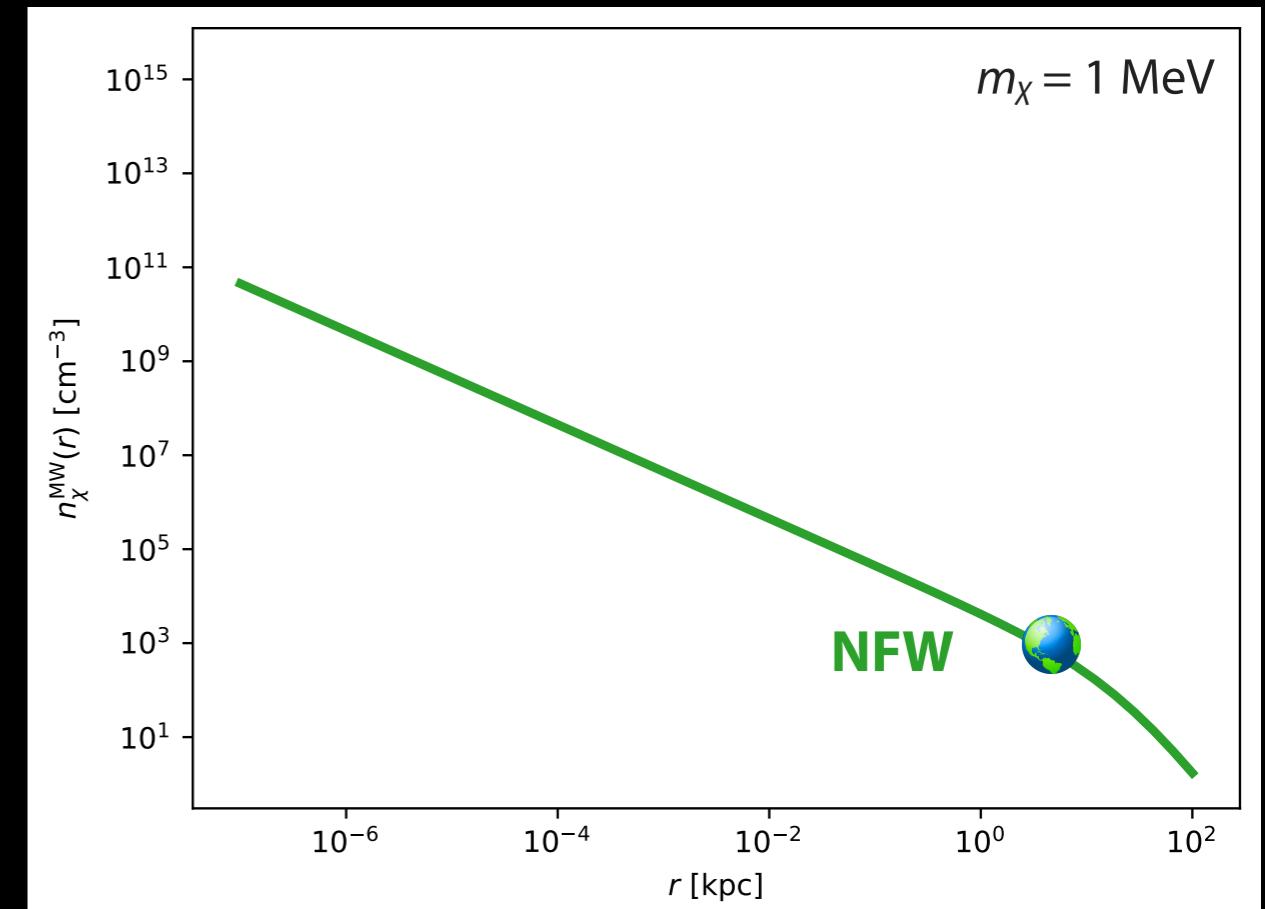
Velocity



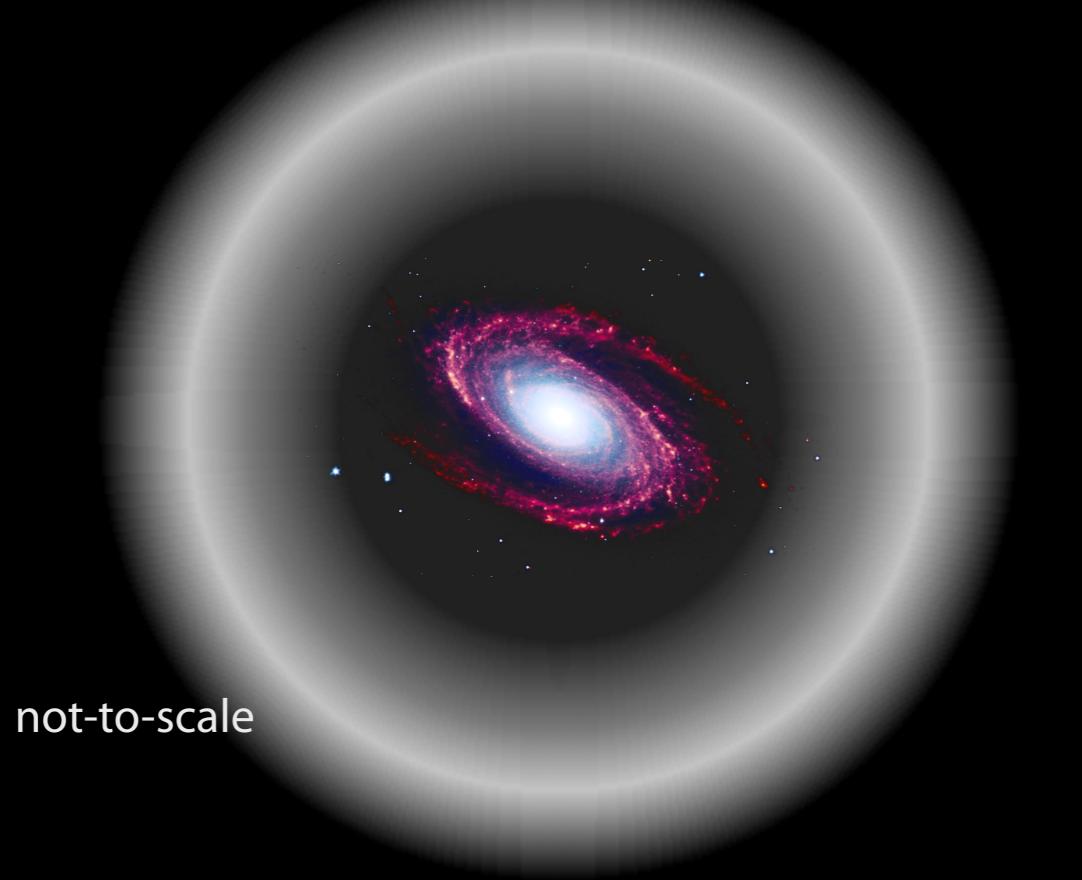
Galactic rotation curves

- Galaxies are generally enclosed by a large DM halo with radial density profile
Navarro+ 1996
Bertone+ 2004
- Our MW is assumed following Navarro-Frenk-White (NFW) profile: $\rho_s = 184 \text{ MeV cm}^{-3}$, $r_s = 24.4 \text{ kpc}$ and $n = 2$

$$\rho_\chi(r) = \frac{\rho_s}{r_s} \left(1 + \frac{r}{r_s}\right)^n$$



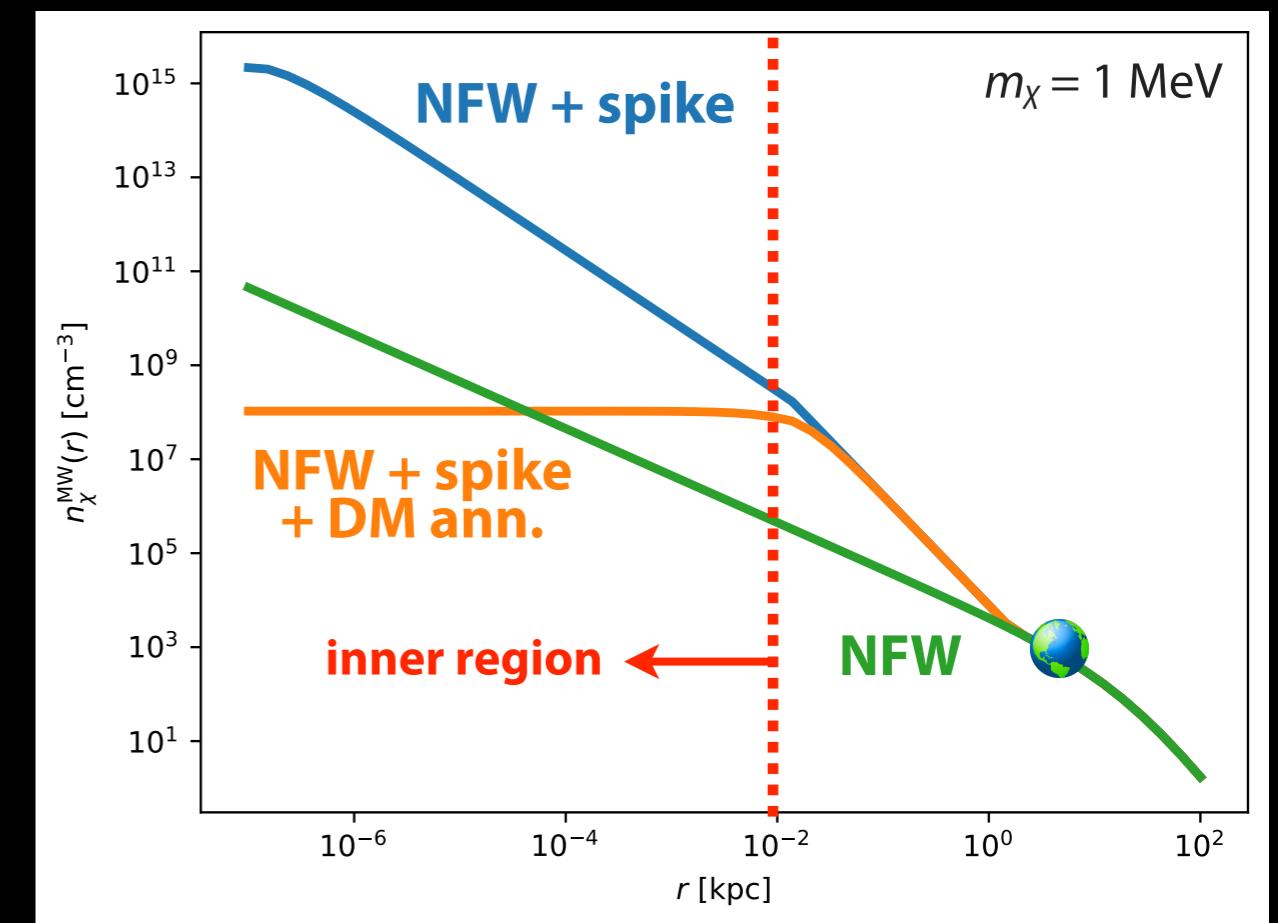
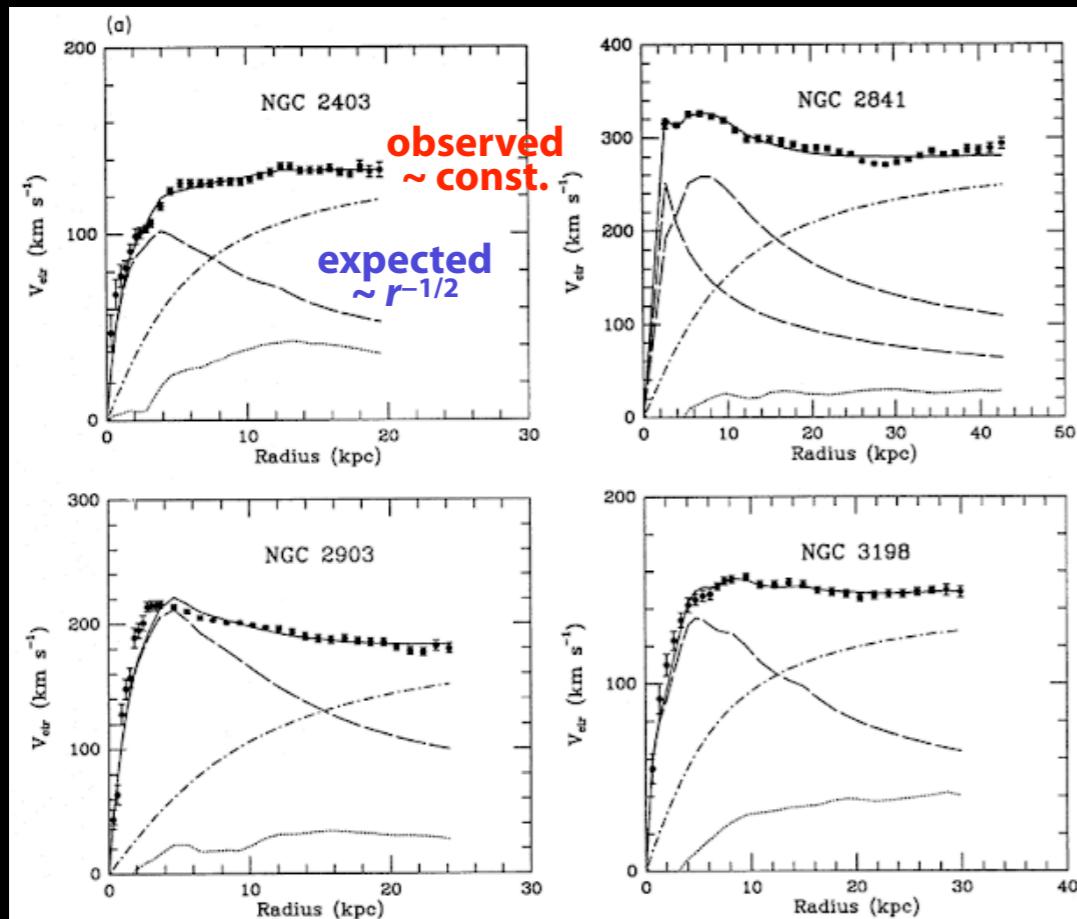
DM halo



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 - More sharp density spike could arise due to supermassive black hole in the galactic center

Gondolo+ 1999
Ullio+ 2001
Gnedin+2004
Cline+ 2023

Velocity

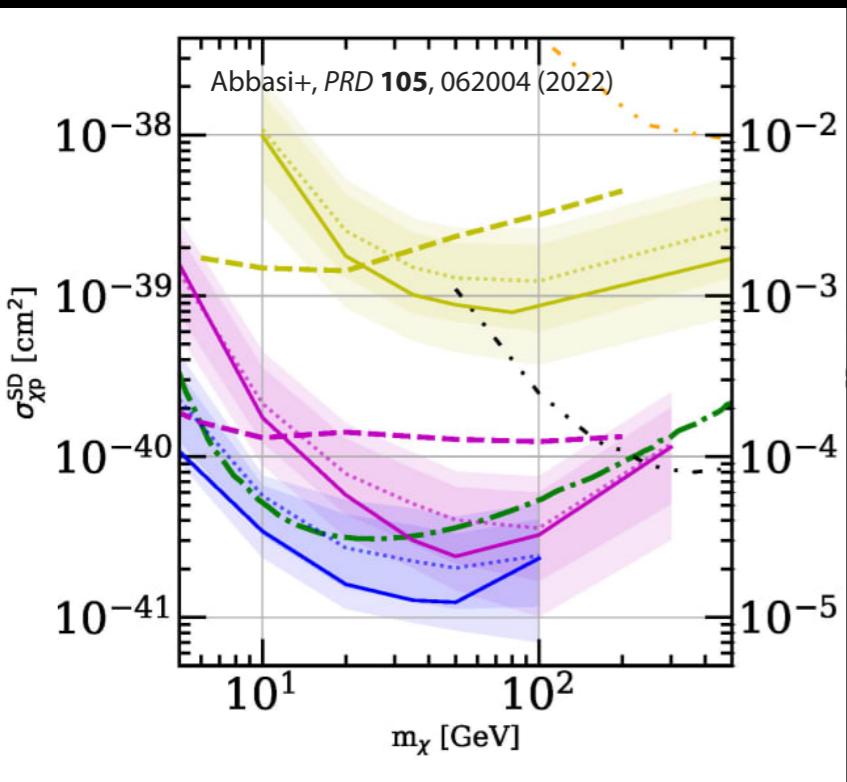


Current constraints

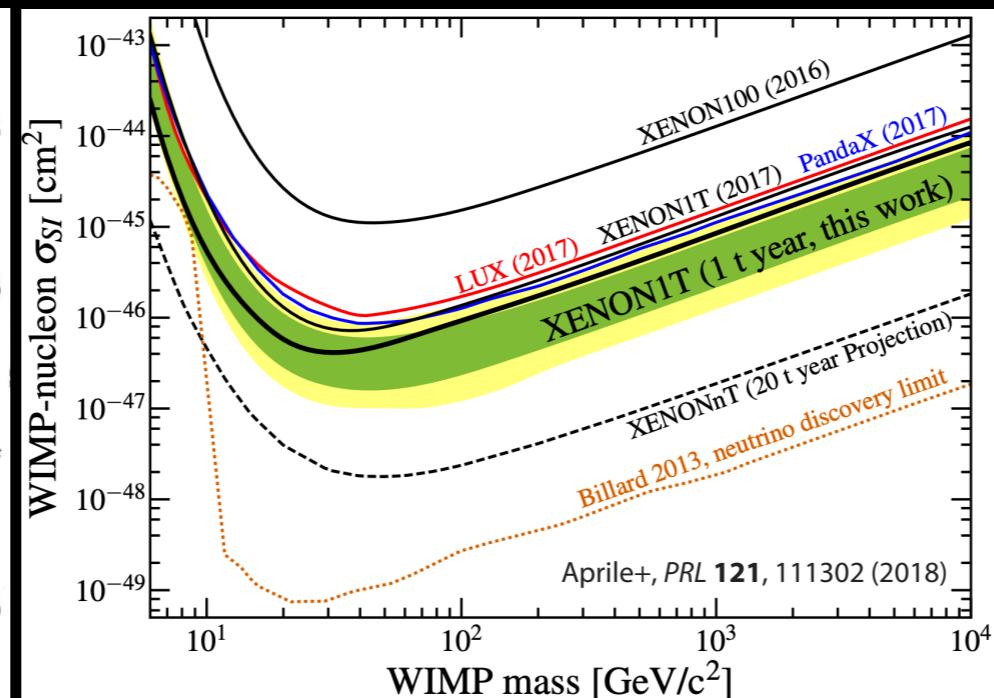
See: Jungman+, *PR* **267**, 195 (1996)
 Bertone+, *PR* **405**, 279 (2005)
 Battaglieri+, 1707.04591
 Knapen+, *PRD* **96**, 115021 (2017)
 Lin (TASI2018), 1904.07915 (2019)

Essig+, 2203.08297
 Billard+, *RPP* **85**, 056201 (2022)
 Cooley+, 2209.07426
 ... for comprehensive reviews

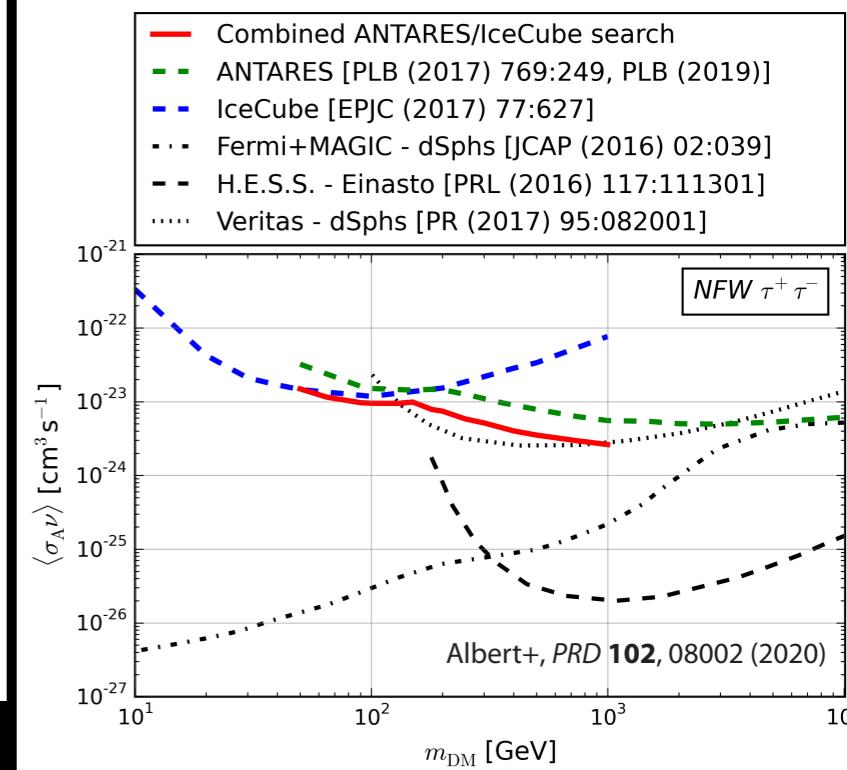
Direct: Spin-dependent $\sigma_{\chi n}$



Direct: Spin-independent $\sigma_{\chi n}$



Indirect: Annihilation cross section $\langle \sigma v \rangle$



- The most stringent constraints happen around

$$\sigma_{\chi p}^{\text{SD}} \sim 10^{-41} \text{ cm}^2$$

$$m_\chi \sim 30 \text{ GeV}$$

$$\sigma_{\chi p}^{\text{SI}} \sim 10^{-47} \text{ cm}^2$$

$$m_\chi \sim 30 \text{ GeV}$$

$$\langle \sigma v \rangle \sim 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

$$m_\chi \sim 10 \text{ GeV}$$

- But **none** of these can directly measure the **cross section** and **mass** concurrently

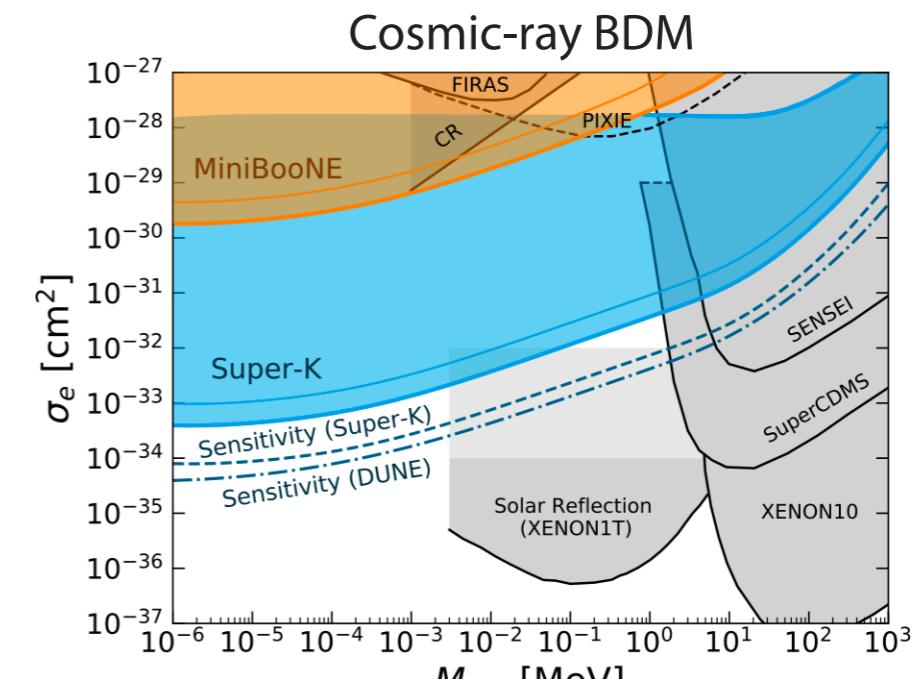
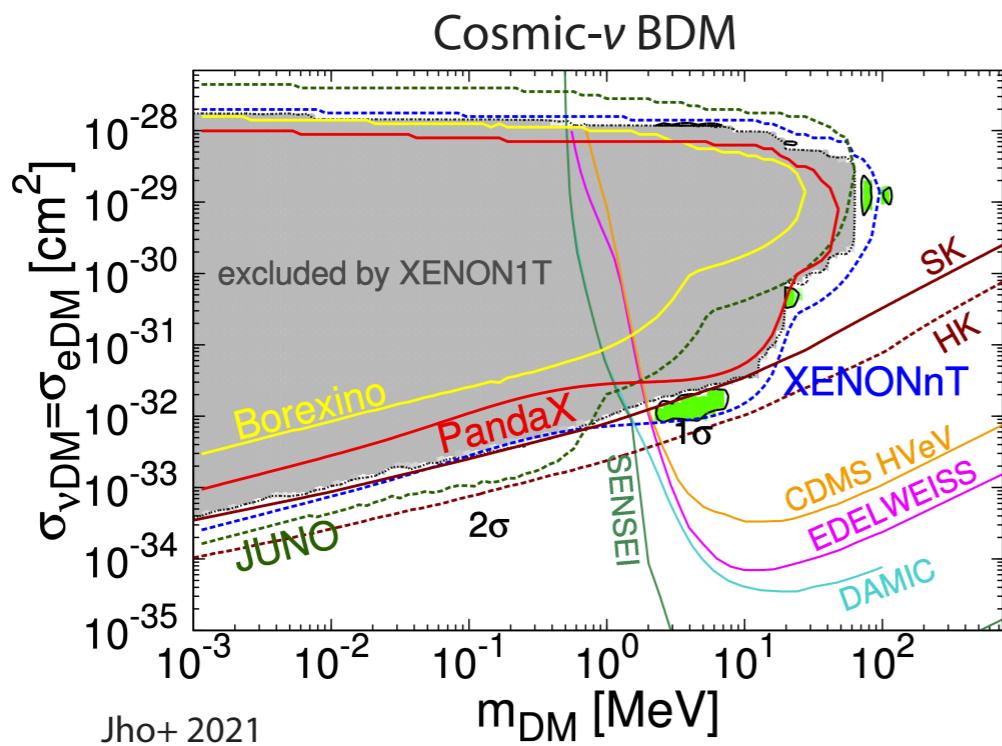


Origin of SNv BDM and direct m_χ differentiation

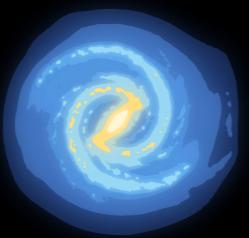
Origin of boosted DM



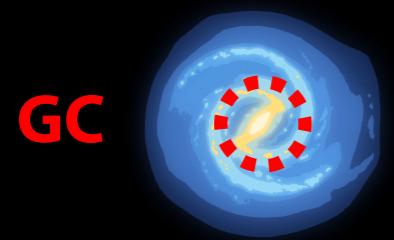
- DM in the halo can be boosted by high-energy cosmic particles, e.g. ν, e^-, p
- Boosted DM carries energy large enough to surpass the detection threshold, e.g. Super-K, DUNE



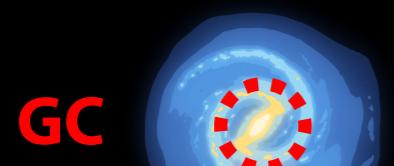
Milky Way



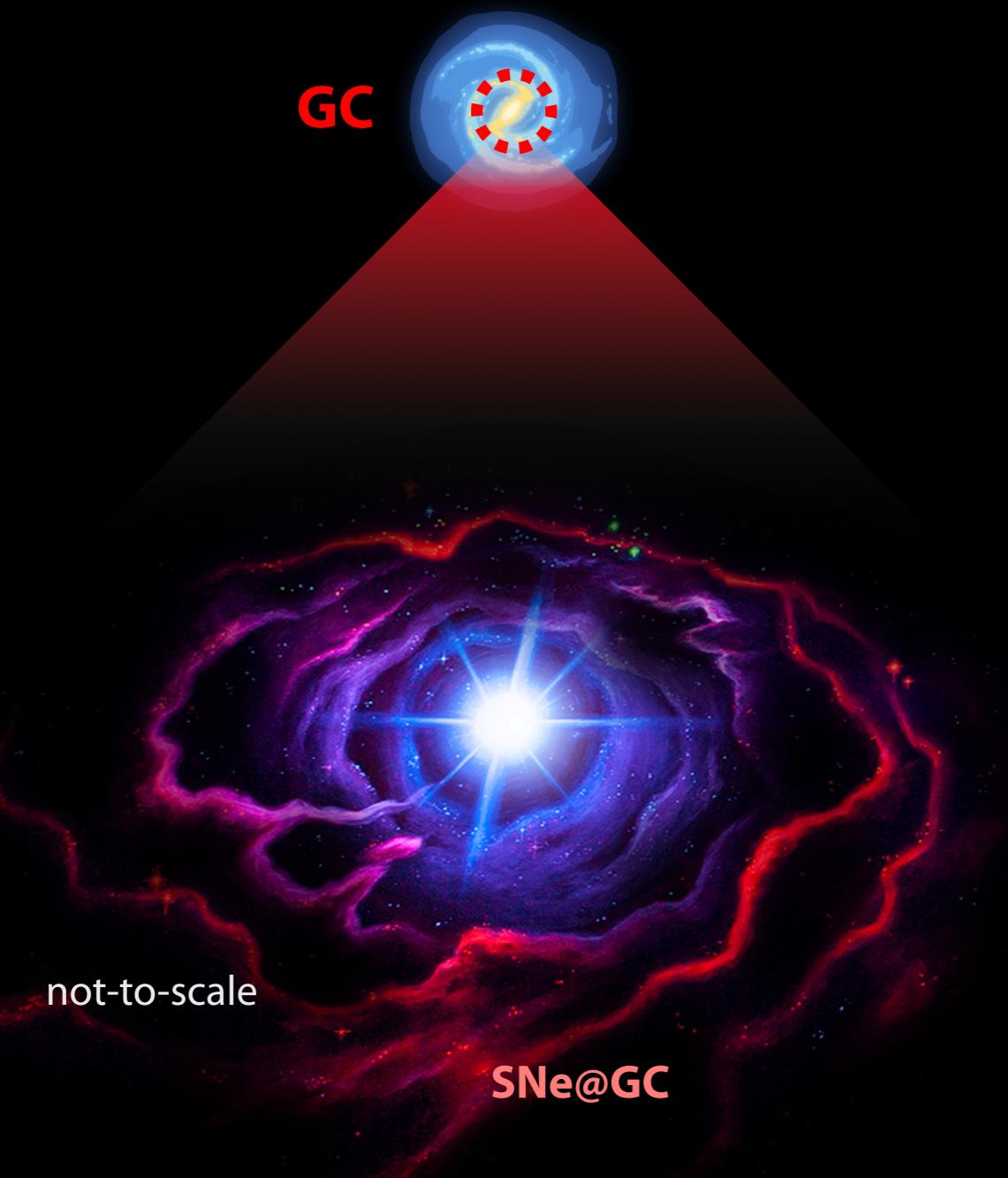
Milky Way



Milky Way



Milky Way



Duration: ~ 10 s

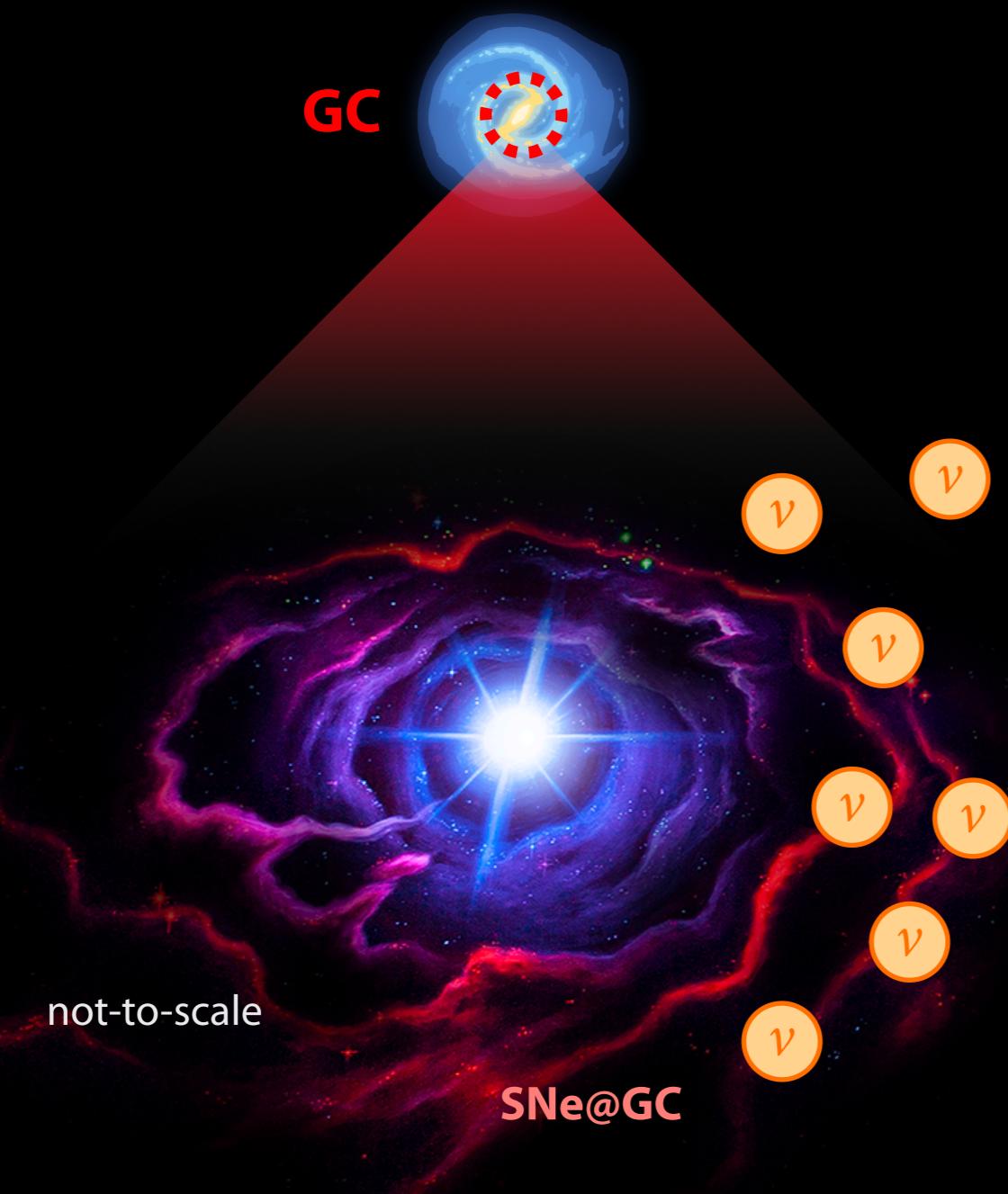
$$N_\nu \approx 10^{58}$$

$$\bar{E}_\nu \approx 10 - 15 \text{ MeV}$$

$$\frac{d\phi_\nu}{dE_\nu} = \sum_i \frac{L_\nu}{4\pi r^2 \langle E_{\nu_i} \rangle} E_\nu^2 f_{\nu_i}(E_\nu)$$

Duan+ 2006

Milky Way



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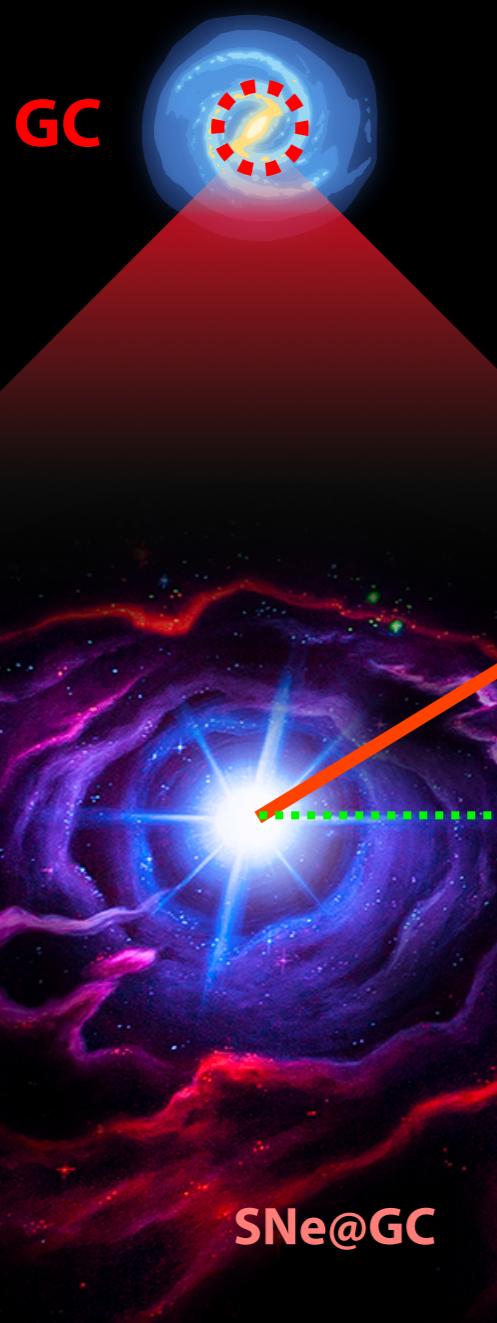
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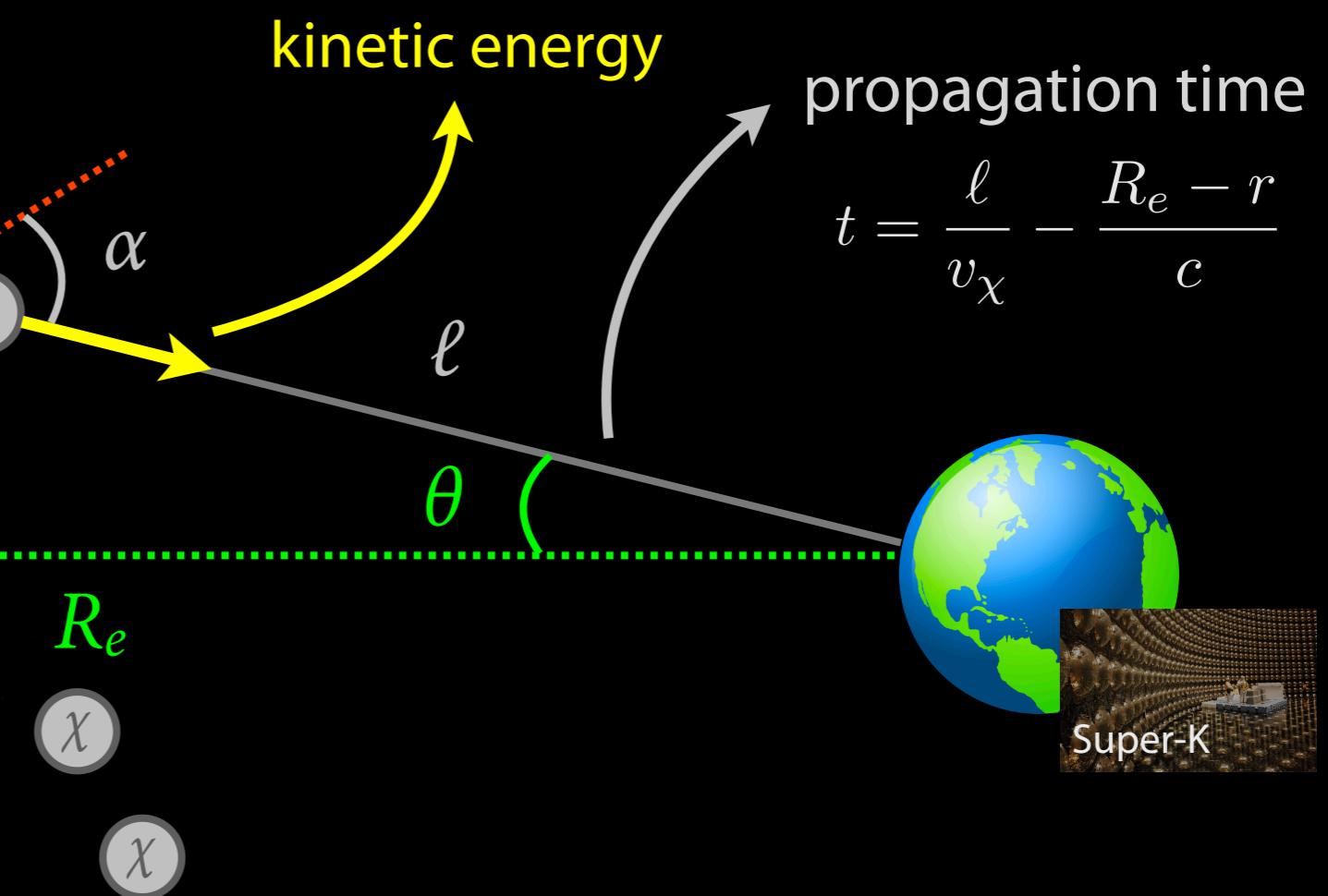
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Milky Way



$$T_\chi = \frac{E_\nu^2}{E_\nu + m_\chi/2} \left(\frac{1 + \cos \theta_c}{2} \right)$$



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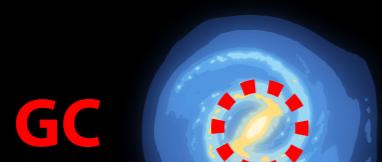
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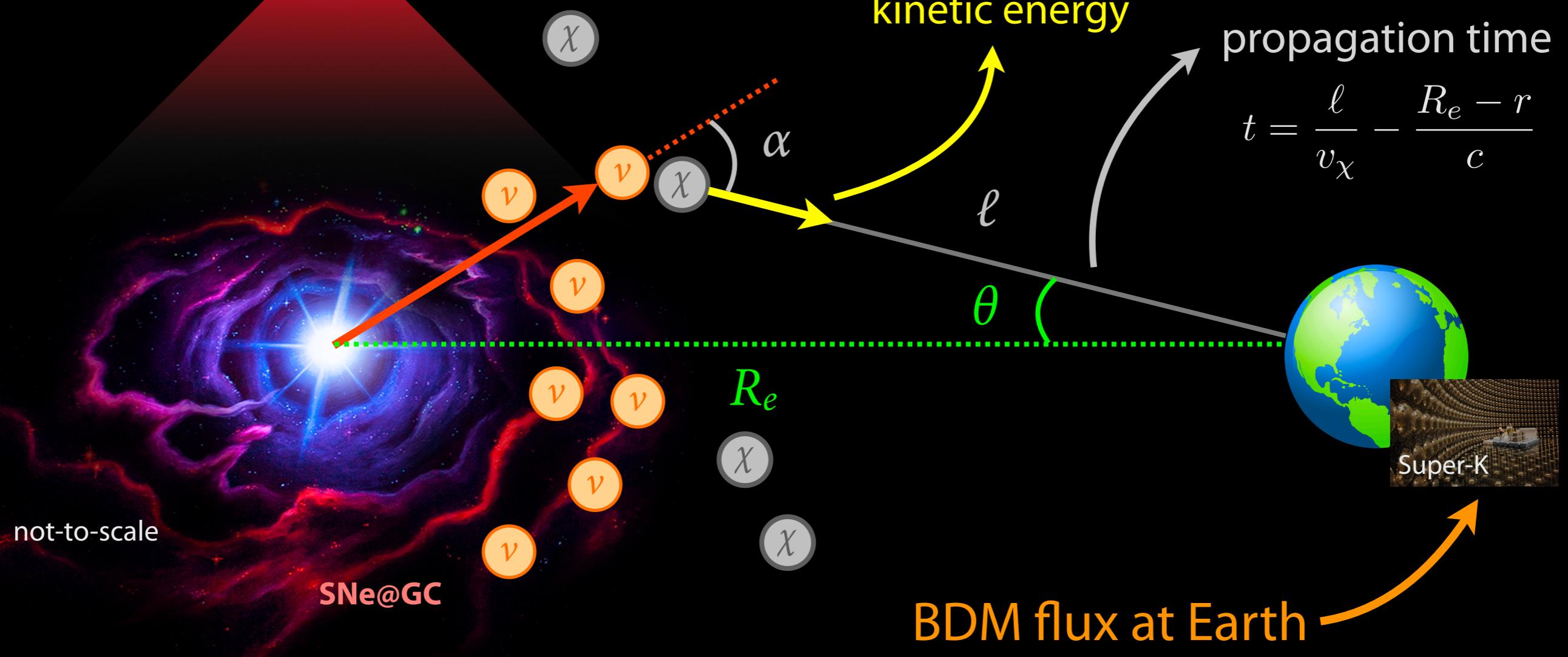
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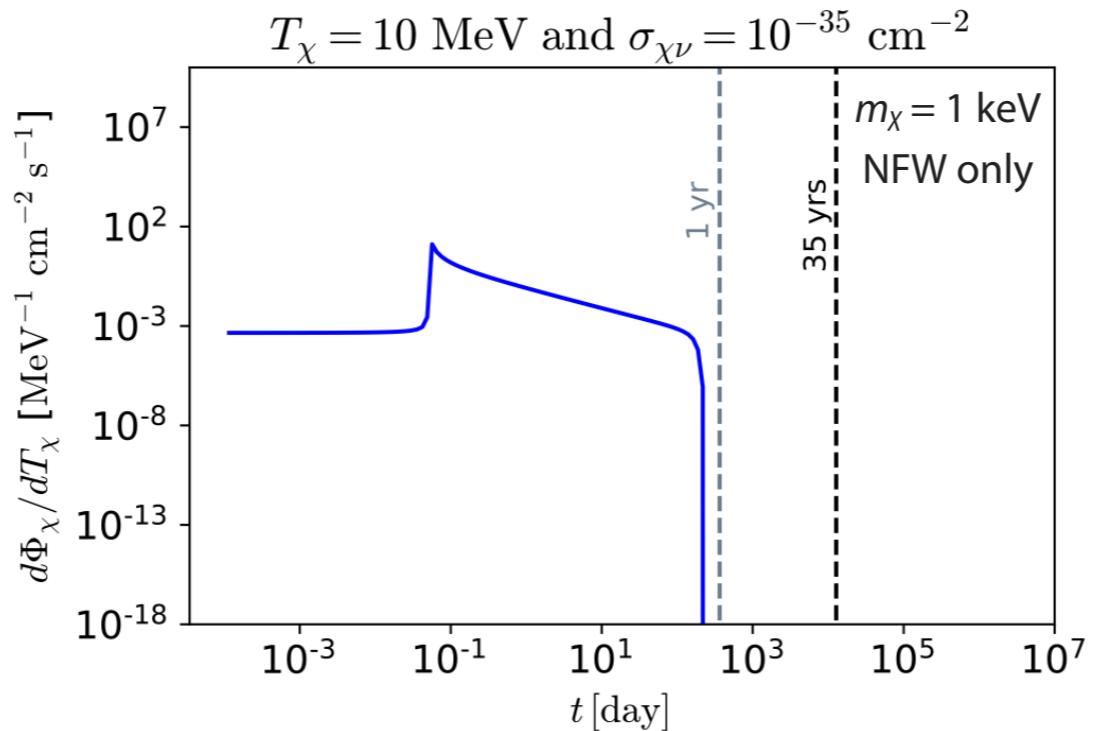
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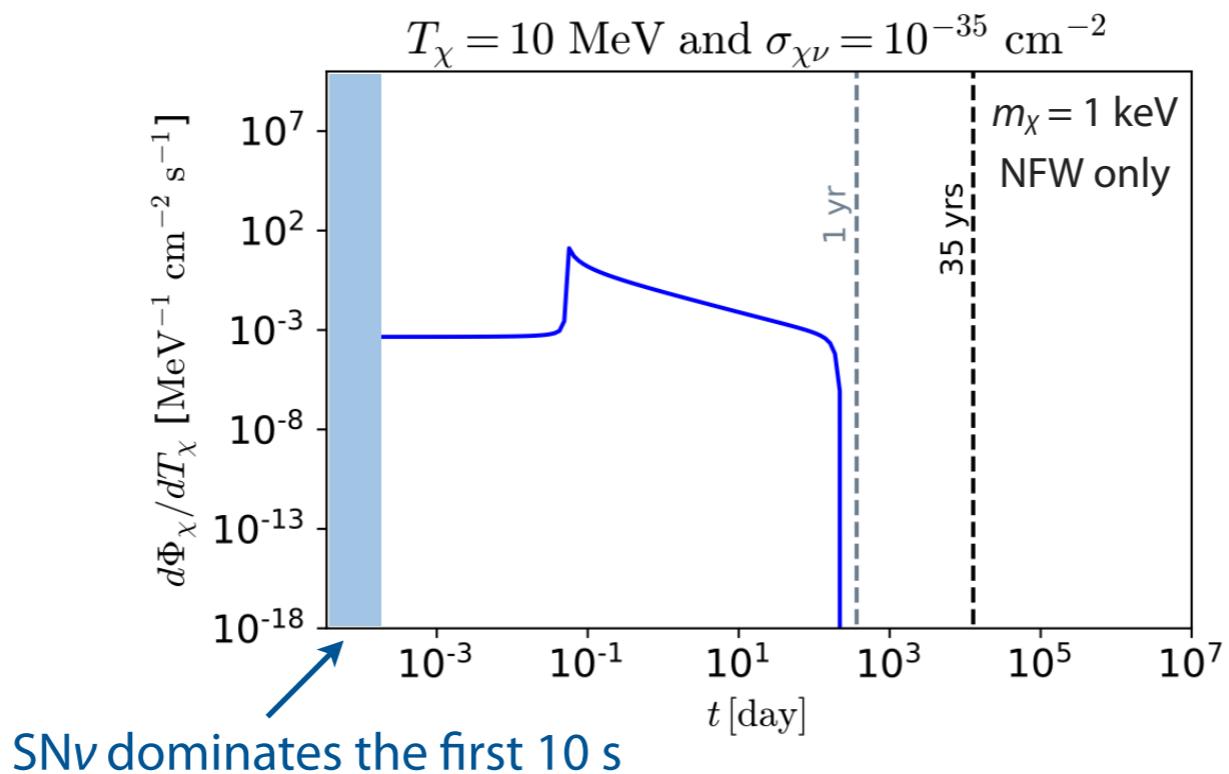
Duan+ 2006

$$\frac{d\Phi_\chi(T_\chi, t)}{dT_\chi} = 2\pi r \int_0^1 d\cos\theta \mathcal{J} j_\chi(r, T_\chi, \alpha) \Big|_{t'=\frac{r}{c} + \frac{\ell}{v_\chi}}$$

Inferring m_χ directly from the time-of-flight

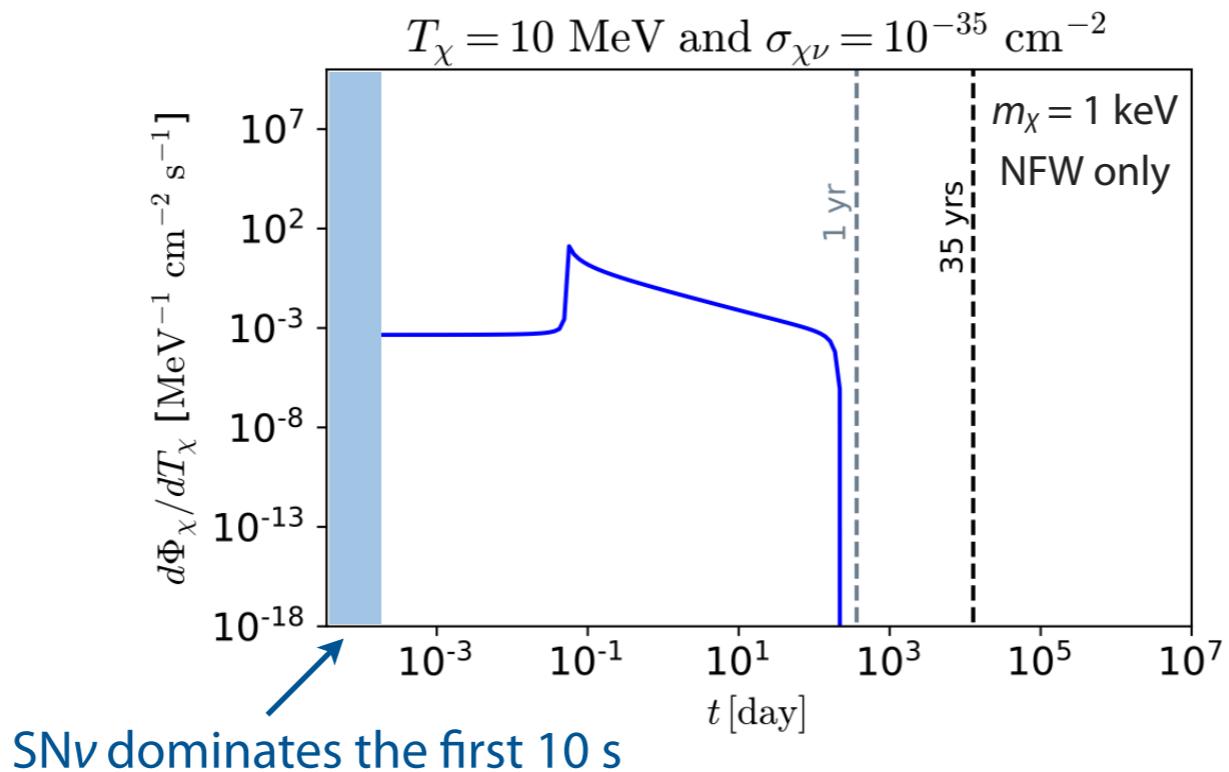


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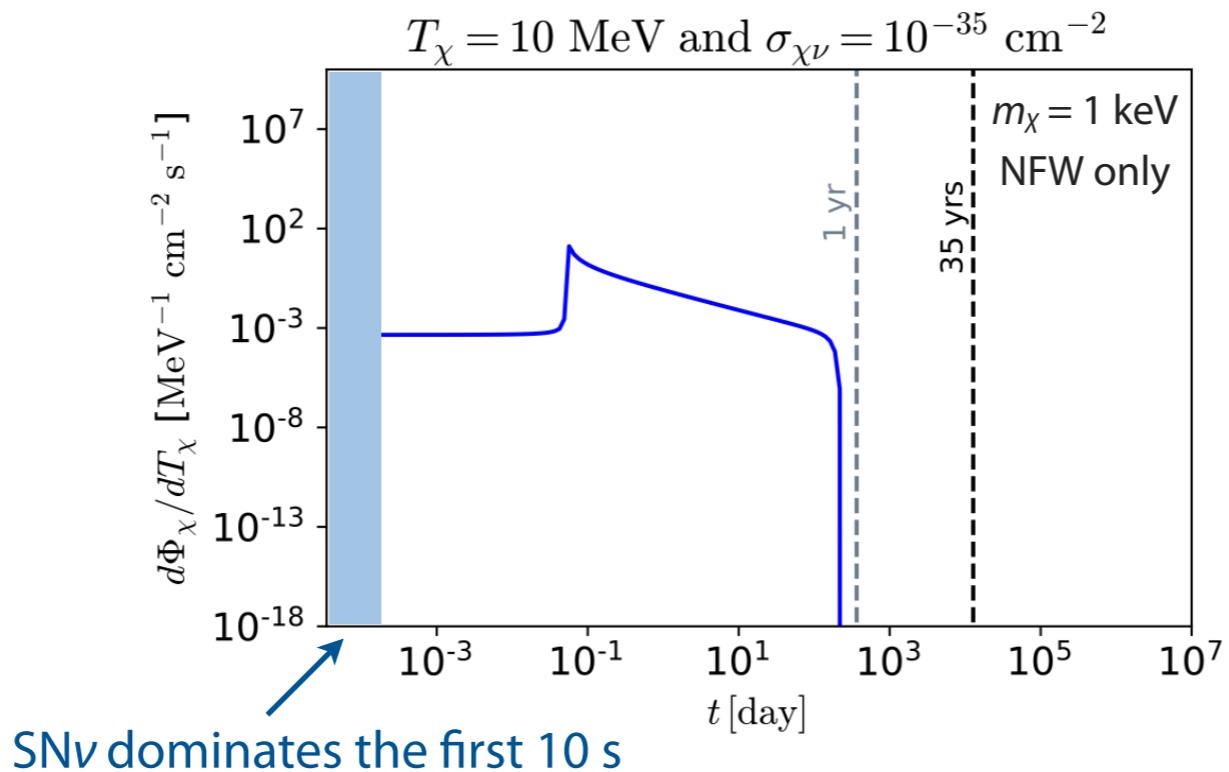
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Inferring m_χ directly from the time-of-flight



- SNv serves as the *anchor point* for **time-zero** in the detector and dominates **the first 10 seconds**
- The BDM flux exhibits a clearly **time-evolving** feature

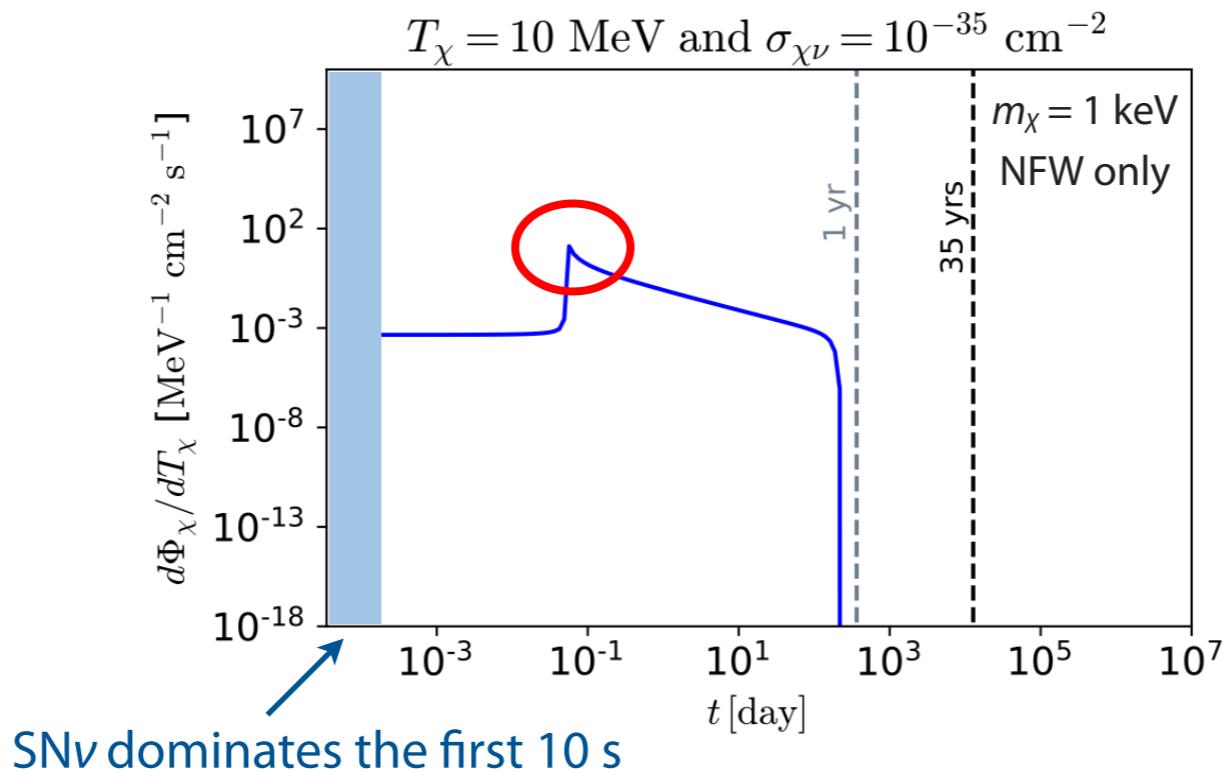
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- The delayed time can be estimated based on traveling a distance ℓ

$$t_{\text{delay}} \simeq 10 \text{ days} \times \left(\frac{\ell}{8 \text{ kpc}} \right) \left(\frac{m_\chi}{10 \text{ keV}} \right)^2 \left(\frac{T_\chi}{10 \text{ MeV}} \right)^{-2}$$

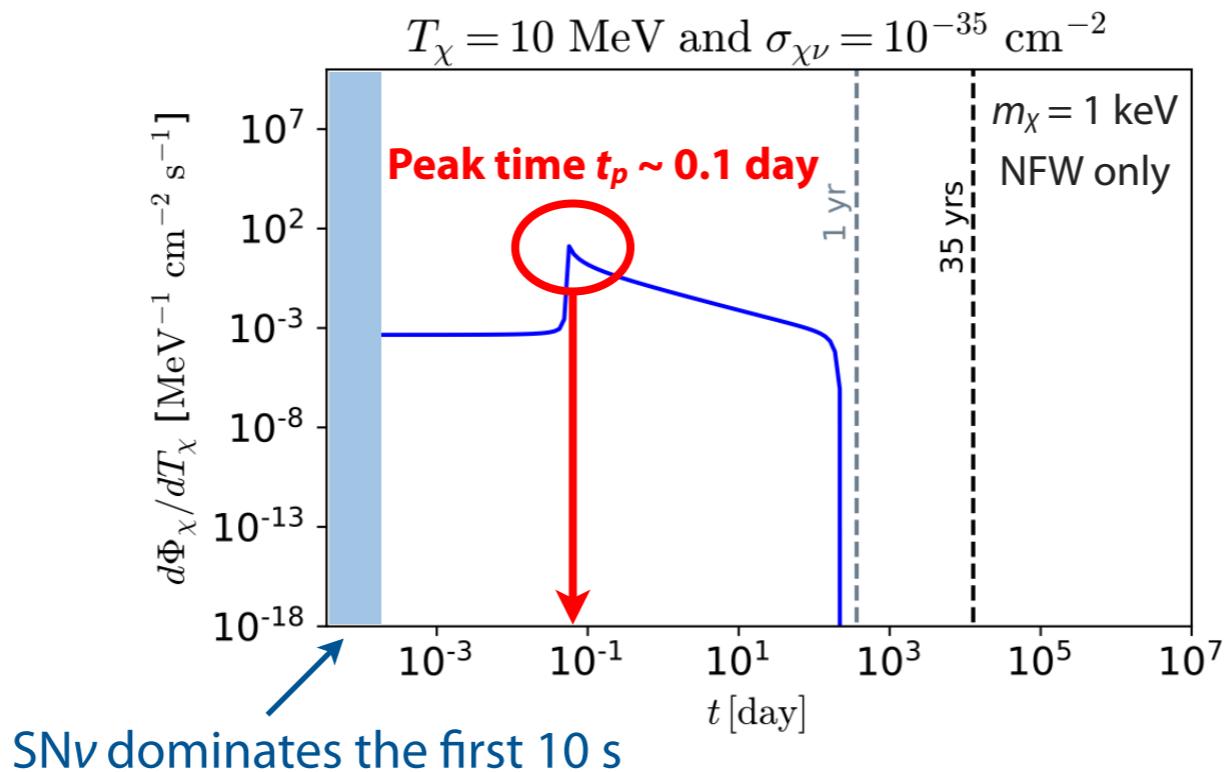
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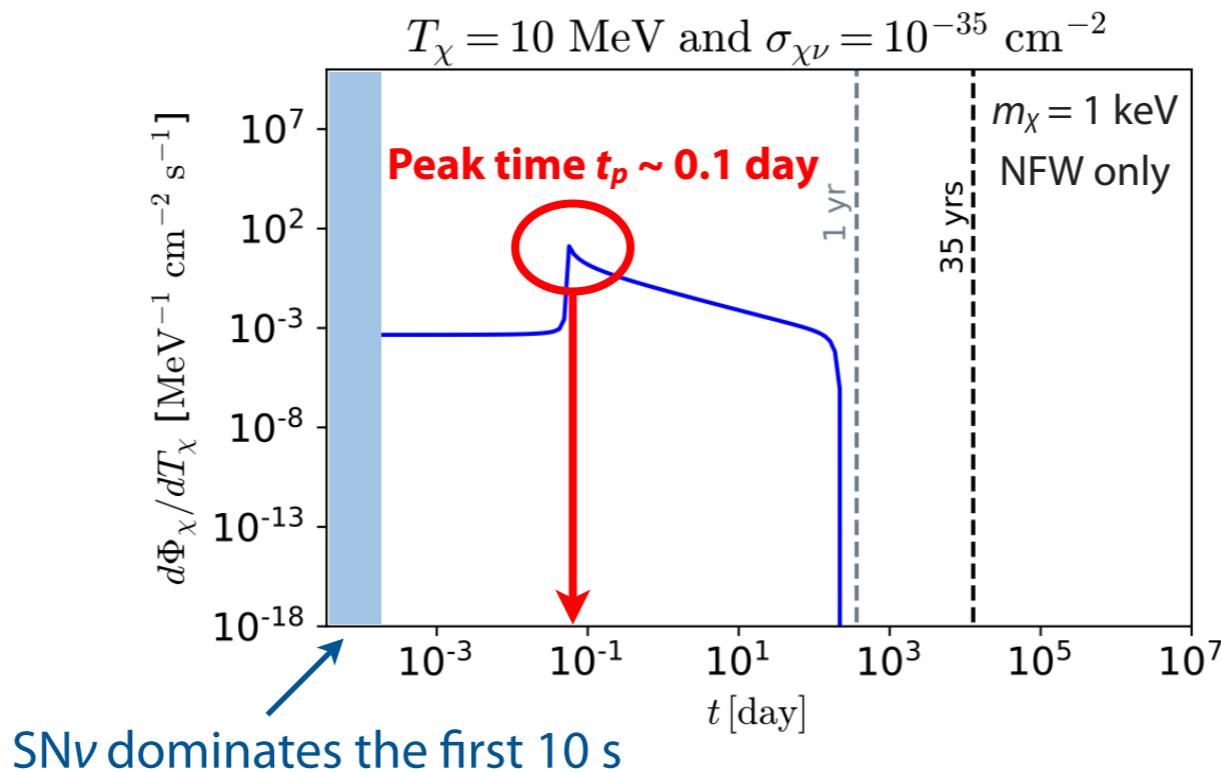
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Inferring m_χ directly from the time-of-flight



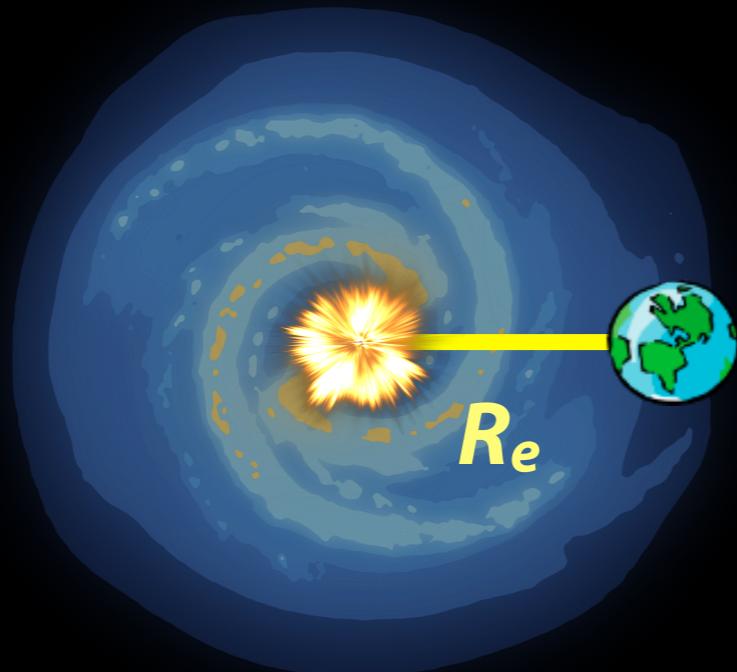
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- The **peak time t_p** (coming from the GC with $\ell \sim 8.5$ kpc) infers **DM mass m_χ** directly

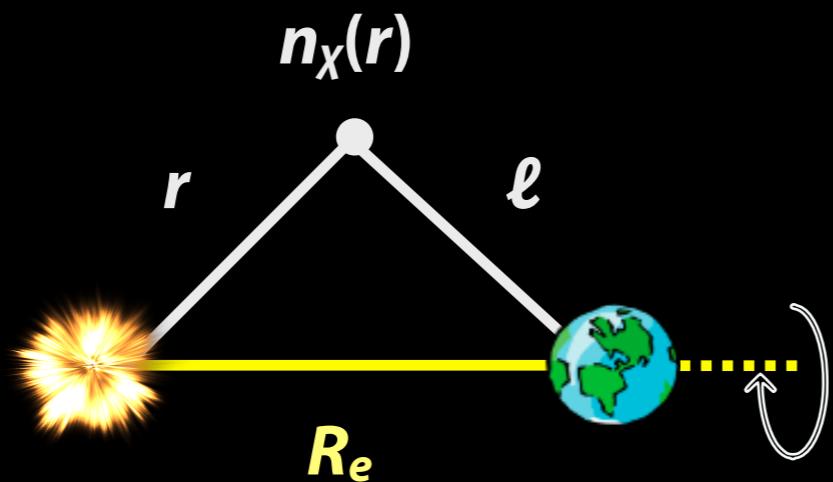
$$m_\chi \simeq 9.7 \text{ keV} \times \left(\frac{t_p}{10 \text{ days}} \right)^{1/2} \left(\frac{T_\chi}{10 \text{ MeV}} \right)$$

top-view



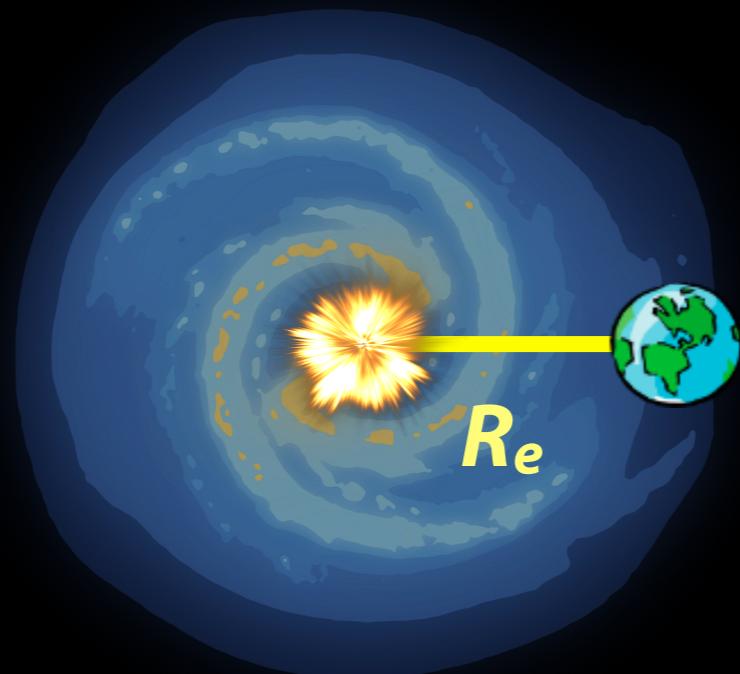
GC

side-view



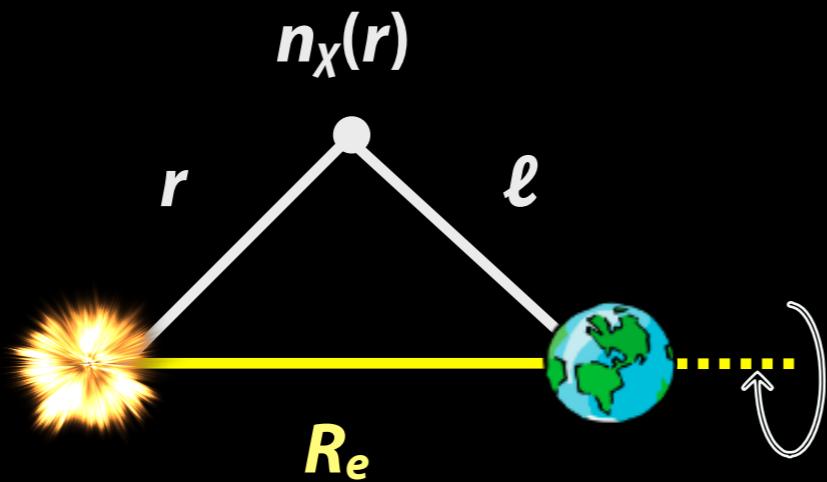
When SNe is NOT at the GC

top-view

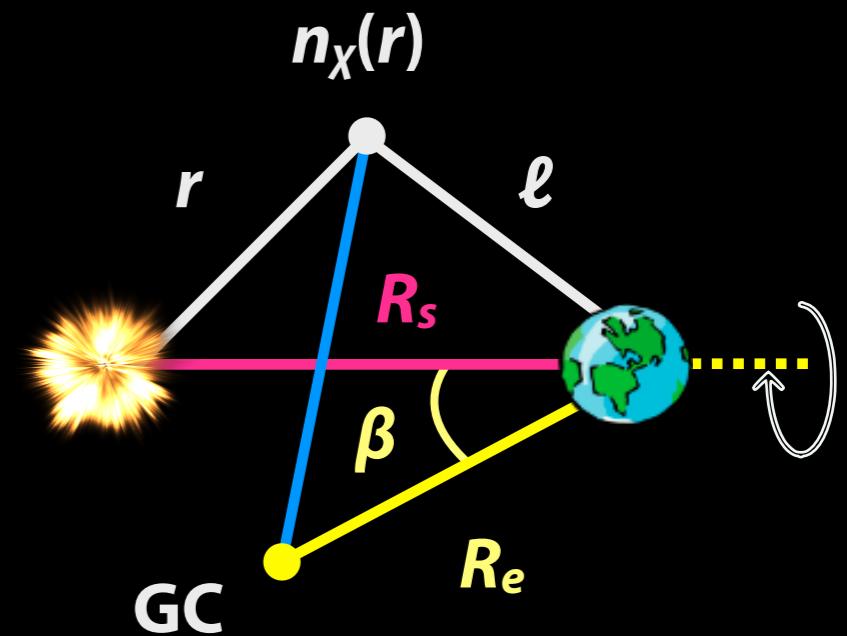


GC

side-view



off GC

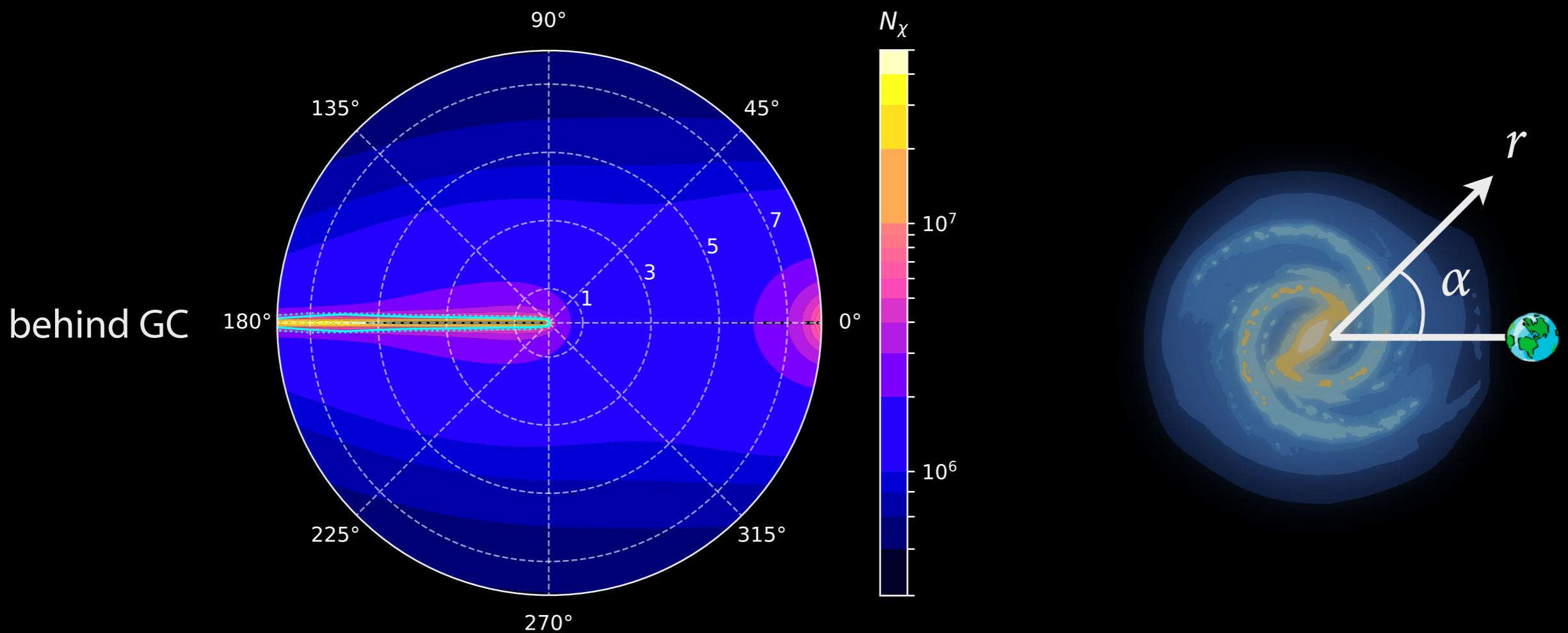


Map of Galactic SNv BDM events

- Given the detector exposure time and the number of electron N_e , the BDM event number N_χ can be estimated by

$$N_\chi = \int_{10\text{ s}}^{t_{\max}} dt \int_{T_{\chi,\min}}^{T_{\chi,\max}} \frac{d\Phi_\chi(T_\chi, t)}{dT_\chi dt}$$

- N_χ at different locations in the MW



$$m_\chi = 1 \text{ keV} \text{ and } \sigma_{\chi\nu} = \sigma_{\chi e} = 10^{-35} \text{ cm}^2$$

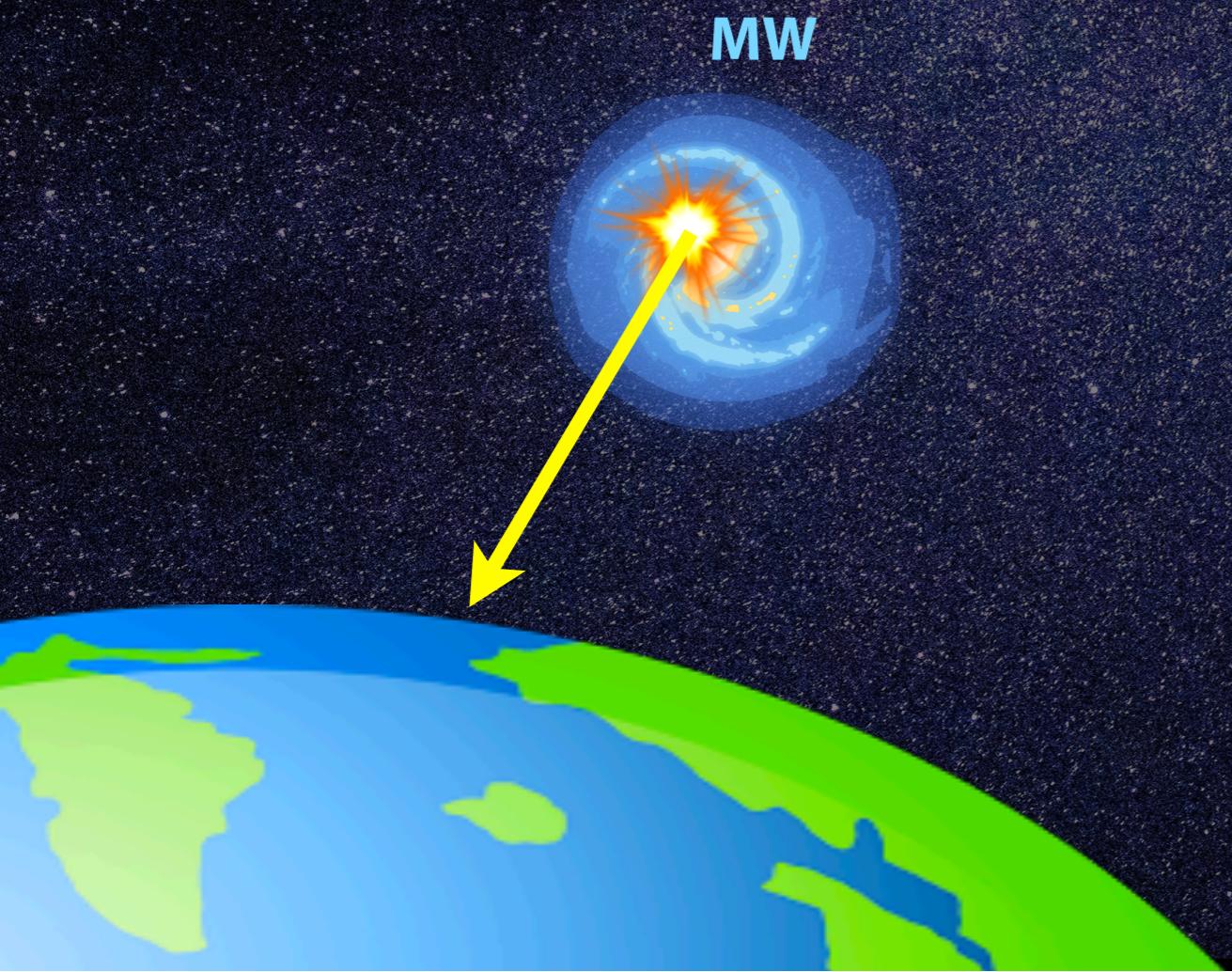


Diffuse SN ν BDM from the present and past Universe

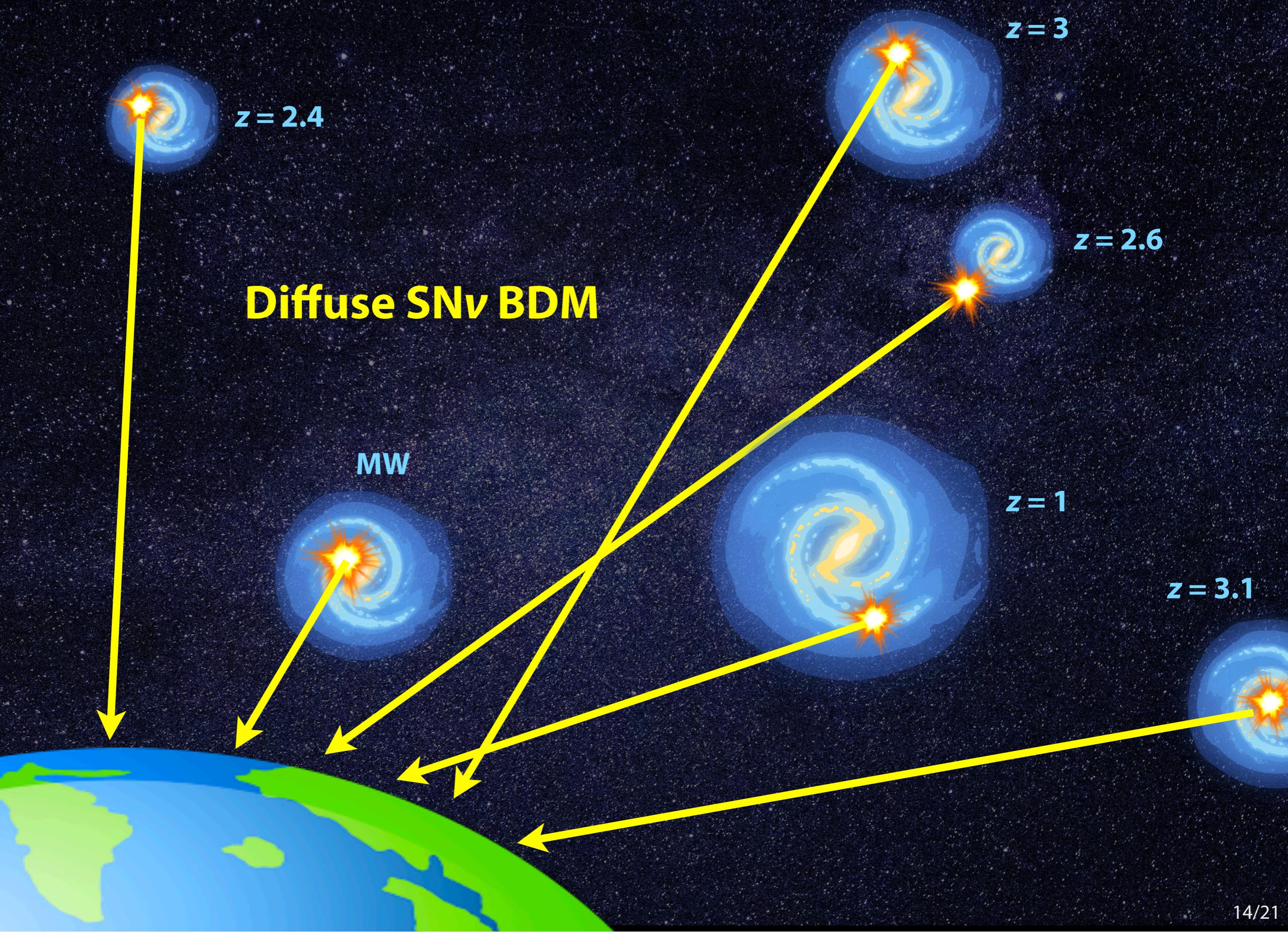
not-to-scale

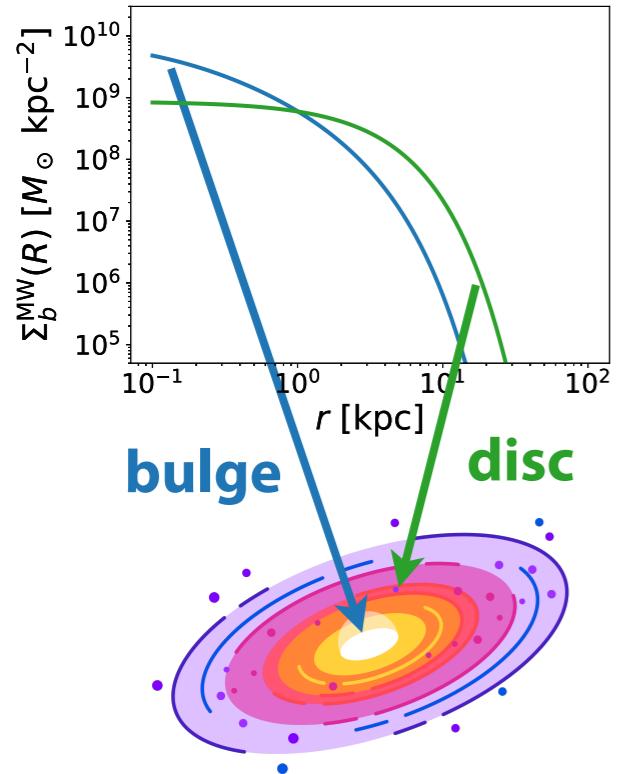


not-to-scale



not-to-scale





McMillan 2017

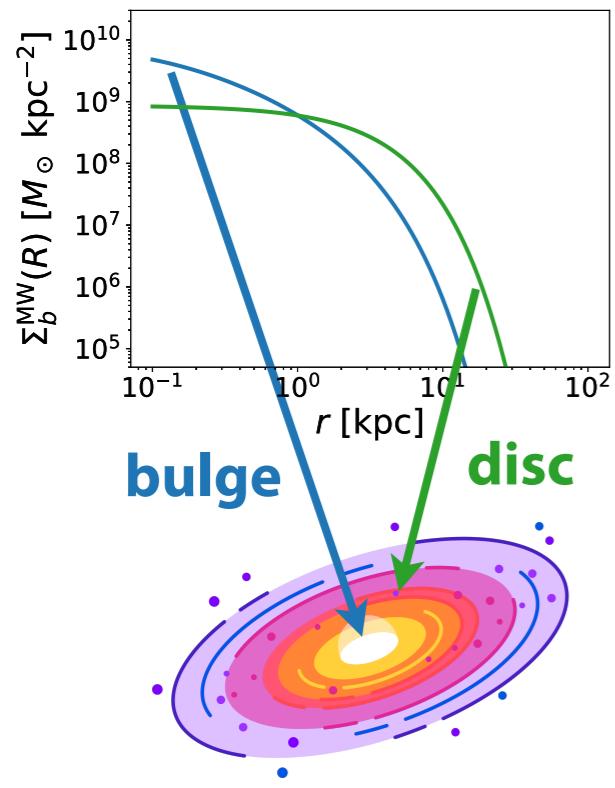
$$\rho_b(R, h) = \frac{\rho_{0,b}}{[1 + r'(R, h)/r_0]^\alpha} e^{-\frac{r'^2(R, h)}{r_{\text{cut}}^2}}$$

$$\rho_d(R, h) = \frac{\Sigma_0}{2h_d} e^{-\frac{|h|}{h_d} - \frac{R}{R_d}}$$

$$r_0 \text{ and } r_{\text{cut}} \propto M_G^{1/3}$$

$$R_m, R_d \text{ and } h_d \propto M_G^{1/2}$$

MW w/t $M_G = M_{\text{MW}}$



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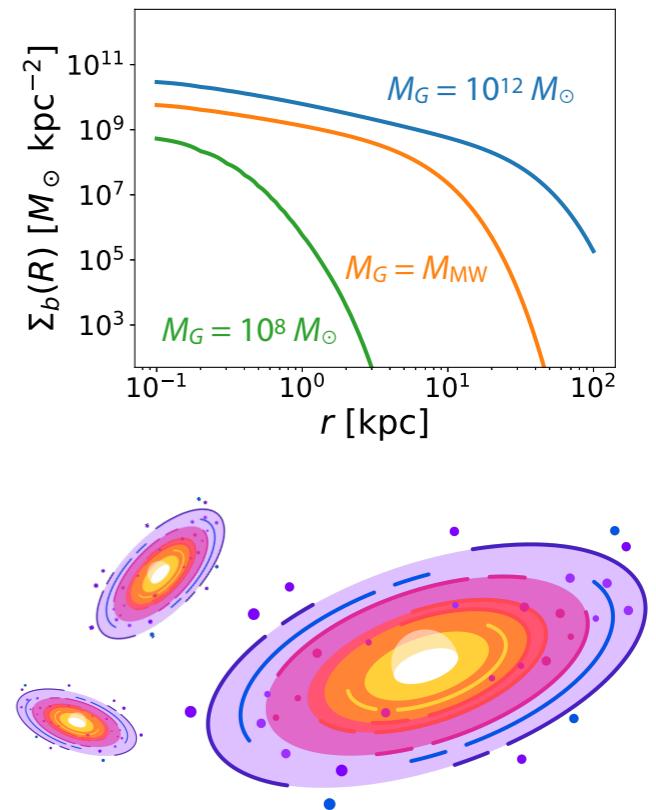
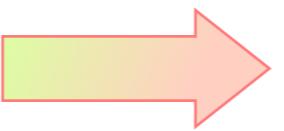
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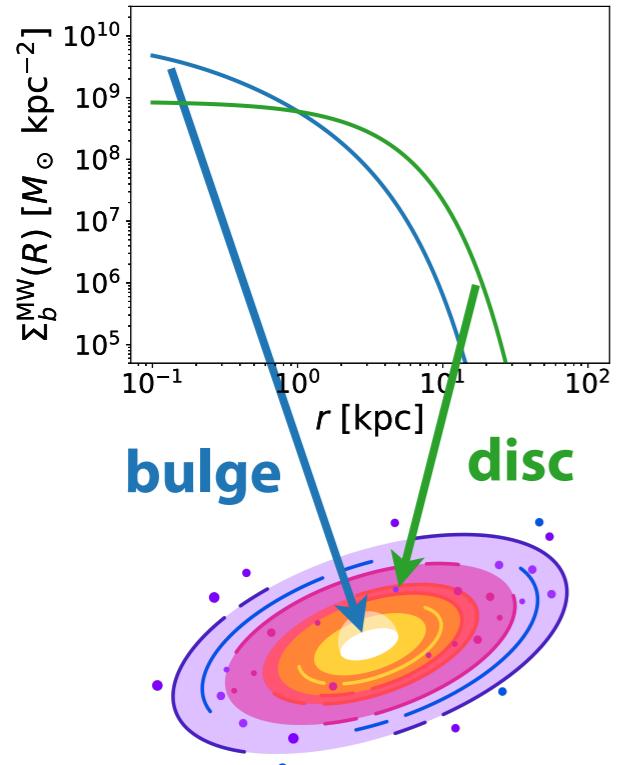
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Galaxies w/t arbitrary M_G



MW w/t $M_G = M_{\text{MW}}$

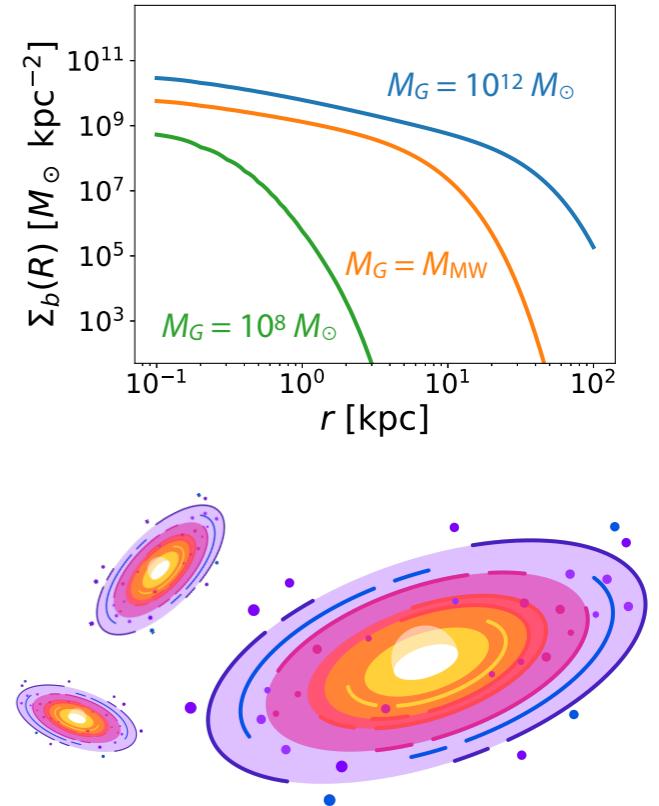
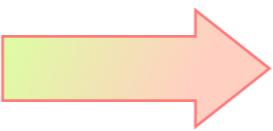
McMillan 2017

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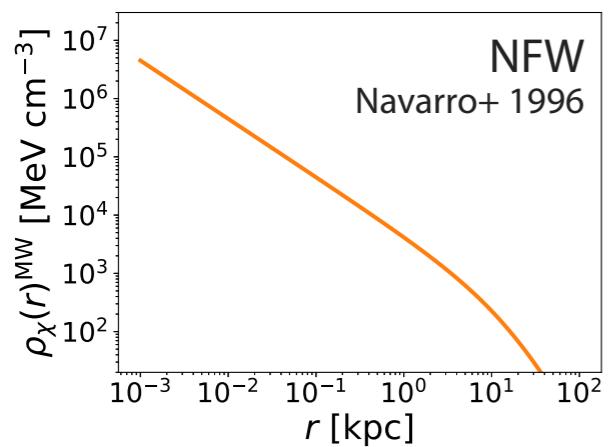
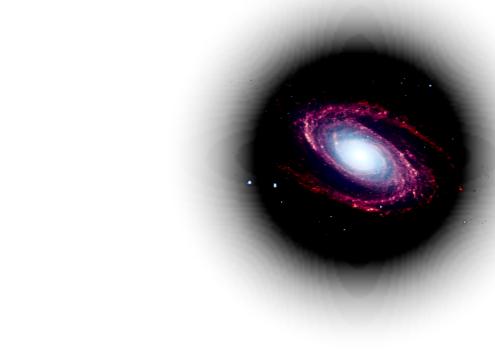
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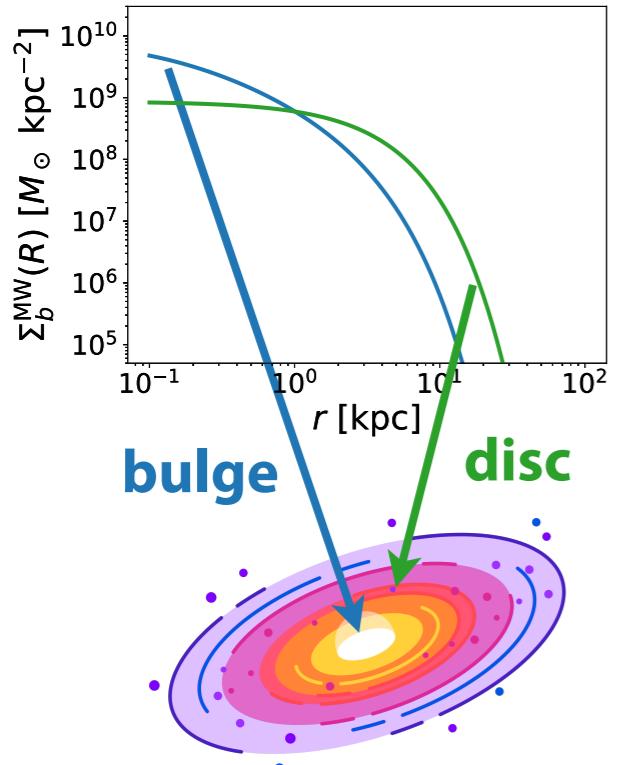
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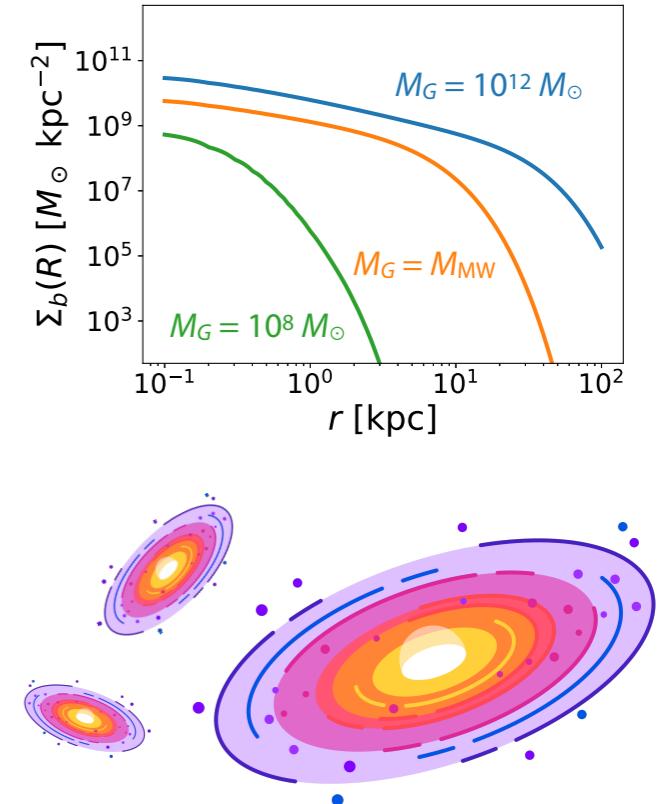
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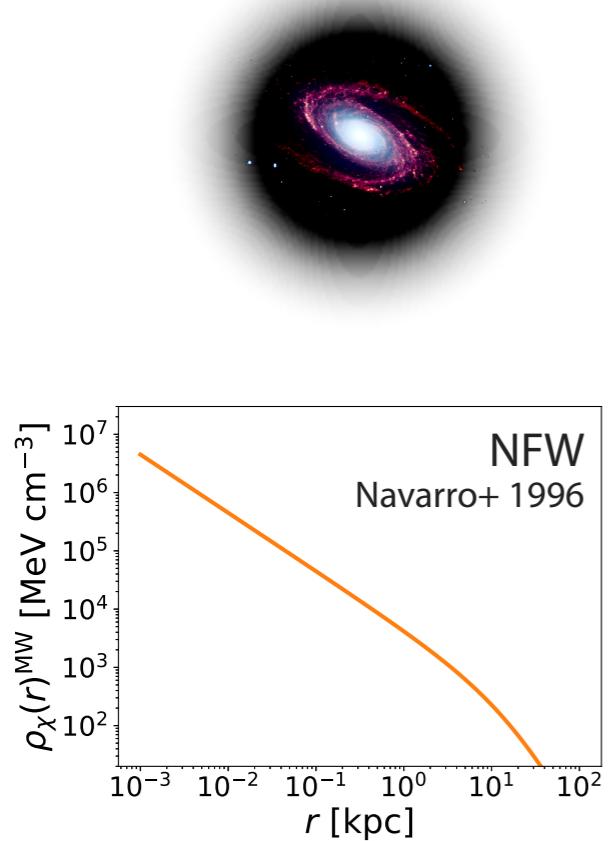
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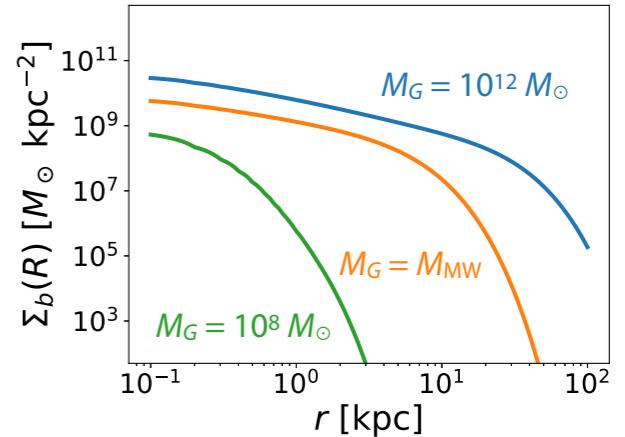
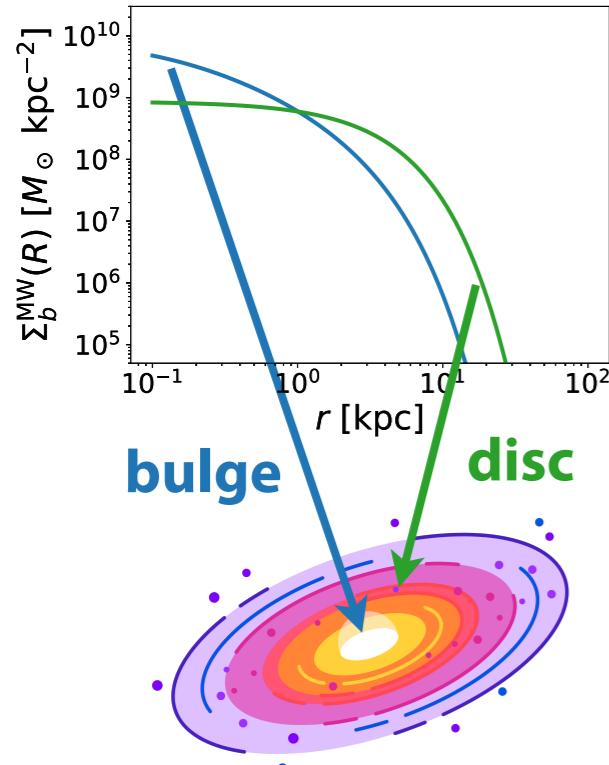
Galaxies w/t arbitrary M_G



$$\rho_\chi(r) = \frac{\rho_s}{r_s} \left(1 + \frac{r}{r_s}\right)^n$$

$r_s \propto M_{\text{halo}}^{1/3}$

$$\rho_s = \frac{M_{\text{halo}}}{\int \rho_\chi(r) d^3r}$$

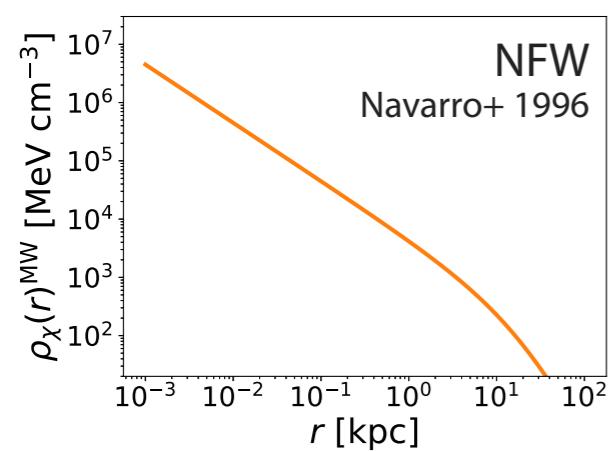


MW w/t $M_G = M_{\text{MW}}$

Galaxies w/t arbitrary M_G



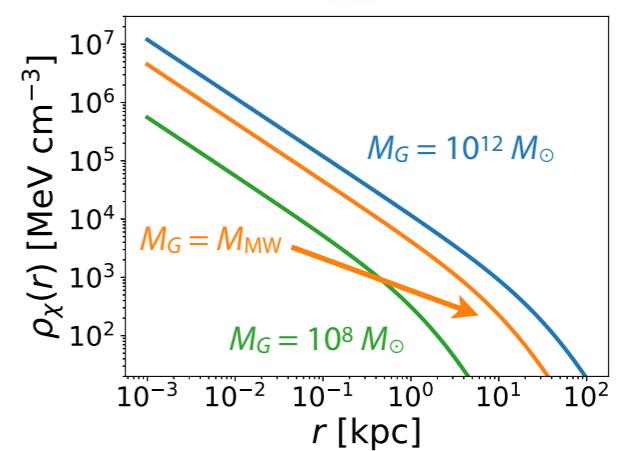
$M_{\text{halo}} = \eta M_G$
 $\eta \sim 20 - 50$
 Moster+ 2010
 Grielli+ 2020

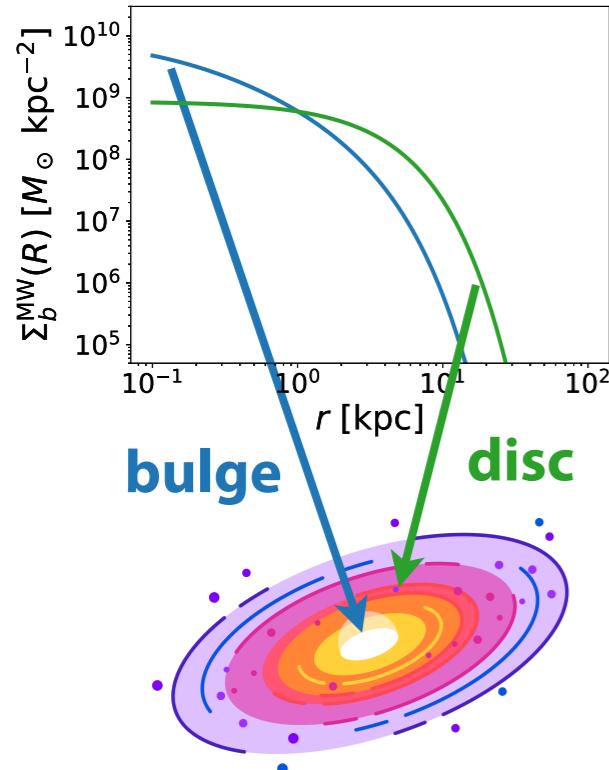


$$\rho_{\chi}(r) = \frac{\rho_s}{r_s} \left(1 + \frac{r}{r_s}\right)^n$$

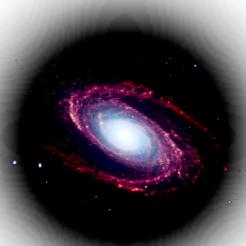
$$r_s \propto M_{\text{halo}}^{1/3}$$

$$\rho_s = \frac{M_{\text{halo}}}{\int \rho_{\chi}(r) d^3r}$$





MW w/t $M_G = M_{\text{MW}}$

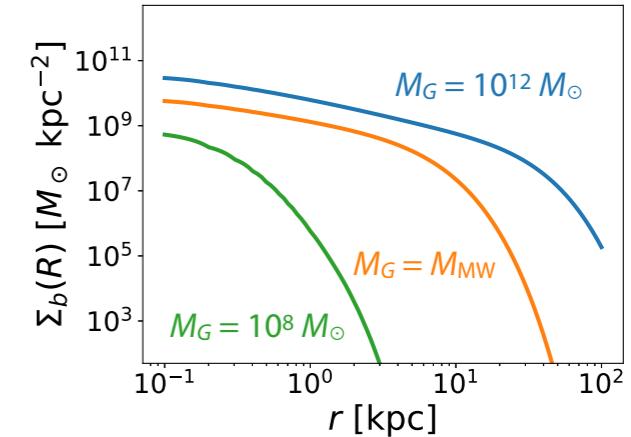


McMillan 2017

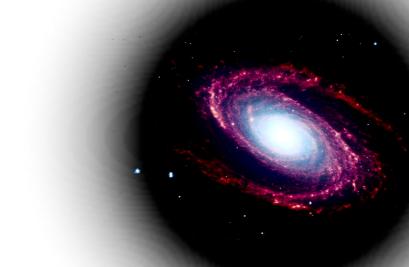
$$\rho_b(R, h) = \frac{\rho_{0,b}}{[1 + r'(R, h)/r_0]^\alpha} e^{-\frac{r'^2(R, h)}{r_{\text{cut}}^2}}$$

$$\rho_d(R, h) = \frac{\Sigma_0}{2h_d} e^{-\frac{|h|}{h_d} - \frac{R}{R_d}}$$

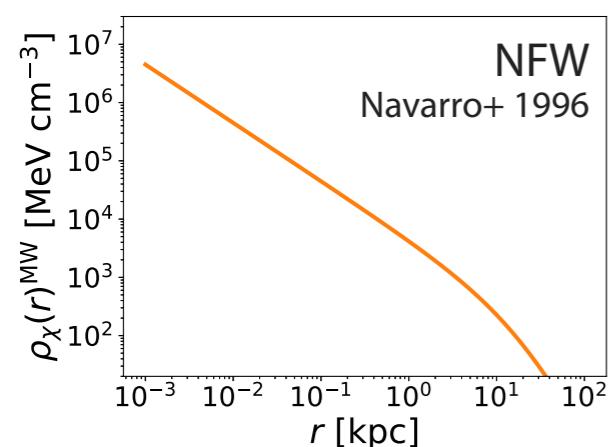
r_0 and $r_{\text{cut}} \propto M_G^{1/3}$
 R_m, R_d and $h_d \propto M_G^{1/2}$



Galaxies w/t arbitrary M_G



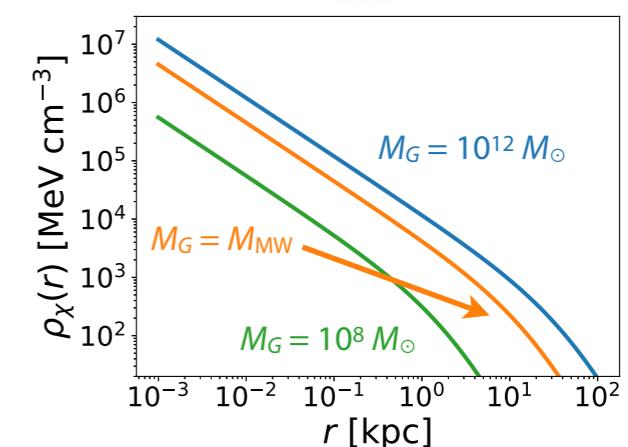
$M_{\text{halo}} = \eta M_G$
 $\eta \sim 20 - 50$
 Moster+ 2010
 Grielli+ 2020



$$\rho_\chi(r) = \frac{\rho_s}{r_s} \left(1 + \frac{r}{r_s}\right)^n$$

$$r_s \propto M_{\text{halo}}^{1/3}$$

$$\rho_s = \frac{M_{\text{halo}}}{\int \rho_\chi(r) d^3r}$$



Diffuse SN ν BDM (DBDM) flux

- The DBDM flux

$$\frac{d\Phi_\chi}{dT_\chi} = \frac{v_\chi}{H_0} \int_0^{z_{\max}} \frac{dz}{\epsilon(z)} \int dM_G \frac{d\Gamma_{\text{SN}}(z)}{dM_G} \frac{d\bar{N}_\chi(M_G)}{dT'_\chi}, \quad T'_\chi(1+z)T_\chi$$

- Given the SN rate per coming volume per M_G at z

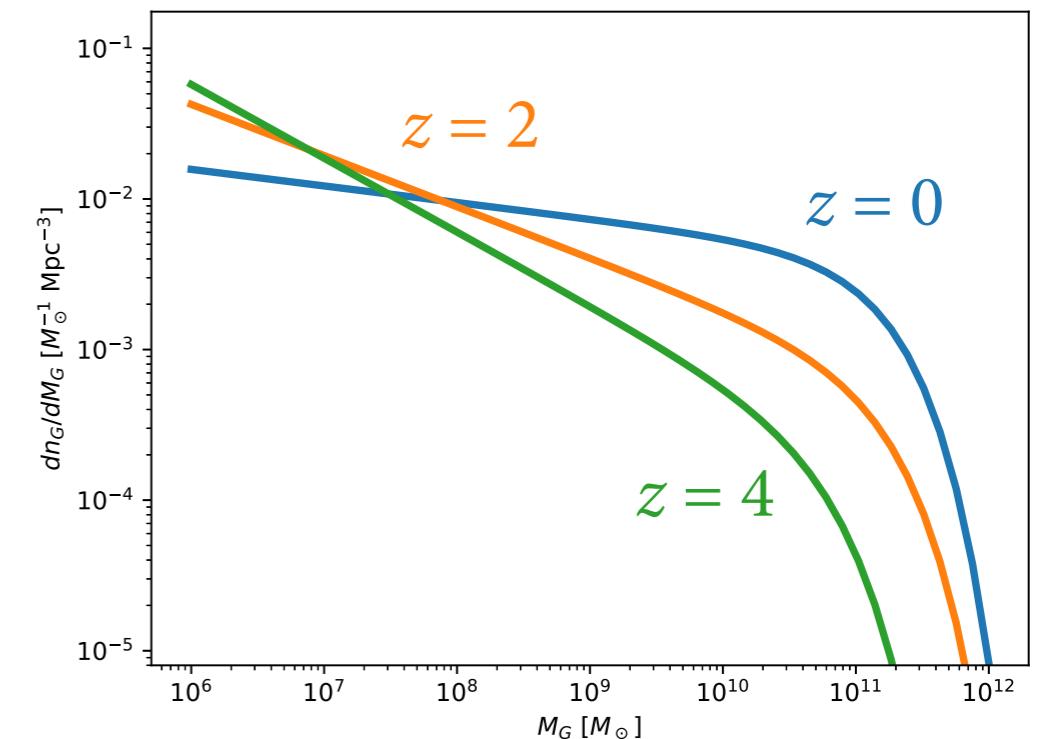
$$\frac{d\Gamma_{\text{SN}}(z)}{dM_G} = \frac{dn_G(z)}{dM_G} \frac{\dot{\rho}_*(z)}{\dot{\rho}_*(0)} \frac{M_G}{M_{\text{MW}}} R_{\text{SN},0}$$

- The galactic number density per coming volume per M_G at z ($m = \log_{10} M_G/M_\odot$)

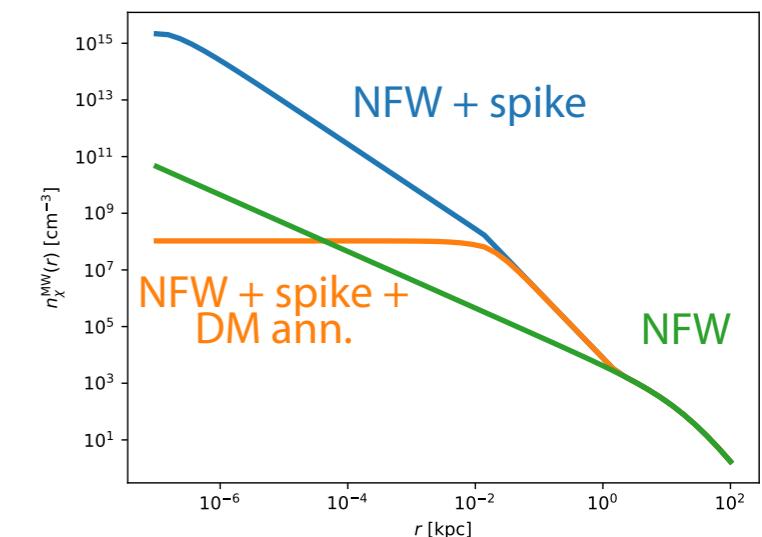
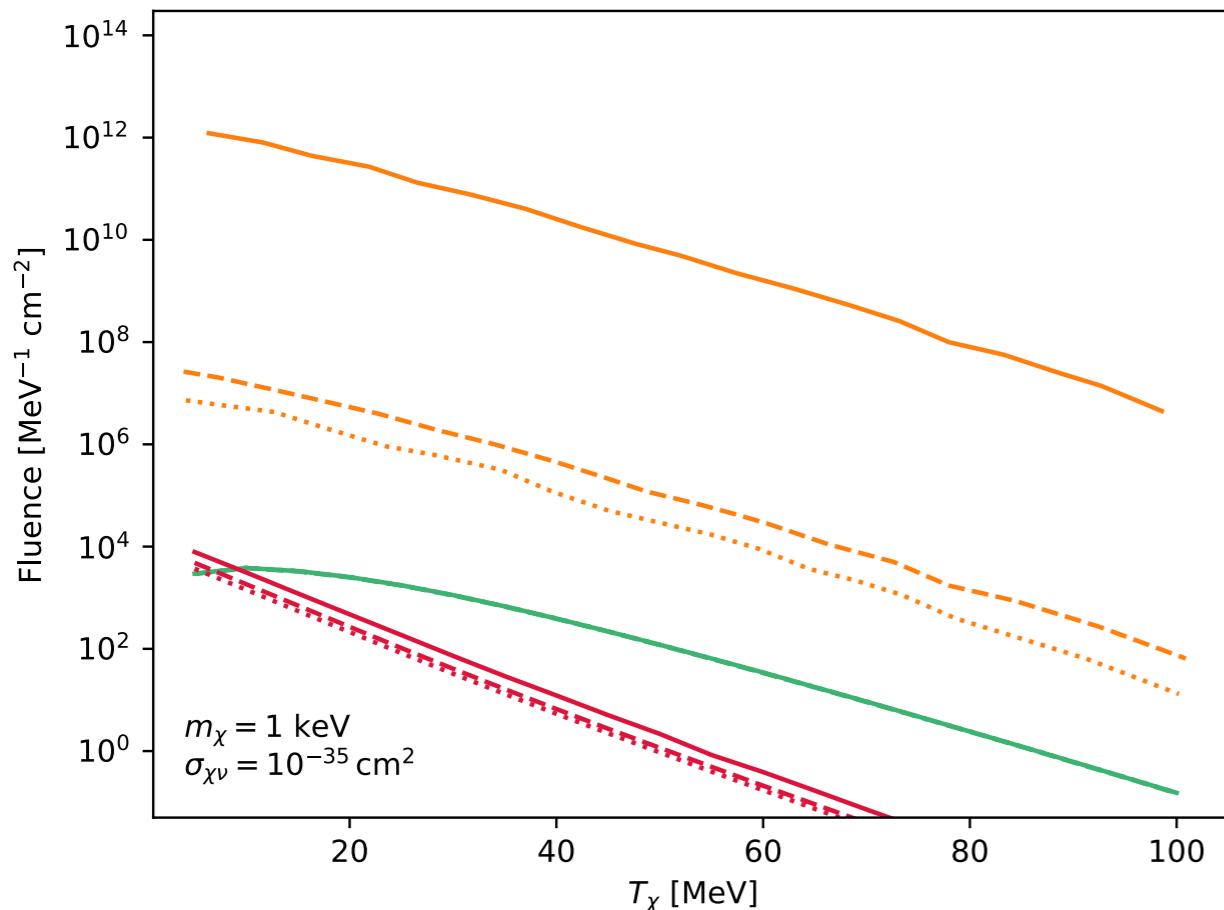
$$\frac{dn_G(z)}{dm} = \phi_0 \ln 10 \times 10^{(m-M)(1+\gamma)} e^{-10^{m-M_c}}$$

| Redshift (z) | γ | $\log_{10}(M_c/M_\odot)$ | $\phi_0 (\times 10^{-4}) (\text{Mpc}^{-3})$ | References |
|------------------|----------|--------------------------|---|------------------------------|
| 0.0 – 0.7 | -1.11 | 11.22 | 18.2 | Fontana+04 [15] in Ref. [14] |
| 0.7 – 1.0 | -1.27 | 11.37 | 11.0 | |
| 1.0 – 1.4 | -1.28 | 11.26 | 6.2 | |
| 1.4 – 1.7 | -1.31 | 11.25 | 4.3 | |
| 1.8 – 2.2 | -1.34 | 11.22 | 3.1 | Fontana+06 [16] in Ref. [14] |
| 2.2 – 2.6 | -1.38 | 11.16 | 2.4 | |
| 2.6 – 3.0 | -1.41 | 11.09 | 1.9 | |
| 3.0 – 3.5 | -1.45 | 10.97 | 1.5 | |
| 3.5 – 4.0 | -1.49 | 10.81 | 1.1 | |
| 4.0 – 4.5 | -1.53 | 10.44 | 3.0 | Song+16 [17] in Ref. [14] |
| 4.5 – 5.5 | -1.67 | 10.47 | 1.3 | |
| 5.5 – 6.5 | -1.93 | 10.30 | 0.3 | |
| 6.5 – 8.0 | -2.05 | 10.42 | 0.1 | |

Galactic number density at different z



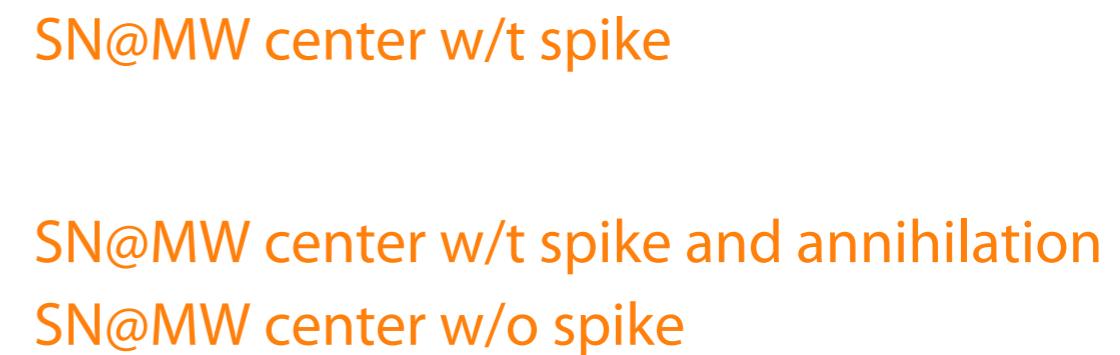
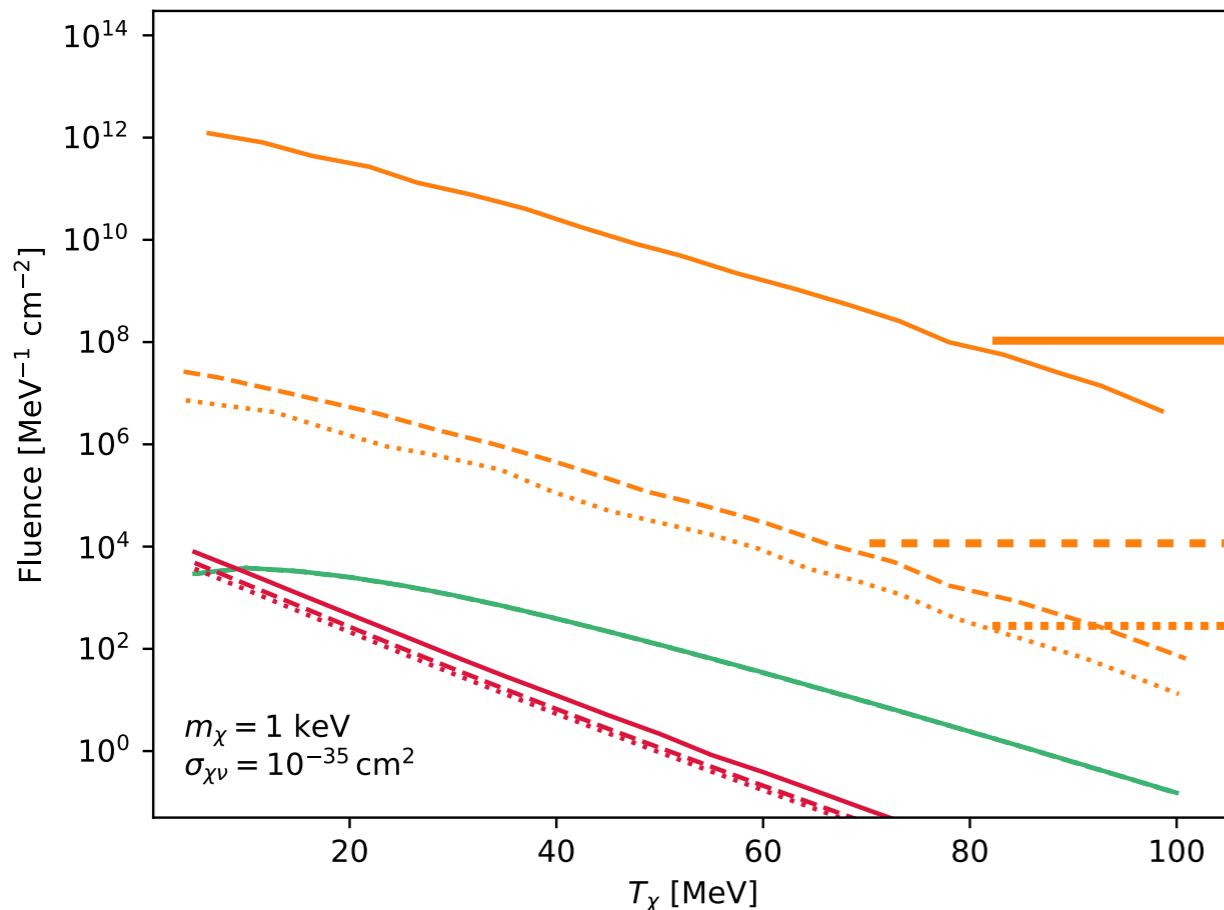
The fluences



- We show the **fluences** for SN at different locations for comparison

$$\text{Fluence} = \int_{t_{\min}}^{t_{\max}} dt \frac{d\Phi_\chi}{dT_\chi}$$

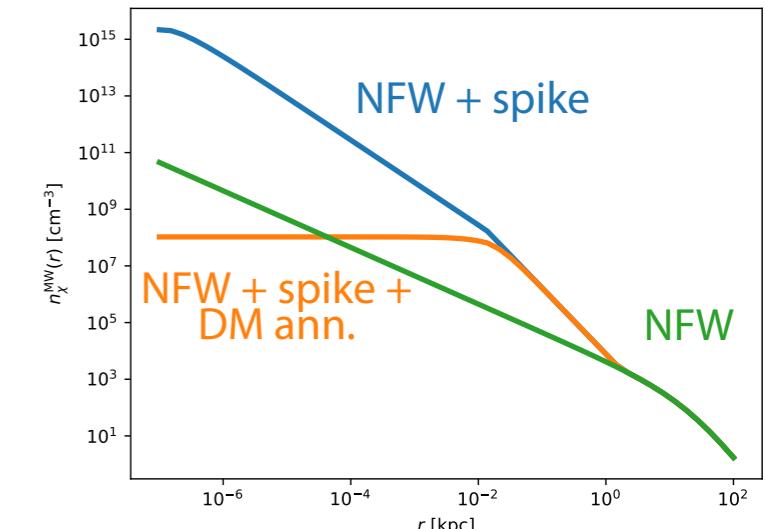
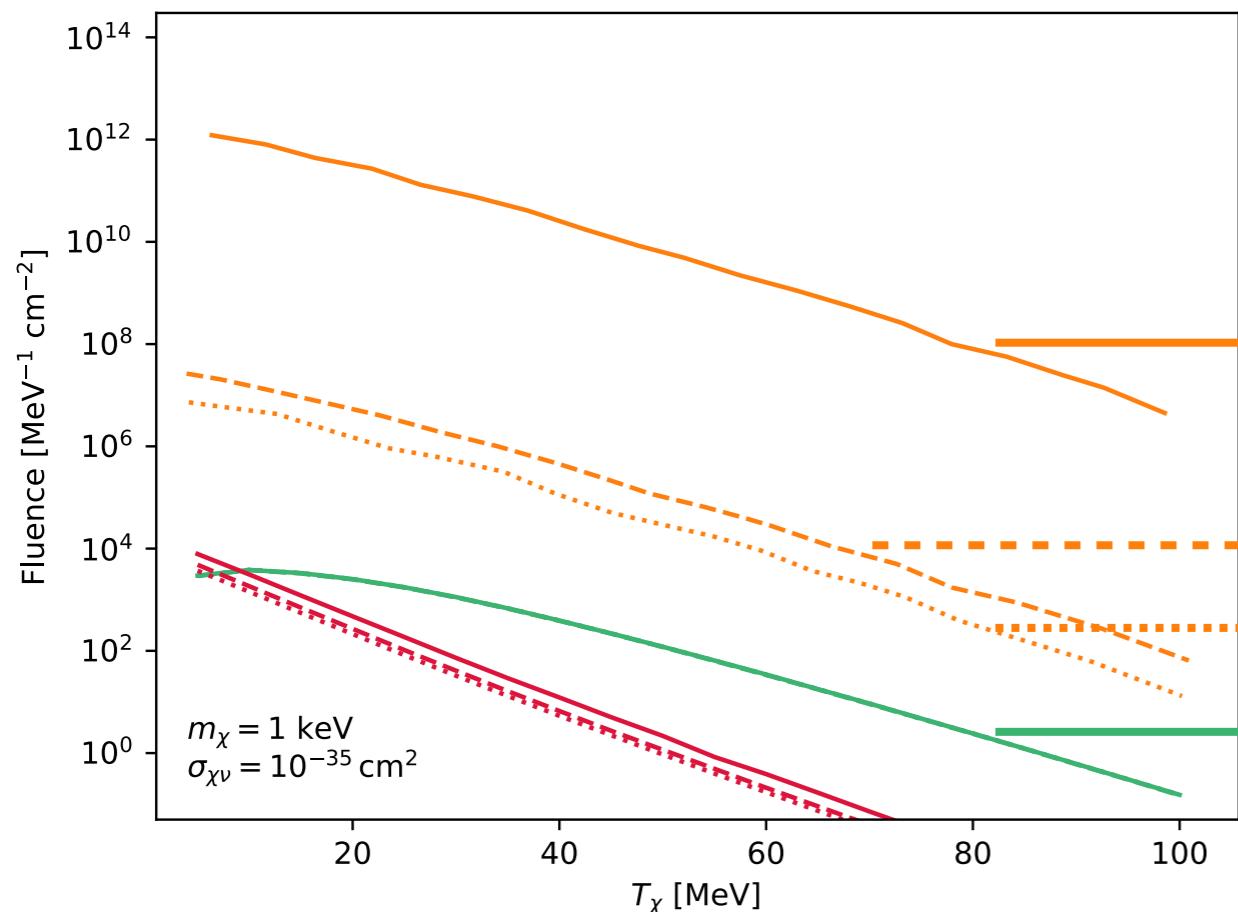
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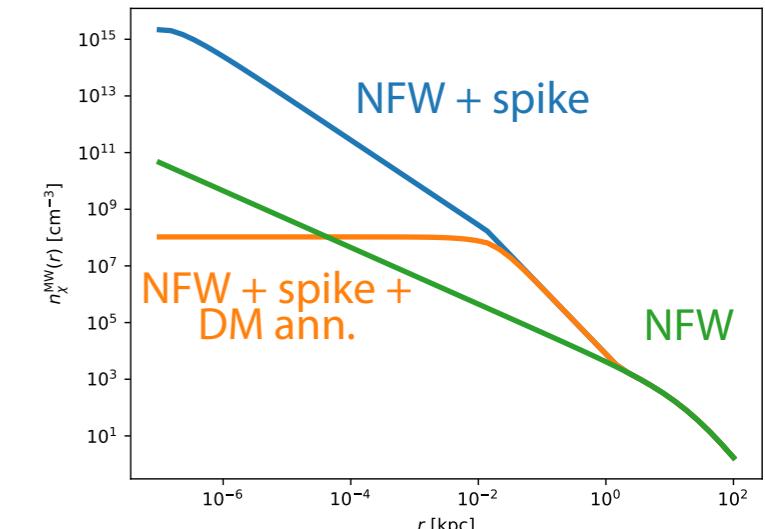
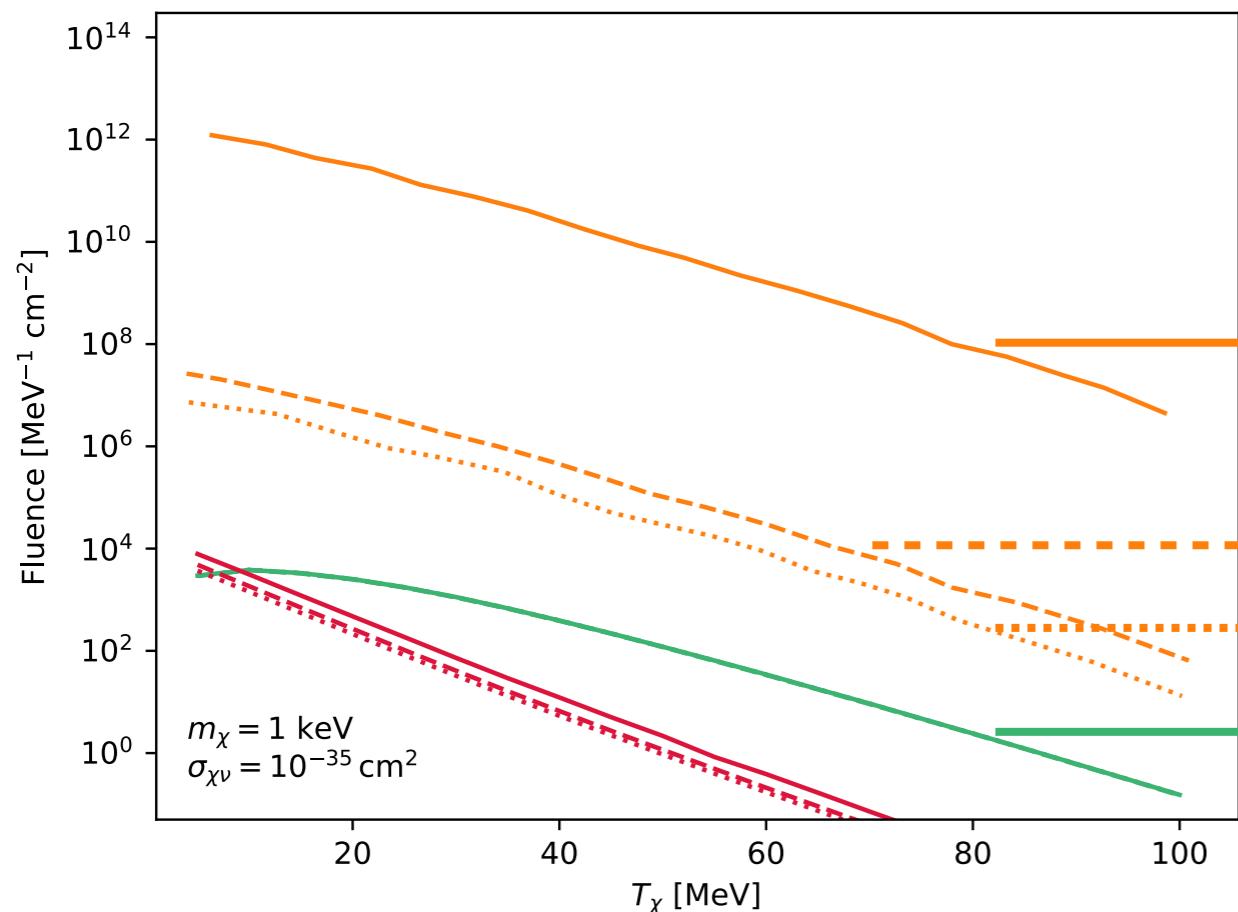
- SN@MW center w/t spike
- SN@MW center w/t spike and annihilation
- SN@MW center w/o spike
- SN1987a

- We show the **fluences** for SN at different locations for comparison

$$\text{Fluence} = \int_{t_{\min}}^{t_{\max}} dt \frac{d\Phi_\chi}{dT_\chi}$$

- The documented location of SN1987a indicates a separation of 1.75 kpc from the LMC center

The fluences

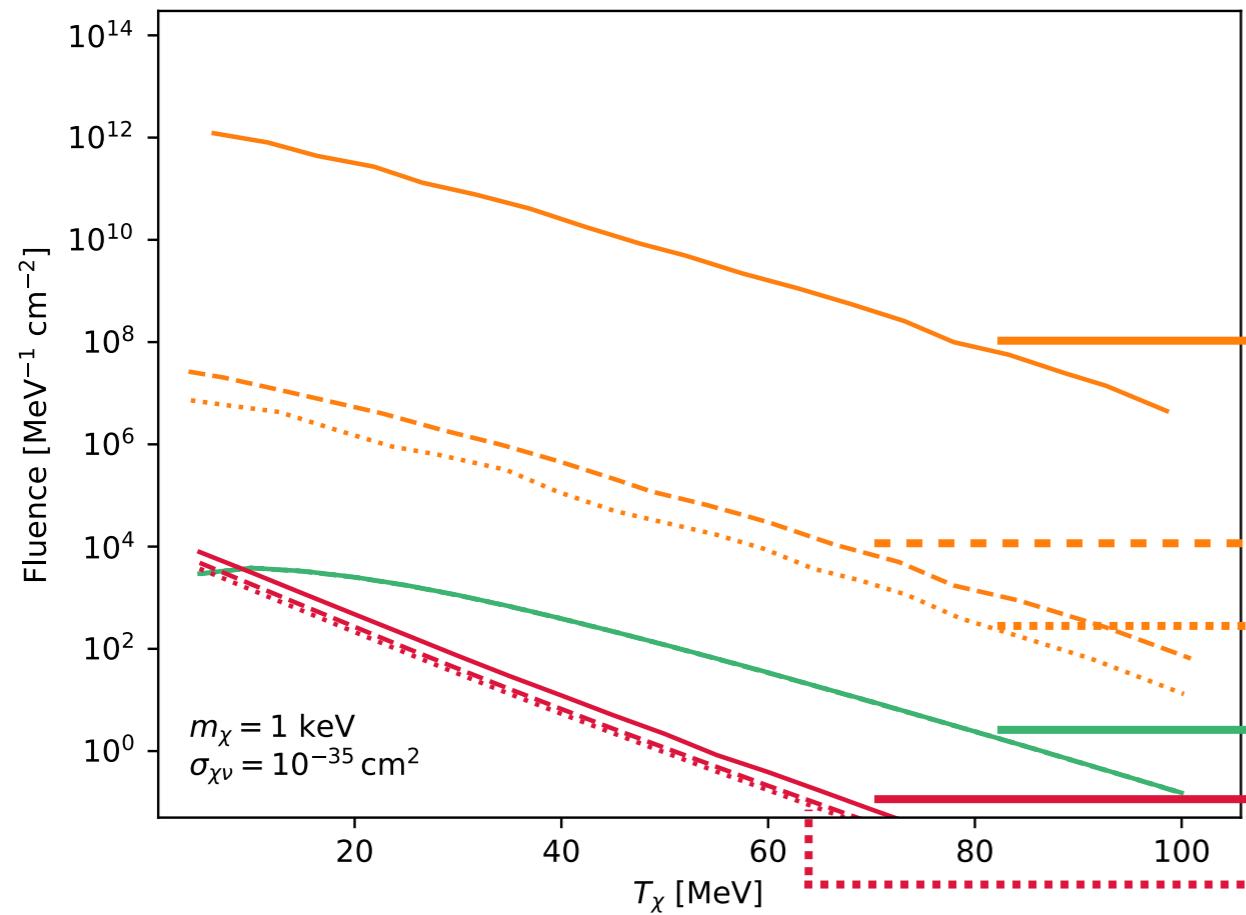


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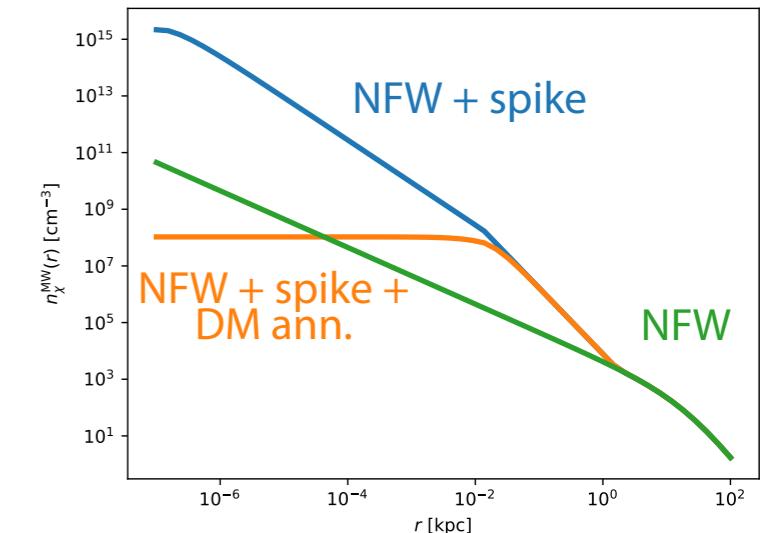
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- The documented location of SN1987a indicates a separation of 1.75 kpc from the LMC center
- The effect of DM spike is highly sensitive to the SN location and becomes less apparent when the SN is farther away from the GC

The fluences



- SN@MW center w/t spike
- SN@MW center w/t spike and annihilation
- SN@MW center w/o spike
- SN1987a
- DBDM w/t spike
- DBDM w/t spike and annihilation w/o spike

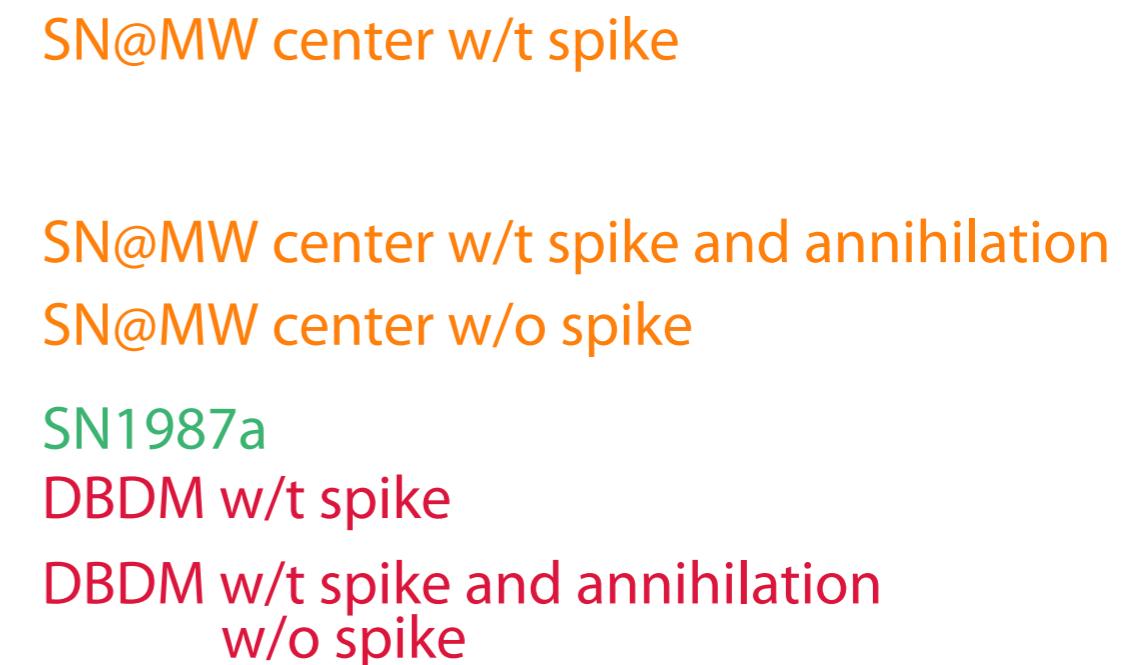
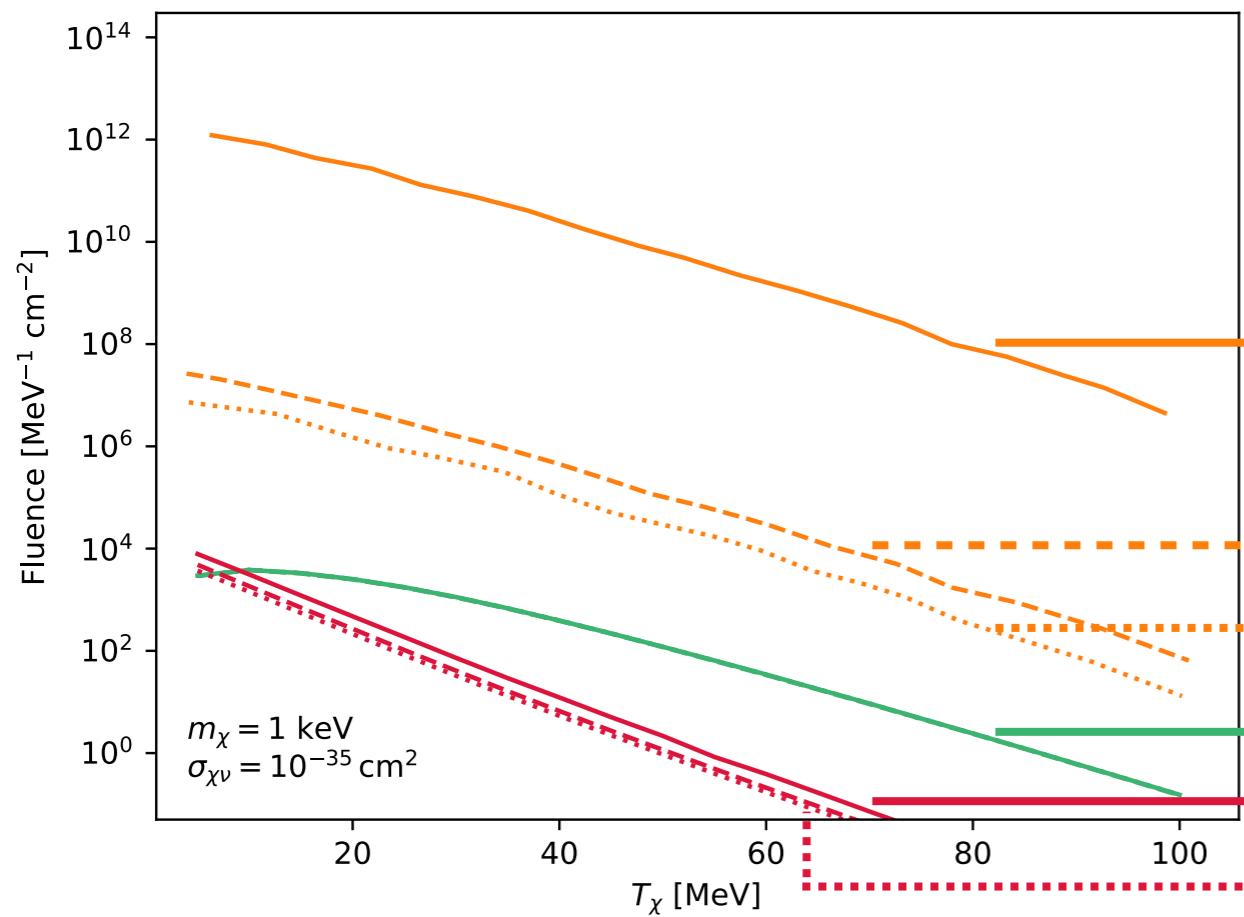


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- The documented location of SN1987a indicates a separation of 1.75 kpc from the LMC center
- The effect of DM spike is highly sensitive to the SN location and becomes less apparent when the SN is farther away from the GC
- The DBDM is **robust against** the uncertainties related to DM spike



Constrain and projected sensitivities

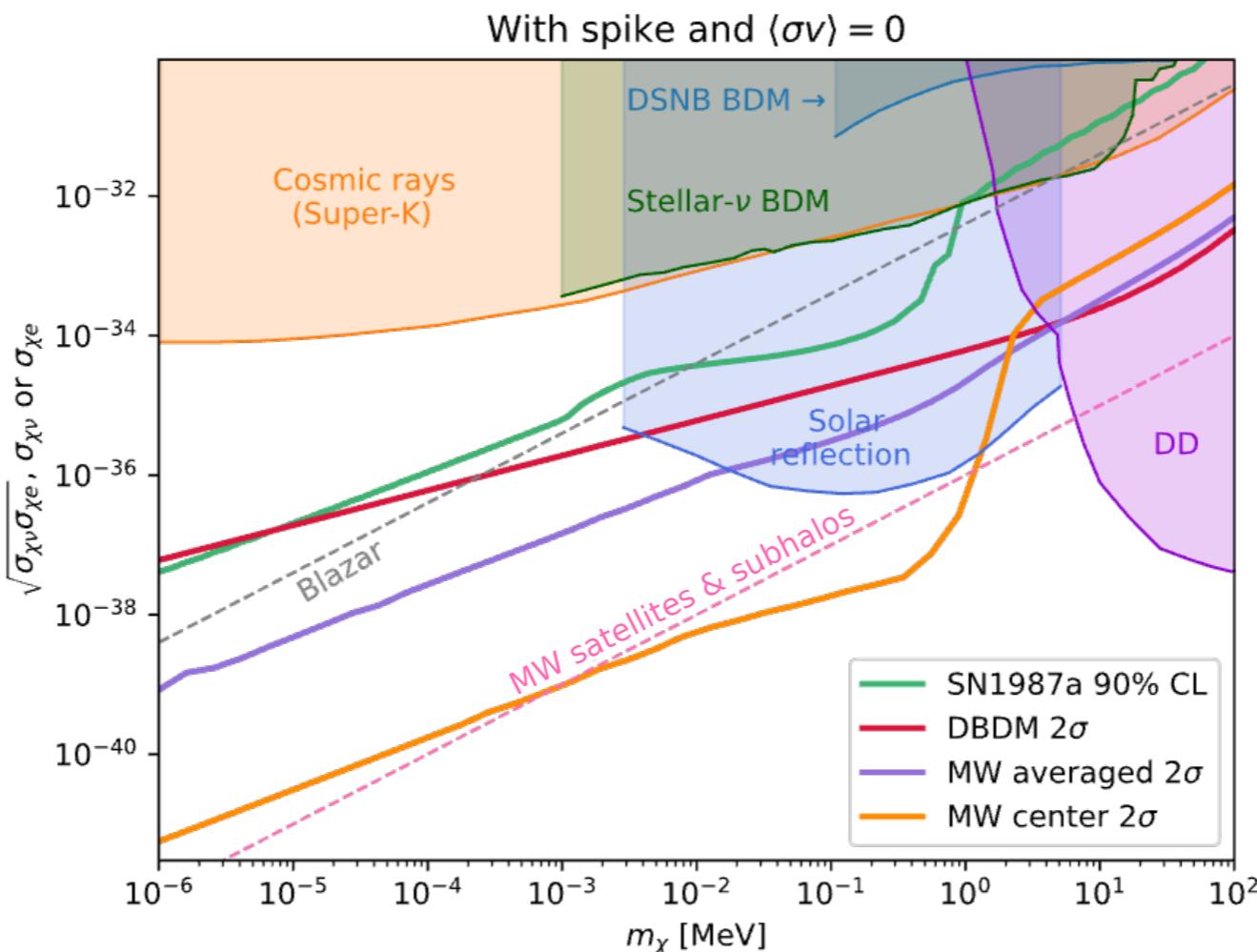
Constraints and projected sensitivities

- Assuming cross sections $\sigma_{\chi\nu} = \sigma_{\chi e}$, we obtain the 2-sigma sensitivity by

$$\frac{N_s}{\sqrt{N_s + N_b}} = 2\sigma$$

assuming Hyper-K detector and the background $N_b \sim 1.1 \times 10^5 \text{ yr}^{-1}$

- The exposure time t_{exp} for DBDM is 5 years, while for MW SNv BDM it is up to 35 years



See Lin & Wu, PRL 133, 111004 (2024) and refs. therein

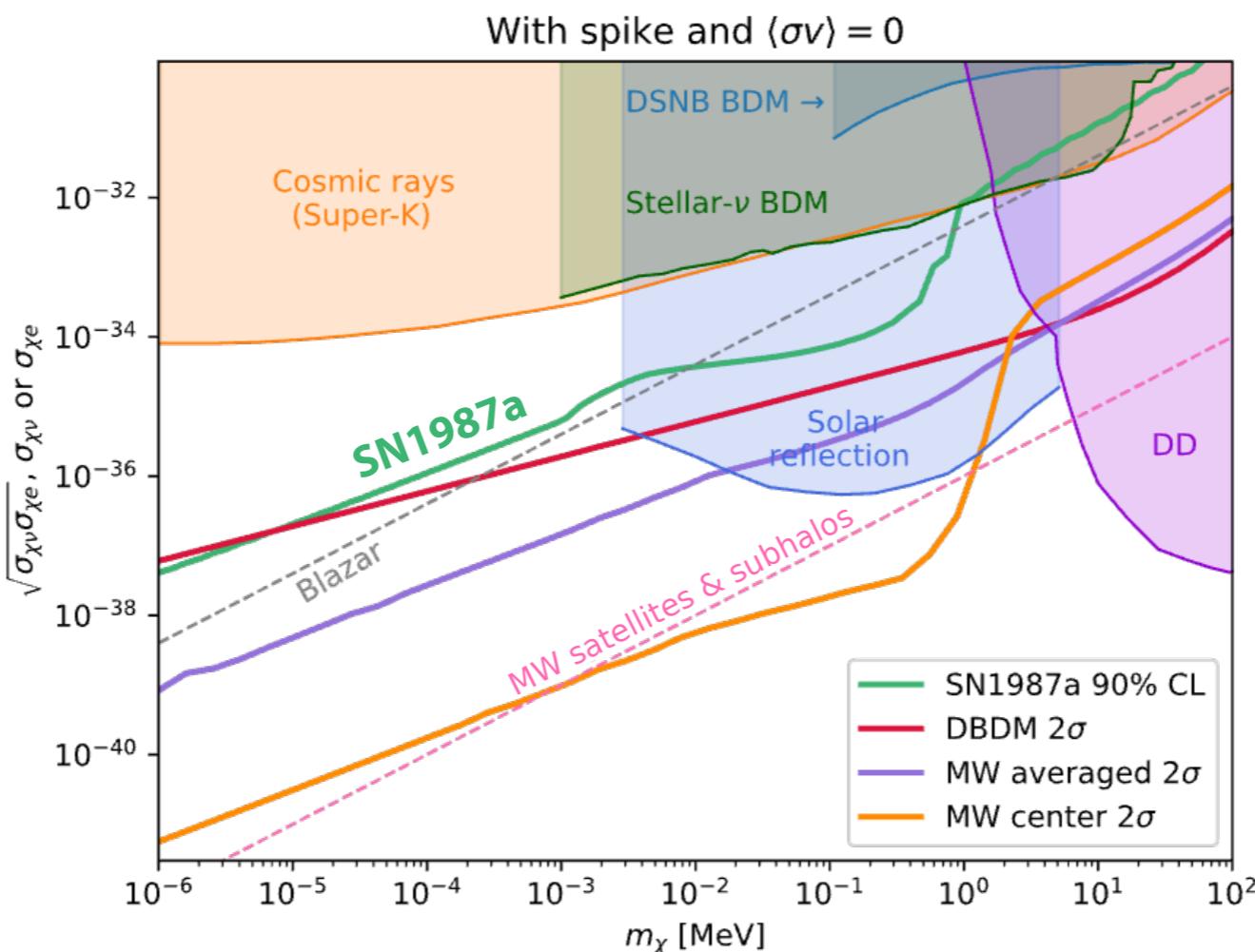
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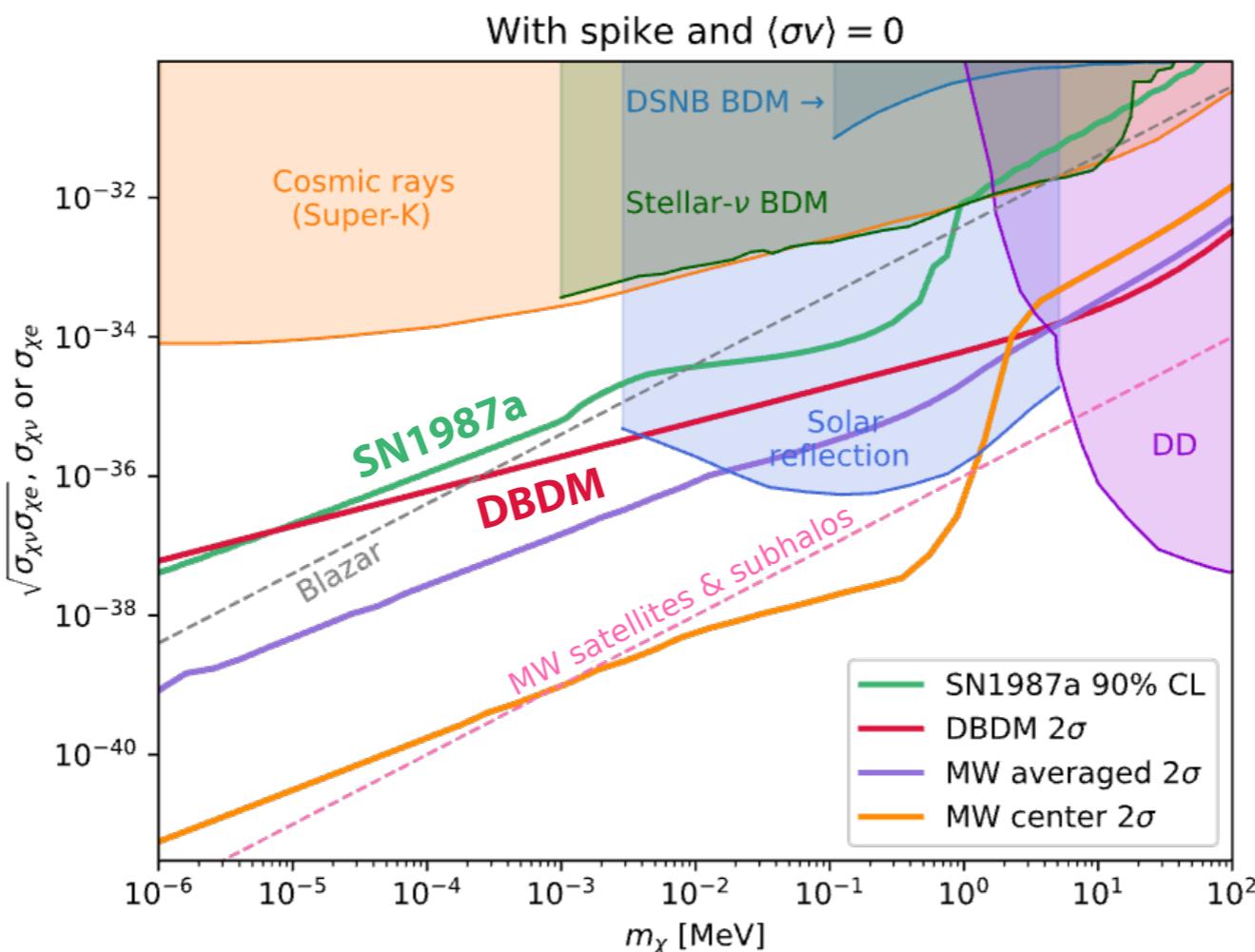
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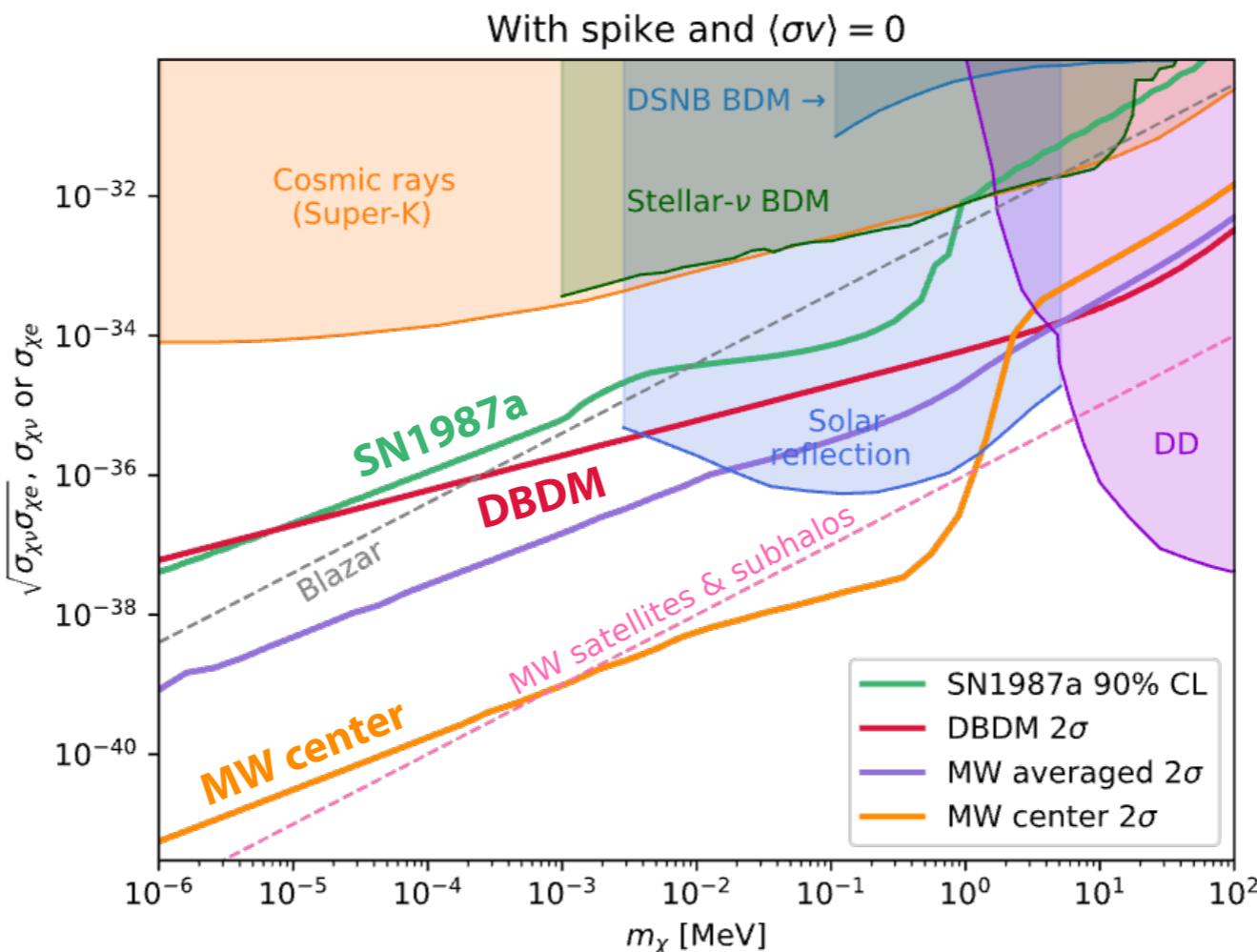
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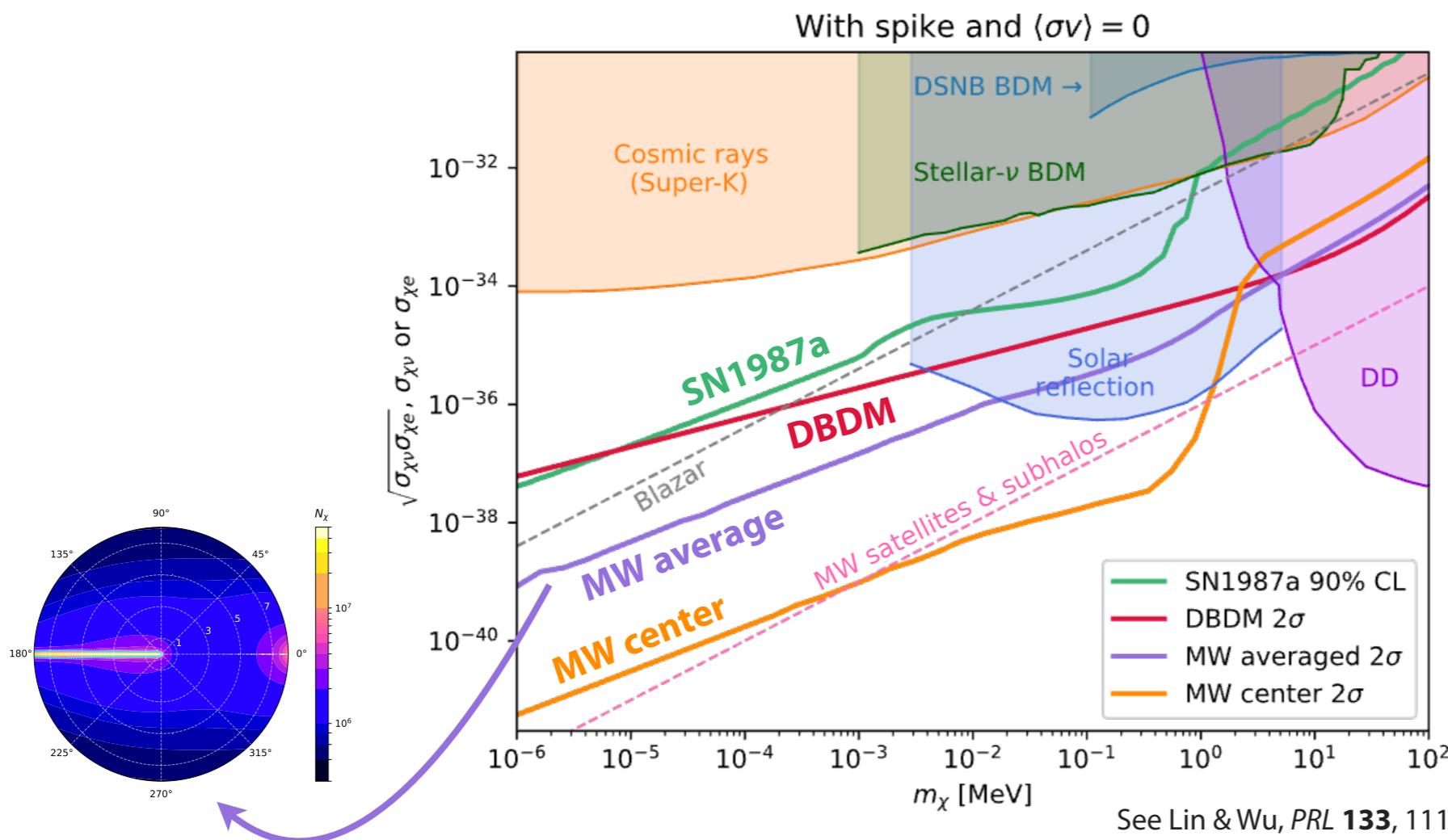
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Summary

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- SNv BDM offers a comprehensive and unified framework for probing light DM
- An innovative methodology to *directly measure DM mass* via *time-of-flight* is proposed
- Utilizing SNv BDM originating from SNe in galaxies throughout cosmic evolution forms a persistent and isotropic *diffuse BDM* (DBDM) flux
- DBDM is *robust against* uncertainties related to DM spikes, making it a reliable probe