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### Natural supersymmetry without cancellations in the quiver supersymmetric standard model

### Ken-ichi Okumura Iwate Medical University

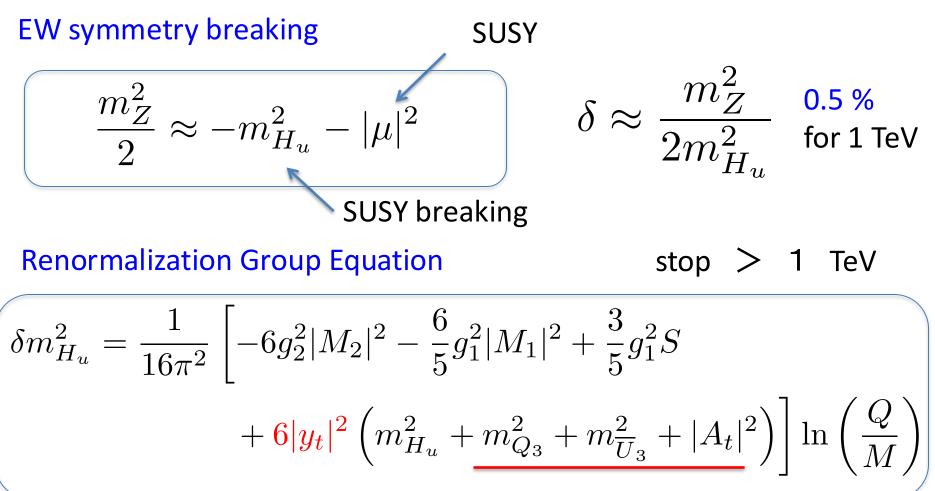


KO, JPS meeting March 2022 KO, Planck2023 June 2023 KO, Corfu2024 June 2024 KO in progress

### Introduction

- SUSY Standard Model looks suffering from the little hierarchy problem.
  - EW symmetry breaking (100 GeV) vs SUSY breaking (gluino 2 TeV, stop 1 TeV over)
  - fine-tuning of O(0.1) %
- Any attempt realizing natural multi-TeV supersymmetry would be welcome for future LHC run/FCC
- <u>We propose Quiver Supersymmetric Standard</u> <u>Model + "Sliding 3<sup>rd</sup> Generation"</u>

### Little SUSY hierarchy problem



Even a RG scale ambiguity can generates a few hundred GeV correction!

### Little SUSY hierarchy problem

### Lesson:

If we do not assume a miraculous cancellation, the Higgs field should not touch the SUSY breaking via gauge and Yukawa interactions until just before the gaugino, squark and slepton decouple.

$$\delta m_{H_u}^2 = \frac{1}{16\pi^2} \left[ -6g_2^2 |M_2|^2 - \frac{6}{5}g_1^2 |M_1|^2 + \frac{3}{5}g_1^2 S + \frac{6|y_t|^2}{(m_{H_u}^2 + m_{Q_3}^2 + m_{\overline{U}_3}^2 + |A_t|^2)} \right] \ln\left(\frac{Q}{M}\right)$$

0

4

Any such a model in the market ?

### Quiver (SUSY) Standard Model

C.Csaki, J.Erlich, C.Grojean, G.Kribs (2001) H-C. Cheng, D.E.Kaplan, M. Schmaltz, W.Skiba (2001)

$$\begin{array}{ccc} G_A \times G_{B(SM)} \to G_{SM} & (G_A \supset G_{SM}) & & & \\ \mbox{Gaugino Mass} & & & & & \\ M_A \neq 0 & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & &$$

**Deconstructed Gaugino mediation (Tree)** 

$$\frac{1}{2}M_A \overline{\lambda_A^c} \lambda_A = \frac{1}{2}M_A \frac{\overline{(g_A \lambda_H^c + g_B \lambda_{SM}^c)}(g_A \lambda_H + g_B \lambda_{SM})}{g_A^2 + g_B^2}$$
$$\langle \Sigma \rangle = \langle \overline{\Sigma} \rangle \approx M_A \quad \text{Decouple before the log corrections}$$

### Sequestering of the top Yukawa

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KO (2020) JPS meeting

Scalar mass

### Sequestering of the top Yukawa

### Sliding 3<sup>rd</sup> Generation

$$\mu_V = \mu' \cos \theta \qquad \lambda \langle X \rangle = \mu' \sin \theta$$

$$Q_H = \cos \theta \, Q + \sin \theta \, Q'$$
$$Q_{SM} = -\sin \theta \, Q + \cos \theta \, Q'$$

$$y_t^{SM} = y_t \sin^2 \theta$$
$$m_{Q_H}^2 = m_{Q'}^2 \sin^2 \theta \qquad m_{Q_{SM}}^2 = m_{Q'}^2 \cos^2 \theta$$

$$\mathcal{W}_{\Sigma} = \sum_{i=2,3} \left[ \lambda_i^A \operatorname{tr}(\Sigma_i A_i \overline{\Sigma}_i) + \lambda_i^S S_i \operatorname{tr}(\Sigma_i \overline{\Sigma}_i) \right] + \frac{1}{3!} \kappa_i^X S_i^3$$

+ spectator for the unification

Nontrivial Vacuum  $\ \langle \Sigma 
angle \neq 0 \ \langle X 
angle \neq 0 \$  due to the SUSY breaking

### **RG** running

Radiative "quiver" symmetry breaking

$$\mathcal{W}_{\Sigma} = \sum_{i=2,3} \left[ \lambda_i^A \operatorname{tr}(\Sigma_i A_i \overline{\Sigma}_i) + \lambda_i^S S \operatorname{tr}(\Sigma_i \overline{\Sigma}_i) \right] + \frac{1}{3!} \kappa^X S^3$$

$$\mathcal{L}_{SUSY} = m_{\Sigma}^2 \left( |\Sigma|^2 + |\overline{\Sigma}|^2 \right) + m_S^2 |S|^2 + (A \text{ terms})$$

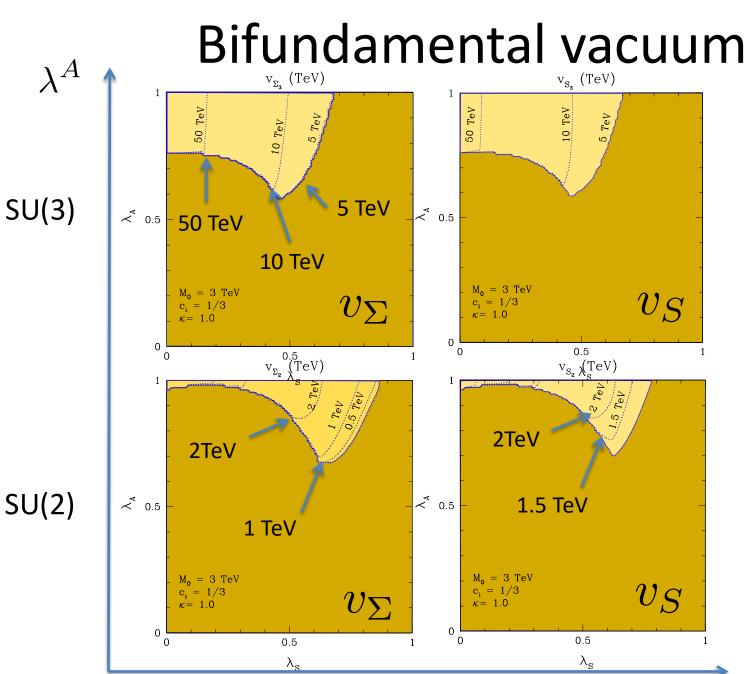
$$M_A = M_0$$

$$m_{\Sigma}^2 = c_{\Sigma} M_0^2$$

$$m_S^2 = c_S M_0^2$$

$$M_{SUSY}$$

$$M_{GUT} \log Q_{\text{renom}}$$



#### Non-trivial Vacuum via SUSY breaking effect

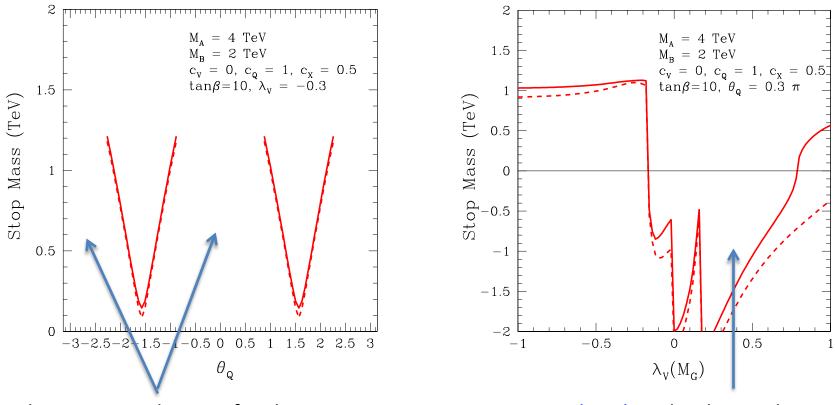
O(1) coupling is Required for the vacuum deeper than the origin

 $\lambda^{S}$ 

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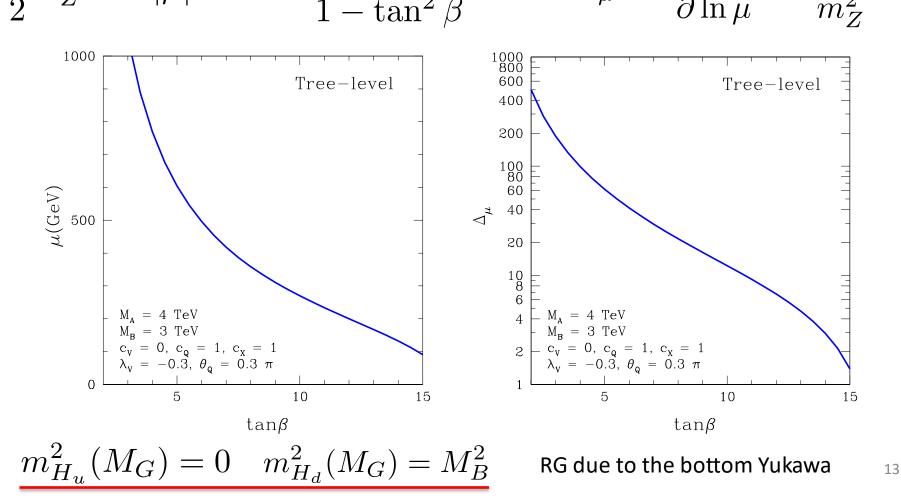
### Stop mass

It's not easy to lift the stop mass to multi-TeV



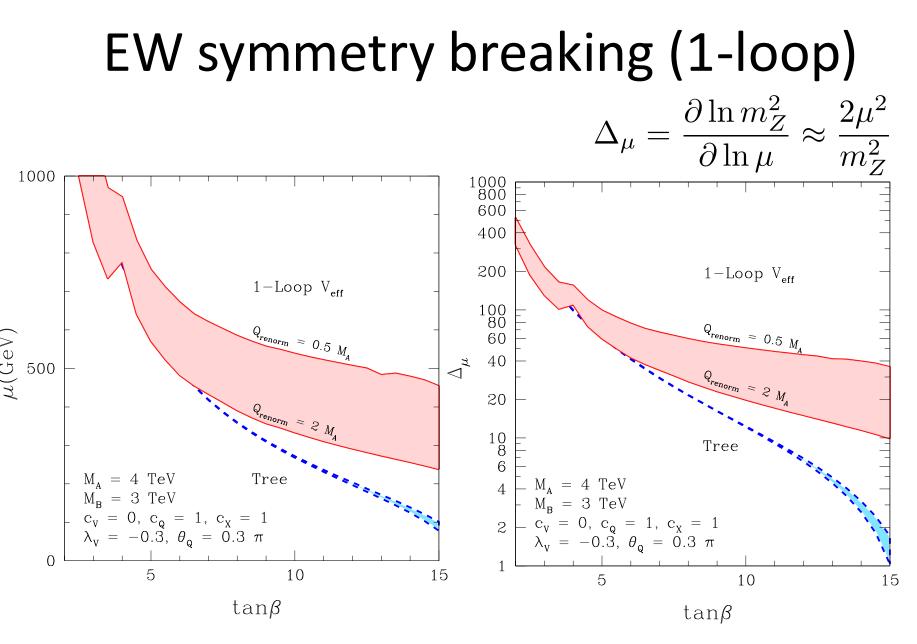
The SM top Yukawa is fixed and a small mixing hits the Landau pole SUSY breaking by the singlet F term generates mixing with  $\overline{Q}^*$  and reduce the stop mass.

## EW symmetry breaking (Tree-level) $\frac{1}{2}m_Z^2 = -|\mu|^2 - \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2 \beta}{1 - \tan^2 \beta} \quad \Delta_{\mu} = \frac{\partial \ln m_Z^2}{\partial \ln \mu} \approx \frac{2\mu^2}{m_Z^2}$



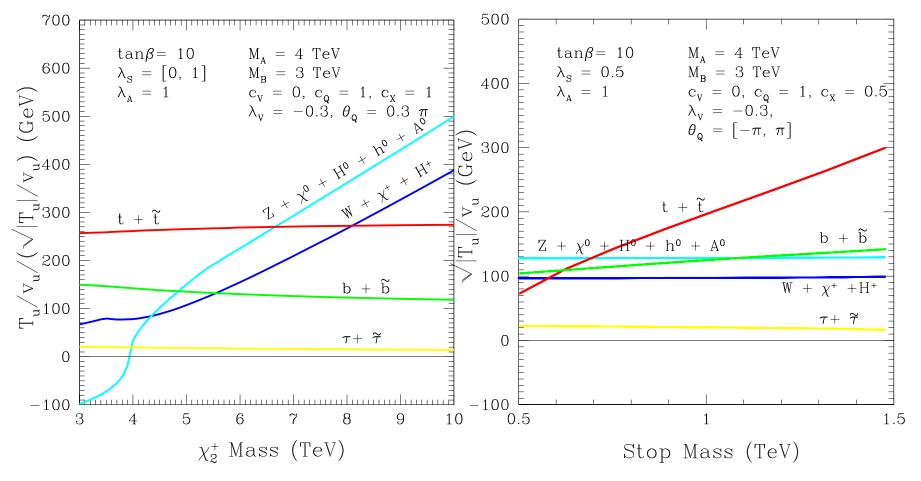
### Effective potential and Tadpole

$$\begin{aligned} V_{eff} &= \frac{1}{64\pi^2} Str M^4 \left( \ln \left( \frac{M^2}{Q_{\text{renorm}}^2} \right) - \frac{3}{2} \right) \\ T_{u,d} &= -\frac{\partial V_{eff}}{\partial H_{u,d}} \\ H_{u,d} &= -\frac{M^2}{2} \int \Phi \\ \frac{1}{2} m_Z^2 &= -|\mu|^2 - \frac{(m_{H_d}^2 - T_d/v_d) - (m_{H_u} - T_u/v_u) \tan^2 \beta}{1 - \tan^2 \beta} \\ &\approx T_u/v_u - m_{H_u}^2 - |\mu|^2 + \frac{m_{H_d}^2}{\tan^2 \beta} \end{aligned}$$



### Breakdown of the tadpole

 $T_u = -\frac{\partial V_{eff}}{\partial H_u}$ 



### Summary

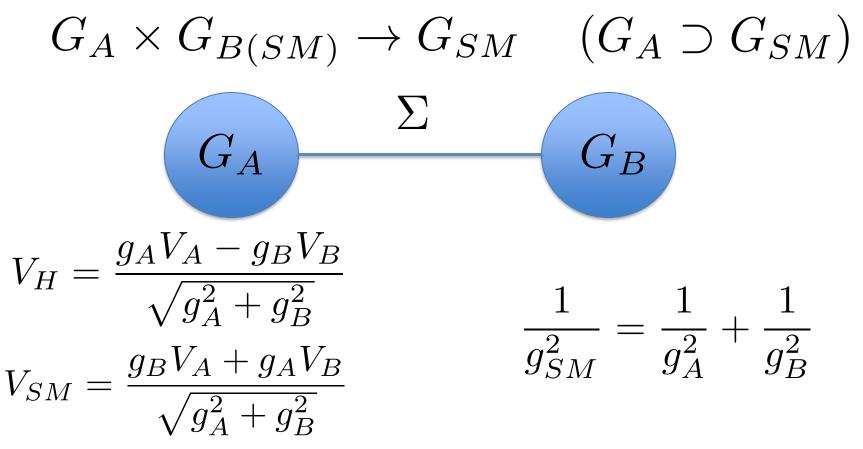
- We analysed a model with a natural SUSY little hierarchy combining the quiver supersymmetric SM and sliding 3rd generation.
- We can obtain required bifundamental vaccums with a relatively simple superpotential.
- Landau poles and non-holomorphic mixing due to SUSY breaking appears to be obstacles to lift the stop mass to multi-TeV.
- Tadpoles due to the multi-TeV gaugino are small.
- Tadpoles due to the stop dominate the cause of fine-tuing (<~3-5%), a factor improvement could have a strong impact.

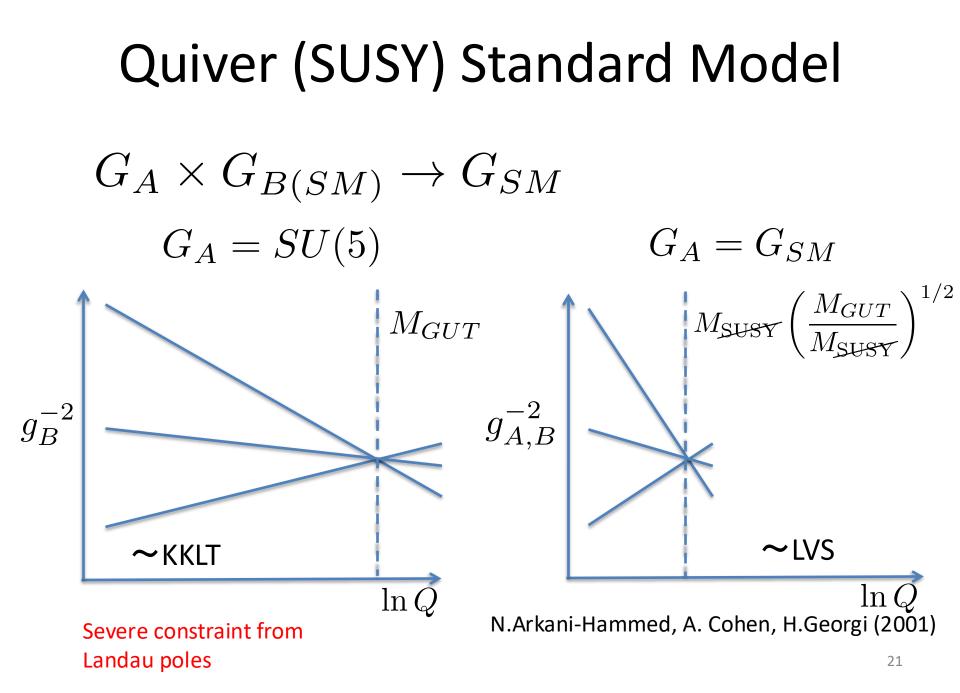
# Thank You

### **BACK UP**

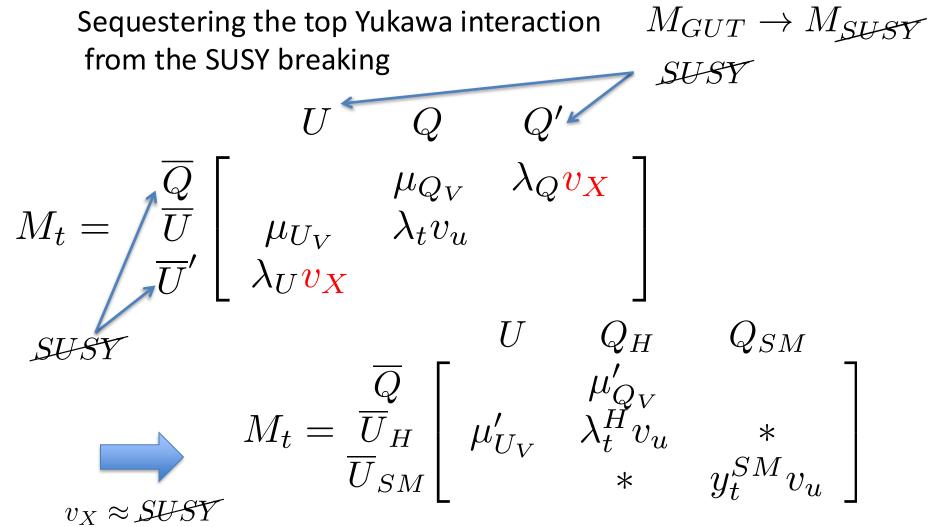
### Quiver (SUSY) Standard Model

C.Csaki, J.Erlich, C.Grojean, G.Kribs (2001) H-C. Cheng, D.E.Kaplan, M. Schmaltz, W.Skiba (2001) .....Many others





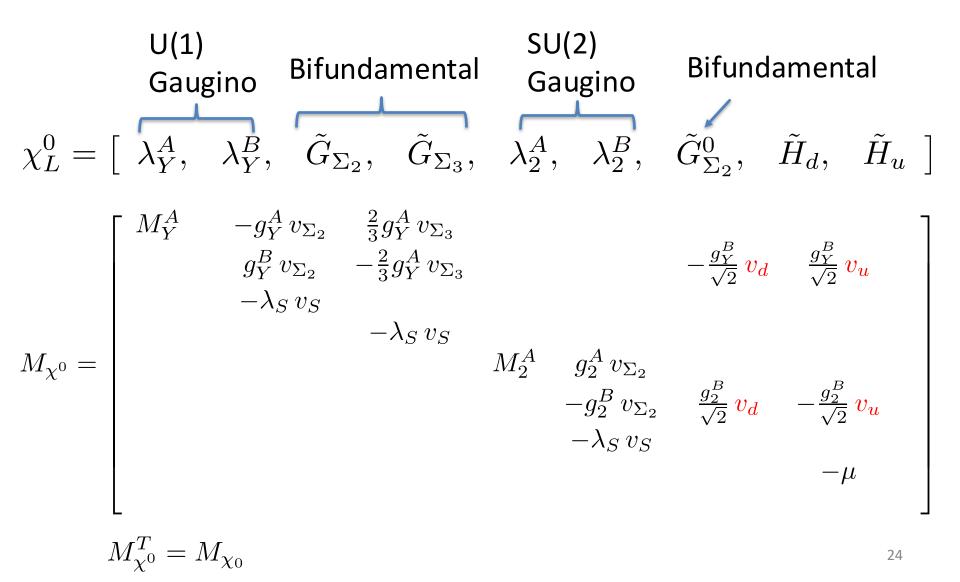
## Sliding 3<sup>rd</sup> Generation



### Effective potential and tadpole

$$\begin{split} T_{u,d} &= -\frac{\partial V_{eff}}{\partial H_{u,d}} \\ &= -\frac{1}{32\pi^2} \sum_{i} (-)^{2S_i} \frac{\partial \hat{M}_i^2}{\partial H_{u,d}} \hat{M}^2{}_i \left( \ln\left(\frac{\hat{M}_i^2}{Q_{\text{renorm}}^2}\right) - 1 \right) \\ & \frac{\partial \hat{M}_i^2}{\partial H_{u,d}} = \frac{\partial}{\partial H_{u,d}} \left( UMU^{\dagger} \right)_{ii} \\ &= \left( U \frac{\partial M}{\partial H_{u,d}} U^{\dagger} \right)_{ii} \end{split}$$

### Neutralino Mass



### **Chargino Mass**

SU(2) Gaugino Bifundamental  $\chi_L^- = \begin{bmatrix} \lambda_L^{A-}, & \lambda_L^{B-}, & \tilde{G}_L^-, & \tilde{H}_d^- \end{bmatrix}$  $\chi_B^- = \begin{bmatrix} \lambda_L^{A+c}, & \lambda_L^{B+c}, & \tilde{G}_L^{+c}, & \tilde{H}_u^{+c} \end{bmatrix}$ 

$$\begin{split} & \mathcal{Stop Mass} \\ \Psi_{\tilde{t}} = \left[ \begin{array}{ccc} Q', & \overline{Q}^{*}, & Q, & \overline{U}'^{*}, & U, & \overline{U}^{*} \end{array} \right] \\ & M_{\tilde{t}}^{2} = \left[ \begin{array}{ccc} m_{Q'}^{2} + \lambda_{Q}^{2} v_{X}^{2} & \lambda_{Q}(A_{Q}v_{X} & \mu_{Q}\lambda_{Q}v_{X} & \mu_{Q}\lambda_{Q}v_$$

