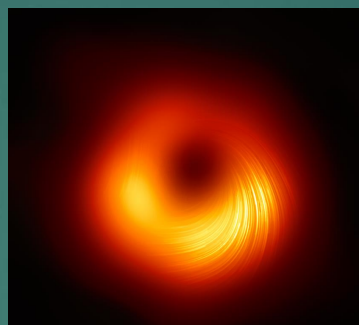


GRMHD Positron Applications from the Present and Primordial Universe



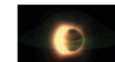
UTSA
The University of Texas
at San Antonio™



Event Horizon Telescope



Black Hole Initiative
Harvard University



CENTER FOR **ASTROPHYSICS**
HARVARD & SMITHSONIAN

RICHARD ANANTUA (UTSA/EHT)

10-9-2023

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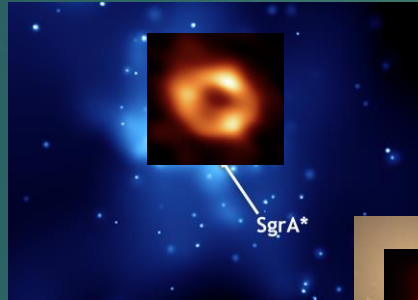
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RICE UNIVERSITY – TACOS

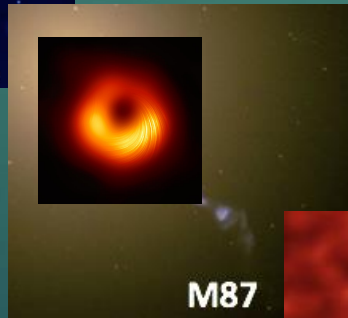
“Observing” JAB Systems

1. Start with general relativistic magnetohydrodynamic (GRMHD) simulation or semi-analytic model of jet (or outflow)/accretion flow/black hole (JAB) system
2. Convert GRMHD variables to radiation prescriptions for emission, absorption, polarization, particle acceleration and/or dissipation to emulate sources
3. Add “observer” viewing sources, e.g., Event Horizon Telescope (EHT) targets:

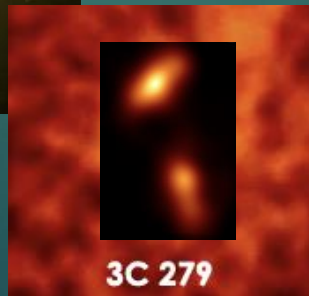
I. Sgr A*



II. M87

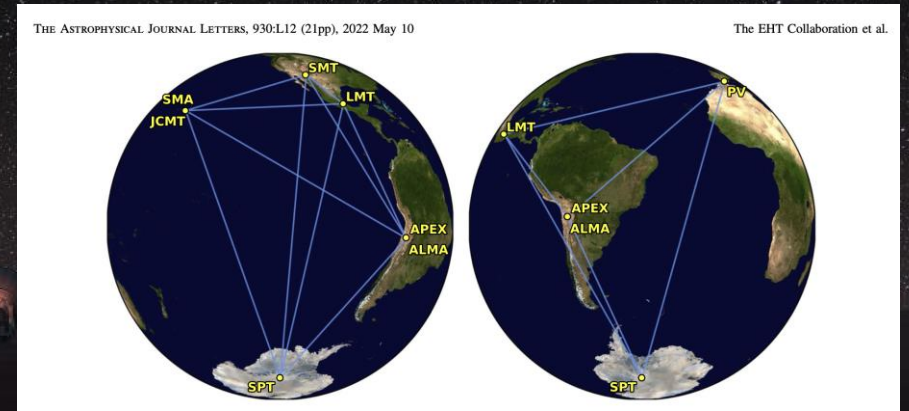


III. 3C 279



Application I.

Positron Modeling of M87*

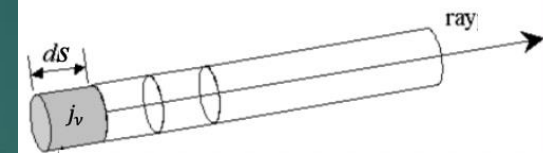


Zooming towards M87's Jet and Central Black Hole
Courtesy of European Southern Observatory (ESO)

Radiative Transfer

- ▶ Radiative transfer links source properties such as emissivity j_ν to observed radiation

$$\frac{dI_\nu}{ds} = j_\nu \Rightarrow I_\nu = \int_0^s j_\nu ds'$$



- ▶ Polarized radiative transfer equations w./absorption and Faraday effects (Dexter 2016):

$$\frac{d}{ds} \begin{bmatrix} I \\ Q \\ U \\ V \end{bmatrix} = \begin{bmatrix} j_I \\ j_Q \\ j_U \\ j_V \end{bmatrix} - \begin{bmatrix} \chi_I & \chi_Q & \chi_U & \chi_V \\ \chi_Q & \chi_I & \rho_V & \rho_U \\ \chi_U & -\rho_V & \chi_I & \rho_Q \\ \chi_V & -\rho_U & -\rho_Q & \chi_I \end{bmatrix} \begin{bmatrix} I \\ Q \\ U \\ V \end{bmatrix}$$

For synchrotron radiation

$$j_I \rightarrow j_\nu \sim P_e F(\vec{B}, \nu), \quad P_e \sim \int \gamma N(\gamma) d\gamma$$

- ▶ Emitting particle distribution functions $N(\gamma)$:

- ▶ Thermal

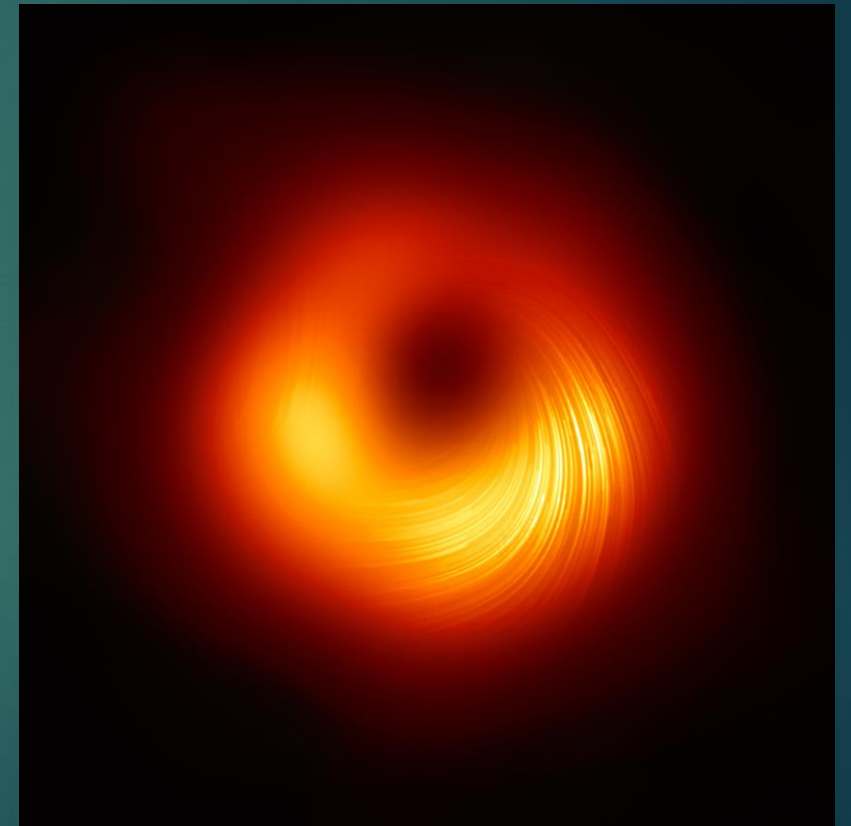
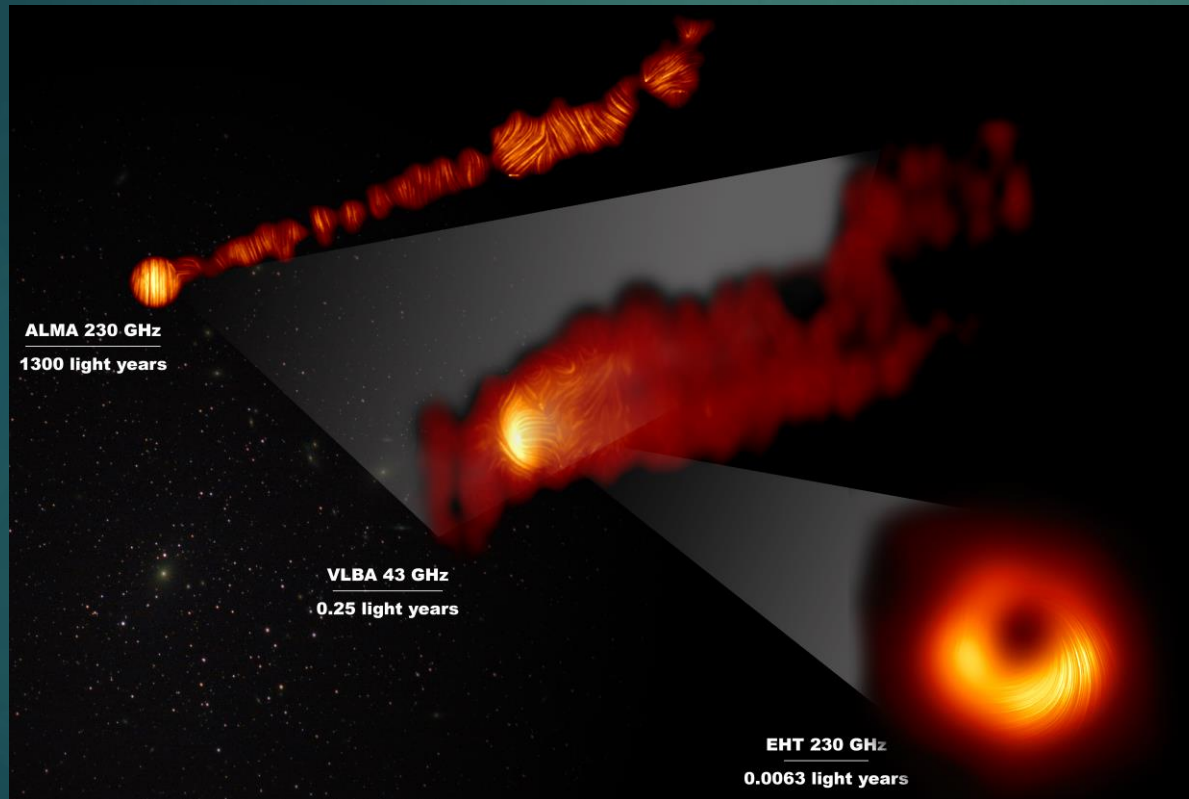
$$N(\gamma) \sim \exp(-\gamma/\theta_e)$$

- ▶ Power law

$$N(\gamma) \sim \gamma^{-p}$$

Polarized M87 Observations

- ▶ M87 polarization has been observed by ALMA, VLBA and EHT



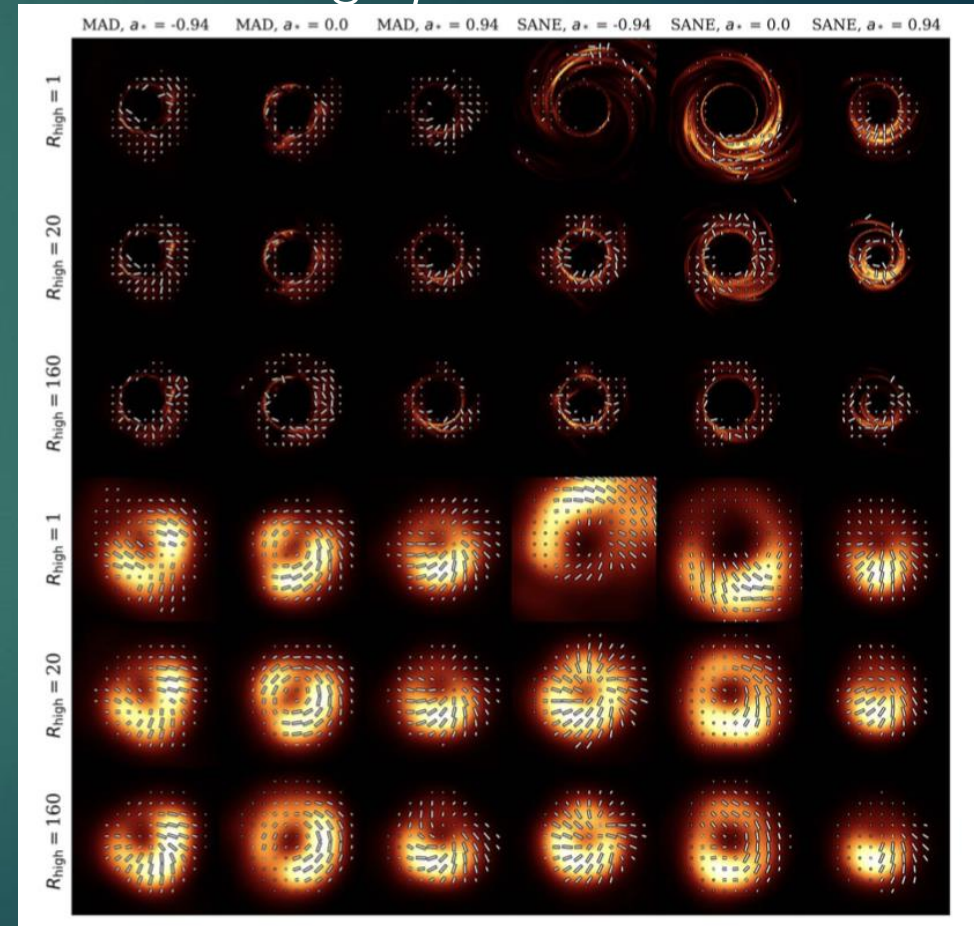
EHT M87 Simulation Library

- ▶ Turbulent heating physics (Howes 2010): Relativistic electrons preferentially heated at low $\beta = \frac{P_g}{P_B}$; protons and other ions at high β , relativistically cold plasma
- ▶ R-Beta Model (EHTC Papers I-VIII)

$$R = \frac{T_i}{T_e} = \frac{1}{1 + \beta^2} R_{\text{low}} + \frac{\beta^2}{1 + \beta^2} R_{\text{high}}$$

- ▶ Using the R-Beta Model (w./ $R_{\text{low}} = 1$) and SANE and MAD simulations (w./ $\frac{a}{M} = -0.94, 0, 0.94$):
 - ▶ Increasing spin magnitude increases asymmetry
 - ▶ MAD has mostly spiral EVPA/vertical implied B-field
 - ▶ SANE has mostly radial EVPA/toroidal implied B-field

EHTC Paper VIII



Emission Prescriptions with Magnetic Energy Conversion

- ▶ Constant Electron Beta (β_e) Model – Magnetic-to-Particle Energy Conversion:

$$\beta_e = \frac{P_e}{P_B} = \frac{(\gamma_e - 1)u_e}{B^2/2} \Rightarrow u_e = \rho T_e = \frac{1}{(\gamma_e - 1)} \beta_e \frac{B^2}{2}$$

Equipartition for
 $P_e \sim P_B$

- ▶ Magnetic Bias Model

$$P_e = K_n \left(\frac{b}{\sqrt{2}} \right)^{2n}, \quad K_n = K_1 \frac{\langle \frac{b^2}{2} \rangle}{\langle \left(\frac{b}{\sqrt{2}} \right)^{2n} \rangle}, \quad K_1 = 1$$

M87 Simulation Assumptions and Fluid Equations

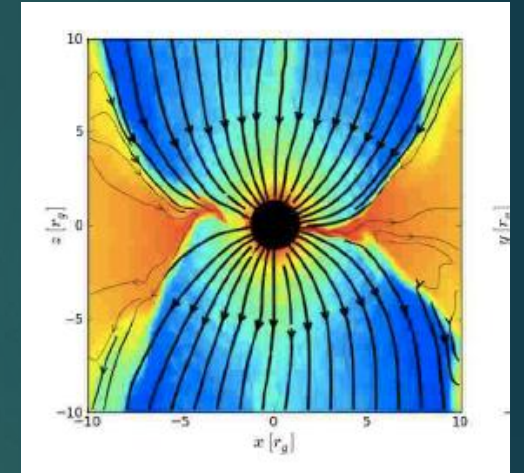
- ▶ Start with a HARM GRMHD simulation assuming:
 - ▶ Geometrically thick disk
 - ▶ Magnetically arrested disk
 - ▶ Jet power derived from flux threading black hole of mass M and spin $a/M=0.92$

- ▶ Mass conservation $\nabla_{\mu}(\rho u^{\mu}) = 0$

- ▶ Energy-momentum conservation

$$\nabla_{\mu} T^{\mu\nu} = 0$$

$$T_{\nu}^{\mu} = (\rho + u_g + P_g + b^2)u^{\mu}u_{\nu} + (P_g + b^2/2)\delta_{\nu}^{\mu} - b^{\mu}b_{\nu}$$



McKinney, Tchekhovskoy and Blandford
MNRAS **423** 3083 (2012)

$$r_g = M = \frac{GM_{\text{BH}}}{c^2} = 5.0 \times 10^{12} \text{m}$$

- ▶ Assume power law coefficients for radiative transfer in jet models

Connecting with Observations: M87 43 GHz Radio Map Time Series vs. Current Density Model

- Current density (j) model based on having particles accelerated at current layers

$$j_\nu \propto \tilde{P}_e \propto j^2$$

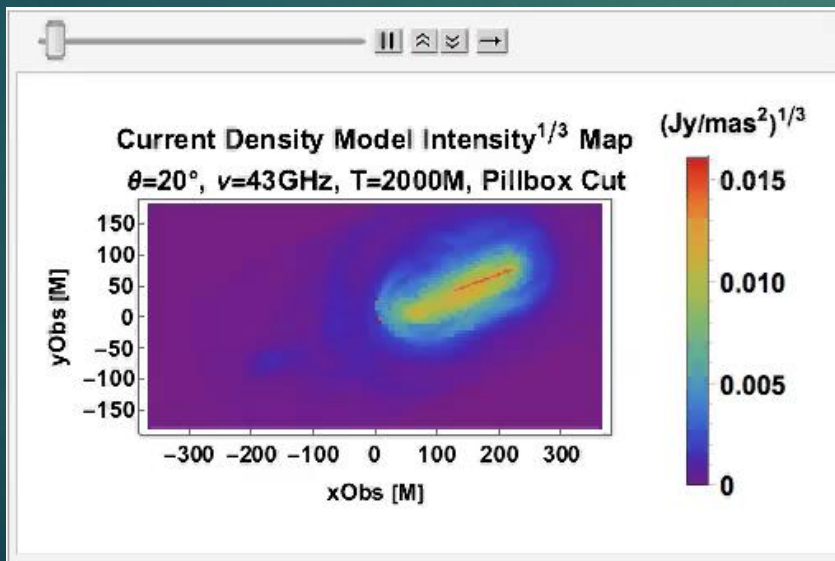
$(\theta_{\text{Obs}}, \Phi_{\text{Obs}}) = (20^\circ, 0^\circ)$, $T_{\text{Obs}} = 2000\text{M}, 2056\text{M}, \dots, 2560\text{M}$

Emissivity: Current Density Model

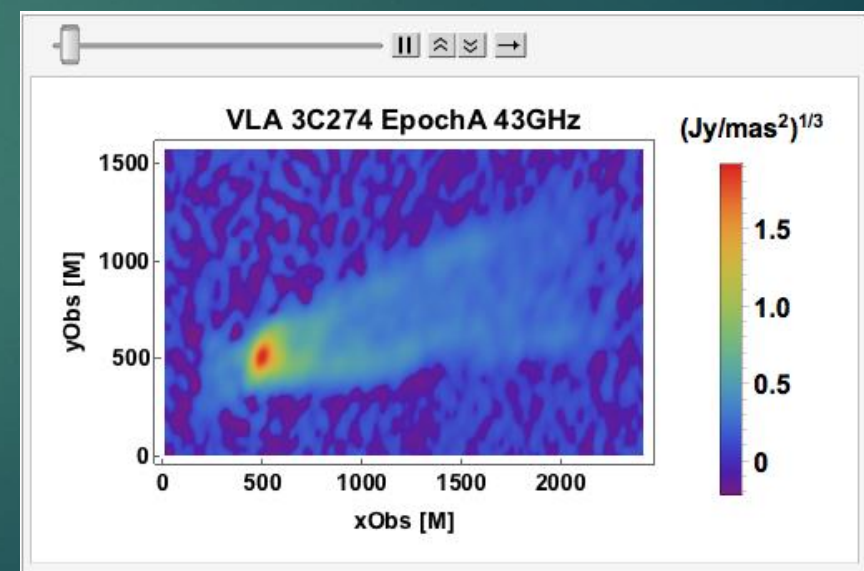
Disk subtraction: $|z| > 35\text{M}$

$L_{\text{JSq}} = 1\text{e}4 \text{ M}$

M87 43GHz (7mm) VLA maps
21-Day frame rate, Epochs A,B,D-L



Anantua, Blandford and
Tchekhovskoy (2018) Galaxies, 6, 31



Courtesy of Craig Walker (NRAO), Chun Ly (UCLA), Bill Junor (Los Alamos), and Phil Hardee (U. Alabama)

Stationary Axisymmetric Self-Similar Semi-Analytic Jet Model

- Assume stationary ($d/dt=0$), axisymmetric ($d/d\phi = 0$) parabolic jet with self-similarity parameter $\xi = s^2/z$
- Use force-free $\rho\vec{E} + \vec{j} \times \vec{B} = \vec{0}$ jet region of a HARM simulation
 - Relate GRMHD variables to fieldline angular speed $\Omega_B(\xi)$ and flux $\Phi_B(\xi)$ connected to horizon

$$I = -2\Omega_B \xi \Phi' \quad \begin{pmatrix} B_s \\ B_\phi \\ B_z \end{pmatrix} = \begin{pmatrix} -\frac{1}{2\pi s} \frac{\partial \Phi}{\partial z} \\ \frac{I}{2\pi s} \\ \frac{1}{2\pi s} \frac{\partial \Phi}{\partial s} \end{pmatrix} \quad \begin{pmatrix} v_s \\ v_\phi \\ v_z \end{pmatrix} = \begin{pmatrix} \frac{s}{2z} v_z \\ s\Omega_B(1-v_z) \\ v_{z0} e^{-0.001s^8/z^4} \end{pmatrix} \quad \vec{E} = \vec{B} \times (\hat{\Omega}_B \times \vec{r})$$

and at $z=50M$, derive fitting forms for flux threading the horizon

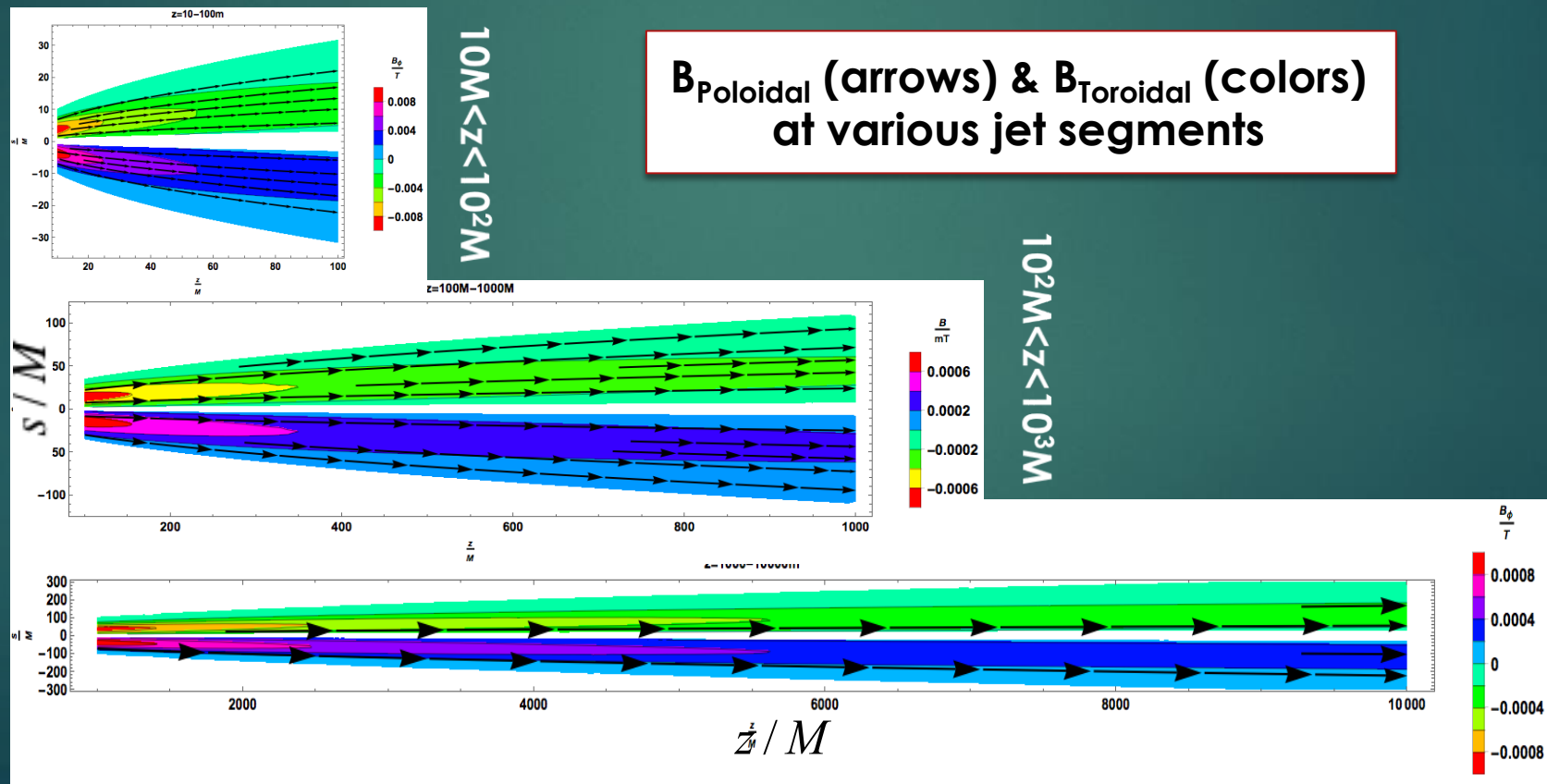
$$\Phi_B(\xi) = \tanh[-0.3\xi]$$

and fieldline angular speed

$$\Omega_B(\xi) = 0.15 \exp[-0.3\xi^2]$$

Semi-Analytic Jet Model

- ▶ Assume stationary ($d/dt=0$), axisymmetric ($d/d\phi = 0$) parabolic jet with self-similarity based on force-free $\rho\vec{E} + \vec{j} \times \vec{B} = \vec{0}$ region of HARM jet simulation
- ▶ Use self-similarity to obtain GRMHD flow on different scales



Positron Physics in JAB Systems

▶ Positrons can be created in AGN jet/accretion flow/black hole (JAB) systems via:

▶ Photon-photon interactions: $\gamma\gamma \rightarrow e^-e^+$ (Breit-Wheeler Pair Production):

▶ Electrons in Compton clouds of disk photons may scatter soft photons to MeV energies, which photons undergo photon-photon interactions resulting in e-e+ pairs (Laurent & Titarchuk 2018) in jet funnel walls

▶ Funnel wall positron number densities predicted for Sgr A* ($n_{\pm} = 10^{-8} \text{ cm}^{-3}$) and M87 ($n_{\pm} = 10 \text{ cm}^{-3}$) walls (Moscibrodzka et al. 2011)

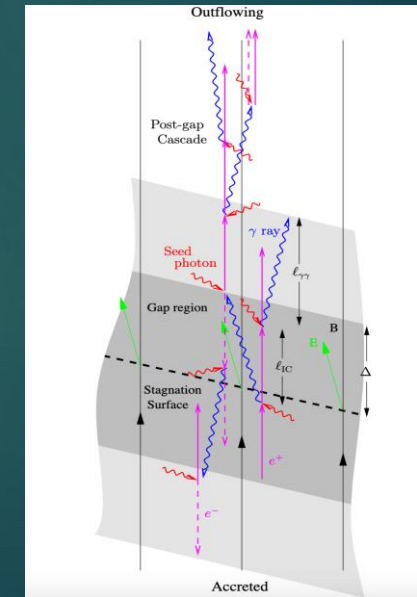
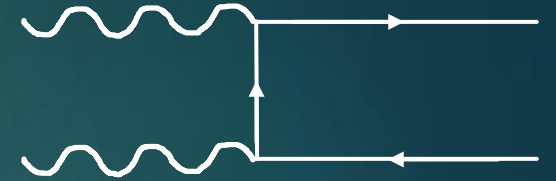
▶ Spark gap processes

▶ Jets in AGN generically host a spark gap in which plasma moves away from the black hole beyond the outer light cylinder but must fall toward the central black hole within a stagnation surface at smaller radii from the hole (Levinson & Segev 2017)

▶ Positron effects can be included by in GRMHD postprocessors by generalizing:

▶ Particle number density $n = n_i + n_{e+} + n_{e-}$ (Anantua et al. 2020a) and:

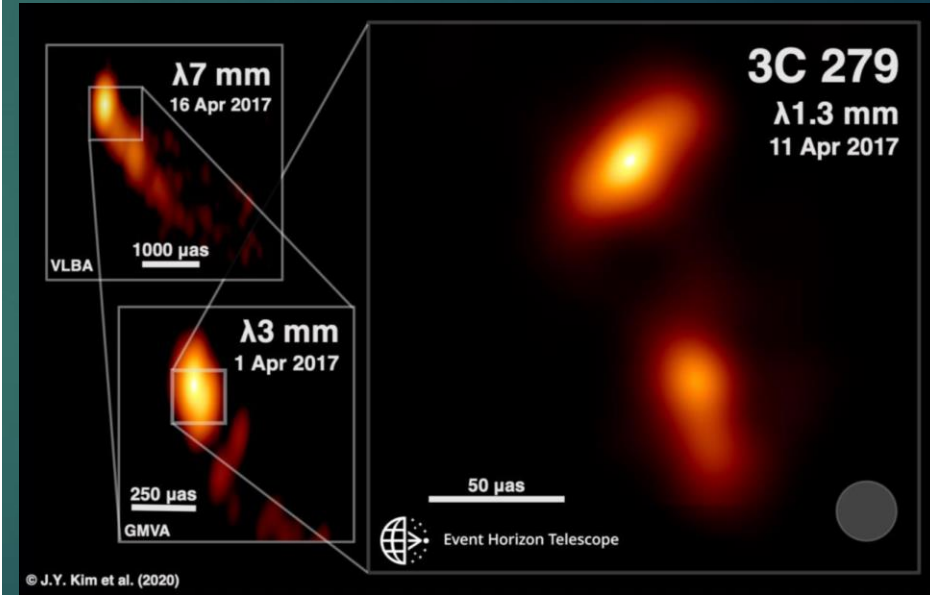
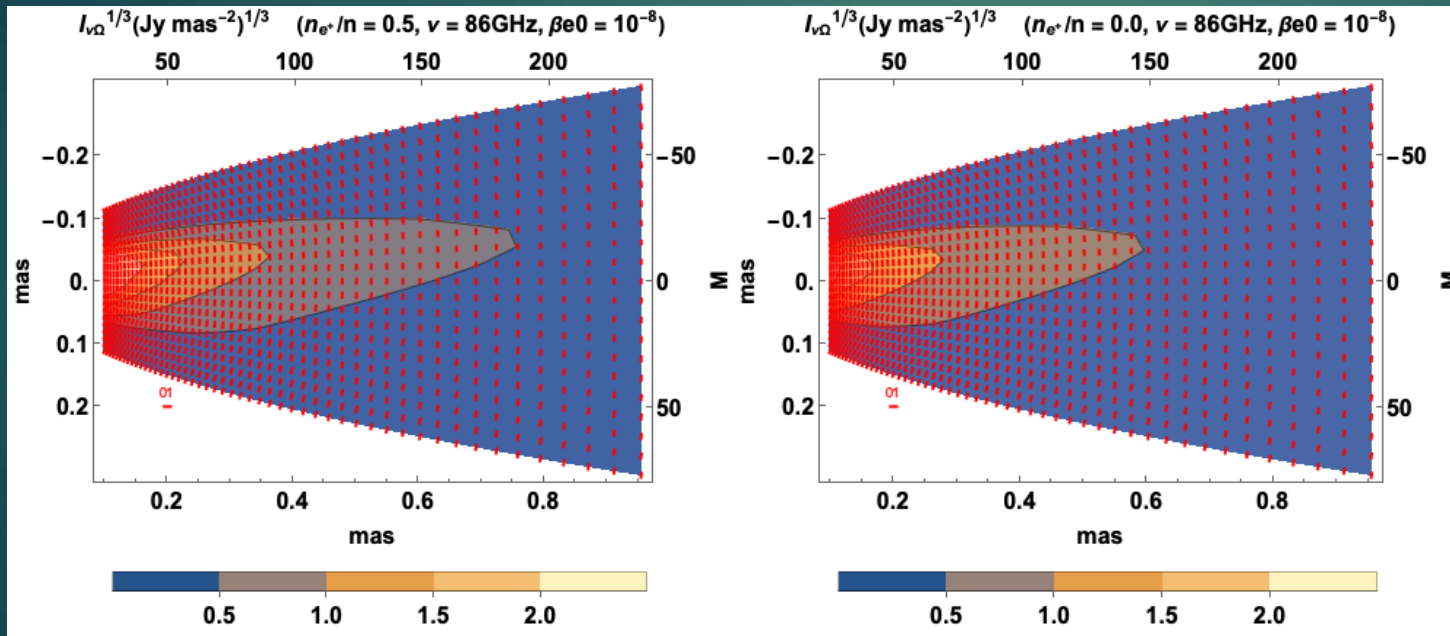
$$j_{I,Q,U} \rightarrow j_{I,Q,U} \left(1 + \frac{n_{e+}}{n_{e-}} \right), \quad j_V \rightarrow j_V \left(1 - \frac{n_{e+}}{n_{e-}} \right) \quad \chi_{I,Q,U} \rightarrow \chi_{I,Q,U} \left(1 + \frac{n_{e+}}{n_{e-}} \right), \quad \chi_V \rightarrow \chi_V \left(1 - \frac{n_{e+}}{n_{e-}} \right) \quad \rho_{Q,U} \rightarrow \rho_{Q,U} \left(1 + \frac{n_{e+}}{n_{e-}} \right), \quad \rho_V \rightarrow \rho_V \left(1 - \frac{n_{e+}}{n_{e-}} \right)$$



Broderick and Tchekhovskoy (2015) ApJ, 801, 1

Synchrotron Intensity Asymmetry with Positrons

- ▶ In the $\beta_{e0} = 10^{-8}$ Constant Electron Beta model ($j_\nu \propto P_e P_B^{\frac{1+\alpha}{2}} \nu^{-\alpha} \propto \beta_{e0} P_B^{\frac{3+\alpha}{2}} \nu^{-\alpha}$) with positrons, at 86 GHz, as ion content increases from 0% to 100% of positive charge carriers (or n_{e^+}/n goes from 0.5 \rightarrow 0), the intensity map
 - ▶ Becomes inwardly core shifted
 - ▶ Remains bilaterally asymmetric



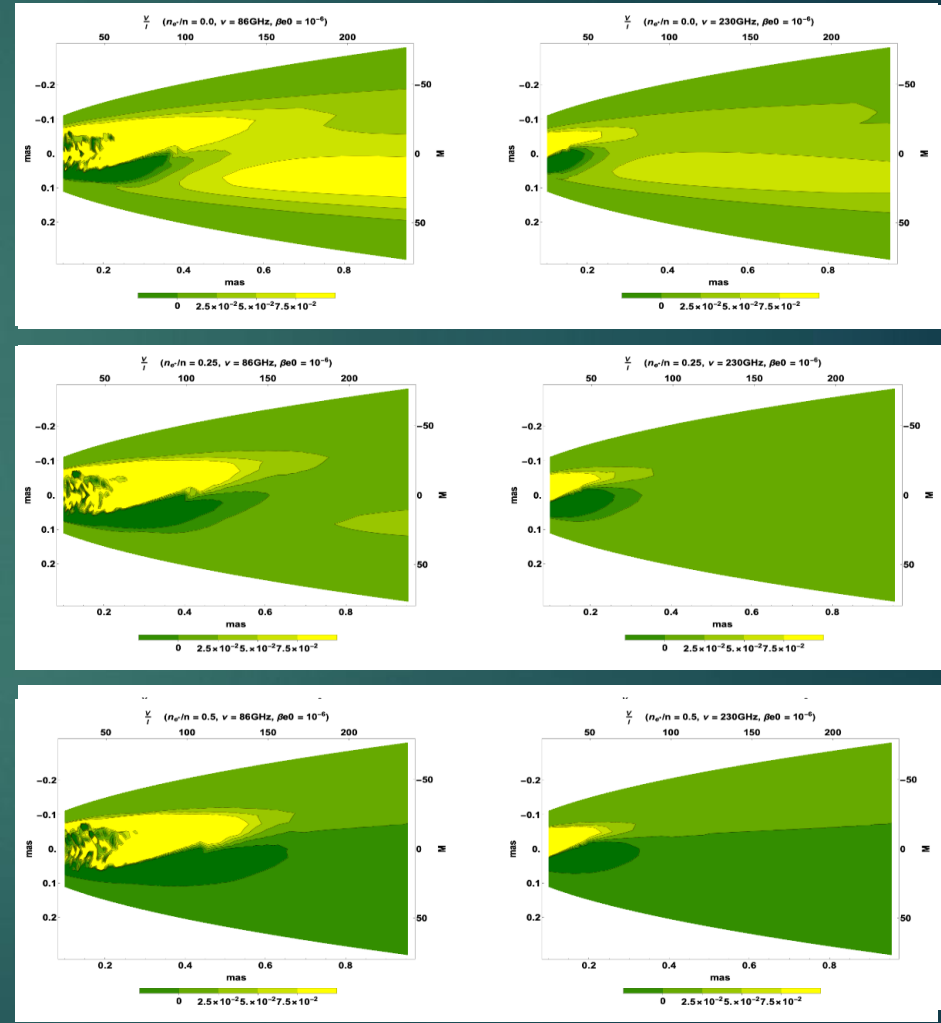
- ▶ Our fiducial $\gamma_{\min} = 10$ and $\gamma_{\max} = \infty$

Degree of Circular Polarization

$$\beta_{e0} = 10^{-6}$$

- ▶ For the parameter space $86\text{GHz} \leq \nu \leq 230\text{GHz}$, $0 \leq n_{e+}/n \leq 0.5$, $10^{-10} \leq \beta_{e0} \leq 10^{-6}$, circular polarization degree V/I
 - ▶ Tends to increase for ionic plasma at lower frequencies and higher β_{e0}
 - ▶ Ranges from 0 to $O(10^{-3})$
 - ▶ Is maximized near the black hole and along the jet axis, as seen for $\beta_{e0} = 10^{-8}$, except for the most leptonic plasma
- ▶ Symmetric e^-e^+ plasma virtually destroys V/I , despite minor Faraday conversion

Anantua, Emami, Loeb and Chael
ApJ 896 30 (2020)



86 GHz

230 GHz

0.0

0.25

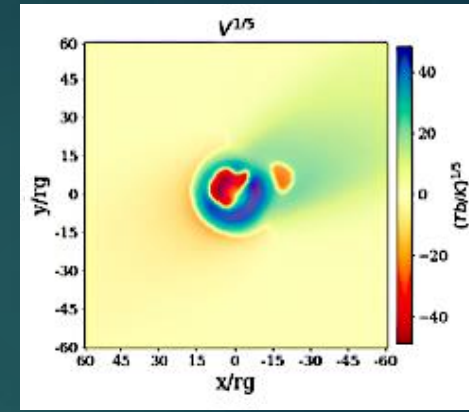
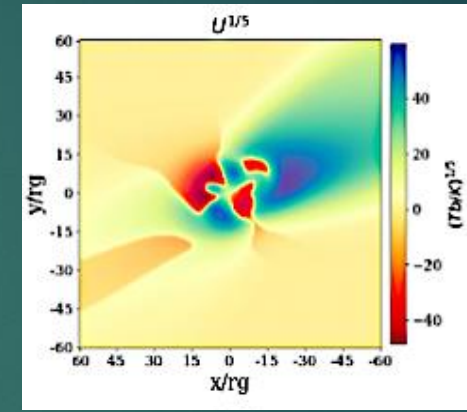
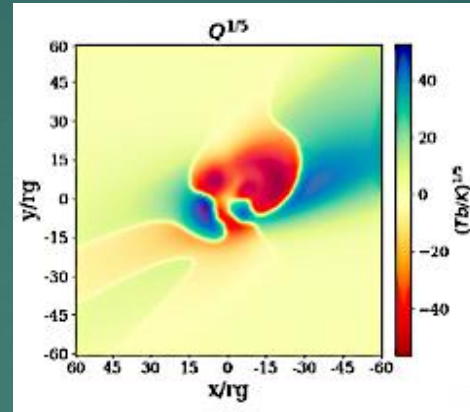
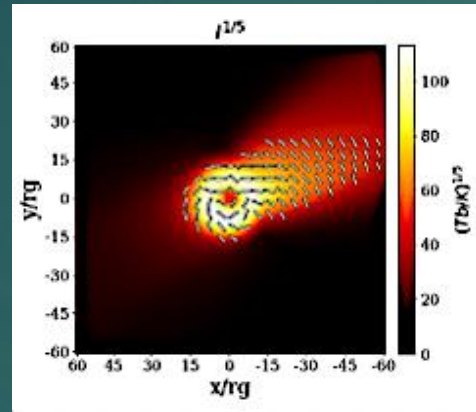
0.5

n_{e+}/n_i

ν

Near-Horizon Jet Model Stokes Maps: M87

- ▶ Constant Electron Beta Model ($j_\nu \propto P_e P_B^{\frac{1+\alpha}{2}}$), $\nu = 230$ GHz

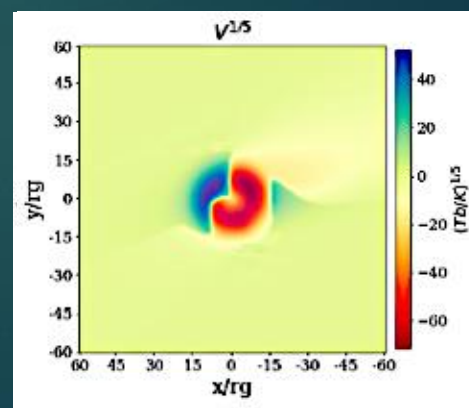
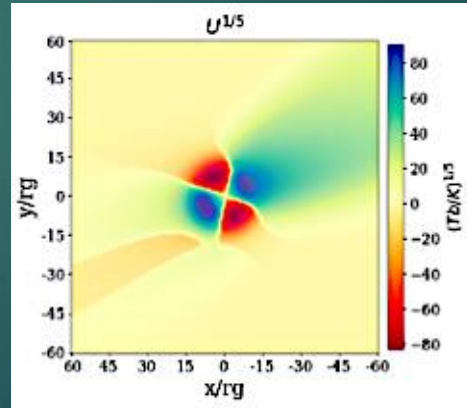
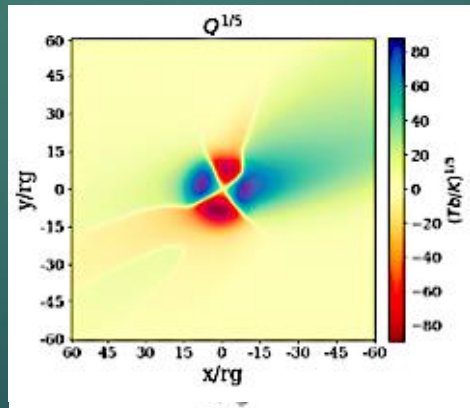
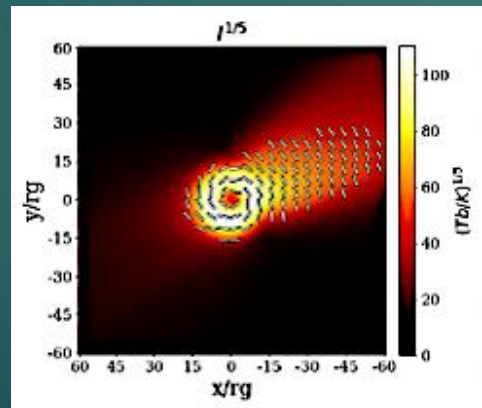


$$(P_e)_{\text{Beta}} = \beta_{e0} P_B,$$

$$\beta_{e0} = 10^{-4}, 10^{-2}, \dots$$

$$\beta_{e0} = 10^{-2}, f_{\text{Pos}} = 0$$

$$0 \leq f_{\text{Pos}} = \frac{n_{e+}}{n_{e-}} \leq 1$$



$$\beta_{e0} = 10^{-2}, f_{\text{Pos}} = 1$$

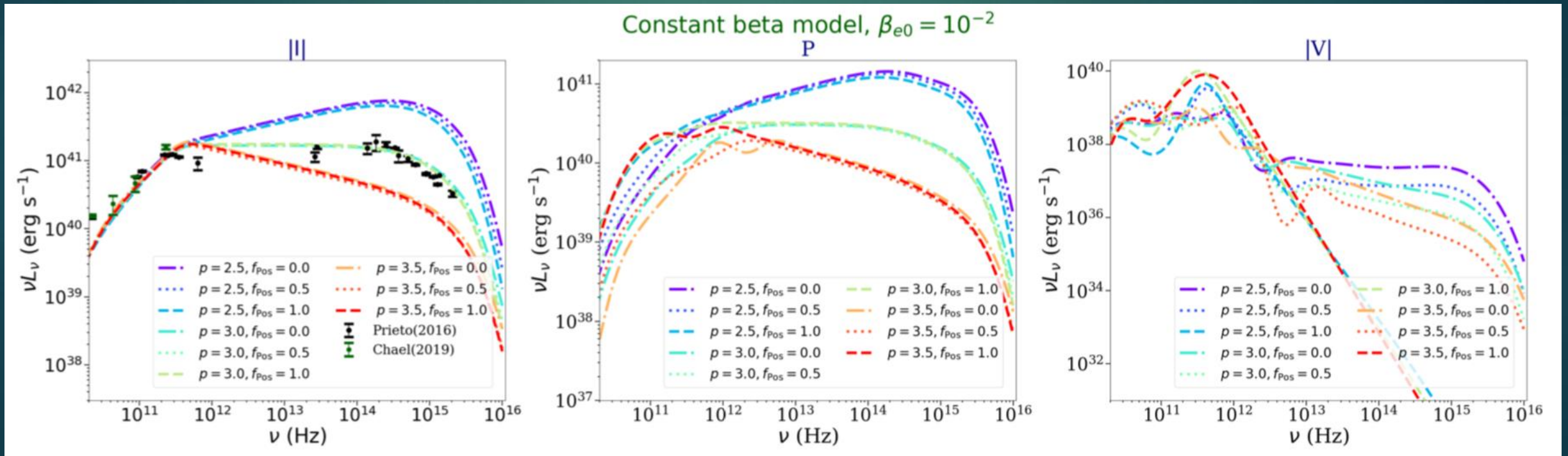
Near-Horizon Jet Model Polarized Spectra: M87

17

▶ Constant Electron Beta Model polarized spectral decomposition

- ▶ I insensitive to f_{pos}
- ▶ P sensitive to f_{pos} at low ν
- ▶ V sensitive to f_{pos} since

$$j_V, \rho_V \propto (1 - f_{\text{pos}}), \rho_{Q,U} \propto (1 + f_{\text{pos}})$$

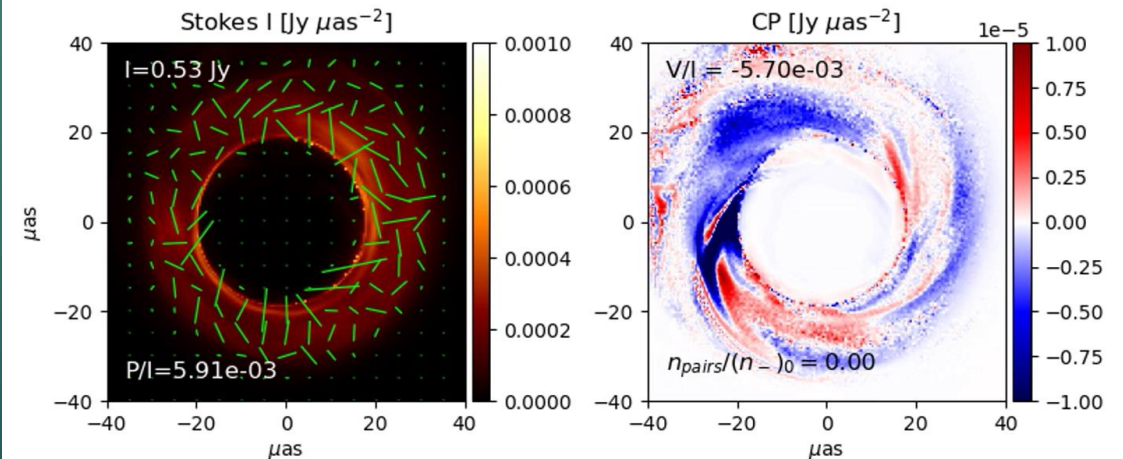
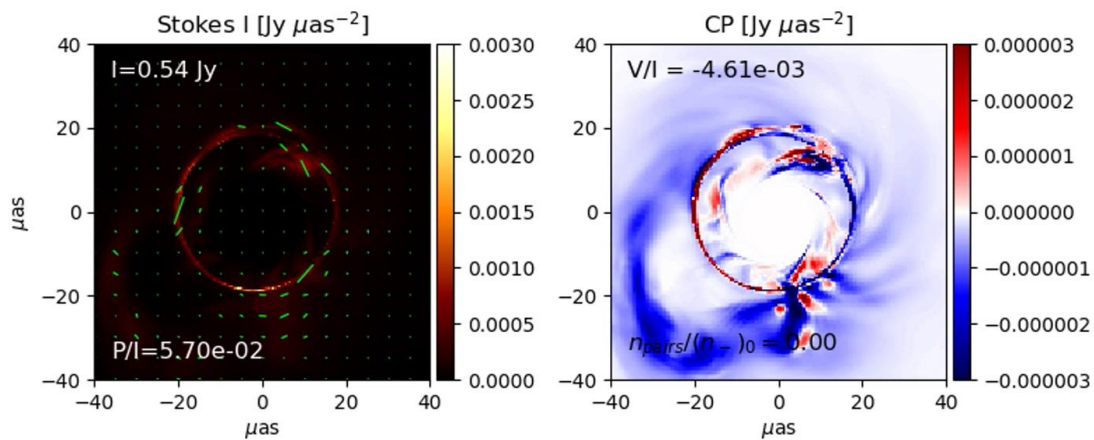


Positron Effects on “Observing” GRMHD Simulations: MAD vs. SANE

- ▶ Using a HARM GRMHD simulation and adding e^+/e^- pairs so $n = n_p + (n_{e^-})_0 + n_{\text{pairs}}$ in ray tracing at 230 GHz results in
 - ▶ Magnetically Arrested Disk (MAD) simulations with decreasing V/I with increasing $n_{e^+} = \frac{n_{\text{pairs}}}{2}$ due to positrons cancelling intrinsic circular polarization
 - ▶ MAD simulation models have lower Faraday depth than Standard and Normal Evolution (SANE), resulting in slower rates of EVPA rotation

MAD $R_{\text{high}}=20$, $\alpha/M = -0.5$

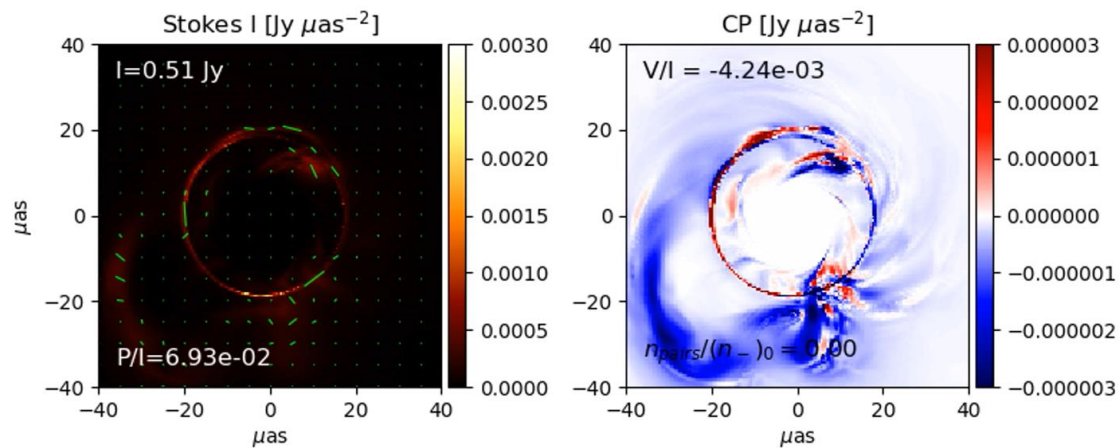
SANE $R_{\text{high}}=20$, $\alpha/M = -0.5$



Positron Effects on “Observing” GRMHD Simulations: Critical Beta Model

- ▶ Using a HARM GRMHD simulation and adding e⁺/e⁻ pairs so with Critical Beta Model $\frac{T_e}{T_p + T_e} = f \text{Exp}[-\beta/\beta_c]$ results in $n = n_p + (n_{e^-})_0 + n_{\text{pairs}}$ in ray tracing at 230 GHz
 - ▶ Magnetically Arrested Disk (MAD) simulations with decreasing V/I with increasing $n_{e^+} = \frac{n_{\text{pairs}}}{2}$ due to positrons cancelling intrinsic circular polarization
 - ▶ MAD simulation models have lower Faraday depth than Standard and Normal Evolution (SANE), resulting in slower rates of EVPA rotation

$$\text{MAD } f = 0.5, \beta_{\text{crit}} = 1, a/M = -0.5$$



Comparison of AGN with GRMHD Simulations. II: M87 15

Table 3. Linear polarization $|m|_{\text{net}}$ and $\langle |m| \rangle$ for fiducial models at $T = 25,000M$. The observational constraints from EHT M87 Paper VII take the form of the polarization ranges $0.01 \leq |m|_{\text{net}} \leq 0.037$ and $0.057 \ll \langle |m| \rangle < 0.107$. Note that the bold values refer to fiducial models which satisfy the net linear polarization constraints.

	R-Beta	SANE R-Beta w./ Jet	($a = -0.5$) Crit. Beta	Crit. Beta w./ Jet	R-Beta	MAD R-Beta w./ Jet	($a = -0.5$) Crit. Beta	Crit. Beta w./ Jet
$ m _{\text{net}}(f_{\text{pos,min}})$	$3.93 \cdot 10^{-3}$	$3.97 \cdot 10^{-3}$	$8.51 \cdot 10^{-3}$	$2.26 \cdot 10^{-3}$	$5.51 \cdot 10^{-2}$	$4.07 \cdot 10^{-2}$	$6.93 \cdot 10^{-2}$	$4.86 \cdot 10^{-2}$
$ m _{\text{net}}(f_{\text{pos,max}})$	$1.62 \cdot 10^{-3}$	$2.88 \cdot 10^{-3}$	$2.73 \cdot 10^{-3}$	$2.50 \cdot 10^{-3}$	$3.67 \cdot 10^{-2}$	$3.10 \cdot 10^{-2}$	$5.21 \cdot 10^{-2}$	$3.55 \cdot 10^{-2}$
$\langle m \rangle(f_{\text{pos,min}})$	$1.20 \cdot 10^{-1}$	$1.38 \cdot 10^{-1}$	$1.35 \cdot 10^{-1}$	$1.44 \cdot 10^{-1}$	$3.49 \cdot 10^{-1}$	$3.30 \cdot 10^{-1}$	$2.71 \cdot 10^{-1}$	$2.53 \cdot 10^{-1}$
$\langle m \rangle(f_{\text{pos,max}})$	0.31	0.31	0.40	0.40	0.51	0.60	0.60	0.60
					R-Beta	MAD R-Beta w./ Jet	($a = +0.94$) Crit. Beta	Crit. Beta w./ Jet
$ m _{\text{net}}(f_{\text{pos,min}})$					$4.91 \cdot 10^{-2}$	$4.56 \cdot 10^{-2}$	$3.35 \cdot 10^{-2}$	$3.67 \cdot 10^{-2}$
$ m _{\text{net}}(f_{\text{pos,max}})$					$5.17 \cdot 10^{-2}$	$5.06 \cdot 10^{-2}$	$4.59 \cdot 10^{-2}$	$4.82 \cdot 10^{-2}$
$\langle m \rangle(f_{\text{pos,min}})$					$5.76 \cdot 10^{-1}$	$5.18 \cdot 10^{-1}$	$5.18 \cdot 10^{-1}$	$4.81 \cdot 10^{-1}$
$\langle m \rangle(f_{\text{pos,max}})$					$5.86 \cdot 10^{-1}$	$5.25 \cdot 10^{-1}$	$5.81 \cdot 10^{-1}$	$5.26 \cdot 10^{-1}$

MAD Observationally Preferred!

Positron Effects on “Observing” GRMHD Simulations: Hybrid Models

- ▶ Using a HARM GRMHD simulation and adding e+/e- pairs so in ray tracing at 230 GHz

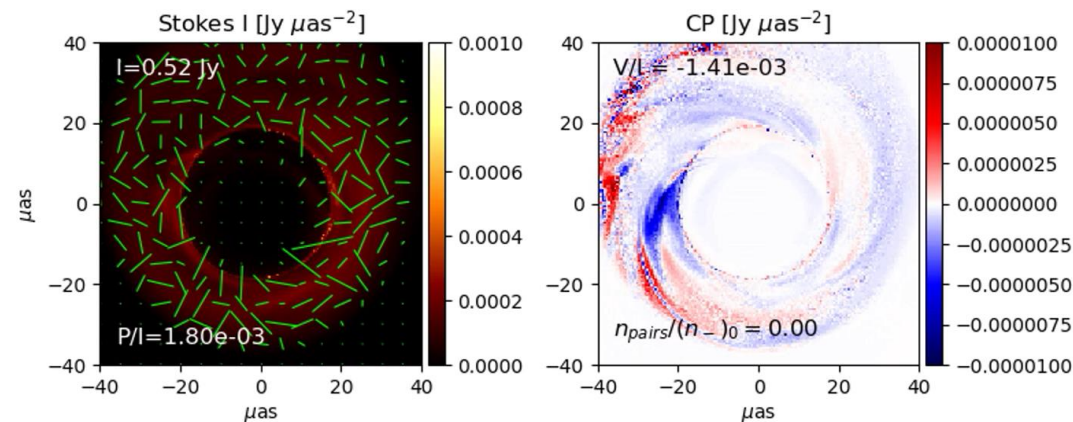
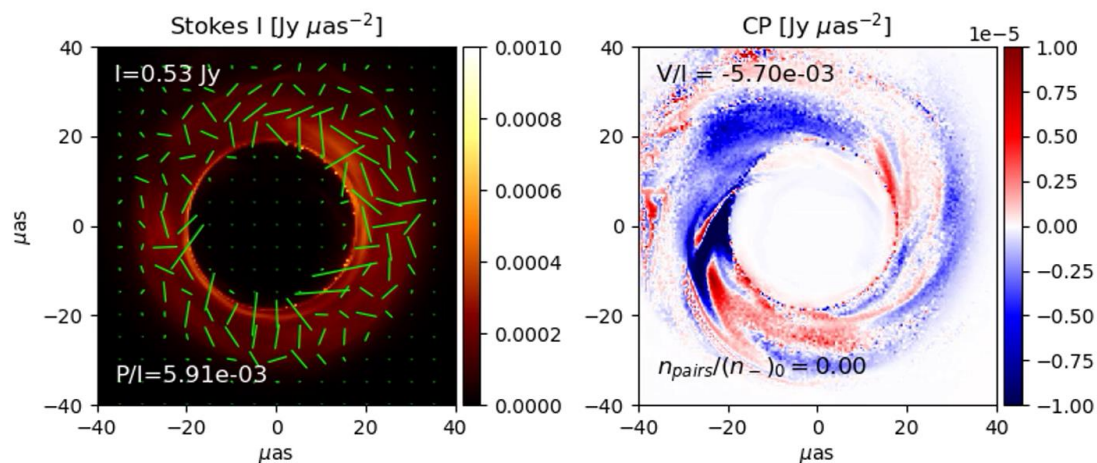
$$n = n_p + (n_{e^-})_0 + n_{\text{pairs}}$$

- ▶ Hybrid models can be constructed with different emission in the high σ (electromagnetic-to-particle flux density ratio) jet funnel by setting $P_e = \beta_{e0} P_B$ between a disk-jet transition sigma and a sigma cut above which the simulation becomes numerically unstable

SANE $R_{\text{high}}=20$, $a/M = -0.5$

SANE $R_{\text{high}}=20$, $a/M = -0.5$

$$\beta_e = 10^{-2} \text{ for } \sigma_{\text{trans}} < \sigma < \sigma_{\text{cut}}$$



Application II.

Positronium. Accretion of
Primordial Black Holes

The Primordial Universe: First 14 Seconds

- ▶ Wienberg (1977) “The First 3 Minutes”
 - ▶ For $t_{\text{Uni}} \gtrsim 10^{-2}\text{s}$, $T_{\text{Uni}} \lesssim 10^{11}\text{K}$, energetic photons regularly created particle-antiparticle pairs
 - ▶ For $10^{-2}\text{s} \lesssim t_{\text{Uni}} \lesssim 14\text{s}$ there were around 10^9 electron-positron pairs for every proton
- ▶ Fowler and Anantua (2023) <https://arxiv.org/abs/2303.09341>
 - ▶ Primordial black hole (PBH) accretion of positronium plasma under magnetorotational instability (MRI) can result in
 - ▶ A PBH population with masses $10^{15}\text{g} \lesssim M \lesssim 10^{17}\text{g}$ contributing to dark matter
 - ▶ Hawking radiation PBH supplying the present gamma ray background
- ▶ Curd, Fowler and Anantua (in prep)
 - ▶ General Relativistic Magnetohydrodynamic (GRMHD) simulations with PBH accretion of positronium

PBH Bondi Accretion

- ▶ Under Bondi (spherical) accretion around 1s after the Big Bang, primordial black holes grow rapidly accreting the ambient medium around the horizon

- ▶ Under Bondi accretion,

$$\frac{M}{t} \approx \frac{dM}{dt} \approx 4\pi R_g^2 v \rho_{\text{Amb}}, \quad v \approx c \text{ near horizon}$$

- ▶ Using ambient density

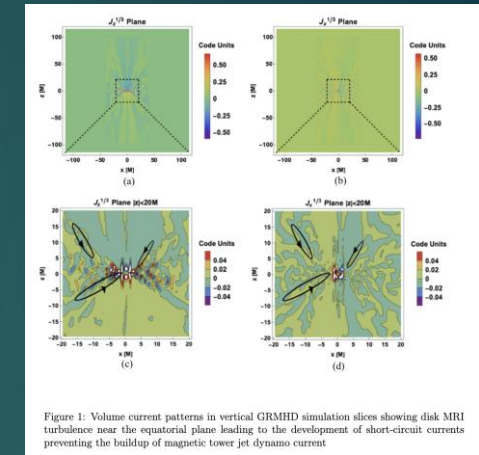
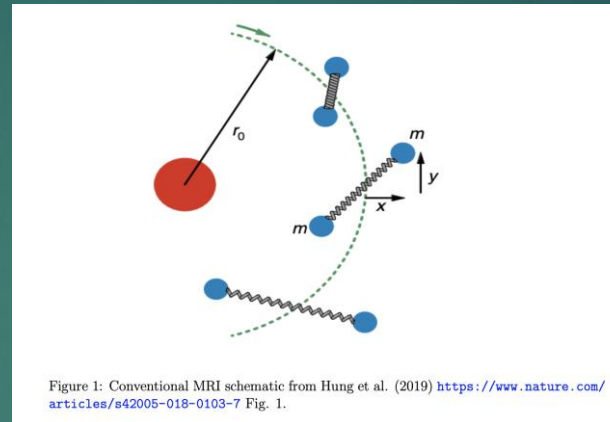
$$\rho_{\text{Amb}} \approx \frac{10^5}{t^2} \text{s}^2 \frac{\text{g}}{\text{cm}^3}$$

- ▶ The black hole mass after 1s is

$$M_{\text{PBH,Bondi}} \approx 4 \cdot 10^{39} \text{g}$$

PBH Accretion Under MRI

- ▶ Magnetorotational instability -



- ▶ Our model including MRI in the primordial plasma slowly accretes from a long range R_0 :

$$\frac{dM}{dt} \approx \frac{M}{t} \approx 4\pi R_0^2 \rho_{\text{Amb}} C^* v_k, \quad v_k = \sqrt{\frac{GM}{R_0}}$$

$$\rho_{\text{Amb}} \approx \frac{10^5}{t^2} \text{ s}^2 \frac{\text{g}}{\text{cm}^3}$$

$$R_0 = \frac{0.02 \left(\frac{\text{cm}^3}{\text{g}}\right)^{1/3}}{\left(\frac{\xi}{R}\right)^{4/3}} M(t)^{1/3} t^{2/3} \propto M(t)^{1/3} t^{2/3}, \quad \text{Accretion Radius – Time Relation}$$

$$\left(\frac{\xi}{R}\right)_{\text{MRI}} \approx 0.01$$

Leading to identity

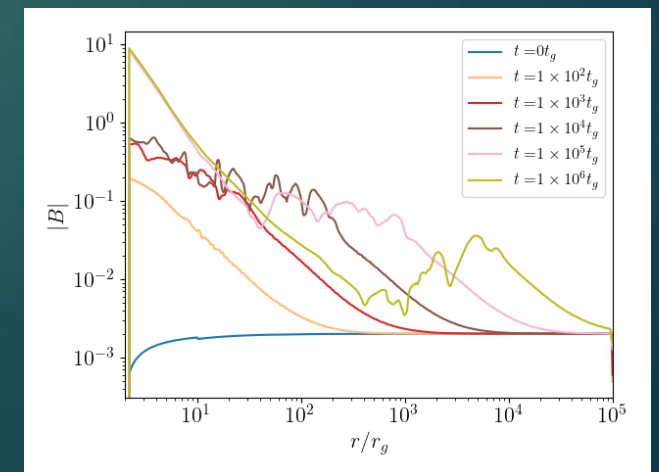
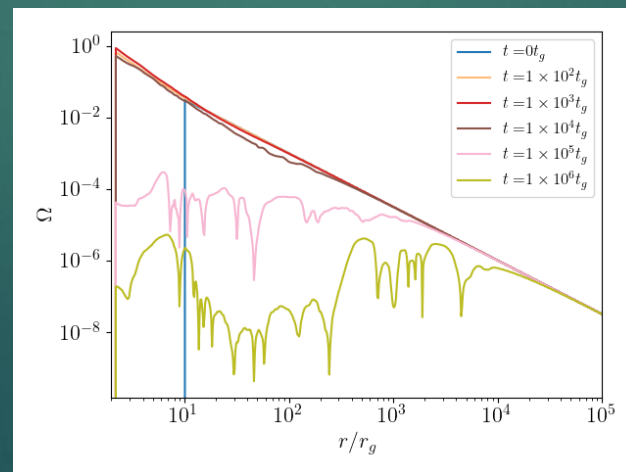
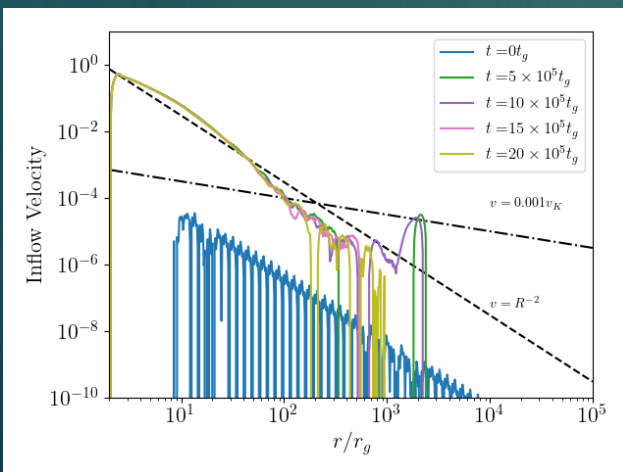
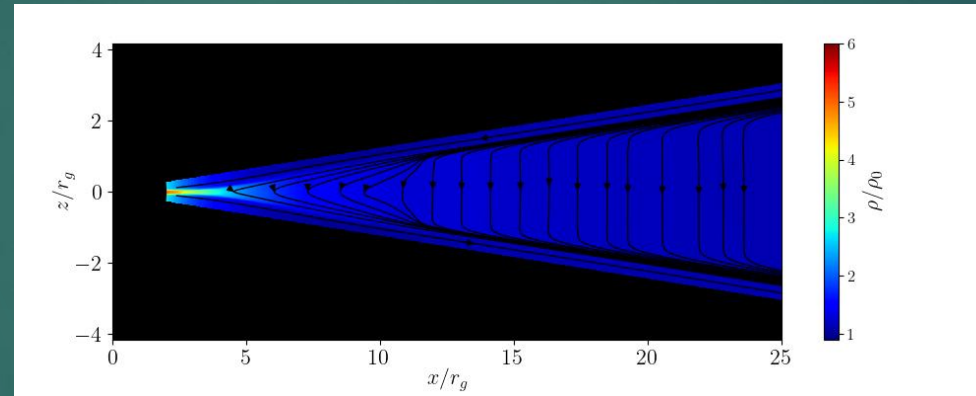
$$\frac{M}{t} \approx 4\pi \frac{10^5}{t^2} \text{ s}^2 \frac{\text{g}}{\text{cm}^3} \sqrt{GC^*} \left(\frac{0.02 \left(\frac{\text{cm}^3}{\text{g}}\right)^{1/3}}{\left(\frac{\xi}{R}\right)^{4/3}} \right)^{3/2} \frac{M}{t}$$

(in our model, t determines R_0)

GRMHD PBH Simulation

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- ▶ In KORAL simulations in Curd et al. (in prep), the inflow velocity and magnetic field under magnetorotational instability yield percent-level PBH contributions to current dark matter density



Conclusions

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- ▶ Observing Jet/Accretion Flow/Black Hole (JAB) Systems is a methodology that links intuitive e-/e+ emission models of phenomenological processes such as turbulent heating and conversion of magnetic to particle energy with discrete near-horizon AGN observations
- ▶ M87
 - ▶ Using polarized emission modeling between 43 GHz and 230 GHz
 - ▶ Observations favor Blandford-Znajek jet sourced by dynamically strong, spiral magnetic fields on the ring surrounding the black hole
 - ▶ GRMHD simulations accentuate MAD/SANE dichotomy by positron effects. e.g., rotating EVPA, altered V/I
- ▶ The accretion of positronium under magnetorotational instability may result in $10^{15}g \lesssim M \lesssim 10^{17}g$ primordial black holes associated with percent-level present dark matter contributions and a gamma ray background