Two Symmetries & a Mechanism: UV Info at Low Energies

(*the Highland Program*)

Relaxation, Scaling and Supersymmetry CPB @ CERN, Aug 31, 2023

wanderlusters.

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2111.07286 *Yoga DE* 2202.05344 *dS & inflation*

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Builds on earlier work on ubiquity of accidental scale invariance and supersymmetry in EFTs for string vacua

2006.06694

$M \sim 10^{11}$ GeV $M_w \sim 10^2$ GeV $M_p \sim 10^{18} \text{ GeV}$

Life at Low Energies

Nature comes to us with many scales

EFTs show why most low-energy predictions are robust and some are UV sensitive

> eg for QCD *UV sensitive: value of proton mass UV insensitive: soft pion theorems*

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Swampland hypothesis *Difficulty finding dS is UV informative*

Swampland Program

Swampland Hypothesis:

Many EFTs (eq those with dS solutions) have no UV completion M_p (making it useful to identify which ones are which) $\qquad \qquad$ $\qquad \qquad$ $\qquad \qquad$ $\qquad \qquad$ \qquad $\qquad \qquad$ $\qquad \qquad$

Some things indeed seem rare:

- Global symmetries
- Non-supersymmetric control
- Standard Model & no extras
- de Sitter solutions (possibly)

M Swamplementarity:

A swampland feature's plausibility is inversely proportional to its predictive power at low energies

M_{ν} Stringy `non

descriptions of physics part way up a tower

 $\frac{1.16}{\text{Vafa }05}$ 25

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Swampland hypothesis

Difficulty finding dS is UV informative

Will instead use symmetries to extract robust *low-energy implications of strings)*

Key generic approximate symmetries

Supersymmetry (especially of the gravity sector)

Rigid scaling symmetries

Usual approach (for which dS is hard to obtain): SCALE BREAKING >> susy breaking

KKLT 03 LVS 05

More promising approach: SUSY BREAKING >> scale breaking

2202.05344

Key generic approximate symmetries

Supersymmetry (especially of the gravity sector) Rigid scaling symmetries

MECHANISM FOR SUPPRESSING V:

Together these can be more than the sum of their parts…

Outline UV Motivations *Two symmetries and a mechanism*

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Low-energy EFT *RG modulus stabilization de Sitter vacua*

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Yoga exercises: adding relaxation

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Yoga exercises: adding relaxation *Features*

$$
V_{\rm min} \sim 10^{-91} M_p^4
$$

UV Motivations *Two symmetries and a mechanism*

Low-energy EFT *RG modulus stabilization de Sitter vacua*

Yoga exercises: adding relaxation *Features* $V_{\rm min} \sim 10^{-91} M_p^4$ $m_e = m_e(t)$ (Hubble Tension)

UV Motivations *Two symmetries and a mechanism*

Low-energy EFT *RG modulus stabilization de Sitter vacua*

Yoga exercises: adding relaxation

Features

(tests of gravity) *Challenges*

 $m^2 \sim V_{\rm min}/M_p^2$

UV Motivations

Two symmetries and a mechanism

Scaling Symmetries

String vacua (and therefore also essentially all extra-dimensional supergravities) share a class of accidental approximate scaling symmetries

 $g_{\mu\nu} \to \lambda^r g_{\mu\nu}$ $\Phi \to \lambda^s \Phi$ $\mathscr{L} \to \lambda^p \mathscr{L}$

Witten 85 CPB, Font & Quevedo 85 2006.06694

Scaling Symmetries

String vacua (and therefore also essentially all extra-dimensional supergravities) share a class of accidental approximate scaling symmetries

$$
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$$

WHY? String theory has no parameters so all perturbative expansions are in powers of fields

$$
\mathscr{L} = \sum_{mn} f_{mn} \, \Phi^m \, \Psi^n
$$

 $\mathscr{L}_{mn} \to \lambda^{mp+nq} \mathscr{L}_{mn}$ $\Phi \rightarrow \lambda^p \Phi \quad \Psi \rightarrow \lambda^q \Psi$

Evidence for Accidental Scaling

and so on for Type I and IIA and heterotic vacua corresponding to g_s and α' expansions..

11D sugra:
$$
\mathcal{L}_{11} \rightarrow \lambda^9 \mathcal{L}_{11}
$$

\n $g_{MN} \rightarrow \lambda^2 g_{MN}$
\n $A_{MNP} \rightarrow \lambda^3 A_{MNP}$
\n+ fermion transforms
\n10D IIB sugra: $\mathcal{L}_B \rightarrow \lambda^{4u} \mathcal{L}_B$
\n $g_{MN} \rightarrow \lambda^u g_{MN} \quad B_{MN} \rightarrow \lambda^{2u-w} B_{MN}$
\n $C_{MN} \rightarrow \lambda^w C_{MN} \quad \tau \rightarrow \lambda^{2(w-u)} \tau$
\n $C_{MNPR} \rightarrow \lambda^{2u} C_{MNPR}$
\n+ fermion transforms

Accidental Scaling can enforce $V = 0$ at extremum

V = 0 despite scaling symmetry being spontaneously broken!

$$
V(\lambda^p\Psi)=\lambda^w V(\Psi)
$$

$$
\sum_{i} p_{i} \phi^{i} \left(\frac{\partial V}{\partial \phi^{i}} \right) = wV(\phi)
$$

if
$$
\frac{\partial V}{\partial \phi^{i}} = 0 \quad \text{then}^* \quad V = 0
$$

$$
p_j \frac{\partial V}{\partial \phi^j} + \sum_i p_i \phi^i \frac{\partial^2 V}{\partial \phi^i \partial \phi^j} = w \frac{\partial V}{\partial \phi^j}
$$

if $\phi^i = 0$ then^{*} $\frac{\partial V}{\partial \phi^i} = 0$

Corrections to scaling

2006.06694

$$
\mathcal{L} = \int d^4 \theta \, \overline{\Phi} \, \Phi \, e^{-K/3}
$$

$$
+ \int d^2 \theta \Big[\Phi^3 W + f_{ab} \overline{\mathcal{F}}^a \mathcal{F}^b \Big] + \text{c.c.}
$$

$$
\mathcal{L}_{\text{kin}} = -\sqrt{-g} \, K_{i\bar{j}} \partial_{\mu} z^i \partial^{\mu} \overline{z}^j
$$

Can supersymmetry combine with scale invariance to suppress lifting of flat directions?

4D susy specified by functions *K*(*z*,*z*^{*}), *W*(*z*), $f_{ab}(z)$

$$
\mathcal{L}_{kin} = -\sqrt{-g} K_{i\bar{j}} \partial_{\mu} z^{i} \partial^{\mu} \bar{z}^{j}
$$

$$
V(z, \bar{z}) = e^{K} \Big[K^{i\bar{j}} D_{i} W \overline{D_{j} W} - 3 |W|^{2} \Big]
$$

$$
D_{i} W = W_{i} + K_{i} W
$$

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Can supersymmetry combine with scale invariance to suppress lifting of flat directions?

4D susy specified by functions *K*(*z*,*z*^{*}), *W*(*z*), $f_{\text{ch}}(z)$

Scale invariance implies rules for how *W, f_{ab}* and $e^{-K/3}$ scale as the fields *z* scale

$$
\mathcal{L}_{kin} = -\sqrt{-g} K_{i\bar{j}} \partial_{\mu} z^i \partial^{\mu} \bar{z}^j
$$

$$
V(z, \bar{z}) = e^K \Big[K^{i\bar{j}} D_i W \overline{D_j W} - 3 |W|^2 \Big]
$$

$$
D_i W = W_i + K_i W
$$

if
$$
z^i \rightarrow \lambda z^i
$$
 implies $e^{-K/3} \rightarrow \lambda e^{-K/3}$
then $K^{i\bar{j}}K_iK_{\bar{j}} = 3$
if $W_i = 0$ then

$$
V = e^{K} \left[K^{i\bar{j}} K_{i} K_{\bar{j}} - 3 \right] |W|^{2} = 0
$$

$$
D_{i} W = W_{i} + K_{i} W = K_{i} W \neq 0
$$

Special things happen if $e^{-K/3}$ is homogeneous degree 1:

0811.1503 Sufficient condition for flat direction along which susy breaks

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 implies $e^{-K/3} \rightarrow \lambda e^{-K/3}$
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'no-scale' model

if
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W_i = 0
$$
 then
\n
$$
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\n
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0811.1503 Sufficient condition for flat direction along which susy breaks

> *No-Scale supergravity:* scalar potential has a flat direction along which susy breaks

> > Cremmer et al 83 Barbieri et al 85

Scale invariance is *sufficient* for noscale supergravity, but is *not necessary*.

$$
e^{-K/3} = T + T^* + f(z, z^*)
$$

No-scale condition is sufficient for flat directions, but is also not necessary

A mechanism

Flat directions can persist in no-scale models to higher orders than naively expected

e.g. suppose τ ⁻¹ is an expansion field and scale invariance gives leading scale invariant result

scale invariant & no-scale

$$
e^{-K/3} = A_0 \tau
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Flat directions can persist at subleading order 'by accident'

Not scale invariant but still no-scale

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 $e^{-K/3} = A_0 \tau$

Flat directions can persist at subleading order 'by accident'

Not scale invariant but still no-scale

neither

$$
e^{-K/3} = A_0 \tau + A_1
$$

though are eventually lifted

$$
e^{-K/3} = A_0 \tau + A_1 + \frac{A_2}{\tau}
$$

scale invariant & no-scale

Extended No-Scale Structure

This actually happens in some string compactifications

> Berg, Haack & Kors 05 Berg, Haack & Pajer 07 Cicoli, Conlon & Quevedo 08

$$
e^{-K/3} = (\sigma - \sigma^*)^{1/3} A_0 \mathcal{V}^{2/3} \left[1 + \frac{B_n}{\mathcal{V}^{2/3}} (\sigma - \sigma^*)^{1-n} + \cdots \right]
$$

corresponding to an α'^2 string loop correction

These corrections preserve the flat direction for *V* to order α'^3 when evaluated at $D_t W = 0$

RG Stabilization.

Exponentially large dimensions de Sitter vacua

Supersymmetry and accidental scale invariance: There is a dilaton supermultiplet: $T = \{ \tau + i \alpha, \xi \}$ Action arises as expansion in dilaton field $\tau = T + T^*$

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 $k = k(Y, \overline{Y})$ $h = h(Y, \overline{Y})$ $W = w_0 + w(Y)$

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Axion symmetry ensures W independent of *T*

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Weyl scaling makes particle masses depend on τ in EF: $m = \tilde{m} e^{K/6} = \frac{\tilde{m}}{\sqrt{p}} \sim \frac{\tilde{m}}{\sqrt{\tau}} + \cdots$
Toy Model

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$$
k = k(Y, \overline{Y}) \qquad h = h(Y, \overline{Y}) \qquad W = w_0 + w(Y)
$$

k, *h* 'independent' of τ though loops can give *k* and *h* dependence on $\ln(m_1/m_2) \sim \ln {\cal P}$

Toy Model

Scalar potential for ^t

$$
V=-\tfrac{3k_T\overline{T}}{\mathcal{P}^2}\left[1+\mathcal{O}(\mathcal{P}^{-1})\right]\simeq \tfrac{3(k'-k'')}{\mathcal{P}^4}
$$

where primes denote differentiation with respect to

log τ dependence can stabilize the dilaton.

 $V \simeq \frac{U[\log \tau]}{\tau^4}$

log τ dependence can stabilize the dilaton.

$$
V \simeq \frac{U[\log \tau]}{\tau^4}
$$

 $Z\alpha$

eg suppose log τ dependence arises due to loop effects:

$$
k \simeq k_0 + k_1 \alpha(\tau) + k_2 \alpha^2(\tau) + \cdots
$$

with
$$
\frac{1}{\alpha(\tau)} = \frac{1}{\alpha_0} + \hat{b} \log \left(\frac{m_1}{m_2}\right) = \frac{1}{\alpha_0} + b \log \tau
$$

This implies
$$
U \simeq U_0 \alpha^2 + U_1 \alpha^3 + U_2 \alpha^4 + \cdots
$$

 \cup 1

Generates minima at exponentially large values for τ

$$
U(\ln \tau) \simeq U_0 \alpha^2 + U_1 \alpha^3 + U_2 \alpha^4 + \cdots
$$

eg if $\frac{U_0}{U_1} \sim \frac{U_1}{U_2} \sim O(\epsilon)$
can have U minimized at $\alpha(\tau) \sim \epsilon$ and so $\log \tau \sim \frac{1}{\epsilon}$

 $U \sim \epsilon^5$

Generates minima at exponentially large values for τ

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eg if $\frac{U_0}{U_1} \sim \frac{U_1}{U_2} \sim O(\epsilon)$
can have U minimized at $\alpha(\tau) \sim \epsilon$ and so $\log \tau \sim \frac{1}{\epsilon}$
Notice RG ensures can still trust $\frac{1}{\alpha(\tau)} = \frac{1}{\alpha_0} + b \log \tau$

Potential at minimum:

Minimum can be dS or AdS depending on coefficients *Uⁱ*

$$
U(\ln \tau) \simeq U_0 \alpha^2 + U_1 \alpha^3 + U_2 \alpha^4 + \cdots
$$

Two reasons why dS not disfavoured relative to AdS:

1. Perturbing around scale invariance starts one 'near' $V = 0$

2. Supersymmetry always broken at minimum because

$$
D_{\scriptscriptstyle T} W = K_{\scriptscriptstyle T} w_0 = -\tfrac{3w_0}{\mathcal{P}} \neq 0
$$

Preference for AdS lost because W(T) is not used to stabilize potential and so not drawn to supersymmetric minima

Yoga Models *SM fields and natural relaxation*

Supergravity Coupled to nonSUSY matter

How to couple this to SM fields?

How can supersymmetry play a role at low energies when we know the Standard Model is not supersymmetric?

General coupling of supergravity to nonsupersymmetric matter is known

Why should it matter if gravity is supersymmetric when the SM sector is not supersymmetric anyway?

Auxiliary fields are important in the low-energy scalar potential (and so also for naturalness arguments)

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Non-propagating – topological – fields play similarly important roles in eg Quantum Hall systems.

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Auxiliary fields are important in the low-energy scalar potential (and so also for naturalness arguments)

Non-propagating – topological – fields play similarly important roles in eg Quantum Hall systems.

Auxiliary fields actually start life as topological fields in higher dimensions

> Bielleman, Ibanez & Valenzuela 15 1509.04209

Yoga Models

Coupling to SM fields

There is a dilaton supermultiplet: $T = \{ \tau + i \alpha, \xi \}$

Action arises as expansion in dilaton field $\tau = T + T^*$

Goldstino *X* and other fields *Y* enter in nonsupersymmetric way

$$
\mathcal{P} := e^{-K/3} = \tau - k + \frac{h}{\tau} + \cdots
$$

$$
k = k_0(Y, \overline{Y}) + [k_X(Y, \overline{Y})X + \text{h.c.}] + \overline{X}X \text{ term}
$$

$$
W = w_0(Y) + w_X(Y, \overline{Y})X \quad \text{NEW}
$$

2111.07286

Yoga Models

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$$

$$
W = w_0(Y) + w_X(Y, \overline{Y})X
$$

$$
\mathbf{F}^X = e^{K/2}K^{X\overline{B}}(w_{\overline{B}} + K_{\overline{B}}w_0)
$$
Must keep this large to use nonlinearly realized susy

Yoga Models

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\mathcal{P} := e^{-K/3} = \tau - k + \frac{h}{\tau} + \cdots
$$
\n
$$
k = k_0(Y, \overline{Y}) + [k_X(Y, \overline{Y})X + \frac{\text{As opposed to just this}}{\text{Soposed to just this}}]
$$
\n
$$
W = w_0(Y) + w_X(Y, \overline{Y})X
$$
\n
$$
F^X = e^{K/2} K^{X \overline{B}} (w_{\overline{B}} + K_{\overline{B}} w_0)
$$
\n
$$
\text{Must keep this large to use nonlinearly realized susy}
$$

$$
\mathcal{L}_{\text{ad}} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)
$$

Leading part of the matter/dark interactions has the form:

axio-dilaton: $T = \tau + i$ *a* $\tilde{g}_{\mu\nu}=e^{K/3}g_{\mu\nu}\simeq\frac{g_{\mu\nu}}{\tau}$

$$
\mathcal{L}_{\text{ad}} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)
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$$
m_{sm} \propto \frac{M_p}{\sqrt{\tau}} \qquad m_{\nu} \propto \frac{M_p}{\tau}
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This can work if: $\sigma \sim 10^{28}$

BUT:

- Can potential generate this large a vev?
- Where would such a large number come from in the UV?

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- Where would such a large number come from in the UV?
- Axion decay constant is also very small: $f_a = M_p/\tau \sim m_\nu$

Possible UV completion exists at eV energies (2 large extra dimensions):

- SM particles must be localized on a non-SUSic brane
- SUSY in bulk broken by KK scale (supersymmetric gravity)

$$
\tilde{g}_{MN} \mathrm{d} x^M \mathrm{d} x^N = \tfrac{1}{r^2} \, g_{\mu\nu} \mathrm{d} x^\mu \mathrm{d} x^\nu + r^2 g_{mn} \mathrm{d} x^m \mathrm{d} x^n
$$

Missing energy constraints require $\ M_q > 10 \ \mathrm{TeV}$ - so for eV sized dimensions volume in natural units is *Hannesteed &*

Raffelt 02

(th/0304256)

$$
\mathcal{V} = (M_g r)^2 \sim 10^{26}
$$

Large value for τ corresponds in UV to size of extra dimensions

Axions in such theories arise as 2-form gauge potentials - For instance in bulk

$$
S = \int d^6x \sqrt{-\tilde{g}} e^{-2\phi} H_{LMN} H^{LMN} + \frac{1}{M^2} \int_{M_4} {}^{\star}H \wedge J
$$

$$
\widetilde{B}_{MN} dx^M dx^N = \frac{b(x)}{r} \omega_{mn} dx^m dx^n
$$

This gives effective 4D description

$$
S = \int d^4x \sqrt{-g} \left[\frac{(\partial \tau)^2 + (\partial b)^2}{\tau^2} + \frac{1}{F} \partial_\mu b \, J^\mu \right]
$$

with $\tau = r^2 e^{\phi}$ and $F \sim M^2 r \sim M_p$

Decay constant is *M^p* because interaction also depends on *r*

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$$

\n
$$
\widetilde{B}_{MN} dx^M dx^N = \begin{bmatrix} 0 \\ \text{But if instead use} \\ \widetilde{B}_{MN} dx^M dx^N = b_{\mu\nu}(x) dx^{\mu} dx^{\nu} \\ \widetilde{B}_{MN} dx^M dx^N = b_{\mu\nu}(x) dx^{\mu} dx^{\nu} \end{bmatrix}
$$

\n
$$
S = \int d^4x \sqrt{-g} \begin{bmatrix} (\partial \tau) \\ \frac{(\partial \tau)}{\partial \tau} \end{bmatrix} \begin{matrix} \text{and} & S_{\text{int}} = \frac{1}{M^2} \int_{M_4} H \wedge J \\ \text{then} & F \sim M_p/\tau \end{matrix}
$$

\nwith $\tau = r^2 e^{\phi}$ and $\tau = \frac{r^2}{M^2} \frac{1}{M^2} \frac$

Decay constant is *M^p* because interaction also depends on *r*

Such completions inherit promising features of SLED models

- 4D SM behaviour for particle physics on brane and only gravity sector knows about extra dimensions
- Large SM vacuum energy on branes can curve extra dimensions rather than the 4 dimensions seen by cosmology

Explains why SLED models never quite succeeded: did not stabilize moduli in a way consistent with no-scale structure

Stabilization mechanism (fluxes) broke accidental symmetries

 $K = -\ln(STU)$ $W = W(U)$ Fayet Iliopoulos term

$$
\mathcal{L}_{\text{ad}} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)
$$

$$
m_{sm} \propto \frac{M_p}{\sqrt{\tau}} \quad m_{\nu} \propto \frac{M_p}{\tau} \quad m_{3/2} \propto \frac{M_p}{\tau}
$$

What about the potential for τ ?

$$
\mathcal{L}_{\text{ad}} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)
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$$

$$
V(\tau) \simeq M_p^4 \left[\frac{w_x^2}{\tau^2} + \frac{Aw_x}{\tau^3} + \frac{B}{\tau^4} + \cdots \right]
$$

 w_X, A, B functions of other fields and $\ln \tau$

$$
\mathcal{L}_{\text{ad}} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)
$$

$$
m_{sm} \propto \frac{M_p}{\sqrt{\tau}} \quad m_{\nu} \propto \frac{M_p}{\tau} \quad m_{3/2} \propto \frac{M_p}{\tau}
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Q(m⁴_{sm}) NOT SMALL BECAUSE OF SUSY BREAKING

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$$
m_{sm} \propto \frac{M_p}{\sqrt{\tau}}
$$

$$
V(\tau) \simeq \frac{M_p^4}{\tau^4} \, U(\ln \tau)
$$

 $\tau_{\rm min} \sim 10^{28}$ $\ln \tau_{\rm min} \sim 65$

$$
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$$

 $V_{\rm min} \propto \frac{M_p^4}{\tau_{\rm min}^4} \propto \left(\frac{m_{sm}^2}{M_p}\right)^4$ 00 *Suggestive numerology!*

$$
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$$

$$
F \sim \frac{w_0}{\tau^{3/2} M_p} \qquad w_0 \sim M_p^3 \, \tau_{\min}^{1/2}
$$

More honest comparison:

$$
V_{\min} \sim \frac{\epsilon^5 |w_0|^2}{\tau_{\min}^4 M_p^2} \sim \frac{\epsilon^5}{\tau_{\min}} F^* F
$$

 $\epsilon \sim 1/(\log \tau_{\min})$
$$
\mathcal{L}_{\text{ad}} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)
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$$

Out of the box: $V_{min} = 10^{-91} M_p^4$ *(*not *quite 10-120, but…)*

$$
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$$

HH

Small V_{min} *implies small* τ *mass: below 10⁻⁸⁰* M_p^4 *must* W_p^4 *must* worry about long-range forces in the solar system (WIP)

$$
\mathcal{L}_{\text{ad}} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)
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Interesting axio-dilaton cosmology for DE and H tension

Yoga Models Screening and solar system tests

Implications for astrophysics and cosmology

$$
\mathcal{L} = -\sqrt{-g} \left\{ M_p^2 \left[\frac{\mathcal{R}}{2} + \frac{3}{4} \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \frac{U}{\tau^4} \right\} + \mathcal{L}_m
$$

Dilaton mass $m_D \simeq \sqrt{V}_{\rm min}/M_p \sim H_0$

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$$

Dilaton mass
$$
\;\; m_D \simeq \sqrt{V}_{\rm min}/M_p \sim H_0
$$

Generically true for any Planck coupled scalar if potential energy dominates universe

 $\mathcal{L}=M_{p}^{2}(\partial\theta)^{2}+v^{4}f(\theta)$ and $f(\theta)\sim f'(\theta)\sim f''(\theta)\sim 1$ imply $m \sim v^2/M_p$

Implications for astrophysics and cosmology

$$
\mathcal{L} = -\sqrt{-g} \left\{ M_p^2 \left[\frac{\mathcal{R}}{2} + \frac{3}{4} \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \frac{U}{\tau^4} \right\} + \mathcal{L}_m
$$

Dilaton mass
$$
\;\; m_D \simeq \sqrt{V}_{\rm min}/M_p \sim H_0
$$

These become relevant to solar system tests for Compton wavelengths > 1000 km and so

$$
V_{\rm min}<(10~{\rm MeV})^4\sim 10^{-80}M_p^4
$$

When $V = 0$: dilaton is a Brans-Dicke scalar

$$
\tilde{g}_{\mu\nu} = \Omega^2(\tau)g_{\mu\nu} \qquad \Omega(\tau) = \exp\Bigl(g\chi\Bigr)
$$

 $2g^2 = (3 + 2\omega)^{-1}$

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$$
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Brans-Dicke coupling

$$
g = -\frac{1}{\sqrt{6}} \simeq -0.41 \qquad 2g^2 = (3 + 2\omega)^{-1} = \frac{1}{3}
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$$

BD scalar is constrained by solar system tests, eg Cassini bound

$$
1-\gamma\simeq 4g^2<10^{-5}\qquad\text{\tiny{Bertotti\ et\ al\ O3}}
$$

Why isn't *g* too large?

Presence of axion w dilaton interactions changes PPN predictions

$$
\mathcal{L} = -\frac{3}{4} M_p^2 \sqrt{-g} \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2}
$$

$$
g = -\frac{1}{\sqrt{6}} \simeq -0.41 \qquad 1 = \sqrt{24g^2} < 10^{-5}
$$

Seek a screening mechanism, in which macroscopic objects couple to dilaton more weakly than does each of their constituents.

Existing screening mechanism (eg chameleon) seem not useful. Little known about multi-field screening – Open Problem.

Multi-field Screening Mechanisms

Best example so far:

$$
\mathcal{L} = -\frac{1}{2} M_p^2 \sqrt{-g} \left[(\partial \phi)^2 + W^2 (\phi) (\partial a)^2 \right]
$$

If axion experiences different minimum inside/outside of matter *Hook & Huang 17*

then axion necessarily has gradient near object's surface, whose interaction with the dilaton reduces the object's dilaton charge

$$
\phi'(R_+) \simeq \phi'(R_-) + \left(\frac{WW'}{2\ell}\right)_{r=R} (a_+ - a_-)^2
$$

(narrow width approximation)

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matter couplings ruled out?
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$$

(narrow width approximation)

Screening

Good news: very general methods exist to generate exterior solutions:

$$
\mathcal{L} = -\frac{1}{2}M_p^2\sqrt{-g}\Big[\mathcal{R} + \mathcal{G}_{ab}(\phi)\,\partial_\mu\phi^a\,\partial_\nu\phi^b\Big]
$$

Any target-space geodesic

$$
\phi^a(\sigma) \qquad \text{with} \qquad \ddot{\phi}^a + \Gamma^a_{bc}(\phi) \, \dot{\phi}^b \, \dot{\phi}^c = 0
$$

is an exact solution provided $\sigma(x)$ solves the Klein-Gordon/Einstein equations

$$
\mathcal{R}_{\mu\nu} + \frac{3}{4} \,\partial_{\mu}\sigma \,\partial_{\nu}\sigma = 0 \qquad \qquad \Box \sigma = 0
$$

Screening

For instance for the Yoga axio-dilaton system:

$$
a(r) = A - B \tanh X
$$

$$
\tau(r) = B \operatorname{sech} X
$$

$$
X(r) = D + (BC/r)
$$

$$
\tau^2 + (a - A)^2 = B^2
$$

Yoga Models *Cosmological surprises?*

5% increase in all masses at recombination helps with H0

Table 1: Test of the models based on dataset $\mathcal{D}_{\text{baseline}}$ (Planck 2018 + BAO + Pantheon), using the direct measurement of M_b by SH0ES for the quantification of the tension (3rd column) or the computation of the AIC (5th column). Eight models pass at least one of these three tests at the 3σ level.

H0 Olympics: 2107.10291

5% increase in all masses at recombination helps with H0 *Sekiguchi & Takahashi 2007.03381*

CMB does not change (except small nonequilibrium effects) if:

$$
\Delta_{m_e}=\Delta_{\omega_b}=\Delta_{\omega_c}
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$$
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$$
\Delta_{a_{*}}=-\Delta_{m_{e}}
$$

Leaves BAO unchanged if small spatial curvature

$$
\Delta_h=1.5\Delta_{m_e}\quad\omega_k=-0.125\Delta_{m_e}
$$

5% increase in all masses at recombination helps with H0 *Sekiguchi & Takahashi 2007.03381*

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Leaves BAO unchanged if small spatial curvature

$$
\Delta_h = 1.5 \Delta_{m_e} \quad \omega_k = -0.125 \Delta_{m_e}
$$

Requires 10% reduction in τ ; equal abundance-shifts automatic

Dilaton evolution constrained because it changes particle masses relative to the Planck mass, leaving mass ratios unchanged

UV properties can be predictive

But it is robust properties like accidental scale invariance and supersymmetric gravity sector that are informative

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Remarkably rich physics at very low energies

Suppressed DE density; possibly light axio-dilaton; screening mechanisms; dark fermions; and so on

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Much to check and many directions to explore

Framework to trade progress on the cc problem for model-building issues elsewhere

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Thanks for your time & attention!

