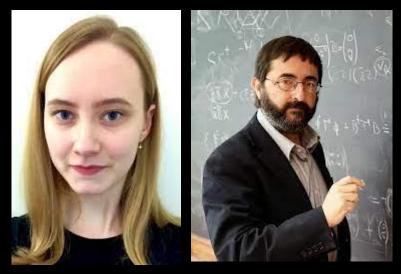
Two Symmetries & a Mechanism: UV Info at Low Energies

(the Highland Program)



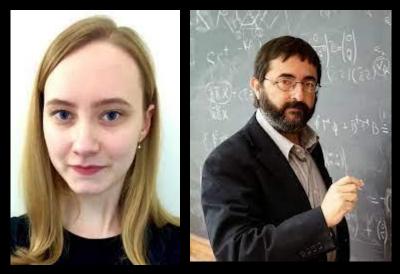
Relaxation, Scaling and Supersymmetry CERN Aug 31, 2023



F. Quevedo

2111.07286 Yoga DE 2202.05344 dS & inflation

D. Dineen



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D. Dineen

Builds on earlier work on ubiquity of accidental scale invariance and supersymmetry in EFTs for string vacua S. Krippendorf M. Cicoli



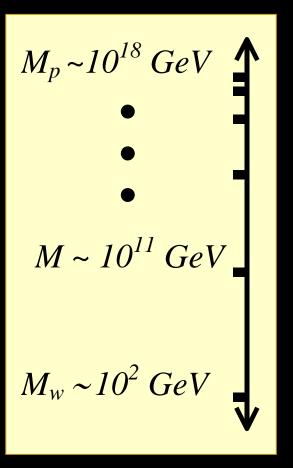
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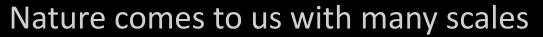
Nature comes to us with many scales

EFTs show why most low-energy predictions are robust and some are UV sensitive

eg for QCD UV sensitive: value of proton mass UV insensitive: soft pion theorems



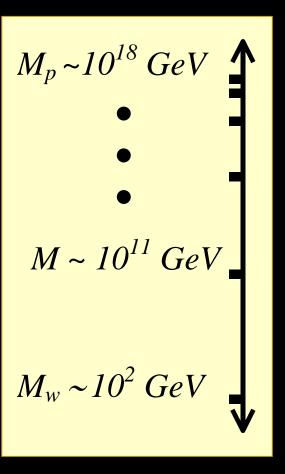




EFTs show why most low-energy predictions are robust and some are UV sensitive

eg for QCD UV sensitive: value of proton mass UV insensitive: soft pion theorems

Swampland hypothesis Difficulty finding dS is UV informative



Swampland Program

Swampland Hypothesis:

Many EFTs (eq those with dS solutions) have no UV completion (making it useful to identify which ones are which)

Some things indeed seem rare:

- Global symmetries

 M_{t}

 \boldsymbol{M}

 M_{ν}

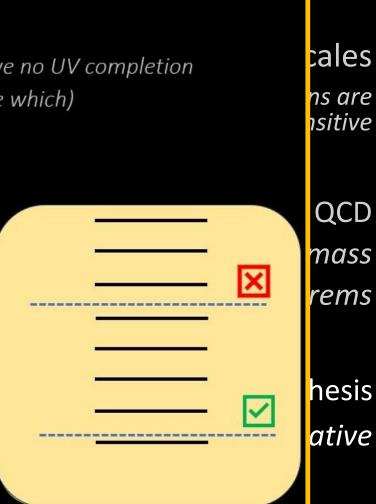
- Non-supersymmetric control
- Standard Model & no extras
- de Sitter solutions (possibly)

Swamplementarity:

A swampland feature's plausibility is inversely proportional to its predictive power at low energies

Stringy `non-EFT' surprises

Most seem examples of EFTs never being valid descriptions of physics part way up a tower



Vafa 05



Nature comes to us with many scales

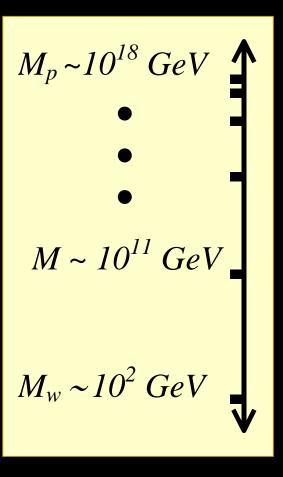
EFTs show why most low-energy predictions are robust and some are UV sensitive

eg for QCD UV sensitive: value of proton mass UV insensitive: soft pion theorems

Swampland hypothesis

Difficulty finding dS is UV informative

Will instead use symmetries to extract robust low-energy implications of strings



Key generic approximate symmetries

Supersymmetry (especially of the gravity sector)

Rigid scaling symmetries

Usual approach (for which dS is hard to obtain): SCALE BREAKING >> susy breaking KKLT 03 LVS 05

More promising approach: SUSY BREAKING >> scale breaking

2202.05344

Key generic approximate symmetries

Supersymmetry (especially of the gravity sector)

Rigid scaling symmetries

MECHANISM FOR SUPPRESSING V:

Together these can be more than the sum of their parts...

Outline UV Motivations Two symmetries and a mechanism

Low-energy EFT RG modulus stabilization de Sitter vacua

Yoga exercises: adding relaxation Features Challenges

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Low-energy EFT RG modulus stabilization de Sitter vacua

Yoga exercises: adding relaxation $V_{\min} \sim 10^{-91} M_p^4$ FeaturesFeatures

UV Motivations Two symmetries and a mechanism

Low-energy EFT RG modulus stabilization de Sitter vacua

Yoga exercises: adding relaxation $V_{
m min}\sim 10^{-91}M_p^4$ Features $m_e=m_e(t)$ (Hubble Tension)

UV Motivations Two symmetries and a mechanism

Low-energy EFT RG modulus stabilization de Sitter vacua

Yoga exercises: adding relaxation

Features Challenges

(tests of gravity)

 $m^2 \sim V_{\rm min}/M_p^2$



UV Motivations

Two symmetries and a mechanism

Scaling Symmetries

String vacua (and therefore also essentially all extra-dimensional supergravities) share a class of accidental approximate scaling symmetries

 $g_{\mu\nu} \to \lambda^r g_{\mu\nu} \quad \Phi \to \lambda^s \Phi \qquad \mathscr{L} \to \lambda^p \mathscr{L}$

Witten 85 CPB, Font & Quevedo 85 2006.06694

Scaling Symmetries

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WHY? String theory has no parameters so all perturbative expansions are in powers of fields

$$\mathscr{L} = \sum_{mn} f_{mn} \, \Phi^m \, \Psi^n$$

 $\Phi \to \lambda^p \Phi \quad \Psi \to \lambda^q \Psi \qquad \mathscr{L}_{mn} \to \lambda^{mp+nq} \mathscr{L}_{mn}$

Evidence for Accidental Scaling

and so on for Type I and IIA and heterotic vacua corresponding to g_s and α' expansions..

11D sugra: $\mathscr{L}_{11} \rightarrow \lambda^9 \mathscr{L}_{11}$ $g_{MN} \rightarrow \lambda^2 g_{MN}$ $A_{MNP} \rightarrow \lambda^3 A_{MNP}$ + fermion transfns 10D IIB sugra: $\mathscr{L}_B \to \lambda^{4u} \mathscr{L}_B$ $g_{MN} \rightarrow \lambda^{\mu} g_{MN} \quad B_{MN} \rightarrow \lambda^{2u-w} B_{MN}$ $C_{MN} \rightarrow \lambda^w C_{MN} \qquad \tau \rightarrow \lambda^{2(w-u)} \tau$

$$C_{MNPR} \rightarrow \lambda^{2u} C_{MNPR}$$

Accidental Scaling can enforce V = 0 at extremum



V = 0 despite scaling symmetry
 being spontaneously broken!

$$V(\lambda^p \Psi) = \lambda^w V(\Psi)$$

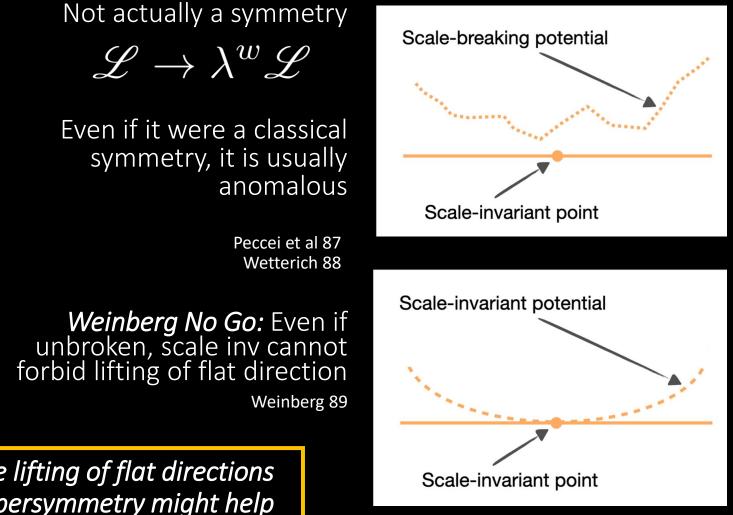
$$\sum_{i} p_{i} \phi^{i} \left(\frac{\partial V}{\partial \phi^{i}} \right) = wV(\phi)$$

if $\frac{\partial V}{\partial \phi^{i}} = 0$ then^{*} $V = 0$

$$p_{j}\frac{\partial V}{\partial \phi^{j}} + \sum_{i} p_{i}\phi^{i}\frac{\partial^{2}V}{\partial \phi^{i}\partial \phi^{j}} = w\frac{\partial V}{\partial \phi^{j}}$$

if $\phi^{i} = 0$ then^{*} $\frac{\partial V}{\partial \phi^{i}} = 0$

Corrections to scaling



Restricting the lifting of flat directions is where supersymmetry might help

2006.06694

$$\begin{aligned} \mathscr{L} &= \int d^4 \theta \ \overline{\Phi} \ \Phi \ e^{-K/3} \\ &+ \int d^2 \theta \Big[\Phi^3 W + f_{ab} \overline{\mathscr{F}}^a \mathscr{F}^b \Big] + \text{c.c.} \end{aligned}$$
$$\begin{aligned} \mathscr{L}_{\text{kin}} &= -\sqrt{-g} \ K_{i\bar{\imath}} \ \partial_\mu z^i \ \partial^\mu \bar{z}^j \end{aligned}$$

Can supersymmetry combine with scale invariance to suppress lifting of flat directions?

4D susy specified by functions $K(z,z^*), W(z), f_{ab}(z)$

$$\mathcal{L}_{kin} = -\sqrt{-g} K_{i\bar{j}} \partial_{\mu} z^{i} \partial^{\mu} \bar{z}^{j}$$
$$V(z, \bar{z}) = e^{K} \left[K^{i\bar{j}} D_{i} W \overline{D_{j} W} - 3 |W|^{2} \right]$$
$$D_{i} W = W_{i} + K_{i} W$$

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4D susy specified by functions $K(z,z^*), W(z), f_{ab}(z)$

Scale invariance implies rules for how *W*, f_{ab} and $e^{-K/3}$ scale as the fields *z* scale

$$D_i W = W_i + K_i W$$

 $V(z,\bar{z}) = e^{K} \left| K^{i\bar{j}} D_{i} W \overline{D_{j} W} - 3 |W|^{2} \right|$

if
$$z^i \rightarrow \lambda z^i$$
 implies $e^{-K/3} \rightarrow \lambda e^{-K/3}$
then $K^{i\bar{j}}K_iK_{\bar{j}} = 3$
if $W_i = 0$ then

Sufficient condition for flat direction along which susy breaks 0811.1503

if
$$W_i = 0$$
 then

$$V = e^K \left[K^{i\bar{j}} K_i K_{\bar{j}} - 3 \right] |W|^2 = 0$$

$$D_i W = W_i + K_i W = K_i W \neq 0$$

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'no-scale' model

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Special things happen if $e^{-K/3}$ is homogeneous degree 1:

Sufficient condition for flat direction along which susy breaks 0811.1503

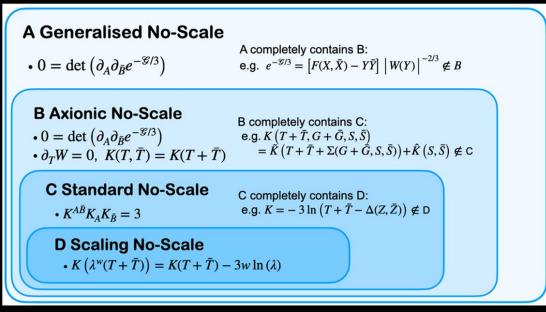
No-Scale supergravity: scalar potential has a flat direction along which susy breaks

Cremmer et al 83 Barbieri et al 85

Scale invariance is *sufficient* for no-scale supergravity, but is *not necessary*.

$$e^{-K/3} = T + T^* + f(z, z^*)$$

No-scale condition is sufficient for flat directions, but is also not necessary



A mechanism

Flat directions can persist in no-scale models to higher orders than naively expected

e.g. suppose τ^{-1} is an expansion field and scale invariance gives leading scale invariant result

scale invariant & no-scale

$$e^{-K/3} = A_0 \ \tau$$

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Flat directions can persist at subleading order 'by accident'

Not scale invariant but still no-scale

$$e^{-K/3} = A_0 \ \tau + A_1$$

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Not scale invariant but still no-scale

neither

$$e^{-K/3} = A_0 \ \tau + A_1$$

though are eventually lifted

$$e^{-K/3} = A_0 \ \tau + A_1 + \frac{A_2}{\tau}$$

scale invariant & no-scale

Extended No-Scale Structure

This actually happens in some string compactifications

Berg, Haack & Kors 05 Berg, Haack & Pajer 07 Cicoli, Conlon & Quevedo 08

$$e^{-K/3} = (\sigma - \sigma^*)^{1/3} A_0 \mathcal{V}^{2/3} \left[1 + \frac{B_n}{\mathcal{V}^{2/3}} (\sigma - \sigma^*)^{1-n} + \cdots \right]$$

corresponding to an α'^2 string loop correction

These corrections preserve the flat direction for V to order α'^3 when evaluated at $D_{\tau}W = 0$

RG Stabilization

Exponentially large dimensions de Sitter vacua

Supersymmetry and accidental scale invariance: There is a dilaton supermultiplet: $T = \{\tau + i \ a, \xi\}$ Action arises as expansion in dilaton field $\tau = T + T^*$

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 $h = h(Y, \overline{Y})$ $W = w_0 + w(Y)$

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Axion symmetry ensures W independent of T

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Weyl scaling makes particle masses depend on τ in EF: $m = \tilde{m} e^{K/6} = \frac{\tilde{m}}{\sqrt{\mathcal{P}}} \sim \frac{\tilde{m}}{\sqrt{\tau}} + \cdots$

Toy Model

Supersymmetry and accidental scale invariance: There is a dilaton supermultiplet: $T = \{\tau + i \ a, \xi\}$ Action arises as expansion in dilaton field $\tau = T + T^*$

$$\mathcal{P} := e^{-K/3} = \tau - k + \frac{h}{\tau} + \cdots$$

$$k = k(Y, \overline{Y})$$
 $h = h(Y, \overline{Y})$ $W = w_0 + w(Y)$

k, h 'independent' of τ though loops can give k and h dependence on $\ln(m_1/m_2) \sim \ln \mathcal{P}$

Toy Model

Scalar potential for au

$$V = -\frac{3k_T\overline{T}}{\mathcal{P}^2} \left[1 + \mathcal{O}(\mathcal{P}^{-1}) \right] \simeq \frac{3(k' - k'')}{\mathcal{P}^4}$$

where primes denote differentiation with respect to $\ln \mathcal{P}$

 $\log \tau$ dependence can stabilize the dilaton.

 $V \simeq \frac{U[\log \tau]}{\tau^4}$

 $\log \tau$ dependence can stabilize the dilaton.

$$V \simeq \frac{U[\log \tau]}{\tau^4}$$

eg suppose log τ dependence arises due to loop effects:

$$k \simeq k_0 + k_1 \alpha(\tau) + k_2 \alpha^2(\tau) + \cdots$$

with $\frac{1}{\alpha(\tau)} = \frac{1}{\alpha_0} + \hat{b} \log\left(\frac{m_1}{m_2}\right) = \frac{1}{\alpha_0} + b \log \tau$

This implies $U\simeq U_0lpha^2+U_1lpha^3+U_2lpha^4+\cdots$

Generates minima at exponentially large values for $\boldsymbol{\tau}$

$$\begin{split} U(\ln \tau) \simeq U_0 \alpha^2 + U_1 \alpha^3 + U_2 \alpha^4 + \cdots \\ & \text{eg if } \ \frac{U_0}{U_1} \sim \frac{U_1}{U_2} \sim O(\epsilon) \\ & \text{can have U minimized at } \alpha(\tau) \sim \epsilon \text{ and so } \log \tau \sim \frac{1}{\epsilon} \end{split}$$

 $\overline{U} \sim \epsilon^5$

Generates minima at exponentially large values for $\boldsymbol{\tau}$

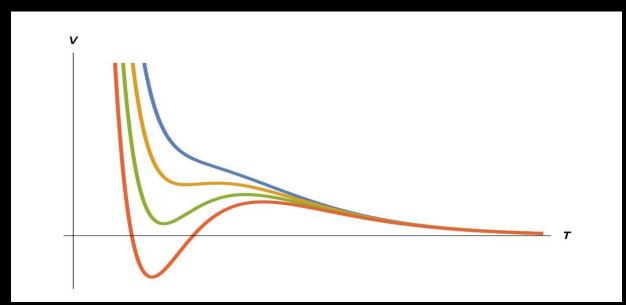
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$$\end{split}$$
Notice RG ensures can still trust \quad \frac{1}{\alpha(\tau)} = \frac{1}{\alpha_0} + b \log \tau

Potential at minimum:

Minimum can be dS or AdS depending on coefficients U_i

$$U(\ln \tau) \simeq U_0 \alpha^2 + U_1 \alpha^3 + U_2 \alpha^4 + \cdots$$



Two reasons why dS not disfavoured relative to AdS:

1. Perturbing around scale invariance starts one 'near' V = 0

2. Supersymmetry always broken at minimum because

$$D_T W = K_T w_0 = -\frac{3w_0}{\mathcal{P}} \neq 0$$

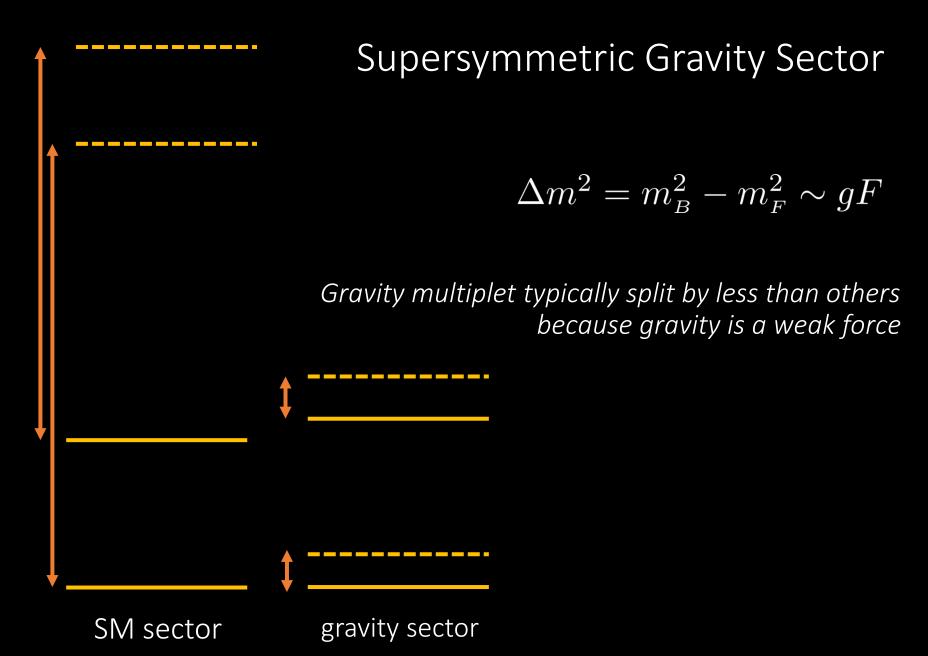
Preference for AdS lost because W(T) is not used to stabilize potential and so not drawn to supersymmetric minima

Yoga Models SM fields and natural relaxation

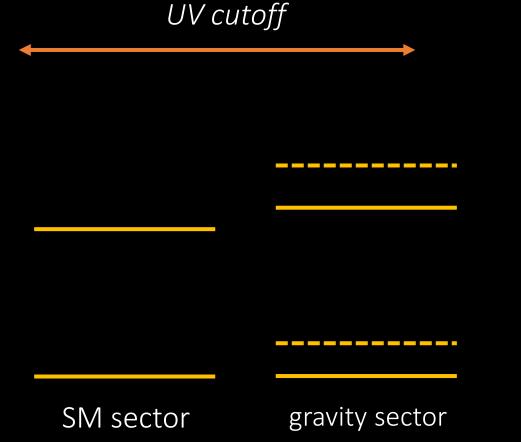
Supergravity Coupled to nonSUSY matter

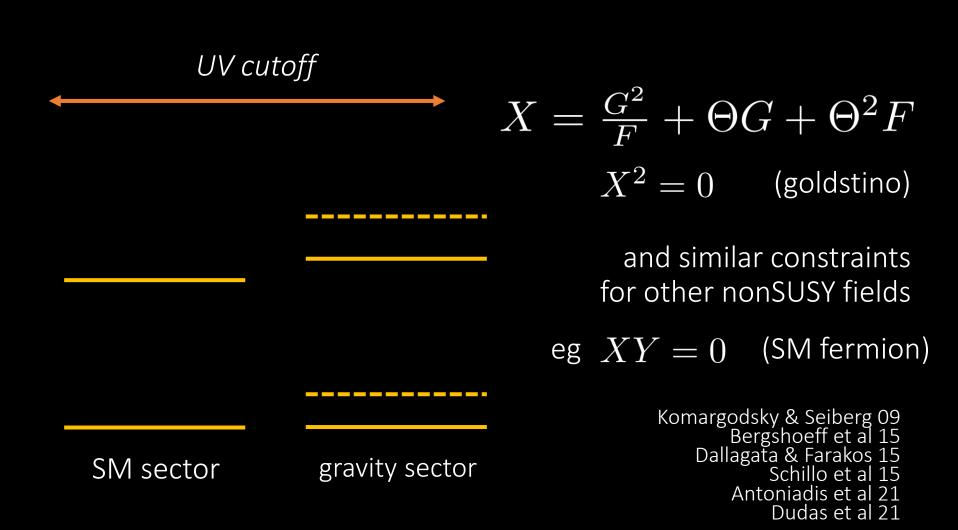
How to couple this to SM fields?

How can supersymmetry play a role at low energies when we know the Standard Model is not supersymmetric?



General coupling of supergravity to nonsupersymmetric matter is known





Why should it matter if gravity is supersymmetric when the SM sector is not supersymmetric anyway?

Auxiliary fields are important in the low-energy scalar potential (and so also for naturalness arguments)

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Non-propagating – topological – fields play similarly important roles in eg Quantum Hall systems.

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Auxiliary fields are important in the low-energy scalar potential (and so also for naturalness arguments)

Non-propagating – topological – fields play similarly important roles in eg Quantum Hall systems.

Auxiliary fields actually start life as topological fields in higher dimensions

> Bielleman, Ibanez & Valenzuela 15 1509.04209

Yoga Models

Coupling to SM fields

There is a dilaton supermultiplet: $T = \{\tau + i a, \xi\}$

Action arises as expansion in dilaton field $\tau = T + T^*$

Goldstino X and other fields Y enter in nonsupersymmetric way

$$\mathcal{P} := e^{-K/3} = \tau - k + \frac{h}{\tau} + \cdots$$
$$k = k_0(Y, \overline{Y}) + \left[k_X(Y, \overline{Y})X + \text{h.c.}\right] + \overline{X}X \text{ term}$$
$$W = w_0(Y) + w_X(Y, \overline{Y})X \text{ NEW}$$

2111.07286

Yoga Models

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$$\begin{aligned} F^X &= e^{K/2} K^{X\overline{B}} (w_{\overline{B}} + K_{\overline{B}} w_0) \\ \text{Must keep this large to use nonlinearly realized susy} \end{aligned}$$

Yoga Models

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$$\begin{split} \mathcal{P} &:= e^{-K/3} = \tau - k + \frac{h}{\tau} + \cdots \\ k &= k_0(Y,\overline{Y}) + [k_x(Y,\overline{Y})X + \text{As opposed to just this} \\ W &= w_0(Y) + w_x(Y,\overline{Y})X \\ \hline F^X &= e^{K/2}K^{X\overline{B}}(w_{\overline{B}} + K_{\overline{B}}w_0) \\ \text{Must keep this large to use nonlinearly realized susy} \end{split}$$

$$\mathcal{L}_{\rm ad} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)$$

Leading part of the matter/dark interactions has the form: axio-dilaton: $T = \tau + i a$ $\tilde{g}_{\mu\nu} = e^{K/3} g_{\mu\nu} \simeq \frac{g_{\mu\nu}}{\tau}$

$$\mathcal{L}_{ad} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)$$
$$m_{sm} \propto \frac{M_p}{\sqrt{\tau}} \qquad m_\nu \propto \frac{M_p}{\tau}$$

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This can work if: $au \sim 10^{28}$

BUT:

- Can potential generate this large a vev?
- Where would such a large number come from in the UV?

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BUT:

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- Where would such a large number come from in the UV?
- Axion decay constant is also very small: $~f_a = M_p/ au \sim m_
 u$

Possible UV completion exists at eV energies (2 large extra dimensions):

- SM particles must be localized on a non-SUSic brane
- SUSY in bulk broken by KK scale (supersymmetric gravity)

$$\tilde{g}_{MN} \mathrm{d}x^M \mathrm{d}x^N = \frac{1}{r^2} g_{\mu\nu} \mathrm{d}x^\mu \mathrm{d}x^\nu + r^2 g_{mn} \mathrm{d}x^m \mathrm{d}x^n$$

Missing energy constraints require $M_g > 10 \text{ TeV}$ - so for eV sized dimensions volume in natural units is

Hannesteed & Raffelt 02

(th/0304256)

$$\mathcal{V} = (M_g r)^2 \sim 10^{26}$$

Large value for τ corresponds in UV to size of extra dimensions

Axions in such theories arise as 2-form gauge potentials - For instance in bulk

$$\begin{split} S &= \int \mathrm{d}^6 x \; \sqrt{-\tilde{g}} \; e^{-2\phi} H_{LMN} H^{LMN} + \frac{1}{M^2} \int_{M_4} {}^*H \wedge J \\ & \widetilde{B}_{MN} \mathrm{d} x^M \mathrm{d} x^N = \frac{b(x)}{r} \, \omega_{mn} \mathrm{d} x^m \mathrm{d} x^n \end{split}$$

This gives effective 4D description

$$\begin{split} S &= \int \mathrm{d}^4 x \; \sqrt{-g} \left[\frac{(\partial \tau)^2 + (\partial b)^2}{\tau^2} + \frac{1}{F} \partial_\mu b \, J^\mu \right] \\ \text{with} \quad \tau &= r^2 \, e^\phi \qquad \text{and} \qquad F \sim M^2 r \sim M_p \end{split}$$

Decay constant is M_p because interaction also depends on r

Axions in such theories arise as 2-form gauge potentials - For instance in bulk

$$\begin{split} S &= \int \mathrm{d}^{6}x \; \sqrt{-\tilde{g}} \; e^{-2\phi} H_{LMN} H^{LMN} + \frac{1}{M^{2}} \int_{M_{4}} {}^{\star}H \wedge J \\ & \widetilde{B}_{MN} \mathrm{d}x^{M} \mathrm{d}x^{N} = \\ \text{This gives effective 4D description} \\ S &= \int \mathrm{d}^{4}x \; \sqrt{-g} \left[\frac{(\partial \tau)}{\Gamma} \right]^{M} \text{ and } S_{\mathrm{int}} = \frac{1}{M^{2}} \int_{M_{4}} H \wedge J \\ & \text{and } S_{\mathrm{int}} = \frac{1}{M^{2}} \int_{M_{4}} H \wedge J \\ & \text{then } F \sim M_{p}/\tau \\ & \text{with } \tau = r^{2} \; e^{\phi} \quad \text{and } T \sim M \to \infty M p \end{split}$$

Decay constant is M_{p} because interaction also depends on r

Such completions inherit promising features of SLED models

- 4D SM behaviour for particle physics on brane and only gravity sector knows about extra dimensions
- Large SM vacuum energy on branes can curve extra dimensions rather than the 4 dimensions seen by cosmology

Explains why SLED models never quite succeeded: did not stabilize moduli in a way consistent with no-scale structure

Stabilization mechanism (fluxes) broke accidental symmetries

 $K = -\ln(STU)$ W = W(U) Fayet Iliopoulos term

$$\mathcal{L}_{ad} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)$$
$$m_{sm} \propto \frac{M_p}{\sqrt{\tau}} \quad m_\nu \propto \frac{M_p}{\tau} \quad m_{3/2} \propto \frac{M_p}{\tau}$$

What about the potential for τ ?

$$\mathcal{L}_{ad} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)$$

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$$V(\tau) \simeq M_p^4 \left[\frac{w_X^2}{\tau^2} + \frac{Aw_X}{\tau^3} + \frac{B}{\tau^4} + \cdots \right]$$

 w_X, A, B functions of other fields and $\ln \tau$

$$\mathcal{L}_{ad} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)$$
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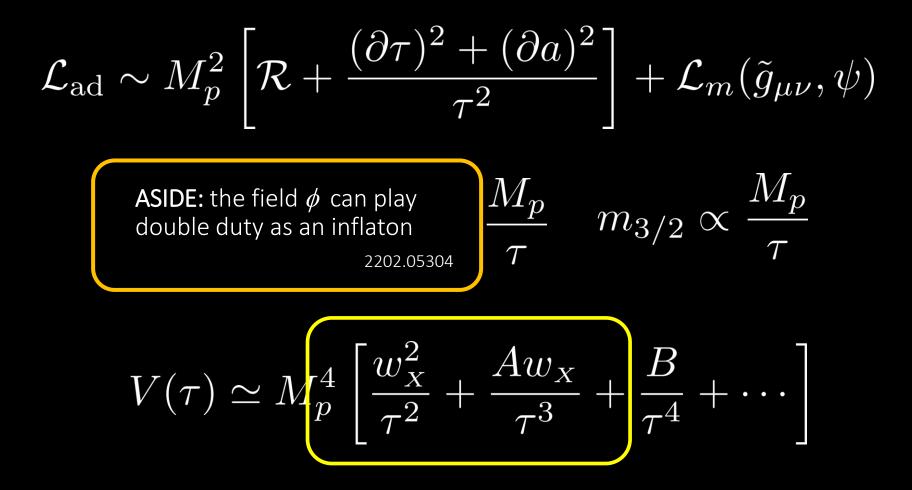
$$V(\tau) \simeq M_p^4 \left[\frac{w_X^2}{\tau^2} + \frac{Aw_X}{\tau^3} + \frac{B}{\tau^4} + \cdots \right]$$

 $\mathcal{O}(m_{sm}^4)$

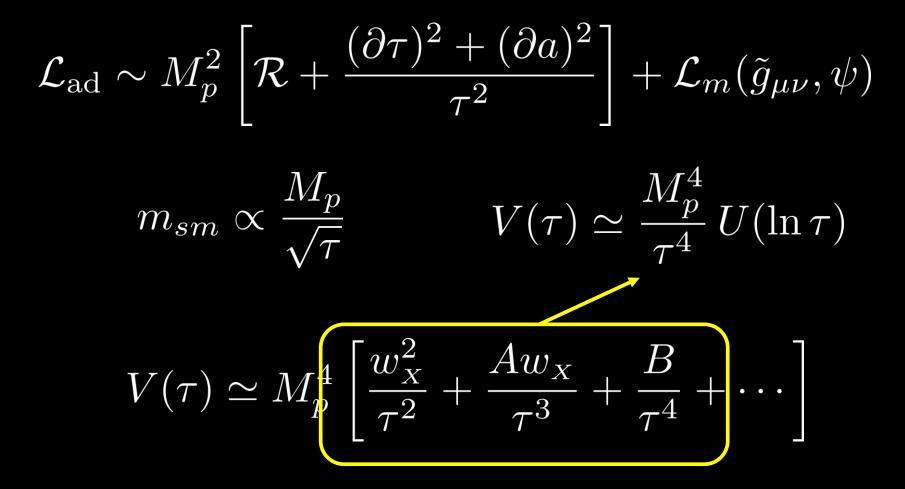
NOT SMALL BECAUSE OF SUSY BREAKING

$$\mathcal{L}_{ad} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)$$
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$$V(\tau) \simeq \frac{M_p^4}{\tau^4} U(\ln \tau)$$

 $\ln \tau_{\rm min} \sim 65 \qquad \tau_{\rm min} \sim 10^{28}$

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Suggestive $V_{\min} \propto \frac{M_p^4}{\tau_{\min}^4} \propto \left(\frac{m_{sm}^2}{M_p}\right)^4$

$$\mathcal{L}_{ad} \sim M_p^2 \left[\mathcal{R} + \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \mathcal{L}_m(\tilde{g}_{\mu\nu}, \psi)$$

$$F \sim \frac{w_0}{\tau^{3/2} M_p} \qquad w_0 \sim M_p^3 \, \tau_{\min}^{1/2}$$

$$V_{\min} \sim \frac{\epsilon^5 |w_0|^2}{\tau_{\min}^4 M_p^2} \sim \frac{\epsilon^5}{\tau_{\min}} F^* F$$

 $\epsilon \sim 1/(\log \tau_{\min})$

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Out of the box: $V_{min} = 10^{-91} M_p^4$ (not quite 10⁻¹²⁰, but...)

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Small V_{min} implies small τ mass: below 10⁻⁸⁰ M_p^4 must worry about long-range forces in the solar system (WIP)

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Interesting axio-dilaton cosmology for DE and H tension



Yoga Models Screening and solar system tests

Implications for astrophysics and cosmology

$$\mathcal{L} = -\sqrt{-g} \left\{ M_p^2 \left[\frac{\mathcal{R}}{2} + \frac{3}{4} \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2} \right] + \frac{U}{\tau^4} \right\} + \mathcal{L}_m$$

Dilaton mass
$$m_D \simeq \sqrt{V_{\min}}/M_p \sim H_0$$

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Dilaton mass
$$m_D \simeq \sqrt{V}_{\min}/M_p \sim H_0$$

Generically true for any Planck coupled scalar if potential energy dominates universe

 $\mathcal{L} = M_p^2 (\partial \theta)^2 + v^4 f(\theta) \text{ and } f(\theta) \sim f'(\theta) \sim f''(\theta) \sim 1$

imply $m \sim v^2/M_p$

Implications for astrophysics and cosmology

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$$m_D \simeq \sqrt{V_{\min}}/M_p \sim H_0$$

These become relevant to solar system tests for Compton wavelengths > 1000 km and so

$$V_{\rm min} < (10 \ {
m MeV})^4 \sim 10^{-80} M_p^4$$

When V = 0: dilaton is a Brans-Dicke scalar

$$\tilde{g}_{\mu\nu} = \Omega^2(\tau)g_{\mu\nu} \quad \Omega(\tau) = \exp\left(g\chi\right)$$

$$2g^2 = (3+2\omega)^{-1}$$

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$$\tilde{g}_{\mu\nu} = \Omega^2(\tau)g_{\mu\nu} \quad \Omega(\tau) = \exp(g\chi) = \tau^{-1/2}$$

Brans-Dicke coupling

$$g = -\frac{1}{\sqrt{6}} \simeq -0.41$$
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Brans-Dicke coupling

$$g = -\frac{1}{\sqrt{6}} \simeq -0.41$$
 $2g^2 = (3+2\omega)^{-1} = \frac{1}{3}$

BD scalar is constrained by solar system tests, eg Cassini bound

$$1-\gamma\simeq 4g^2 < 10^{-5}$$
 Bertotti et al 03

Why isn't *g* too large?

Presence of axion w dilaton interactions changes PPN predictions

$$\mathcal{L} = -\frac{3}{4} M_p^2 \sqrt{-g} \frac{(\partial \tau)^2 + (\partial a)^2}{\tau^2}$$

$$q = -\frac{1}{\sqrt{6}} \simeq -0.41 \qquad 1 - \gamma \simeq 4g^2 < 10^{-5}$$

Seek a screening mechanism, in which macroscopic objects couple to dilaton more weakly than does each of their constituents.

Existing screening mechanism (eg chameleon) seem not useful. Little known about multi-field screening – Open Problem.

Multi-field Screening Mechanisms

Best example so far:

$$\mathcal{L} = -\frac{1}{2} M_p^2 \sqrt{-g} \Big[(\partial \phi)^2 + W^2(\phi) (\partial a)^2 \Big]$$

If axion experiences different minimum inside/outside of matter Hook & Huang 17

then axion necessarily has gradient near object's surface, whose interaction with the dilaton reduces the object's dilaton charge

$$\phi'(R_+) \simeq \phi'(R_-) + \left(\frac{WW'}{2\ell}\right)_{r=R} (a_+ - a_-)^2$$

(narrow width approximation)

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(narrow width approximation)

Screening

Good news: very general methods exist to generate exterior solutions:

$$\mathcal{L} = -\frac{1}{2}M_p^2\sqrt{-g} \Big[\mathcal{R} + \mathcal{G}_{ab}(\phi)\,\partial_\mu\phi^a\,\partial_\nu\phi^b\Big]$$

Any target-space geodesic

$$\phi^a(\sigma)$$
 with $\ddot{\phi}^a + \Gamma^a_{bc}(\phi) \, \dot{\phi}^b \, \dot{\phi}^c = 0$

is an exact solution provided $\sigma(x)$ solves the Klein-Gordon/Einstein equations

$$\mathcal{R}_{\mu\nu} + \frac{3}{4} \,\partial_{\mu}\sigma \,\partial_{\nu}\sigma = 0 \qquad \qquad \Box \sigma = 0$$

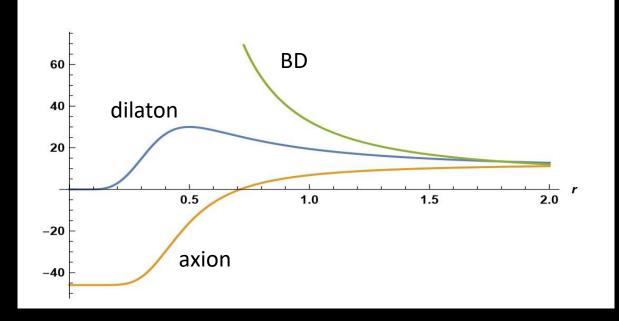
Screening

For instance for the Yoga axio-dilaton system:

$$a(r) = A - B \tanh X$$

 $\tau(r) = B \operatorname{sech} X$
 $X(r) = D + (BC/r)$

$$\tau^2 + (a - A)^2 = B^2$$



Yoga Models Cosmological surprises?

5% increase in all masses at recombination helps with H0

Model	$\Delta N_{ m param}$	M_B	Gaussian Tension	$Q_{\rm DMAP}$ Tension		$\Delta \chi^2$	ΔΑΙC		Finalist
ACDM	0	-19.416 ± 0.012	4.4σ	4.5σ	X	0.00	0.00	X	X
$\Delta N_{ m ur}$	1	-19.395 ± 0.019	3.6σ	3.8σ	X	-6.10	-4.10	X	X
SIDR	1	-19.385 ± 0.024	3.2σ	3.3σ	X	-9.57	-7.57	\checkmark	🗸 🐵
mixed DR	2	-19.413 ± 0.036	3.3σ	3.4σ	X	-8.83	-4.83	X	X
DR-DM	2	-19.388 ± 0.026	3.2σ	3.1σ	X	-8.92	-4.92	X	X
$SI\nu + DR$	3	$-19.440\substack{+0.037\\-0.039}$	3.8σ	3.9σ	\boldsymbol{X}	-4.98	1.02	X	X
Majoron	3	$-19.380\substack{+0.027\\-0.021}$	3.0σ	2.9σ	~	-15.49	-9.49	~	 ✓ (10)
primordial B	1	10.200 ± 0.018 -0.024	2.50	2.50	X	11.42	0.42	1	
varying m_e	1	-19.391 ± 0.034	2.9σ	2.9σ	~	-12.27	-10.27	~	V 😐
varying $m_e + \Omega_k$	2	-19.368 ± 0.048	2.0σ	1.9σ	~	-17.26	-13.26	~	1 😐
EDE	ა	$-19.390_{-0.035}^{+0.016}$	3.0σ	1.0σ	V	-21.98	-10.98	V	V ®
NEDE	3	$-19.380\substack{+0.023\\-0.040}$	3.1σ	1.9σ	~	-18.93	-12.93	~	 ✓ ②
EMG	3	$-19.397\substack{+0.017\\-0.023}$	3.7σ	2.3σ	~	-18.56	-12.56	~	 ✓ ②
CPL	2	-19.400 ± 0.020	3.7σ	4.1σ	\boldsymbol{X}	-4.94	-0.94	\boldsymbol{X}	X
PEDE	0	-19.349 ± 0.013	2.7σ	2.8σ	~	2.24	2.24	X	X
GPEDE	1	-19.400 ± 0.022	3.6σ	4.6σ	\boldsymbol{X}	-0.45	1.55	X	X
$\rm DM \rightarrow \rm DR + \rm WDM$	2	-19.420 ± 0.012	4.5σ	4.5σ	X	-0.19	3.81	X	X
$\rm DM \rightarrow \rm DR$	2	-19.410 ± 0.011	4.3σ	4.5σ	X	-0.53	3.47	X	X

Table 1: Test of the models based on dataset $\mathcal{D}_{\text{baseline}}$ (Planck 2018 + BAO + Pantheon), using the direct measurement of M_b by SH0ES for the quantification of the tension (3rd column) or the computation of the AIC (5th column). Eight models pass at least one of these three tests at the 3σ level.

H0 Olympics: 2107.10291

5% increase in all masses at recombination helps with H0 Sekiguchi & Takahashi 2007.03381

CMB does not change (except small nonequilibrium effects) if:

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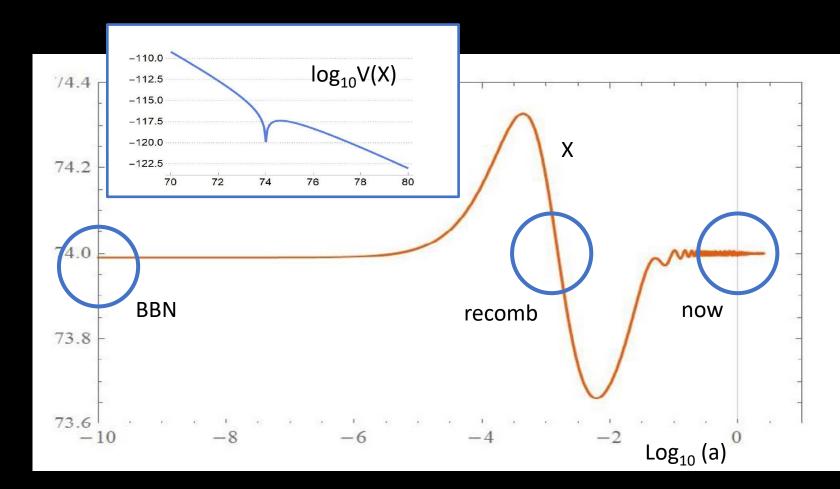
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Leaves BAO unchanged if small spatial curvature $\Lambda = 1.5 \Lambda$

$$\Delta_h = 1.5 \Delta_{m_e} \quad \omega_k = -0.125 \Delta_{m_e}$$

Requires 10% reduction in τ ; equal abundance-shifts automatic

Dilaton evolution constrained because it changes particle masses relative to the Planck mass, leaving mass ratios unchanged



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But it is robust properties like accidental scale invariance and supersymmetric gravity sector that are informative

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Thanks for your time & attention!

