



# Probing heavy New Physics through entanglement at the LHC

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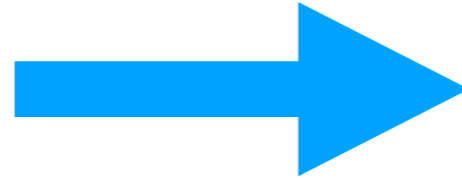
**Luca Mantani**

In collaboration with:  
R. Aoude, E. Madge, F. Maltoni



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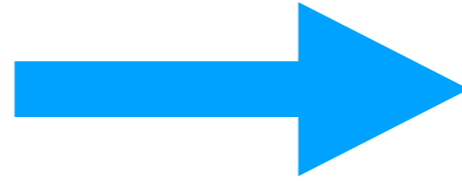
**Quantum Information**



Unveil the inner behaviour  
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Entanglement is a pure quantum phenomenon.  
A measurement at the high energies of the LHC would be a first.

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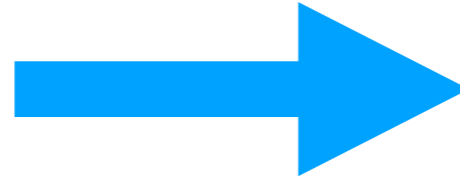


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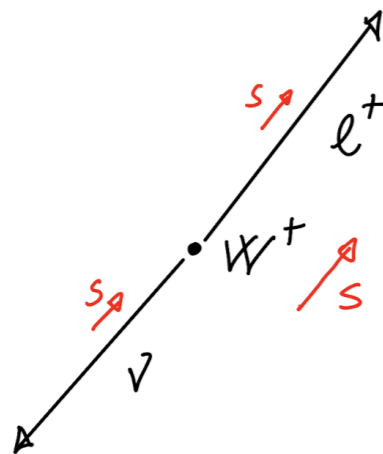


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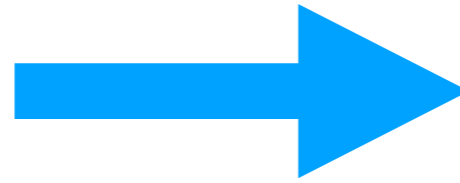
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lepton decays along W spin



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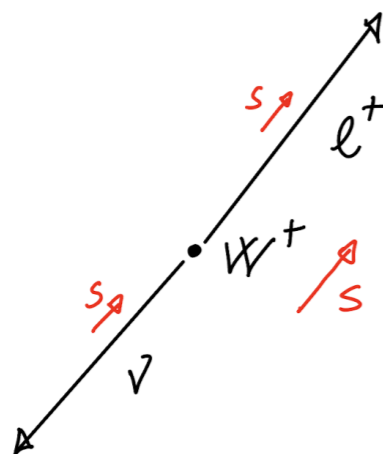


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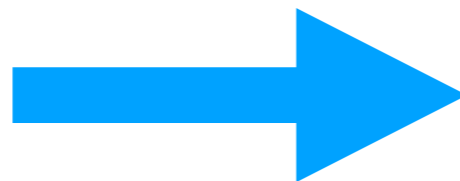


Top decay:  
lepton decay correlated with top spin

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \phi} = \frac{1 + \cos \phi}{2}$$

$\phi$  angle between lepton and spin

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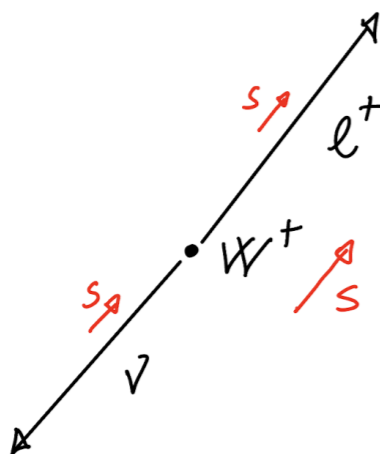


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**Z boson more complicated but doable:  
spin can be reco if right/left asymmetry**

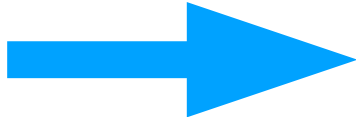
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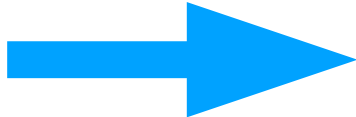
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**Maximally entangled states: spin 1/2**

$$|\Phi^\pm\rangle = \frac{|\uparrow\uparrow\rangle \pm |\downarrow\downarrow\rangle}{\sqrt{2}} \quad |\Psi^\pm\rangle = \frac{|\uparrow\downarrow\rangle \pm |\downarrow\uparrow\rangle}{\sqrt{2}}$$

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In the case of a statistical ensemble (mixed state)

$$\rho = \sum_k p_k \rho_k \quad \text{entangled if } \rho_k \neq \rho_1 \otimes \rho_2$$

The fundamental object to study quantum observables is the spin density matrix

One particle of spin  $s$ :  
 $d=2s+1$


$$\rho = \frac{1}{d} \mathbb{I} + \sum_{i=1}^{d^2-1} a_i \lambda_i$$

 Generalised Gell-Mann matrix

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**The parameters completely characterise the quantum spin state of the system**

We define the R-matrix

$$R_{\alpha_1 \alpha_2, \beta_1 \beta_2}^I \equiv \frac{1}{N_a N_b} \sum_{\substack{\text{colors} \\ \text{a,b spins}}} \mathcal{M}_{\alpha_2 \beta_2}^* \mathcal{M}_{\alpha_1 \beta_1}$$

Sum over initial state only

$$\mathcal{M}_{\alpha\beta} \equiv \langle t(k_1, \alpha) \bar{t}(k_2, \beta) | \mathcal{T} | a(p_1) b(p_2) \rangle$$

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$$\rho = \frac{R}{\text{tr}(R)}$$



The R matrix can be decomposed in the spin space

$$R = \tilde{A} \mathbb{1}_2 \otimes \mathbb{1}_2 + \tilde{B}_i^+ \sigma^i \otimes \mathbb{1}_2 + \tilde{B}_i^- \mathbb{1}_2 \otimes \sigma^i + \tilde{C}_{ij} \sigma^i \otimes \sigma^j$$

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**Cross section**

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### Spin correlations

If normalised, we define the density matrix of the system

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Concurrence

$$\mathcal{C}(\rho) = \inf \left[ \sum_i p_i c(|\psi_i\rangle) \right] \quad \text{Entangled if } > 0$$

$$(\mathcal{C}(\rho))^2 \geq 2 \max(0, \text{Tr}[\rho^2] - \text{Tr}[\rho_A^2], \text{Tr}[\rho^2] - \text{Tr}[\rho_B^2]) \equiv \mathcal{C}_{\text{LB}}^2$$

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**Bell inequality**

$$\langle \mathcal{B} \rangle_{\text{max}} = \max_{U,V} \left( \text{Tr} \left( \rho (U^\dagger \otimes V^\dagger) \mathcal{B} (U \otimes V) \right) \right) \geq 2$$

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{1}{\Lambda} \mathcal{O}_i^5 + \sum_i \frac{1}{\Lambda^2} \mathcal{O}_i^6 + \dots$$

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- ❖ **Higher dimensional operators preserve SM symmetries.**
- ❖ **Mappable to a large class of BSM models.**
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**EFT to-do list**

- ❖ **Define target operators: e.g. top-philic EFT** [[arXiv:1802.07237](https://arxiv.org/abs/1802.07237)]
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## The density matrix opens the window to new sensitivities

$$e^+ e^- \rightarrow W^+ W^-$$

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$+ - 00$	$-2\sqrt{2}G_F m_Z^2 \sin \theta$	-
$+ - - +$	$2\sqrt{2}G_F m_W^2 \sin \theta$	-
$+ - + -$	$-\frac{1}{\sqrt{2}}G_F m_W^2 \sin^3 \theta \csc^4(\theta/2)$	-
$+ - \pm \pm$	-	$3 \cdot 2^{1/4} \sqrt{G_F} m_W \sin \theta (4m_W^2 x^2 - m_Z^2)$
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$$\tilde{a}_1(\mathcal{O}_W) \simeq \tilde{b}_1(\mathcal{O}_W) \simeq \bar{c}_W 2^{5/4} x \cos^4(\theta/2) (\cos \theta + 3) \csc \theta,$$

**Resurrected sensitivity: energy growth!**

Top pairs ideal probe: spin correlations preserved after decay

$$R_{\alpha_1\alpha_2,\beta_1\beta_2}^I \equiv \frac{1}{N_a N_b} \sum_{\substack{\text{colors} \\ \text{a,b spins}}} \mathcal{M}_{\alpha_2\beta_2}^* \mathcal{M}_{\alpha_1\beta_1}$$

At LO in QCD

$$I = gg, q\bar{q}$$

[arXiv: 2203.05619]

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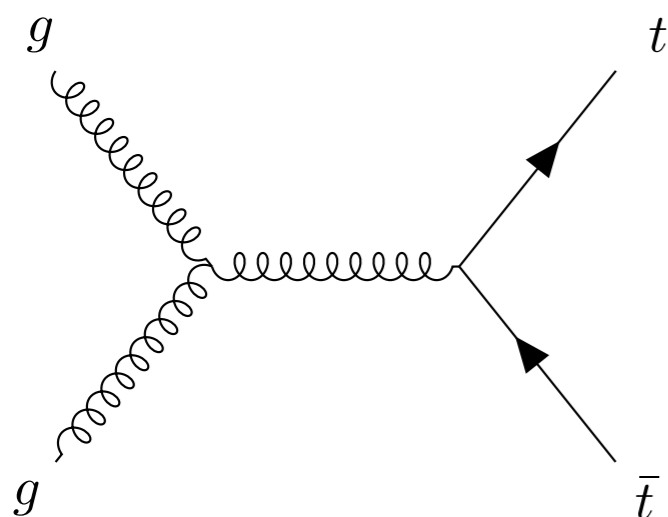
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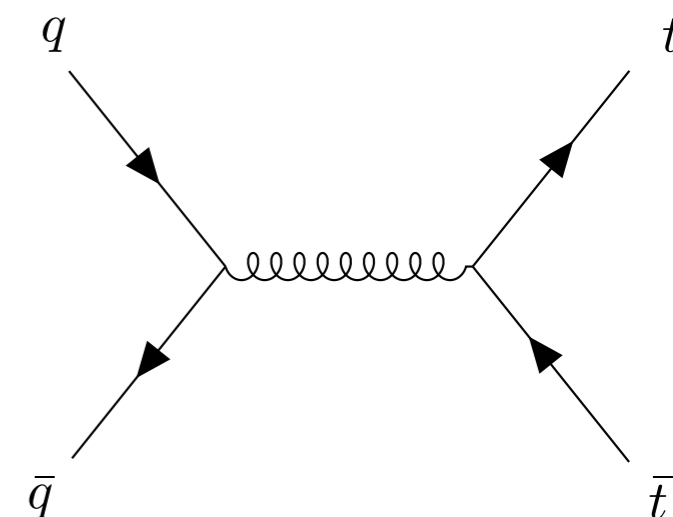
At LO in QCD

$$I = gg, q\bar{q}$$

[arXiv: 2203.05619]



We collide protons



Top pairs ideal probe: spin correlations preserved after decay

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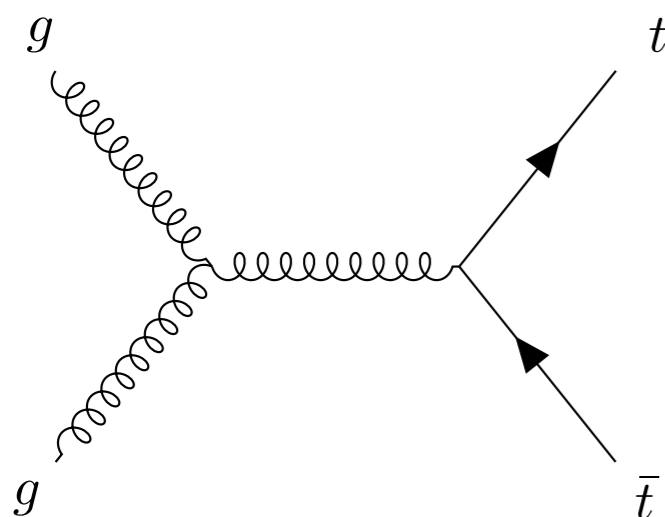
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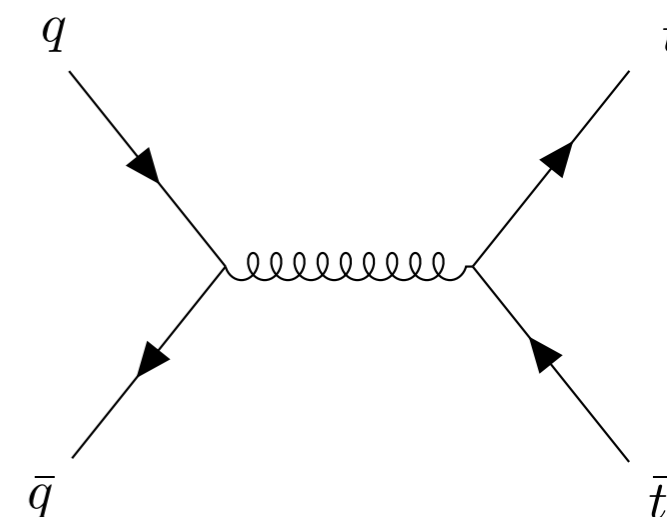
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We collide protons



$$R(\hat{s}, \mathbf{k}) = \sum_I L^I(\hat{s}) R^I(\hat{s}, \mathbf{k})$$

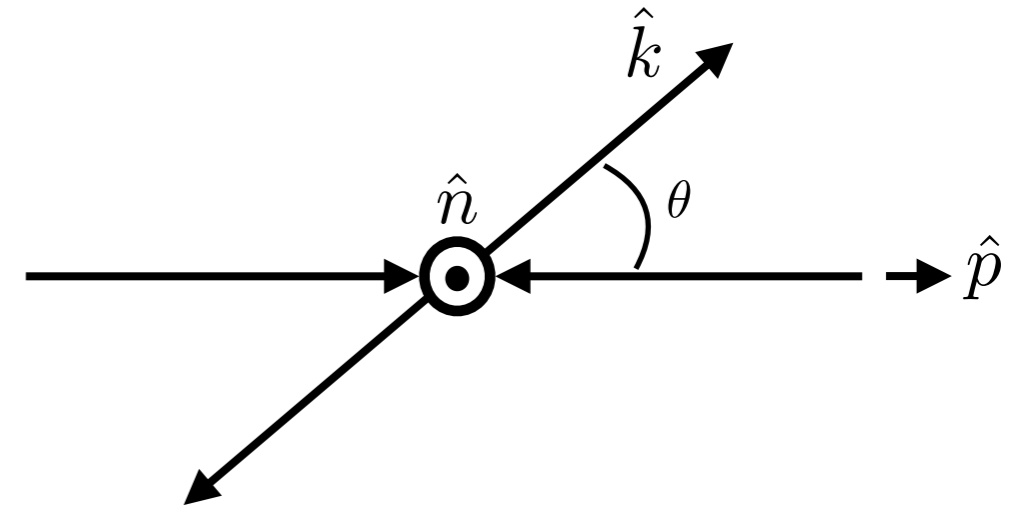


Full correlation matrix is mixed state, weighted by parton luminosity

$$\{\mathbf{k}, \mathbf{n}, \mathbf{r}\} : \mathbf{r} = \frac{(\mathbf{p} - z\mathbf{k})}{\sqrt{1 - z^2}}, \quad \mathbf{n} = \mathbf{k} \times \mathbf{r},$$

To expand in this basis, e.g.

$$C_{nn} = \text{tr}[C_{ij} \mathbf{n} \otimes \mathbf{n}]$$



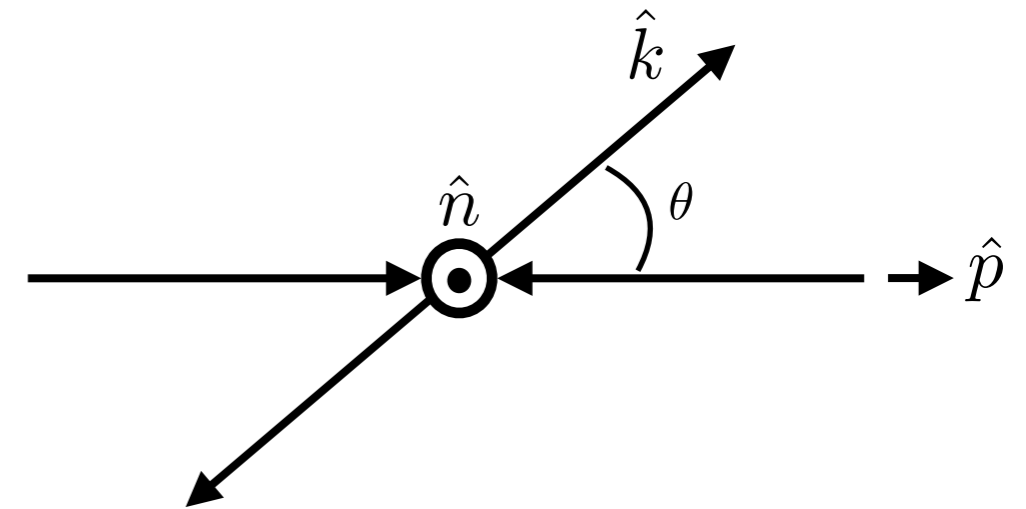
$$\beta^2 = (1 - 4m_t^2 / \hat{s})$$

$$\cos \theta$$

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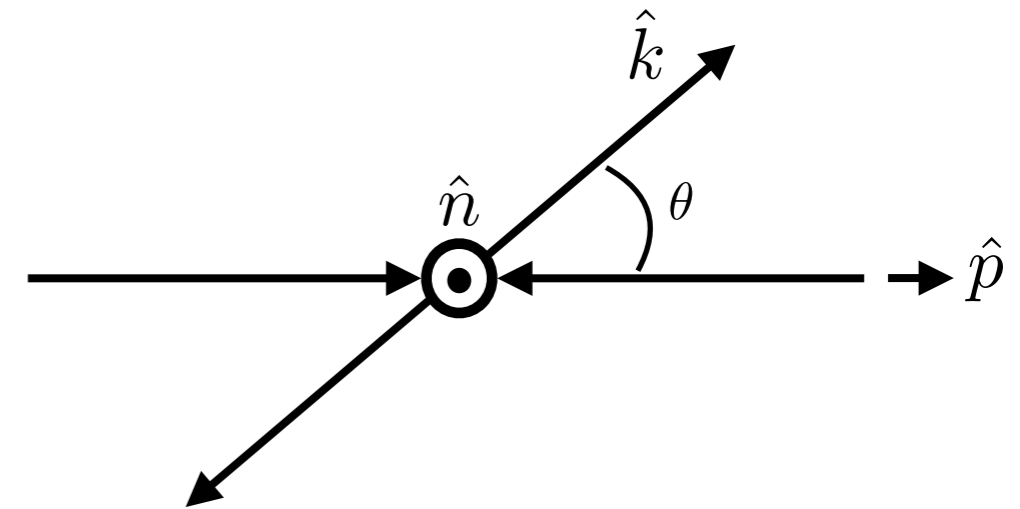
Operative definition of entanglement:

$$\Delta = -C_{nn} + |C_{kk} + C_{rr}| - 1 > 0 \quad \text{entangled}$$

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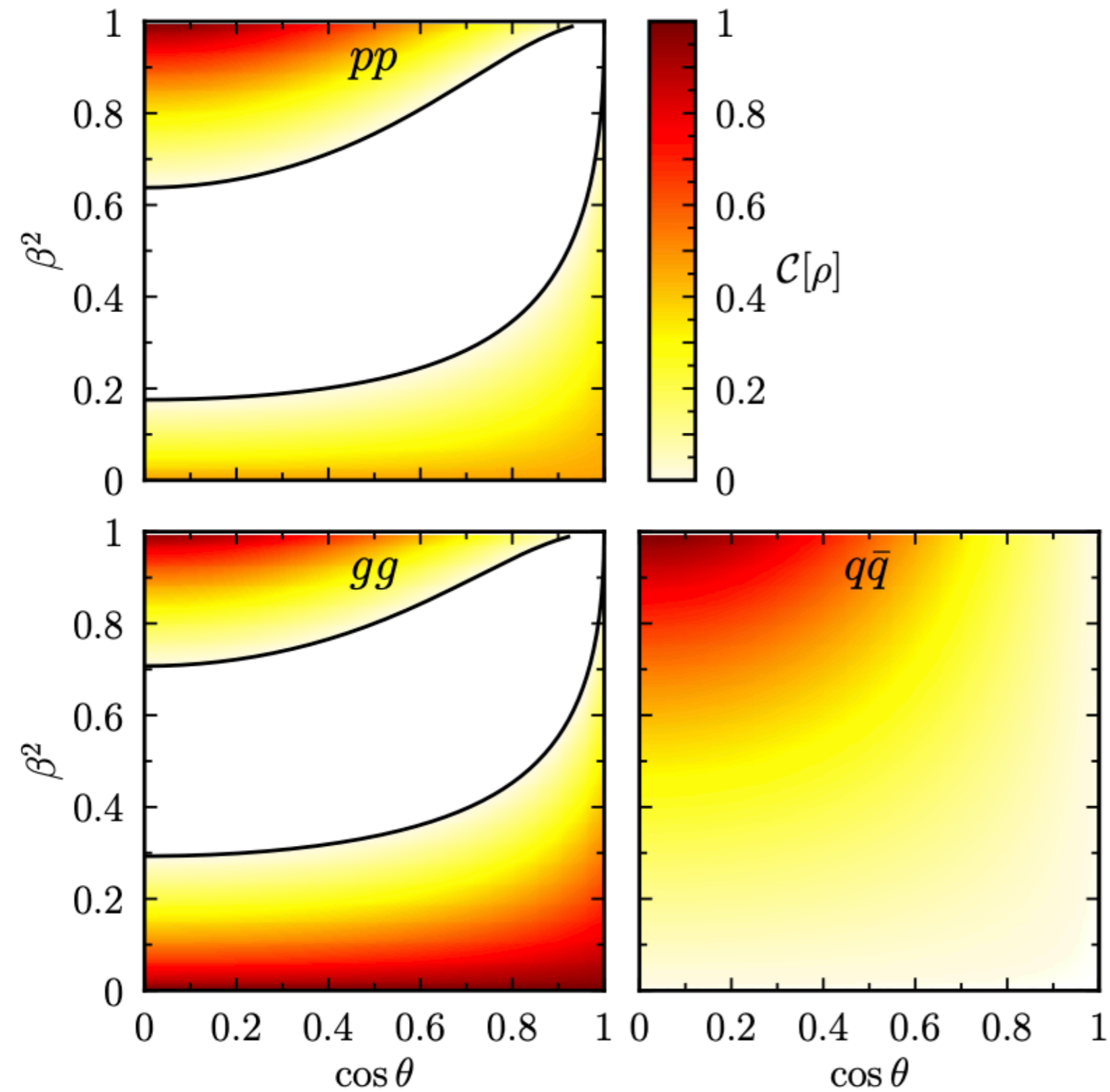
**We can then define the concurrence**

$$C[\rho] = \max(\Delta/2, 0)$$

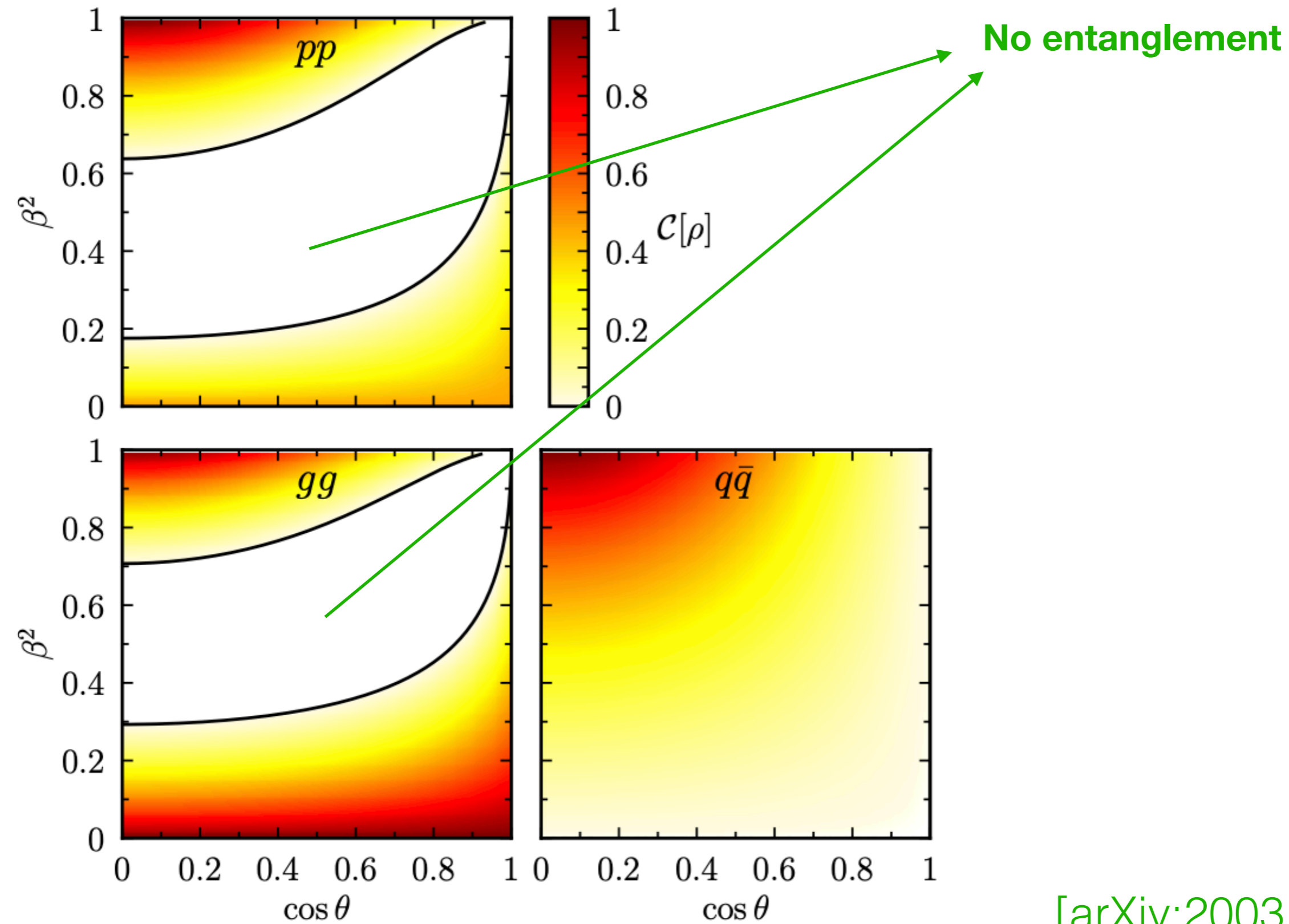
$$C[\rho] = 1$$

Max entanglement

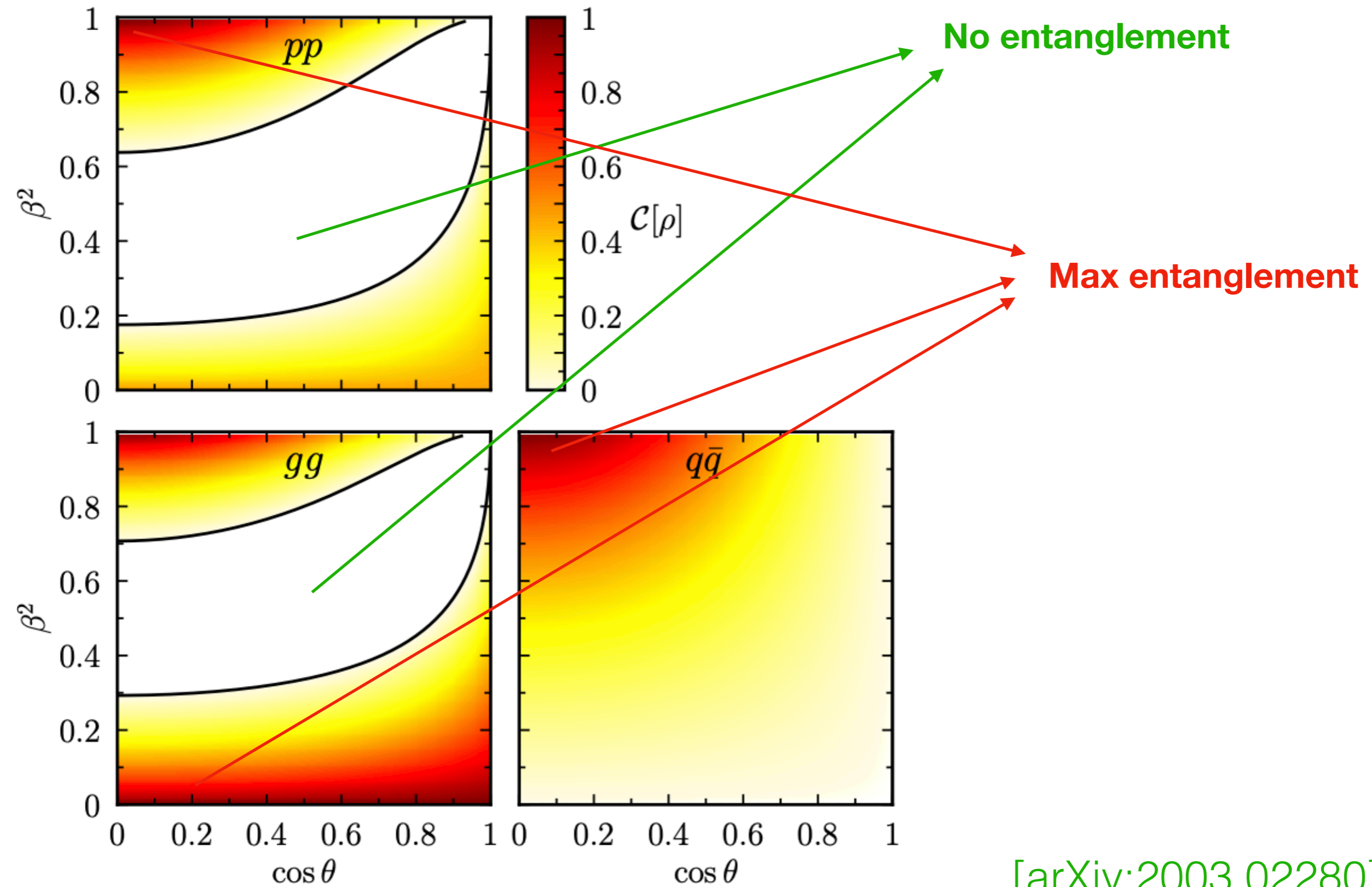




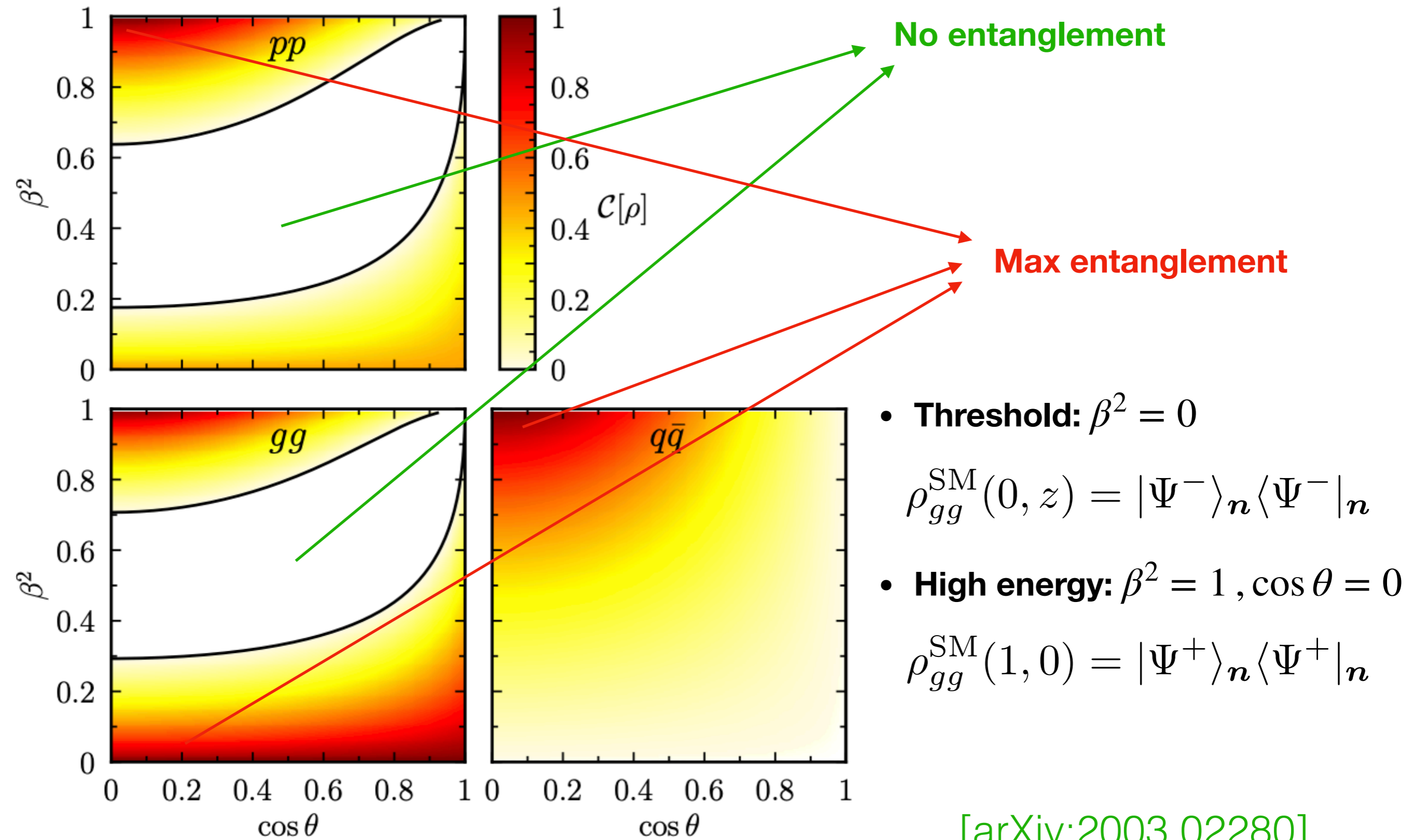
[arXiv:2003.02280]



[arXiv:2003.02280]



[arXiv:2003.02280]



- **Threshold:**  $\beta^2 = 0$

$$\rho_{gg}^{\text{SM}}(0, z) = |\Psi^-\rangle_{\mathbf{n}} \langle \Psi^-|_{\mathbf{n}}$$

- **High energy:**  $\beta^2 = 1, \cos \theta = 0$

$$\rho_{gg}^{\text{SM}}(1, 0) = |\Psi^+\rangle_{\mathbf{n}} \langle \Psi^+|_{\mathbf{n}}$$

[arXiv:2003.02280]

$$R_{\alpha_1 \alpha_2, \beta_1 \beta_2}^I \equiv \frac{1}{N_a N_b} \sum_{\substack{\text{colors} \\ \text{a,b spins}}} \mathcal{M}_{\alpha_2 \beta_2}^* \mathcal{M}_{\alpha_1 \beta_1}$$

$$\mathcal{M}_{\alpha\beta} = \mathcal{M}_{\alpha\beta}^{\text{SM}} + \frac{1}{\Lambda^2} \mathcal{M}_{\alpha\beta}^{(\text{d6})} \quad \longrightarrow \quad \rho = \frac{R^{\text{SM}} + R^{\text{EFT}}}{\text{tr}(R^{\text{SM}}) + \text{tr}(R^{\text{EFT}})}$$

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At  $\mathcal{O}(1/\Lambda^2)$

$$\tilde{A}^{gg,(1)} = \frac{g_s^2}{\Lambda^2} \frac{1}{1 - \beta^2 z^2} \left[ \frac{g_s^2 v m_t (9\beta^2 z^2 + 7)}{12\sqrt{2}} c_{tG} - \frac{\beta^2 m_t^4}{4m_t^2 - (1 - \beta^2)m_h^2} c_{\varphi G} + \frac{9g_s^2 \beta^2 m_t^2 z^2}{8} c_G \right],$$

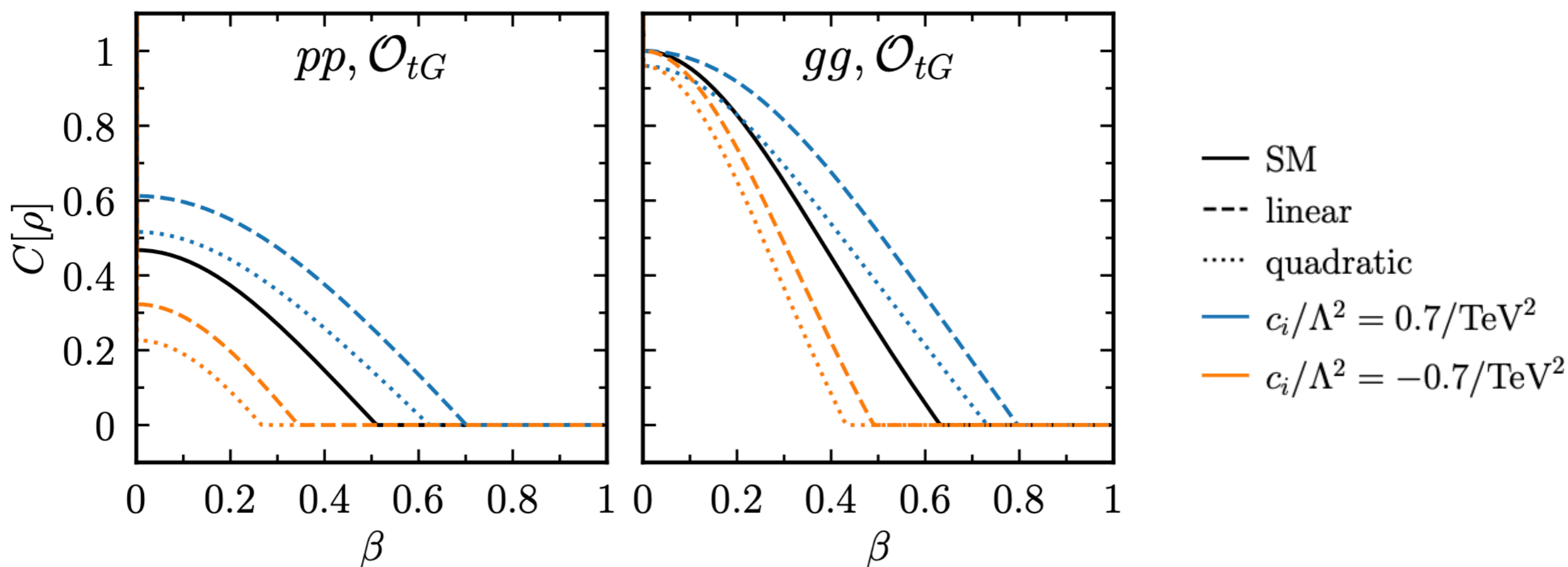
$$\tilde{C}_{nn}^{gg,(1)} = \frac{g_s^2}{\Lambda^2} \frac{1}{1 - \beta^2 z^2} \left[ \frac{-7g_s^2 v m_t}{12\sqrt{2}} c_{tG} - \frac{\beta^2 m_t^4}{4m_t^2 - (1 - \beta^2)m_h^2} c_{\varphi G} + \frac{9g_s^2 \beta^2 m_t^2 z^2}{8} c_G \right],$$

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$$\bar{R} = (4\pi)^{-1} \int d\Omega R(\hat{s}, \mathbf{k}), \quad \longrightarrow \quad \begin{aligned} \delta &\equiv -C_z + |2C_\perp| - 1 > 0 \\ C[\rho] &= \max(\delta/2, 0) \end{aligned}$$

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**gg-induced**

$$\rho_{gg}^{\text{EFT}}(0, z) = p_{gg} |\Psi^+\rangle_{\mathbf{p}} \langle \Psi^+|_{\mathbf{p}} + (1 - p_{gg}) |\Psi^-\rangle_{\mathbf{p}} \langle \Psi^-|_{\mathbf{p}}$$

$$p_{gg} = \frac{72}{7\Lambda^4} m_t^2 (3\sqrt{2}m_t c_G + v c_{tG})^2 \quad \text{Only quadratic effects!}$$

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$$\rho_{q\bar{q}}^{\text{EFT}}(0, z) = p_{q\bar{q}} |\uparrow\uparrow\rangle_{\mathbf{p}} \langle \uparrow\uparrow|_{\mathbf{p}} + (1 - p_{q\bar{q}}) |\downarrow\downarrow\rangle_{\mathbf{p}} \langle \downarrow\downarrow|_{\mathbf{p}}$$

$$p_{q\bar{q}} = \frac{1}{2} - 4 \frac{c_{VA}^{(8),u}}{\Lambda^2} + \frac{8m_t^4}{\Lambda^4} \left( \frac{v\sqrt{2}}{m_t} c_{VA}^{(8),u} c_{tG} - 9c_{VA}^{(1),u} c_{VV}^{(1),u} + 2c_{VA}^{(8),u} c_{VV}^{(8),u} \right)$$

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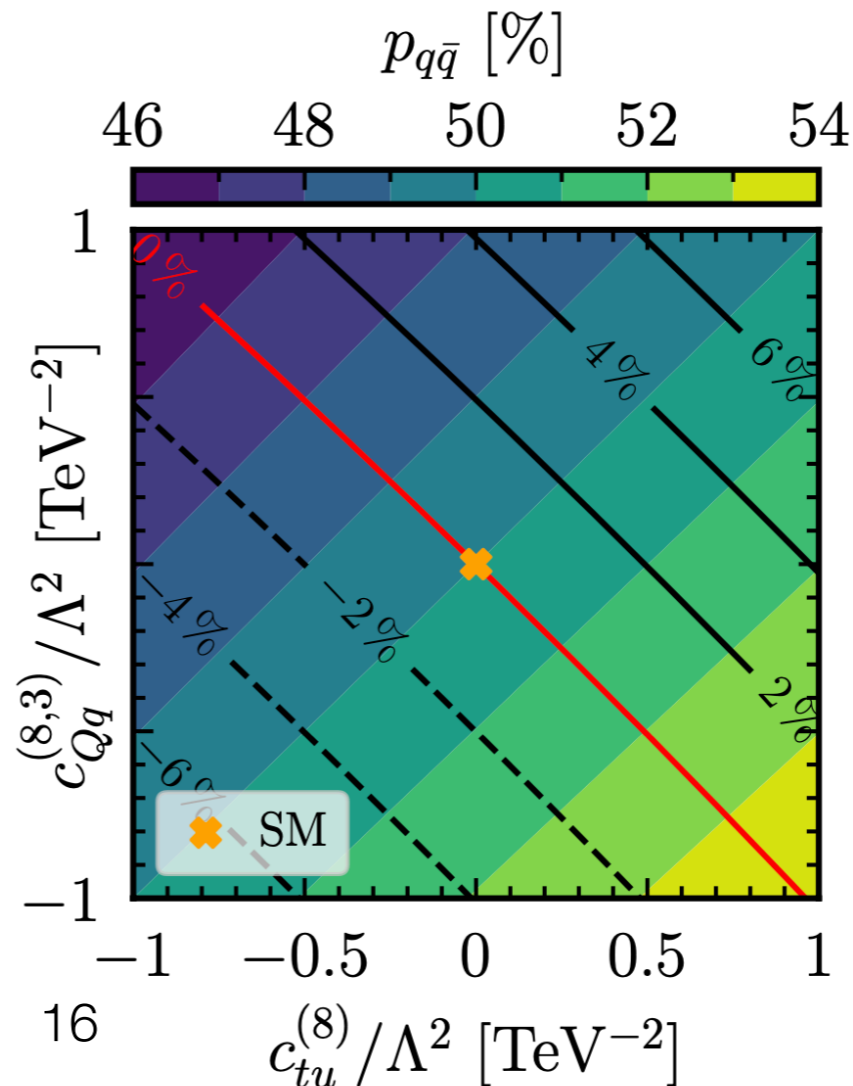
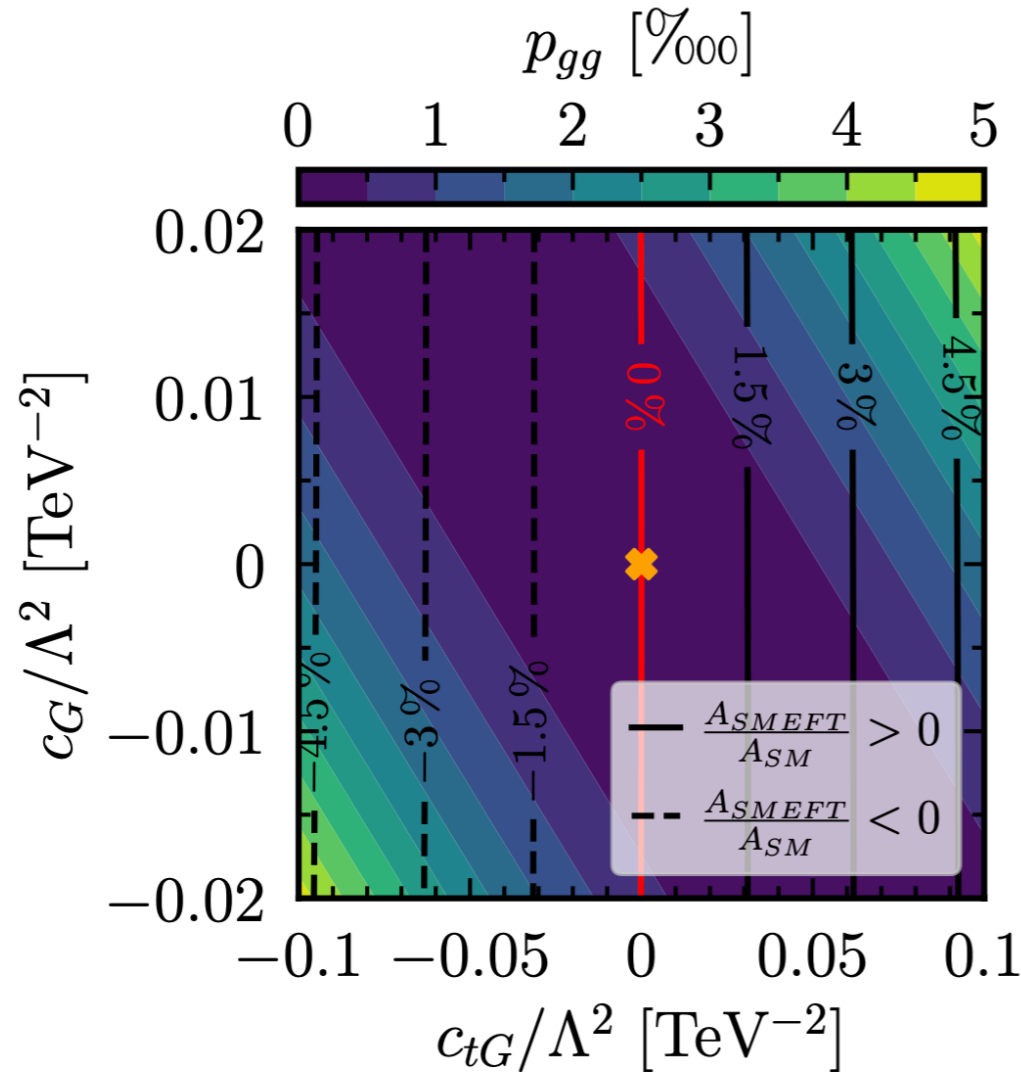
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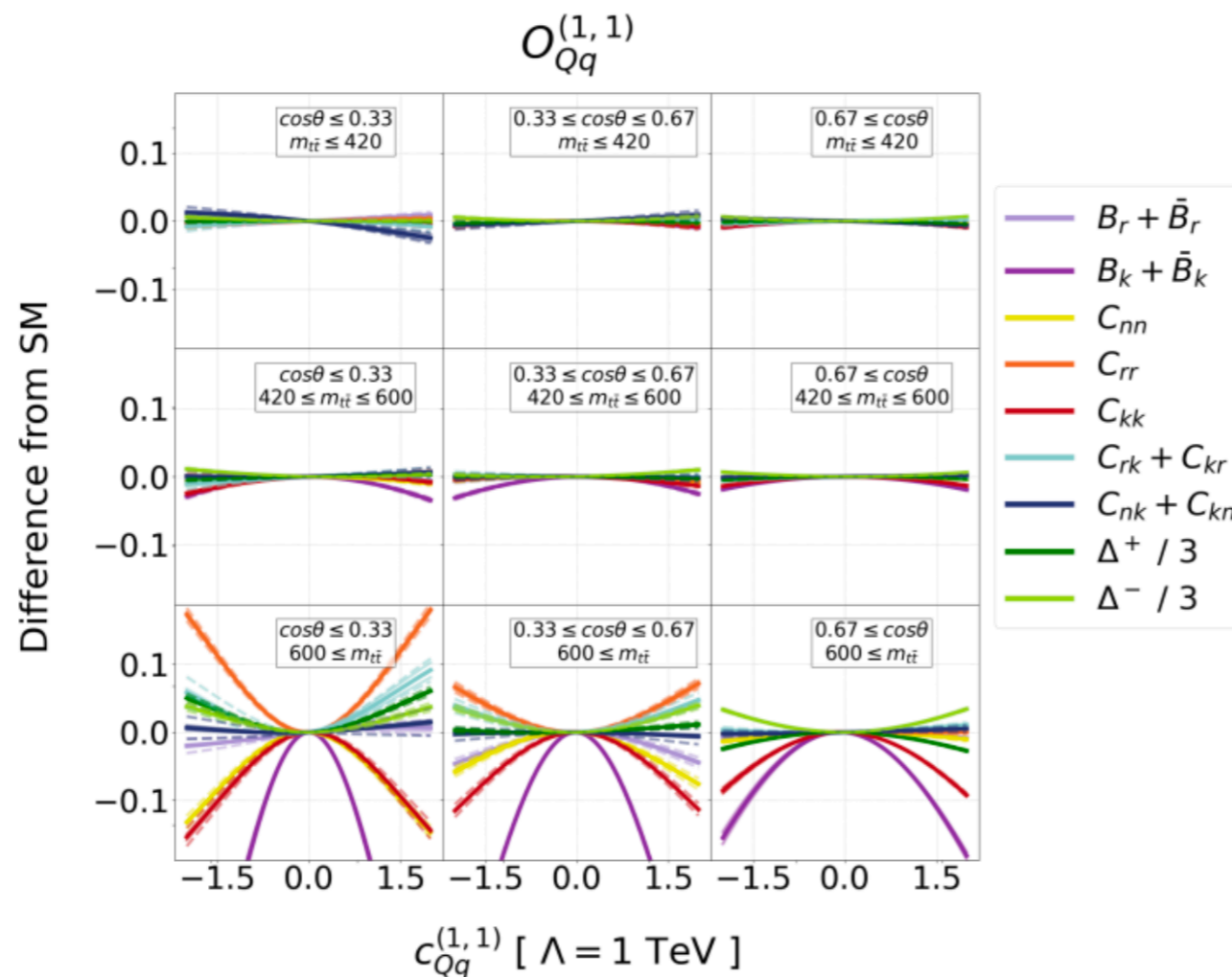
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Stolen slide

[arXiv:2210.09330]

The structure of spin correlations in phase space makes a differential measurement ~ 10x more effective than an inclusive one.



Quantum observables and spin correlations in general will yield remarkable improvements to BSM searches and SMEFT global fits.

[\[arXiv: 2307.10370\]](#) Diboson production is also a promising candidate:  
**broad sensitivity to SMEFT operators**

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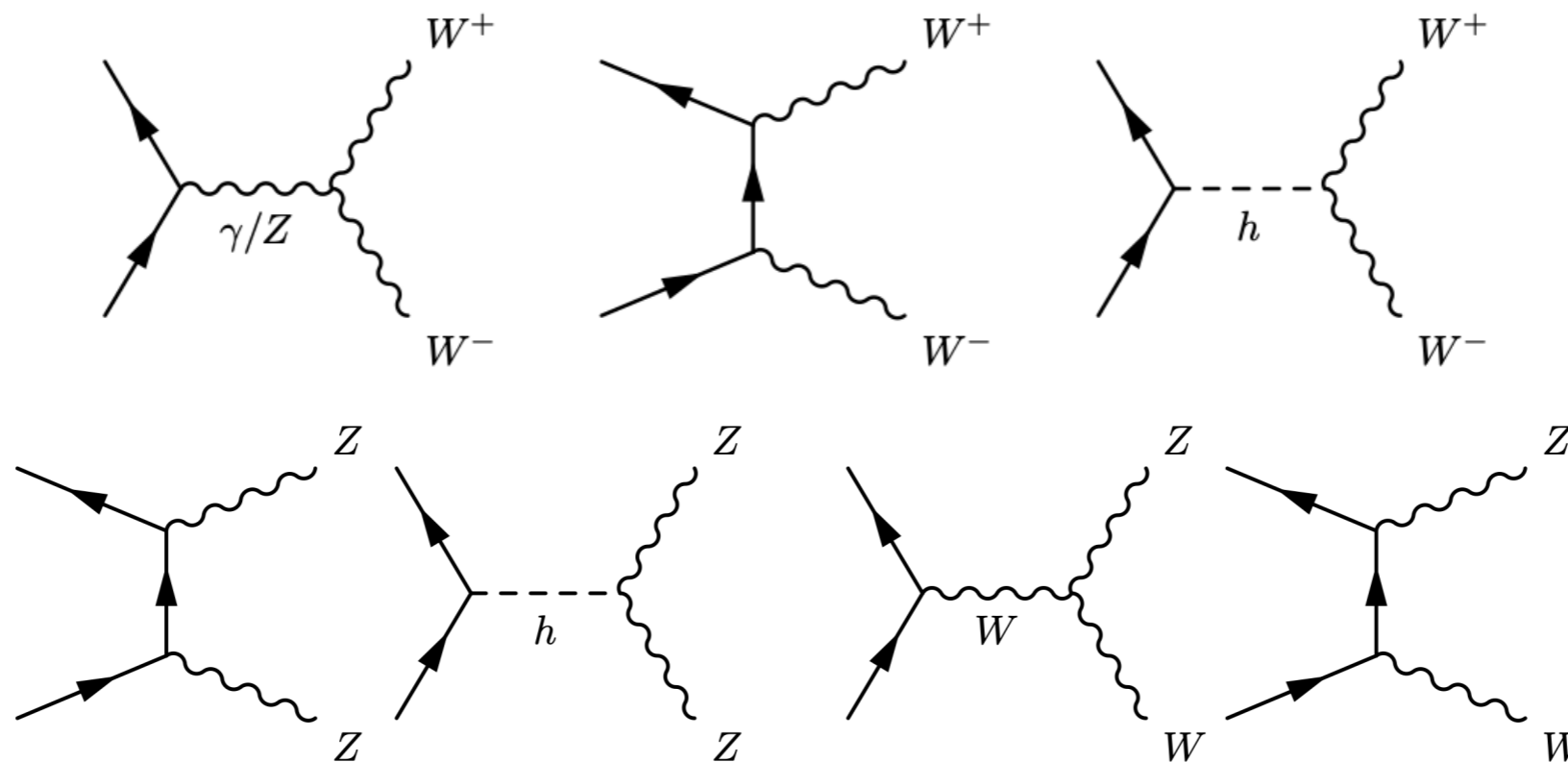
$$\rho = \frac{1}{9} \mathbb{I} \otimes \mathbb{I} + \frac{1}{3} \sum_{i=1}^8 a_i \lambda_i \otimes \mathbb{I} + \frac{1}{3} \sum_{j=1}^8 b_j \mathbb{I} \otimes \lambda_j + \sum_{i=1}^8 \sum_{j=1}^8 c_{ij} \lambda_i \otimes \lambda_j$$

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We studied both lepton and hadron collider



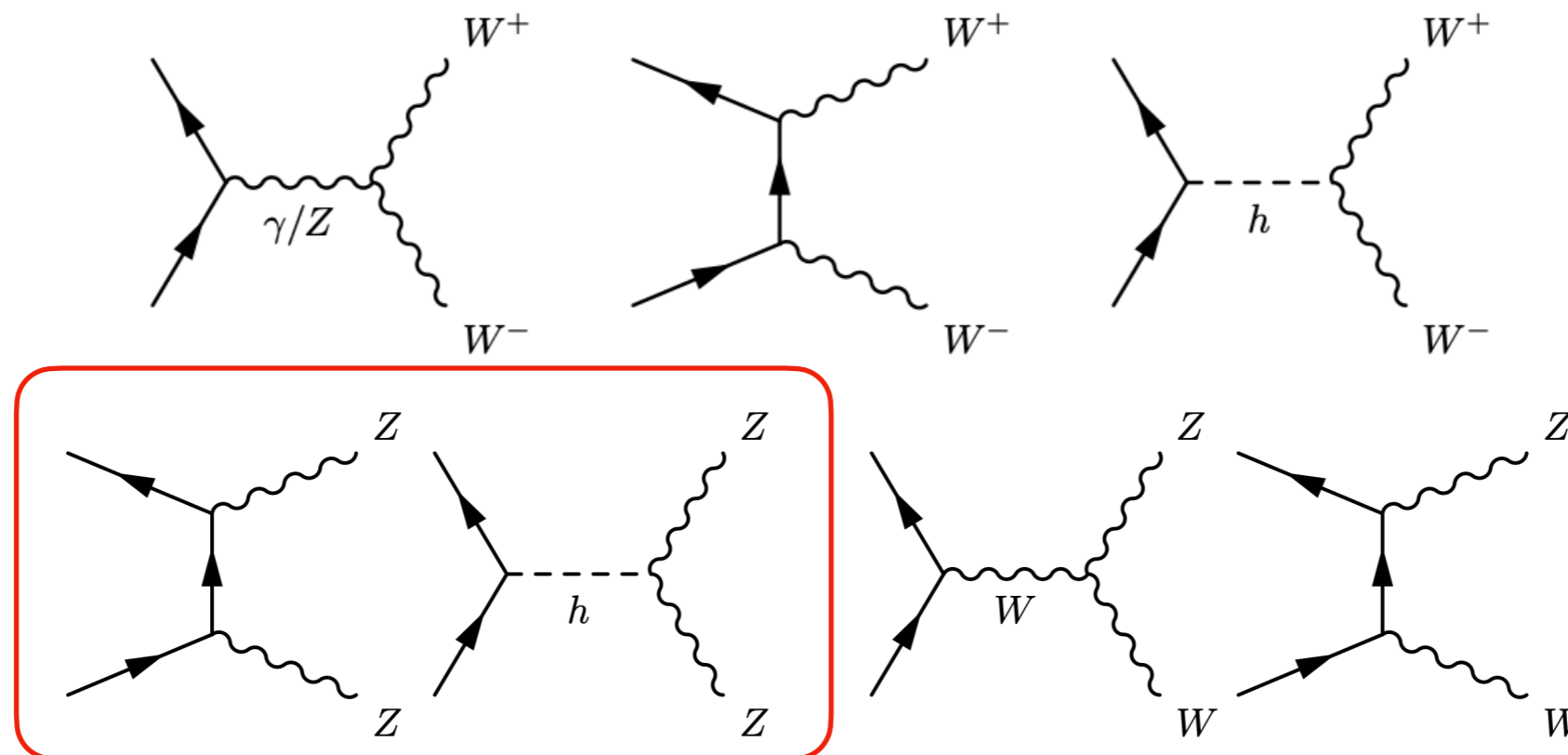
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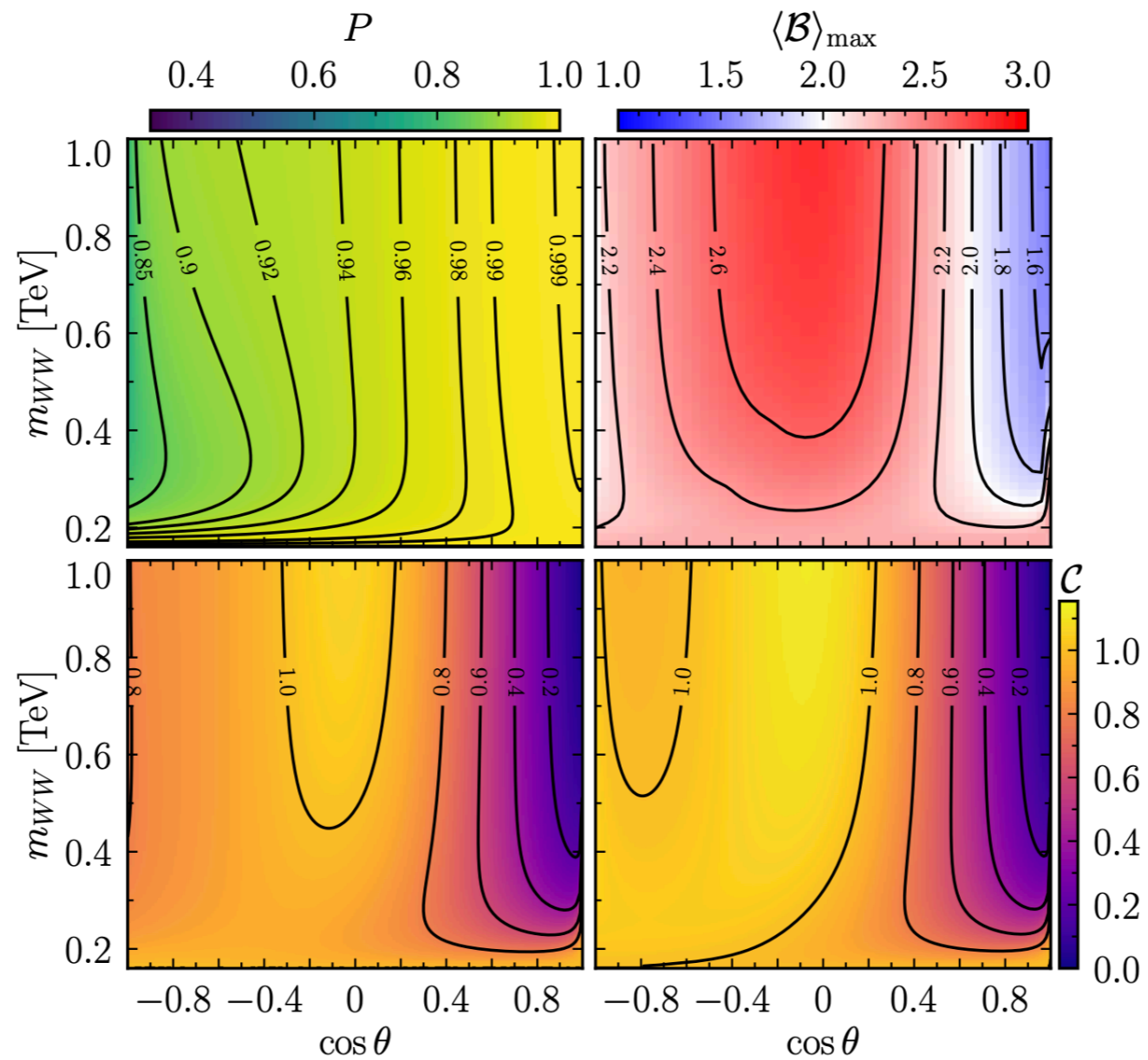
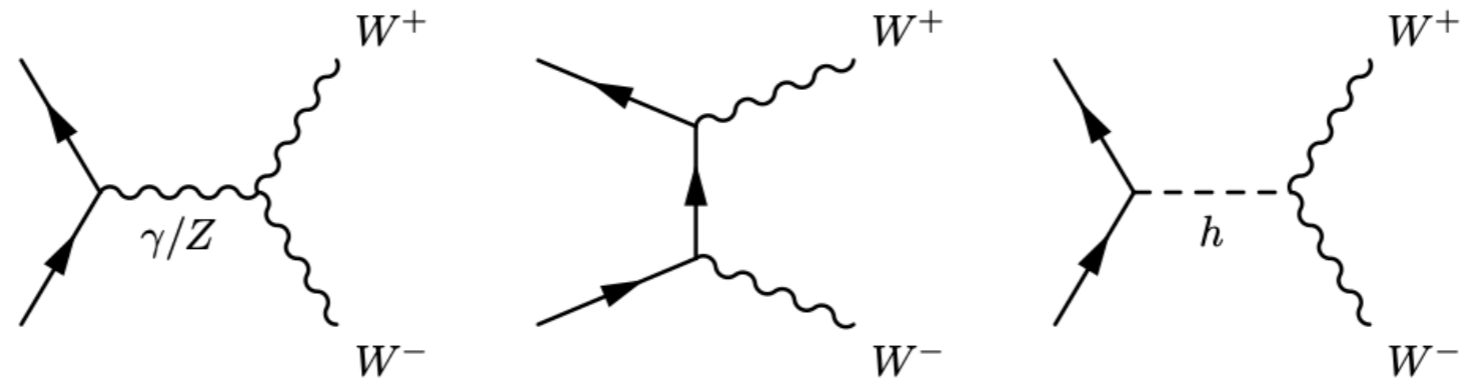
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We studied both lepton and hadron collider

Not very sensitive





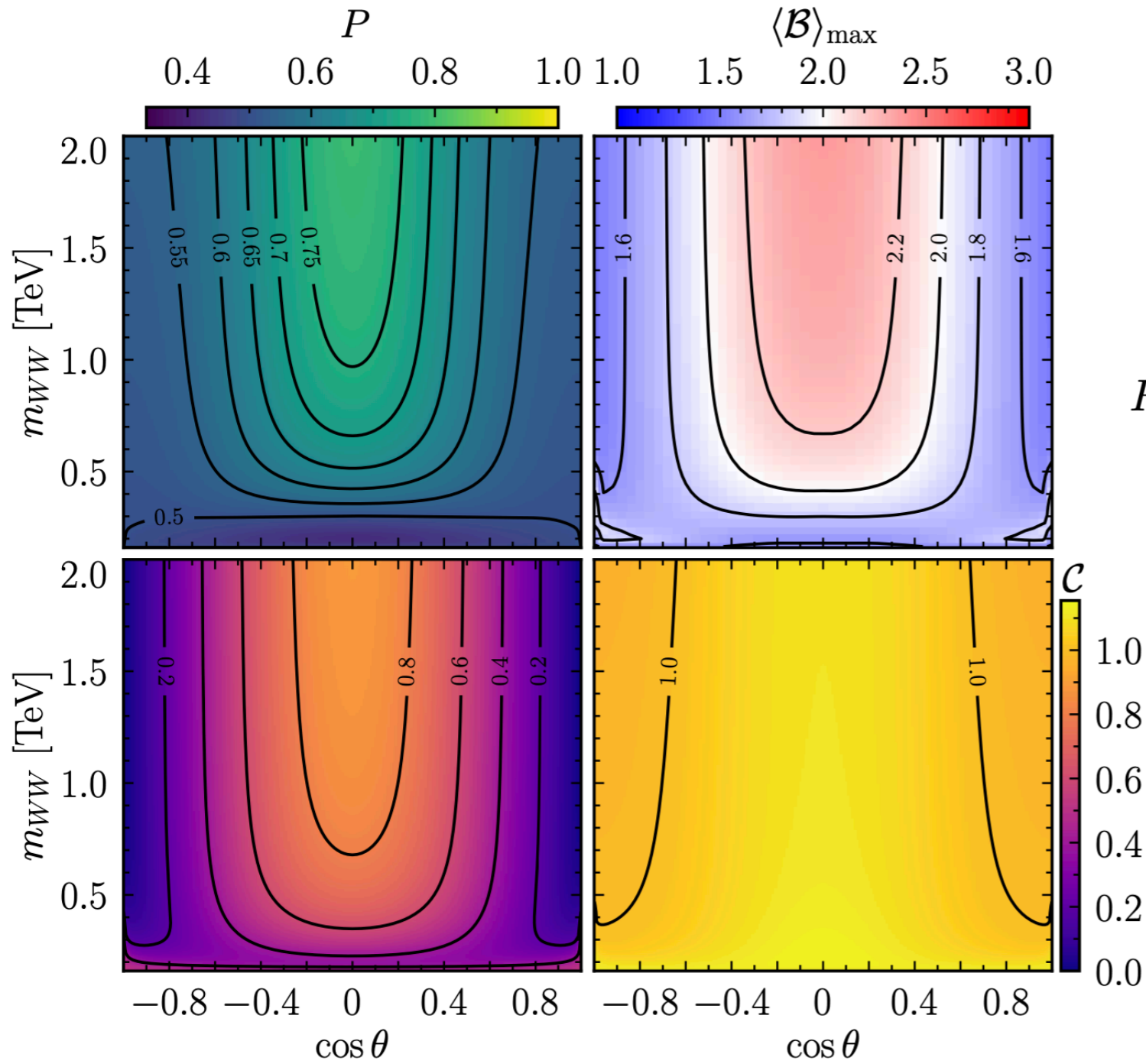


$$e^+ e^- \rightarrow W^+ W^-$$



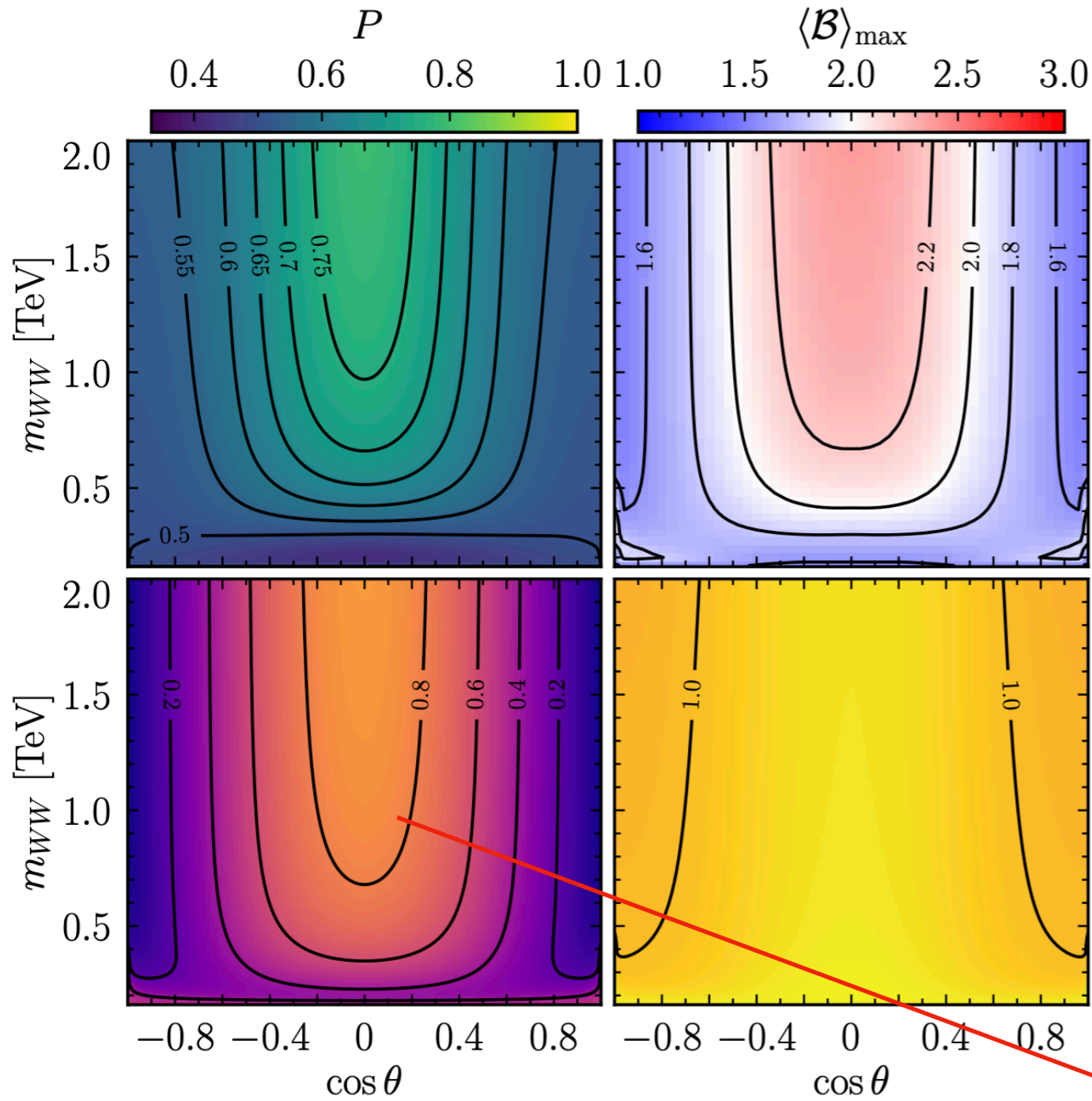






Milder signs due to the initial state mixing

$$R(\hat{s}, \theta) = \sum_q L^{q\bar{q}}(\hat{s}) (R^{q\bar{q}}(\hat{s}, \theta) + R^{q\bar{q}}(\hat{s}, \theta + \pi))$$

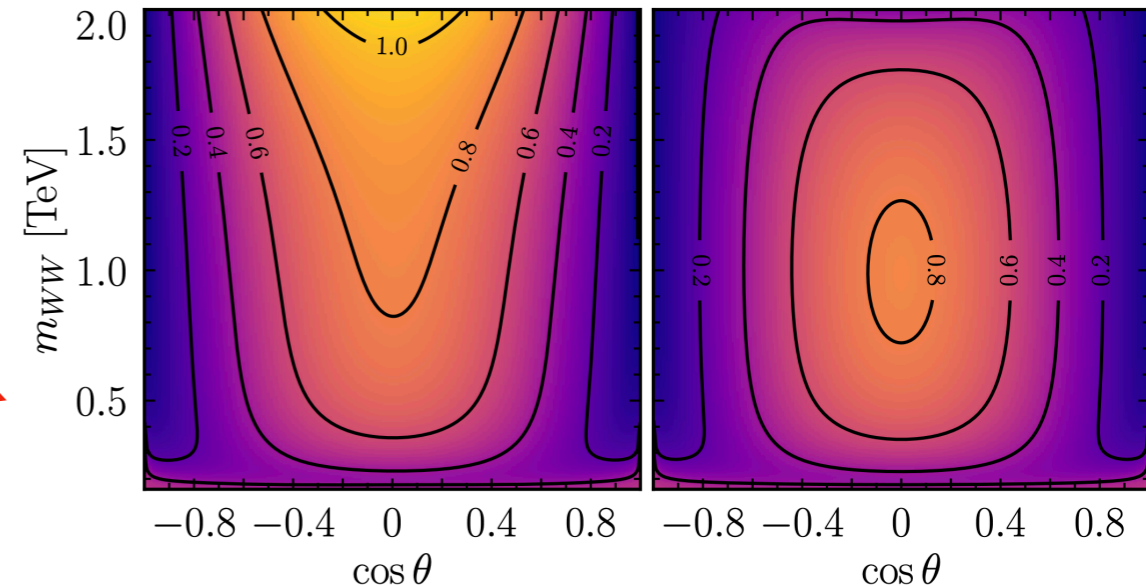


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$$c_{\varphi q}^{(3)} = 0.05 \text{ TeV}^{-2}$$

$$c_W = 0.03 \text{ TeV}^{-2}$$



How do we reconstruct the spin density matrix at colliders?

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**Quantum tomography**

Measure angular distributions of the decay products



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### Quantum tomography

Measure angular distributions of the decay products

For example, for the density matrix of a W boson [\[arXiv: 2209.13990\]](#)

$$\Phi_1^{P\pm} = \sqrt{2}(5 \cos \theta \pm 1) \sin \theta \cos \phi$$

$$\Phi_5^{P\pm} = 5 \sin^2 \theta \sin 2\phi$$

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$$a_j = \frac{1}{2} \int d\Omega_{\hat{\mathbf{n}}} p(\ell_{\hat{\mathbf{n}}}^{\pm}; \rho) \Phi_j^{P\pm}$$

Expectation value  
of the Wigner P functions

$$c_{ij} = \left(\frac{1}{2}\right)^2 \iint d\Omega_{\hat{\mathbf{n}}_1} d\Omega_{\hat{\mathbf{n}}_2} p(\ell_{\hat{\mathbf{n}}_1}^+, \ell_{\hat{\mathbf{n}}_2}^-; \rho) \Phi_i^P(\hat{\mathbf{n}}_1) \Phi_j^P(\hat{\mathbf{n}}_2)$$

In the case of top pair things are simpler

[\[arXiv: 2003.02280\]](#)

$$\frac{1}{\sigma} \frac{d\sigma}{d\Omega_+ d\Omega_-} = \frac{1 + \mathbf{B}^+ \cdot \hat{\mathbf{q}}_+ - \mathbf{B}^- \cdot \hat{\mathbf{q}}_- - \hat{\mathbf{q}}_+ \cdot \mathbf{C} \cdot \hat{\mathbf{q}}_-}{(4\pi)^2}$$

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Direction of decay  
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Spin density matrix coefficients

Interestingly, at threshold, a specific angular distributions is **directly proportional to the entanglement**

$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \varphi} = \frac{1}{2} (1 - D \cos \varphi)$$

$$D = \frac{\text{tr}[\mathbf{C}]}{3}$$

$$C[\rho] = \max(-1 - 3D, 0)/2$$

Angle between leptons

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Angle between leptons

**However not trivial!**

Despite high degree of entanglement in certain phase space,  
when integrating we wash out the effects: **design of optimal signal region needed.**



## ATLAS CONF Note

ATLAS-CONF-2023-069

28th September 2023



# Observation of quantum entanglement in top-quark pair production using $pp$ collisions of $\sqrt{s} = 13$ TeV with the ATLAS detector

entanglement detection is expected to be significant. The entanglement observable is measured in a fiducial phase-space with stable particles. The entanglement witness is measured to be  $D = -0.547 \pm 0.002$  (stat.)  $\pm 0.021$  (syst.) for  $340 < m_{t\bar{t}} < 380$  GeV. The large spread in predictions from several mainstream event generators indicates that modelling this property is challenging. The predictions depend in particular on the parton-shower algorithm used. The observed result is more than five standard deviations from a scenario without entanglement and hence constitutes the first observation of entanglement in a pair of quarks, and the observation of entanglement at the highest energy to date.



- ❖ Possibility to exploit quantum spin observables as entanglement proposed.
- ❖ Measurement of entanglement at LHC would be highest energy evidence ever.
- ❖ In the SM, specific spin configurations are expected, dictated by interactions.
- ❖ SMEFT effects induce presence of different quantum states, modifying the overall pattern.
- ❖ Quantum observables probe complementary directions to the cross-section in EFT param space and can resurrect the interference.

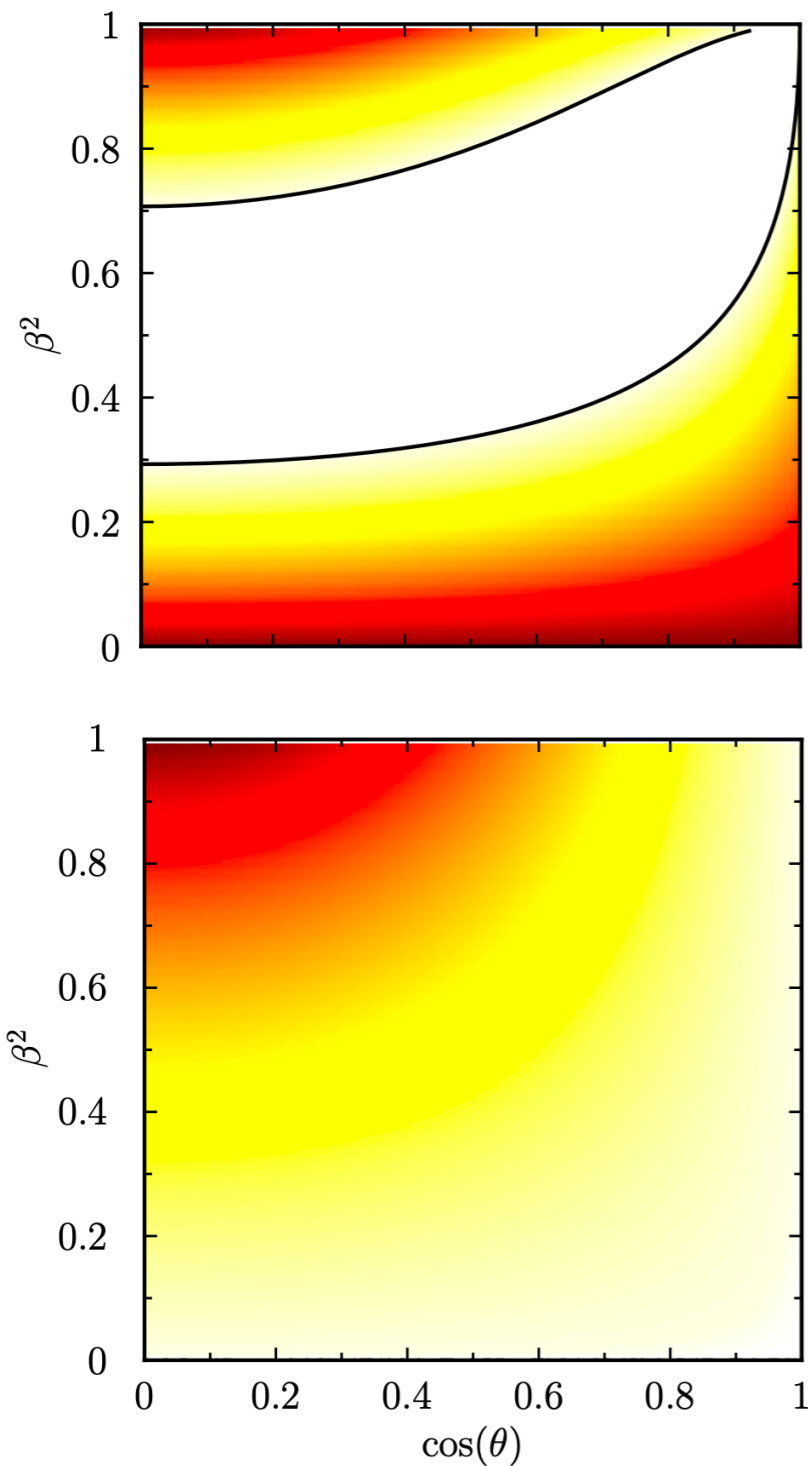
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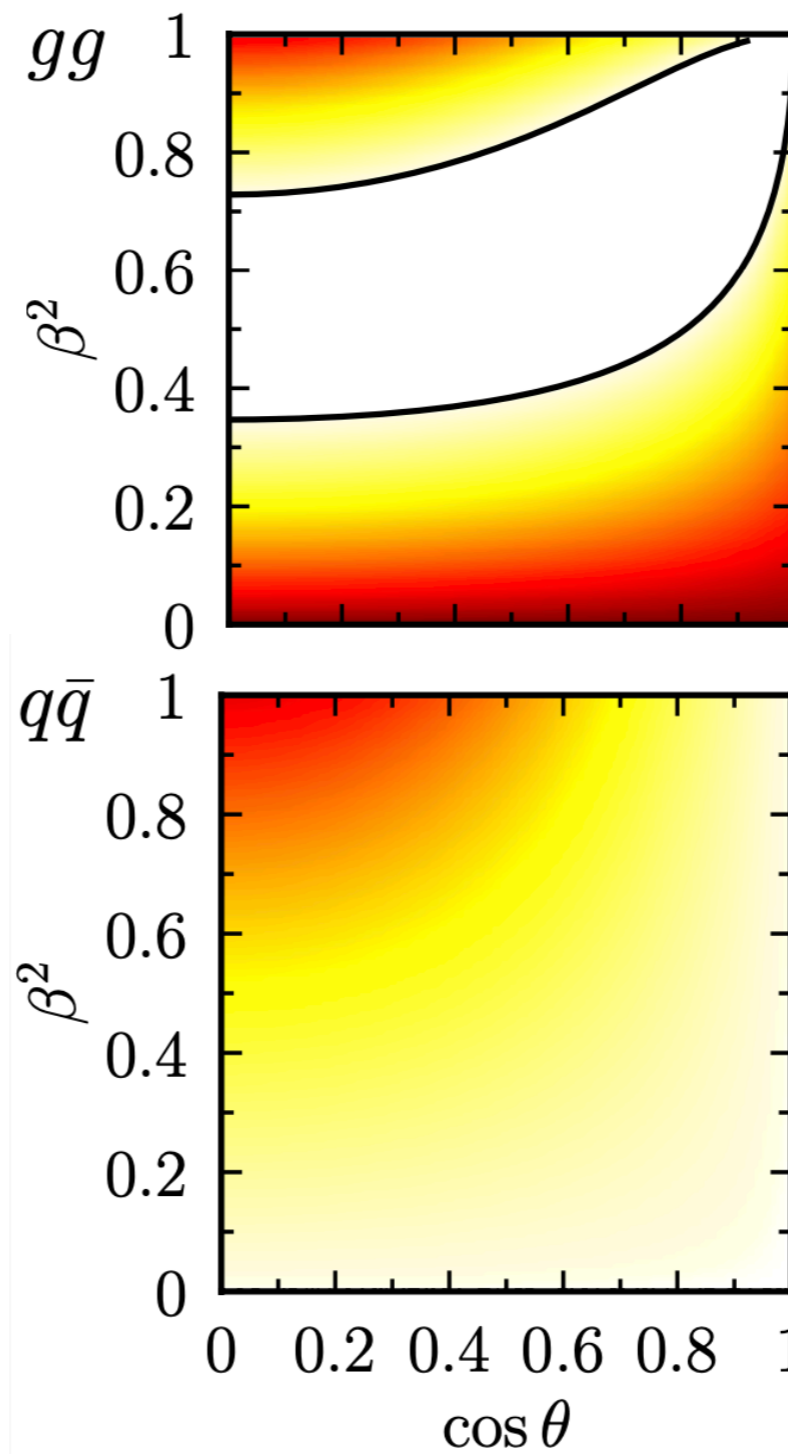
# Backup

$$\mathcal{O}_{tG} = g_s (\bar{Q} \sigma^{\mu\nu} T^A t) \tilde{\varphi} G_{\mu\nu}^A + \text{h.c.}$$

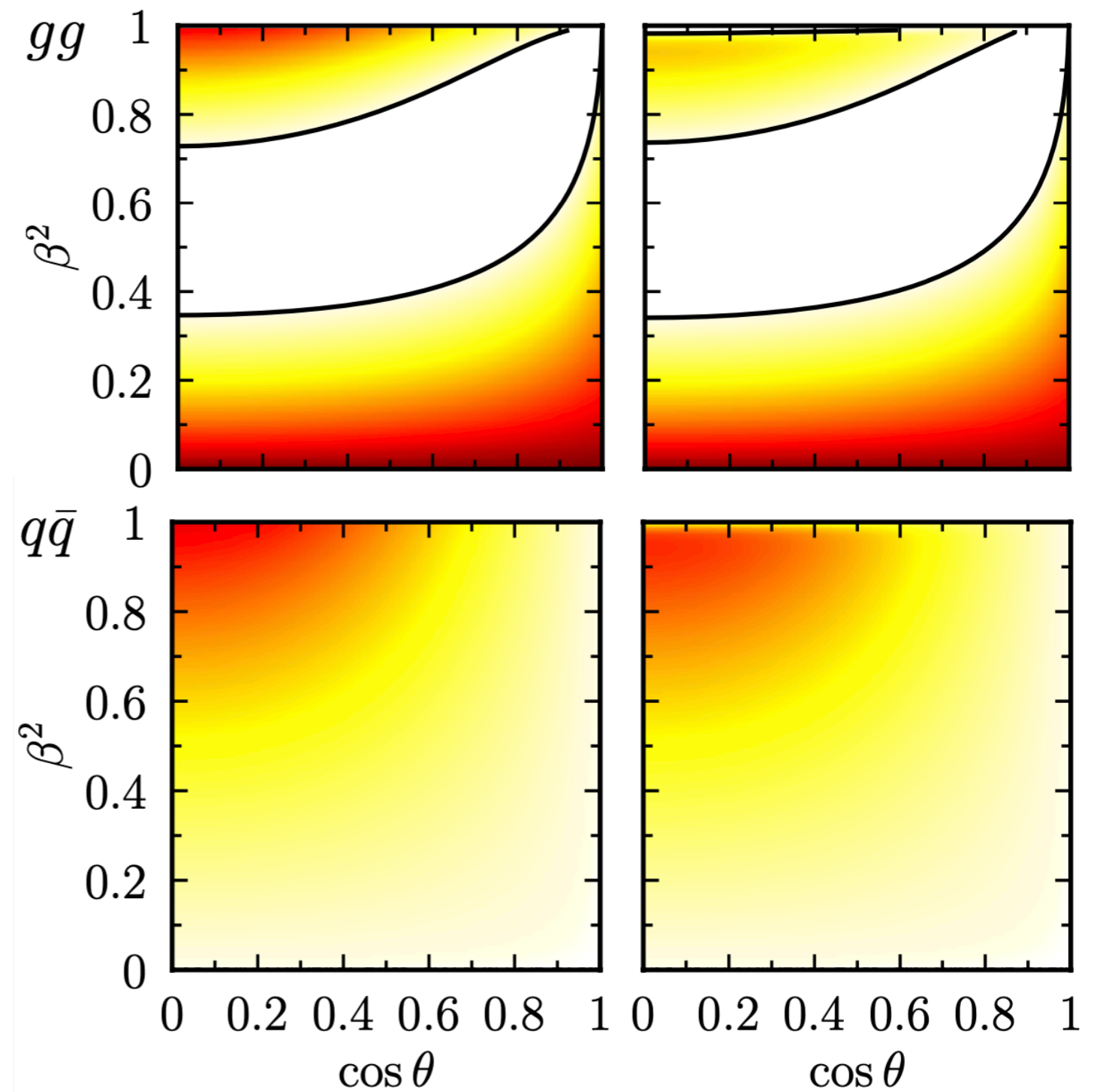
SM



Linear



Quad



$$\Delta = -C_{nn} + |C_{kk} + C_{rr}| - 1 > 0$$

$$\Delta_1 \equiv \Delta - \Delta_0$$

$\Delta$  computed up to  $\mathcal{O}(1/\Lambda^2)$

$$\Delta_2 \equiv \Delta - \Delta_1 - \Delta_0$$

$\Delta$  computed up to  $\mathcal{O}(1/\Lambda^4)$

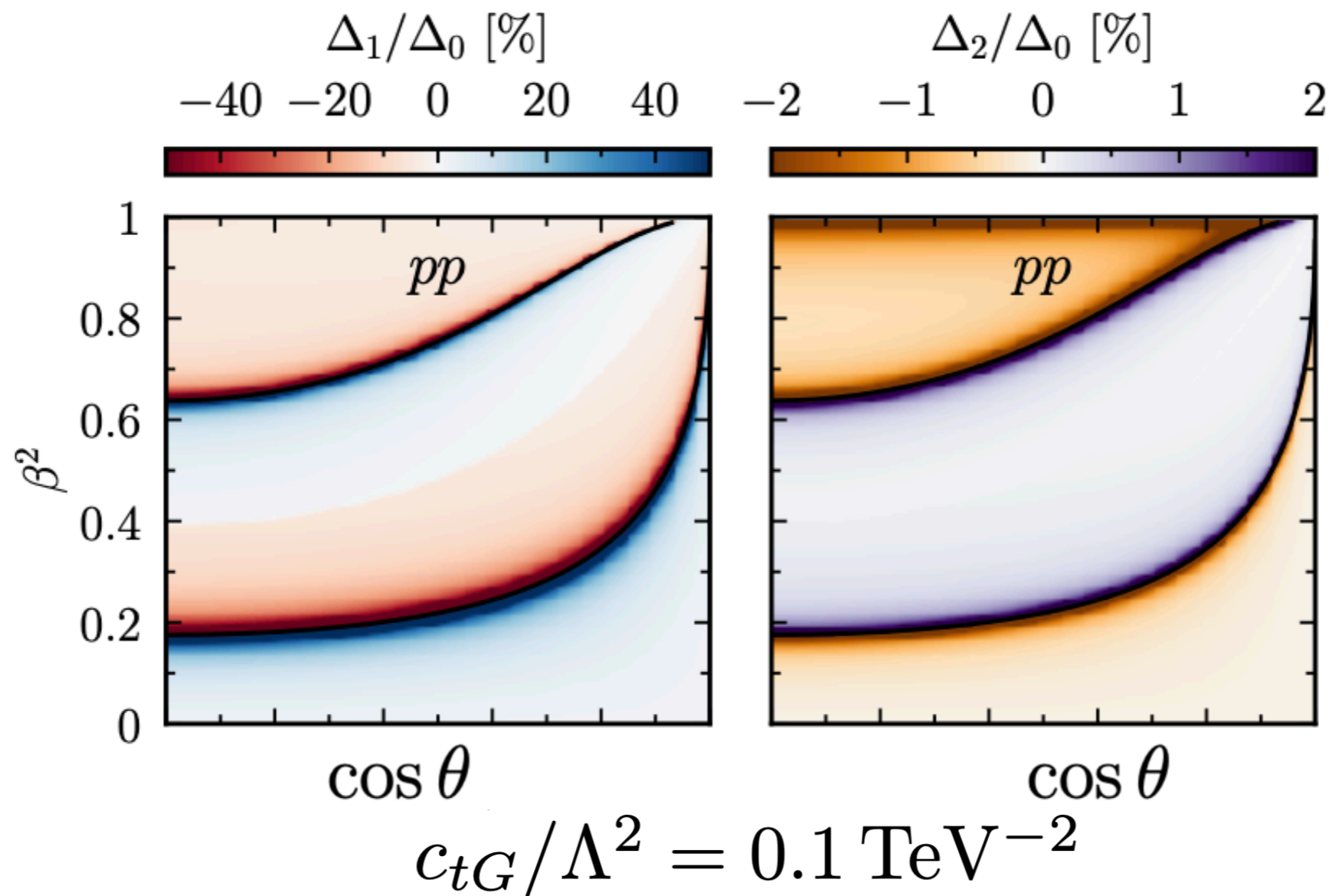
$$\Delta = -C_{nn} + |C_{kk} + C_{rr}| - 1 > 0$$

$$\Delta_1 \equiv \Delta - \Delta_0$$

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### 4-Fermion operators

$$\mathcal{O}_{Qq}^{(8,1)}, \mathcal{O}_{Qq}^{(8,3)}, \mathcal{O}_{tu}^{(8)}, \mathcal{O}_{td}^{(8)}, \mathcal{O}_{Qu}^{(8)}, \mathcal{O}_{Qd}^{(8)}, \mathcal{O}_{tq}^{(8)}$$

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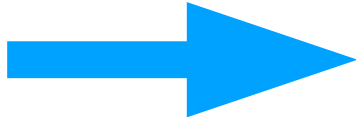
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What are the effects of NP on the entanglement regions?

Is NP affecting the quantum state?

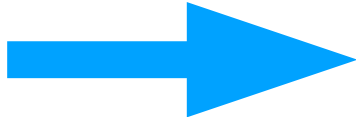
Given a bipartite system, with Hilbert space  $\mathcal{H} = \mathcal{H}_1 \otimes \mathcal{H}_2$

If state **separable**  $|\Psi\rangle = |\Psi\rangle_1 \otimes |\Psi\rangle_2$   **No entanglement**

Operative definition of entanglement: **Peres-Horodecki criterion**

$$\Delta = -C_{nn} + |C_{kk} + C_{rr}| - 1 > 0 \quad \text{entangled}$$

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**We can then define the concurrence**

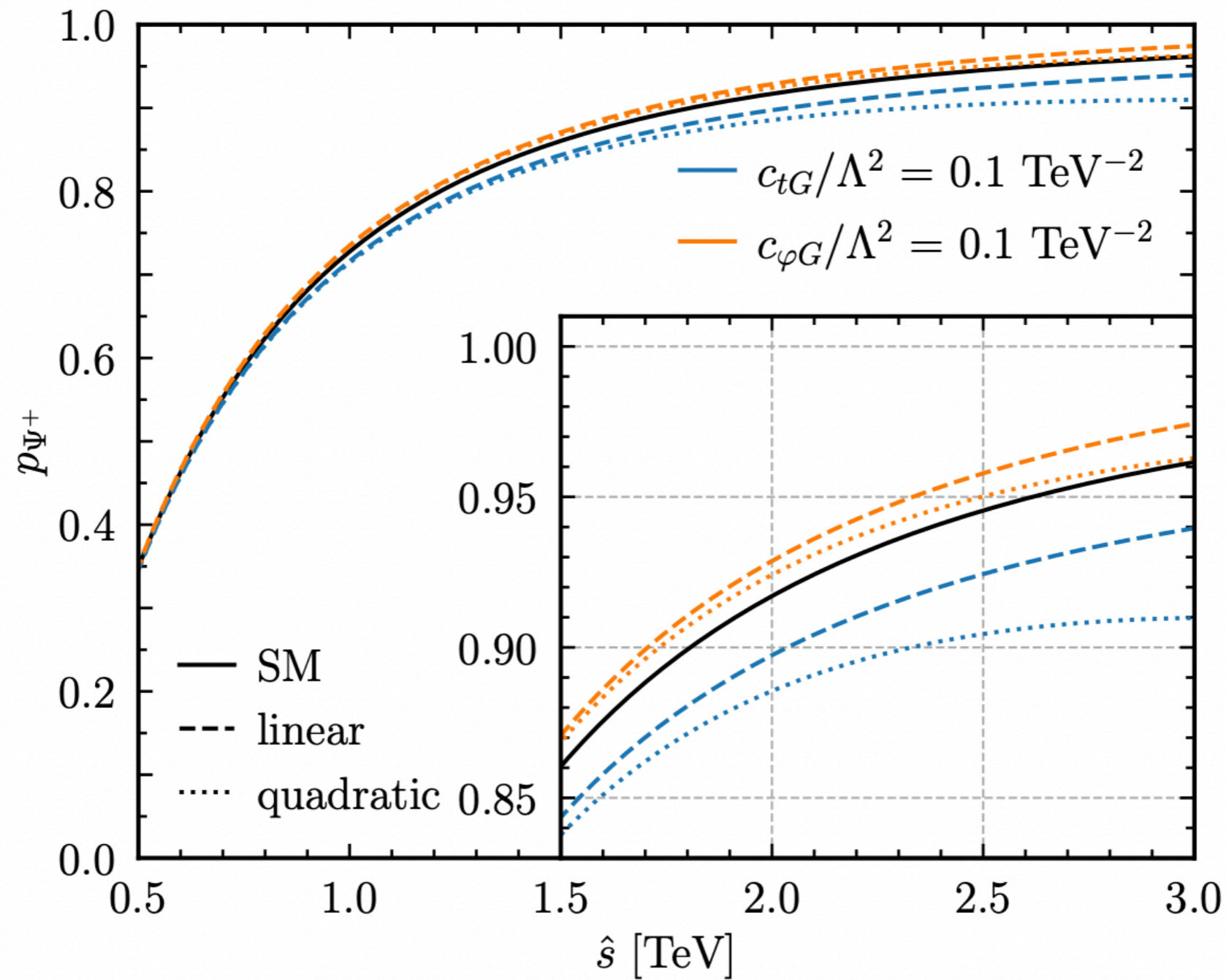
$$C[\rho] = \max(\Delta/2, 0)$$

$$C[\rho] = 1$$

Max entanglement

$$p_{\Psi^+} = \langle \Psi^+ | {}_n \rho | \Psi^+ \rangle_n$$

Probability triplet state



# LO coefficients - gg channel

$$\begin{aligned}
\tilde{A}^{gg,(1)} &= \frac{g_s^2}{\Lambda^2} \frac{1}{1 - \beta^2 z^2} \left[ \frac{g_s^2 v m_t (9\beta^2 z^2 + 7)}{12\sqrt{2}} c_{tG} - \frac{\beta^2 m_t^4}{4m_t^2 - (1 - \beta^2)m_h^2} c_{\varphi G} + \frac{9g_s^2 \beta^2 m_t^2 z^2}{8} c_G \right], \\
\tilde{C}_{nn}^{gg,(1)} &= \frac{g_s^2}{\Lambda^2} \frac{1}{1 - \beta^2 z^2} \left[ \frac{-7g_s^2 v m_t}{12\sqrt{2}} c_{tG} - \frac{\beta^2 m_t^4}{4m_t^2 - (1 - \beta^2)m_h^2} c_{\varphi G} + \frac{9g_s^2 \beta^2 m_t^2 z^2}{8} c_G \right], \\
\tilde{C}_{kk}^{gg,(1)} &= \frac{g_s^2}{\Lambda^2} \frac{1}{1 - \beta^2 z^2} \left[ \frac{g_s^2 v m_t (9\beta^2 z^2 + 7) (\beta^2 (z^4 - z^2 - 1) + 1)}{12\sqrt{2} (\beta^2 z^2 - 1)} c_{tG} \right. \\
&\quad \left. + \frac{\beta^2 m_t^4}{4m_t^2 - (1 - \beta^2)m_h^2} c_{\varphi G} - \frac{9g_s^2 \beta^2 m_t^2 z^2}{8} c_G \right], \\
\tilde{C}_{rr}^{gg,(1)} &= \frac{g_s^2}{\Lambda^2} \frac{1}{1 - \beta^2 z^2} \left[ \frac{g_s^2 v m_t \left( -9\beta^4 (z - z^3)^2 - 7\beta^2 (z^4 - z^2 + 1) + 7 \right)}{12\sqrt{2} (\beta^2 z^2 - 1)} c_{tG} \right. \\
&\quad \left. - \frac{\beta^2 m_t^4}{4m_t^2 - (1 - \beta^2)m_h^2} c_{\varphi G} + \frac{9g_s^2 \beta^2 m_t^2 z^2}{8} c_G \right], \\
\tilde{C}_{rk}^{gg,(1)} &= \frac{g_s^2}{\Lambda^2} \frac{1}{1 - \beta^2 z^2} \left[ \frac{g_s^2 v m_t \beta^2 z (1 - z^2) (9\beta^2 + (\beta^2 - 2) z^2 (9\beta^2 (z^2 - 1) + 7) - 2)}{24\sqrt{2} \sqrt{(\beta^2 - 1) (z^2 - 1) (\beta^2 z^2 - 1)}} c_{tG} \right. \\
&\quad \left. + \frac{9g_s^2 \beta^2 m_t^2 z}{8} \sqrt{\frac{1 - z^2}{1 - \beta^2}} c_G \right].
\end{aligned}$$

# LO coefficients - qq channel

$$\tilde{A}^{q\bar{q},(1)} = \frac{4g_s^2 m_t^2}{9\Lambda^2(1-\beta^2)} \left[ \sqrt{2}g_s^2 \frac{v}{m_t} (1-\beta^2)c_{tG} + (2 - (1-z^2)\beta^2) c_{VV}^{(8),u} + 2z\beta c_{AA}^{(8),u} \right],$$

$$\tilde{C}_{nn}^{q\bar{q},(1)} = -\frac{g_s^2 m_t^2}{\Lambda^2} \frac{4\beta^2(1-z^2)}{9(1-\beta^2)} c_{VV}^{(8),u},$$

$$\tilde{C}_{kk}^{q\bar{q},(1)} = \frac{2g_s^2 m_t^2}{9\Lambda^2(1-\beta^2)} \left[ 2\sqrt{2}g_s^2 \frac{v}{m_t} (1-\beta^2)z^2 c_{tG} + (2 + \beta^2 - (2-\beta^2)(1-2z^2)) c_{VV}^{(8),u} + 4\beta z c_{AA}^{(8),u} \right]$$

$$\tilde{C}_{rr}^{q\bar{q},(1)} = \frac{4g_s^2 m_t^2 (1-z^2)}{9\Lambda^2(1-\beta^2)} \left[ \sqrt{2}g_s^2 \frac{v}{m_t} (1-\beta^2)c_{tG} + (2-\beta^2)c_{VV}^{(8),u} \right],$$

$$\tilde{C}_{rk}^{q\bar{q},(1)} = -\frac{2g_s^2 m_t^2}{9\Lambda^2} \sqrt{\frac{1-z^2}{1-\beta^2}} \left[ \sqrt{2}g_s^2 \frac{v}{m_t} (2-\beta^2)z c_{tG} + 4z c_{VV}^{(8),u} + 2\beta c_{AA}^{(8),u} \right],$$

$$B_k^{\pm, q\bar{q},(1)} = 4g_s^2 \frac{m_t^2}{9\Lambda^2} \frac{1}{1-\beta^2} \left( \beta(z^2+1)c_{AV}^{(8),u} + 2z c_{VA}^{(8),u} \right),$$

$$B_r^{\pm, q\bar{q},(1)} = -4g_s^2 \frac{m_t^2}{9\Lambda^2} \sqrt{\frac{1-z^2}{1-\beta^2}} \left( \beta z c_{AV}^{(8),u} + 2c_{VA}^{(8),u} \right).$$

$$c_{VV}^{(8),u} = (c_{Qq}^{(8,1)} + c_{Qq}^{(8,3)} + c_{tu}^{(8)} + c_{tq}^{(8)} + c_{Qu}^{(8)})/4,$$

$$c_{AA}^{(8),u} = (c_{Qq}^{(8,1)} + c_{Qq}^{(8,3)} + c_{tu}^{(8)} - c_{tq}^{(8)} - c_{Qu}^{(8)})/4,$$

$$c_{AV}^{(8),u} = (-c_{Qq}^{(8,1)} - c_{Qq}^{(8,3)} + c_{tu}^{(8)} + c_{tq}^{(8)} - c_{Qu}^{(8)})/4,$$

$$c_{VA}^{(8),u} = (-c_{Qq}^{(8,1)} - c_{Qq}^{(8,3)} + c_{tu}^{(8)} - c_{tq}^{(8)} + c_{Qu}^{(8)})/4,$$