

Dynamical origin of neutrino masses and dark matter from confinement



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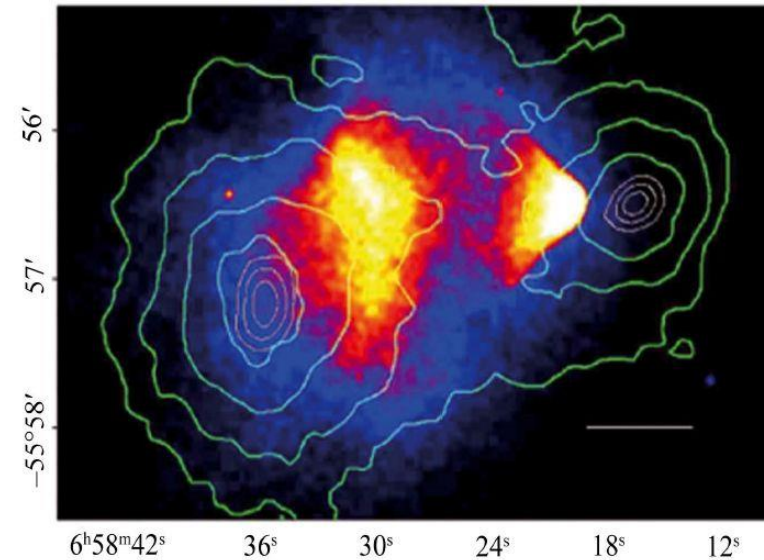
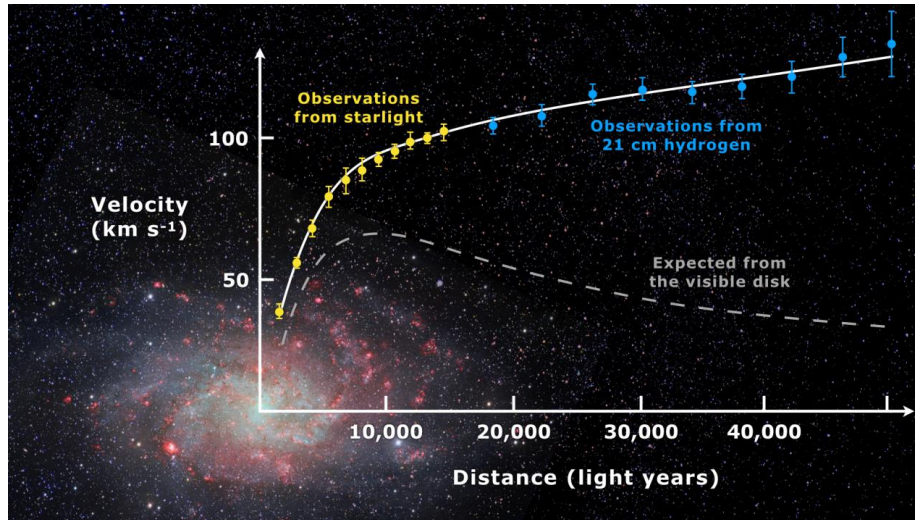


based on [arXiv \[2403.17488\]](https://arxiv.org/abs/2403.17488) Maximilian Berbig, Juan Herrero-Garcia, GL

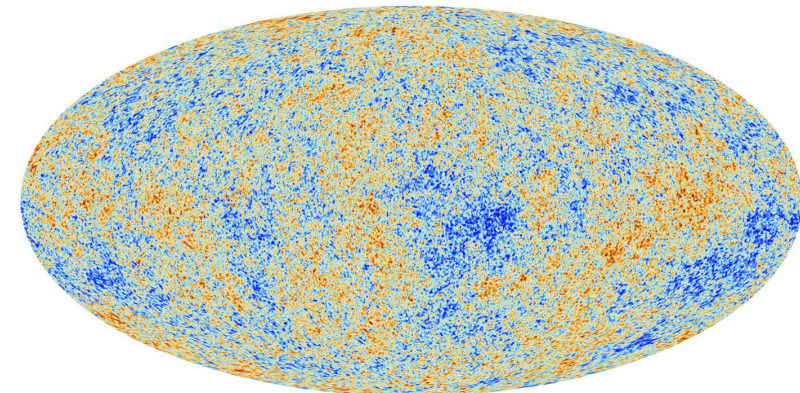


Dark Matter

Dark Matter existence is supported by astrophysical and cosmological evidence



- Neutral and weakly interacting with SM
- Cosmologically stable
- Cold (non-relativistic at structure formation)



Neutrino masses

Neutrinos are massless in the Standard Model

$$L = (\nu_L, e_L) \quad \text{no } \nu_R$$

Accidental U(1) lepton number conservation

Neutrino oscillations require massive neutrinos



Combining oscillation and cosmological data

$$0.05 \text{ eV} \lesssim \sum m_\nu \lesssim 0.12 \text{ eV}$$

The See-Saw

Introduce RHN $N_R \sim (1, 1)_0$

$$\Delta\mathcal{L}_{\text{lepton}} \sim y_\nu \bar{L} \tilde{H} N_R + \frac{1}{2} M_N \overline{N_R^c} N_R$$

Dirac mass Majorana mass

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & m_D \\ m_D^T & M_N \end{pmatrix} \quad m_D = y_\nu v_H / \sqrt{2}$$

$$m_D \ll M_N$$



$$m_\nu = m_D M_N^{-1} m_D^T \sim \frac{v_H^2}{M_N}$$



$$m_\nu \sim 0.05 \text{ eV} \quad \text{if} \quad M_N \sim 10^{14} \text{ GeV}$$

The See-Saw

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Dirac mass Majorana mass

Many variants have been studied!

(type II-III see-saw, inverse see-saw, linear see-saw, scotogenic,...)

Majorana masses are a **crucial** ingredient

Inverse See-Saw

2 basic ingredients

1) Small breaking of lepton number (μ -term)

→ Explicit or spontaneous breaking

→ Need to be small $m_\nu \propto \mu$

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→ Explicit or spontaneous breaking

→ Need to be small $m_\nu \propto \mu$

→ We will propose a **dynamical** generation

2) Extended fermionic sector

→ Need at least 2 new fermionic fields $N_R, N_L \sim (1, 1)_0$

Inverse See-Saw

$$\Delta\mathcal{L}_{\text{lepton}} \sim y_\nu \bar{L} \tilde{H} N_R + M_D \overline{N_L} N_R + \frac{1}{2} \mu \overline{N_R^c} N_R$$

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$$\Delta\mathcal{L}_{\text{lepton}} \sim y_\nu \bar{L} \tilde{H} N_R + \underbrace{M_D \overline{N_L} N_R}_{\text{Dirac mass}} + \frac{1}{2} \underbrace{\mu \overline{N_R^c} N_R}_{\text{Majorana mass}}$$

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M_D \\ 0 & M_D^T & \mu \end{pmatrix} \quad m_D = y_\nu v_H / \sqrt{2}$$

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$$\mu \ll m_D \ll M_D$$



$$m_\nu \sim m_D (M_D^T)^{-1} \mu M_D^{-1} m_D^T \sim \mu \frac{v_H^2}{M_D^2}$$

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$$\begin{array}{l} \text{red arrow} \rightarrow m_\nu \sim 0.05 \text{ eV} \quad \text{if} \quad \mu \sim \text{keV} \\ M_D \sim 10 \text{ TeV} \end{array}$$

Inverse See-Saw

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$$m_\nu \sim 0.05 \text{ eV} \quad \text{if} \quad \begin{matrix} \mu \sim \text{keV} \\ M_D \sim 10 \text{ TeV} \end{matrix}$$

Potentially testable

Inverse See-Saw

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$$\mathcal{M}_\nu = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M_D \\ 0 & M_D^T & \mu \end{pmatrix}$$

How to generate such a small lepton number breaking parameter?

$$\mu \ll m_D \ll M_D$$

$$m_\nu \sim m_D (M_D^T)^{-1} \mu M_D^{-1} m_D^T \sim \mu \frac{v_H^2}{M_D^2}$$

→ $m_\nu \sim 0.05 \text{ eV}$ if $\mu \sim \text{keV}$
 $M_D \sim 10 \text{ TeV}$

Gauge confinement

New confining dark sector \longrightarrow we focus (for simplicity) on $SU(3)_D$

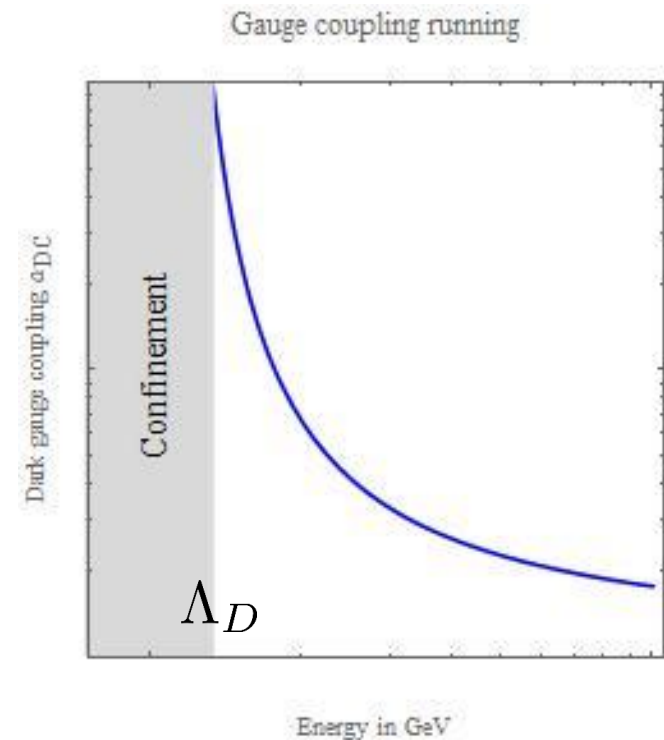
1 vector-like dark quark in the fundamental representation (q_L, q_R)

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The theory confines at the scale Λ_D



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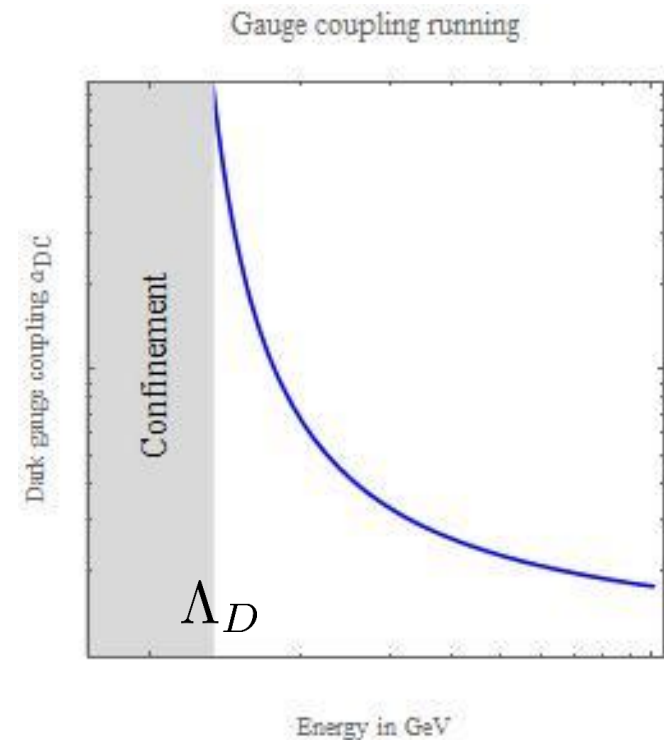
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(1) Quark condensate $\langle \overline{q_L} q_R \rangle \simeq \Lambda_D^3$
(similar to QCD)



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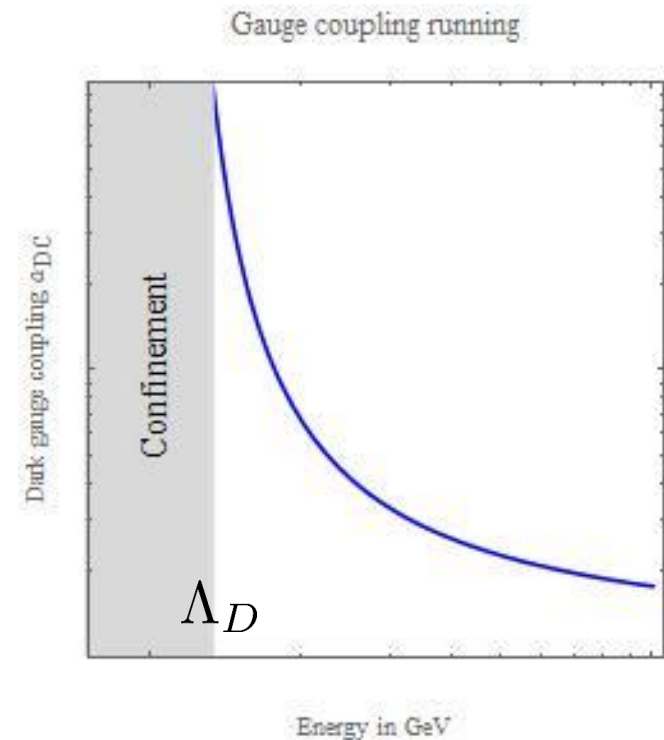
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(similar to QCD)

(2) Quarks combine into *baryons* and *mesons*



Neutrino mass from confinement

$$\mathcal{L} \sim y_Q \sigma \overline{q_L} q_R + y_{N_R} \sigma \overline{N_R^c} N_R + m_\sigma^2 \sigma^2 + \dots$$

Neutrino mass from confinement

$$\mathcal{L} \sim y_Q \sigma \overline{q_L} q_R + y_{N_R} \sigma \overline{N_R^c} N_R + m_\sigma^2 \sigma^2 + \dots$$

Real scalar field

Neutrino mass from confinement

$$\mathcal{L} \sim y_Q \sigma \overline{q_L} q_R + y_{N_R} \sigma \overline{N_R^c} N_R + \underline{m_\sigma^2} \sigma^2 + \dots$$

Hard mass $m_\sigma^2 > 0$

Neutrino mass from confinement

$$\mathcal{L} \sim y_Q \sigma \overline{q_L} q_R + y_{N_R} \sigma \overline{N_R^c} N_R + m_\sigma^2 \sigma^2 + \dots$$

Example

	SU(3) _D	\mathcal{Z}_4
q_L	3	$-i$
q_R	3	i
N_L	1	i
N_R	1	i
σ	1	-1

No bare masses for the fermions

Scalar couples to quark and RHN sectors

Neutrino mass from confinement

$$\mathcal{L} \sim y_Q \sigma \overline{q_L} q_R + y_{N_R} \sigma \overline{N_R^c} N_R + m_\sigma^2 \sigma^2 + \dots$$

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Gauge confinement $\langle \overline{q_L} q_R \rangle \simeq \Lambda_D^3$

generate a scalar vev \downarrow $V(\sigma) \sim y_Q \langle \overline{q_L} q_R \rangle \sigma + m_\sigma^2 \sigma^2$

$$\langle \sigma \rangle \simeq y_Q \frac{\Lambda_D^3}{m_\sigma^2}$$

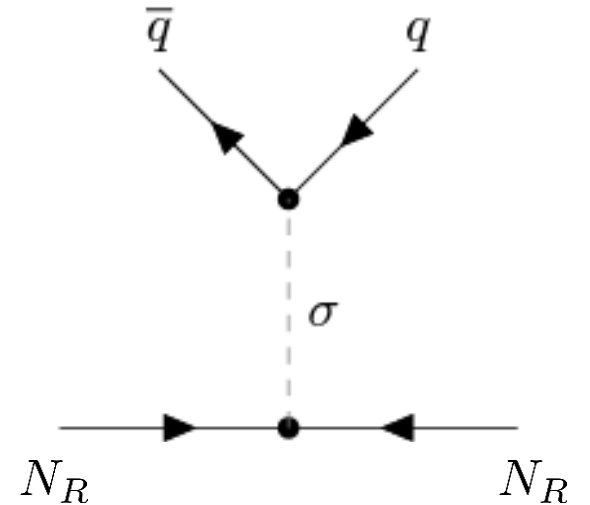
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Gauge confinement $\langle \bar{q}_L q_R \rangle \simeq \Lambda_D^3$

generate a scalar vev

$$\langle \sigma \rangle \simeq y_Q \frac{\Lambda_D^3}{m_\sigma^2}$$



Dynamical generation of Majorana mass $\mu \simeq y_{N_R} y_Q \frac{\Lambda_D^3}{m_\sigma^2}$

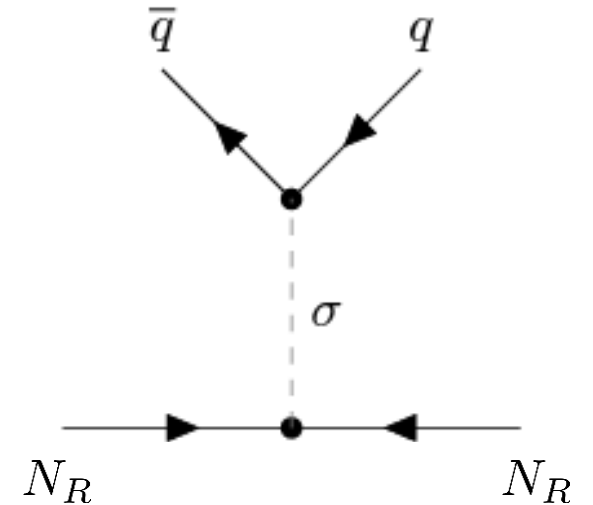
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generate a scalar vev

$$\langle \sigma \rangle \simeq y_Q \frac{\Lambda_D^3}{m_\sigma^2}$$



Dynamical generation of Majorana mass $\mu \simeq y_{N_R} y_Q \frac{\Lambda_D^3}{m_\sigma^2}$

Generic mechanism to generate Majorana masses

It can be applied in any neutrino mass model (e.g. Type I see-saw)

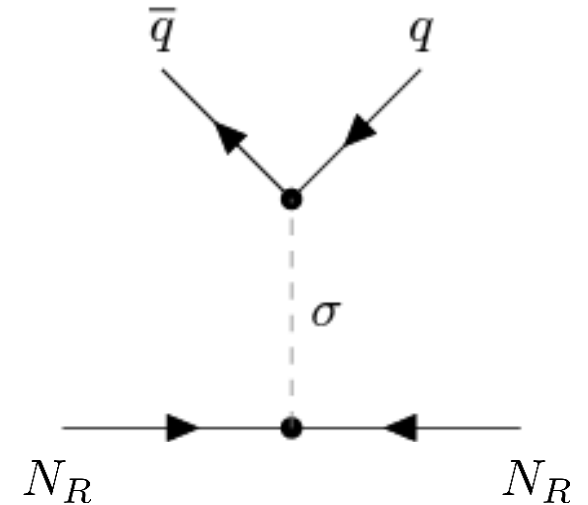
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Gauge confinement $\langle \bar{q}_L q_R \rangle \simeq \Lambda_D^3$

generate a scalar vev

$$\langle \sigma \rangle \simeq y_Q \frac{\Lambda_D^3}{m_\sigma^2}$$



Dynamical generation of Majorana mass $\mu \simeq y_{N_R} y_Q \frac{\Lambda_D^3}{m_\sigma^2}$

If $\Lambda_D \ll m_\sigma$ \longrightarrow dynamical generation of small Majorana mass for inverse see-saw

The Model

	SU(3) _D	\mathcal{Z}_4	generations
q_L	3	$-i$	1
q_R	3	i	1
N_L	1	i	3
N_R	1	i	3
L	1	i	3
e_R	1	i	3
σ	1	-1	1

Can be generated dynamically by
the vev of an additional scalar

$$\mathcal{L}_{LN} = y_e \bar{L} H e_R + y_\nu \bar{L} \tilde{H} N_R + M_D \bar{N}_L N_R + \text{h.c.},$$

$$\mathcal{L}_D = \underline{y_Q \sigma \bar{q}_L q_R} + \underline{y_{N_L} \sigma \bar{N}_L^c N_L} \\ + \underline{y_{N_R} \sigma \bar{N}_R^c N_R} + \text{h.c.},$$

$$V_{\sigma,\varphi} = (m_\sigma^2 + \lambda_\sigma \sigma^2 + \lambda_{H\sigma} |H|^2) \sigma^2$$

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & \mu & M_D \\ 0 & M_D^T & \mu' \end{pmatrix}$$

$$m_D = y_\nu \langle H \rangle$$

$$\mu = y_Q y_{N_R} \frac{\Lambda_D^3}{m_\sigma^2} \quad \mu' = y_Q y_{N_L} \frac{\Lambda_D^3}{m_\sigma^2}$$

The Spectrum

The theory confines at the scale Λ_D



Quarks combine into *baryons* and *mesons*

The Spectrum

The theory confines at the scale Λ_D



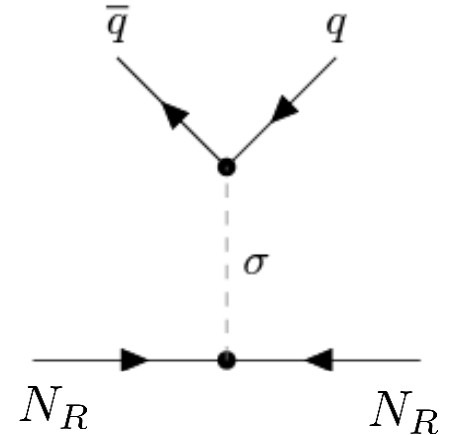
Mesons

The lightest meson is pseudo-scalar

$$m_{\mathcal{M}} \simeq \Lambda_D$$

$$f_{\mathcal{M}} \equiv \langle 0 | \bar{q} \gamma_5 q | \mathcal{M} \rangle \sim \Lambda_D^2$$

(with 1 quark flavor there are no light dark pions)



Mesons can decay into neutrinos (both RHNs and active)

The Spectrum

The theory confines at the scale Λ_D



Baryons

$\mathcal{B} \sim qqq$ bound state with spin $3/2$

$$m_{\mathcal{B}} \simeq 5\Lambda_D$$

	$U(1)_D$
q_L	1
q_R	1
\mathcal{M}	0
\mathcal{B}	3

Accidental $U(1)_D$ of the renormalizable Lagrangian

Protected up to dimension-8 operators (*spin protection*)

Baryons are stable  **Dark Matter!**

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$



σ is not in thermal bath

$$LL, HH \leftrightarrow NN$$

$$LH \leftrightarrow N$$

$$NN \leftrightarrow \bar{q}q$$

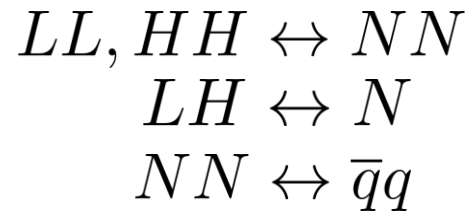
The dark sector is produced from the SM bath and thermalizes

The Cosmology

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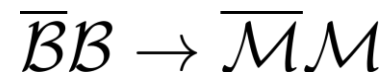


The dark sector is produced from the SM bath and thermalizes

Confinement $T \simeq \Lambda_D$



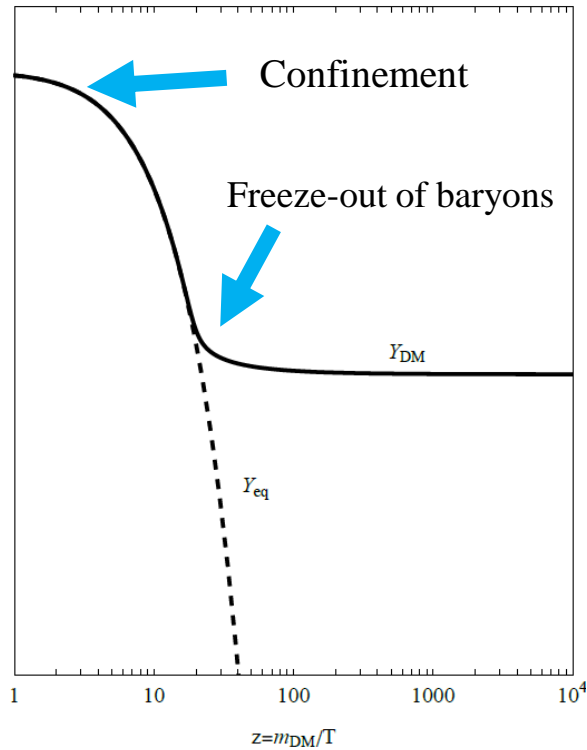
Strong (dark) interactions convert baryons to mesons



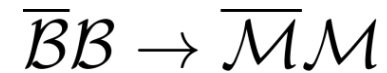
Mesons decay to neutrinos keeping equilibrium with the SM

$$\Gamma(\mathcal{M} \rightarrow NN) \simeq \frac{y_Q^2 y_N^2}{32\pi} \frac{\Lambda_D^5}{m_\sigma^4} \quad \Lambda_D > 2M_D$$

The Cosmology



Baryon DM freeze-out



$$\langle \sigma v \rangle \simeq \pi / \Lambda_D^2 \simeq 2.2 \times 10^{-26} \frac{\text{cm}^3}{\text{s}} \left(\frac{41 \text{ TeV}}{\Lambda_D} \right)^2$$

The DM relic abundance can be reproduced if $\Lambda_D \sim (1 - 100) \text{ TeV}$

Indirect Detection: neutrino lines

Baryons annihilate to mesons

$$\bar{B}B \rightarrow \bar{M}M$$

$$E_M \simeq m_B$$

Indirect Detection: neutrino lines

Baryons annihilate to mesons decay to heavy neutrinos

$$\bar{B}B \rightarrow \bar{M}M$$

$$E_M \simeq m_B$$



$$M \rightarrow NN$$

$$E_N \simeq m_B/2$$

Indirect Detection: neutrino lines

Baryons annihilate to mesons decay to heavy neutrinos decay to active neutrinos

$$\bar{B}B \rightarrow \bar{M}M$$

$$E_M \simeq m_B$$



$$M \rightarrow NN$$

$$E_N \simeq m_B/2$$

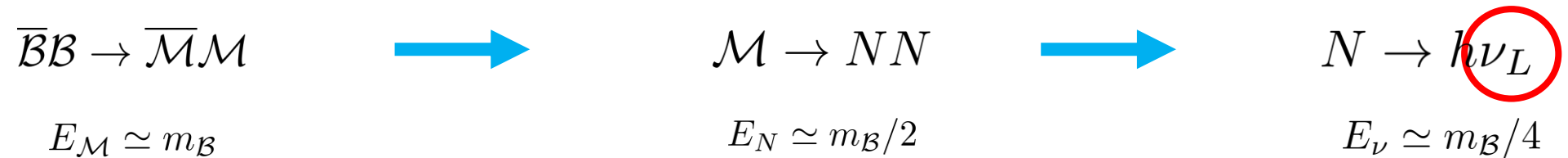


$$N \rightarrow h\nu_L$$

$$E_\nu \simeq m_B/4$$

Indirect Detection: neutrino lines

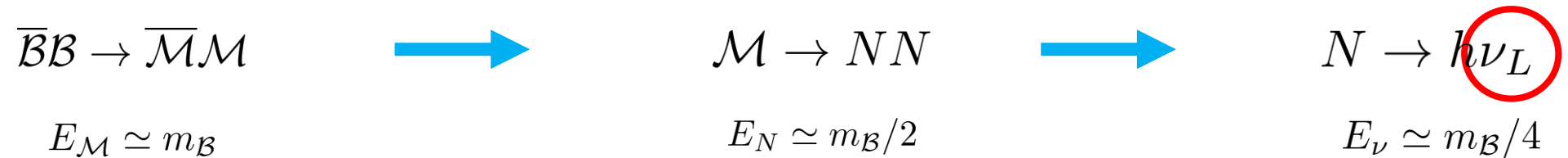
Baryons annihilate to mesons decay to heavy neutrinos decay to active neutrinos



Monochromatic neutrino lines $E_\nu \simeq m_B/4 \sim (1 - 100) \text{ TeV}$

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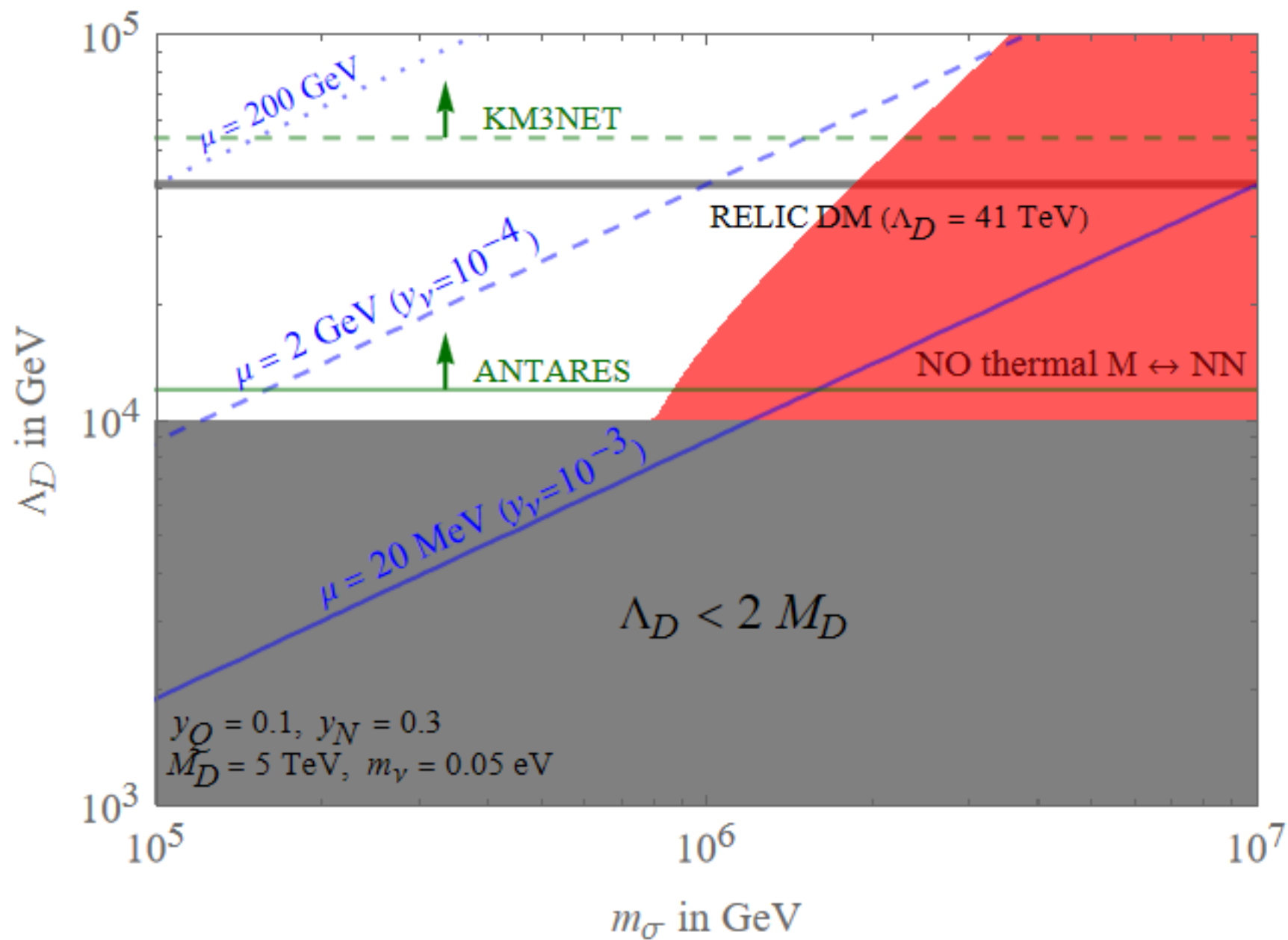


Monochromatic neutrino lines $E_\nu \simeq m_B/4 \sim (1 - 100) \text{ TeV}$

Testable with neutrino telescopes!

Current bound from ANTARES collaboration $\Lambda_D > 12 \text{ TeV} \sqrt{\frac{0.25 \times 10^{-24} \text{ cm}^3/\text{s}}{\langle \sigma v \rangle}}$

It will be improved by KM3NeT up to $\Lambda_D \simeq 54 \text{ TeV}$



Backup slides

Dark baryon number

Higher-dimensional operators breaks dark baryon number

The first baryon number-breaking operators arise at dimension 8 for spin 3/2
(*spin protection*)

$$\frac{c_8^{(1)}}{\Lambda_{\text{UV}}^4} (qqq)_\mu \bar{L} \left(D^\mu \tilde{H} \right) + \text{h.c.},$$

$$\longrightarrow \mathcal{B} \rightarrow h\nu, Z\nu, Wl, HZ\nu, \gamma N, \dots$$

$$\frac{c_8^{(2)}}{\Lambda_{\text{UV}}^4} (qqq)_\mu [\gamma^\alpha, \gamma^\beta] \gamma^\mu N_{L,R} B_{\alpha\beta} + \text{h.c.},$$

$$\frac{c_{10}}{\Lambda_{\text{UV}}^6} (qqq)_\mu N_{L,R} (\partial^\mu \bar{q}q) + \text{h.c.},$$

$$\frac{c_{11}}{\Lambda_{\text{UV}}^7} (qqq)_\mu \bar{L} (\partial^\mu \bar{q}q) \tilde{H} + \text{h.c.},$$

$$\tau_B \gtrsim 10^{28} \text{ sec} \longrightarrow \Lambda_{\text{UV}} \gtrsim 10^{12} \text{ GeV} \left(\frac{\Lambda_D}{40 \text{ TeV}} \right)$$

(DM indirect detection)

Constraints

Small active-sterile neutrino mixings evade current bounds

$$|V_{iN}|^2 \simeq m_\nu/\mu \lesssim 10^{-8} \quad i = e, \mu, \tau$$

EW precision observables

$$|V_{iN}| \lesssim 10^{-3}$$

$$M_D \sim \text{TeV}$$

$$\mu \rightarrow e\gamma$$

$$|V_{eN}V_{\mu N}| \lesssim 10^{-5}$$

$$M_D \sim 100 \text{ GeV}-10 \text{ TeV}$$

Electron dipole moment

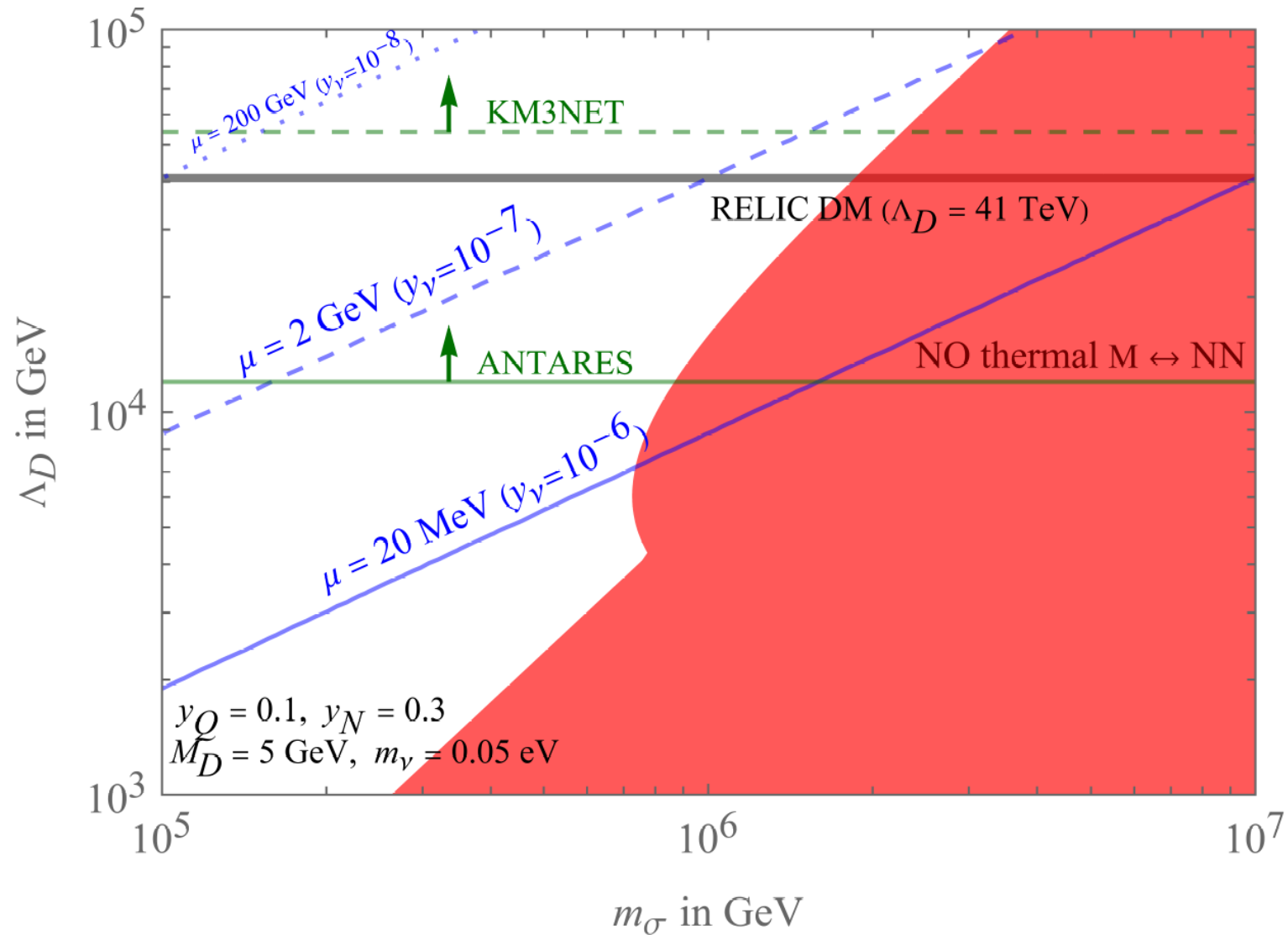
$$d_e^{\text{max}} \simeq 10^{-[31,32]} e \text{ cm} \quad (d_e^{\text{exp}} < 1.1 \times 10^{-29} e) \text{ cm}$$

DM Direct detection bounds are evaded

Very small mixing among the SM Higgs and σ

$$\theta_{h\sigma} \propto \frac{v_H \langle \sigma \rangle}{m_\sigma^2} \sim \frac{v_H \Lambda_D^3}{m_\sigma^4} \ll 1$$

Lighter Dirac masses imply smaller Yukawa couplings



$|V_{iN}|^2 \simeq m_\nu / \mu \lesssim 10^{-8}$ Close to experimental sensitivity for GeV-ish RHN

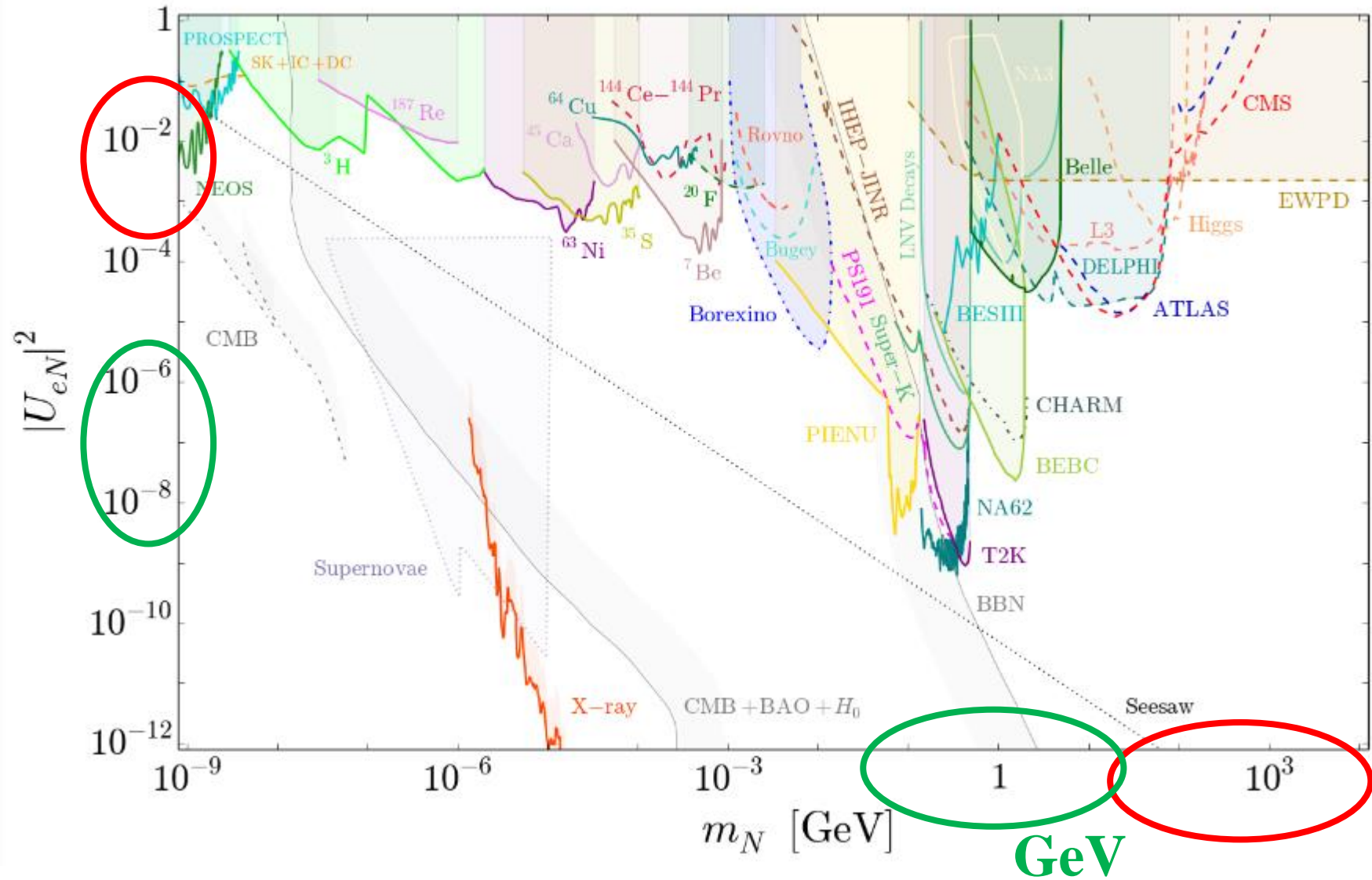
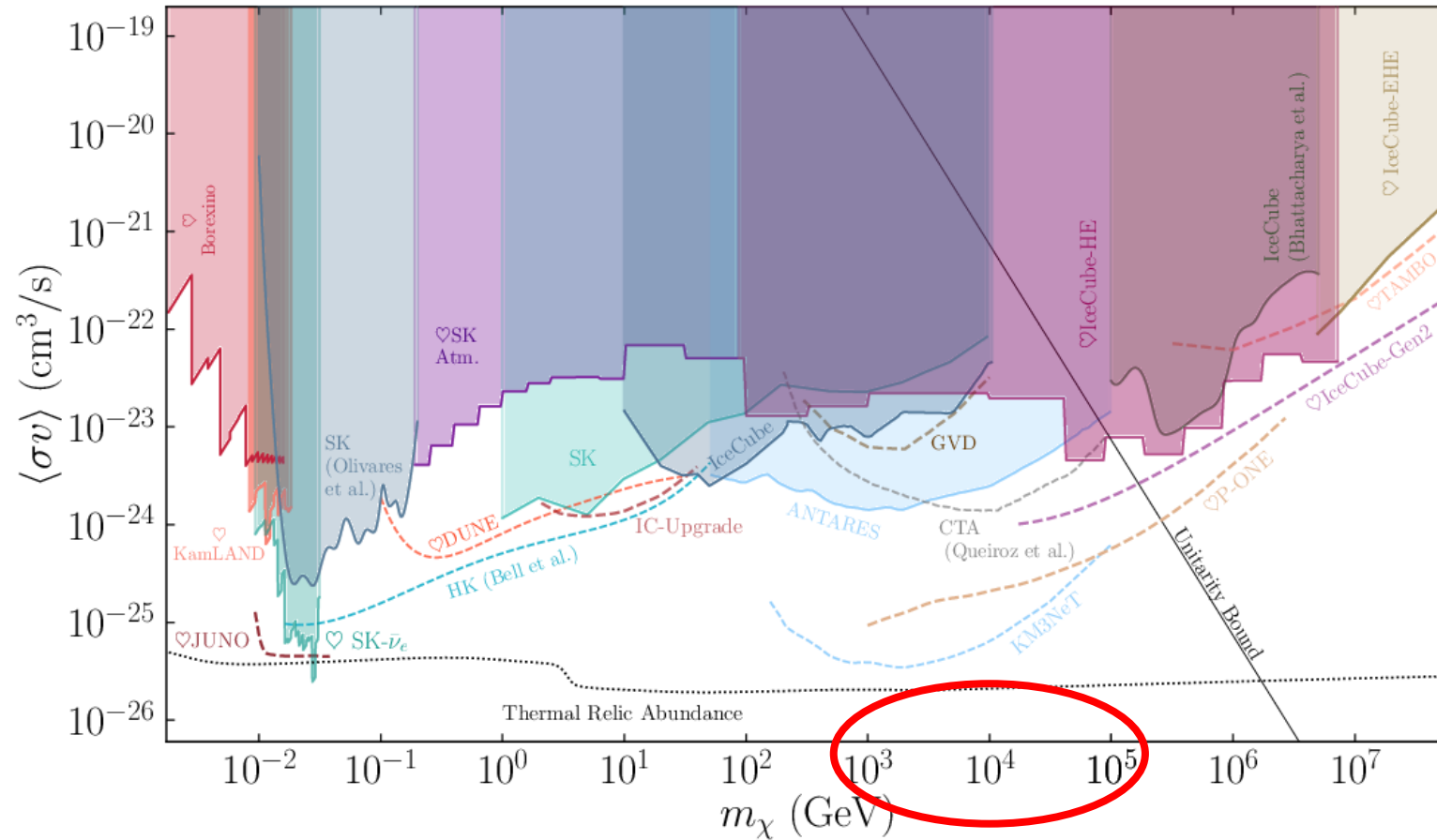


Figure made by Patrick Bolton, <https://www.hep.ucl.ac.uk/~pbolton/index.html>

Indirect Detection: neutrino lines

Testable with neutrino telescopes!



Dark sector thermalization

$$LL, HH \leftrightarrow NN$$

$$LH \leftrightarrow N$$

$$\Gamma \sim \frac{y_\nu^2}{32\pi} T \quad \longrightarrow \quad \Gamma \gg H \quad \longrightarrow \quad T < 7 \times 10^7 \text{ GeV} \left(\frac{y_\nu}{10^{-4}}\right)^2 \sqrt{\frac{106.75}{g_*}}$$

$$NN \leftrightarrow \bar{q}q$$

$$\Gamma \sim y_Q y_N \frac{T^5}{m_\sigma^4} \quad \longrightarrow \quad \Gamma \gg H \quad \longrightarrow \quad T > 100 \text{ GeV} \times \frac{1}{(y_Q y_N)^{1/3}} \left(\frac{m_\sigma}{10^6 \text{ GeV}}\right)^{4/3}$$

$$< \Lambda_D \sim 1 - 100 \text{ TeV}$$

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$

After dark confinement $T < \Lambda_D$

All hadrons are not relativistic

$$m_{\text{hadron}} \gtrsim \Lambda_D \gtrsim T$$

However they inherit the initial (relativistic) quark abundance

$$Y_q = \frac{n_q}{s} = \frac{135\zeta(3)}{\pi^4 g_s}$$

Over-abundance of dark hadrons?

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$

After dark confinement $T < \Lambda_D$

Meson (inverse) decays to neutrinos keep the hadrons in thermal equilibrium with the SM

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Hadrons evolves with the same temperature of the SM

$$Y_{\text{hadron}} \sim \exp(-m_{\text{hadron}}/T)$$

The Cosmology

For a non-relativistic (decoupled) dark sector

$$R \equiv \frac{s_D}{s}$$

$$s_D \approx \frac{\rho_D^{\text{eq}}}{T_D} = \frac{M n_D^{\text{eq}}}{T_D} \quad n_D^{\text{eq}} = \left(\frac{M T_D}{2\pi} \right)^{3/2} e^{-M/T_D} \quad T_d \sim 1/\log a$$

$$Y_D^{\text{eq}} \equiv \frac{n_D^{\text{eq}}}{s} = \frac{n_D^{\text{eq}}}{s_D} R = \frac{T_D}{M} R \quad \frac{T_D^*}{M} \approx \frac{1}{3 \log Q} \quad \log Q \simeq \mathcal{O}(1 - 10)$$

$$R \sim \mathcal{O}(0.1) \quad \frac{\Omega h^2}{0.12} \simeq \left(\frac{M}{0.4 \text{ eV}} \right) \frac{R}{3 \log Q} \simeq \frac{M}{100 \text{ eV}}$$

DM is either over-abundant or excluded (Bullet cluster, Lyman-alpha,...)

Cross section

O(1) factors are unknown because strong dynamics is non-perturbative

$$\bar{B}B \rightarrow \bar{M}M$$

Dimensional analysis \longrightarrow geometrical cross-section

$$\sigma v \sim 1/\Lambda_D^2$$

$$\mu = m_B/2$$

$$|\vec{v}| \simeq \sqrt{T/m_B}$$

$$l_{\max} \sim \mu v b \sim \sqrt{T m_B}/2\Lambda_D < 1$$

$$m_B \simeq 5\Lambda_D$$

$$b \sim 1/\Lambda_D$$

The cross section is dominated by the s-wave contribution

Dark pions

With more than 1 flavor of dark quarks the spectrum contains dark pions

$$m_\pi \simeq \Lambda_D^2 / m_\sigma \qquad m_\pi < M_D$$

Dark pions decay into active neutrinos

$$\Gamma_\pi \sim m_\nu^2 \Lambda_D^4 / m_\sigma^5$$

Decay is super-slow

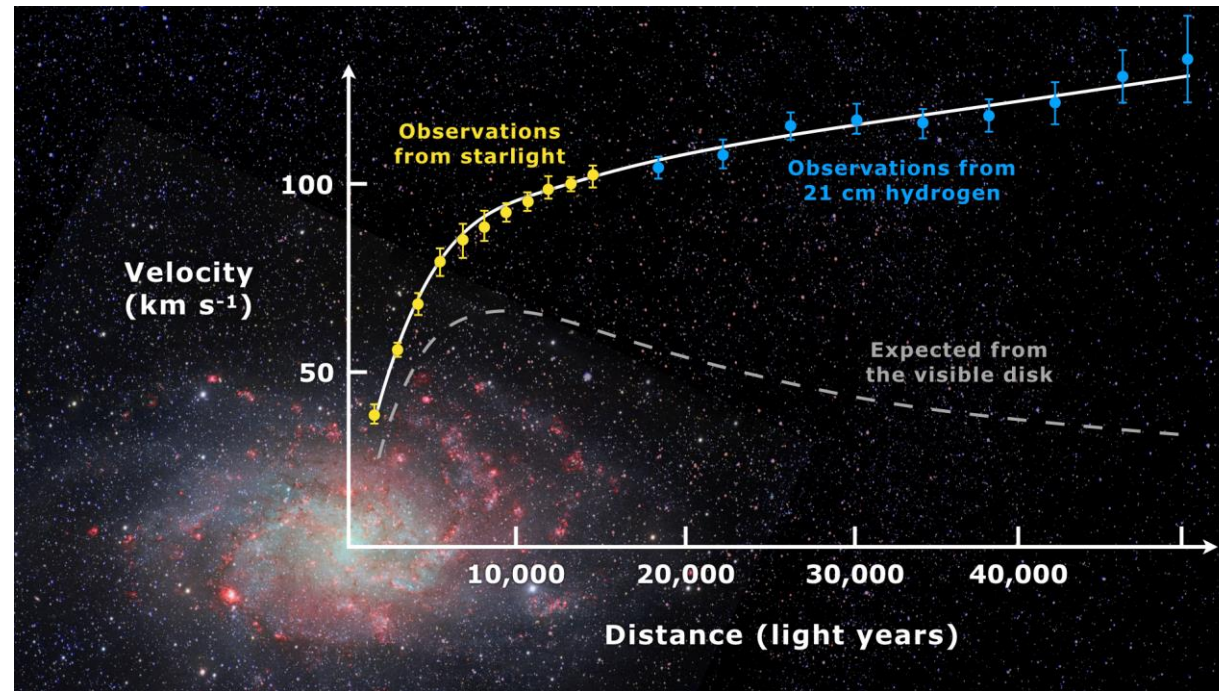


BBN constraints
Overclosure

(pions decouple with relativistic abundance)

Dark Matter evidence

Dark Matter existence is supported by astrophysics and cosmology

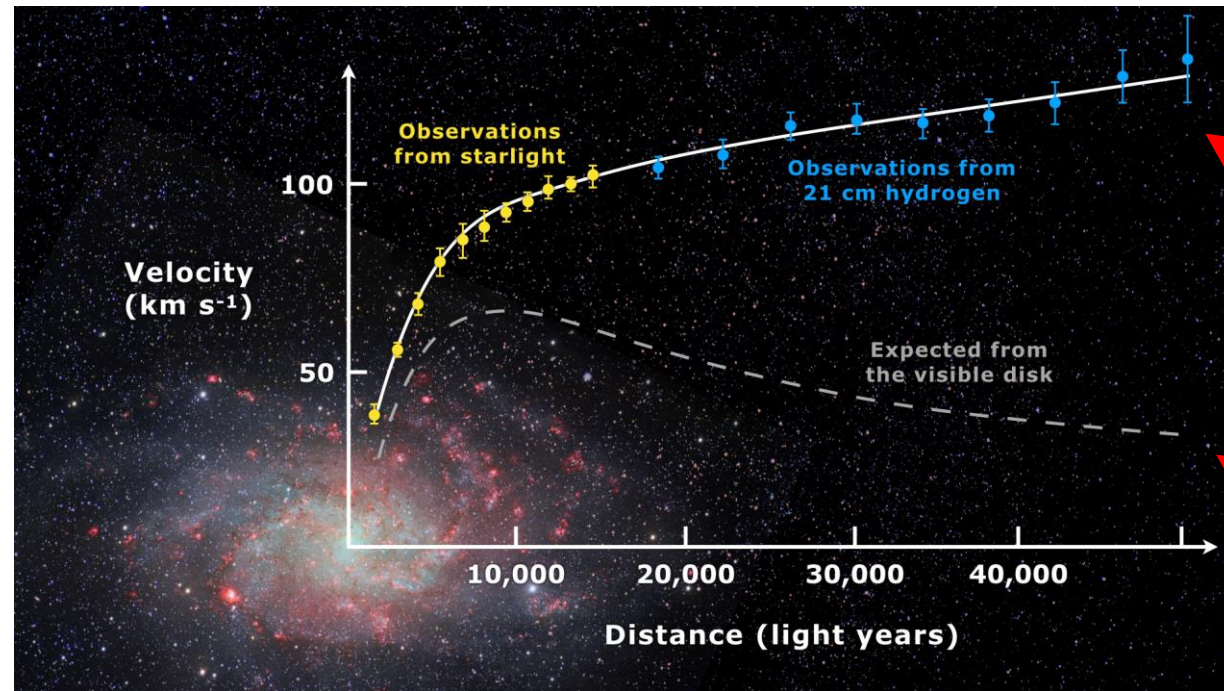


Rotation curves of spiral galaxies flatten at large distances

Dark Matter evidence

Dark Matter existence is supported by astrophysics and cosmology

$$v(r) = \sqrt{\frac{GM(r)}{r}}$$



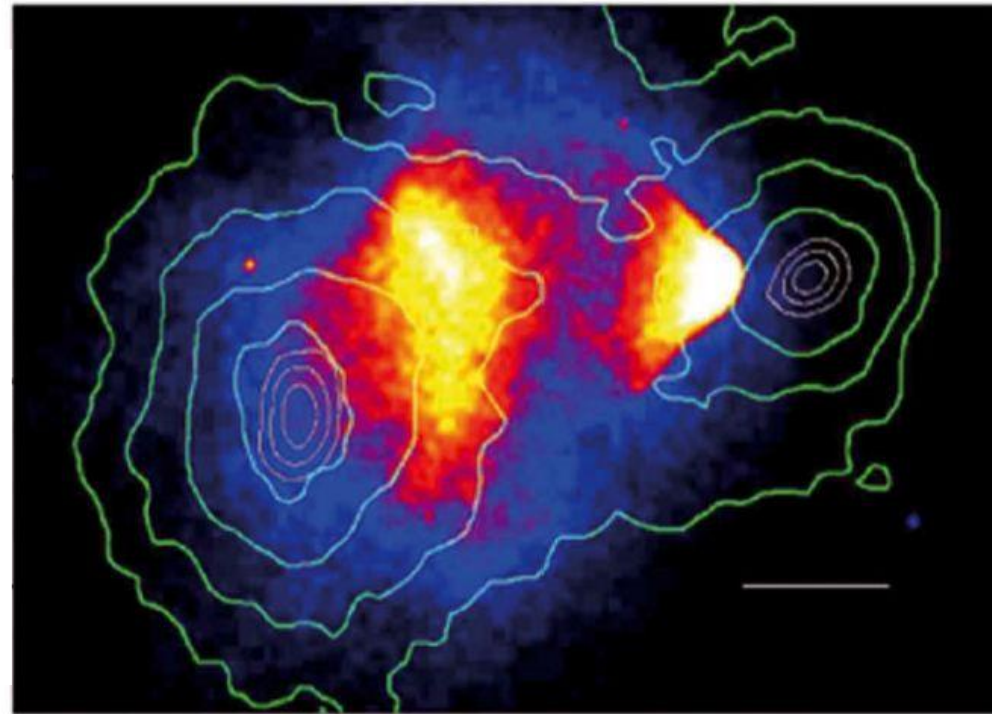
$$M_{\text{dark}}(r) = 4\pi r$$

$$M_{\text{vis}}(r) = M_{\text{vis}}$$

This implies the existence of a *dark* matter halo at large radius

Dark Matter evidence

Dark Matter existence is supported by astrophysics and cosmology

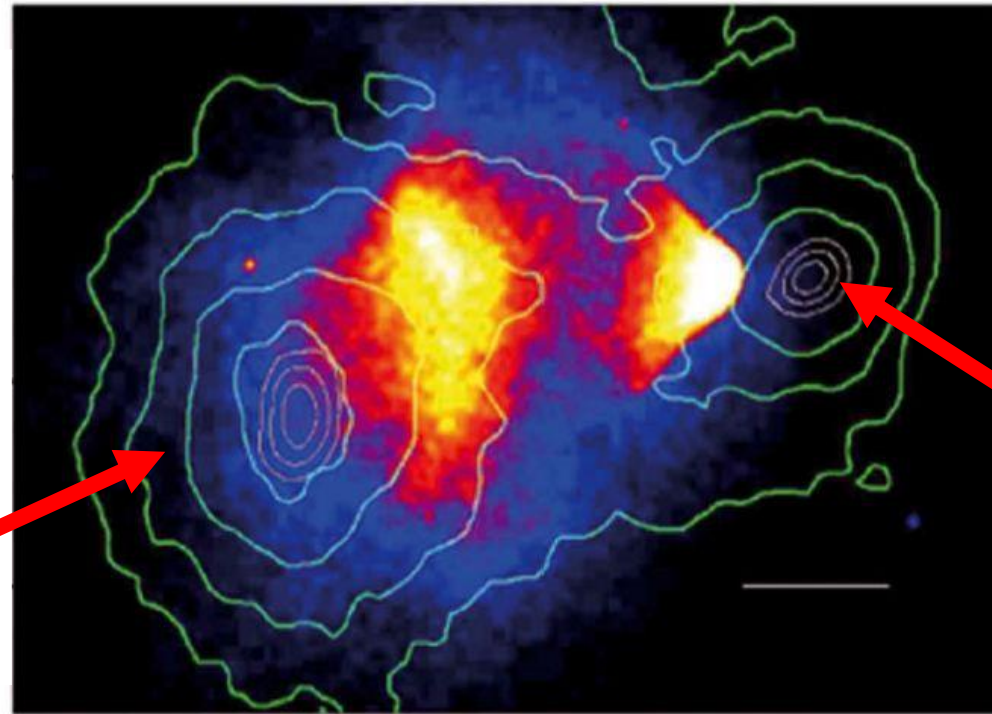


12^s

Visible and total matter have different distributions in galaxy clusters

Dark Matter evidence

Dark Matter existence is supported by astrophysics and cosmology



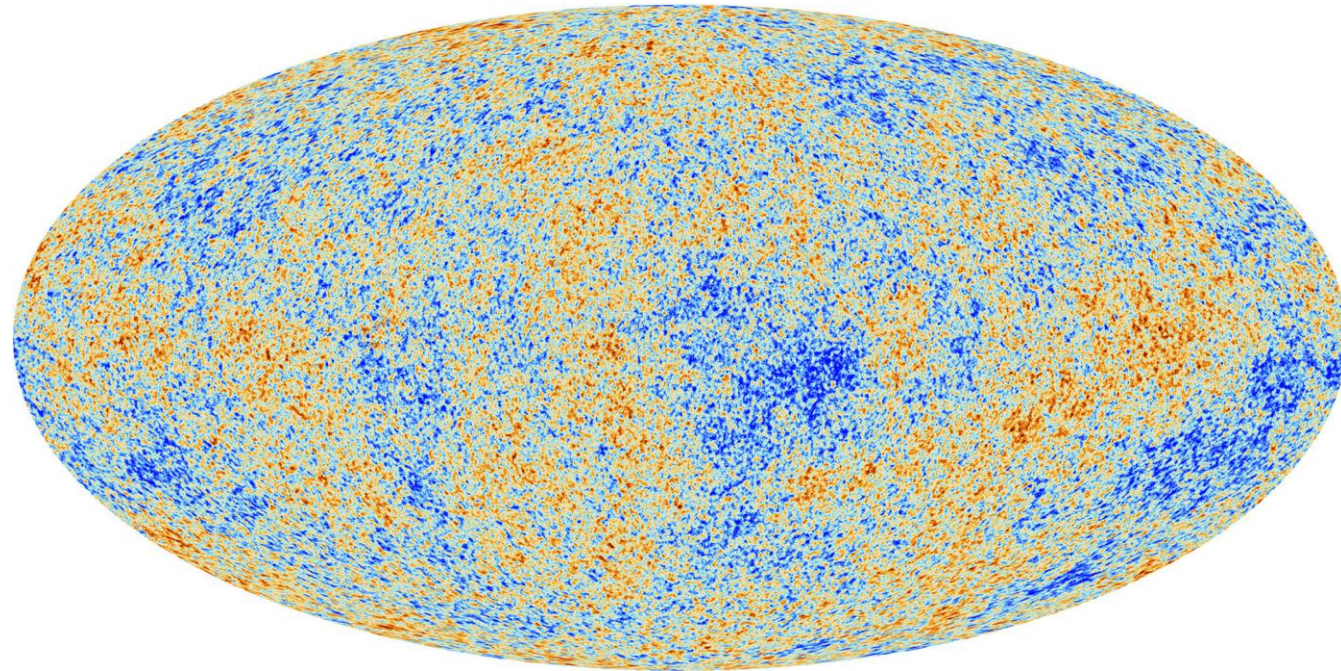
Dark Matter is collision-less:
the 2 DM clouds pass through
each other

12^s

Visible and total matter have different distributions in galaxy clusters

Dark Matter evidence

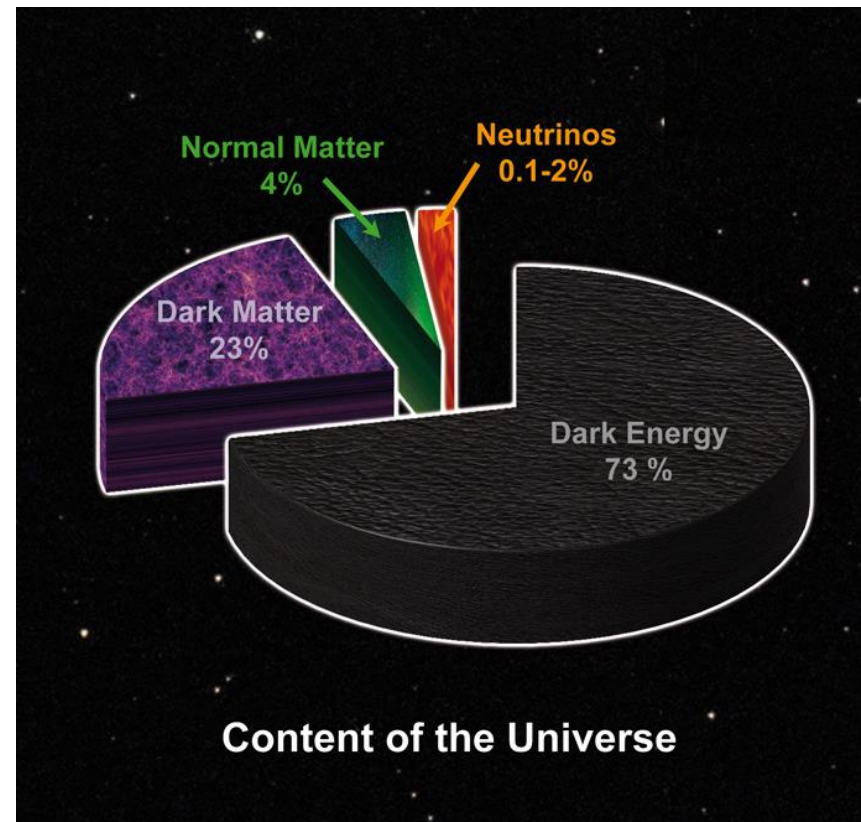
Dark Matter existence is supported by astrophysics and cosmology



CMB properties and structure formation require DM

Dark Matter evidence

Today most of the Universe is dark!



$$\Omega_{\text{DM}} h^2 \simeq 0.12$$

$$\Omega_{\text{DM}} \simeq 5\Omega_b$$

Dark Matter fills the 84% of the matter content of the Universe

Dark Matter properties

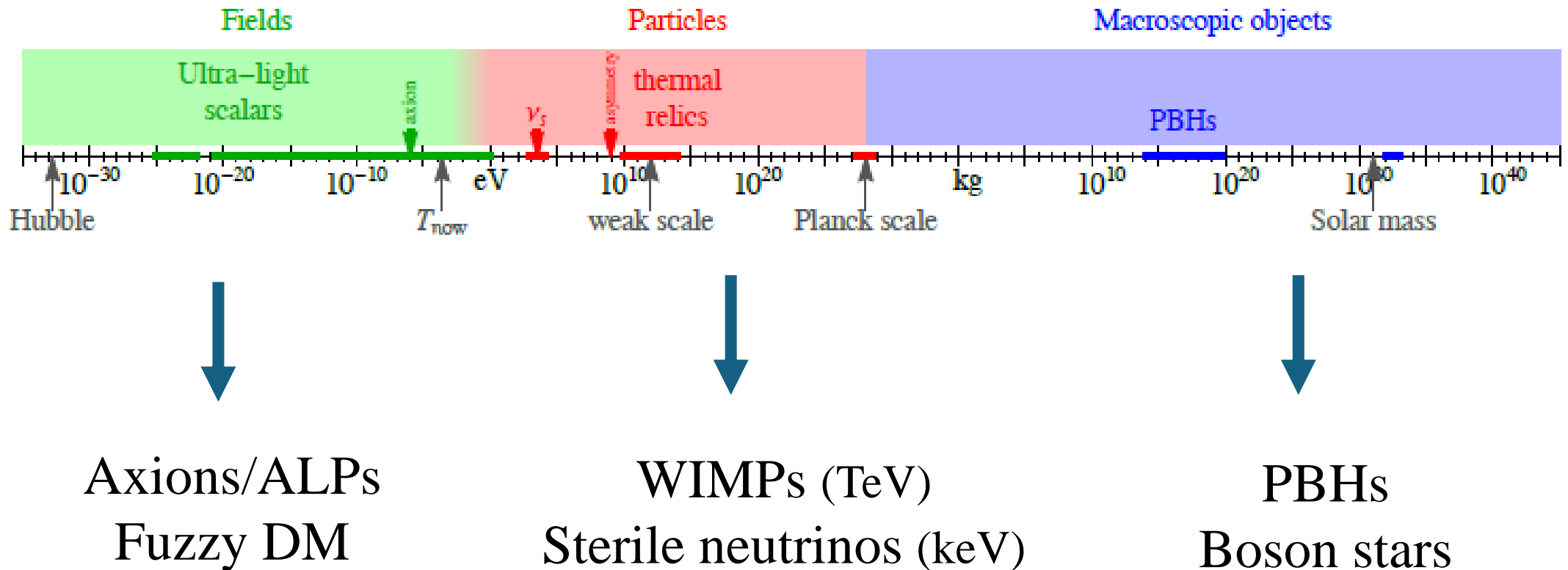
- Neutral and weakly interacting with the Standard Model sector
- Stable on cosmological scales
- Cold = non-relativistic at the time of structure formation

Dark Matter is an evidence of physics beyond the Standard Model

Dark Matter candidates

The mass range of DM candidates spans over 80 order of magnitudes

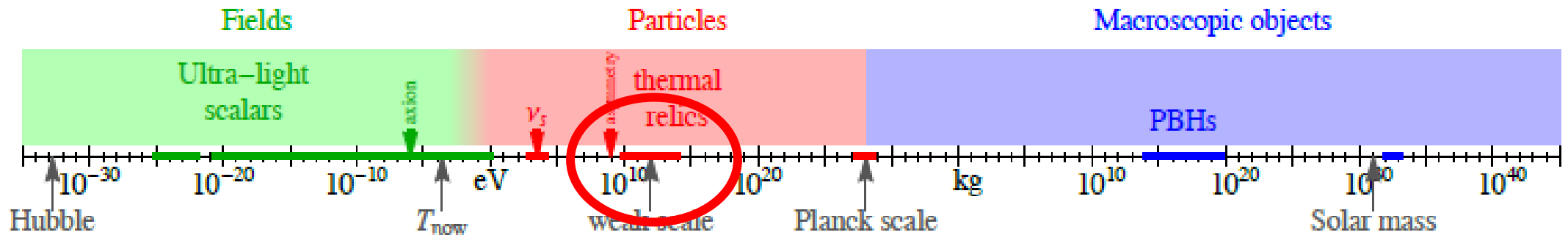
Figure made by *M. Cirelli, A. Strumia, J. Zupan*



Dark Matter candidates

The mass range of DM candidates spans over 80 order of magnitudes

Figure made by *M. Cirelli, A. Strumia, J. Zupan*



↓
New confining sector

Neutrino masses

Neutrinos are massless in the Standard Model

$$L = (\nu_L, e_L) \quad \text{No } \nu_R$$

$$\mathcal{L}_{\text{lepton}} = y_e \bar{L} H e_R + h.c.$$

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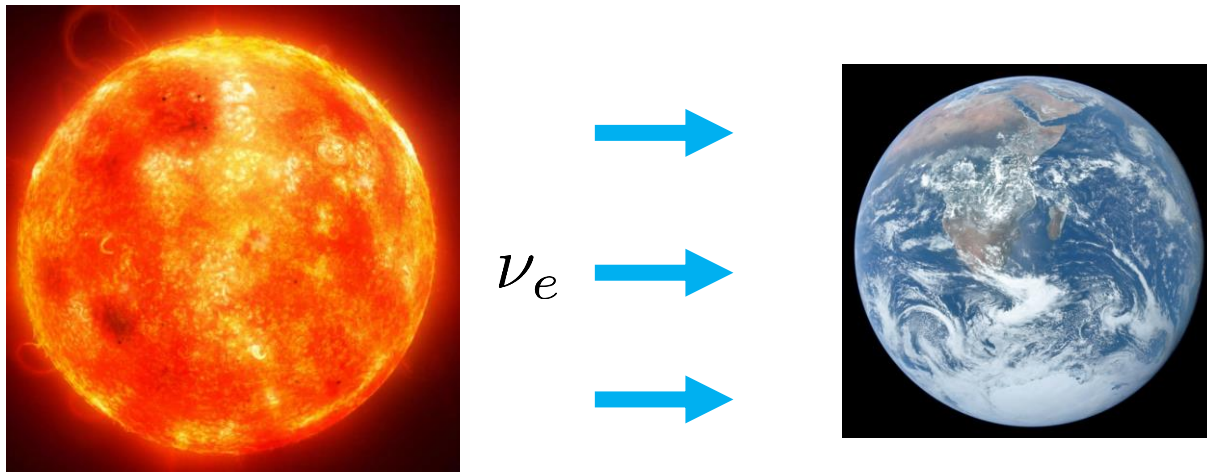
EWSB

$$\langle H \rangle = (0, \frac{v_H}{\sqrt{2}}) \quad \longrightarrow \quad \mathcal{L}_{\text{lepton}} = m_e (\bar{e}_L e_R + \bar{e}_R e_L) \quad \longrightarrow \quad \begin{aligned} m_e &= y_e v_H / \sqrt{2} \\ m_\nu &= 0 \end{aligned}$$

Accidental U(1) lepton number conservation

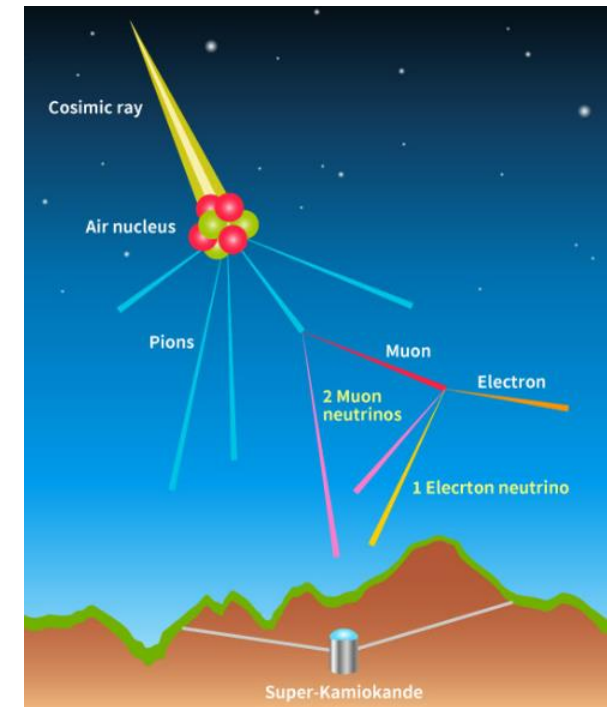
Neutrino masses

Solar neutrino problem



$$N_{\text{observed}} \approx \frac{1}{3} N_{\text{expected}}$$

Atmospheric neutrino problem



$$\frac{N_{\nu\mu}}{N_{\nu e}} < 2$$

Neutrino masses

Neutrino oscillations among different flavors solve the problems

Only possible if flavor basis \neq mass basis



Neutrinos must be massive!

Neutrino masses

Neutrino oscillations among different flavors solve the problems

Only possible if flavor basis \neq mass basis



Neutrinos must be massive!

Combining oscillation and cosmological data

$$0.05 \text{ eV} \lesssim \sum m_\nu \lesssim 0.12 \text{ eV}$$

Dirac neutrinos?

Introduce RHN $N_R \sim (1, 1)_0$

Assuming lepton number
conservation

$$\Delta\mathcal{L}_{\text{lepton}} \sim y_\nu \bar{L} \tilde{H} N_R$$

$$\langle H \rangle = \left(0, \frac{v_H}{\sqrt{2}}\right) \quad \longrightarrow \quad \mathcal{L}_\nu = m_\nu (\bar{\nu}_L N_R + \bar{N}_R \nu_L) \quad \longrightarrow \quad m_\nu = y_\nu v_H / \sqrt{2}$$

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$$m_\nu \sim 0.05 \text{ eV} \quad \longrightarrow \quad y_\nu \sim 10^{-13} \quad \longrightarrow \quad \text{un-observable!}$$

Why lepton number should be a good symmetry?

The Model

	$SU(3)_D$	\mathcal{Z}_4	generations
q_L	3	$-i$	1
q_R	3	i	1
N_L	1	i	3
N_R	1	i	3
L	1	i	3
e_R	1	i	3
σ	1	-1	1
φ	1	1	1

$$\mathcal{L}_{LN} = y_e \bar{L} H e_R + y_\nu \bar{L} \tilde{H} N_R + y_\varphi \varphi \overline{N_L} N_R + \text{h.c.},$$

$$\mathcal{L}_D = y_Q \sigma \overline{q_L} q_R + y_{N_L} \sigma \overline{N_L^c} N_L + y_{N_R} \sigma \overline{N_R^c} N_R + \text{h.c.},$$

$$V_{\sigma,\varphi} = (m_\sigma^2 + \lambda_\sigma \sigma^2 + \lambda_{\varphi\sigma} \varphi^2 + \lambda_{H\sigma} |H|^2) \sigma^2 + (\mu_\varphi^2 + \lambda_\varphi \varphi^2 + \lambda_{H\varphi} |H|^2) \varphi^2,$$

$$V_{\text{soft}} = (\kappa_\varphi \varphi^2 + \kappa_\sigma \sigma^2 + \kappa_H |H|^2) \varphi,$$

The Model


	$SU(3)_D$	Z_4	Z_2	$U(1)_D$	generations
q_L	3	$-i$	$+$	1	1
q_R	3	i	$+$	1	1
N_L	1	i	$+$	0	3
N_R	1	i	$-$	0	3
L	1	i	$-$	0	3
e_R	1	i	$-$	0	3
σ	1	-1	$+$	0	1
φ	1	1	$-$	0	1

$$\mathcal{L}_{LN} = y_e \bar{L} H e_R + y_\nu \bar{L} \tilde{H} N_R + y_\varphi \varphi \bar{N}_L N_R + \text{h.c.},$$

$$\mathcal{L}_D = y_Q \sigma \bar{q}_L q_R + y_{N_L} \sigma \bar{N}_L^c N_L + y_{N_R} \sigma \bar{N}_R^c N_R + \text{h.c.},$$

$$V_{\sigma,\varphi} = (m_\sigma^2 + \lambda_\sigma \sigma^2 + \lambda_{\varphi\sigma} \varphi^2 + \lambda_{H\sigma} |H|^2) \sigma^2 + (\mu_\varphi^2 + \lambda_\varphi \varphi^2 + \lambda_{H\varphi} |H|^2) \varphi^2,$$

$$V_{\text{soft}} = (\kappa_\varphi \varphi^2 + \kappa_\sigma \sigma^2 + \kappa_H |H|^2) \varphi,$$

Z_2  No $\bar{L} H N_L$ coupling (otherwise linear see-saw with different pheno)
 Generate dynamically Dirac mass $M_D \propto \langle \varphi \rangle$

The Model


	$SU(3)_D$	Z_4	Z_2	$U(1)_D$	generations
q_L	3	$-i$	$+$	1	1
q_R	3	i	$+$	1	1
N_L	1	i	$+$	0	3
N_R	1	i	$-$	0	3
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σ	1	-1	$+$	0	1
φ	1	1	$-$	0	1

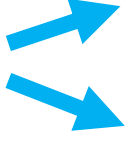
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$$V_{\text{soft}} = (\kappa_\varphi \varphi^2 + \kappa_\sigma \sigma^2 + \kappa_H |H|^2) \varphi,$$

Z_2  No $\bar{L} H N_L$ coupling (otherwise linear see-saw with different pheno)
 Generate dynamically Dirac mass $M_D \propto \langle \varphi \rangle$

No Domain Walls  Z_2 explicitly broken by V_{soft}
 Z_4 explicitly broken by $\langle \overline{q_L} q_R \rangle$

The Model

	SU(3) _D	Z ₄	Z ₂	U(1) _D	generations
q_L	3	$-i$	$+$	1	1
q_R	3	i	$+$	1	1
N_L	1	i	$+$	0	3
N_R	1	i	$-$	0	3
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$$\mathcal{L}_{LN} = y_e \bar{L} H e_R + y_\nu \bar{L} \tilde{H} N_R + y_\varphi \varphi \overline{N_L} N_R + \text{h.c.},$$

$$\begin{aligned} \mathcal{L}_D &= y_Q \sigma \overline{q_L} q_R + y_{N_L} \sigma \overline{N_L^c} N_L \\ &\quad + y_{N_R} \sigma \overline{N_R^c} N_R + \text{h.c.}, \end{aligned}$$

$$\begin{aligned} V_{\sigma,\varphi} &= (m_\sigma^2 + \lambda_\sigma \sigma^2 + \lambda_{\varphi\sigma} \varphi^2 + \lambda_{H\sigma} |H|^2) \sigma^2 \\ &\quad + (\mu_\varphi^2 + \lambda_\varphi \varphi^2 + \lambda_{H\varphi} |H|^2) \varphi^2, \end{aligned}$$

$$V_{\text{soft}} = (\kappa_\varphi \varphi^2 + \kappa_\sigma \sigma^2 + \kappa_H |H|^2) \varphi,$$

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & \mu & M_D \\ 0 & M_D^T & \mu' \end{pmatrix} \quad \begin{aligned} m_D &= y_\nu \langle H \rangle \\ M_D &= y_\varphi \langle \varphi \rangle \end{aligned}$$

$$\mu = y_Q y_{N_R} \frac{\Lambda_D^3}{m_\sigma^2} \quad \mu' = y_Q y_{N_L} \frac{\Lambda_D^3}{m_\sigma^2}$$

The Spectrum

The theory confines at the scale Λ_D



Mesons

The lightest meson is pseudo-scalar

$$m_{\mathcal{M}} \simeq \Lambda_D$$

$$f_{\mathcal{M}} \equiv \langle 0 | \bar{q} \gamma_5 q | \mathcal{M} \rangle \sim \Lambda_D^2$$

With 1 quark flavor there are no light dark pions!

The Spectrum

The theory confines at the scale Λ_D



Baryons

$\mathcal{B} \sim qqq$ bound state with spin $3/2$

$$m_{\mathcal{B}} \simeq 5\Lambda_D$$

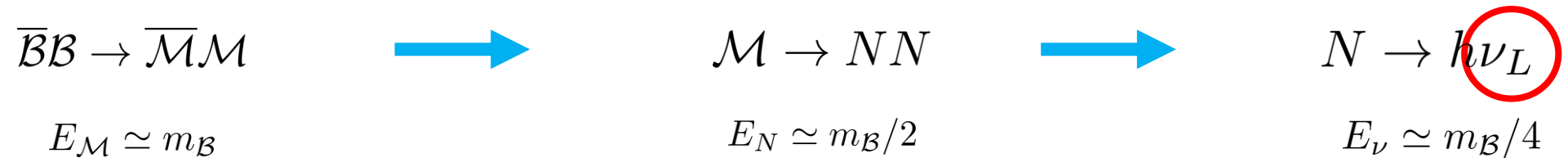
	$U(1)_D$
q_L	1
q_R	1
\mathcal{M}	0
\mathcal{B}	3

Higher-dimensional operators break dark baryon number

Are baryons decays compatible with bounds on DM?

Indirect Detection: neutrino lines

Baryons annihilate to mesons decay to heavy neutrinos decay to active neutrinos

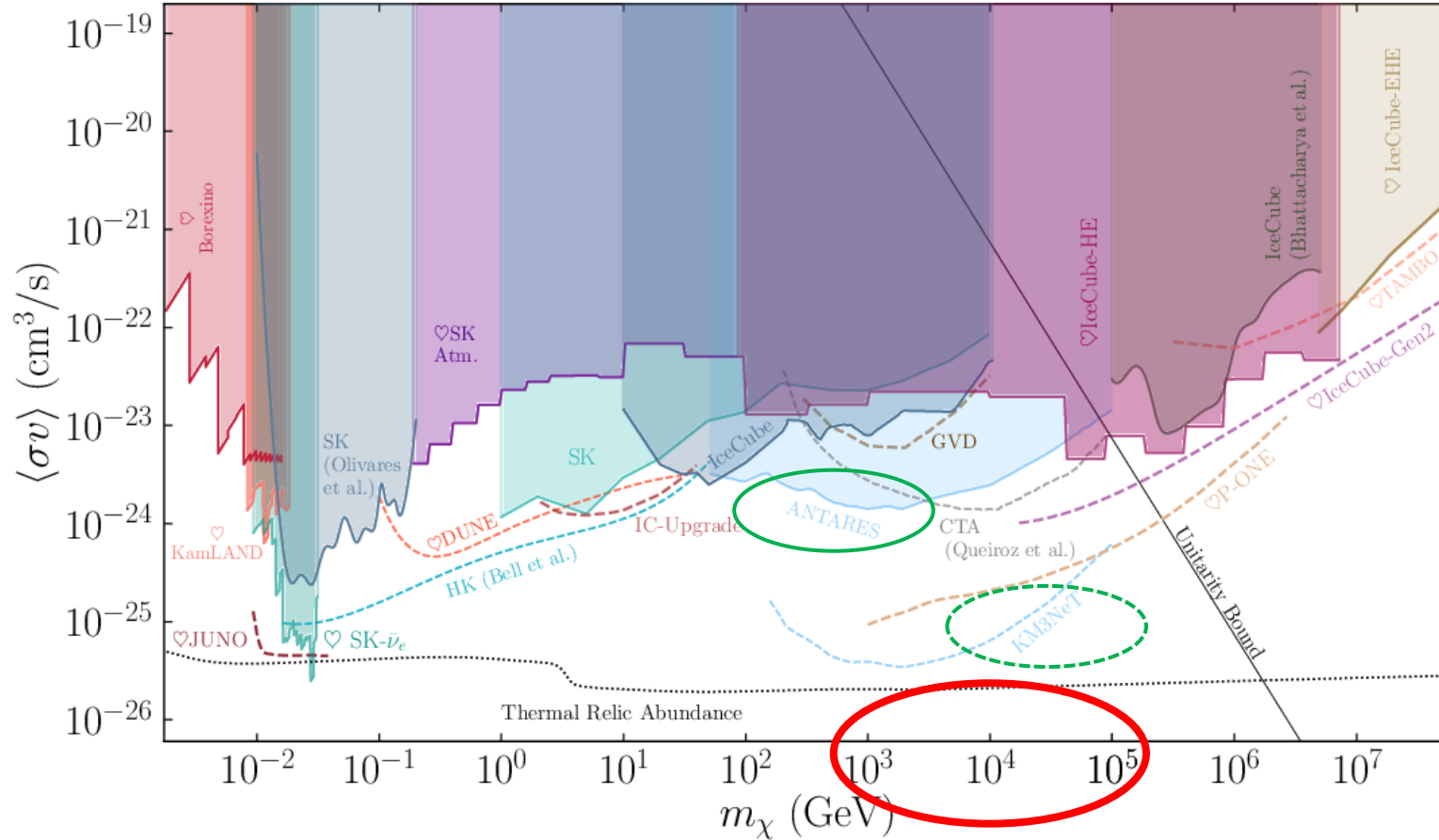


Monochromatic neutrino lines $E_\nu \simeq m_B/4 \sim (1 - 100) \text{ TeV}$

Testable with neutrino telescopes!

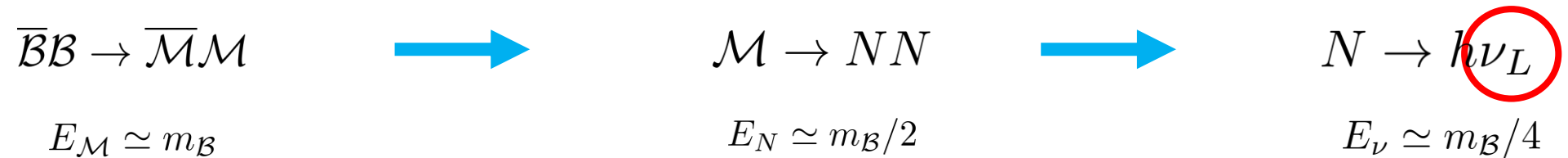
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Indirect Detection: neutrino lines

Baryons annihilate to mesons decay to heavy neutrinos decay to active neutrinos



Monochromatic neutrino lines $E_\nu \simeq m_B/4 \sim (1 - 100) \text{ TeV}$

Testable with neutrino telescopes!

Current bound from ANTARES collaboration $\longrightarrow \Lambda_D > 12 \text{ TeV} \sqrt{\frac{0.25 \times 10^{-24} \text{ cm}^3/\text{s}}{\langle \sigma v \rangle}}$

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$



σ is not in thermal bath

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$

Before dark confinement $T > \Lambda_D$

The dark sector is produced by steps and thermalize with the SM before confining

$$\begin{array}{l} LL, HH \leftrightarrow NN \\ LH \leftrightarrow N \end{array} \quad \rightarrow$$

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$

Before dark confinement $T > \Lambda_D$

The dark sector is produced by steps and thermalize with the SM before confining

$$\begin{array}{l} LL, HH \leftrightarrow NN \\ LH \leftrightarrow N \end{array}$$



$$NN \leftrightarrow \bar{q}q$$



keep thermal equilibrium

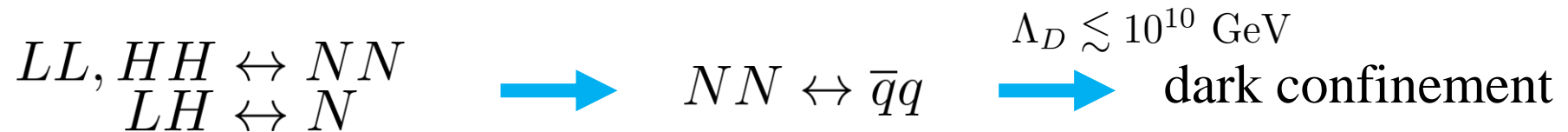
$$Y_q = \frac{n_q}{s} = \frac{135\zeta(3)}{\pi^4 g_s}$$

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$

Before dark confinement $T > \Lambda_D$

The dark sector is produced by steps and thermalize with the SM before confining



keep thermal equilibrium

$$Y_q = \frac{n_q}{s} = \frac{135\zeta(3)}{\pi^4 g_s}$$

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$

After dark confinement $T < \Lambda_D$

Quarks combine into hadrons: *baryons* and *mesons*

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$

After dark confinement $T < \Lambda_D$

Quarks combine into hadrons: *baryons* and *mesons*

Strong (dark) interactions convert baryons to mesons

$$\bar{B}B \rightarrow \bar{M}M$$

Baryons and mesons are kept in thermal equilibrium among them...

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$

After dark confinement $T < \Lambda_D$

Quarks combine into hadrons: *baryons* and *mesons*

Strong (dark) interactions convert baryons to mesons

$$\bar{B}B \rightarrow \bar{M}M$$

Baryons and mesons are kept in thermal equilibrium among them... ...and with the SM?

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$

After dark confinement $T < \Lambda_D$

All hadrons are not relativistic

$$m_{\text{hadron}} \gtrsim \Lambda_D \gtrsim T$$

The Cosmology

We assume that $m_\sigma \gg T_{\text{RH}} \gg M_D, \Lambda_D$

After dark confinement $T < \Lambda_D$

All hadrons are not relativistic

$$m_{\text{hadron}} \gtrsim \Lambda_D \gtrsim T$$

However they inherit the initial (relativistic) quark abundance

$$Y_q = \frac{n_q}{s} = \frac{135\zeta(3)}{\pi^4 g_s}$$