



**Universidad de Granada**

**FTAE**  
High Energy Theory

# On-Shell matching in effective field theories

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with M. Chala, J. López-Miras and J. Santiago [2406.xxxxx]

# Why do we need effective field theories?

EFT's are perturbative (Taylor) expansions of a full theory

In QFT's :

Operators of mass dimension  $d > 4$    $\mathcal{O}_i^{(d)}$

Useful for finite  
precision computations

Search for  
new physics

# Green's basis and redundant operators

EFT Lagrangian :

$$\mathcal{L} = \mathcal{L}^{(4)} + \sum_{d>4} \sum_i \frac{c_i^{(d)}}{\Lambda^{d-4}} \mathcal{O}_i^{(d)}$$

# Green's basis and redundant operators

EFT Lagrangian : 
$$\mathcal{L} = \mathcal{L}^{(4)} + \sum_{d>4} \sum_i \frac{c_i^{(d)}}{\Lambda^{d-4}} \mathcal{O}_i^{(d)}$$

## Valid operators

Local operators

Preserve the symmetries of the Lagrangian

Finite number of operators



Integration by parts



**Green's basis**

# Green's basis and redundant operators

## Green's basis of the bosonic sector of the SMEFT

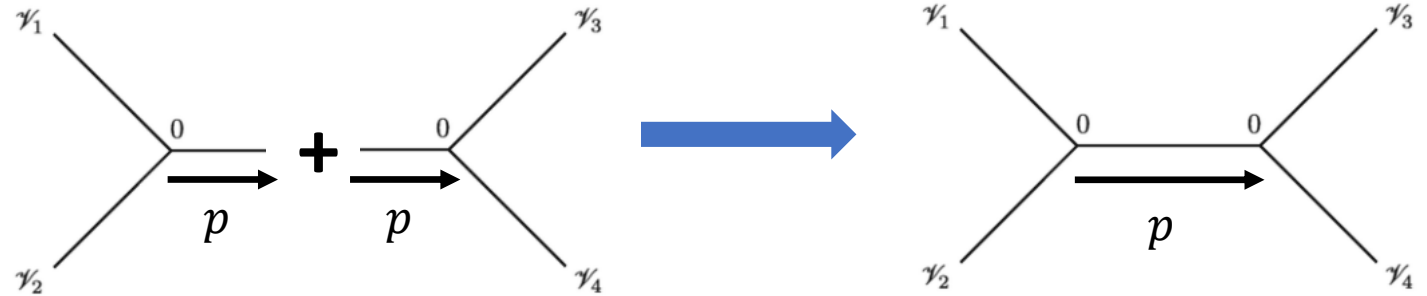
$X^3$		$X^2 H^2$		$H^2 D^4$	
$\mathcal{O}_{3G}$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{HG}$	$G_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$\mathcal{O}_{DH}$	$(D_\mu D^\mu H)^\dagger (D_\nu D^\nu H)$
$\mathcal{O}_{\widetilde{3G}}$	$f^{ABC} \widetilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{H\widetilde{G}}$	$\widetilde{G}_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$H^4 D^2$	
$\mathcal{O}_{3W}$	$\epsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{HW}$	$W_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{H\Box}$	$(H^\dagger H) \Box (H^\dagger H)$
$\mathcal{O}_{\widetilde{3W}}$	$\epsilon^{IJK} \widetilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{H\widetilde{W}}$	$\widetilde{W}_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{HD}$	$(H^\dagger D^\mu H)^\dagger (H^\dagger D_\mu H)$
$X^2 D^2$		$\mathcal{O}_{HB}$	$B_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}'_{HD}$	$(H^\dagger H) (D_\mu H)^\dagger (D^\mu H)$
$\mathcal{O}_{2G}$	$-\frac{1}{2} (D_\mu G^{A\mu\nu}) (D^\rho G_{\rho\nu}^A)$	$\mathcal{O}_{H\widetilde{B}}$	$\widetilde{B}_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}''_{HD}$	$(H^\dagger H) D_\mu (H^\dagger \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{2W}$	$-\frac{1}{2} (D_\mu W^{I\mu\nu}) (D^\rho W_{\rho\nu}^I)$	$\mathcal{O}_{HWB}$	$W_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$H^6$	
$\mathcal{O}_{2B}$	$-\frac{1}{2} (\partial_\mu B^{\mu\nu}) (\partial^\rho B_{\rho\nu})$	$\mathcal{O}_{H\widetilde{W}B}$	$\widetilde{W}_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$\mathcal{O}_H$	$(H^\dagger H)^3$
		$H^2 X D^2$			
		$\mathcal{O}_{WDH}$	$D_\nu W^{I\mu\nu} (H^\dagger i \overleftrightarrow{D}_\mu^I H)$		
		$\mathcal{O}_{BDH}$	$\partial_\nu B^{\mu\nu} (H^\dagger i \overleftrightarrow{D}_\mu H)$		

V. Gherardi, D. Marzocca y E. Venturini (2021) [\[2003.12525v5\]](#)

# Matching: Off-Shell vs On-shell

## Off-Shell matching

- Small number of diagrams (1 LPI)



- Heavy bridges contribution directly local

$$\sim \frac{1}{p^2 - M^2} \stackrel{p^2 \ll M^2}{=} -\frac{1}{M^2} \left( 1 + \frac{p^2}{M^2} + \frac{p^4}{M^4} + \dots \right)$$

- But requires the construction and reduction of the Green's basis

# Reduction to the physical basis

## Identification of redundant operators

Field redefinitions

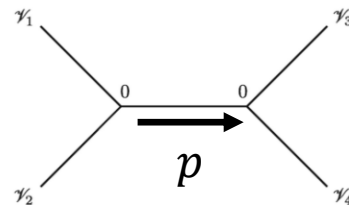
EOMs (only valid up to linear order)

Non-trivial process

Hard to program it in a systematic way

## On-Shell matching

- Huge number of diagrams



- There is delicate cancellation of non-local contributions between UV and EFT

$$\frac{1}{p^2 - m^2} \Big|_{\text{UV}} - \frac{1}{p^2 - m^2} \Big|_{\text{EFT}} = \text{Polynomial}(p^2)$$

# Reduction to the physical basis

## Identification of redundant operators

Field redefinitions

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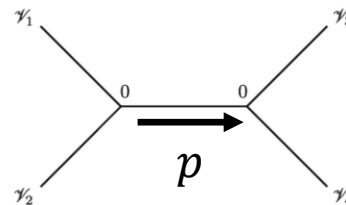


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## On-Shell matching

- Huge number of diagrams



- There is delicate cancellation of non-local contributions between UV and EFT

## Substitution of randomly generated physical momenta






M. Accettulli [2304.01589]

$$\frac{1}{p^2 - m^2} \Big|_{\text{UV}} - \frac{1}{p^2 - m^2} \Big|_{\text{EFT}} = \text{Polynomial}(p^2)$$



# On-Shell matching approach

- Find the Green's basis up to dimension  $d$    $\mathcal{L}_{Green}$
- Find the physical basis   $\mathcal{L}_{phys}$   

R. Fonseca [1907.12584]  
J.C. Criado [1901.03501]
- Compute n-points amplitudes with  $n \leq d$  **on-shell**  **By the substitution of randomly generated physical momenta**
- Solve the system  $\mathcal{M}_{i,Green} = \mathcal{M}_{i,phys}$

# Some results in the SMEFT

**HIGG'S SECTOR**

$$\mathcal{L}_{Green} = \mathcal{L}^{(4)} + \mathcal{L}_{Green}^{(6)}$$



$$\mathcal{L}_{phys} = \mathcal{L}^{(4)} + \mathcal{L}_{phys}^{(6)} + \mathcal{L}_{phys}^{(8)}$$

# Some results in the SMEFT

## HIGG'S SECTOR

$$\mathcal{L}_{Green} = \mathcal{L}^{(4)} + \mathcal{L}_{Green}^{(6)}$$



$$\mathcal{L}_{phys} = \mathcal{L}^{(4)} + \mathcal{L}_{phys}^{(6)} + \mathcal{L}_{phys}^{(8)}$$

$$\mathcal{L}^{(4)} = \frac{1}{2} (D_\mu H)^\dagger (D^\mu H) - m_0^2 H^\dagger H - \lambda (H^\dagger H)^2$$

$$\begin{aligned} \mathcal{L}_{Green}^{(6)} = & c_H (H^\dagger H)^3 + c_{H\Box} (H^\dagger H) \Box (H^\dagger H) + c_{HD} (H^\dagger D^\mu H)^\dagger (H^\dagger D_\mu H) + \\ & r'_{HD} (H^\dagger H) (D_\mu H)^\dagger (D^\mu H) + r''_{HD} (H^\dagger H) D_\mu \left( H^\dagger i \overleftrightarrow{D}^\mu H \right) + r_{DH} (D^2 H)^\dagger (D^2 H) \end{aligned}$$

# Some results in the SMEFT

## HIGG'S SECTOR

$$\mathcal{L}_{Green} = \mathcal{L}^{(4)} + \mathcal{L}_{Green}^{(6)}$$

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$$\mathcal{L}^{(4)} = \frac{1}{2} (D_\mu H)^\dagger (D^\mu H) - m_0^2 H^\dagger H - \lambda (H^\dagger H)^2$$

 $\mathcal{L}_{phys}^{(6)}$ 

$$\mathcal{L}_{Green}^{(6)} = c_H (H^\dagger H)^3 + c_{H\Box} (H^\dagger H) \Box (H^\dagger H) + c_{HD} (H^\dagger D^\mu H)^\dagger (H^\dagger D_\mu H) + r'_{HD} (H^\dagger H) (D_\mu H)^\dagger (D^\mu H) + r''_{HD} (H^\dagger H) D_\mu (H^\dagger i \overleftrightarrow{D}^\mu H) + r_{DH} (D^2 H)^\dagger (D^2 H)$$

# Some results in the SMEFT

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$$r'_{HD} (H^\dagger H) (D_\mu H)^\dagger (D^\mu H) + r''_{HD} (H^\dagger H) D_\mu \left( H^\dagger i \overleftrightarrow{D}^\mu H \right) + r_{DH} (D^2 H)^\dagger (D^2 H)$$

$$\mathcal{L}_{phys}^{(8)} = c_{H^8} (H^\dagger H)^4 + c_{H^6 D^2}^{(1)} (H^\dagger H)^2 (D_\mu H^\dagger D^\mu H) + c_{H^6 D^2}^{(2)} (H^\dagger H) (H^\dagger \sigma^I H) (D_\mu H^\dagger \sigma^I D^\mu H) +$$

$$c_{H^4 D^4}^{(1)} (D_\mu H^\dagger D_\nu H) (D^\nu H^\dagger D^\mu H) + c_{H^4 D^4}^{(2)} (D_\mu H^\dagger D_\nu H) (D^\mu H^\dagger D^\nu H) +$$

$$c_{H^4 D^4}^{(3)} (D^\mu H^\dagger D_\mu H) (D^\nu H^\dagger D_\nu H)$$

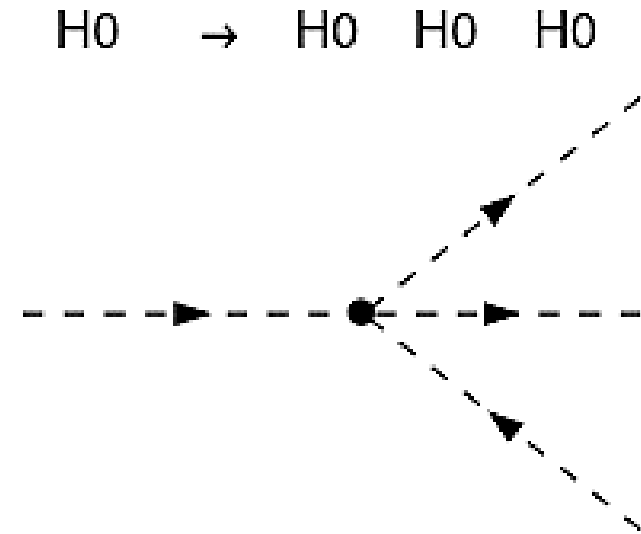
```

rules12 = Rules[4, 0, 10] /. {rules`k → k, rules`Pair → Pair} // Simplify;
equations = {};
For[j = 1, j ≤ Length[amp1], j++,
  [para cada [longitud]
    For[i = 1, i ≤ Length[rules12], i++,
      [para cada [longitud]
        final = amp1[[j]] /. Flatten[rules12[[i]]] // TermCollect;
        [aplana]
        final = I Sum[final[[aa], {aa, 1, Length[final]}] // Expand;
        [· suma [longitud [expande factores]
        final = final /. Sust;
        final = final /. {x^3 → 0, x^4 → 0, x^5 → 0, x^6 → 0} /. {x → 1};
        ampIR = final /. propEFT /. limitIR;
        ampUV = Z^2 final /. propEFT /. limitUV;
        ampsUV[[i]] = ampsUV[[i]] + ampUV;
        ampsIR[[i]] = ampsIR[[i]] + ampIR;

      ];
      AppendTo[equations, Table[ampsUV[[i]] == ampsIR[[i]], {i, 1, Length[rules12]}]];
      [añade al final [tabla [longitud]
    ];
  ];

solution1 = Solve[Flatten[equations], coefsol] /. massPhys // Simplify;
[resuelve [aplana [simplifica]

```



`rules12 = Rules[4, 0, 10] /. {rules`k → k, rules`Pair → Pair} // Simplify;` → Replacing momenta by randomly generated values

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equations = {};
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→ Running through every amplitude in the process

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Replacing momenta by randomly generated values  
 Running through every amplitude in the process  
 Setting both theories amplitudes with their propagators and wavefunction renormalizations

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Matching both theories

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      ampsIR[[i]] = ampsIR[[i]] + ampIR;
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→ Setting both theories amplitudes with their propagators and wavefunction renormalizations

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solution1 = Solve[Flatten[equations], coefsol] /. massPhys // Simplify;
```

→ Solving the system

```
[resuelve [aplana
```

```
[simplifica
```

# Some results in the SMEFT

## Final solution: redefinition of coefficients

$$c_H \rightarrow a_H - \lambda \text{mbd}^2 r_{DH} + \lambda \text{mbd} r_{HDp} + m^2 \left( 6 a_H r_{DH} + a_{HD} \lambda \text{mbd} r_{DH} - 8 a_{HDD} \lambda \text{mbd} r_{DH} - 11 \lambda \text{mbd}^2 r_{DH}^2 - \frac{a_{HD} r_{HDp}}{2} + 4 a_{HDD} r_{HDp} + 9 \lambda \text{mbd} r_{DH} r_{HDp} - \frac{r_{HDp}^2}{4} - r_{HDpp}^2 \right)$$

$$c_{H41} \rightarrow 0$$

$$c_{H42} \rightarrow 0$$

$$c_{H43} \rightarrow 0$$

$$c_{H61} \rightarrow a_{HD} \lambda \text{mbd} r_{DH} + 8 a_{HDD} \lambda \text{mbd} r_{DH} + \lambda \text{mbd}^2 r_{DH}^2 - \frac{a_{HD} r_{HDp}}{2} - 4 a_{HDD} r_{HDp} + 3 \lambda \text{mbd} r_{DH} r_{HDp} - \frac{7 r_{HDp}^2}{4} + r_{HDpp}^2$$


$$c_{H62} \rightarrow 2 a_{HD} \lambda \text{mbd} r_{DH} - a_{HD} r_{HDp}$$

$$c_{HD} \rightarrow a_{HD} + 4 a_{HD} m^2 r_{DH}$$

$$c_{HDD} \rightarrow \frac{1}{2} (2 a_{HDD} + r_{HDp}) + m^2 (4 a_{HDD} r_{DH} + 2 r_{DH} r_{HDp})$$

$$m_{H^2} \rightarrow m^2 + m^4 r_{DH} + 2 m^6 r_{DH}^2$$

$$\lambda \rightarrow \lambda \text{mbd} + m^2 (4 \lambda \text{mbd} r_{DH} - 2 r_{HDp}) + m^4 (16 \lambda \text{mbd} r_{DH}^2 - 10 r_{DH} r_{HDp})$$



J. Aebischer, M. Fael and J. Fuentes-Martín | 2023  
[\[2307.08745v1\]](#)

V. Gherardi, D. Marzocca and E. Venturini | 2021  
[\[2003.12525v5\]](#)

# Some results in the SMEFT

## Final solution: redefinition of coefficients

$$c_H \rightarrow a_H - \lambda^2 r_{DH} + \lambda r_{HDp} + m^2 \left( 6 a_H r_{DH} + a_{HD} \lambda r_{DH} - 8 a_{HDD} \lambda r_{DH} - 11 \lambda^2 r_{DH}^2 - \frac{a_{HD} r_{HDp}}{2} + 4 a_{HDD} r_{HDp} + 9 \lambda r_{DH} r_{HDp} - \frac{r_{HDp}^2}{4} - r_{HDpp}^2 \right)$$

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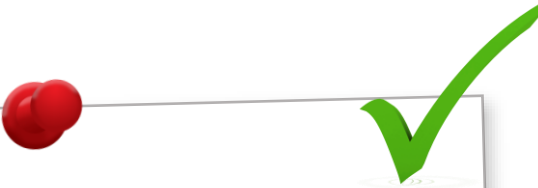
$$c_{H62} \rightarrow 2 a_{HD} \lambda r_{DH} - a_{HD} r_{HDp}$$

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$$m_H^2 \rightarrow m^2 + m^4 r_{DH} + 2 m^6 r_{DH}^2$$

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# Some results in the SMEFT

## Final solution: redefinition of coefficients

$$c_H \rightarrow a_H - \lambda \text{mbd}^2 r_{DH} + \lambda \text{mbd} r_{HDp} + m^2 \left( 6 a_H r_{DH} + a_{HD} \lambda \text{mbd} r_{DH} - 8 a_{HDD} \lambda \text{mbd} r_{DH} - 11 \lambda \text{mbd}^2 r_{DH}^2 - \frac{a_{HD} r_{HDp}}{2} + 4 a_{HDD} r_{HDp} + 9 \lambda \text{mbd} r_{DH} r_{HDp} - \frac{r_{HDp}^2}{4} - r_{HDpp}^2 \right)$$

$$c_{H41} \rightarrow 0$$

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$$c_{H62} \rightarrow 2 a_{HD} \lambda \text{mbd} r_{DH} - a_{HD} r_{HDp}$$

$$c_{HD} \rightarrow a_{HD} + 4 a_{HD} m^2 r_{DH}$$

$$c_{HDD} \rightarrow \frac{1}{2} (2 a_{HDD} + r_{HDp}) + m^2 (4 a_{HDD} r_{DH} + 2 r_{DH} r_{HDp})$$

$$m_{H^2} \rightarrow m^2 + m^4 r_{DH} + 2 m^6 r_{DH}^2$$

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# Future work



**BOSONIC  
SECTOR**

$X^3$		$X^2 H^2$		$H^2 D^4$	
$\mathcal{O}_{3G}$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{HG}$	$G_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$\mathcal{O}_{DH}$	$(D_\mu D^\mu H)^\dagger (D_\nu D^\nu H)$
$\mathcal{O}_{3\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{H\tilde{G}}$	$\tilde{G}_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$H^4 D^2$	
$\mathcal{O}_{3W}$	$\epsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{HW}$	$W_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{H\Box}$	$(H^\dagger H) \Box (H^\dagger H)$
$\mathcal{O}_{3\tilde{W}}$	$\epsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{H\tilde{W}}$	$\tilde{W}_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{HD}$	$(H^\dagger D^\mu H)^\dagger (H^\dagger D_\mu H)$
$X^2 D^2$		$\mathcal{O}_{HB}$	$B_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}'_{HD}$	$(H^\dagger H) (D_\mu H)^\dagger (D^\mu H)$
$\mathcal{O}_{2G}$	$-\frac{1}{2} (D_\mu G^{A\mu\nu}) (D^\rho G_{\rho\nu}^A)$	$\mathcal{O}_{H\tilde{B}}$	$\tilde{B}_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}''_{HD}$	$(H^\dagger H) D_\mu (H^\dagger \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{2W}$	$-\frac{1}{2} (D_\mu W^{I\mu\nu}) (D^\rho W_{\rho\nu}^I)$	$\mathcal{O}_{HWB}$	$W_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$H^6$	
$\mathcal{O}_{2B}$	$-\frac{1}{2} (\partial_\mu B^{\mu\nu}) (\partial^\rho B_{\rho\nu})$	$\mathcal{O}_{H\tilde{W}B}$	$\tilde{W}_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$\mathcal{O}_H$	$(H^\dagger H)^3$
		$H^2 X D^2$			
		$\mathcal{O}_{WDH}$	$D_\nu W^{I\mu\nu} (H^\dagger i \overleftrightarrow{D}_\mu^I H)$		
		$\mathcal{O}_{BDH}$	$\partial_\nu B^{\mu\nu} (H^\dagger i \overleftrightarrow{D}_\mu H)$		

# Future work

**BOSONIC  
SECTOR**

$X^3$		$X^2 H^2$		$H^2 D^4$	
$\mathcal{O}_{3G}$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{HG}$	$G_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$\mathcal{O}_{DH}$	$(D_\mu D^\mu H)^\dagger (D_\nu D^\nu H)$
$\mathcal{O}_{3\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{H\tilde{G}}$	$\tilde{G}_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$H^4 D^2$	
$\mathcal{O}_{3W}$	$\epsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{HW}$	$W_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{H\Box}$	$(H^\dagger H) \Box (H^\dagger H)$
$\mathcal{O}_{3\tilde{W}}$	$\epsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{H\tilde{W}}$	$\tilde{W}_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{HD}$	$(H^\dagger D^\mu H)^\dagger (H^\dagger D_\mu H)$
$X^2 D^2$		$\mathcal{O}_{HB}$	$B_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}'_{HD}$	$(H^\dagger H) (D_\mu H)^\dagger (D^\mu H)$
$\mathcal{O}_{2G}$	$-\frac{1}{2} (D_\mu G^{A\mu\nu}) (D^\rho G_{\rho\nu}^A)$	$\mathcal{O}_{H\tilde{B}}$	$\tilde{B}_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}''_{HD}$	$(H^\dagger H) D_\mu (H^\dagger \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{2W}$	$-\frac{1}{2} (D_\mu W^{I\mu\nu}) (D^\rho W_{\rho\nu}^I)$	$\mathcal{O}_{HWB}$	$W_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$H^6$	
$\mathcal{O}_{2B}$	$-\frac{1}{2} (\partial_\mu B^{\mu\nu}) (\partial^\rho B_{\rho\nu})$	$\mathcal{O}_{H\tilde{W}B}$	$\tilde{W}_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$\mathcal{O}_H$	$(H^\dagger H)^3$
		$H^2 X D^2$			
		$\mathcal{O}_{WDH}$	$D_\nu W^{I\mu\nu} (H^\dagger i \overleftrightarrow{D}_\mu^I H)$		
		$\mathcal{O}_{BDH}$	$\partial_\nu B^{\mu\nu} (H^\dagger i \overleftrightarrow{D}_\mu H)$		



# Future work

## BOSONIC SECTOR

$$m_0^2 \rightarrow m_0^2$$

$$\lambda \rightarrow \lambda - 2m_0^2 r'_{HD}$$

$$c_{H^4 D^4}^{(1)} \rightarrow 2r_{BDH}^2$$

$$c_{H^4 D^4}^{(2)} \rightarrow -2r_{BDH}^2$$

$$c_{H^4 D^4}^{(3)} \rightarrow 0$$

$$c_{H\Box} \rightarrow c_{H\Box} + \frac{1}{2}g' r_{BDH} + \frac{1}{2}r'_{HD}$$

$$c_{HD} \rightarrow c_{HD} + 2g' r_{BDH}$$

$X^3$		$X^2 H^2$		$H^2 D^4$	
$\mathcal{O}_{3G}$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{HG}$	$G_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$\mathcal{O}_{DH}$	$(D_\mu D^\mu H)^\dagger (D_\nu D^\nu H)$
$\mathcal{O}_{3\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{H\tilde{G}}$	$\tilde{G}_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$H^4 D^2$	
$\mathcal{O}_{3W}$	$\epsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{HW}$	$W_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{H\Box}$	$(H^\dagger H) \Box (H^\dagger H)$
$\mathcal{O}_{3\tilde{W}}$	$\epsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{H\tilde{W}}$	$\tilde{W}_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{HD}$	$(H^\dagger D^\mu H)^\dagger (H^\dagger D_\mu H)$
$X^2 D^2$		$\mathcal{O}_{HB}$	$B_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}'_{HD}$	$(H^\dagger H) (D_\mu H)^\dagger (D^\mu H)$
$\mathcal{O}_{2G}$	$-\frac{1}{2} (D_\mu G^{A\mu\nu}) (D^\rho G_{\rho\nu}^A)$	$\mathcal{O}_{H\tilde{B}}$	$\tilde{B}_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}''_{HD}$	$(H^\dagger H) D_\mu (H^\dagger \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{2W}$	$-\frac{1}{2} (D_\mu W^{I\mu\nu}) (D^\rho W_{\rho\nu}^I)$	$\mathcal{O}_{HWB}$	$W_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$H^6$	
$\mathcal{O}_{2B}$	$-\frac{1}{2} (\partial_\mu B^{\mu\nu}) (\partial^\rho B_{\rho\nu})$	$\mathcal{O}_{H\tilde{W}B}$	$\tilde{W}_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$\mathcal{O}_H$	$(H^\dagger H)^3$
		$H^2 X D^2$			
		$\mathcal{O}_{WDH}$	$D_\nu W^{I\mu\nu} (H^\dagger i \overleftrightarrow{D}_\mu^I H)$		
		$\mathcal{O}_{BDH}$	$\partial_\nu B^{\mu\nu} (H^\dagger i \overleftrightarrow{D}_\mu H)$		

$$D_\mu = \partial_\mu - ig' B_\mu$$

$$g' \rightarrow g'$$

$$c_{HB} \rightarrow c_{HB}$$

# Future work

## BOSONIC SECTOR

$$m_0^2 \rightarrow m_0^2$$

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$X^3$		$X^2 H^2$		$H^2 D^4$	
$\mathcal{O}_{3G}$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{HG}$	$G_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$\mathcal{O}_{DH}$	$(D_\mu D^\mu H)^\dagger (D_\nu D^\nu H)$
$\mathcal{O}_{3\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$\mathcal{O}_{H\tilde{G}}$	$\tilde{G}_{\mu\nu}^A G^{A\mu\nu} (H^\dagger H)$	$H^4 D^2$	
$\mathcal{O}_{3W}$	$\epsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{HW}$	$W_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{H\Box}$	$(H^\dagger H) \Box (H^\dagger H)$
$\mathcal{O}_{3\tilde{W}}$	$\epsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$\mathcal{O}_{H\tilde{W}}$	$\tilde{W}_{\mu\nu}^I W^{I\mu\nu} (H^\dagger H)$	$\mathcal{O}_{HD}$	$(H^\dagger D^\mu H)^\dagger (H^\dagger D_\mu H)$
$X^2 D^2$		$\mathcal{O}_{HB}$	$B_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}'_{HD}$	$(H^\dagger H) (D_\mu H)^\dagger (D^\mu H)$
$\mathcal{O}_{2G}$	$-\frac{1}{2} (D_\mu G^{A\mu\nu}) (D^\rho G_{\rho\nu}^A)$	$\mathcal{O}_{H\tilde{B}}$	$\tilde{B}_{\mu\nu} B^{\mu\nu} (H^\dagger H)$	$\mathcal{O}''_{HD}$	$(H^\dagger H) D_\mu (H^\dagger i \overleftrightarrow{D}^\mu H)$
$\mathcal{O}_{2W}$	$-\frac{1}{2} (D_\mu W^{I\mu\nu}) (D^\rho W_{\rho\nu}^I)$	$\mathcal{O}_{HWB}$	$W_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$H^6$	
$\mathcal{O}_{2B}$	$-\frac{1}{2} (\partial_\mu B^{\mu\nu}) (\partial^\rho B_{\rho\nu})$	$\mathcal{O}_{H\tilde{W}B}$	$\tilde{W}_{\mu\nu}^I B^{\mu\nu} (H^\dagger \sigma^I H)$	$\mathcal{O}_H$	$(H^\dagger H)^3$
		$H^2 X D^2$			
		$\mathcal{O}_{WDH}$	$D_\nu W^{I\mu\nu} (H^\dagger i \overleftrightarrow{D}_\mu^I H)$		
		$\mathcal{O}_{BDH}$	$\partial_\nu B^{\mu\nu} (H^\dagger i \overleftrightarrow{D}_\mu H)$		

$$D_\mu = \partial_\mu - ig' B_\mu$$

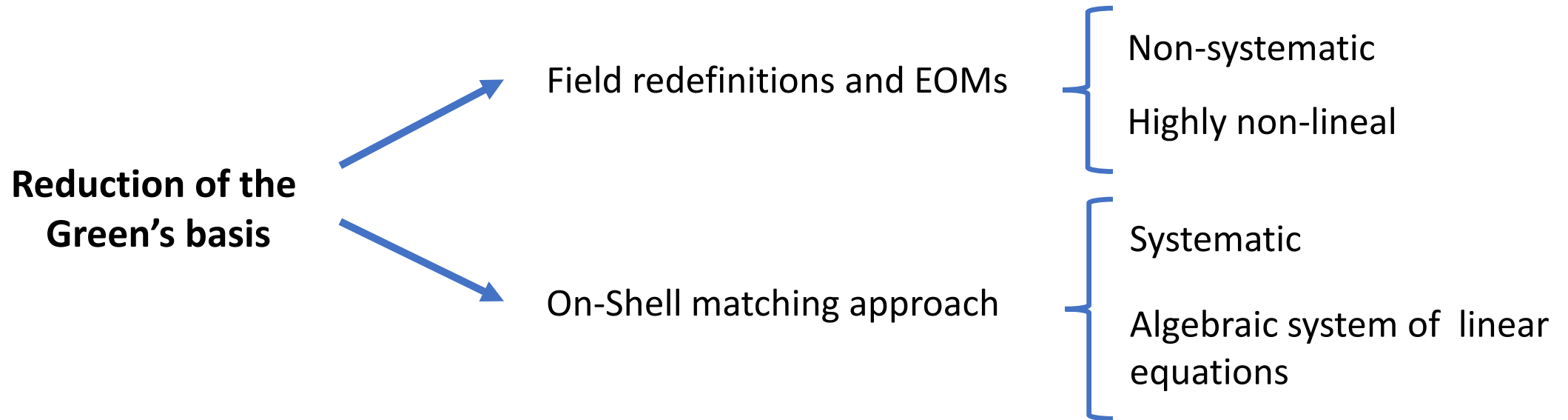
$$g' \rightarrow g'$$

$$c_{HB} \rightarrow c_{HB}$$

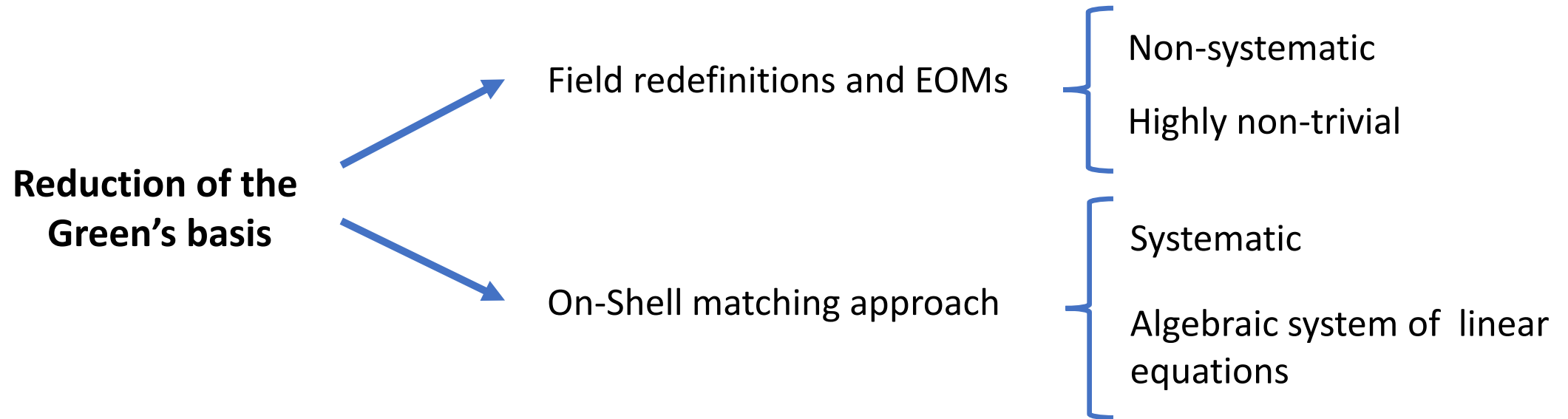
Fermions ✓

Evanescent operators

# Notice that ...



# Notice that ...



The reduction of **ANY** theory to **ANY** physical basis will be completely **AUTOMATIC**



Universidad de Granada

**FTAE**  
High Energy Theory

**THANKS FOR YOUR ATTENTION !**

# Generation of random momenta

$$SL(2, \mathbb{C}) \cong SU(2)_L \times SU(2)_R \quad \left\{ \begin{array}{l} \lambda \in SU(2)_L \\ \tilde{\lambda} \in SU(2)_R \end{array} \right. \quad \begin{array}{l} \lambda^\alpha = \varepsilon^{\alpha\beta} \lambda_\beta \\ \tilde{\lambda}_{\dot{\alpha}} = \varepsilon_{\dot{\alpha}\dot{\beta}} \tilde{\lambda}^{\dot{\beta}} \end{array}$$

**Massless momenta :**  $P_{\alpha\dot{\alpha}} = \lambda_\alpha \tilde{\lambda}_{\dot{\alpha}} \quad \rightarrow \quad P = p_\mu \sigma^\mu = \begin{pmatrix} p_0 + p_3 & p_1 - ip_2 \\ p_1 + ip_2 & p_0 - p_3 \end{pmatrix}$

**Massive momenta :**  $P^\mu := q^\mu + \frac{m^2}{2q \cdot k} k^\mu \quad \left| \begin{array}{l} q^2, k^2 = 0 \\ q_{\alpha\dot{\alpha}} = \lambda_\alpha \tilde{\lambda}_{\dot{\alpha}} \\ k_{\alpha\dot{\alpha}} = \mu_\alpha \tilde{\mu}_{\dot{\alpha}} \end{array} \right.$

# Evanescent operators

$$\mathcal{R} = \alpha \mathcal{O} \quad \xrightarrow{d = 4 - 2\epsilon} \quad \mathcal{R} = \alpha \mathcal{O} + \mathcal{E}$$

$$IR^{(0)} + IR^{(1)} = UV^{(0)} + UV^{(1)}$$

$\mathcal{O}(\epsilon)$

Additional finite local contributions in loop amplitudes

$$IR^{(0)} + IR_{soft}^{(1)} = UV^{(0)} + UV_{hard}^{(1)} + UV_{soft}^{(1)}$$

We take the hard region

$$\int \mathcal{O} = \frac{1}{\epsilon} (a + b_O \epsilon)$$

$$\int \mathcal{R} = \frac{1}{\epsilon} (a + b_{\mathcal{R}} \epsilon)$$

$$\int \mathcal{R} - \mathcal{O} = \frac{1}{\epsilon} (b_{\mathcal{R}} \epsilon - b_O \epsilon) = b$$

$$\text{---} \circlearrowleft \text{---} \stackrel{\text{1PI}}{=} \frac{i}{p^2 - m^2 - \Pi(p^2)} = \frac{iZ}{p^2 - m_{phys}^2} + \dots,$$

$$p^2 - m^2 - \Pi(p^2) \Big|_{p^2=m_{phys}^2} = 0$$

$$\Pi(p^2) = \Pi(m_{phys}^2) + \Pi'(m_{phys}^2)(p^2 - m_{phys}^2) + \dots$$

$$\begin{aligned} \frac{i}{p^2 - m^2 - \Pi(p^2)} &= \frac{i}{p^2 - m^2 - \left( \Pi(m_{phys}^2) + \Pi'(m_{phys}^2)(p^2 - m_{phys}^2) + \dots \right)} \\ &= \frac{i}{(p^2 - m_{phys}^2) \left( 1 - \Pi'(m_{phys}^2) + \dots \right)} \rightsquigarrow \frac{i \left( 1 - \Pi'(m_{phys}^2) \right)^{-1}}{(p^2 - m_{phys}^2)} \end{aligned}$$