

Hubble-induced phase transitions

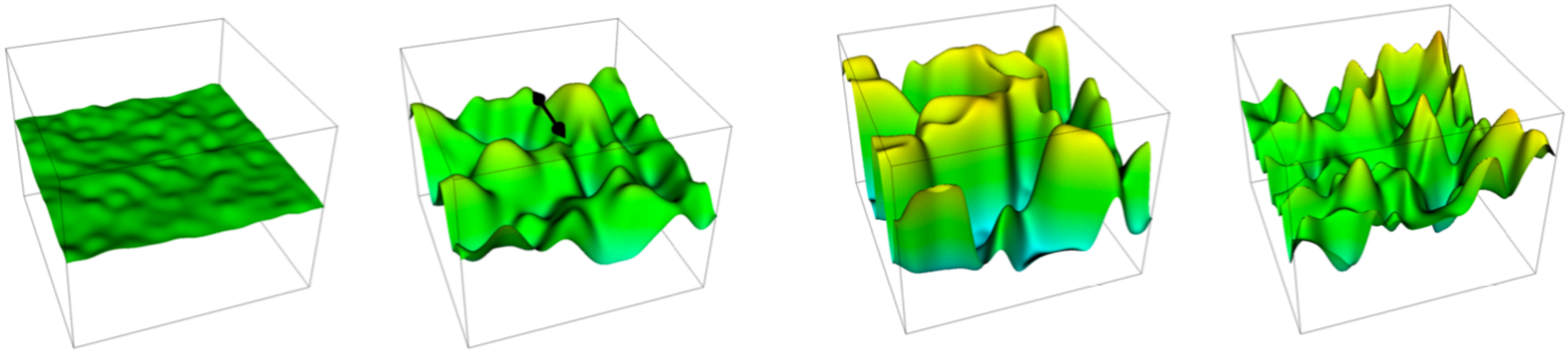
Javier Rubio

Based on D.Bettoni, A. Lopez-Eiguren, JR, JCAP 01 (2022) 01, 002
G. Laverda, JR, JCAP 03 (2024) 033



The general paradigm

$$\frac{\mathcal{L}}{\sqrt{-g}} = \frac{M_P^2}{2} R - \frac{1}{2} (\partial\chi)^2 - f(R, R_{\mu\nu}) \chi^2 - V(\chi)$$



- Natural triggering mechanism for phase transitions
- Non-thermal & non-perturbative
- Short-lived topological defects
- Specific gravitational waves signatures

A dedicated program

1. Quintessential Affleck-Dine baryogenesis with non-minimal couplings,
D. Bettoni, J. Rubio Phys.Lett.B 784 (2018) 122-129
2. Gravitational waves from global cosmic strings in quintessential inflation,
D. Bettoni, G. Domènech, J. Rubio, JCAP 02 (2019) 034
3. Hubble-induced phase transitions: Walls are not forever.
D. Bettoni, J. Rubio, JCAP 01 (2020) 002
4. Hubble-induced phase transitions on the lattice with applications to Ricci reheating.
D. Bettoni, J.Rubio, JCAP 01 (2022) 01, 002
5. Ricci reheating reloaded,
G. Laverda, JCAP 03 (2024) 033
6. From Hubble to Bubble,
M. Kierkla, G.Laverda, M. Lewicki, A. Mantziris, M.Piani, JHEP 11 (2023) 077
7. The rise and fall of the Standard-Model Higgs: electroweak vacuum stability during kination.
G. Laverda, J. Rubio, JHEP 05 (2024) 339

For a review see [D. Bettoni, JR, Galaxies 10 \(2022\) 1, 22](#)

A worked-out example

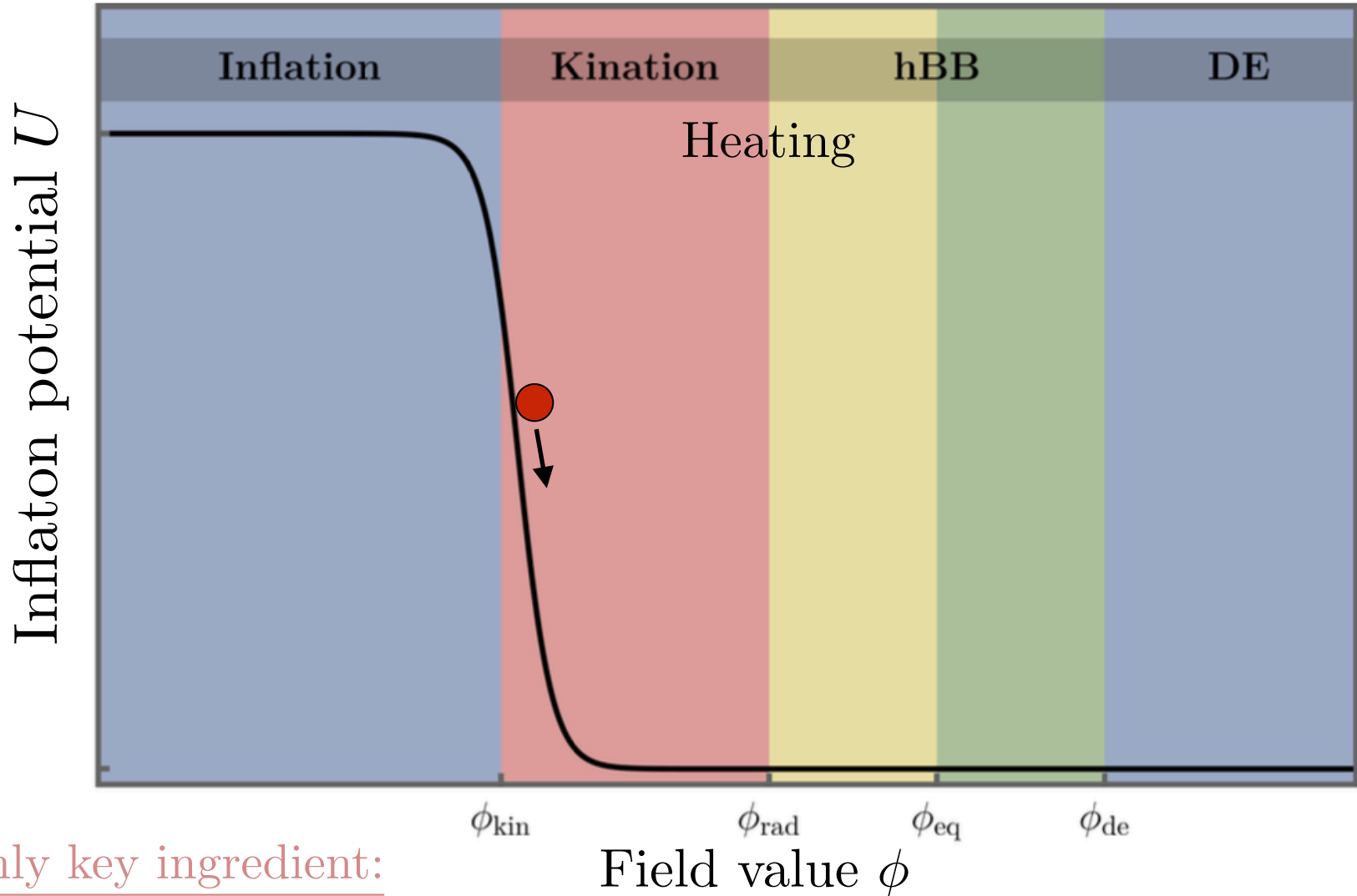
- A single scalar field ϕ for both inflation and dark energy
- A non-minimal coupling of a spectator field χ to gravity

$$\frac{\mathcal{L}}{\sqrt{-g}} = \frac{M_P^2}{2} R - \frac{1}{2} (\partial\chi)^2 - \xi R \chi^2 - V(\chi) + \mathcal{L}_\phi$$

Interesting outputs

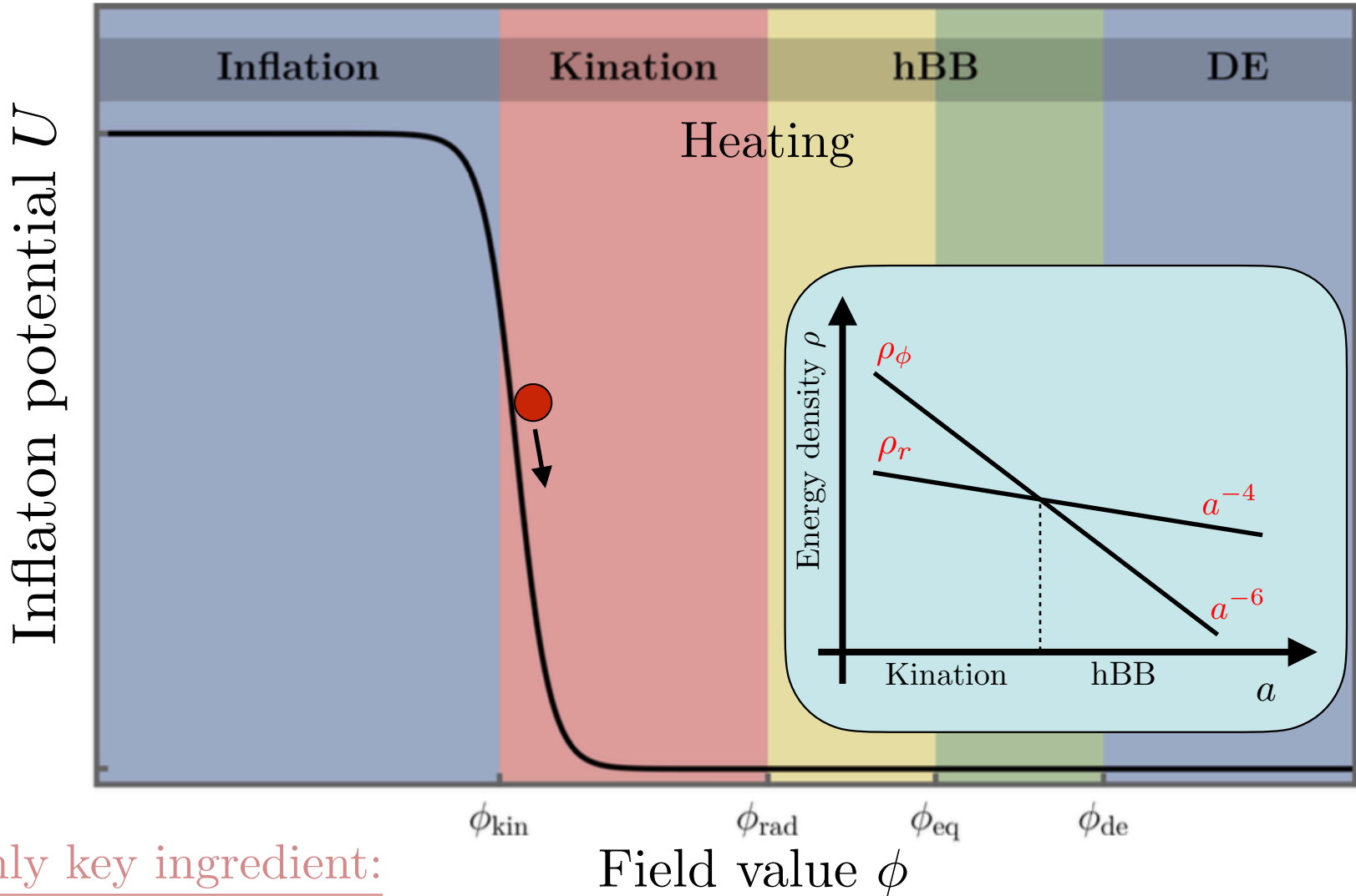
- No isocurvature perturbations even if χ is light
- Highly efficient heating mechanism
- Onset of radiation domination rather independent of $V(\chi)$

Quintessential inflation



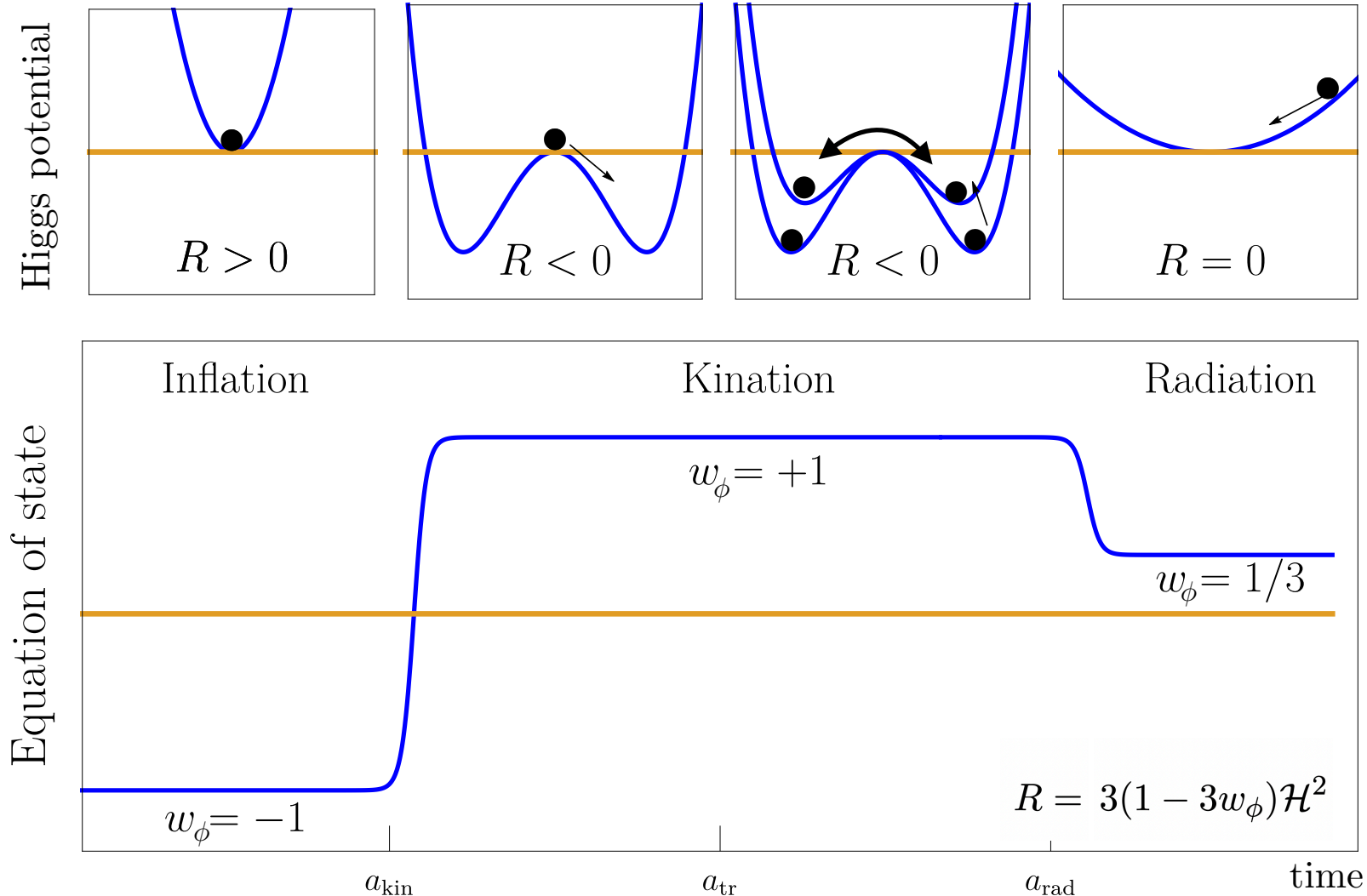
Only key ingredient:
Period of kination

Quintessential inflation



Only key ingredient:
Period of kination

Equation of state as order parameter



Linear dynamics

$$Y \equiv \frac{a}{a_{\text{kin}}} \frac{\chi}{\chi_*}, \quad \vec{y} \equiv a_{\text{kin}} \chi_* \vec{x}, \quad \chi_* \equiv \sqrt{6\xi} H_{\text{kin}}$$
$$z \equiv a_{\text{kin}} \chi_* \tau$$

$$S_\chi = \int d^3\vec{y} dz \left[\frac{1}{2} (Y')^2 - \frac{1}{2} |\nabla Y|^2 + \frac{1}{2} M^2(z) Y^2 - V(Y) \right]$$

Spinodal/Tachyonic instability

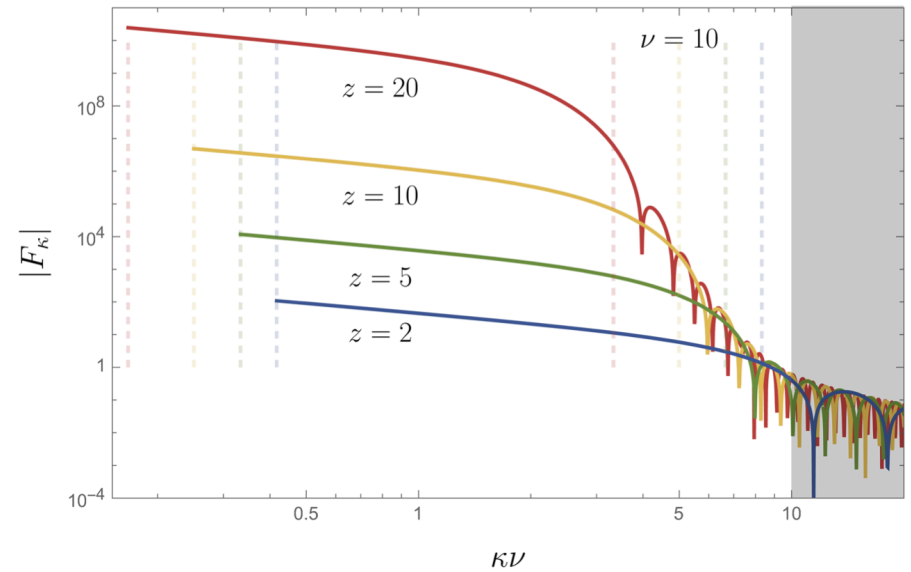
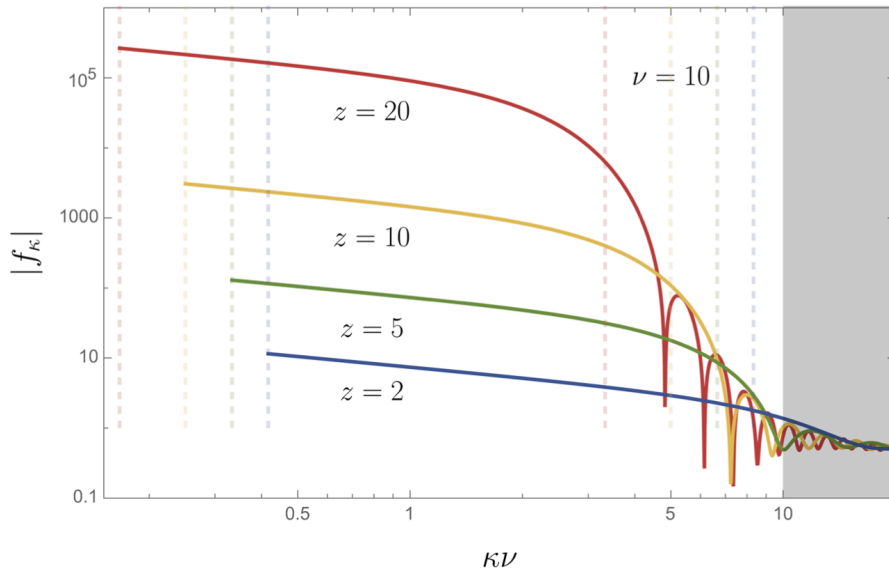
$$M^2(z) \equiv (4\nu^2 - 1) \mathcal{H}^2 \quad \nu \equiv \sqrt{\frac{3\xi}{2}}$$

- The Z_2 symmetry of the action is preserved by the dynamics.
- The field is *not* classical but rather quantum.
- A homogeneous component description is *completely inaccurate*.

Classicalization

$$f''_{\kappa} + (\kappa^2 - M^2(z))f_{\kappa} = 0$$

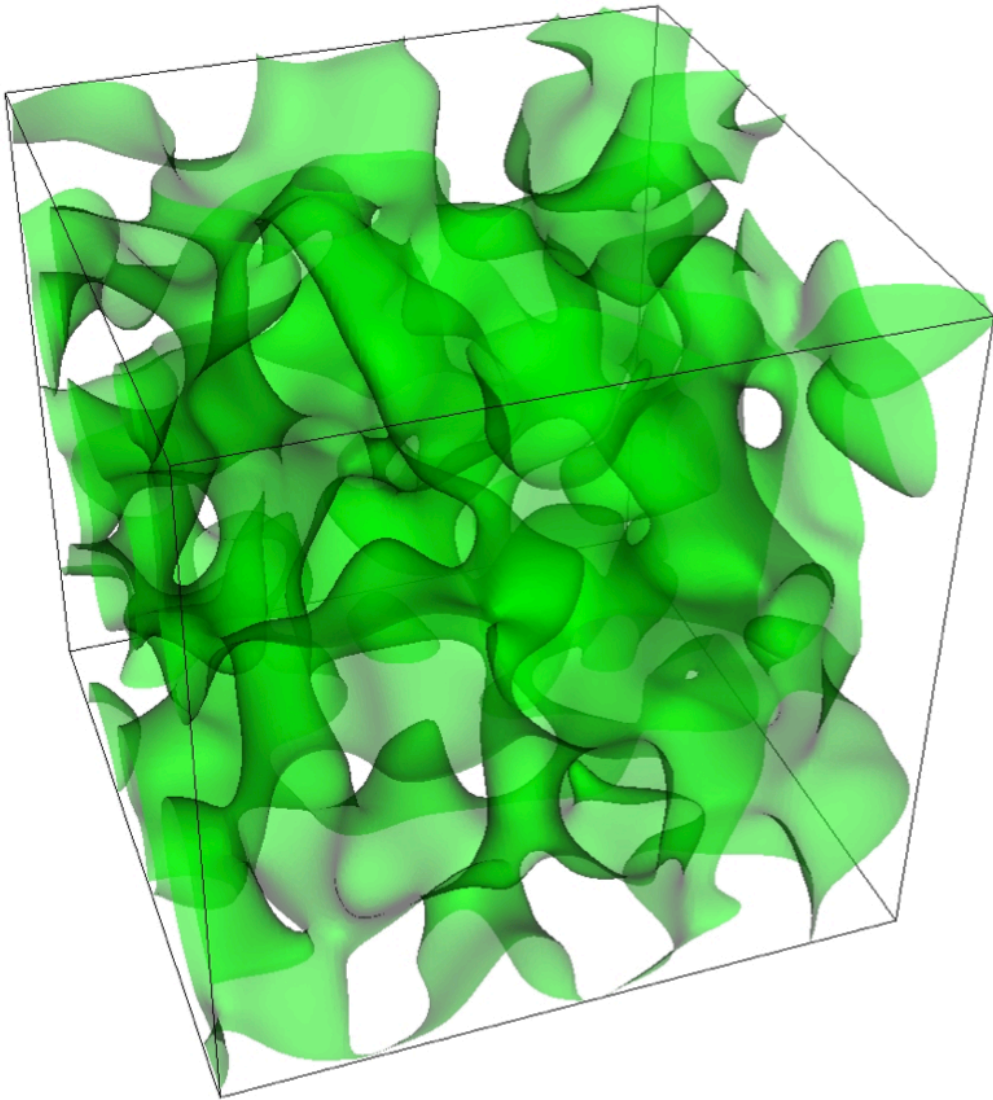
$$F_{\kappa}(z) = \text{Re}(f_{\kappa}^* f'_{\kappa})$$



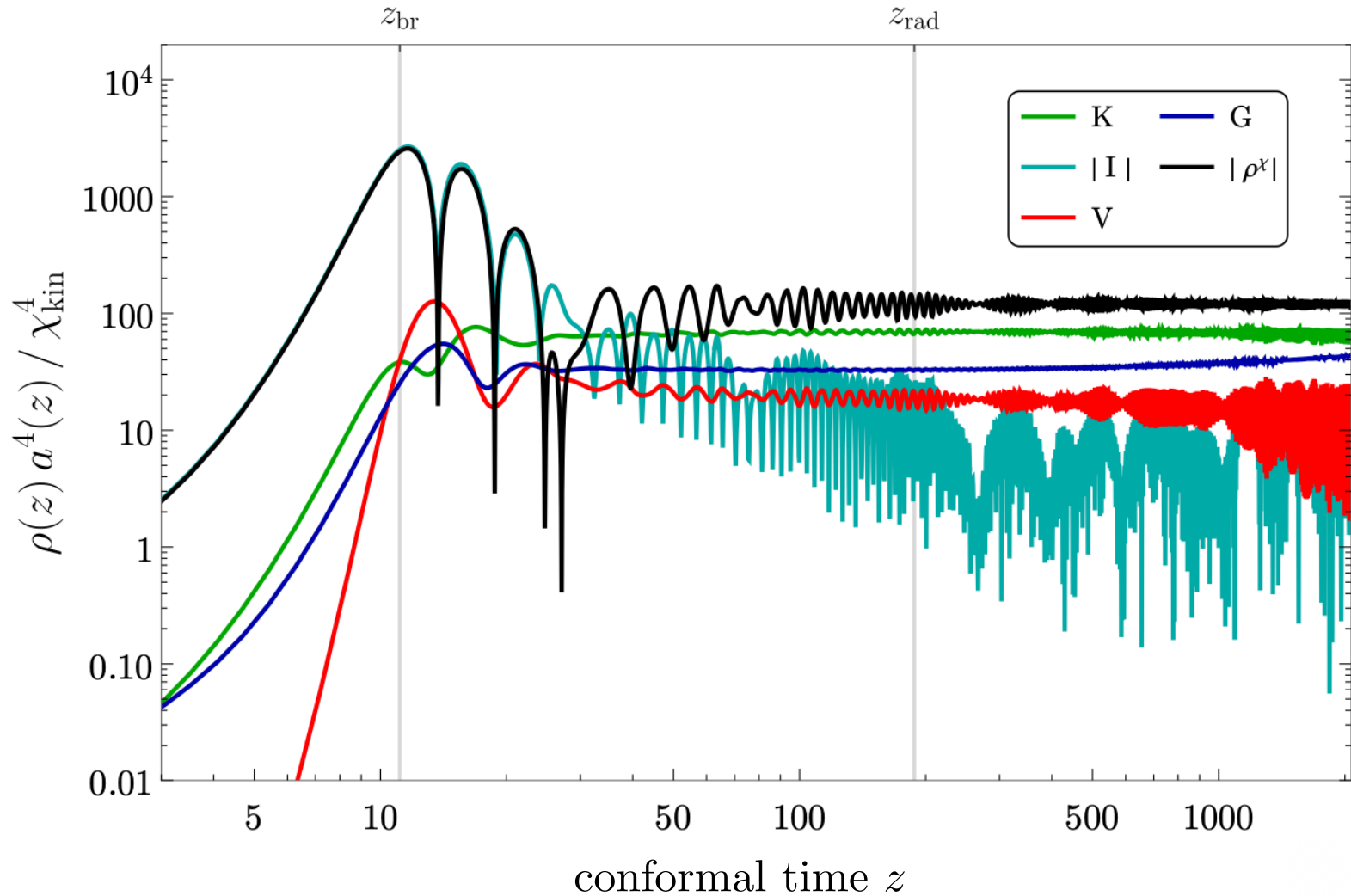
$$\Delta Y_{\kappa}^2 \Delta \Pi_{\kappa}^2 = |F_{\kappa}(z)|^2 + \frac{1}{4} \geq \frac{1}{4} \left| \langle [Y_{\kappa}(z), \Pi_{\kappa}^{\dagger}(z)] \rangle \right|^2$$

- Following dynamics needs non-analytical techniques.
- High occupation numbers \rightarrow Classical Lattice Simulations

Beating Domain Walls



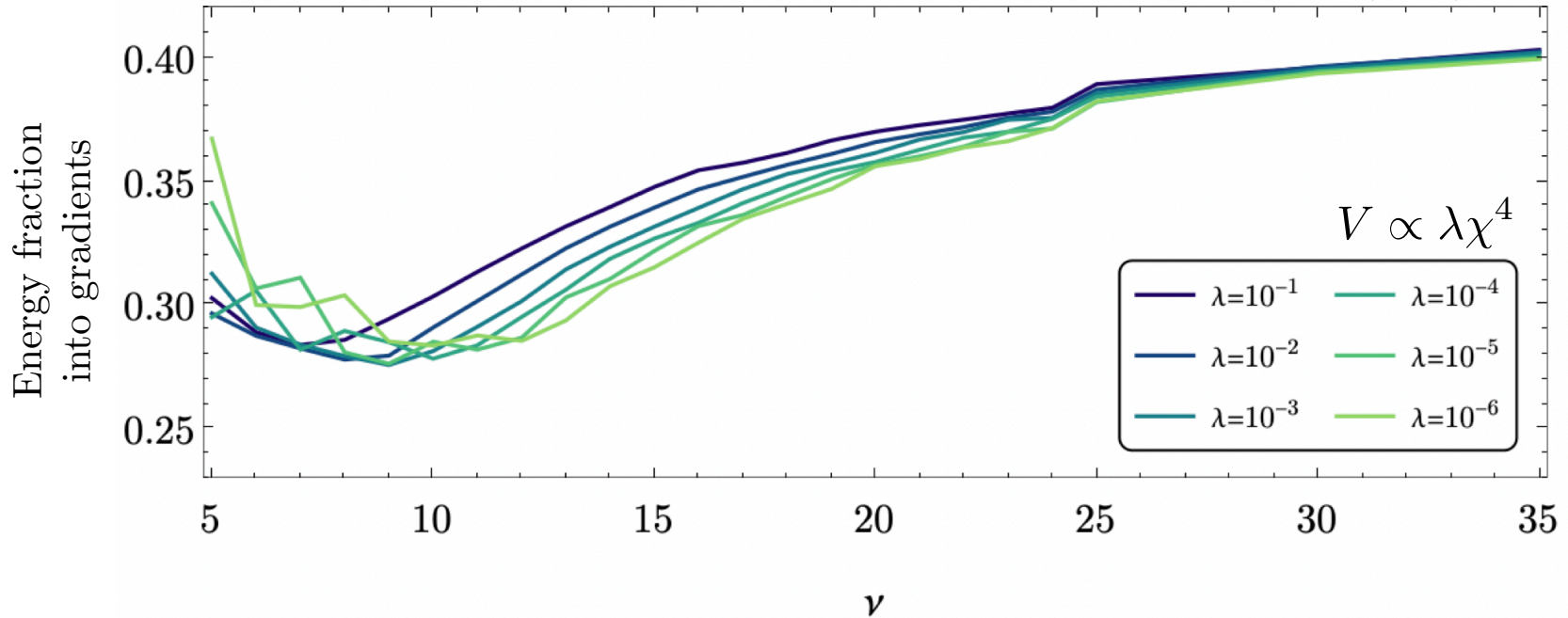
Energy distribution



$$\nu = \sqrt{\frac{3\xi}{2}}$$

Gradients are crucial

G. Laverda, JR, JCAP 03 (2024) 033

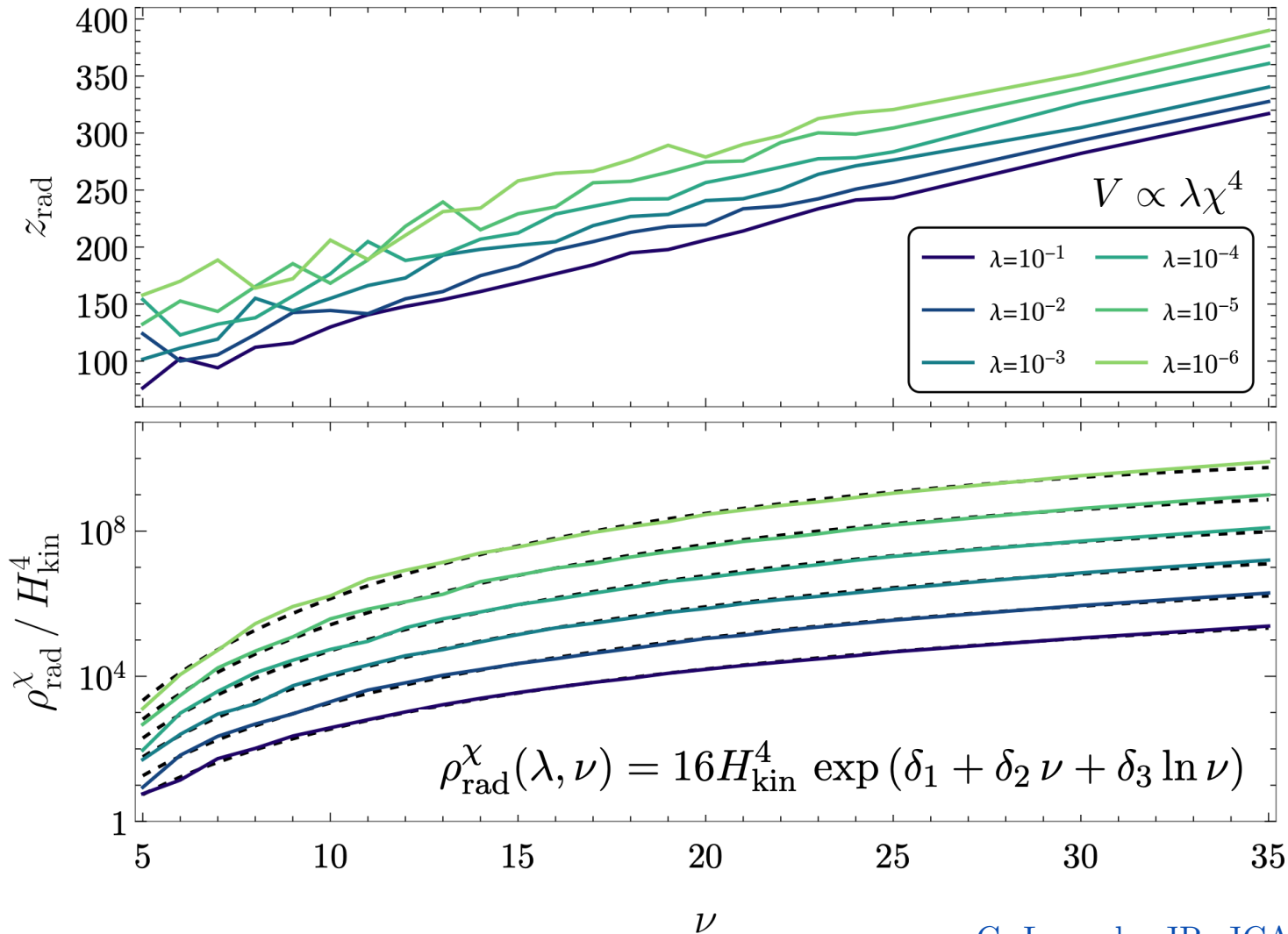


Radiation-like products for arbitrary potential

$$w_\chi = \frac{1}{3} + \frac{2}{3} \frac{(n-2)}{(n+1) + \langle (\nabla \chi/a)^2 \rangle / \langle V \rangle} \quad V \propto \chi^{2n}$$

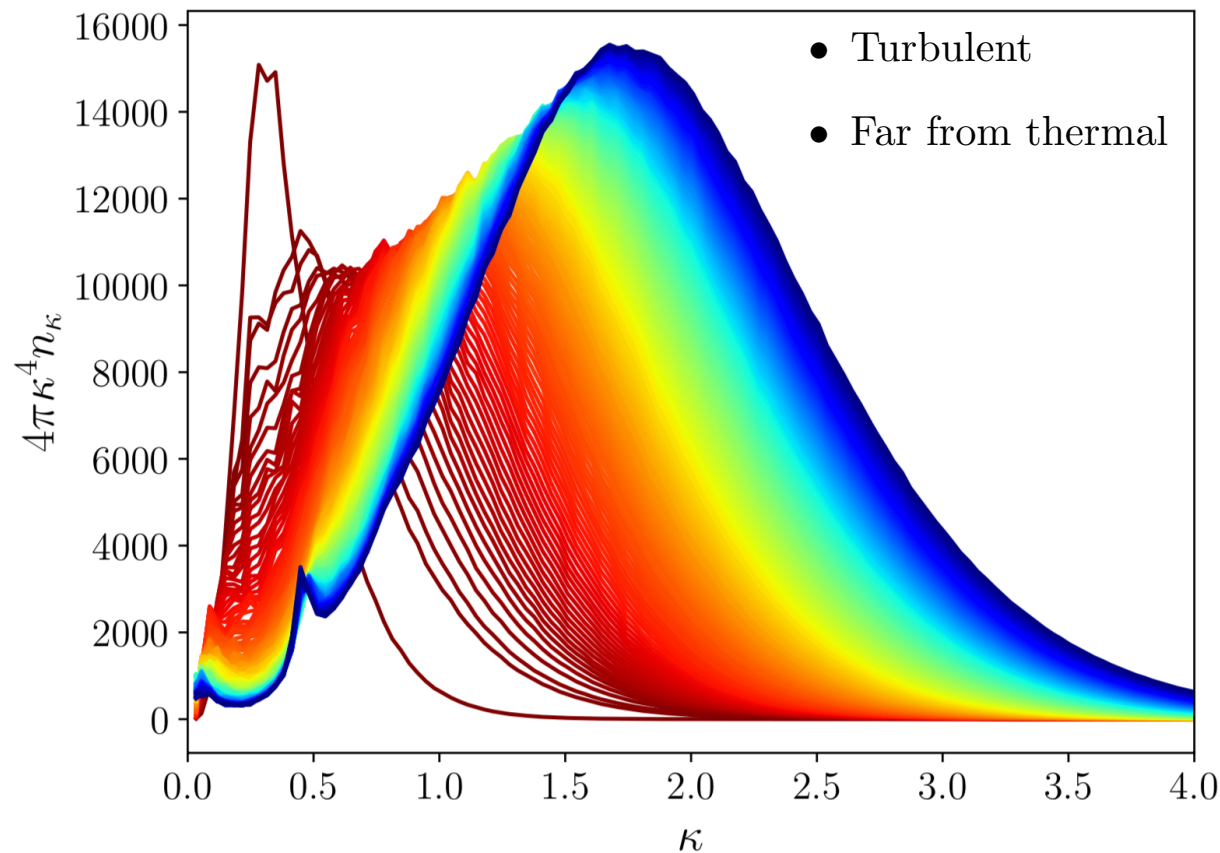
Onset of radiation domination

Lattice-based fitting formulas: $O(100)$ 3+1 classical lattice simulations



Heating “temperature”

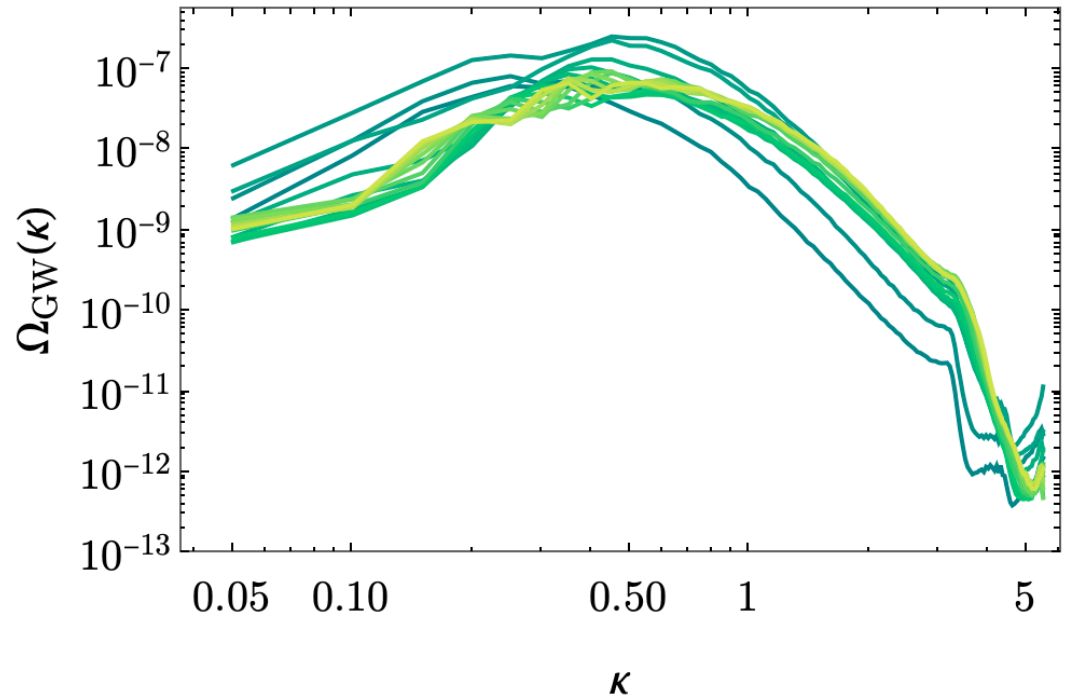
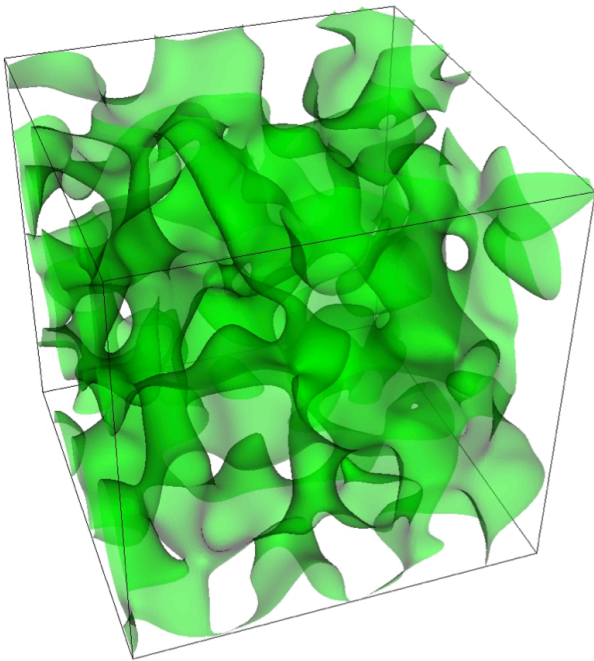
By-product
First lattice characterisation
of Ricci reheating



$$T_{\text{ht}} \simeq 2.7 \times 10^8 \text{ GeV} \left(1 + \frac{z_{\text{rad}}}{\nu}\right)^{-3/4} \left(\frac{\rho_{\text{rad}}^{\chi}/\rho_{\text{rad}}^{\phi}}{10^{-8}}\right)^{3/4} \left(\frac{H_{\text{kin}}}{10^{11} \text{ GeV}}\right)^{1/2}$$

Gravitational waves

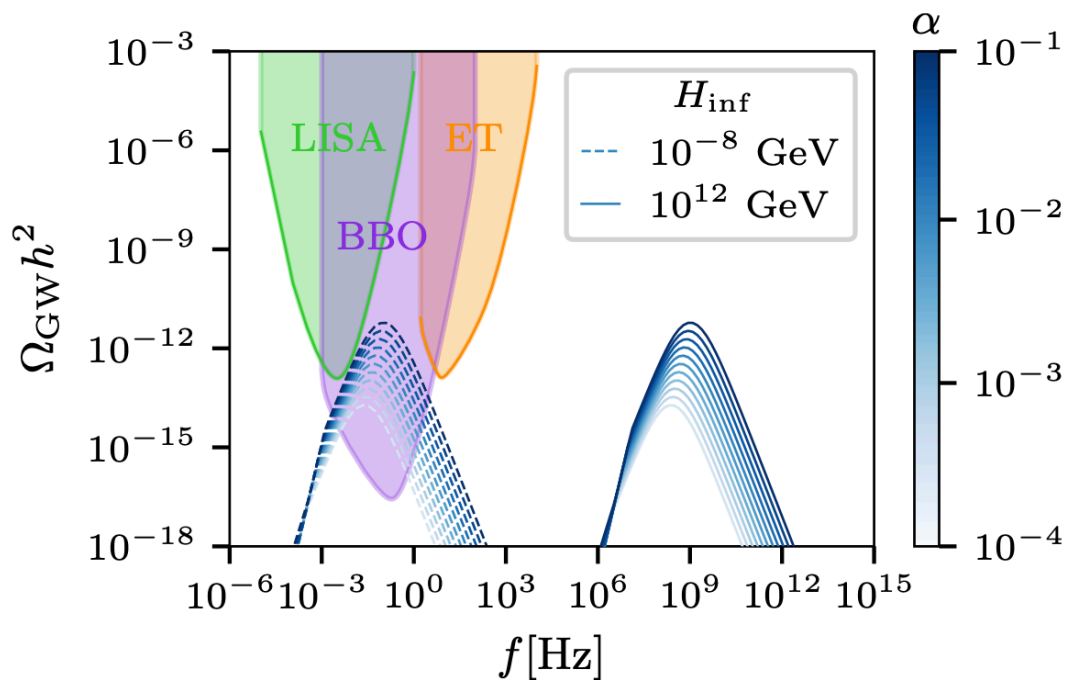
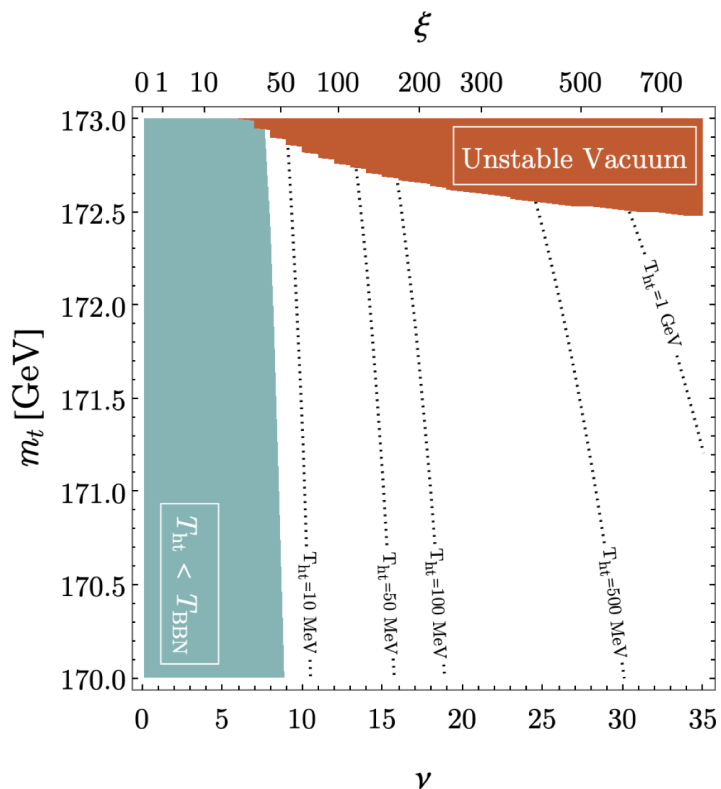
$$(h_{ij}^{TT})'' + 2H(h_{ij}^{TT})' - \frac{\nabla^2 h_{ij}^{TT}}{a^2} \simeq \frac{2a^2}{M_P^2} \Pi_{ij}^{TT}$$



Frequencies typically out of range of current experiments

Further applications & generalizations

- The SM Higgs can be responsible for heating the Universe See G. Laverda's talk on Tuesday
- Coupling to other species can lead to stabilization of defects
- Possible extensions to radiation/matter domination in an EFT framework
- Easily generalizable to other symmetry groups, defects and FOPT



Conclusions

- Non-minimal couplings to gravity may lead to the spontaneous symmetry breaking of internal symmetries.
- These interactions act as a natural cosmic clock, triggering the formation of short-topological defects and potentially detectable gravitational wave backgrounds
- The eventual fragmentation of these objects allows heating the Universe after inflation.
- Easily generalizable to other groups and topological defects.

