# Extending the SM with Vector-Like Quarks: consequences for CKM unitarity and CP violation

# **José Filipe Bastos**

#### CFTP, Instituto Superior Técnico, Lisbon

In collaboration with: Francisco Botella, Gustavo C. Branco, M. N. Rebelo, J. Silva-Marcos, Francisco Albergaria

#### Lisbon, June 6, 2024



Based on: [2111.15401] [2210.14248]



#### **Motivation**

A fourth chiral generation of quarks is ruled out, but the quark sector can be extended with VLQs.

VLQs take part in many models from GUTs, to the Nelson-Barr solutions to the strong CP problem. They have a rich phenomenology that can be used to try to explain several types of anomalies/ tensions. A fourth chiral generation of quarks is ruled out, but the quark sector can be extended with VLQs.

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**Cabibbo Angle Anomaly (CAA):** The independent determinations of  $|V_{us}|$  (semi-leptonic kaon decays), the ratio  $|V_{us}/V_{ud}|$  (kaon and pion leptonic decays) and  $|V_{ud}|$  ( $\beta$  decays) are not in agreement with each other within the framework of the CKM unitary of SM (discrepancy of ~3 $\sigma$ ). These values fit best to the relation

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 - \Delta^2, \quad \Delta \approx 0.04$$

Extensions with VLQs iso-singlets are natural candidates to explain this anomaly because they introduce deviations to CKM unitarity.

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**CP Violation:** The introduction of VLQs leads to larger mass matrices and, in principle, more physical phases which could lead to the enhancement of CP violation in the quark sector.

Introducing a Q = 2/3 VLQ iso-singlet  $T = T_L + T_R$  with mass  $m_T$  leads to:

• 
$$-\mathcal{L}_{Y} = y_{ij}^{u} \overline{Q'_{iL}} \tilde{\Phi} u'_{jR} + y_{i4}^{u} \overline{Q'_{iL}} \tilde{\Phi} T'_{R} + y_{ij}^{d} \overline{Q'_{iL}} \Phi d'_{jR} + M_{i}^{u} \overline{T}'_{L} u'_{iR} + M_{4}^{u} \overline{T}'_{L} T'_{R} + h.c.$$
  
Bare mass terms
$$\mathcal{M}_{u} = \begin{pmatrix} m_{u} \\ M_{u} \end{pmatrix} \}_{1}^{3}$$

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In the mass basis we get **non-unitary mixing** and **tree-level FCNCs**:

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 $vy_{u,d}$ 

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We have for the first row of the mixing:  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 - s_{14}^2 \xrightarrow{\text{CAA}} s_{14} \approx 0.04 \sim \lambda^2$ 

General solution and its parameter space analyzed in **Branco et al. [2103.13409**] for  $m_T > 1$  TeV

At first glance, a "minimal" solution to the CAA could be:  $s_{14} \approx 0.04$   $s_{24}, s_{34} = 0$   $\delta_{14}, \delta_{24} \longrightarrow$  Factored out We study this case in **Botella et al. [2111.15401].** 



$$V_{\text{CKM}} = \begin{pmatrix} c_{12}c_{13}c_{14} & s_{12}c_{13}c_{14} & s_{13}c_{14}e^{-i\delta} \\ -s_{12}c_{23} - e^{i\delta}c_{12}s_{13}s_{23} & c_{12}c_{23} - e^{i\delta}s_{12}s_{13}s_{23} & c_{13}s_{23} \\ s_{12}s_{23} - e^{i\delta}c_{12}s_{13}c_{23} & -c_{12}s_{23} - e^{i\delta}s_{12}s_{13}c_{23} & c_{13}c_{23} \\ -c_{12}c_{13}s_{14} & -s_{12}c_{13}s_{14} & -s_{13}s_{14}e^{-i\delta} \end{pmatrix} \qquad \qquad F_{u} = \begin{pmatrix} c_{14}^{2} & 0 & 0 & -s_{14}c_{14} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ -s_{14}c_{14} & 0 & 0 & s_{14}^{2} \end{pmatrix}$$

• The VLQ decays predominantly to the first generation:  $Br(T \to dW^+) + Br(T \to uZ) + Br(T \to uA) \simeq 1 \implies m_T > 0.685 \text{ TeV}$ Sirunyan et al. (CMS) [1708.02510]

Typically searches assume:  $\operatorname{Br}(T \to bW^+) + \operatorname{Br}(T \to tZ) + \operatorname{Br}(T \to th) \simeq 1 \implies m_T > 1 - 1.3 \text{ TeV}$ 

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or to  $K_L \to \pi^0 \overline{\nu} \nu$  or  $\varepsilon' / \varepsilon$ , since  $\operatorname{Im} (V_{Td} V_{Ts}^*) = 0$ 

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# Phenomenology: Kaon Physics

The kaon system imposes the most stringent constraints.



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# Phenomenology: $s_{14}$ - dominance Fit



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### Weak-Basis Invariants (WBIs) – Standard Model

Weak-basis invariant quantities can relate the parameters in any WB to physical quantities (masses and mixing).

WBIs remain unchanged under weak-basis transformations (WBTs) which leave EW currents flavor-diagonal.

• WBTs in the SM:  $Q'_L \to W_L Q'_L$ ,  $u'_R \to W^u_R u'_R$ ,  $d'_R \to W^d_R d'_R$   $W_L, W^{u,d}_R \longrightarrow$  3x3 unitary matrices

• Hermitian "building blocks": 
$$(h_u)^n = (m_u m_u^{\dagger})^n \to W_L^{\dagger} h_u^n W_L$$
  
 $(h_d)^n = (m_d m_d^{\dagger})^n \to W_L^{\dagger} h_d^n W_L$   
• Moduli of CKM determined by CP-even WBIs:  $\operatorname{tr}(h_u^n h_d^m) = \sum_{\alpha,i=1}^3 m_{u_\alpha}^{2n} m_{d_i}^{2m} |V_{\alpha i}|^2$ 

• CP violating is determined by a single CP-odd WBI:

$$\operatorname{tr}[h_u, h_d]^3 = 6i(m_t^2 - m_c^2)(m_t^2 - m_u^2)(m_c^2 - m_u^2)(m_b^2 - m_s^2)(m_b^2 - m_d^2)(m_s^2 - m_d^2) I_{\mathrm{CP}}$$
$$I_{\mathrm{CP}} = \operatorname{Im}\left(V_{\alpha i}V_{\beta j}V_{\alpha j}^*V_{\beta i}^*\right) = s_{12}s_{13}s_{23}c_{12}c_{13}^2c_{23}\sin\delta$$

• The masses are determined by:

$$\operatorname{tr}(h_q) = m_1^2 + m_2^2 + m_3^2 \qquad \chi(h_q) = m_1^2 m_2^2 + m_1^2 m_3^2 + m_2^2 m_3^2 \qquad \det(h_q) = m_1^2 m_2^2 m_3^2$$

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- Hermitian "building blocks" (all transforming as  $H \to W_L^{\dagger} H W_L$ ):

$$h_d^n = (m_d m_d^{\dagger})^n \qquad h_u^n = (m_u m_u^{\dagger})^n \qquad h_u^{(n)} = m_u (m_u^{\dagger} m_u + M_u^{\dagger} M_u)^{n-1} m_u^{\dagger}$$

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• More CP violating phases imply more independent CP-odd WBI. The WBI of lowest mass dimension is:

$$\operatorname{tr}\left(\left[h_{u},h_{d}\right]h_{u}^{(2)}\right) = 2i\sum_{i=1}^{3}\sum_{\alpha,\beta=1}^{4} m_{d_{i}}^{2}m_{u_{\alpha}}^{4}m_{u_{\beta}}^{2}\operatorname{Im}\left(F_{\alpha\beta}^{u}V_{\alpha i}^{*}V_{\beta i}\right) \sim M^{8}$$

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- The up-type masses are determined by:
  - $\operatorname{tr}(\mathcal{H}_{u}) = m_{u}^{2} + m_{c}^{2} + m_{t}^{2} + m_{T}^{2} \qquad \chi_{1}(\mathcal{H}_{u}) = m_{u}^{2}m_{c}^{2} + m_{u}^{2}m_{t}^{2} + m_{u}^{2}m_{T}^{2} + m_{c}^{2}m_{t}^{2} + m_{c}^{2}m_{T}^{2} + m_{t}^{2}m_{T}^{2} \qquad \mathcal{H}_{u} = \mathcal{M}_{u}^{\dagger}M_{u}$

$$\det \left(\mathcal{H}_{u}\right) = m_{u}^{2}m_{c}^{2}m_{t}^{2}m_{T}^{2} \qquad \qquad \chi_{2}\left(\mathcal{H}_{u}\right) = m_{u}^{2}m_{c}^{2}m_{t}^{2} + m_{u}^{2}m_{c}^{2}m_{T}^{2} + m_{u}^{2}m_{t}^{2}m_{T}^{2} + m_{c}^{2}m_{t}^{2}m_{T}^{2}$$

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# WBIs – Enhancement of CP Violation with VLQs

CP violation should depend on dimensionless quantities such as

$$\mathcal{I}_{\rm SM} = \operatorname{tr} \left[ y_u y_u^{\dagger}, y_d y_d^{\dagger} \right]^3 = \frac{\operatorname{tr} \left[ h_u, h_d \right]^3}{v^{12}} \sim 10^{-25} \qquad \qquad \mathcal{I}_{\rm VLQ} = \frac{\operatorname{tr} \left( \overline{[h_u, h_d] h_u^{(2)}} \right)}{v^6 m_T^2} \qquad \qquad \qquad \mathcal{I}_{\rm VLQ} = \frac{\operatorname{tr} \left( \overline{[h_u, h_d] h_u^{(2)}} \right)}{v^8 m_T^2}$$

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Some CP-odd dimensionless WBIs from VLQ extensions can be significantly larger than the SM one:

| Best-fit (s <sub>14</sub> -do | m.): $\sqrt{\chi^2} \simeq 2.25$      | $m_T = 1477 \text{ GeV}$              |
|-------------------------------|---------------------------------------|---------------------------------------|
| $\theta_{12} = 0.22579,$      | $\theta_{13} = 0.0038275,$            | $\theta_{23} = 0.039524,$             |
| $\theta_{14} = 0.045334,$     | $\theta_{24} = 7.412 \times 10^{-4},$ | $\theta_{34} = 2.346 \times 10^{-4},$ |
| $\delta = 0.382\pi,$          | $\delta_{14} = 1.872\pi,$             | $\delta_{24} = 1.979\pi.$             |

$$\mathcal{I}_{\rm VLQ} = \frac{\operatorname{tr}\left(\left[h_u, h_d\right] h_u^{(2)}\right)}{v^6 m_T^2} \simeq 2.02 \times 10^{-10} \qquad \qquad \mathcal{I}_{\rm VLQ}' = \frac{\operatorname{tr}\left(\left[h_u^2, h_d\right] h_u^{(2)}\right)}{v^8 m_T^2} \simeq 1.16 \times 10^{-10}$$

Important for Baryogenesis??

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| $\delta =$    | $0.382\pi$ ,                 | $\delta_{14} = 1.872\pi,$             | $\delta_{24} = 1.979\pi.$             | Important for Baryogenesis??  |   |
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| $\theta_{12}$ | = 0.22579,                   | $\theta_{13} = 0.0038275,$            | $\theta_{23} = 0.039524,$             | $\mathcal{I}_{\rm VLQ} = \frac{\operatorname{tr}\left(\left[h_u, h_d\right] h_u^{(2)}\right)}{6 - 2} \simeq 2.02 \times 10^{-10}$ | $\mathcal{I}_{\text{VLO}}^{\prime} = \frac{\operatorname{tr}\left(\left[h_{u}^{2}, h_{d}\right] h_{u}^{(2)}\right)}{2} \simeq 1.16 \times 10^{-10}$ |
| Bes           | st-fit (s <sub>14</sub> -doi | m.): $\sqrt{\chi^2} \simeq 2.25$      | $m_T = 1477 \text{ GeV}$              | $\begin{pmatrix} r_1 & r_2 & r_3 \end{pmatrix}$   | $\left( \begin{bmatrix} 1 & 2 & -1 \end{bmatrix} + \begin{bmatrix} 2 \\ 2 \end{bmatrix} \right)$  |

In these extensions we can even obtain CP violation in the limit of extremely high energies (extreme chiral limit) where  $m_u = m_c = m_d = m_s = 0$  and  $\mathcal{I}_{SM} = 0$  (also pointed out in **del Aguila et al. [hep-ph/9703410]**).

$$\operatorname{tr}\left(\left[h_{u},h_{d}\right]h_{u}^{(2)}\right) = 2i \ m_{b}^{2}m_{t}^{2}m_{T}^{2}(m_{T}^{2}-m_{t}^{2})I_{\mathrm{ECL}} \\ I_{\mathrm{ECL}} = c_{23}c_{14}^{2}c_{24}^{2}c_{34}s_{23}s_{24}s_{34}\sin\delta_{\mathrm{ECL}} \\ V_{\mathrm{CKM}} = \begin{pmatrix} c_{14} & 0 & 0 \\ -s_{14}s_{24} & c_{23}c_{24} & s_{23}c_{24} \\ -s_{14}c_{24}s_{34}e^{i\delta_{\mathrm{CL}}} & -s_{23}c_{34} - c_{23}s_{24}s_{34}e^{i\delta_{\mathrm{CL}}} \\ -s_{14}c_{24}c_{34}e^{i\delta_{\mathrm{CL}}} & s_{23}s_{34} - c_{23}s_{24}c_{34}e^{i\delta_{\mathrm{CL}}} & -c_{23}s_{34} - s_{23}s_{24}c_{34}e^{i\delta_{\mathrm{CL}}} \\ -s_{14}c_{24}c_{34}e^{i\delta_{\mathrm{CL}}} & s_{23}s_{34} - c_{23}s_{24}c_{34}e^{i\delta_{\mathrm{CL}}} & -c_{23}s_{34} - s_{23}s_{24}c_{34}e^{i\delta_{\mathrm{CL}}} \\ \end{pmatrix}$$

- Extension with VLQs can provide very simple solutions to the CAA.
- The s<sub>14</sub>-dominance limit is particularly safe in relation to a large variety of pheno. constraints and is related to an unusual decay pattern for the VLQ.

- The assumption of dominant decays of VLQs to the first generation has been largely overlooked but should be more seriously considered.
- The introduction of VLQs to the theory could significantly enhance CP violation in the quark sector and even achieve CP violation at very high energies. This is also a consequence of CKM non-unitarity.

Thank You!

#### CAA

#### B. Belfatto and S. Trifinopoulos [2302.14097]



Best fit: 
$$\delta_{\text{CKM}} \approx 1.7 \times 10^{-3}$$
  
 $\delta_{\text{CKM}} \equiv 1 - |V_{ud}|^2 - |V_{us}|^2 - |V_{ub}|^2$ 

From unitarity:  $|V_{us}|_A = 0.22308(55)$  $|V_{us}|_B = 0.22536(47)$ 

 $|V_{us}|_C = 0.2277(11)$ 

$$\left| V_{us} \right|_{A+B} = 0.22440(51) \\ VS \\ |V_{us}|_{C} = 0.2277(11) \\ |V_{us}|_{A} = 0.22308(55) \\ VS \\ |V_{us}|_{B} = 0.22536(47) \\ |V_{us}|_{A} = 0.22308(55) \\ VS \\ |V_{us}|_{C} = 0.2277(11) \\ \\ \end{array} \right\} CAA1: \sim 2.7\sigma \\ CAA2: \sim 3.1\sigma \\ CAA2: \sim 3.1\sigma \\ |V_{us}|_{C} = 0.2277(11) \\ \left. \begin{array}{c} VS \\ VS \\ VS \\ |V_{us}|_{C} = 0.2277(11) \\ \end{array} \right\} \\ \sim 3.7\sigma \\ \end{array}$$

#### **Neutral Meson Mixings**

$$\Delta m_N^{\rm NP} \simeq \frac{G_F^2 M_W^2 m_N f_N^2 B_N}{6\pi^2} |2\eta_{cT}^N S_{cT} \lambda_c^N \lambda_T^N + 2\eta_{tT}^N S_{tT} \lambda_t^N \lambda_T^N + \eta_{TT}^N S_T (\lambda_T^N)^2| \qquad \lambda_i^{K} = V_{id} V_{is}^* \\ \lambda_i^{B_d} = V_{id} V_{ib}^*$$

$$\left|\epsilon_{K}^{\mathrm{NP}}\right| \simeq \frac{G_{F}^{2} M_{W}^{2} m_{K} f_{K}^{2} B_{K} \kappa_{\epsilon}}{12\sqrt{2}\pi^{2} \Delta m_{K}} \left|\mathrm{Im}\left[2\eta_{cT}^{K} S_{cT} \lambda_{c}^{K} \lambda_{T}^{K} + 2\eta_{tT}^{K} S_{tT} \lambda_{t}^{K} \lambda_{T}^{K} + \eta_{TT}^{K} S_{T} (\lambda_{T}^{K})^{2}\right]\right| = \frac{G_{F}^{2} M_{W}^{2} m_{K} f_{K}^{2} B_{K} \kappa_{\epsilon}}{12\sqrt{2}\pi^{2} \Delta m_{K}} \mathcal{F} \qquad \lambda_{i}^{B_{s}} = V_{is} V_{ib}^{*}$$



• 
$$s_{14} \sim \lambda^2$$
,  $s_{24} = 0$ :  $\mathcal{F} \approx 2\eta_{tT}^K S_{tT} s_{12} s_{14}^2 s_{13} s_{23} \sin \delta$ 

• 
$$s_{14} \sim \lambda^2$$
,  $s_{24} \sim \lambda^4$ :  
 $\mathcal{F} \approx 2s_{12}s_{14}^2 \left(\eta_{tT}^K S_{tT} s_{13} s_{23} \sin \delta - \eta_{TT}^K S_{TT} s_{14} s_{24} \sin \delta'\right)$ 

 $\delta' = \delta_{24} - \delta_{14}$ 

#### Kaon Decays

$$\frac{\operatorname{Br}(K^+ \to \pi^+ \overline{\nu} \nu)}{\operatorname{Br}(K^+ \to \pi^+ \overline{\nu} \nu)_{\mathrm{SM}}} = \left| \frac{\lambda_c^K X^{\mathrm{NNL}}(x_c) + \lambda_t^K X(x_t) + \lambda_T^K X(x_T) + A_{ds}}{\lambda_c^K X^{\mathrm{NNL}}(x_c) + \lambda_t^K X(x_t)} \right|^2$$

$$A_{ds} = \sum_{i,j=c,t,T} V_{is}^* (F^u - I)_{ij} V_{jd} N(x_i, x_j) \simeq -\frac{x_T}{8} c_{14}^2 c_{24}^2 \lambda_T^K$$

$$N(x_i, x_j) = \frac{x_i x_j}{8} \left( \frac{\log x_i - \log x_j}{x_i - x_j} \right)$$
$$N(x_i, x_i) \equiv \lim_{x_j \to x_i} N(x_i, x_j) = \frac{x_i}{8}$$

• 
$$\left(\frac{\epsilon'}{\epsilon}\right)^{\mathrm{NP}} \simeq \tilde{F}(x_i) \mathrm{Im}(\lambda_T^K) \simeq -\tilde{F}(x_i) c_{12}^2 s_{14} s_{24} \sin \delta'$$

$$\tilde{F}(x_T) \equiv F(x_T) - \frac{x_T}{8} \left( P_X + P_Y + P_Z \right)$$

 $F(x_i) = P_0 + P_X X(x_i) + P_Y Y(x_i) + P_Z Z(x_i) + P_E E(x_i)$