DARK ECHOES: FROM COLLIDER TO GRAVITATIONAL WAVES OBSERVABLES

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theoria poiesis praxis



However, it fails to...

- Explain neutrino masses
- **Explain dark matter**
- **Explain CP violation and matter/anti-matter assymetry**
- Explain the observed flavour structure Flavour puzzles
- Suffers from the Higgs mass hierarchy problem

The SM is a tremendously successful theory that explains "boringly" well most its predictions!



LHC and future colliders Stochastic gravitational (SGWB)

Current and future experimental facilities will offer new channels to search for New Physics Phenomena



✓ Superposition of unresolved astrophysical sources

- Cosmological origin
 - Inflation
 - Topological defects
 - Phase transitions

SGWB

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SGWB

A SGWB detection can represent the first direct measurement of the Universe prior to the BBN era, a breakthrough comparable to the discovery of the CMB



NANOGRAV 15-YEAR NEW-PHYSICS SIGNALS [2306.16213]



A SGWB detection can represent the first direct measurement of the Universe prior to the BBN era, a breakthrough comparable to the discovery of the CMB

First order phase transition (FOPT) (Illustration)

Strength α Inverse duration β/H Percolation temperature

 T_*

Credit: Marco Finetti

Effect of the thermodynamic parameters on the SGWB

Case study: A non-abelian SU(2)_D vector dark matter model

[OUT SOON] BELYAEV, BERTENSTAM, GONÇALVES, APM, PASECHNIK, THONGYOI

[Fermionic portal to vector dark matter from a new gauge sector: Belyaev, Dandrea, Moretti, Panizzi, Ross, Thongyuoi, PRD 108 (2023) no. 9 095001, 2204.03510] [A fermion portal to a non-abelian dark sector: Belyaev, Dandrea, Moretti, Panizzi, Ross, Thongyuoi, Front.in.Phys. 12 (2024) 1339886, 2203.04681]

$$\begin{split} \mathcal{L}_{0} &= -\frac{1}{4} (V_{\mu\nu}^{a})^{2} + |D\mu\Phi_{D}|^{2} - \mu_{D}^{2} \Phi_{D}^{\dagger} \Phi_{D} - \lambda_{D} (\Phi_{D}^{\dagger} \Phi_{D})^{2} & \text{Secluded sector} \\ \mathcal{L}_{I} &= \mathcal{L}_{0} - \frac{1}{4} (V_{\mu\nu}^{i})^{2}|_{B,W^{i},G^{i}} + \bar{f}^{\mathrm{SM}} i D f^{\mathrm{SM}} + |D_{\mu}\Phi_{H}|^{2} - \mu_{H}^{2} (\Phi_{H}^{\dagger} \Phi_{H})^{2} \\ &- \lambda_{H} (\Phi_{H}^{\dagger} \Phi_{H})^{2} - (y \bar{f}_{L}^{\mathrm{SM}} \Phi_{H} f^{\mathrm{SM}}_{R} + \mathrm{H.c.}) . & \text{Visible sector} \\ \mathcal{L}_{II} &= \mathcal{L}_{0} + \mathcal{L}_{I} - \lambda_{HD} (\Phi_{H}^{\dagger} \Phi_{H}) (\Phi_{D}^{\dagger} \Phi_{D}) - (y' \bar{\Psi}_{L} \Phi_{D} f^{\mathrm{SM}}_{R} + \mathrm{H.c.}) - m_{f_{D}} \bar{\Psi} \Psi & \text{Fermion and Higg} \\ & \text{Vector -like Fermion Mediator} & \text{Dark Matter} \\ &\Psi = \begin{pmatrix} f_{D} \\ \psi \end{pmatrix} & \text{Vector -like Fermion Mediator} & Dark Matter \\ &\Psi = \begin{pmatrix} f_{D} \\ \psi \end{pmatrix} & \text{Order Matter} \\ &\Phi_{H} = \begin{pmatrix} H^{+} \\ H^{0} \\ H^{0}_{D} \end{pmatrix} \rightarrow \langle \Phi_{H} \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_{D} \end{pmatrix} & (\text{breaking } SU(2)_{L} \times U(1)_{Y} \rightarrow U(1)_{Q}) , \\ &\Phi_{D} = \begin{pmatrix} H^{D} \\ H^{0}_{D} \end{pmatrix} \rightarrow \langle \Phi_{D} \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_{D} \end{pmatrix} & (\text{breaking } SU(2)_{D} \times U(1)_{Y_{D}} \rightarrow U(1)_{Q_{D}}) \\ & m_{V^{\pm}} = g_{D} \frac{v_{D}}{2} \end{split}$$

$$\mathcal{L}_{0} = -\frac{1}{4} (V_{\mu\nu}^{a})^{2} + |D\mu\Phi_{D}|^{2} - \mu_{D}^{2}\Phi_{D}^{\dagger}\Phi_{D} - \lambda_{D}(\Phi_{D}^{\dagger}\Phi_{D})^{2}$$
Secluded sector
$$\mathcal{L}_{1} = \mathcal{L}_{0} - \frac{1}{4} (V_{\mu\nu}^{i})^{2}|_{B,W^{i},G^{i}} + \bar{f}^{SM}iDf^{SM} + |D_{\mu}\Phi_{H}|^{2} - \mu_{H}^{2}(\Phi_{H}^{\dagger}\Phi_{H})^{2}$$

$$- \lambda_{H}(\Phi_{H}^{\dagger}\Phi_{H})^{2} - (y\bar{f}_{L}^{SM}\Phi_{H}f^{SM}_{R} + H.c.) .$$

$$\mathcal{L}_{II} = \mathcal{L}_{0} + \mathcal{L}_{I} - \lambda_{HD}(\Phi_{H}^{\dagger}\Phi_{H})(\Phi_{D}^{\dagger}\Phi_{D}) - (y'\bar{\Psi}_{L}\Phi_{D}f^{SM}_{R} + H.c.) - m_{f_{D}}\bar{\Psi}\Psi$$
Fermion and Higg portals
$$\text{Vector -like Fermion Mediator}$$

$$\Psi = \begin{pmatrix} f_{D} \\ \psi \end{pmatrix}$$

$$\Phi_{H} = \begin{pmatrix} H^{+} \\ H^{0} \\ H^{D} \end{pmatrix} \rightarrow \langle \Phi_{H} \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_{D} \end{pmatrix}$$

$$(\text{breaking } SU(2)_{L} \times U(1)_{Y} \rightarrow U(1)_{Q}) ,$$

$$m_{V^{\pm}} = g_{D} \frac{v_{D}}{2}$$

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$$\mathcal{L}_{II} = \mathcal{L}_{0} + \mathcal{L}_{I} - \lambda_{HD}(\Phi_{H}^{\dagger}\Phi_{H})(\Phi_{D}^{\dagger}\Phi_{D}) - (y'\bar{\Psi}_{L}\Phi_{D}f^{SM}_{R} + H.c.) - m_{f_{D}}\bar{\Psi}\Psi$$
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$$(\text{breaking } SU(2)_{L} \times U(1)_{Y} \rightarrow U(1)_{Q}) ,$$

$$m_{V^{\pm}} = g_{D} \frac{v_{D}}{2}$$

$$- \mu_D^2 \Phi_D^{\dagger} \Phi_D - \lambda_D (\Phi_D^{\dagger} \Phi_D)^2 \qquad \text{Secluded sector}$$

$$\stackrel{\text{SM}}{\overset{\text{SM}}{}} i \not D f^{\text{SM}} + |D_\mu \Phi_H|^2 - \mu_H^2 (\Phi_H^{\dagger} \Phi_H)^2 \qquad \text{Visible sector}$$

$$\stackrel{\text{SM}}{\overset{\text{D}}{}} f_R^{\text{SM}} + \text{H.c.}). \qquad \text{Visible sector}$$

$$\stackrel{\text{D}}{\overset{\text{D}}{}} \Phi_D) - (y' \bar{\Psi}_L \Phi_D f_R^{\text{SM}} + \text{H.c.}) - m_{f_D} \bar{\Psi} \Psi \qquad \text{Fermion and Higg}$$

$$\stackrel{\text{portals}}{\overset{\text{portals}}{}} \text{Dark Matter}$$

$$\stackrel{\Psi}{\overset{\text{P}}{}} = \begin{pmatrix} f_D \\ \psi \end{pmatrix} \qquad \text{Dark Matter}$$

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$$\stackrel{\Psi}{\overset{\text{D}}{}} = \begin{pmatrix} V_\mu^+ \\ V_\mu^0 \\ V_\mu^- \end{pmatrix}$$

$$\stackrel{\text{D}}{\overset{\text{D}}{}} \text{(breaking } SU(2)_L \times U(1)_Y \to U(1)_Q), \qquad m_V \pm = g_D \frac{v_D}{2}$$

$$\Phi_{H} = \begin{pmatrix} H^{+} \\ H^{0} \end{pmatrix} \longrightarrow \langle \Phi_{H} \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}$$
$$\Phi_{D} = \begin{pmatrix} H_{D}^{+} \\ H_{D}^{0} \end{pmatrix} \longrightarrow \langle \Phi_{D} \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_{D} \end{pmatrix}$$

Scenario I: Completely decoupled dark sector

$$\mathcal{L}_0 = -\frac{1}{4} (V_{\mu\nu}^a)^2 + |D\mu\Phi_D|^2 - \mu_D^2 \Phi_D^{\dagger} \Phi_D + |D\mu\Phi_D|^2 + |D\mu$$

$$\mathcal{L}_{\rm I} = \mathcal{L}_0 - \frac{1}{4} (V_{\mu\nu}^i)^2 |_{B,W^i,G^i} + \bar{f}^{\rm SM} i D f^{\rm SM} + |_{A_i} - \lambda_H (\Phi_H^{\dagger} \Phi_H)^2 - (y \bar{f}_L^{\rm SM} \Phi_H f_R^{\rm SM} + {\rm H.c.})$$

 $-\lambda_D (\Phi_D^{\dagger} \Phi_D)^2$

Secluded sector

 $|D_{\mu}\Phi_{H}|^{2} - \mu_{H}^{2}(\Phi_{H}^{\dagger}\Phi_{H})^{2}$

Visible sector

 $\alpha \approx \pi/2$ φ_H

Scenario I: Completely decoupled dark sector

$$\mathcal{L}_0 = -\frac{1}{4} (V_{\mu\nu}^a)^2 + |D\mu\Phi_D|^2 - \mu_D^2 \Phi_D^{\dagger} \Phi_D + |D\mu\Phi_D|^2 + |D\mu\Phi_D|$$

$$\mathcal{L}_{\rm I} = \mathcal{L}_0 - \frac{1}{4} (V_{\mu\nu}^i)^2 |_{B,W^i,G^i} + \bar{f}^{\rm SM} i \not D f^{\rm SM} + |D_{\mu} \Phi_H|^2 - \mu_H^2 (\Phi_H^{\dagger} \Phi_H)^2 - \lambda_H (\Phi_H^{\dagger} \Phi_H)^2 - (y \bar{f}_L^{\rm SM} \Phi_H f_R^{\rm SM} + \text{H.c.}).$$

$$\lambda_D (\Phi_D^\dagger \Phi_D)^2$$

Secluded sector

Visible sector

1-field direction approximation can be used only in case of large $(\sim 0, v_D)$ hierarchies φ_D $v \ll v_D$ $\alpha \approx \pi/2$ φ_H

Parameter space scans for $\lambda_{HD} = y' = 0$

Observable SGWB for:

 $g_D \approx 1.8$ $\alpha \approx 10^{-2}$ $\beta/H \lesssim 10^3$ $M_{H_D} \sim \mathcal{O}(10 \text{ GeV})$

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Parameter space scans for $\lambda_{HD} = y' = 0$

Dark sector FOPT are stronger for larger

LISA, BBO and DECIGO peak integrated sensitivity curves

Scenario II: Include fermion and Higgs portals

$\mathcal{L}_{\mathrm{II}} = \mathcal{L}_0 + \mathcal{L}_{\mathrm{I}} - \lambda_{HD} (\Phi_H^{\dagger} \Phi_H) (\Phi_D^{\dagger} \Phi_D) - (y' \bar{\Psi})$

M_{V_D} (GeV)	$\mid M_{H_D} \text{ (GeV)}$	$ g_D$	$\mid m_{f_D} \; (\text{GeV})$	$ m_F (\text{GeV})$	$ \sin \theta_S $	
[10, 10 000]	$\left[10^{-3}, 10\ 000\right]$	$\left[10^{-8}, 4\pi\right]$	[1500, 5000]	$[1500, 10\ 000]$	[-0.2, 0.2]	$\begin{vmatrix} \lambda_H, \ \lambda_D, \ \lambda_{HD} \\ v_D = 2M_{V_D}/g_D \\ \mu_H^2, \ \mu_D^2 \\ y_t, \ y' \end{vmatrix}$

$$\bar{\Psi}_L \Phi_D f_R^{
m SM} + {
m H.c.}) - m_{f_D} \bar{\Psi} \Psi$$
 Fermion and Higgs portals

Scenario II: Include fermion and Higgs portals

Explanation of DM and observability of SGWB (LISA and/or future facilities)

Sensitivity of colliders to the scalar potential

LHC data will further constrain the available parameter space with possible impact on SGWB predictions

Take home message 1. SGWB from dark SU(2) gauge theory are explored.

- sector and their impact on FOPT.
 - DM and provide observable SGWB.
 - observable SGWB even in the absence of portals.

2. We have studied both Higgs and VL fermion portals for the dark SU(2)

(i) Dark SU(2) with fermion and Higgs portal can successfully explain

(ii) There is an interplay between the dark and visible sectors with

3. Combination with collider observables for complementary tests on the scalar sector (trilinear Higgs coupling, new scalars, mixing angles).

Strength and duration of the PT

$$\alpha = \frac{1}{\rho_{\gamma}} \left(\Delta V - \frac{T}{4} \frac{\partial \Delta V}{\partial T} \right) \bigg|_{T = T_{*}} \qquad \frac{\beta}{H} = T_{*} \frac{\partial}{\partial T} \left(\frac{\hat{S}_{3}}{T} \right) \bigg|_{T = T_{*}}$$

$$\hat{S}_3(\hat{\phi}, T) = 4\pi \int_0^\infty \mathrm{d}r \, r^2 \left\{ \frac{1}{2} \left(\frac{\mathrm{d}\hat{\phi}}{\mathrm{d}r} \right)^2 + V_{\mathrm{eff}}(\hat{\phi}, H(T)) = \frac{1}{3\overline{M}_P} \left(\rho_\gamma + \Delta V(T) \right) , \ \rho_\gamma = g^*(T) \frac{\pi^2}{30} T_{\mathrm{eff}}(T) \right\}$$

 $|_{T_*}$

Dimensional reduction

Theoretical predictions are not robust as they strongly depend on the transition temperature

• Why large uncertainties?

$$\begin{split} m_{\rm eff}^2 &= (m^2 + a_{1-\rm loop} T^2) \ll m^2 & \mbox{Large theorem} \\ b_{2-\rm loop} T^2 &\approx m_{\rm eff}^2 & \mbox{transitions} \\ \mu \frac{d}{d\log\mu} m_{\rm eff}^2 &\approx m_{\rm eff}^2 & \mbox{Large scale} \\ \log\left(T^2/m_{\rm eff}^2\right) \gg 1 & \mbox{Large logs} \end{split}$$

 $h^2 \Omega_{\rm GW} \propto \frac{(\Delta V)^2}{T_{\rm W}^8}$

oretical e phase on

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[Image credit: P. Schicho]

Huge higher order corrections

• In thermal equilibrium heavy "particles" show $\partial_{\mu}\phi(x)\partial^{\mu}\phi(x) \rightarrow \overrightarrow{\nabla}\phi(\overrightarrow{x}) \cdot \overrightarrow{\nabla}\phi(x)$

No time dependence

Use an effective field theory

[Kajantie et al 9508379, Gould et al 2104.04399]

$$\log (T^2/m_{\text{eff}}^2) \rightarrow \log (T^2/\mu^2) + \log (\mu^2/m_{\text{eff}}^2)$$
Match at $\mu \sim T$
RG-evolution
in the EFT

• In thermal equilibrium heavy "particles" show up as an infinite tower of Matsubara (static) modes:

$$(\vec{x}) + \sum_{n=-\infty}^{+\infty} (2\pi nT)^2 \phi(\vec{x})^2$$

Integrate out heavy particles

$$\frac{1}{2}m^2\phi^2 + \frac{1}{4}\lambda\phi^4 \rightarrow \frac{1}{2}m_{3d}^2(T, m, \lambda)\phi^2 + \frac{1}{4}\lambda_{3d}(T, m, \lambda)\phi^$$

In practice: write down the most general 3d-spacial Lagrangian and match the couplings

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Procedure automatised in DRAlgo

[A. Ekstedt et al, Comput. Phys. Commun 288 (2023) 108725, 2205.08815]

$$V_{4d} = TV_{3d}$$

[Image credit: P. Schicho]

 $V_{\rm LO}^{3D}(T) = \frac{1}{2} [\mu_D^{\mathcal{US}}]^2 \varphi_D^2 + \frac{1}{2} [\mu_H^{\mathcal{US}}]^2 \varphi_H^2 + \frac{1}{4} \lambda_D^{\mathcal{US}} \varphi_D^4 + \frac{1}{4} \lambda_H^{\mathcal{US}} \varphi_H^4,$ $V_{\rm NLO}^{3D}(T) = -\frac{1}{12} \sum_{i \in \text{scl.}} M_i^3(\varphi_H, \varphi_D, T) - \frac{2}{12} \sum_{i \in \text{vec.}} M_i^3(\varphi_H, \varphi_D, T)$

 $V_{\text{eff.}}^{4D} = T \left[(V_{\text{LO}}^{3D}(T) + V_{\text{NLO}}^{3D}(T)) \right]$

$\varphi_H(T) = \phi(T) \cos \alpha(T)$ $\varphi_D(T) = \phi(T) \sin \alpha(T)$

$$\sum_{i \in \text{scl.}} [2 \varphi_D^2 + \frac{1}{2} [\mu_H^{\mathcal{US}}]^2 \varphi_H^2 + \frac{1}{4} \lambda_D^{\mathcal{US}} \varphi_D^4 + \frac{1}{4} \lambda_H^{\mathcal{US}} \varphi_H^4 ,$$

$$\sum_{i \in \text{scl.}} M_i^3 (\varphi_H, \varphi_D, T) - \frac{2}{12} \sum_{i \in \text{vec.}} M_i^3 (\varphi_H, \varphi_D, T)$$

 $\checkmark V_{\varphi}(\alpha, T) = d(\alpha, T)\varphi^2 + e(\alpha, T)\varphi^3 + \lambda(\alpha, T)\varphi^4$

FOPT if $e(\alpha, T) < 0$

$$\begin{aligned} \varphi_{D} & \qquad v \sim v_{D} \\ \varphi & \qquad & V_{D} \\ \varphi &$$

$$e(\alpha, T) = -\frac{T^{5/2}}{48} \left\{ 3[g_D^{\mathcal{US}}]^3 \sin^3(\alpha) + \left[2[g_W^{\mathcal{US}}]^3 + \left([g_W^{\mathcal{US}}]^2 + [g_Y^{\mathcal{US}}]^2 \right)^{3/2} \right] \cos^3(\alpha) \right\}$$

Used dimensional reduction

Fopt if
$$e(\alpha,T) < 0$$

Potential barrier between true and false vacua induced by the secluded sector

$\alpha, \beta/H, T_* \longrightarrow$

$$h^2 \Omega_{\rm GW} = h^2 \Omega_{\rm GW}^{\rm peak} \begin{pmatrix} 4 \\ 7 \end{pmatrix}$$

Peak amplitude

 $h^2 \Omega_{\rm GW}^{\rm peak} = 3 \times 10^{-12}$

$$f_{\text{peak}} = 26 \times 10^{-6} \left(\frac{1}{HR}\right) \left(\frac{T_*}{100}\right) \left(\frac{g_*}{100 \text{ GeV}}\right)^{\frac{1}{6}} \text{Hz}$$

We use the templates for SW peak in [Caprini et al. JCAP 03 (2020) 024]

calculated from a certain BSM theory, used as inputs to obtain the GW power spectrum

$$-\frac{7}{2} \left(\frac{f}{f_{\text{peak}}}\right)^3 \left[1 + \frac{3}{4} \left(\frac{f}{f_{\text{peak}}}\right)\right]^{-\frac{7}{2}}$$
Spectral function
$$\left(\frac{100}{g_*}\right)^{\frac{5}{6}} \left(\frac{T_*}{100c_s}\right) f_{\text{peak}}^{-1} K^2$$

$$HR = \frac{H}{\beta} (8\pi)^{\frac{1}{3}} \max (v_b, c_s) \qquad K = \frac{\kappa\alpha}{1+\alpha}$$

Di-Higgs production

Phys.Lett.B 732 (2014) 142-149

Thermal effective potential

$$V_{\text{eff}}(T) = V_0 + V_{\text{CW}}^{(1)} + \Delta V(T) + V_{\text{ct}}$$

$$n_s = 6, \quad n_{A_L} = 1$$

$$n_W = 6, \quad n_Z = 3, \quad n_\gamma = 2$$

$$n_{u,d,c,s,t,b} = 12, \quad n_{e,\mu,\tau} = 4, \quad n_{\nu_{1,2,3}} = n_{N_{1,2}^{\pm}}$$

$$\frac{(\phi_{\alpha})}{T^2} - \sum_f n_f J_F \left[\frac{m_f^2(\phi_{\alpha})}{T^2}\right]$$

$$J_{B/F}(y^2) = \int_0^\infty dx \, x^2 \log\left(1 \mp \exp[-\sqrt{x^2 + y^2}]\right).$$

$$V_{\rm CW}^{(1)} = \sum_{i} (-1)^{F_i} n_i \frac{m_i^4(\phi_\alpha)}{64\pi^2} \left(\log\left[\frac{m_i^2(\phi_\alpha)}{Q^2}\right] - c_i \right)$$

$$V_{\text{eff}}(T) = V_0 + V_{\text{CW}}^{(1)} + \Delta V(T) + V_{\text{ct}}$$

$$n_s = 6, \quad n_{A_L} = 1$$

$$n_W = 6, \quad n_Z = 3, \quad n_{\gamma} = 2$$

$$n_{u,d,c,s,t,b} = 12, \quad n_{e,\mu,\tau} = 4, \quad n_{\nu_{1,2,3}} = n_{N_{1,2}^{\pm}}$$

$$\Delta V(T) = \frac{T^4}{2\pi^2} \left\{ \sum_b n_b J_B \left[\frac{m_b^2(\phi_\alpha)}{T^2} \right] - \sum_f n_f J_F \left[\frac{m_f^2(\phi_\alpha)}{T^2} \right] \right\}$$

$$J_{B/F}(y^2) = \int_0^\infty dx \, x^2 \log \left(1 \mp \exp[-\sqrt{x^2 + y^2}] \right).$$

$$m_i^2 \rightarrow m_i^2 + c_i T^2$$

$$\left\langle \frac{\partial V_{\rm ct}}{\partial \phi_{\alpha}} \right\rangle = \left\langle -\frac{\partial V_{\rm CW}^{(1)}}{\partial \phi_{\alpha}} \right\rangle \qquad \left\langle \frac{\partial^2 V_{\rm ct}}{\partial \phi_{\alpha} \partial \phi_{\beta}} \right\rangle = \left\langle -\frac{\partial^2 V_{\rm CW}^{(1)}}{\partial \phi_{\alpha} \partial \phi_{\beta}} \right\rangle$$

Counterterms are fixed such that the masses are preserved at 1-loop

If a multi-Higgs theory contains multiple vacua, phase transitions can take place: $V_{\rm BSM}(h_1, h_2, T)$

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Scenario II: Include fermion and Higgs portals

Explanation of DM and observability of SGWB (LISA and/or future facilities)

