

Isosinglet vectorlike leptons at e^+e^- colliders

Prudhvi N. Bhattiprolu

 University of Michigan

PIKIMO Fall 2023
Indiana University
November 11

Based on [arXiv:hep-ph/2308.08386](https://arxiv.org/abs/2308.08386)
with Stephen P. Martin and Aaron Pierce

- ▶ Hadron colliders: best discovery reach
- ▶ Lepton colliders: precision studies and indirect searches

This may not be the case for weakly interacting particles

- ▶ Hadron colliders: best discovery reach
- ▶ Lepton colliders: precision studies and indirect searches

This may not be the case for weakly interacting particles

Consider the example of $SU(2)_L$ -singlet **vectorlike** leptons τ' :

$$\tau'_L, \tau'^{\dagger}_R \sim (\mathbf{1}, \mathbf{1}, -1) + (\mathbf{1}, \mathbf{1}, +1)$$

- ▶ Hadron colliders: best discovery reach
- ▶ Lepton colliders: precision studies and indirect searches

This may not be the case for weakly interacting particles

Consider the example of $SU(2)_L$ -singlet **vectorlike** leptons τ' :

$$\tau'_L, \tau'^{\dagger}_R \sim (\mathbf{1}, \mathbf{1}, -1) + (\mathbf{1}, \mathbf{1}, +1)$$

in contrast with the **chiral** τ leptons in the SM:

$$\tau_L, \tau^{\dagger}_R \sim (\mathbf{1}, \mathbf{2}, -1/2) + (\mathbf{1}, \mathbf{1}, +1)$$

- ▶ Hadron colliders: best discovery reach
- ▶ Lepton colliders: precision studies and indirect searches

This may not be the case for weakly interacting particles

Consider the example of $SU(2)_L$ -singlet **vectorlike** leptons τ' :

$$\tau'_L, \tau'^{\dagger}_R \sim (\mathbf{1}, \mathbf{1}, -1) + (\mathbf{1}, \mathbf{1}, +1)$$

in contrast with the **chiral** τ leptons in the SM:

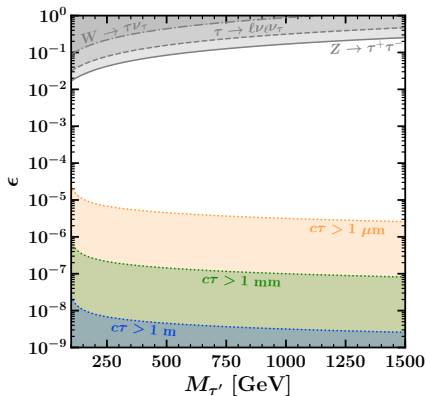
$$\tau_L, \tau^{\dagger}_R \sim (\mathbf{1}, \mathbf{2}, -1/2) + (\mathbf{1}, \mathbf{1}, +1)$$

Motivations:

- ▶ Many new physics models require vectorlike leptons
- ▶ New fermions must be necessarily vectorlike
- ▶ Decouple from flavor and EW precision data for higher masses
- ▶ Automatically anomaly-free (unlike chiral fermions)

Assume mass mixing of τ' and τ :

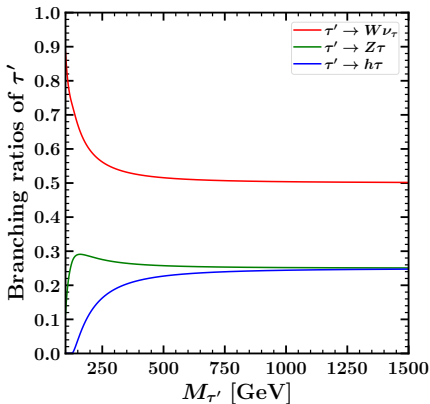
$$\mathcal{M} = \begin{pmatrix} y_{\tau} V & 0 \\ \epsilon V & M \end{pmatrix}$$



Assume tiny mass mixing of τ' and τ :

$$\mathcal{M} = \begin{pmatrix} y_{\tau V} & 0 \\ \epsilon V & M \end{pmatrix}$$

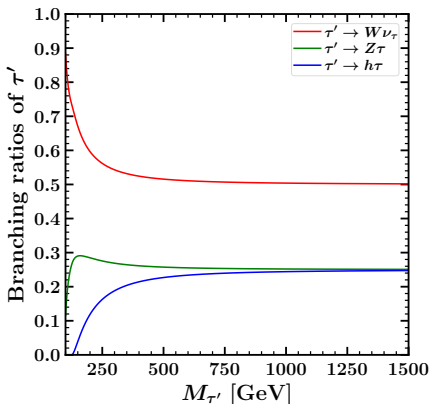
with prompt τ' decays



Assume tiny mass mixing of τ' and τ :

$$\mathcal{M} = \begin{pmatrix} y_{\tau V} & 0 \\ \epsilon V & M \end{pmatrix}$$

with prompt τ' decays



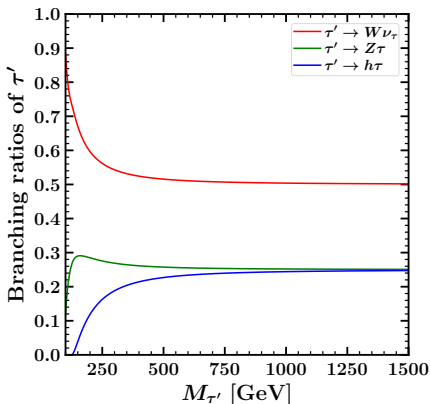
Limited reach for τ' at the

- ▶ LHC [[Kumar, Martin 1510.03456](#)]
- ▶ Future pp colliders [[PNB, Martin 1905.00498](#)]

Assume tiny mass mixing of τ' and τ :

$$\mathcal{M} = \begin{pmatrix} y_{\tau V} & 0 \\ \epsilon V & M \end{pmatrix}$$

with prompt τ' decays

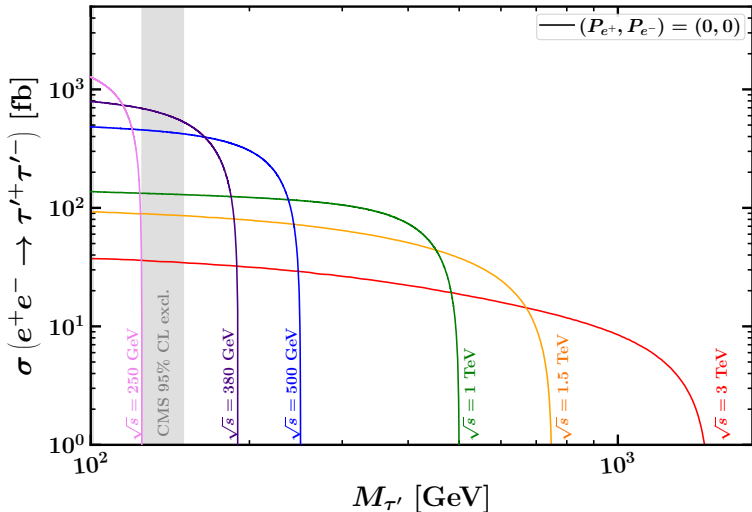


Limited reach for τ' at the

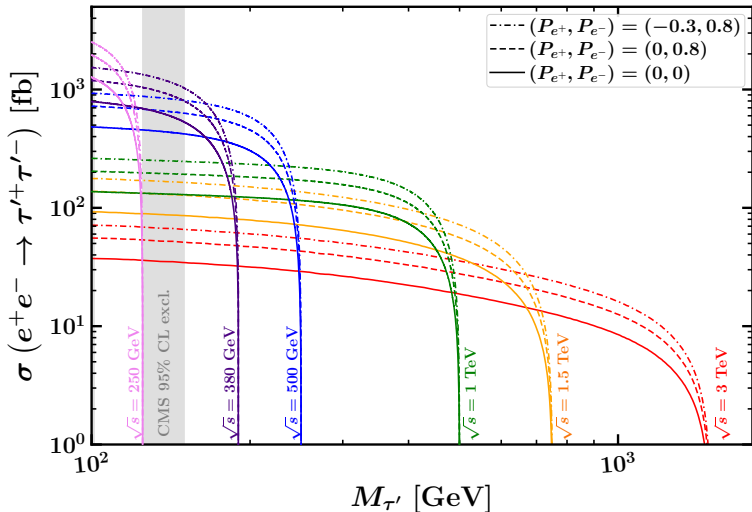
- ▶ LHC [[Kumar, Martin 1510.03456](#)]
- ▶ Future pp colliders [[PNB, Martin 1905.00498](#)]

Current 95% CL exclusions:

- ▶ $M_{\tau'} < 101.2$ GeV [[LEP 0107015](#)]
- ▶ 125 GeV $< M_{\tau'} < 150$ GeV [[CMS 2202.08676](#)]



- ▶ Pair-production mode: $e^+e^- \rightarrow \gamma^*, Z^* \rightarrow \tau'^+\tau'^-$
- ▶ Accounting for the effects of ISR + beamstrahlung



- ▶ Pair-production mode: $e^+e^- \rightarrow \gamma^*, Z^* \rightarrow \tau'^+\tau'^-$
- ▶ Accounting for the effects of ISR + beamstrahlung
- ▶ $(P_{e^+}, P_{e^-}) = (-0.3, 0.8)$ and $(0, 0.8)$ maximize σ for ILC and CLIC

Signal components:

$$e^+e^- \rightarrow \tau'^+\tau'^- \rightarrow \begin{array}{l} ZZ\tau^+\tau^-, \quad hh\tau^+\tau^-, \quad Zh\tau^+\tau^- \\ ZW^\pm\tau^\mp + \cancel{E}, \quad hW^\pm\tau^\mp + \cancel{E}, \\ W^\pm W^\mp + \cancel{E} \text{ (largest!)} \end{array}$$

[†]Relevant files at [github:prudhvibhattiprolu/VLL-UFOs](https://github.com/prudhvibhattiprolu/VLL-UFOs) (being used by ATLAS and CMS)

Signal components:

$$e^+e^- \rightarrow \tau'^+\tau'^- \rightarrow \begin{aligned} & ZZ\tau^+\tau^-, \quad hh\tau^+\tau^-, \quad Zh\tau^+\tau^- \\ & ZW^\pm\tau^\mp + \cancel{E}, \quad hW^\pm\tau^\mp + \cancel{E}, \\ & W^\pm W^\mp + \cancel{E} \text{ (largest!)} \end{aligned}$$

Backgrounds: $t\bar{t}$, $t\bar{t}Z$, $t\bar{t}h$, Zh , Zhh , ZZh , ZZZ , W^+W^-h , W^+W^-Z ,
and $W^+W^-\nu\bar{\nu}$ with $\nu\bar{\nu} \notin Z$

[†]Relevant files at [github:prudhvibhattiprolu/VLL-UFOs](https://github.com/prudhvibhattiprolu/VLL-UFOs) (being used by ATLAS and CMS)

Signal components:

$$e^+e^- \rightarrow \tau'^+\tau'^- \rightarrow \begin{array}{l} ZZ\tau^+\tau^-, \quad hh\tau^+\tau^-, \quad Zh\tau^+\tau^- \\ ZW^\pm\tau^\mp + \cancel{E}, \quad hW^\pm\tau^\mp + \cancel{E}, \\ W^\pm W^\mp + \cancel{E} \text{ (largest!)} \end{array}$$

Backgrounds: $t\bar{t}$, $t\bar{t}Z$, $t\bar{t}h$, Zh , Zhh , ZZh , ZZZ , W^+W^-h , W^+W^-Z ,
and $W^+W^-\nu\bar{\nu}$ with $\nu\bar{\nu} \notin Z$

Events generated at LO while accounting for ISR + beamstrahlung:
FEYNRULES[†] → WHIZARD → PYTHIA8 → DELPHES

[†]Relevant files at [github:prudhvibhattiprolu/VLL-UFOs](https://github.com/prudhvibhattiprolu/VLL-UFOs) (being used by ATLAS and CMS)

Signal components:

$$e^+e^- \rightarrow \tau'^+\tau'^- \rightarrow \begin{array}{l} ZZ\tau^+\tau^-, \quad hh\tau^+\tau^-, \quad Zh\tau^+\tau^- \\ ZW^\pm\tau^\mp + \cancel{E}, \quad hW^\pm\tau^\mp + \cancel{E}, \\ W^\pm W^\mp + \cancel{E} \text{ (largest!)} \end{array}$$

Backgrounds: $t\bar{t}$, $t\bar{t}Z$, $t\bar{t}h$, Zh , Zhh , ZZh , ZZZ , W^+W^-h , W^+W^-Z ,
and $W^+W^-\nu\bar{\nu}$ with $\nu\bar{\nu} \notin Z$

Events generated at LO while accounting for ISR + beamstrahlung:
FEYNRULES[†] → WHIZARD → PYTHIA8 → DELPHES

Goal: Reconstructing mass peaks for various $M_{\tau'}$ in various signal regions

[†]Relevant files at [github:prudhvibhattiprolu/VLL-UFOs](https://github.com/prudhvibhattiprolu/VLL-UFOs) (being used by ATLAS and CMS)

Signal components:

$$e^+e^- \rightarrow \tau'^+\tau'^- \rightarrow \begin{aligned} & ZZ\tau^+\tau^-, \quad hh\tau^+\tau^-, \quad Zh\tau^+\tau^- \\ & ZW^\pm\tau^\mp + \cancel{E}, \quad hW^\pm\tau^\mp + \cancel{E}, \\ & W^\pm W^\mp + \cancel{E} \text{ (largest!)} \end{aligned}$$

Backgrounds: $t\bar{t}$, $t\bar{t}Z$, $t\bar{t}h$, Zh , Zhh , ZZh , ZZZ , W^+W^-h , W^+W^-Z ,
and $W^+W^-\nu\bar{\nu}$ with $\nu\bar{\nu} \notin Z$

Events generated at LO while accounting for ISR + beamstrahlung:
FEYNRULES[†] → WHIZARD → PYTHIA8 → DELPHES

Goal: Reconstructing mass peaks for various $M_{\tau'}$ in various signal regions

Consider a 500 GeV e^+e^- collider with unpolarized beams ...

[†]Relevant files at [github:prudhvibhattiprolu/VLL-UFOs](https://github.com/prudhvibhattiprolu/VLL-UFOs) (being used by ATLAS and CMS)

Signal regions: 15 different signal regions targeting various final states with

$$\begin{aligned}N_\ell + N_j + N_b &= 4 \\ N_\tau &= 1 \text{ or } 2\end{aligned}$$

Reconstruct Z from $\ell^+\ell^-/jj$, h from bb , and also W from jj if $N_\tau = 1$

E.g.,

- ▶ $4\ell + 2\tau$
- ▶ $2\ell + 2b + 2\tau$
- ▶ $4b + 2\tau$
- ▶ $2\ell + 2j + 1\tau$
- ▶ $2j + 2b + 1\tau$
- ▶ $3j + 1b + 2\tau$ ($Z/h/W$ also reconstructed from jb)
- ▶ ...

Signal regions: 15 different signal regions targeting various final states with

$$\begin{aligned}N_\ell + N_j + N_b &= 4 \\ N_\tau &= 1 \text{ or } 2\end{aligned}$$

Reconstruct Z from $\ell^+\ell^-/jj$, h from bb , and also W from jj if $N_\tau = 1$

E.g.,

- ▶ $4\ell + 2\tau \rightarrow ZZ\tau\tau$
- ▶ $2\ell + 2b + 2\tau \rightarrow Zh\tau\tau$
- ▶ $4b + 2\tau \rightarrow hh\tau\tau$
- ▶ $2\ell + 2j + 1\tau \rightarrow ZW\tau\nu\tau$
- ▶ $2j + 2b + 1\tau \rightarrow hW\tau\nu\tau$
- ▶ $3j + 1b + 2\tau \rightarrow ZZ\tau\tau, Zh\tau\tau$
- ▶ ...

Peak reconstruction:

- ▶ Reconstruct Z/h bosons, B_α , and also W bosons, W_β , if $N_\tau = 1$

Peak reconstruction:

- ▶ Reconstruct Z/h bosons, B_α , and also W bosons, W_β , if $N_\tau = 1$
- ▶ Rescale jet momenta if $Z/h/W$ reconstructed from jets such that $M_{JJ} = M_{Z/h/W}$ (Here and below, $J = j, b$)

Peak reconstruction:

- ▶ Reconstruct Z/h bosons, B_α , and also W bosons, W_β , if $N_\tau = 1$
- ▶ Rescale jet momenta if $Z/h/W$ reconstructed from jets such that $M_{JJ} = M_{Z/h/W}$ (Here and below, $J = j, b$)
- ▶ Find all the possible (tau, boson) pairings:

$$\tau'_1 \supset (\tau_1, \nu_1, B_\alpha) \text{ and } \tau'_2 \supset \begin{cases} (\tau_2, \nu_2, B_\beta) \text{ in SRs with exactly } 2\tau \\ (\nu_2, W_\beta) \text{ in SRs with exactly } 1\tau \end{cases}$$

such that the bosons in τ'_1 and τ'_2 are distinct

Peak reconstruction:

- ▶ Reconstruct Z/h bosons, B_α , and also W bosons, W_β , if $N_\tau = 1$
- ▶ Rescale jet momenta if $Z/h/W$ reconstructed from jets such that $M_{JJ} = M_{Z/h/W}$ (Here and below, $J = j, b$)
- ▶ Find all the possible (tau, boson) pairings:

$$\tau'_1 \supset (\tau_1, \nu_1, B_\alpha) \text{ and } \tau'_2 \supset \begin{cases} (\tau_2, \nu_2, B_\beta) \text{ in SRs with exactly } 2\tau \\ (\nu_2, W_\beta) \text{ in SRs with exactly } 1\tau \end{cases}$$

such that the bosons in τ'_1 and τ'_2 are distinct

- ▶ In SRs with 2τ : τ_1 is the τ with highest energy, or it is relabeled to be the τ paired with the leptonically decaying Z if there is exactly one Z reconstructed from leptons

- Use collinear approximation for ν_1 from τ_1 decay:

$$E_{\nu_1} = |\vec{p}_{\nu_1}|, \quad \vec{p}_{\nu_1} = (r - 1)\vec{p}_{\tau_1},$$

and obtain the four-momentum of the other neutrino using:

$$E_{\nu_2} = \cancel{E} - E_{\nu_1}, \quad \vec{p}_{\nu_2} = \frac{E_{\nu_2}}{|\vec{p} - \vec{p}_{\nu_1}|} (\vec{p} - \vec{p}_{\nu_1}),$$

such that both ν_1 and ν_2 are on-shell.

- ▶ Use collinear approximation for ν_1 from τ_1 decay:

$$E_{\nu_1} = |\vec{p}_{\nu_1}|, \quad \vec{p}_{\nu_1} = (r-1)\vec{p}_{\tau_1},$$

and obtain the four-momentum of the other neutrino using:

$$E_{\nu_2} = \cancel{E} - E_{\nu_1}, \quad \vec{p}_{\nu_2} = \frac{E_{\nu_2}}{|\vec{p} - \vec{p}_{\nu_1}|} (\vec{p} - \vec{p}_{\nu_1}),$$

such that both ν_1 and ν_2 are on-shell.

- ▶ For each pairing, solve for r from:

$$p_{\tau'_1}^2 = p_{\tau'_2}^2$$

and impose $E_{\nu_1} \geq 0$ and $E_{\nu_2} \geq 0$

- ▶ Use collinear approximation for ν_1 from τ_1 decay:

$$E_{\nu_1} = |\vec{p}_{\nu_1}|, \quad \vec{p}_{\nu_1} = (r-1)\vec{p}_{\tau_1},$$

and obtain the four-momentum of the other neutrino using:

$$E_{\nu_2} = \cancel{E} - E_{\nu_1}, \quad \vec{p}_{\nu_2} = \frac{E_{\nu_2}}{|\vec{p} - \vec{p}_{\nu_1}|} (\vec{p} - \vec{p}_{\nu_1}),$$

such that both ν_1 and ν_2 are on-shell.

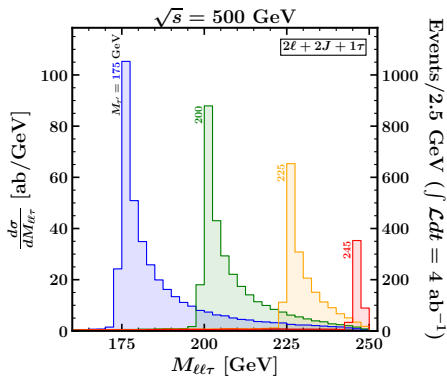
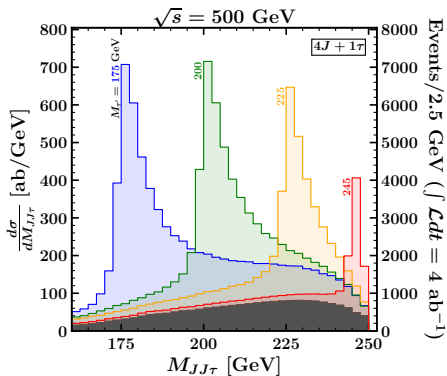
- ▶ For each pairing, solve for r from:

$$p_{\tau'_1}^2 = p_{\tau'_2}^2$$

and impose $E_{\nu_1} \geq 0$ and $E_{\nu_2} \geq 0$

- ▶ If multiple pairings survive, pick a pairing that minimizes $|\vec{p}_{\text{total}}|$ and

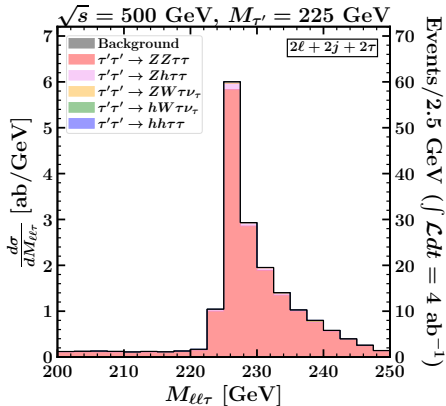
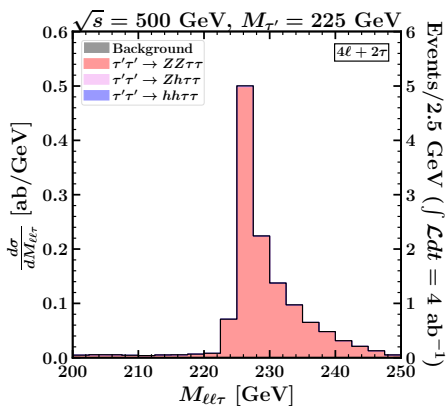
$$M_{\tau'}^{\text{reco}} = \sqrt{p_{\tau'_1}^2}$$



- ▶ Since $\text{BR}(\tau' \rightarrow W\nu_\tau)$ is the largest, we have far better statistics in these SRs
- ▶ Backgrounds are (non-)negligible (but still clearly under control)
- ▶ Similar peak reconstructions also possible in all SRs with 2τ

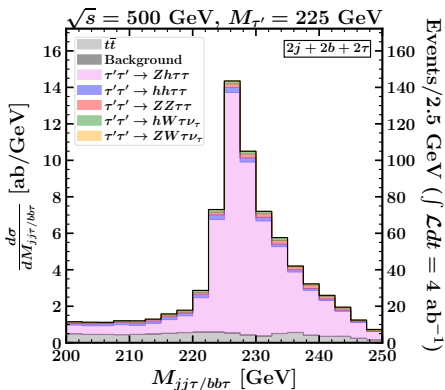
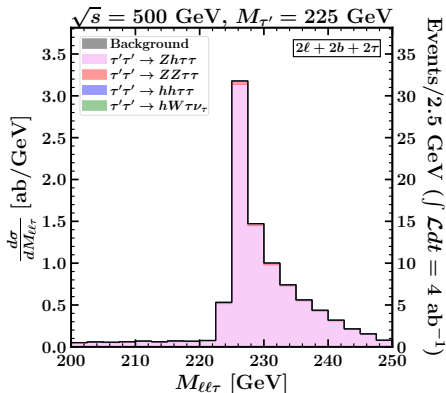
If τ' indeed discovered, the heights of mass peaks in various SRs can be used to determine τ' branching ratios!

If τ' indeed discovered, the heights of mass peaks in various SRs can be used to determine τ' branching ratios!



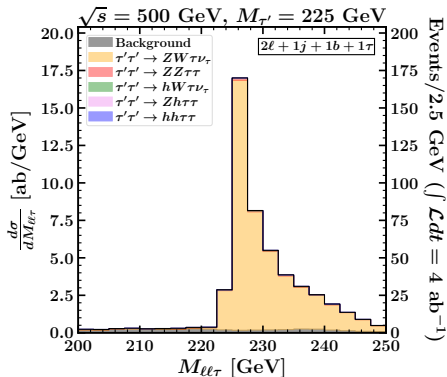
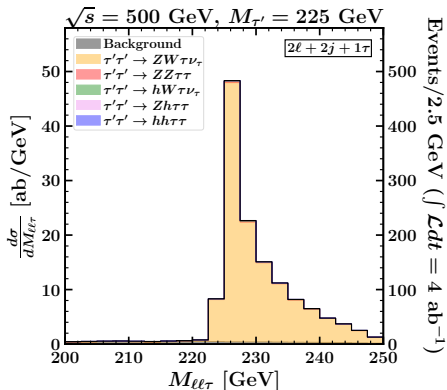
- ▶ $4\ell + 2\tau$ and $2\ell + 2j + 2\tau$ SRs provide a pure sample of $ZZ\tau\tau$ final state

Similarly,



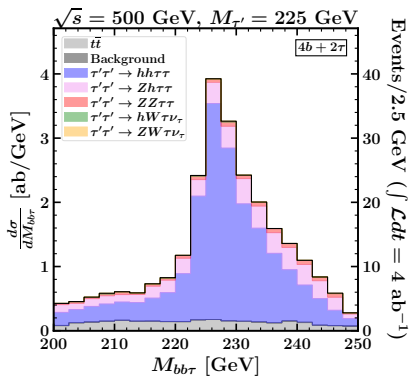
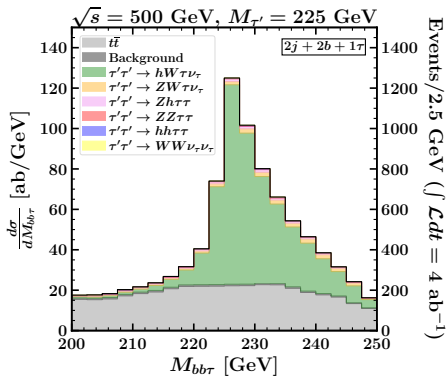
- ▶ $2\ell + 2b + 2\tau$ and $2j + 2b + 2\tau$ SRs provide a pure sample of $Zh\tau\tau$ final state

Similarly,



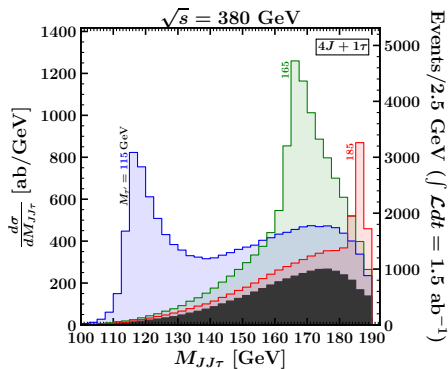
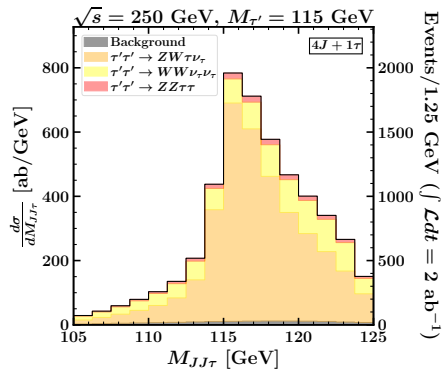
- ▶ $2\ell + 2j + 1\tau$ and $2j + 1j + 1b + 1\tau$ SRs provide a pure sample of $ZW\tau\nu$ final state

Similarly,



- ▶ $2j + 2b + 1\tau$ ($4b + 2\tau$) SR provides a (relatively) pure sample of $hW\tau\nu$ ($hh\tau\tau$) final state

Both Higgs and top factories can also act as discovery machines ...



- ▶ For $M_{\tau'} < M_h + M_{\tau}$, since $\tau' \rightarrow h\tau$ is not accessible, we also reconstruct Z from bb

Conclusions:

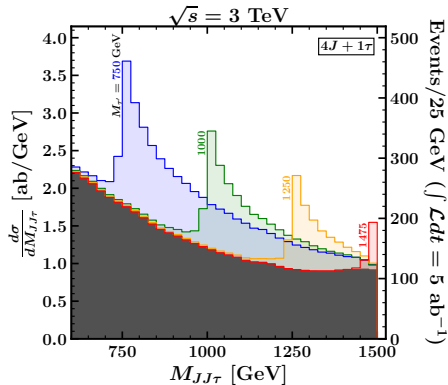
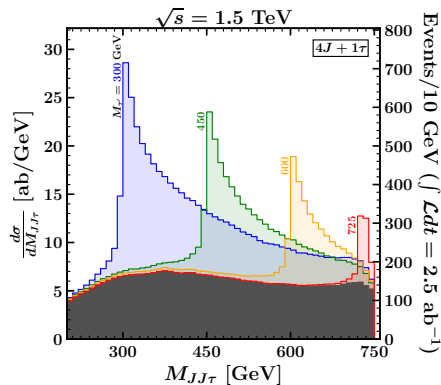
- ▶ Considered an example of weak isosinglet vectorlike leptons that are well-motivated
- ▶ Demonstrated that its mass peaks can be reconstructed in various signal regions up to close to the kinematic limit
- ▶ Heights of the mass peaks in various signal regions can in turn give a handle on the branching ratios

Conclusions:

- ▶ Considered an example of weak isosinglet vectorlike leptons that are well-motivated
- ▶ Demonstrated that its mass peaks can be reconstructed in various signal regions up to close to the kinematic limit
- ▶ Heights of the mass peaks in various signal regions can in turn give a handle on the branching ratios

e^+e^- collider may act as a discovery machine for particles with only electroweak interactions that have limited reach at a hadron collider!

At $\sqrt{s} = 1.5$ and 3 TeV:



- ▶ Since the production cross section falls with \sqrt{s} , a lack of adequate statistics can be an issue in some signal regions
- ▶ Backgrounds can be more significant, but with a smooth mass distribution that should be under good theoretical control

Partonic pair-production cross-section $\hat{\sigma}(e^+e^- \rightarrow \tau'^+\tau'^-)$:

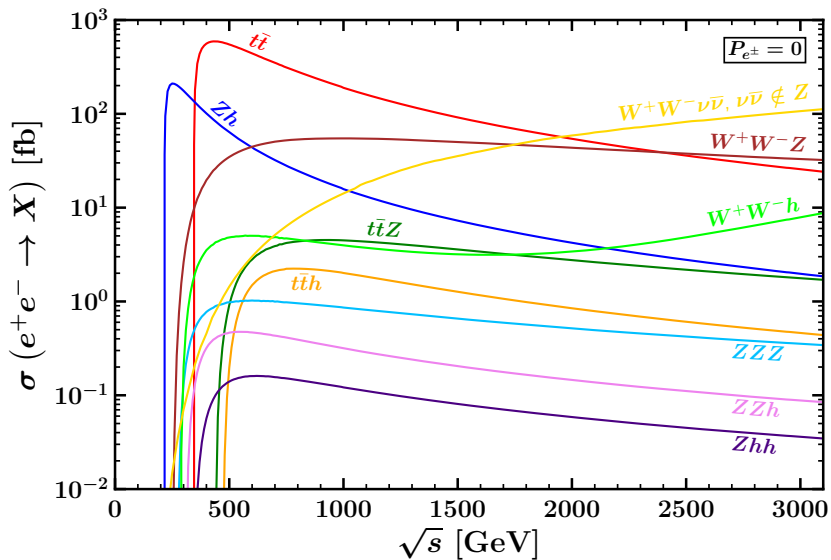
$$\hat{\sigma} = \frac{2\pi\alpha^2}{3}(\hat{s} + 2M_{\tau'}^2) \sqrt{1 - 4M_{\tau'}^2/\hat{s}} \left[|a_L|^2(1 - P_{e^-})(1 + P_{e^+}) + |a_R|^2(1 + P_{e^-})(1 - P_{e^+}) \right],$$

where the left-handed and right-handed amplitude coefficients are

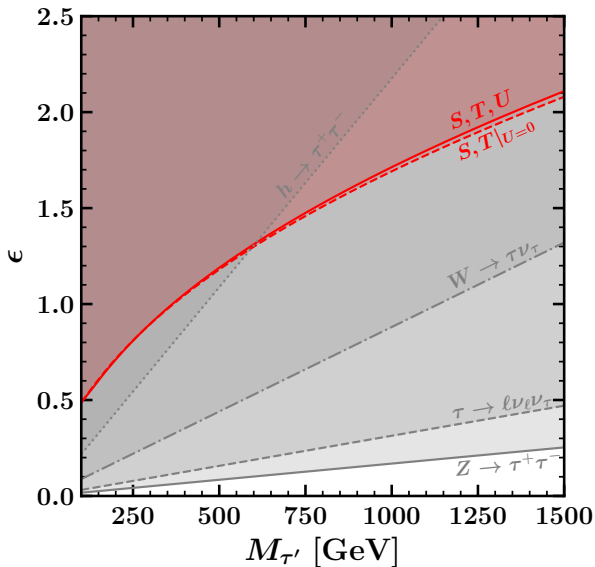
$$a_L = \frac{1}{\hat{s}} + \frac{1}{c_W^2}(s_W^2 - 1/2) \frac{1}{\hat{s} - M_Z^2},$$
$$a_R = \frac{1}{\hat{s}} + \frac{s_W^2}{c_W^2} \frac{1}{\hat{s} - M_Z^2}.$$

- ▶ $P = 1$ and -1 corresponding to pure right-handed and left-handed polarizations
- ▶ Since $|a_L| < |a_R|$ for $\sqrt{\hat{s}} > 93$ GeV, we see that the production cross-section is maximized when P_{e^-} is positive (and, if available, when P_{e^+} is negative)

SM backgrounds:



Precision electroweak:



If τ' is stable over detector lengths, then it can be inferred that $M_{\tau'} \gtrsim 750$ GeV based on the $-dE/dx$ and time of flight measurements in searches for long lived charginos at the LHC

