

# MC-EKRT event generator for initializing 3+1 D hydrodynamics

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In collaboration with  
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- Problem: So far at midrapidity only, cannot study y-dependent observables!  
Overall E-conservation?

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- 7 Run 3+1 D viscous hydro.
- 8 Compute observables.

## Minijets from nucleon-nucleon pairs

- For nucleons  $a \in A$  and  $b \in B$ , the probability to produce  $n \geq 0$  minijet pairs:

$$P_n^{ab}(\bar{b}_{ab}) \equiv \frac{\left(T_{NN}(\bar{b}_{ab}) \sigma_{\text{jet}}^{ab}\right)^n}{n!} e^{-T_{NN}(\bar{b}_{ab}) \sigma_{\text{jet}}^{ab}},$$

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- Dijets' transverse momentum  $p_T$  and rapidities  $y_1, y_2$  sampled from  $\frac{d\sigma_{\text{jet}}^{ab}}{dp_T^2 dy_1 dy_2}$ , and spatial coordinates sampled from  $T_N(\bar{s} - \bar{s}_a) * T_N(\bar{s} - \bar{s}_b)$ .



# Minijet cross section with spatial nPDFs

- LO differential cross section of hard parton production:

$$\frac{d\sigma_{\text{jet}}^{ab}}{dp_T^2 dy_1 dy_2} = K \sum_{ijkl} x_1 f_i^{a/A}(\bar{s}_a, x_1, Q^2) x_2 f_j^{b/B}(\bar{s}_b, x_2, Q^2) \times \frac{d\hat{\sigma}^{ij \rightarrow kl}}{d\hat{t}}.$$

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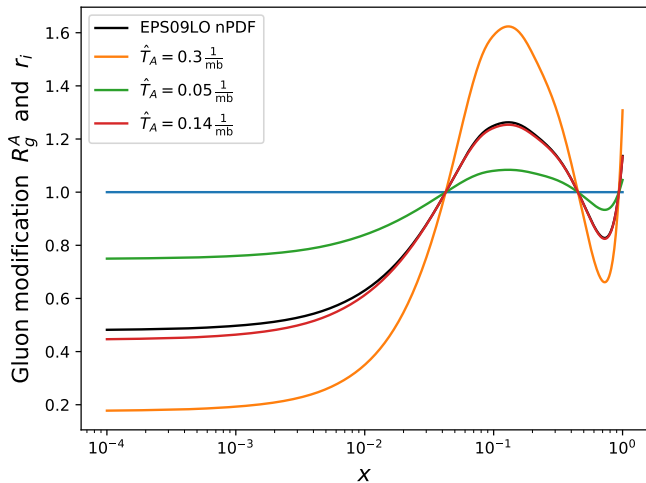
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- Solution: Define the EbyE fluctuating spatially dependent nPDF of the proton  $a$  bound in a nucleus  $A$  as

$$f_i^{a/A}(\bar{s}_a, x, Q^2) \equiv \exp\left(c_A(x, Q^2) \hat{T}_A^a(\bar{s}_a)\right) f_i^p(x, Q^2),$$

where  $c_A(x, Q^2)$  is set by normalizing to the global averaged nuclear modification  $R_A^i(x, Q^2) = f_i^A(x, Q^2)/f_i^p(x, Q^2)$  (EPS09LO).

## Spatial nPDFs



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- Filter in the order of the formation time  $\tau = 1/p_T$ :  
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$$\|\bar{s} - \bar{s}^{\text{cand}}\| < \frac{1}{\kappa_{\text{sat}}} \left( \frac{1}{p_T} + \frac{1}{p_T^{\text{cand}}} \right) \quad \Rightarrow \quad \text{Reject the candidate.}$$

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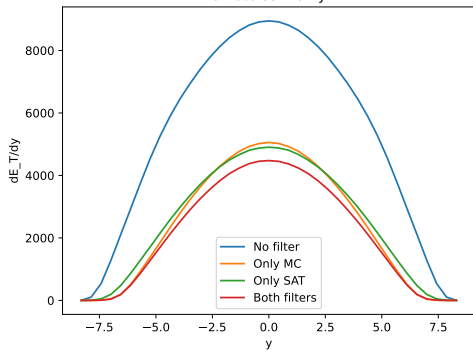
- Momentum conservation at nucleon level: A candidate dijet process with momentum fractions  $x_1$  and  $x_2$  is accepted if

$$x_1 + \sum_{i=1}^n x_1^{(i)} \leq 1 \quad \text{and} \quad x_2 + \sum_{i=1}^m x_2^{(i)} \leq 1,$$

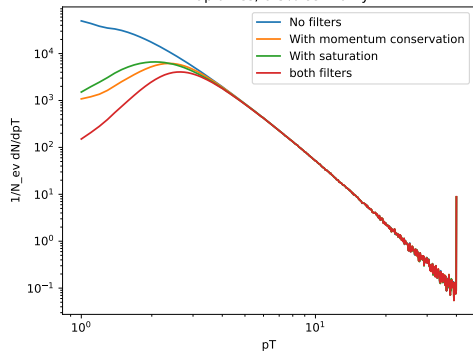
where the summations are over the previously accepted processes from nucleons 1 and 2.

# The effect of the filters

0-10% centrality



All rapidities, 0-5% centrality





## 3+1D viscous hydro

- The accepted minijets are propagated as free particles to the proper time surface  $\tau_0 = 1/p_{T0}$  ( $= 0.2 \text{ fm}/\mathbf{c}$ ) and spacetime rapidity  $\eta = y$ .

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- The initial energy density profile in an event is then:

$$e(\bar{s}, \eta) = \frac{1}{\tau_0 d^2 \bar{s} d\eta} \sum_{i=1}^{N_{\text{jet}}} g_i(\bar{s}, \eta, \sigma_L, \sigma_T) p_{Ti} \cosh(\eta - \eta_i),$$

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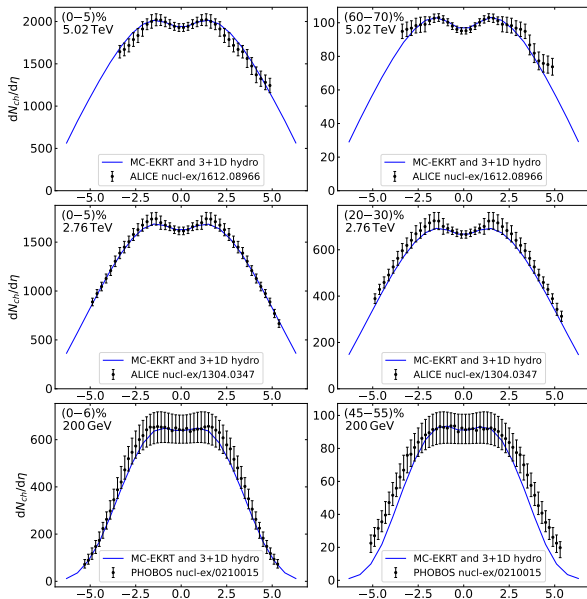
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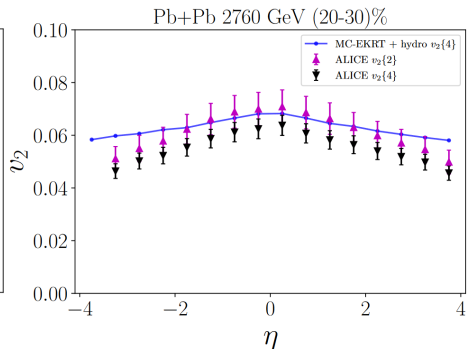
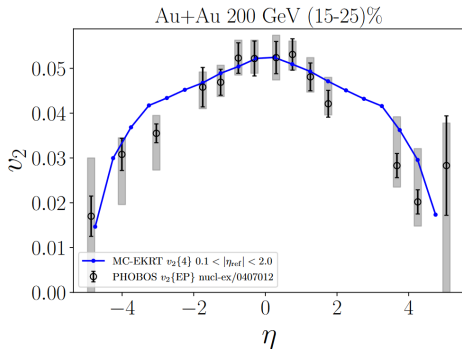
where  $g_i(\bar{s}, \eta, \sigma_L, \sigma_T)$  is a Gaussian-type smearing function.

- In this exploratory work: Constant value  $\eta/s = 0.12$  for the specific shear viscosity; no bulk viscosity; EoS *s95p-PCE* with  $T_{chem} = 150 \text{ MeV}$ ; kinetic freeze-out at  $T_{kin} = 130 \text{ MeV}$ ; resonance decays with PYTHIA; averaged initial states for each centrality class.

# Charged hadron multiplicity



# Elliptic flow $v_2$



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- The initial results are very promising!

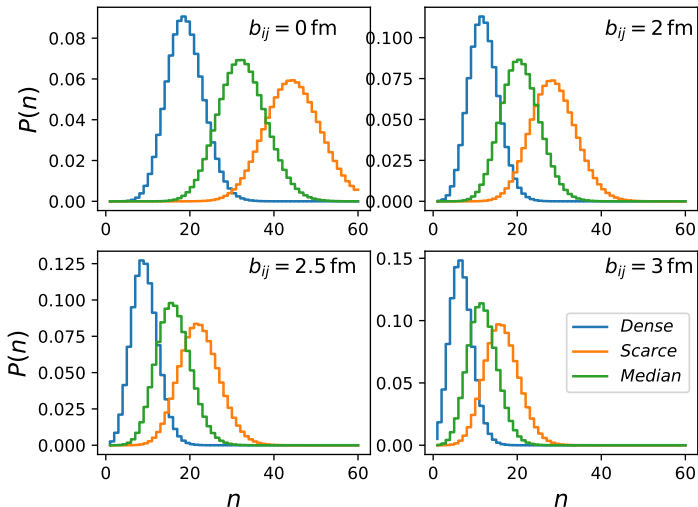


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# Thank you!

# Minijet production probability



## Spatial nPDFs with more detail

$$f_i^{a/A}(\bar{s}_a, x, Q^2) \equiv \exp\left(c_A(x, Q^2) \hat{T}_A^a(\bar{s}_a)\right) f_i^P(x, Q^2),$$

where  $\hat{T}_A^a$  is a  $T_N$ -weighted average of the nuclear thickness function experienced by the nucleon  $a$ ,

$$\hat{T}_A^a(\bar{s}_a) \equiv \sum_{b \neq a}^A T_{NN}(\bar{b}_{ab}).$$

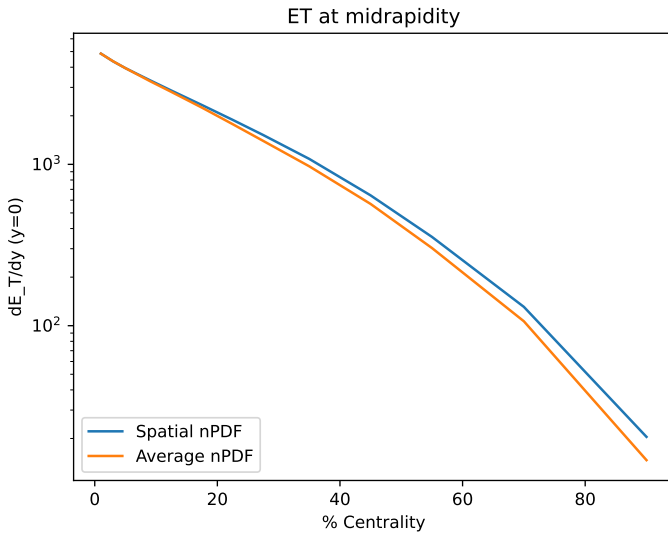
The coefficient  $c_A(x, Q^2)$  is set by normalizing to the global averaged nuclear modification (EPS09LO):

$$R_i^A(x, Q^2) = \left\langle \int d^2\bar{s} \frac{\sum_{a=1}^A f_i^{a/A}(\bar{s}_a, x, Q^2)}{A f_i^P(x, Q^2)} \right\rangle_{\{A\}} \equiv F(c_A(x, Q^2)),$$

where  $\langle \cdot \rangle_{\{A\}}$  is an average over all the sampled nuclei. The function  $F$  can be inverted numerically:

$$c_A(x, Q^2) \equiv F^{-1}\left(R_i^A(x, Q^2)\right).$$

# Spatial vs averaged nPDFs



## 3+1D viscous hydro with more detail

Gaussian-type smearing function

$$g_i(\bar{s}, \eta, \sigma_L, \sigma_T) = \frac{1}{N} e^{-\frac{1}{2} \frac{(\bar{s} - \bar{s}_i)^2}{\sigma_T^2}} e^{-\frac{1}{2} \frac{(\eta - \eta_i)^2}{\sigma_L^2}}$$

The events are divided into centrality classes according to the initial  $E_T$ . For each event, the energy density profile is converted to entropy density using the equation of state *s95p-PCE* with chemical freeze-out at 150 MeV. The event averaged entropy density is then converted back to energy density in each centrality class. The hydrodynamical evolution lasts until kinetic freeze-out temperature  $T_{\text{kin}} = 130$  MeV. We use a constant value  $\eta/s = 0.12$  for the specific shear viscosity and omit the bulk viscous effects.

# Proton-proton minimum bias

