

Emittance Control for Diamond-II

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Talk Outline

Introduction to Diamond-II

- Lattice details

- Target emittance (horizontal and vertical)

- Impact of IDs (max/min/variation)

Vertical Dispersion and Coupling Control using Skew Quadrupoles

- Method

- Impact on dynamic aperture

Emittance Excitation using the Transverse Multi-bunch Feedback (TMBF)

- Method

- Simulation results for Diamond-II

- Experimental tests on Diamond

Diamond-II Lattice

Modified Hybrid 6-Bend Achromat (M-H6BA) for low emittance

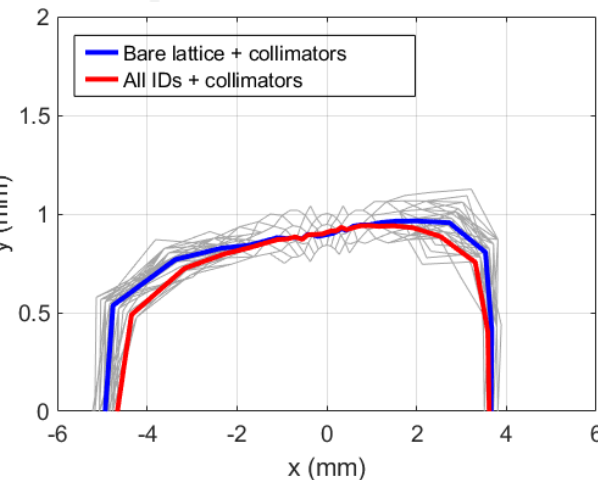
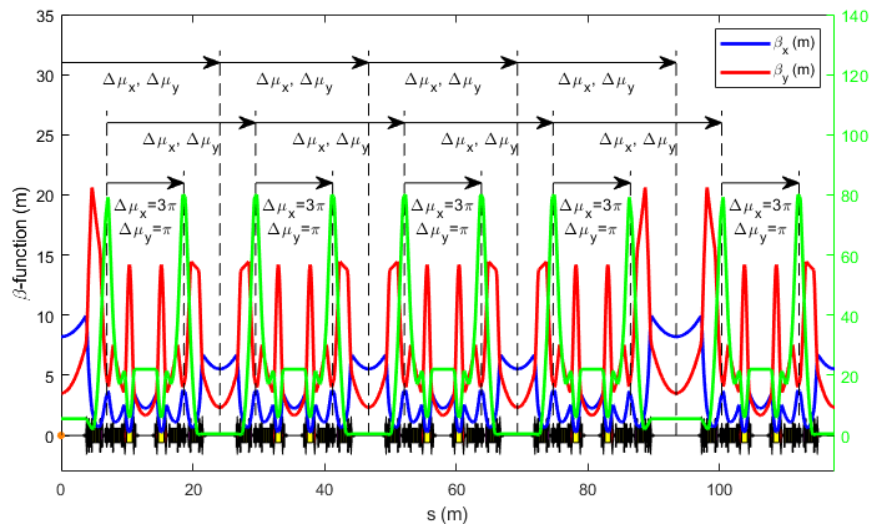
Number of insertion straights increased from 24 to 48

- Long straights: 7.54 m
- Standard straights: 5.06 m
- Mid straights: 2.92 m

Off-axis injection for beam accumulation

‘-I’ transformer plus const. cell phase for nonlinear dynamics

Passive SC harmonic cavity for lifetime / beam stability / IBS



| Parameter | Units | Diamond | Diamond-II |
|------------------------------|------------------|----------------|----------------|
| Energy | GeV | 3.0 | 3.5 |
| Circumference | M | 560.6 | 560.560944 |
| Harmonic Number | - | 936 | 934 |
| RF Frequency | MHz | 499.654 | 499.511 |
| Positive Bending Angle | deg | 360.0 | 374.4 |
| Reverse Bending Angle | deg | 0.0 | 14.4 |
| Total Bending Angle | deg | 360.0 | 388.8 |
| Betatron Tunes | - | [27.21, 12.36] | [54.14, 20.24] |
| Natural Chromaticity | - | [-79.0, -35.6] | [-68.2, -89.1] |
| Corrected Chromaticity | - | [1.7, 2.2] | [2.6, 2.6] |
| Mom. Compaction Factor | $\times 10^{-4}$ | 1.70 | 1.03 |
| Natural Emittance | pm.rad | 2729 | 162 |
| Energy Spread | % | 0.096 | 0.094 |
| Energy Loss per Turn | MeV | 1.01 | 0.724 |
| Natural Bunch Length | ps | 11.4@2.4 MV | 12.4@1.4 MV |
| Horizontal Damping Partition | - | 1.00 | 1.88 |
| Horizontal Damping Time | ms | 11.1 | 9.4 |
| Vertical Damping Time | ms | 11.2 | 18.1 |
| Longitudinal Damping Time | ms | 5.6 | 16.1 |

Target Emittance for Diamond-II

Emittance control will be required for Diamond-II.

User requirements:

- 1) stable conditions
- 2) aim for $\varepsilon_y < 10$ pm (diffraction limit at 10 keV)

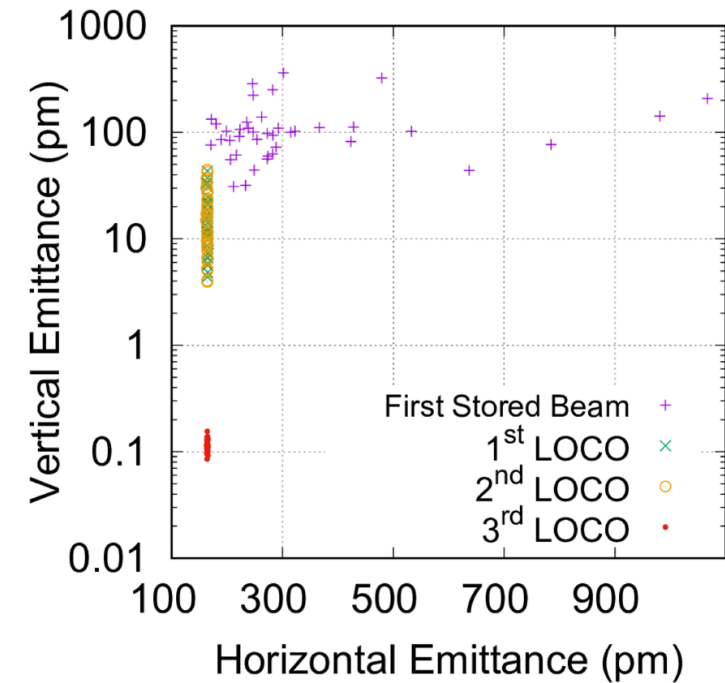
Horizontal emittance can vary between 115 pm and 178 pm depending on ID conditions

Simulated commissioning simulations suggest $\varepsilon_y < 1$ pm after optics and coupling correction

Lifetime favours larger ε_y (targeting $\tau \sim 8$ h with harmonic cavity)

Target emittance (stabilised):

- $\varepsilon_y = 8$ pm (same as current Diamond storage ring)
- $\varepsilon_x \sim 140$ pm (TBD, depending on operational experience)



| Machine Condition | Emittance |
|--|-----------|
| Bare lattice | 162 pm |
| All mid-straight IDs (9 devices) | 178 pm |
| All standard straight IDs (18 devices) | 115 pm |
| All long straight IDs (7 devices) | 145 pm |
| All IDs (34 devices) | 121 pm |

Vertical Dispersion and Coupling Control using Skew Quads

Method:

- 1) Apply LOCO to correct η_y and betatron coupling
- 2) Analytically calculate vector of skew quadrupoles to drive η_y wave without exciting betatron coupling*
 - 1) Use skew-quads at high η_x point to drive η_y wave
 - 2) Use skew-quads at zero η_x point to correct betatron coupling in the straights without altering η_y
- 3) Use feedback to adjust amplitude of skew vector to maintain constant measured vertical emittance

Change in vertical dispersion at BPM #k due to skew quadrupole #j:

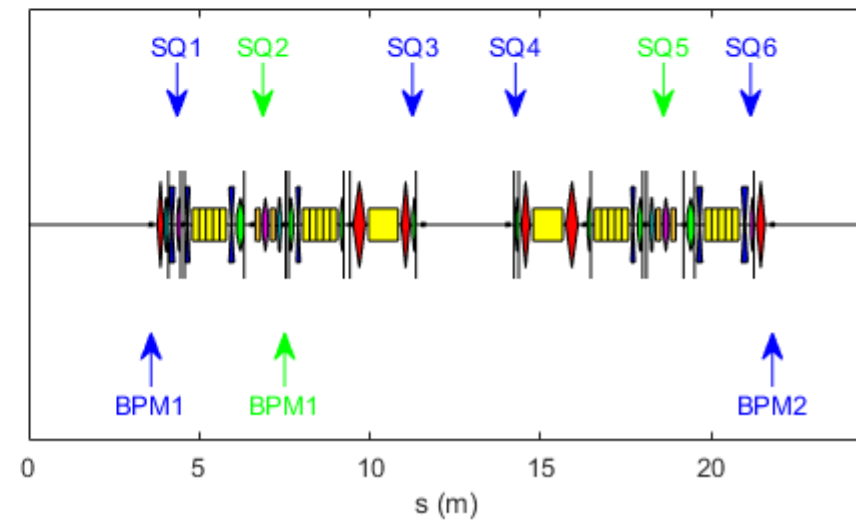
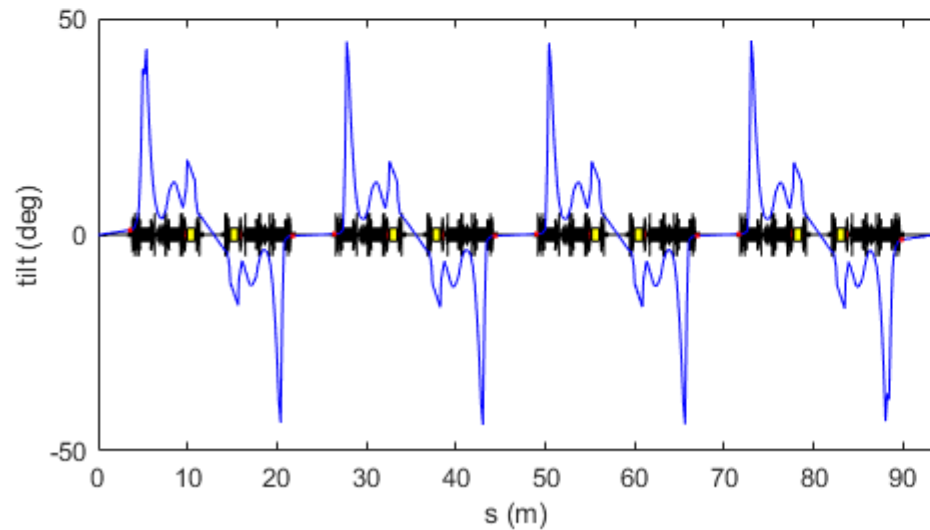
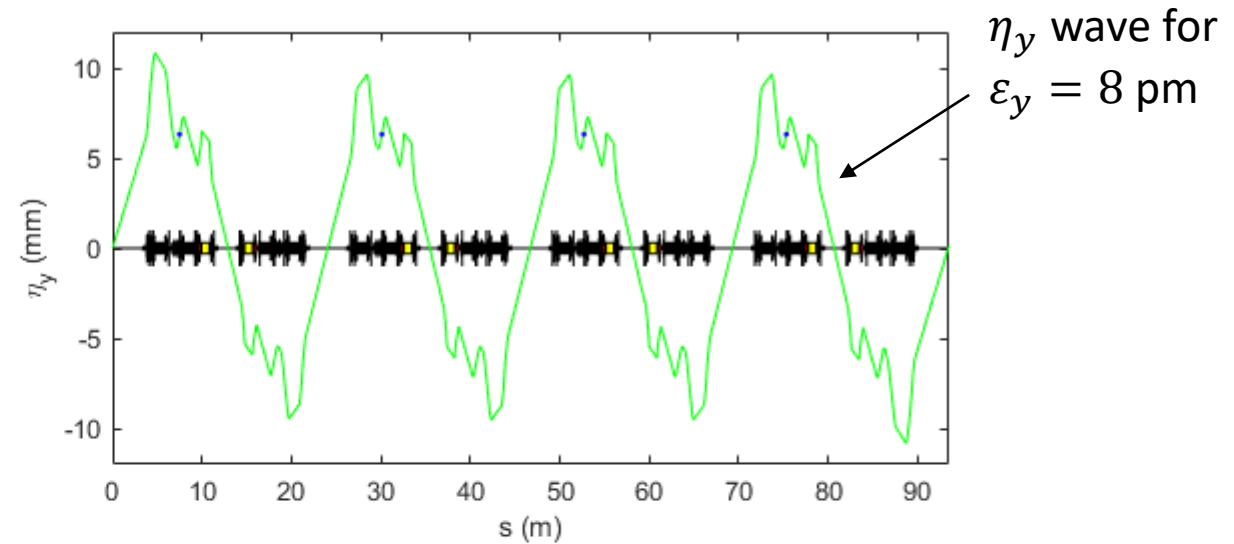
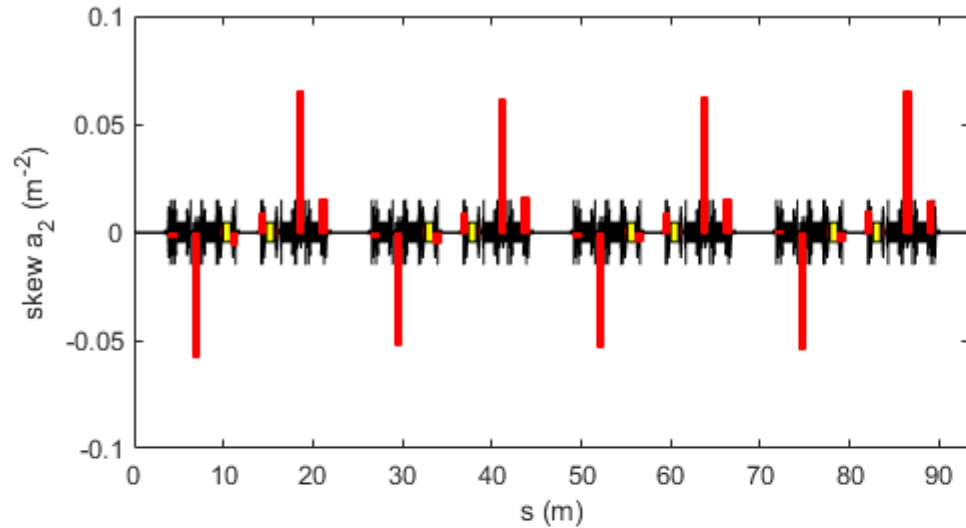
$$\Delta\eta_{y,k} = -(\Delta a_2 L)_j \eta_{x,j} \frac{\sqrt{\beta_{y,j}\beta_{y,k}}}{2 \sin(\pi Q_y)} \cos(\mu_{y,j \rightarrow k} - \pi Q_y)$$

**J. Bengtsson, NSLS-II Tech Note 007, July 2007*

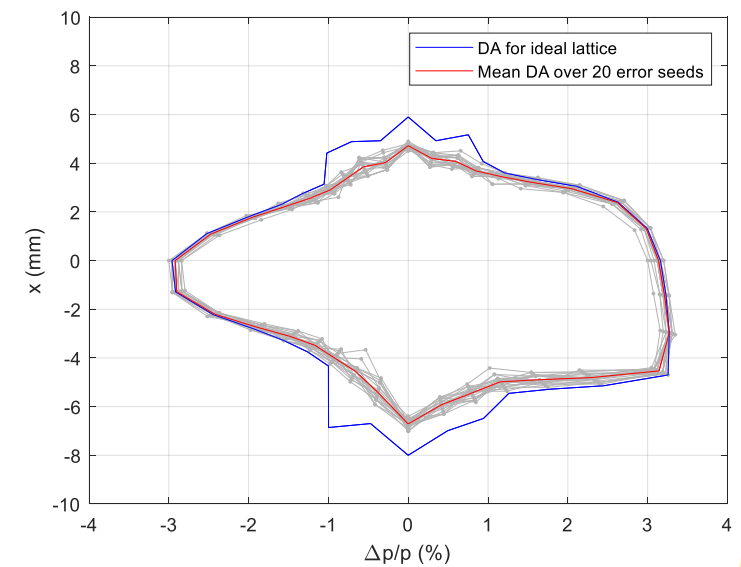
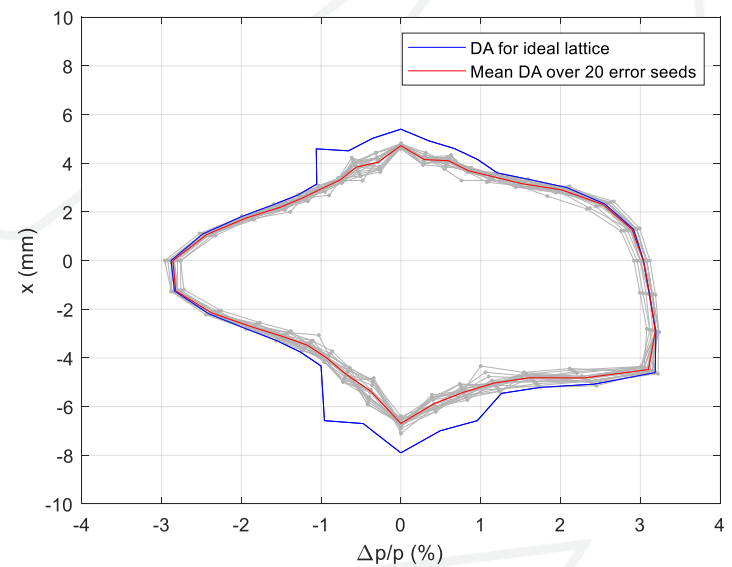
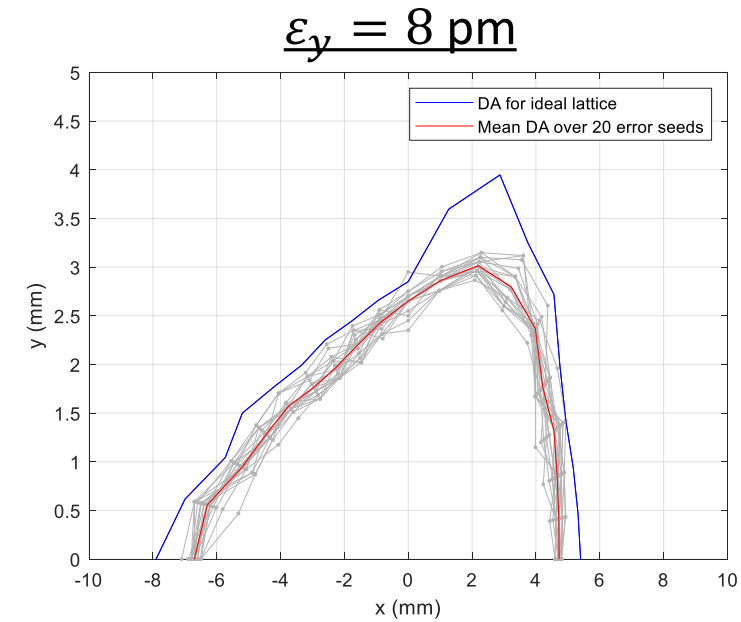
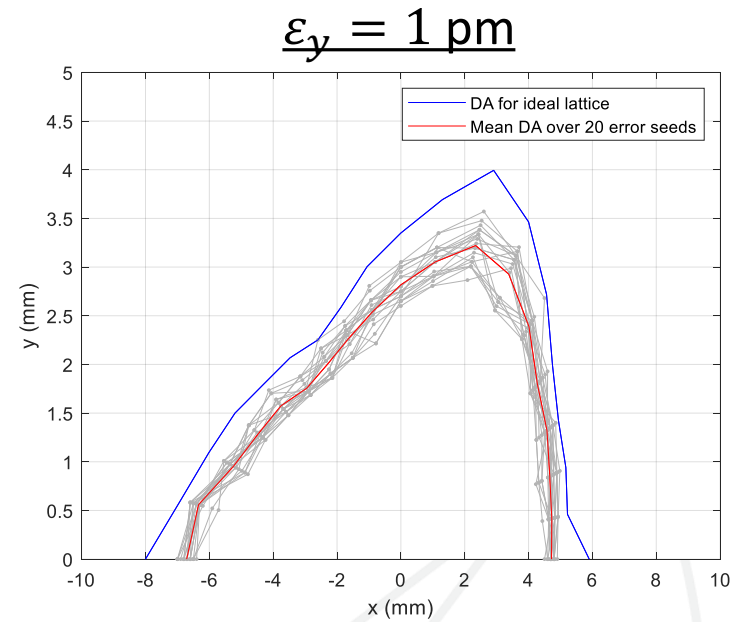
Change in off-diagonal orbit response matrix element for corrector #i due to skew quadrupole #j:

$$\frac{\partial y_k}{\partial \theta_{x,i}} = -(\Delta a_2 L)_j \frac{\sqrt{\beta_{x,i}\beta_{x,j}\beta_{y,j}\beta_{y,k}}}{4 \sin(\pi Q_x) \sin(\pi Q_y)} \cos(\mu_{x,i \rightarrow j} - \pi Q_x) \cos(\mu_{y,j \rightarrow k} - \pi Q_y)$$
$$\frac{\partial x_k}{\partial \theta_{x,i}} = -(\Delta a_2 L)_j \frac{\sqrt{\beta_{y,i}\beta_{y,j}\beta_{x,j}\beta_{x,k}}}{4 \sin(\pi Q_x) \sin(\pi Q_y)} \cos(\mu_{y,i \rightarrow j} - \pi Q_y) \cos(\mu_{x,j \rightarrow k} - \pi Q_x)$$

Vertical Dispersion and Coupling Control using Skew Quads



Vertical Dispersion and Coupling Control using Skew Quads



Vertical Dispersion and Coupling Control using Skew Quads

Seems to work.

Pros:

- Straightforward to implement
- In operation at Diamond for >10 years

Cons:

- Small reduction in dynamic aperture
- Suffers from hysteresis; performance degrades over time
- Can impact off-axis injection if aperture restrictions occur where betatron coupling not controlled
- Cannot stabilise horizontal and vertical emittance simultaneously (due to e.g. ID gap changes)

Emittance Excitation using MBF

Alternative method under investigation using transverse multi-bunch feedback (TMBF) to excite the beam at a synchrotron sideband of the betatron tune

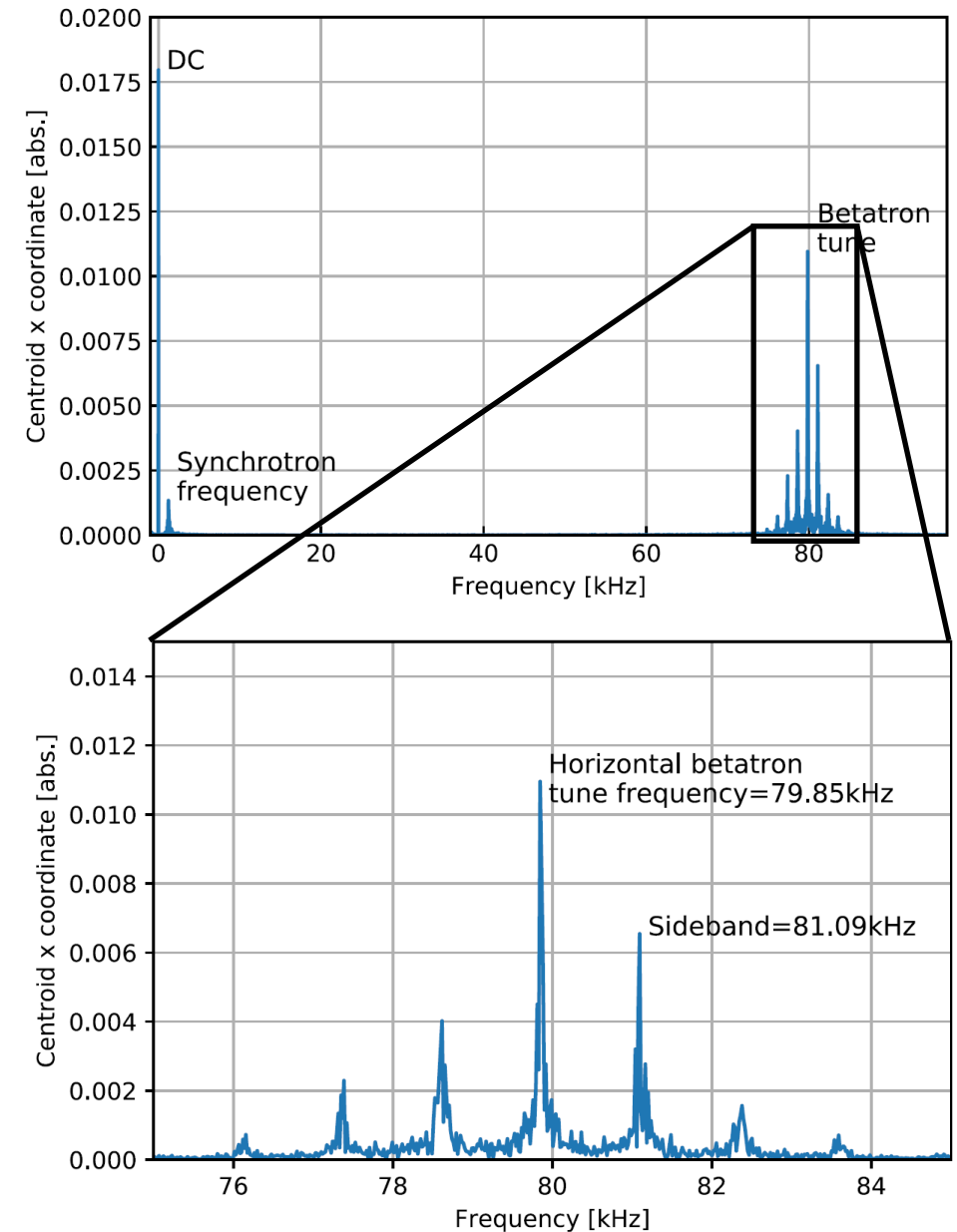
Based on Pulse-Picking by Resonant Excitation (PPRE) method developed at BESSY-II*

- Drives increase in beam size
- Minimises centroid motion

Simulation method for Diamond-II (ELEGANT):

- ILMATRIX + RF cavity + radiation + TMBF kicker
- (tune-shifts with amplitude)
- (higher-order chromaticity)
- (Impedance)
- (Harmonic cavity)

*K Hordack et al., *Nature Communications*, 5, 4010, (2014)



Emittance Excitation for Diamond-II

Linear motion only: Non-zero chromaticity is required to generate the required synchro-betatron coupling

Chromaticity = 0: no increase in vertical beam size. Centroid motion only

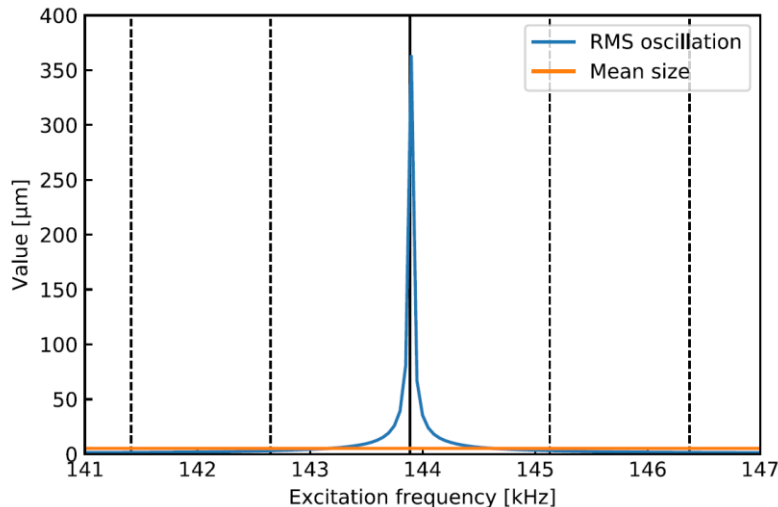
Chromaticity = 1: increase in beam size at side-band with small centroid motion

Chromaticity = 2.3: ratio of beam size growth to centroid motion at sidebands improves

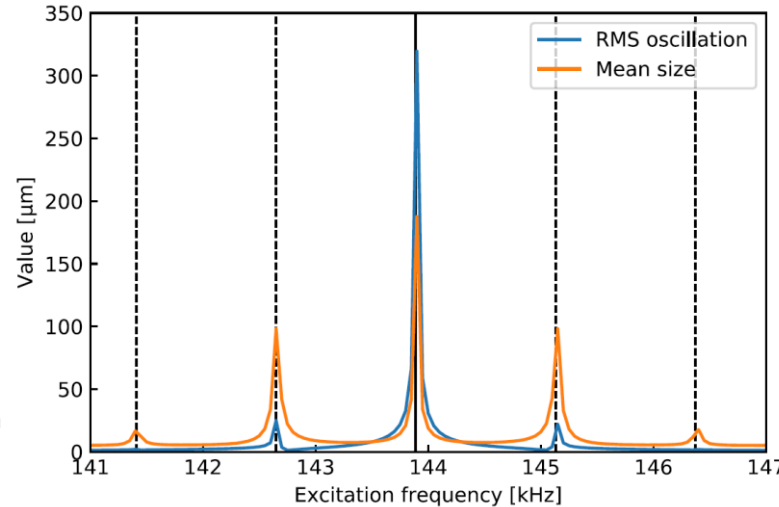
Synchrotron sidebands remain fixed in frequency

Symmetric behaviour for positive and negative sidebands

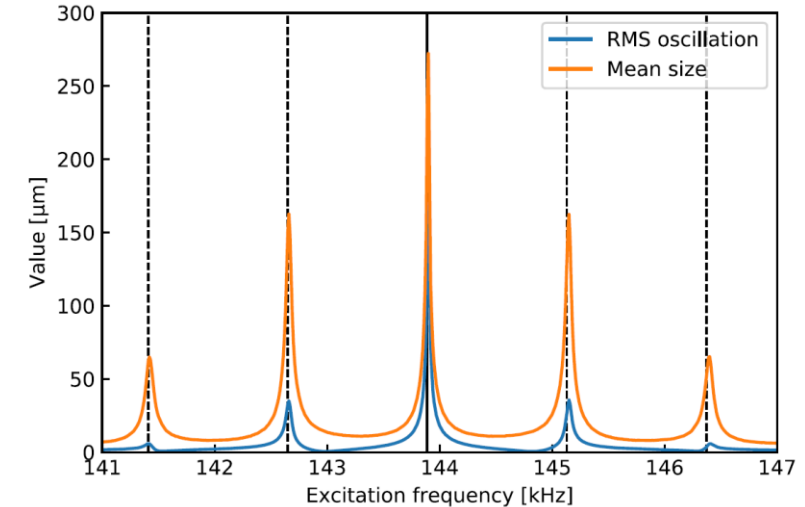
Chromaticity = 0



Chromaticity = 1



Chromaticity = 2.3



Emittance Excitation for Diamond-II

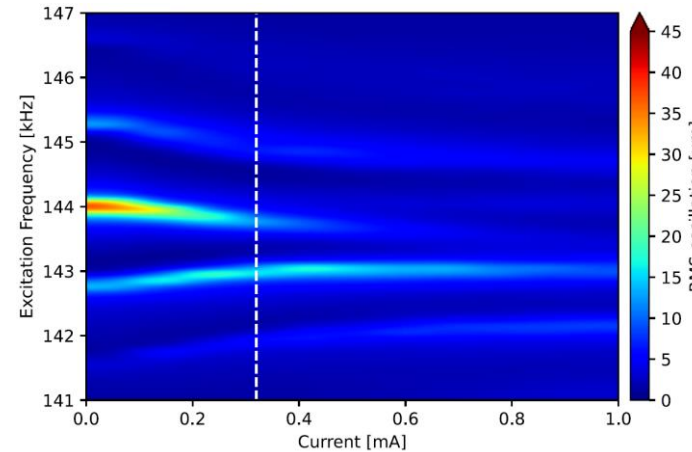
Combined effects:

- Tune shift with amplitude
- Higher order chromaticity
- Transverse impedance
- Longitudinal impedance

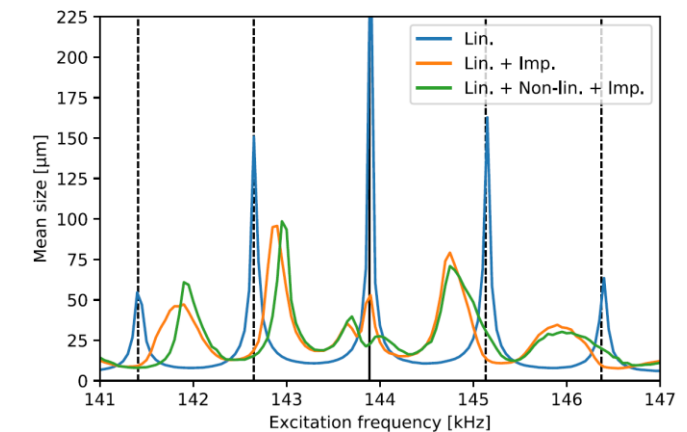
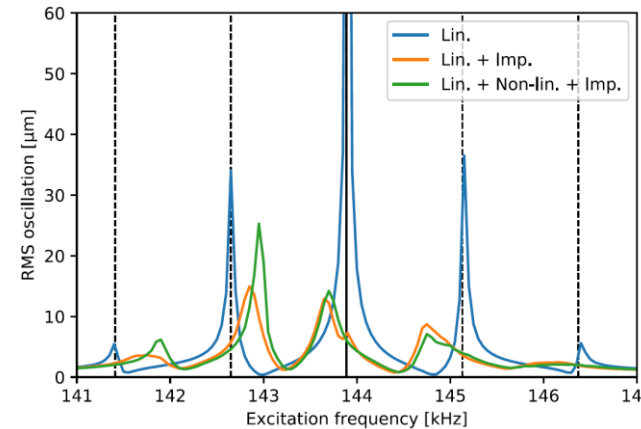
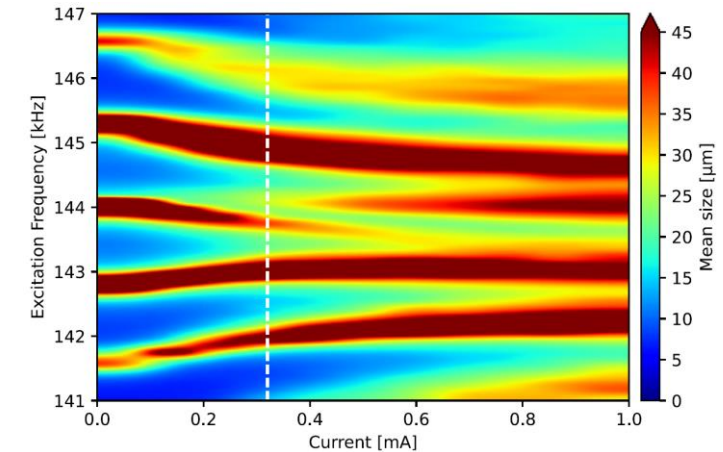
Overall impact:

- Ratio of vertical beam size to centroid motion is reduced, but generally more favourable for upper sidebands
- Upper sidebands: broader and shallower
- Lower sidebands: narrower and taller

Centroid



Vertical Beam Size



Emittance Excitation for Diamond-II

Harmonic cavity set for flat-potential conditions

Impact on bunch motion including all effects:

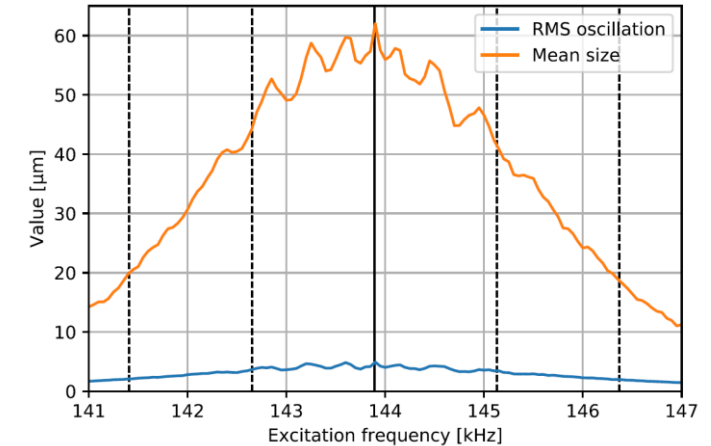
- Synchrotron sidebands broaden and overlap
- Peaks no-longer well-defined
- Achieving exact excitation frequency no longer as significant

Kick strength

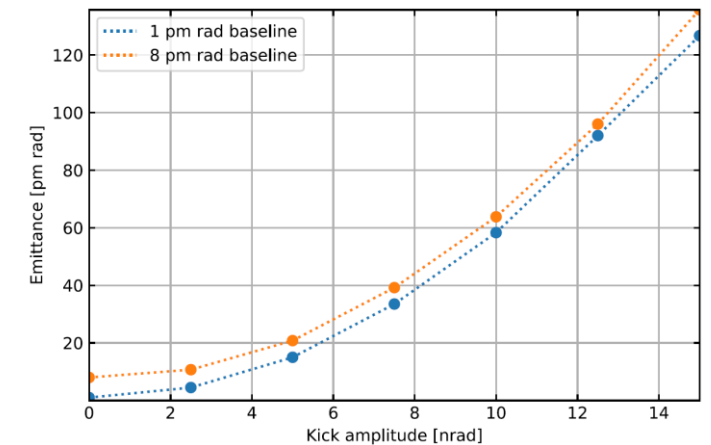
- Quadratic growth in amplitude at small excitation
- Growth becomes more linear and eventually saturates at large excitation due to detuning of the oscillation with amplitude

Assuming ~ 1 pm vertical emittance after LOCO, ~ 3 -4 nrad kicks at the first upper sideband look sufficient to reach target value of 8 pm at standard bunch current (0.3 mA)

Beam size and centroid motion including harmonic cavity

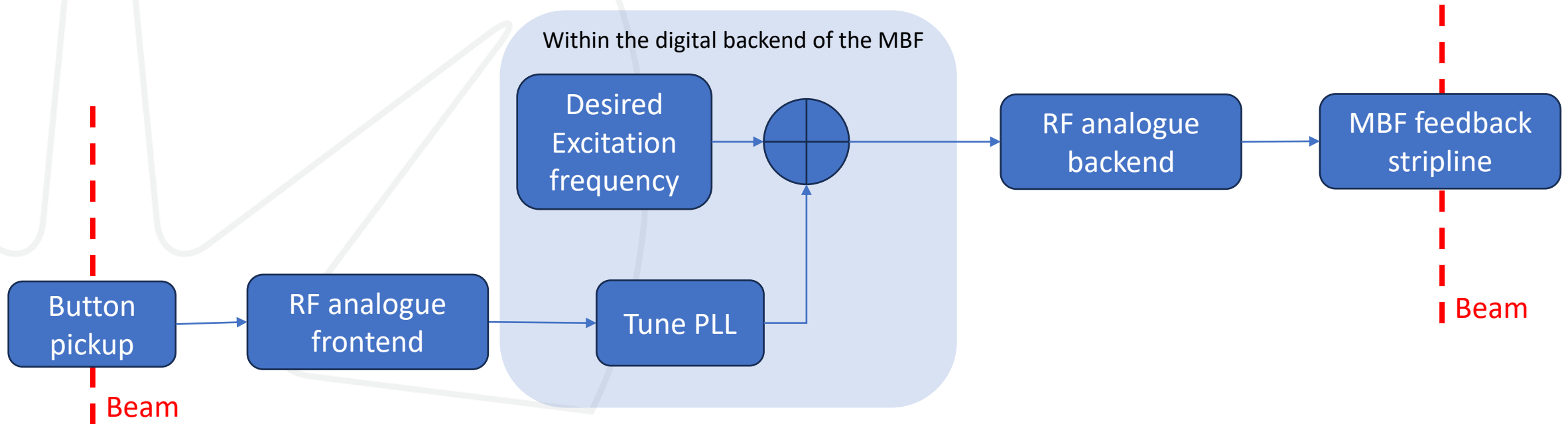


Vertical emittance vs kick strength



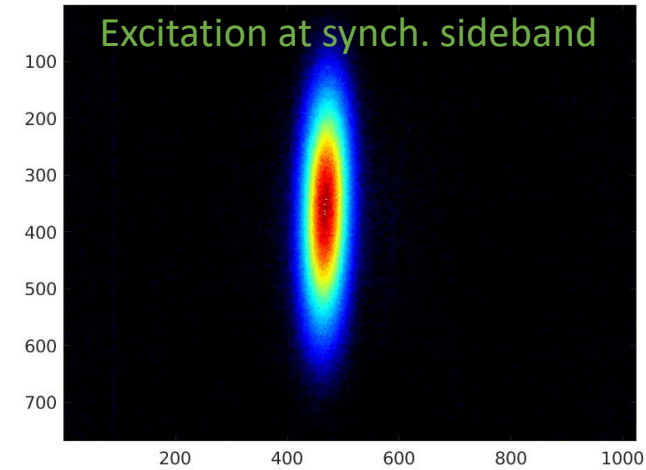
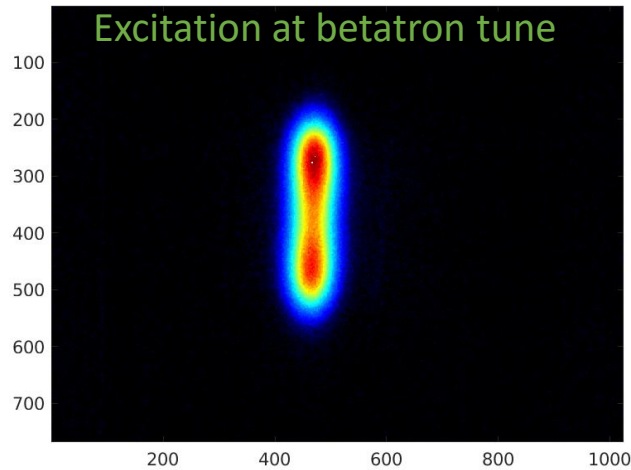
Experimental tests on Diamond

- The excitation is generated using a crystal oscillator at a user defined frequency.
- Phase-locked loop required to track jitter and/or drift in the betatron tune (and hence the sidebands)
 - Keeps excitation at a fixed point of the curve to stabilise excitation amplitude
- Excitation frequency and amplitude can be adjusted to probe the problem space and find optimal settings.
- Excitation can be combined with the signals for standard multi bunch feedback to allow simultaneous use.

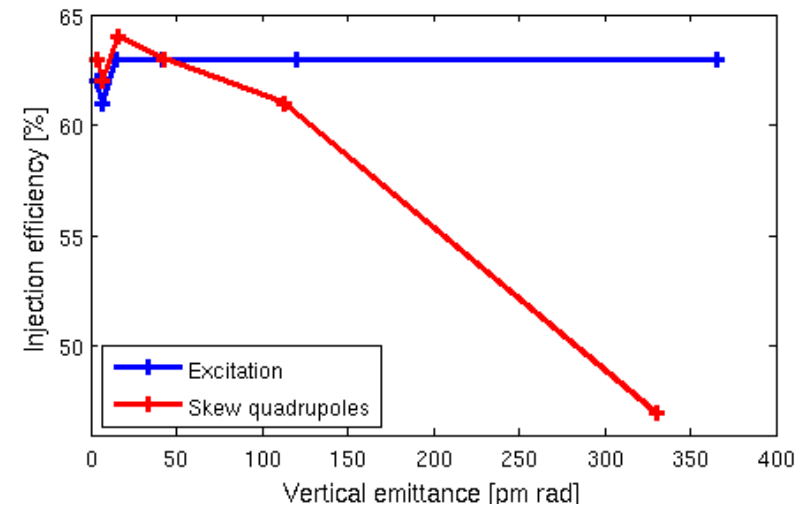
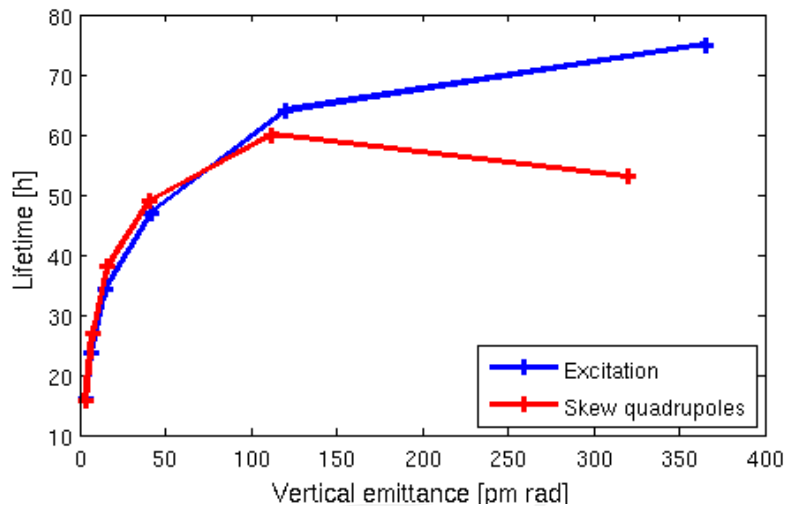


Experimental tests on Diamond

Comparison of beam size using TMBF method: at the betatron tune vs. sideband excitation

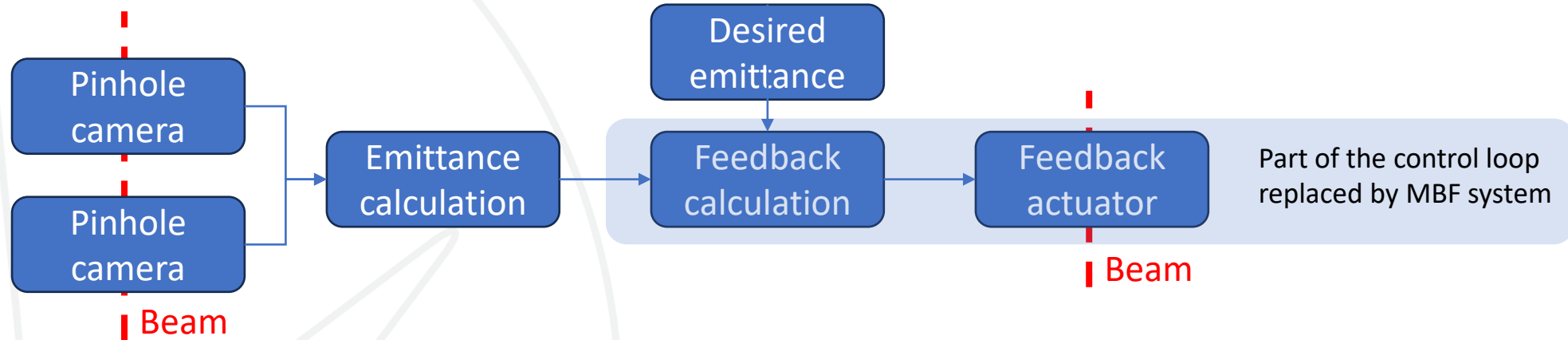


Comparison of lifetime and injection efficiency for different schemes:



Experimental tests on Diamond

- Initial studies on using the TMBF to allow emittance control and stabilisation have been successfully trialled.
- Further work is underway to improve the response of the control loop to insertion device gap changes.



- The emittance was successfully set in both planes and held at user defined values over several hours.
- There are some differences in behaviour which need to be accounted for before it can be used in operation:
 - When feedback switched off, need to leave the machine in the last set state.
 - Control loop needs optimising to account for logarithmic output and excitation step-size

Note: Although the MBF system is faster than using skew-quadrupoles, the overall system response is dominated by the frequency of the camera used to capture the beam sizes.

Conclusions and Future Work

- MBF excitation offers method to control horizontal and vertical emittances independently
- MBF can be controlled to give different excitation to different bunches:
 - how to measure? control bunch lifetime rather than vertical emittance?
- Skew quadrupoles offer alternative method:
 - horizontal and vertical emittances are not independent
 - suffers from magnet hysteresis
 - underlying correction can drift with time affecting off-axis injection

Outstanding questions

- 1) What to do about the hybrid bunch?
 - Response changes with bunch currents due to machine impedance
- 2) Do long range wakes have significant impact on vertical emittance excitation?
- 3) Can MBF effectively suppress residual centroid oscillations?
- 4) What is optimum way of operating with passive harmonic cavity and self-consistent bunch distributions?

Extra Slides

Emittance Excitation for Diamond-II

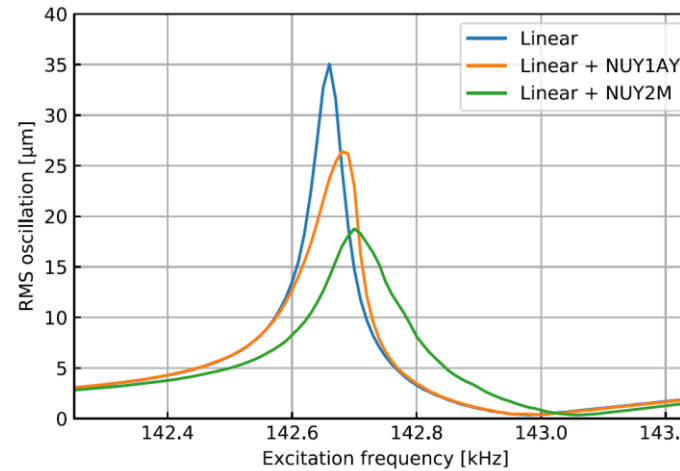
Adding tune-shift with amplitude (NUY1AY):

- Stronger impact on betatron tune peak (where centroid motion is largest)
- Peaks reduce in amplitude, distort, and shift in frequency
- Detuning causes saturation for large excitation amplitudes

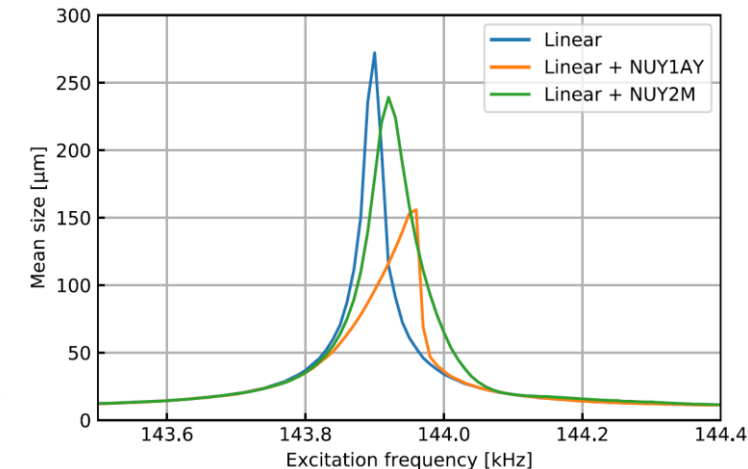
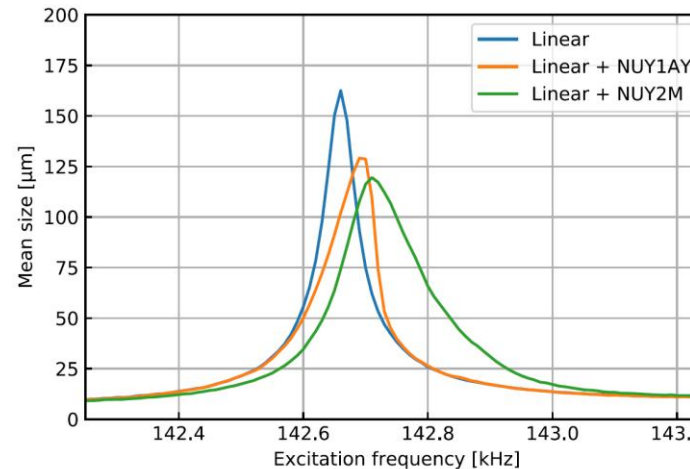
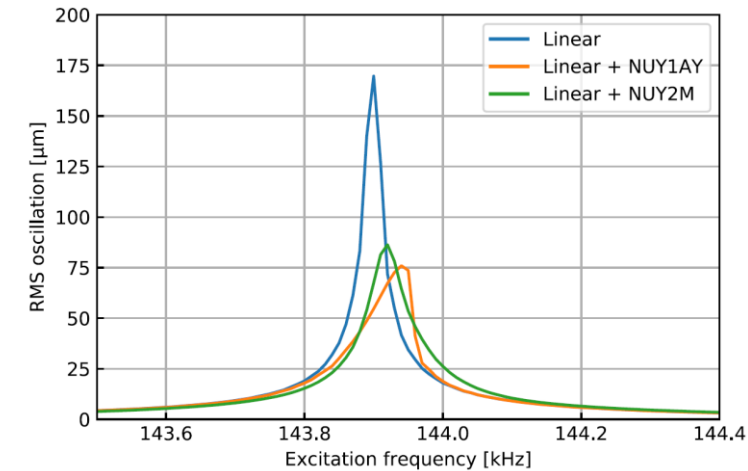
Adding higher-order chromaticity (NUY2M):

- Stronger impact on sidebands
- Peaks reduce in amplitude, broaden, and shift in frequency

Lower sideband



Tune peak



Emittance Excitation for Diamond-II

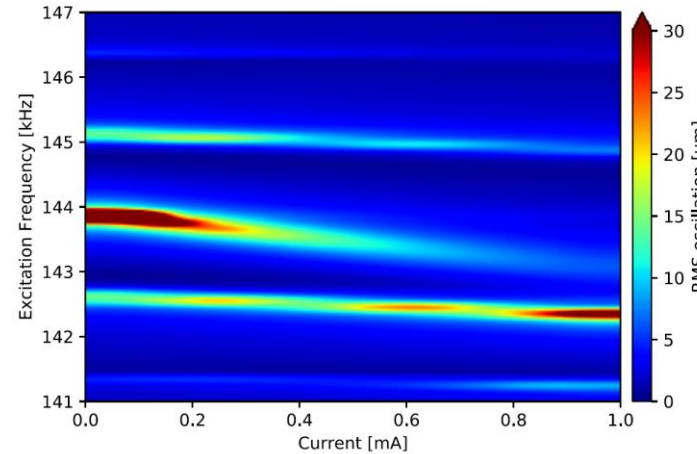
Impact of transverse impedance:

- Amplitudes and widths of peaks shift with bunch current
- Peaks grow with current for lower sidebands and reduce with current for upper sidebands
- Tune peak shifts to lower frequencies
- Peaks at betatron tune are suppressed

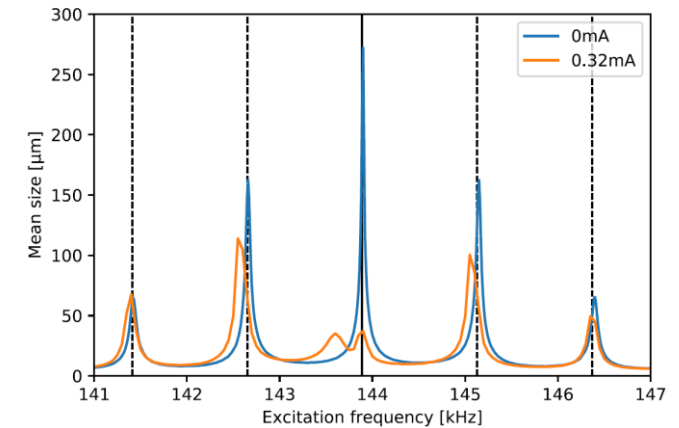
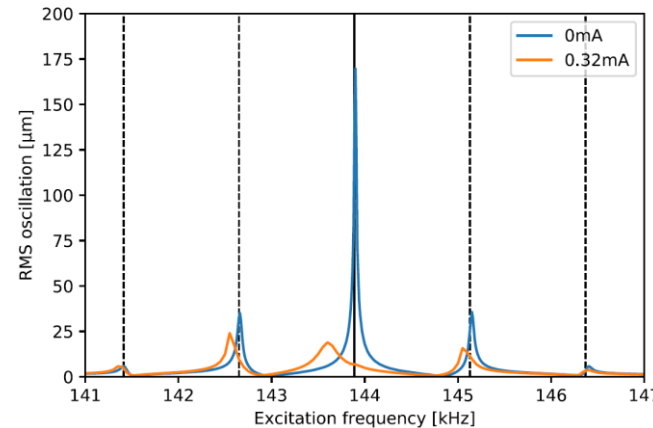
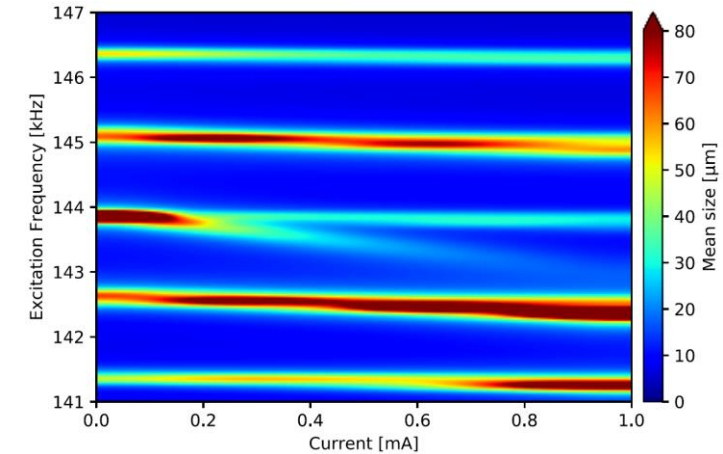
Ratio of beam size increase to centroid motion:

- larger for upper sidebands
- reduces with current

Centroid



Beam Size



Emittance Excitation for Diamond-II

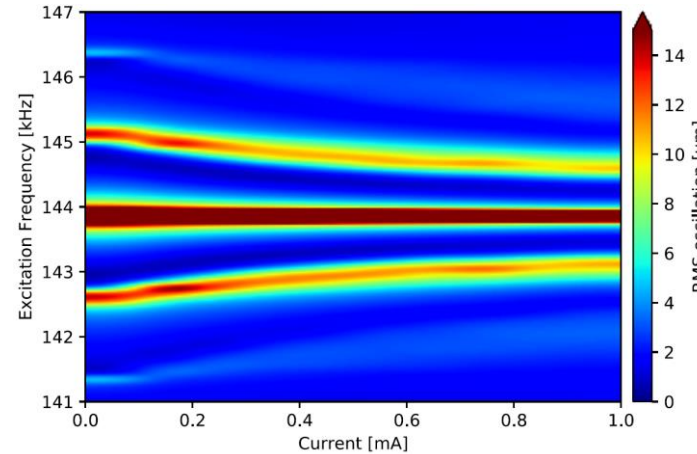
Impact of longitudinal impedance:

- Sidebands shift towards the tune frequency
- Symmetric behaviour for upper and lower sidebands

Change with bunch current:

- Growth in beam size
- Reduction in centroid motion

Centroid



Beam Size

