

Bending Magnet Synchrotron Radiation Imaging with Large Orbital Collection Angles

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iFAST Low Emittance Rings workshop
13th – 16th of February 2024

Outline

- Introduction
- Theoretical calculations for the MAX IV case
- General formula for very large orbital collection angle
- Measurements
- Preparation for measurements at MAX 4-U
- Summary

Introduction

OPTICAL RESOLUTION OF BEAM CROSS-SECTION MEASUREMENTS BY MEANS OF SYNCHROTRON RADIATION

A. HOFMANN and F. MÉOT *

CERN, Geneva, Switzerland

Received 17 February 1982

This paper deals with general theoretical considerations on diffraction and depth of field phenomena involved in the different cases of radiation by relativistic particles in magnetic fields: undulator, (usual) synchrotron, and "short magnet" radiation, and their effects on beam profile image formation. The image formation of extended polychromatic sources is examined. As an example, the beam cross-section imaging at the CERN SPS is given, and the cases of SPS (e^+e^-) and LEP are envisaged.

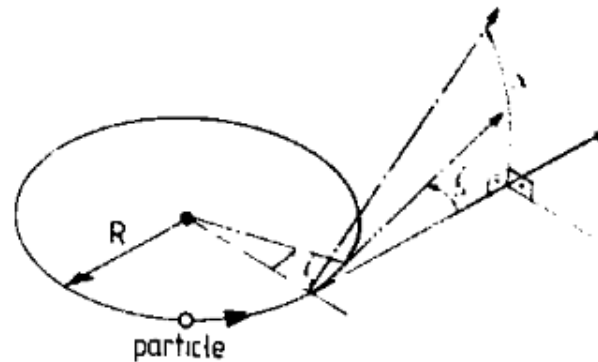
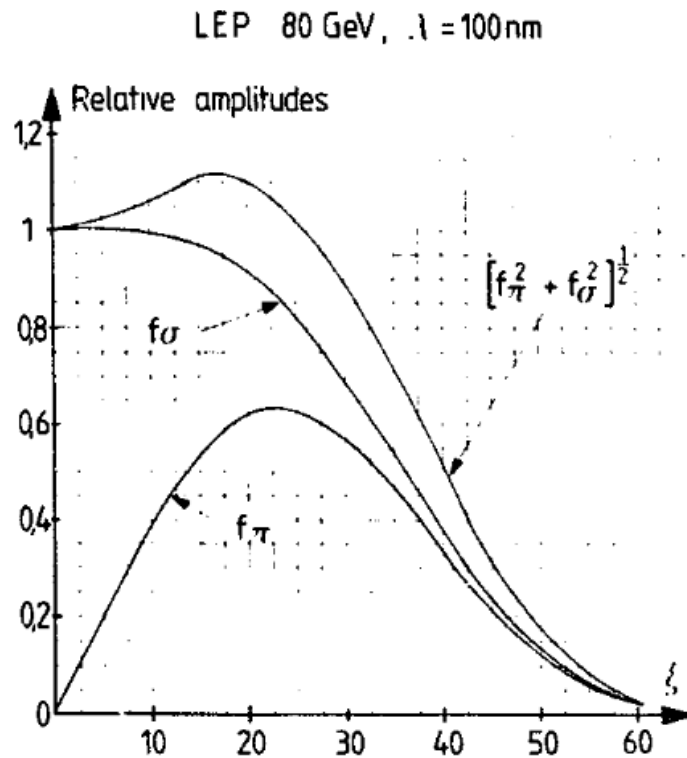


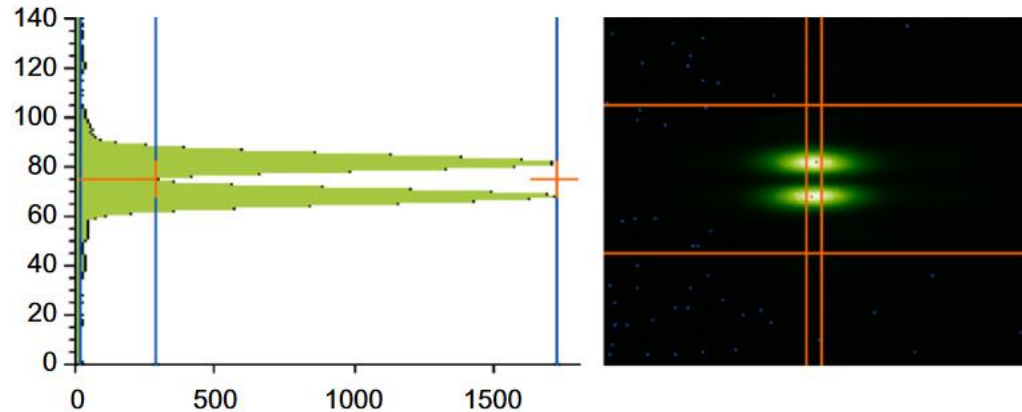
Fig. 4. Coordinates used to describe the synchrotron radiation.

Introduction

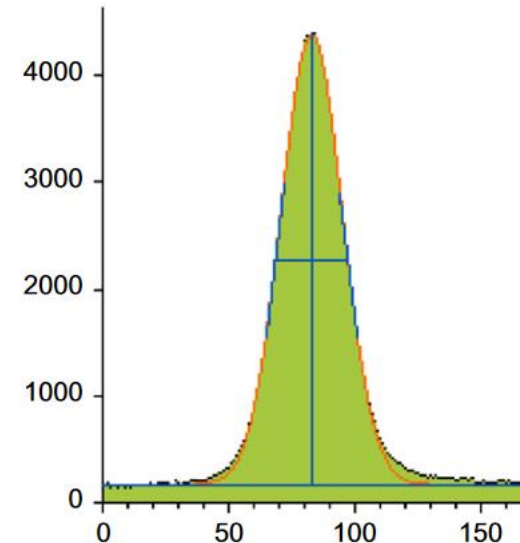
The Π – polarization method:

- Imaging of the SR source.
- Usage of visible or near visible SR.
- The visibility, or Valley to Peak intensity ratio, gives the σ_y
- Introduced as an on-line monitor at Swiss Light Source, in 2007.
- Determines vertical beam sizes down to around 5 μm .
- Best resolution when at largest collection angle in the vertical.
- The natural opening angle of the SR limits the vertical resolution.

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x mid = 0.083 mm
x amp = 4215.7 cts
X sig = 56.86 mic
Y sig = 8.91 mic

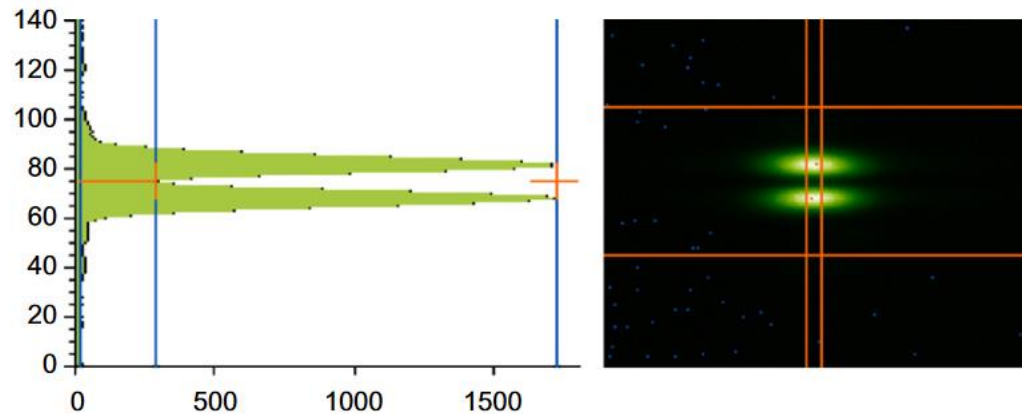


Introduction

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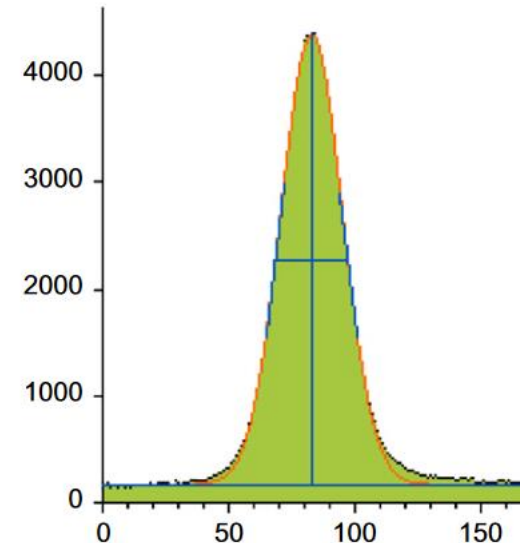
Is there a similar method in the horizontal, when $\sigma_x = 5$ or $10 \mu\text{m}$?

- Is best resolution reached when at largest collection angle in the horizontal?
- Will the horizontal **natural opening angle** of the SR limit the horizontal resolution?



x mid = 0.083 mm
x amp = 4215.7 cts
X sig = 56.86 mic
Y sig = 8.91 mic

4GSR light sources; need to measure 5 to 10 times smaller!



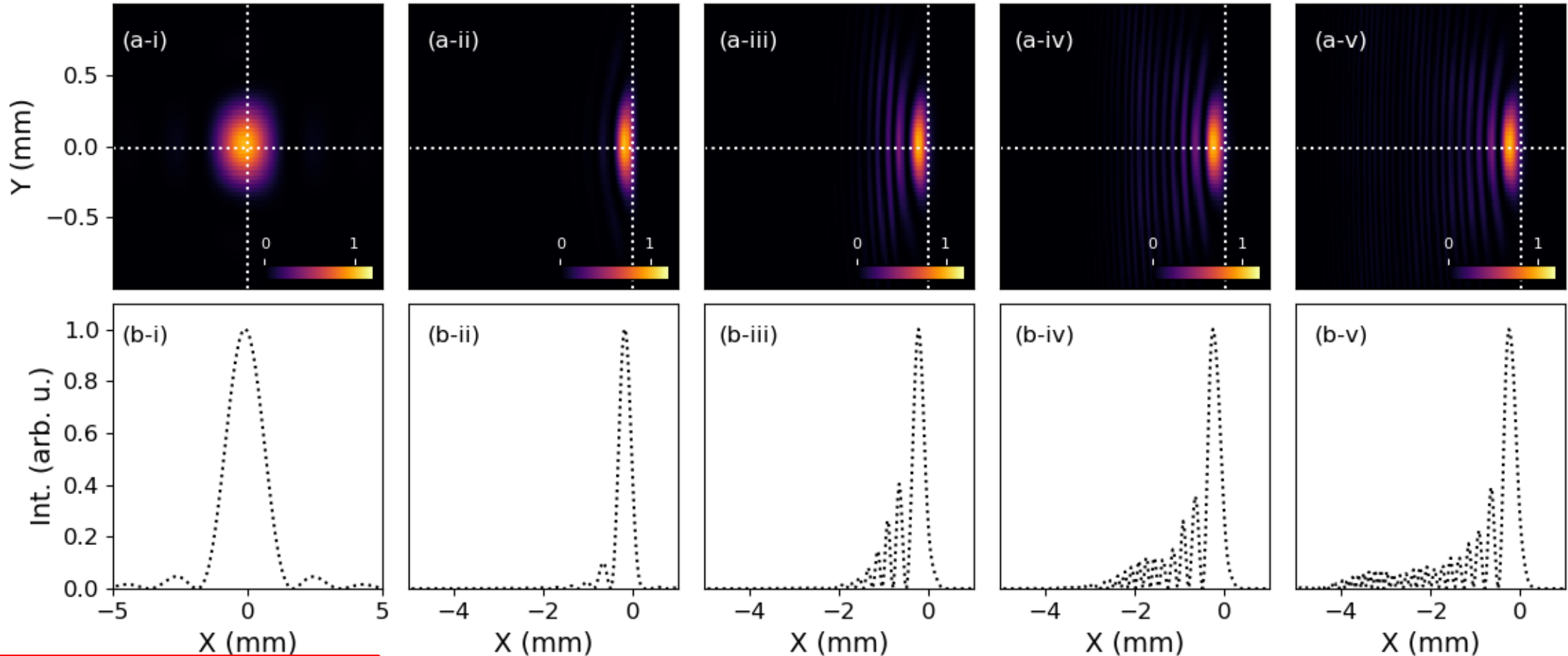
To answer such questions, we joined forces from SOLEIL, NSLS-II and MAX IV

- **Marie Labat** and **Nicolas Hubert** from SOLEIL
- **Oleg Chubar** from NSLS-II
- **Jonas Breunlin** and **Åke Andersson** from MAX-IV

From theory: Image plane **normalized** intensity distributions from a zero-emittance beam, for different $\Delta\theta_x$, using σ -polarized light. $\Delta\theta_y = 7$ mrad

$\lambda = 930$ nm

$\Delta\theta_x =$ 1.6 mrad 9 mrad 15 mrad 20 mrad 25 mrad

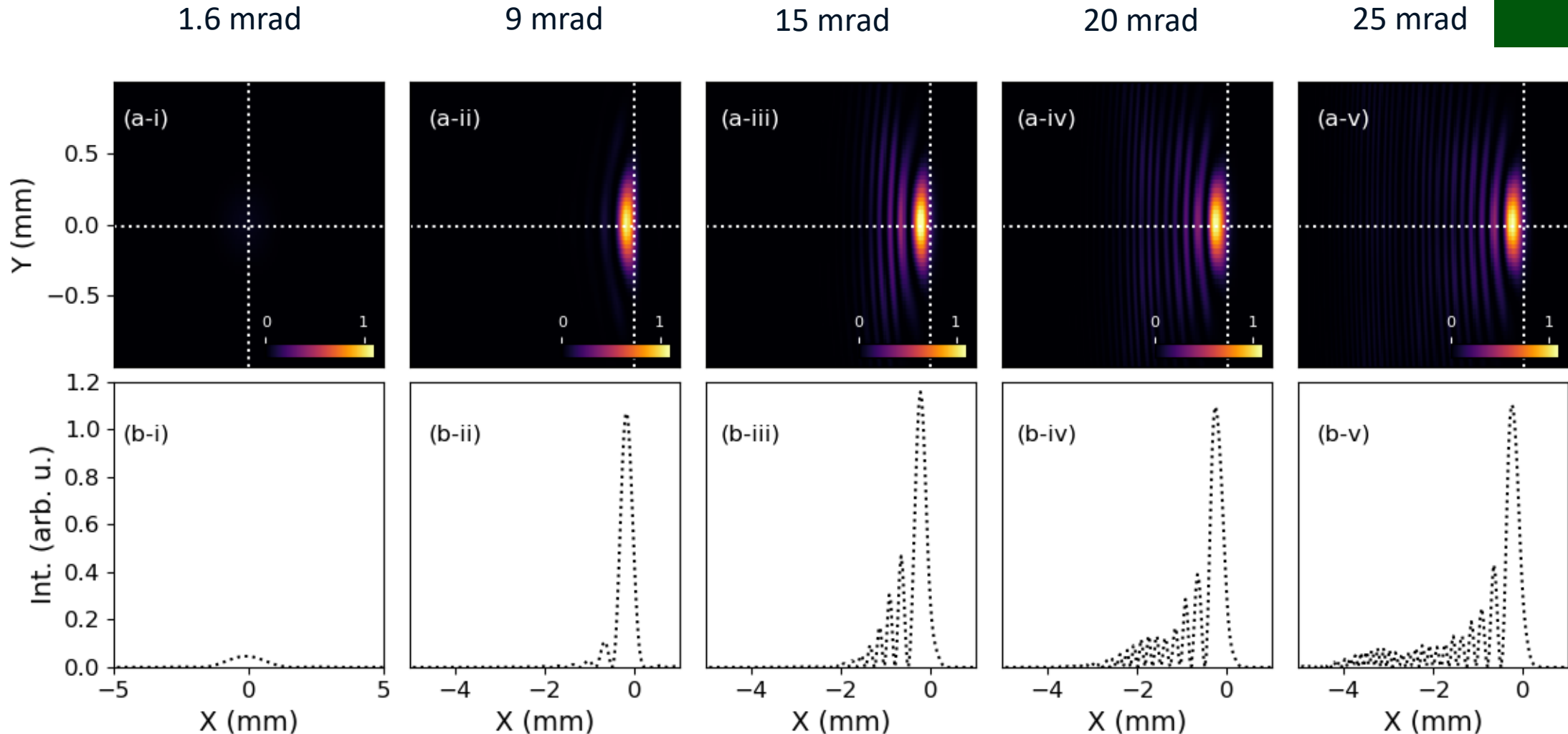


**Diffraction dominated,
Fraunhofer-like**

**Dominated by inherent features of the SR
emission process**

From theory: Image plane **non-normalized** intensity distributions from a zero-emittance beam, for different $\Delta\theta_x$, using σ -polarized light. $\Delta\theta_y = 7$ mrad

$\lambda = 930$ nm

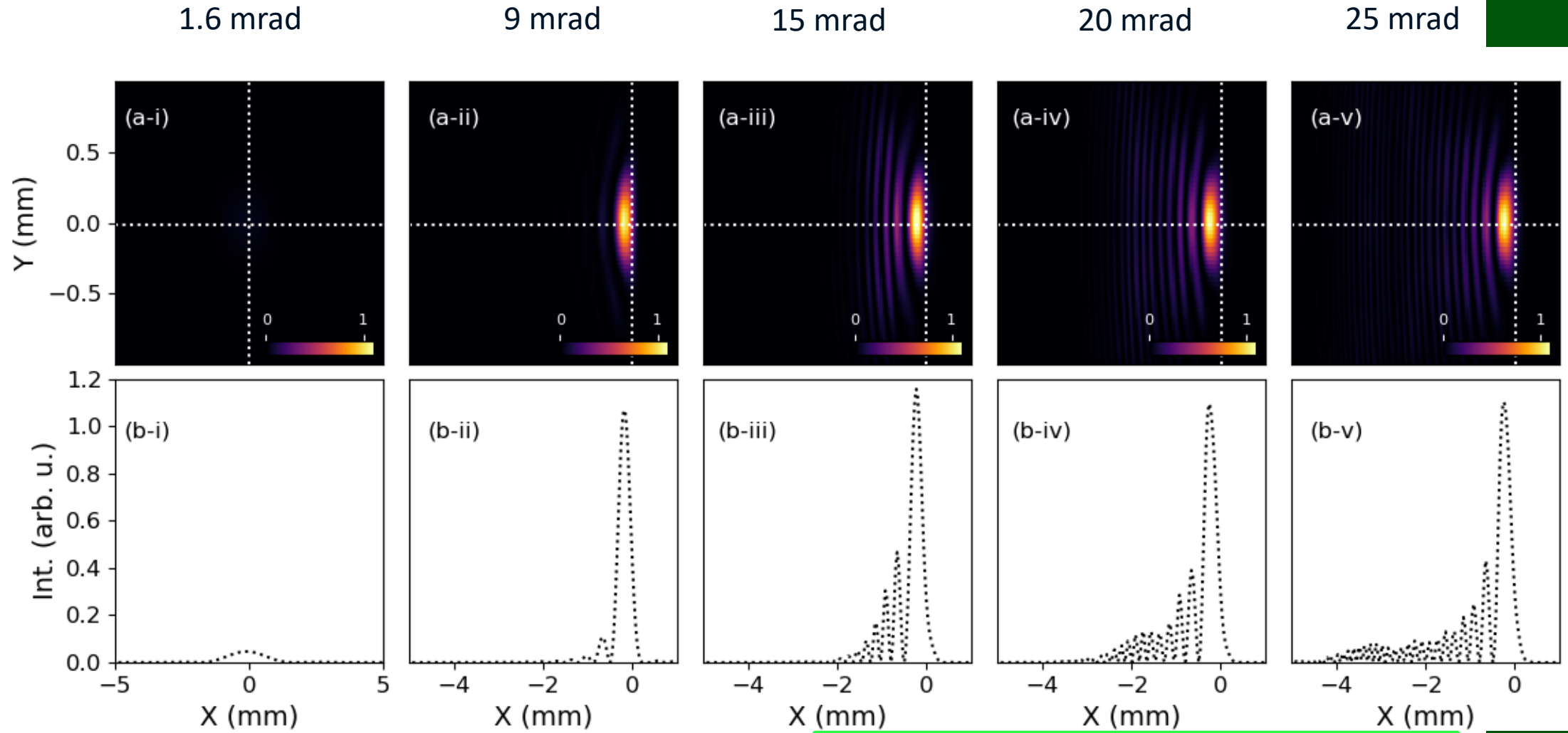


Very low intensity!

No gain in peak intensity by further opening up the collection angle!!

From theory: If we want to explore the visibility of fringes as a measure of the beam size, best resolution possibilities are between 9 and 15 mrad

$\lambda = 930 \text{ nm}$



The SR horizontal natural opening angle does limit further exploration!



Curiosity: The image plane intensity distribution expression, may be simplified, if $\Delta\theta_x$ is very large:

$$E_\sigma(x, y, \lambda) = -\frac{4i\pi^{4/3}e\rho^{1/3}}{c\lambda^{4/3}} \times \int_{\Delta\theta_y} \text{Ai}' \left[\left(\frac{\pi\rho}{\lambda} \right)^{2/3} (\gamma^{-2} + \theta_y^2) \right] \exp \left(\frac{2\pi iy}{\lambda} \theta_y \right) \times \int_{\Delta\theta_x} \exp \left[\frac{i\pi\rho\theta_x}{\lambda} (\gamma^{-2} + \theta_x^2/3 + \theta_y^2) + \frac{2\pi ix}{\lambda} \theta_x \right] \times d\theta_x d\theta_y, \quad (1)$$

$\Delta\theta_x$ large



$$I_\sigma(x, y, \lambda) \propto |E_\sigma(x, y, \lambda)|^2 \propto \left| \int_{\Delta\theta_y} \text{Ai}' \left[\left(\frac{\pi\rho}{\lambda} \right)^{2/3} (\gamma^{-2} + \theta_y^2) \right] \exp \left(\frac{2\pi iy}{\lambda} \theta_y \right) \times \text{Ai} \left[2^{1/3} \frac{(\gamma^{-2} + \theta_y^2)\rho/2 + x}{\rho^{1/3}(\lambda/(2\pi))^{2/3}} \right] d\theta_y \right|^2. \quad (3)$$

$$I_\sigma(x, y, \lambda) = \frac{c^2\alpha I}{4\pi^2 e^3} |E_\sigma(x, y, \lambda)|^2, \quad (2)$$

Details in:

Bending Magnet Synchrotron Radiation Imaging with Large Orbital Collection Angles

M. Labat^{1,*}, O. Chubar,² J. Breunlin,³ N. Hubert,¹ and Å. Andersson³

¹Synchrotron SOLEIL, L'Orme des Merisiers, 91 190 Saint-Aubin, France

²Brookhaven National Laboratory, Building 741, P.O. Box 5000, Upton, New York 11973-5000, USA

³MAX IV Laboratory, P.O. Box 118, SE-221 00 Lund, Sweden

Measurements at MAX-IV:

Intensities are in log-scales
for easier comparison to
theory.

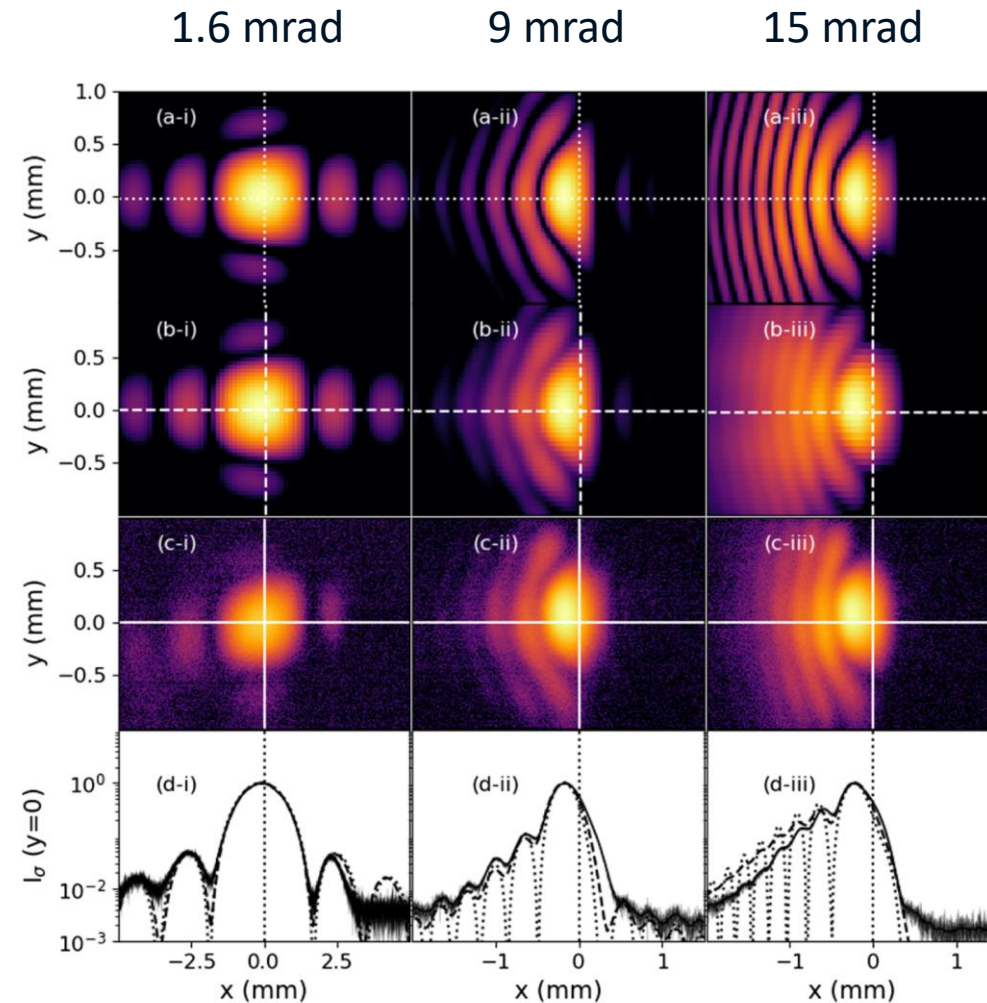
Theory
Zero emittance

Theory (SRW)
 $\epsilon_x = 336$ pmrad

Measured!

Measurements were done at 3
mA, where design $\epsilon_x = 328$ pmrad
Best fit for the 9 mrad case was ϵ_x
 $= 336$ pmrad

Details in:



$\lambda = 930$ nm

Bending Magnet Synchrotron Radiation Imaging with Large Orbital Collection Angles

M. Labat^{1,*}, O. Chubar², J. Breunlin³, N. Hubert¹, and Å. Andersson³

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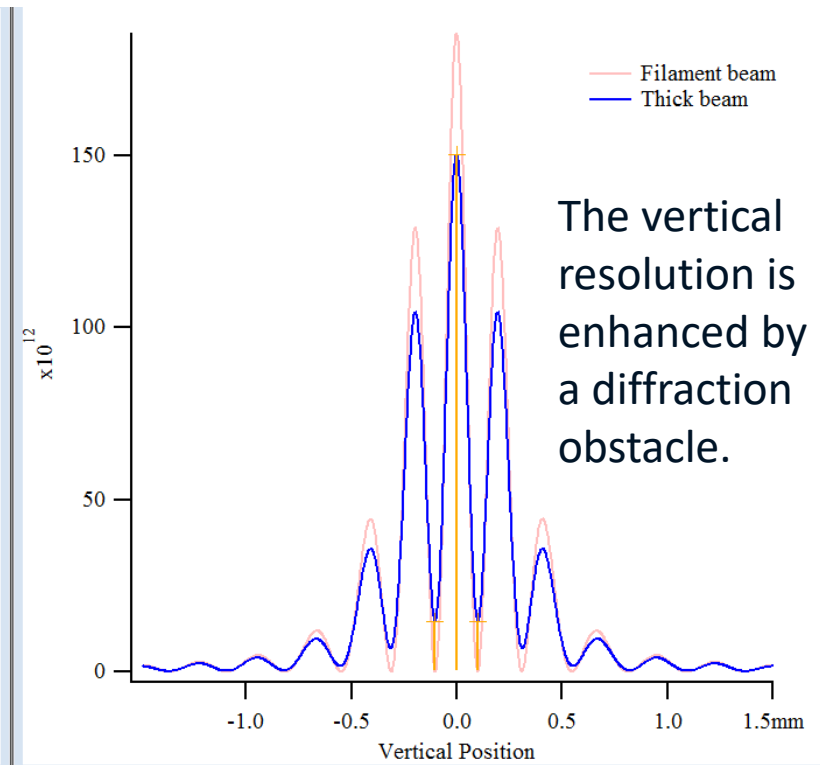
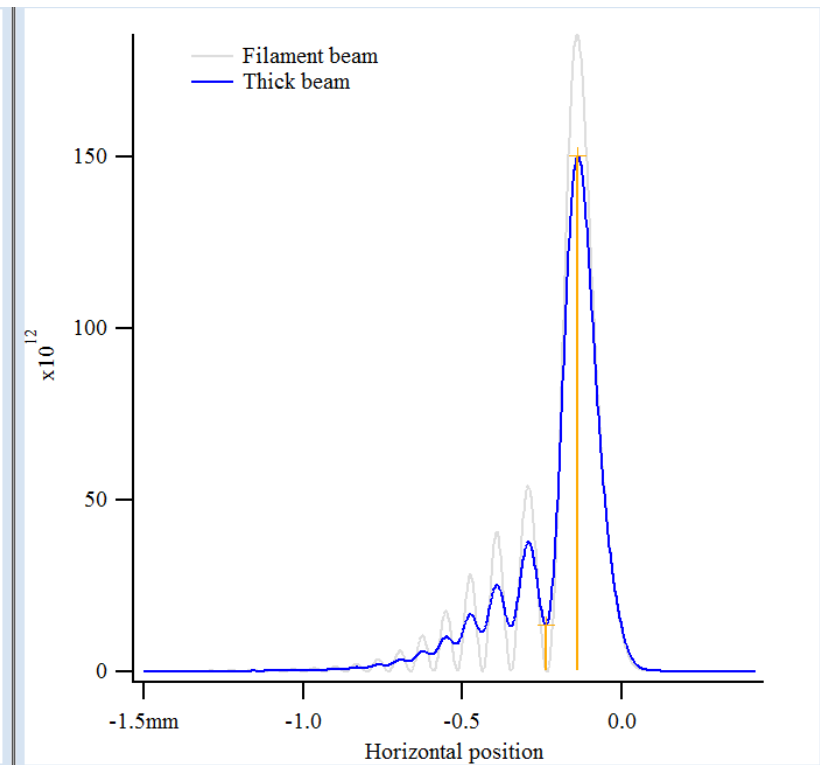
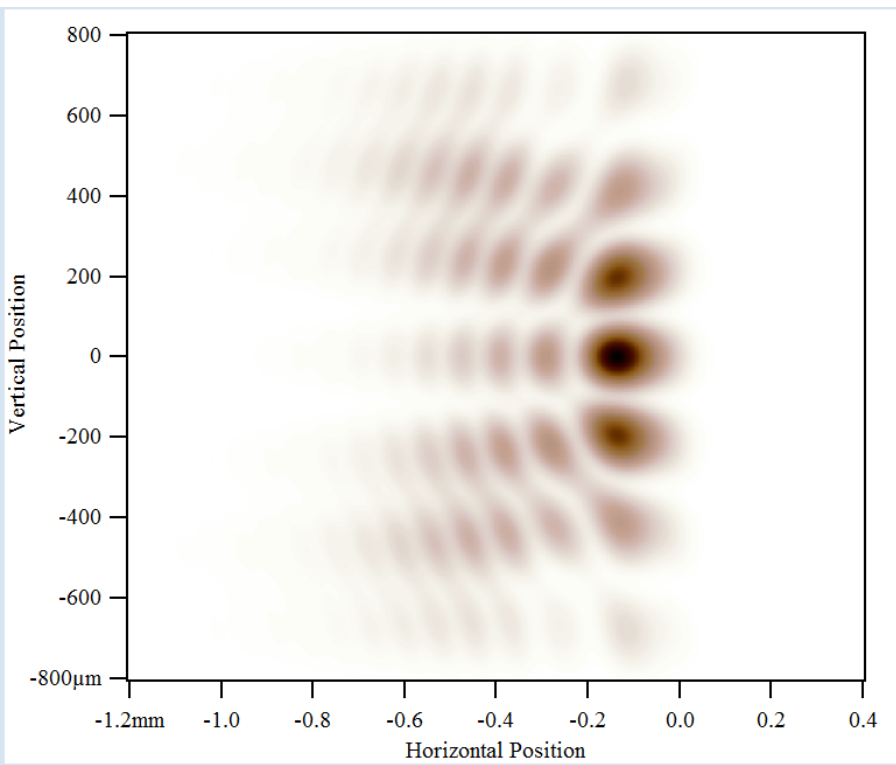
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Preparation for measurements at MAX 4-U:

Assuming
 $\sigma_x = \sigma_y = 10 \mu\text{m}$

Here we use $\lambda = 365 \text{ nm}$, $\Delta\theta_x = 12 \text{ mrad}$, σ -pol light



Summary

- Imaging bending magnet SR with a rather large orbital collection angle, seems to provide a viable method for determining small horizontal beam sizes.
- The image contains an asymmetric fringe pattern, that is diluted to a certain degree, for a given finite beam size.

We had great fun during our collaboration!!!

- Marie Labat and Nicolas Hubert from **SOLEIL**
- Oleg Chubar from **NSLS-II**
- Jonas Breunlin and Åke Andersson from **MAX-IV**

*We all,
Thank You for listening!!!*

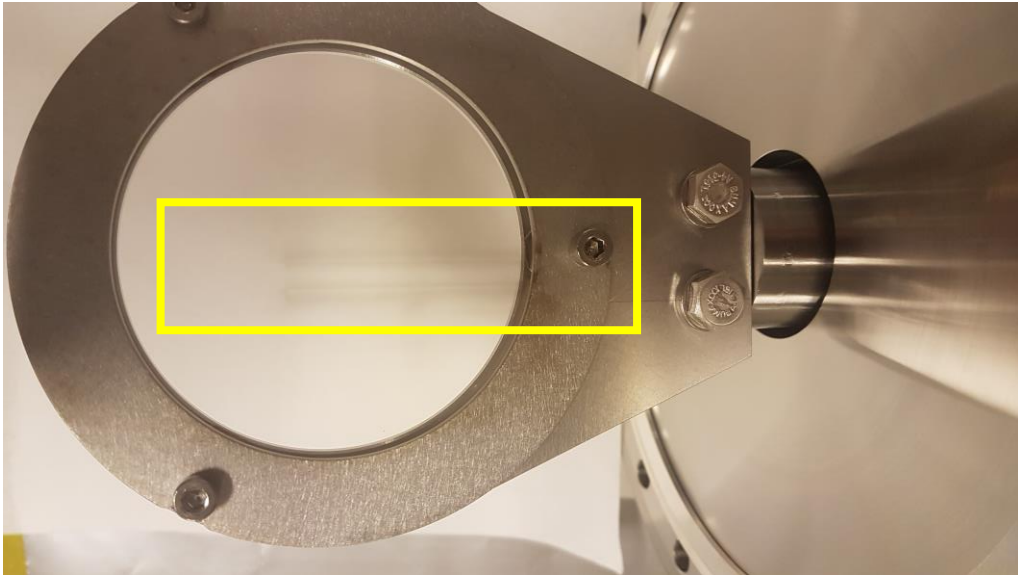
Backup slides

Emittance monitors, for future low emittance lattices

At MAX-IV : Beam size diagnostics in the Visible, or Near-Visible spectral range. => Interpret SR emission effects.

➤ Many advantages, but one must **avoid bad optical components and possible degradation!**

➤ **“Sacrificial optics”** for reduced impact by carbon deposition. The deposition is mainly on our lens.



➤ **“Monochromatisation”** is always **delicate**. Multilayer colour filters often affect the wavefront => Back to basics: Use spatial separation with **Prism**.

