

Dip-bump structures in pp elastic scattering and single diffractive dissociation

István Szanyi

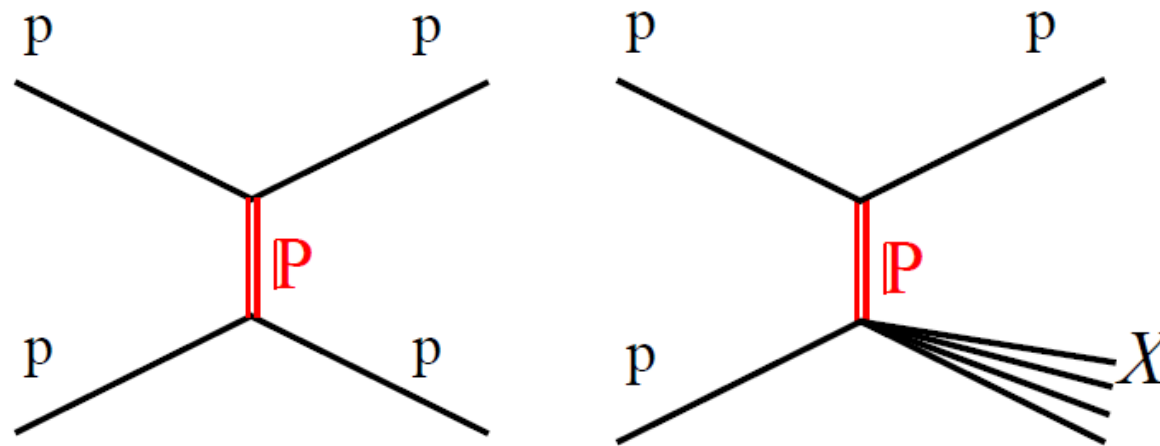
in collaboration with László Jenkovszky

EMMI Workshop

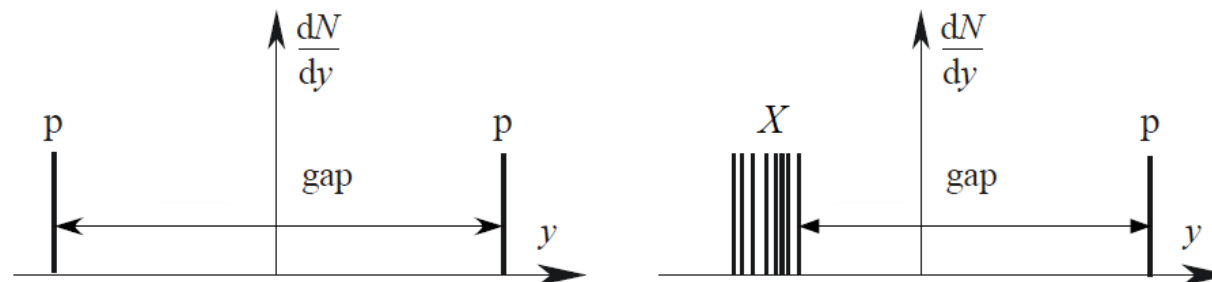
Forward Physics in ALICE 3

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Elastic pp scattering and single diffractive dissociation



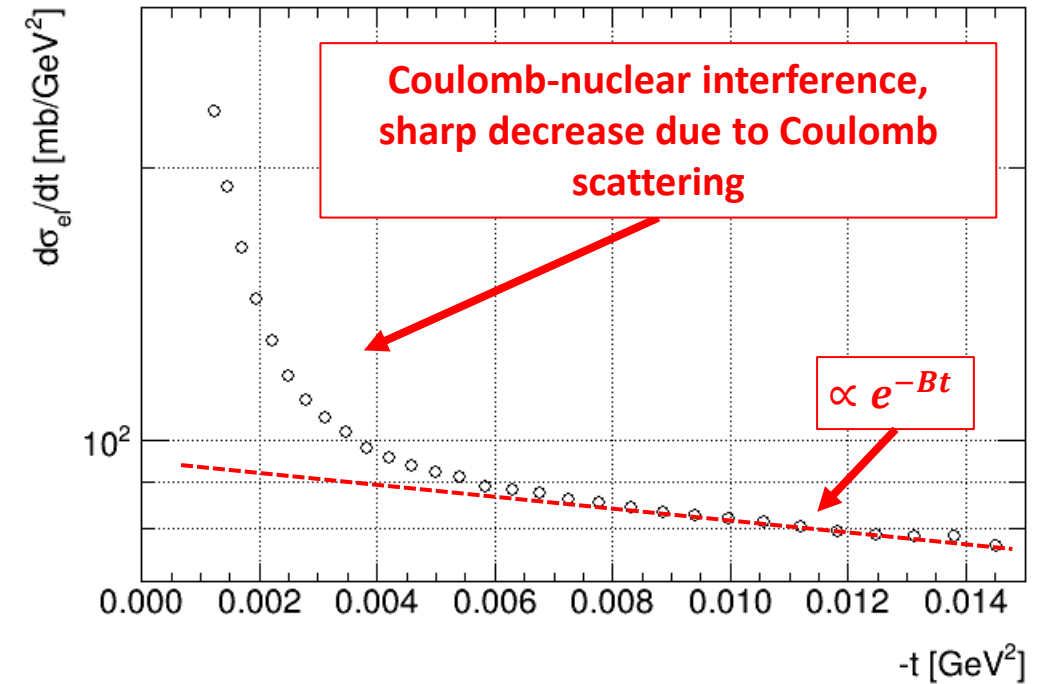
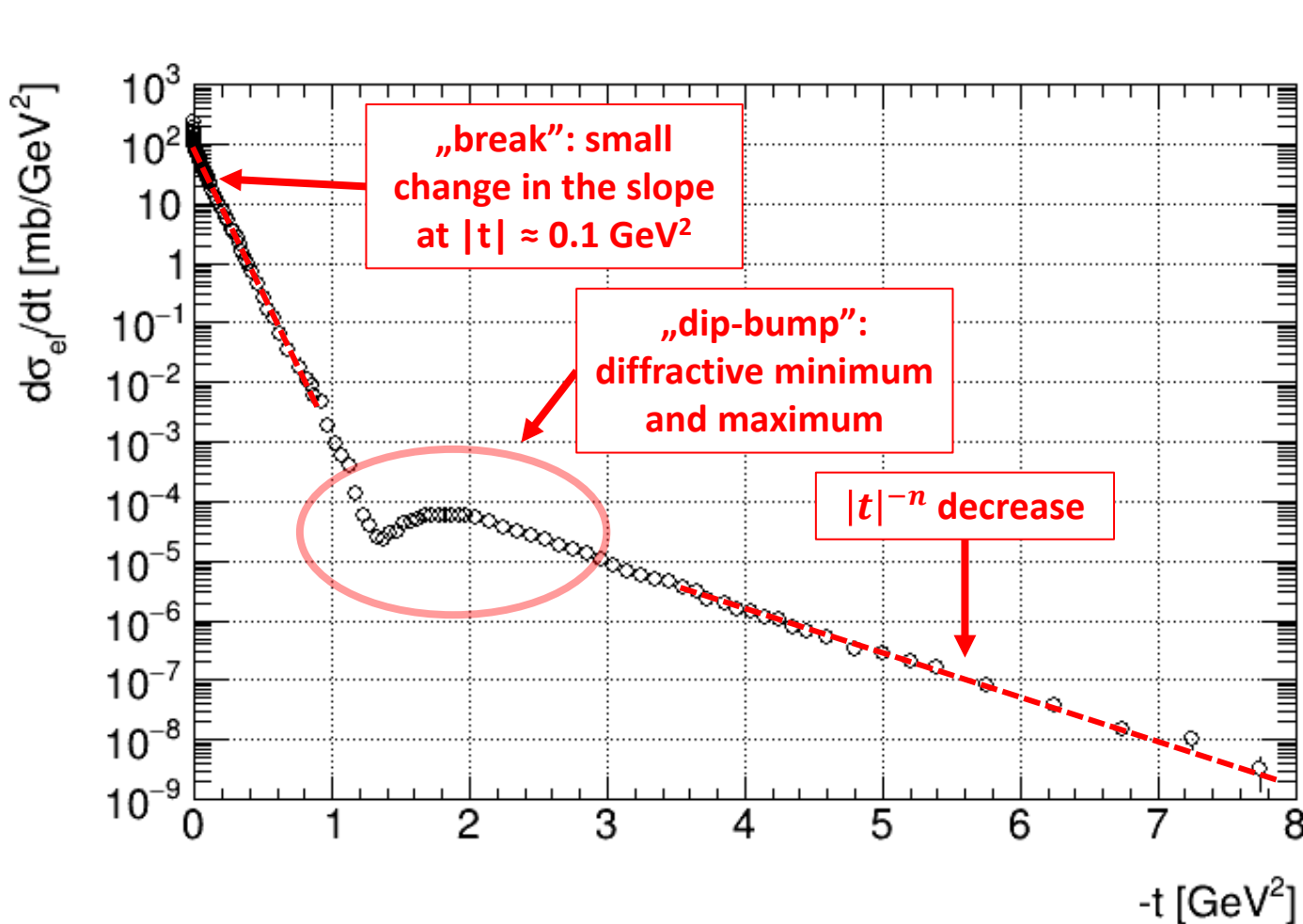
Leading order Pomeron exchange graph contributing to pp elastic scattering and to pp single diffractive dissociation



Schematic rapidity distribution of outgoing particles in pp elastic scattering and in pp single diffractive dissociation

Structures in elastic pp differential cross section

- measurements at CERN ISR in the 1970s revealed the characteristic structures of the high energy elastic pp differential cross section

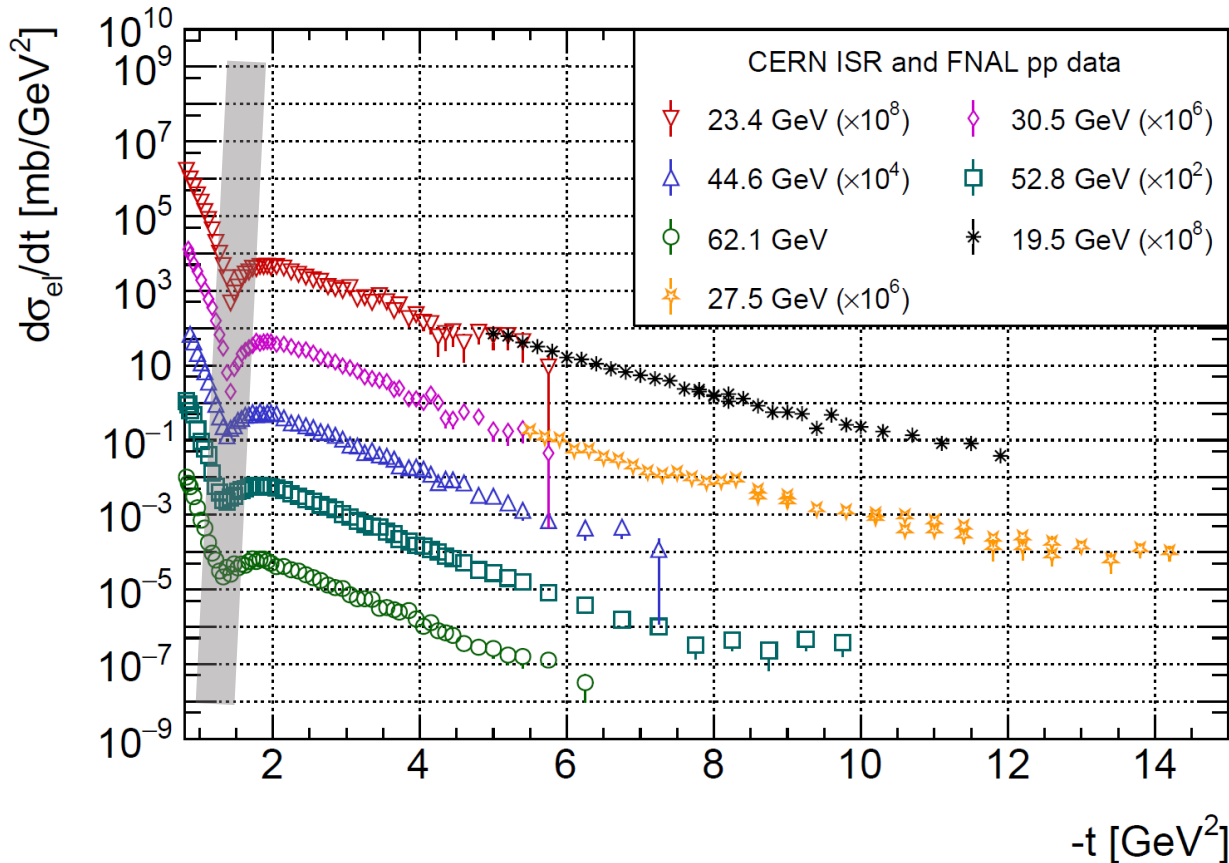


Elastic pp differential cross section measured at CERN ISR at $\sqrt{s} = 53.8$ GeV

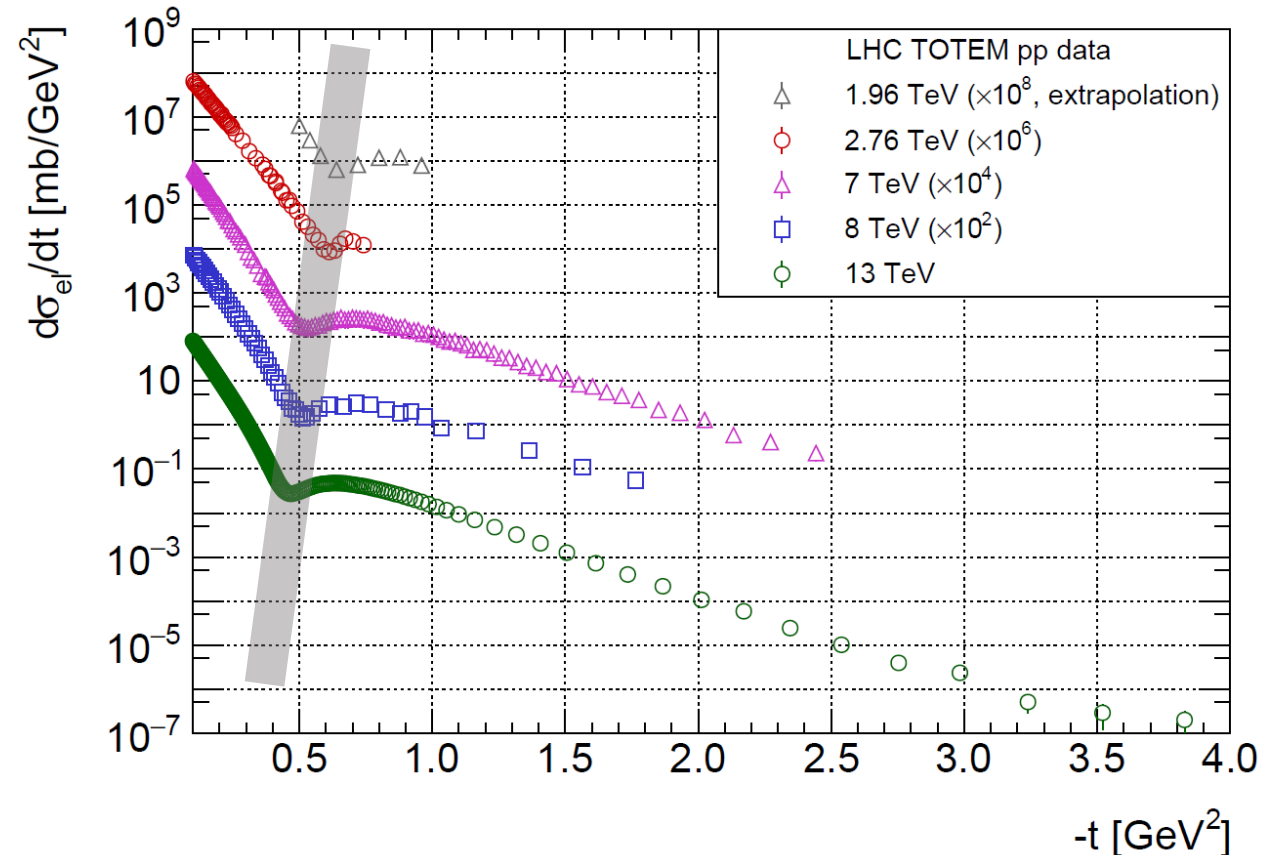
Elastic pp $d\sigma_{el}/dt$ measurements at medium and high $|t|$

E. Nagy et al., Nucl. Phys. B 150, 221 (1979)
 W. Faissler et al., Phys. Rev. D 23, 33 (1981)

TOTEM Collab., EPL 95:4, 41001 (2011)
 TOTEM Collab., Eur. Phys. J. C 79:10, 861 (2019)
 TOTEM Collab., Eur. Phys. J. C 80:2, 91 (2020)
 TOTEM Collab., Eur. Phys. J. C 82:3, 263 (2022)
 TOTEM & D0 Collabs., Phys. Rev. Lett. 127:6, 062003



the position of the dip and the bump moves to lower $|t|$ values as the CM energy increases



no secondary dip-bump structures are observed in the $|t|$ range measured up to now

- basic assumptions:
 - the asymptotic behaviour of the scattering amplitude $A(s, t)$ is determined by an isolated j -plane pole of the second order (dipole)
 - the residue at the pole is independent of t , t -dependence enters only through the trajectory
- the partial wave amplitude is obtained as a derivative of a simple pole:

$$a_j(t) \equiv a(j, t) = \frac{d}{d\alpha(t)} \left[\frac{\beta(j)}{j - \alpha(t)} \right] = \frac{\beta(j)}{[j - \alpha(t)]^2}$$

- the dipole scattering amplitude is obtained as a derivative of a simple pole scattering amplitude:

$$A^{\text{DP}}(s, \alpha) = \frac{d}{d\alpha} A^{\text{SP}}(s, \alpha) = e^{-\frac{i\pi\alpha}{2}} \left(\frac{s}{s_0} \right)^\alpha \left[G'(\alpha) + \left(L - \frac{i\pi}{2} \right) G(\alpha) \right]$$

$$A^{\text{SP}}(s, \alpha) = e^{-\frac{i\pi\alpha}{2}} G(\alpha) \left(\frac{s}{s_0} \right)^\alpha$$

$$\alpha = \alpha(t)$$

$$L \equiv \ln \frac{s}{s_0}$$

$$A^{\text{DP}}(s, \alpha) = e^{-\frac{i\pi\alpha}{2}} \left(\frac{s}{s_0}\right)^\alpha \left[G'(\alpha) + \left(L - \frac{i\pi}{2}\right) G(\alpha) \right]$$

- motivated by the shape of the diffraction cone (exponential decrease), the parameterization of $G'(\alpha)$ is:

$$G'(\alpha) = a e^{b[\alpha-1]}$$

- $G(\alpha)$ is obtained by integrating $G'(\alpha)$:

$$G(\alpha) = \int G'(\alpha) d\alpha = a \left(\frac{e^{b[\alpha-1]}}{b} - \gamma \right)$$

- introducing that $\varepsilon = \gamma b$ the amplitude can be rewritten as:

$$A^{\text{DP}}(s, t) = i \frac{a}{b} \left(\frac{s}{s_0}\right)^{\alpha(t=0)} e^{-\frac{i\pi}{2}(\alpha(t=0)-1)} \left[r_1^2(s) e^{r_1^2(s)[\alpha(t)-1]} - \varepsilon r_2^2(s) e^{r_2^2(s)[\alpha(t)-1]} \right]$$

$$r_1^2(s) = b + L(s) - i\pi/2$$

$$r_2^2(s) = L(s) - i\pi/2$$

Model for elastic pp and $\bar{p}p$ scattering amplitude

$$A(s, t)_{pp}^{\bar{p}p} = A_P^{DP}(s, t) + A_f^{SP}(s, t) \pm [A_O^{DP}(s, t) + A_\omega^{SP}(s, t)]$$

- the dipole pomeron and odderon amplitudes are:

$$A_P^{DP}(s, t) = e^{-\frac{i\pi\alpha_P(t)}{2}} \left(\frac{s}{s_{0P}}\right)^{\alpha_P} \left[G'_P(t) + \left(L_P(s) - \frac{i\pi}{2} \right) G_P(t) \right]$$

$$A_O^{DP}(s, t) = -iA_{P \rightarrow O}^{DP}(s, t)$$

(with free parameters labeled by "O")

$$G'_P(t) = a_P e^{b_P[\alpha(t)-1]}$$

$$G_P(t) = a_P (e^{b_P[\alpha_P(t)-1]} / b_P - \gamma_P)$$

$$L_P(s) = \ln \frac{s}{s_{0P}}$$

$$\alpha_P(t) = 1 + \delta_P + \alpha'_P t$$

- the simple pole f and ω reggeon amplitudes are:

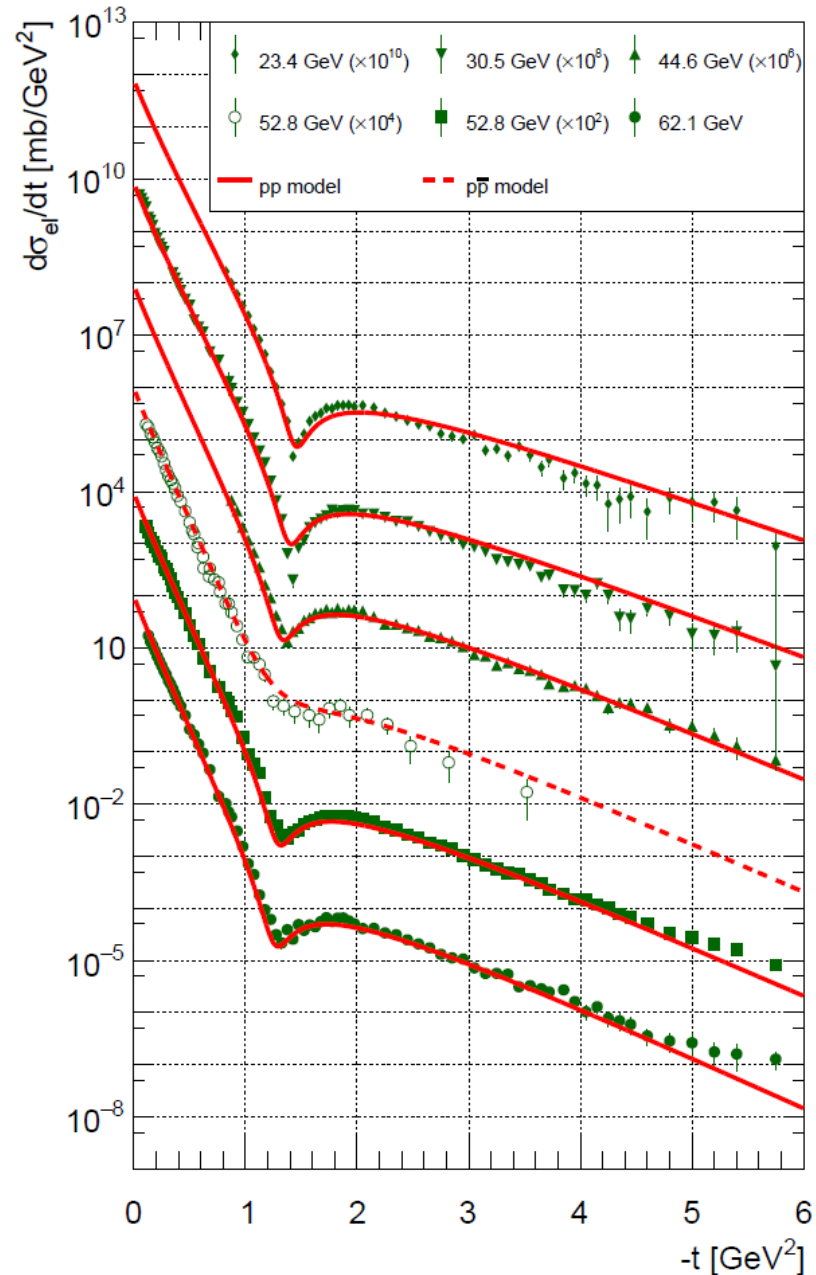
$$A_f(s, t) = a_f e^{-\frac{i\pi\alpha_f(t)}{2}} (s/s_0)^{\alpha_f(t)} e^{b_f t}$$

$$A_\omega(s, t) = iA_{f \rightarrow \omega}(s, t)$$

$$\alpha_f(t) = \alpha_f^0 + \alpha'_f t$$

(with free parameters labeled by " ω ")

ISR $d\sigma_{e\ell}/dt$ data and the model

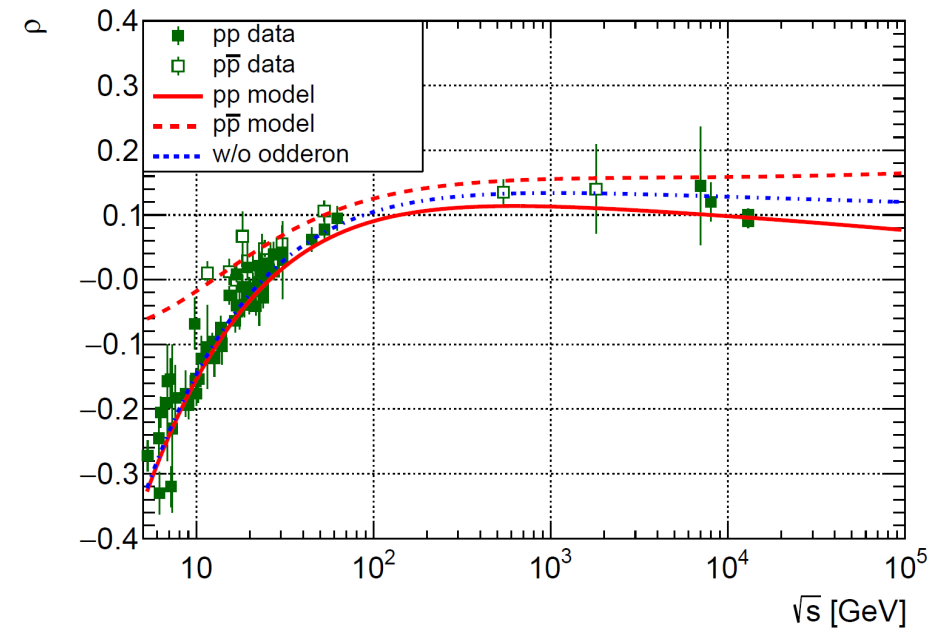
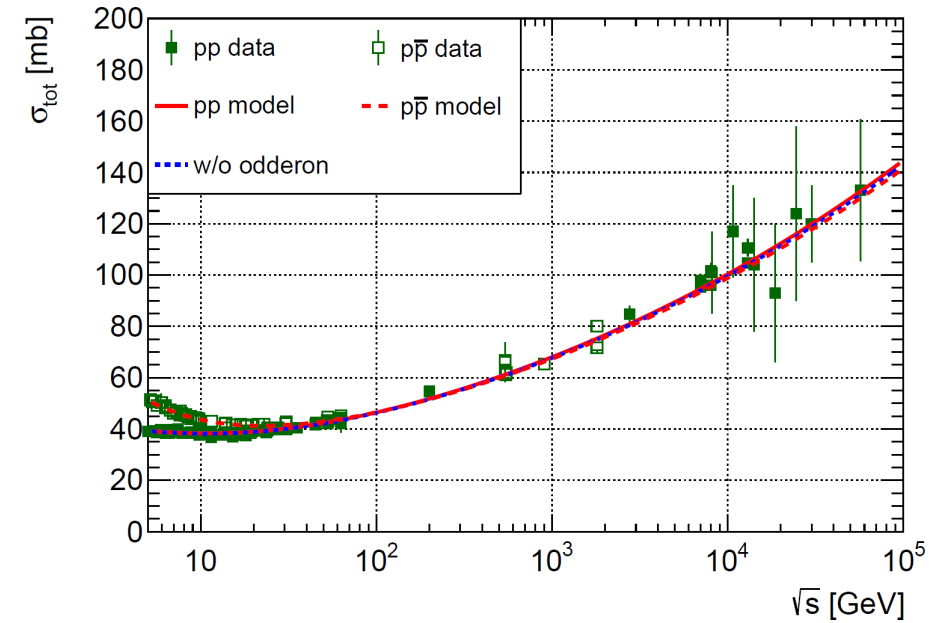
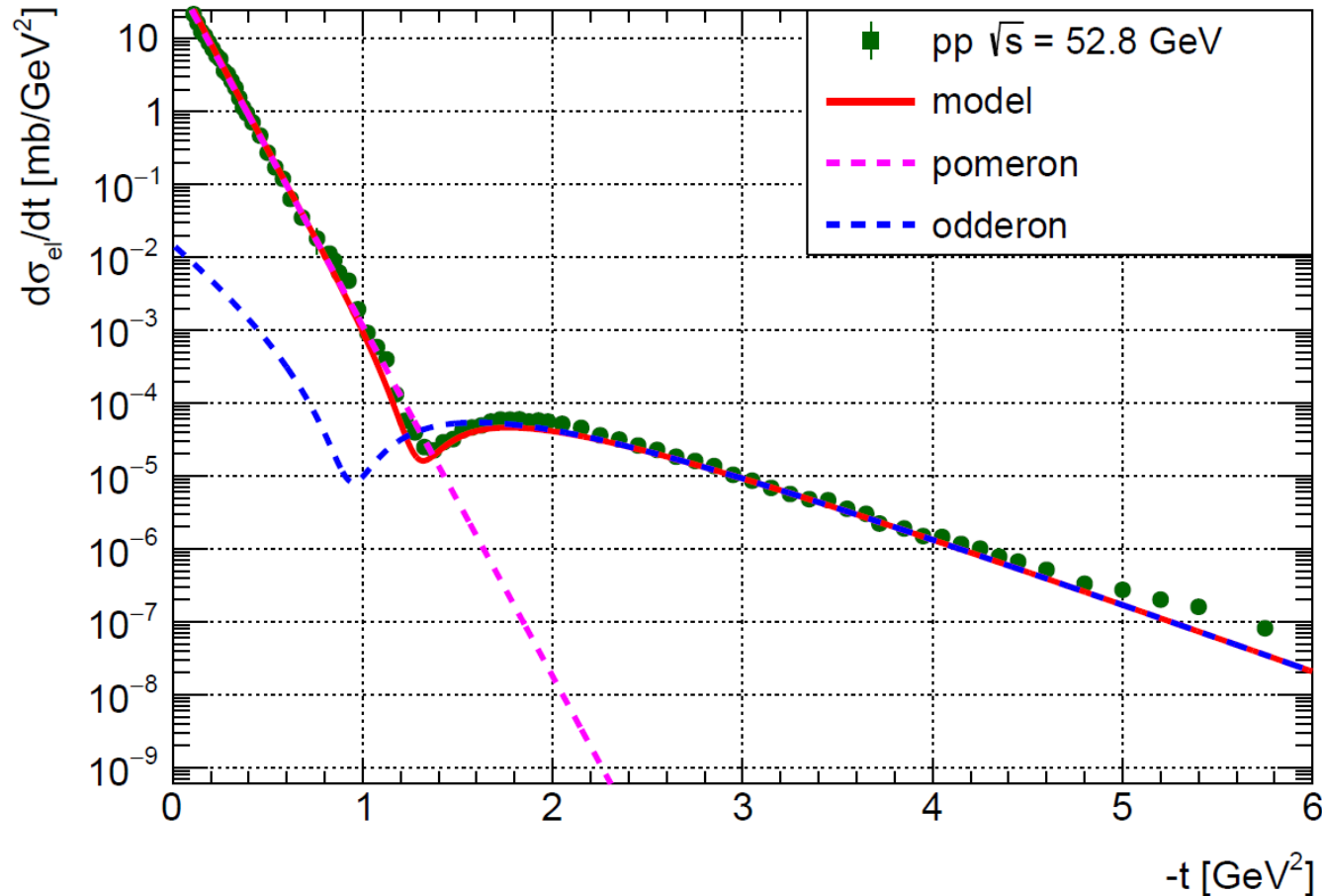


Pomeron	Odderon	f-reggeon	ω -reggeon
$\delta_P = 0.043$	$\delta_O = 0.14$	$\alpha_f^0 = 0.69$	$\alpha_\omega^0 = 0.44$
$\alpha'_P = 0.36$	$\alpha'_O = 0.13$	$\alpha'_f = 0.84$	$\alpha'_\omega = 0.93$
$a_P = 9.10$	$a_O = 0.029$	$a_f = -15.4$	$a_\omega = 9.69$
$b_P = 8.47$	$b_O = 6.96$	$b_f = 4.78$	$b_\omega = 3.5$
$\gamma_P = 0$	$\gamma_O = 0.11$	-	-
$s_{0P} = 2.88$	$s_{0O} = 1$	$s_{0f} = 1$	$s_{0\omega} = 1$

Fit to proton-proton and proton-antiproton differential cross section data at ISR energy region, and to ρ and total cross section data from 5 GeV up to the highest energies

$d\sigma_{el}/dt$ with P and O contribution, ρ and σ_{tot} w/o O

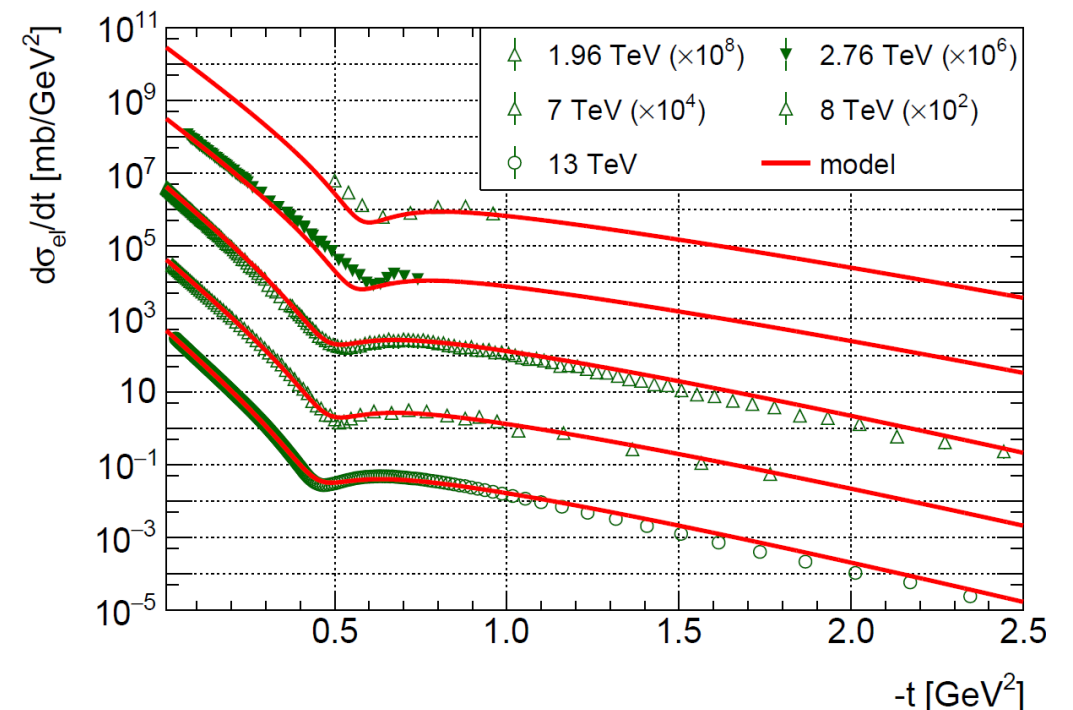
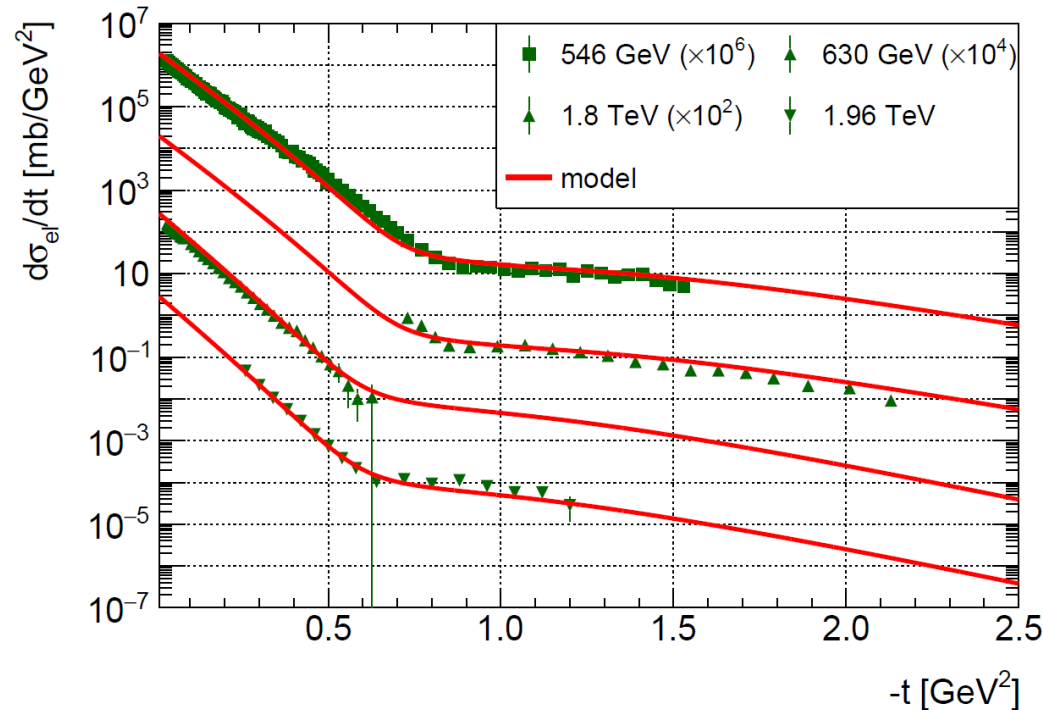
the odderon contribution takes over completely after the bump but at low- $|t|$ the odderon contribution is small



SPS + TEVATRON + LHC $d\sigma_{e_l}/dt$ data and the model

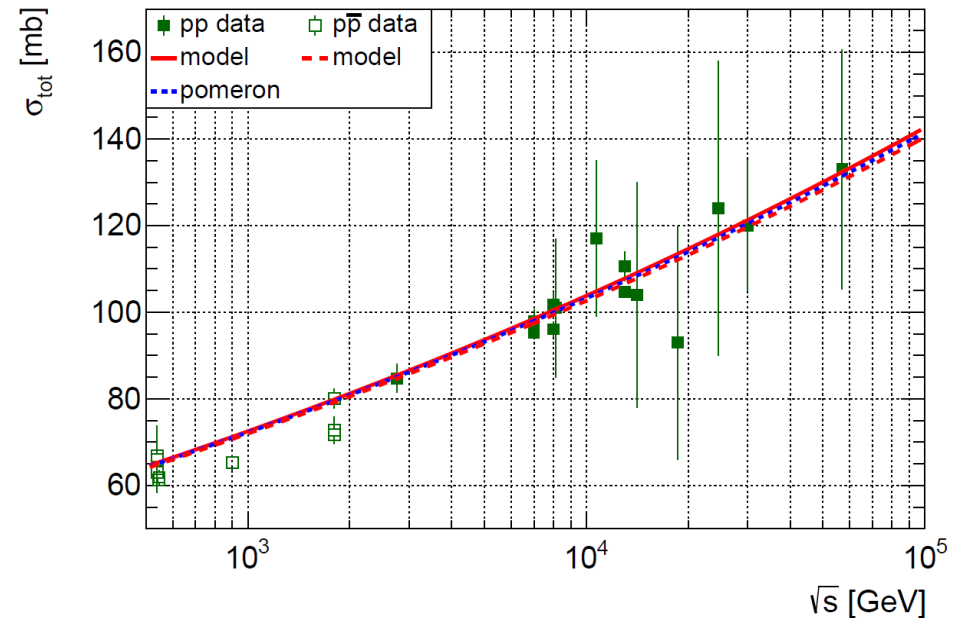
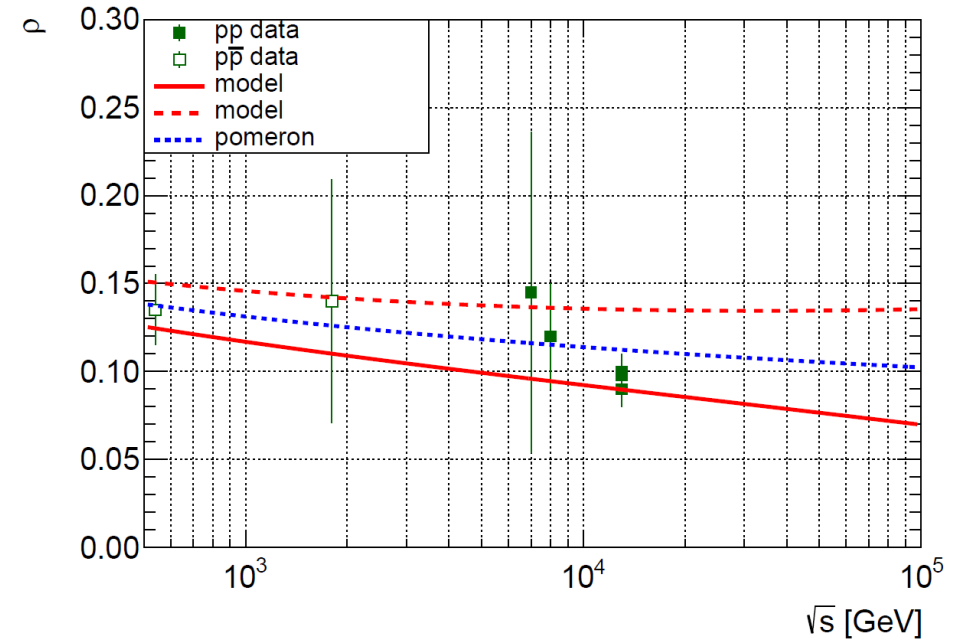
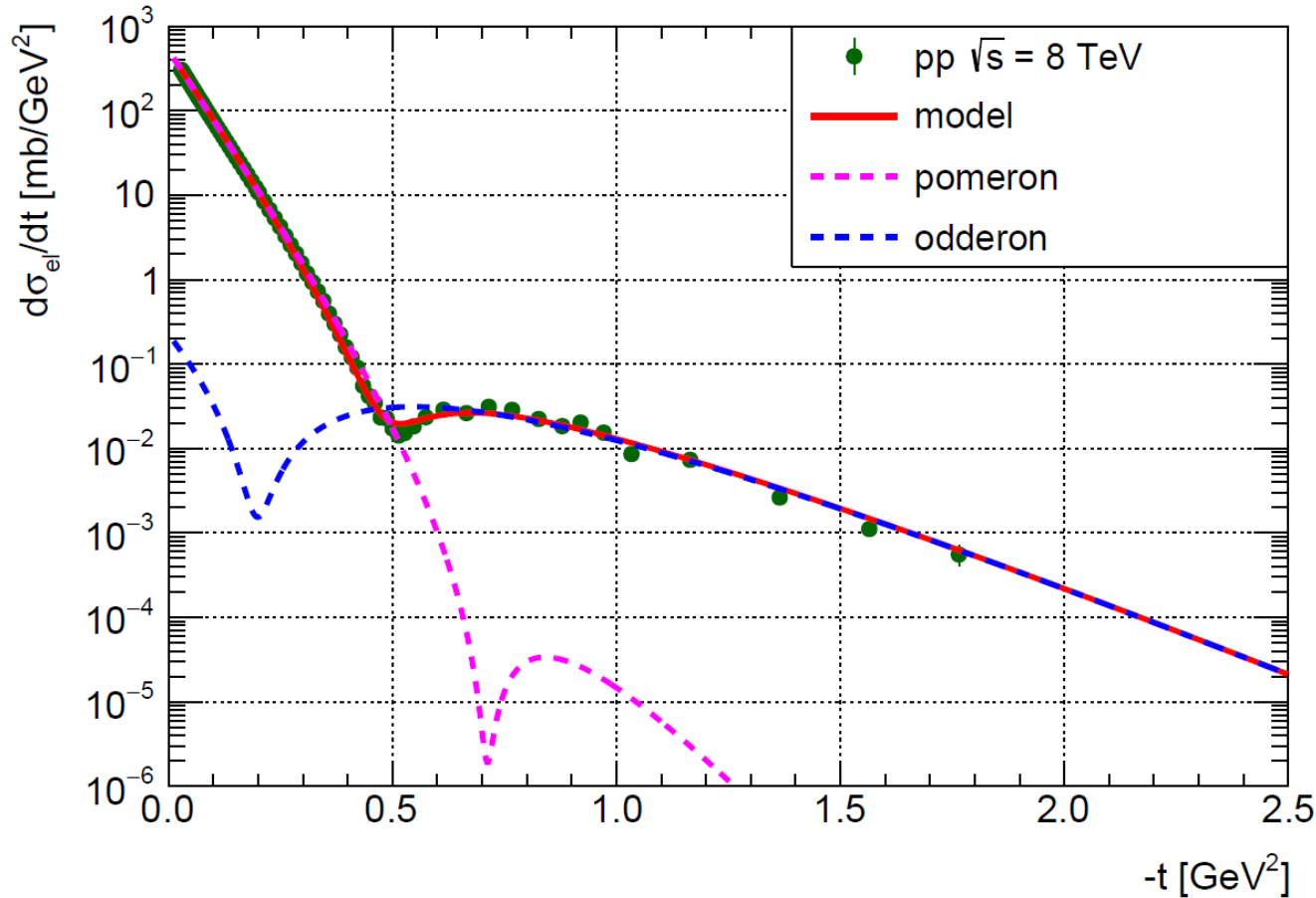
fit to proton-proton and proton-antiproton differential cross section data, and to ρ and total cross section data from 0.5 TeV up to the highest energies

Pomeron	Odderon
$\delta_P = 0.029$	$\delta_O = 0.2$
$\alpha'_P = 0.43$	$\alpha'_O = 0.15$
$a_P = 45.62$	$a_O = 0.019$
$b_P = 4.87$	$b_O = 2.16$
$\gamma_P = 0.061$	$\gamma_O = 0.487$
$s_{0P} = 11.26$	$s_{0O} = 1.03$



$d\sigma_{el}/dt$ with P and O contribution, ρ and σ_{tot} w/o O

the odderon contribution takes over completely after the bump but at low- $|t|$ the odderon contribution is small



Dip and bump position in $d\sigma_{el}/dt$ in a dipole Regge model

$$A^{\text{DP}}(s, \alpha) = e^{-\frac{i\pi\alpha}{2}} \left(\frac{s}{s_0}\right)^\alpha \left[G'(\alpha) + \left(L - \frac{i\pi}{2}\right) G(\alpha) \right]$$

$$G'(\alpha) = a e^{b[\alpha-1]}$$

$$G(\alpha) = a \left(\frac{e^{b[\alpha-1]}}{b} - \gamma \right)$$

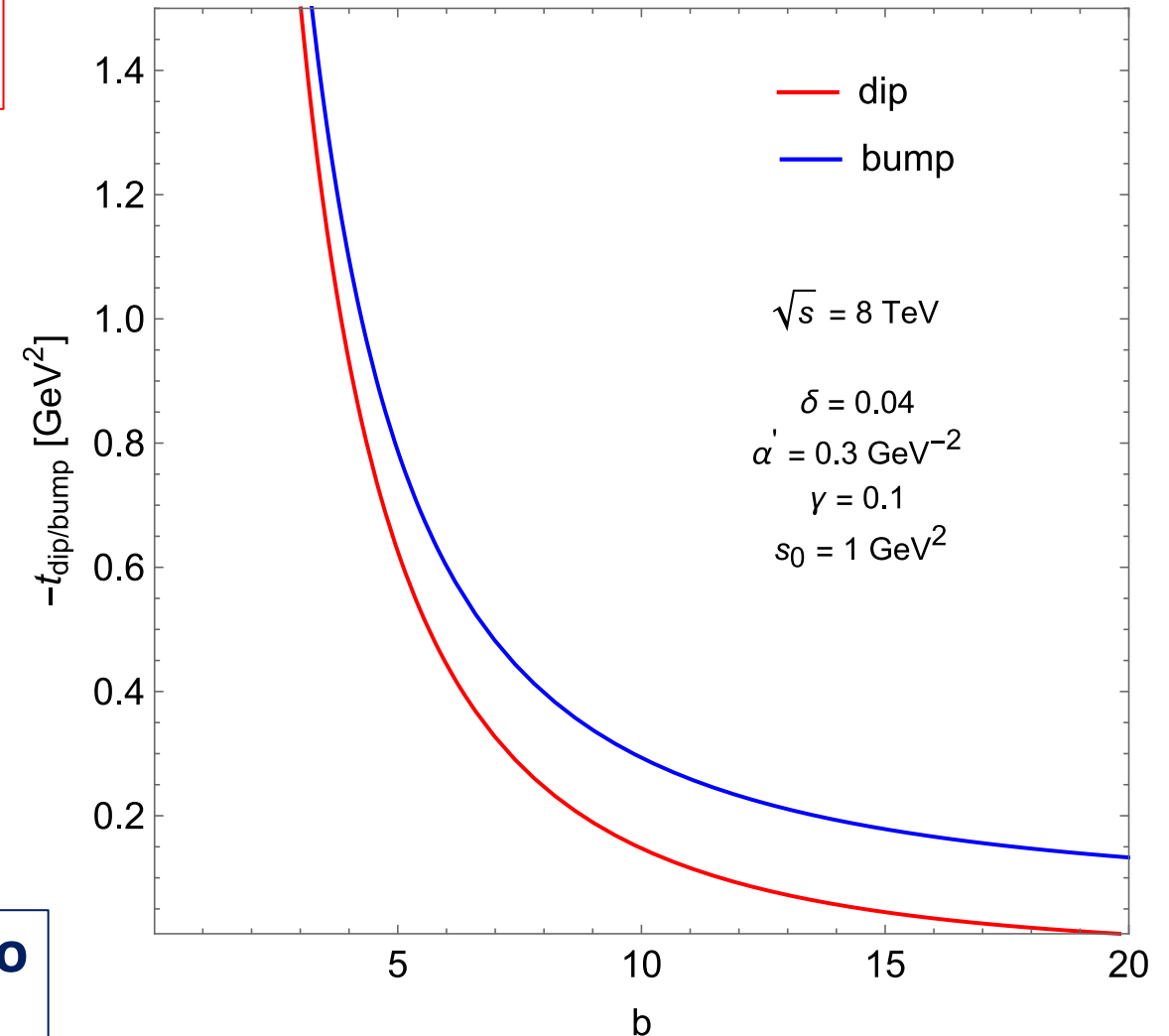
$$\alpha = 1 + \delta + \alpha' t$$

$$L = \ln \frac{s}{s_0}$$

$$-t_{\min} = \frac{1}{\alpha' b} \ln \frac{b + L}{\gamma b L}$$

$$-t_{\max} = \frac{1}{\alpha' b} \ln \frac{4(b + L)^2 + \pi^2}{\gamma b (4L^2 + \pi^2)}$$

the position of the dip and of the bump goes to smaller $-t$ values as slope parameter rises

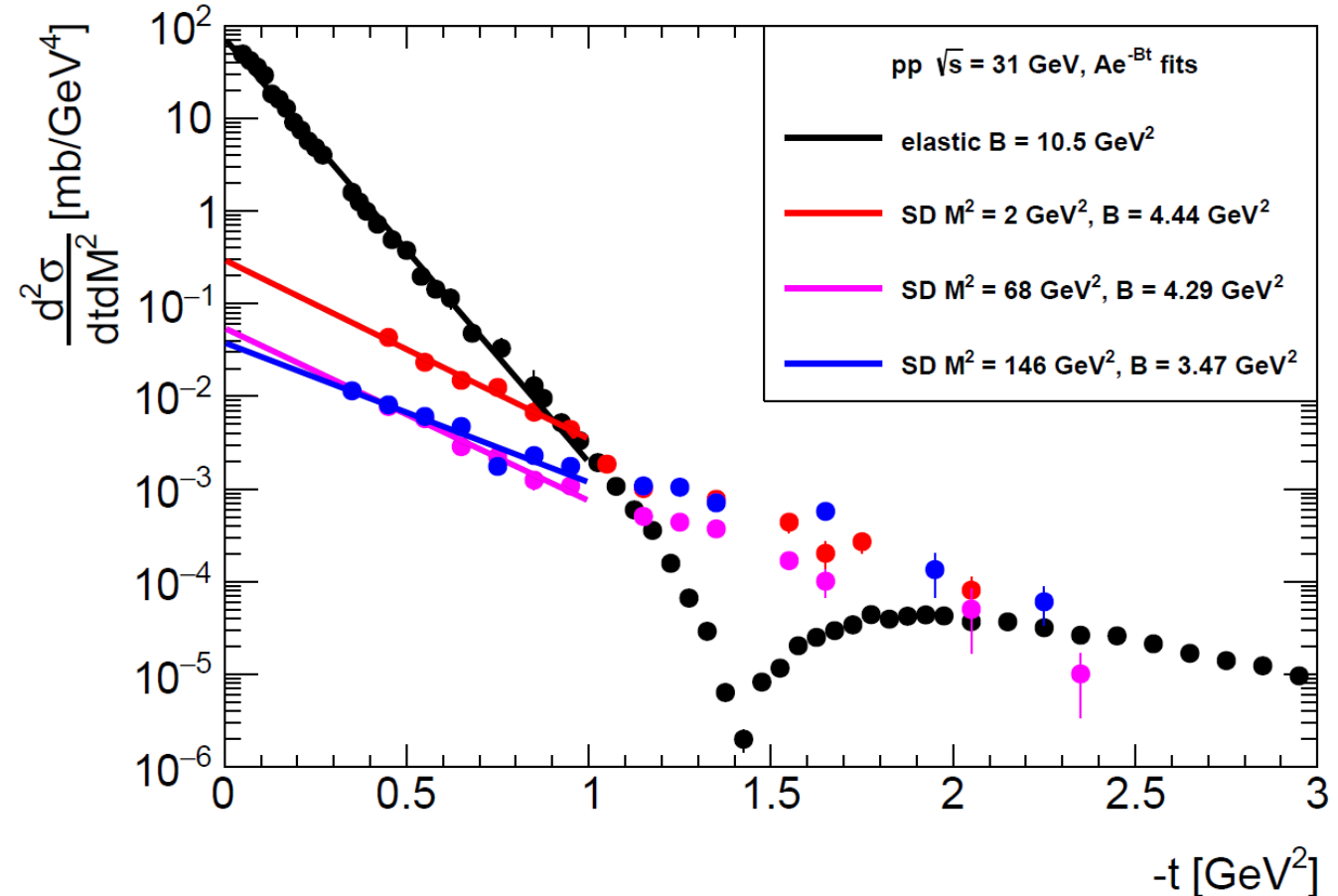


Dip-bump structures in single diffractive dissociation?

- measurements of pp single diffractive dissociation at ISR do not show a dip-bump structure at $|t|$ values where such a structure is observed in elastic pp scattering

M.G. Albrow et al., Nucl. Phys. B72, 376 (1974)

- it can be explained in a framework of a dipole Regge model in which the dip-bump structure moves to higher $|t|$ values as the value of the slope parameter decreases
- a dipole odderon+pomeron Regge approach can be used to predict dip-bump structures in pp single diffractive dissociation at LHC energies**



Dipole Regge approach for single diffraction (SD)

- in the triple Regge approach the triple pomeron vertex results the following contribution for the double differential SD cross section:

$$\frac{d^2 \sigma_{SD}^P}{dt dM^2} = \frac{1}{16\pi^2} \frac{1}{M^2} g_{PPp}^2(t) (s/M^2)^{2\alpha_P(t)-2} g_{PPP}(t) g_{PPP}(0) (M^2)^{\delta_P}$$

- g_{PPP} is found to be t-independent
- assumption: the t-dependent part of the amplitude of the SD process has the form in case the pomeron a simple pole:**

$$A_{SD}^{SP}(s, M^2, \alpha(t)) \sim e^{-\frac{i\pi\alpha}{2}} G(\alpha) (s/M^2)^\alpha$$

- $G(\alpha)$ incorporates the t-dependence coming from $g_{PPp}(t)$
- a dipole pomeron amplitude is obtained as:

$$A_{SD}^{DP}(s, M^2, \alpha) = \frac{d}{d\alpha} A_{SD}^{SP}(s, M^2, \alpha) \sim e^{-\frac{i\pi\alpha}{2}} \left(\frac{s}{M^2}\right)^\alpha \left[G'(\alpha) + \left(L_{SD} - \frac{i\pi}{2} \right) G(\alpha) \right]$$

$$L_{SD} \equiv \ln(s/M^2)$$

Dipole Regge approach for single diffraction (SD)

- the double differential cross section for the SD process resulting from the dipole pomeron amplitude is:

$$\frac{d^2\sigma_{SD}^P}{dt dM^2} = \frac{1}{M^2} \left(G'^2(\alpha) + 2L_{SD}G(\alpha)G'(\alpha) + G^2(\alpha) \left(L_{SD}^2 + \frac{\pi^2}{4} \right) \right) (s/M^2)^{2\alpha(t)-2} \sigma^{Pp}(M^2)$$

$$G'(\alpha) = a e^{b[\alpha-1]}$$

$$\alpha = 1 + \delta + \alpha't$$

$$G(\alpha) = \int G'(\alpha) d\alpha = a \left(\frac{e^{b[\alpha-1]}}{b} - \gamma \right)$$

$$\sigma^{Pp}(M^2) = g_{PPP} g_{Ppp}(0) (M^2)^{\delta_P}$$

- Using the $\xi = M^2/s$ proton's relative momentum loss variable, we have:

$$\frac{d^2\sigma_{SD}}{dt d\xi} = \left(G'^2(\alpha) + 2L_{SD}G(\alpha)G'(\alpha) + G^2(\alpha) \left(L_{SD}^2 + \frac{\pi^2}{4} \right) \right) \xi^{1-2\alpha(t)} \sigma^{Pp}(s\xi)$$

$$L_{SD} \equiv \ln(s/M^2) = -\ln\xi$$

- dip and bump appear at:**

$$-t_{dip}^{SD} = \frac{1}{\alpha'b} \ln \frac{b + L_{SD}}{\gamma b L_{SD}}$$

$$-t_{bump}^{SD} = \frac{1}{\alpha'b} \ln \frac{4(b + L_{SD})^2 + \pi^2}{\gamma b (4L_{SD}^2 + \pi^2)}$$

Odderon contribution in SD in form of a OOP vertex

- the odderon-odderon-pomeron vertex results the following contribution for the double differential SD cross section:

$$\frac{d^2\sigma_{SD}^0}{dt dM^2} = \frac{1}{16\pi^2} \frac{1}{M^2} g_{Opp}^2(t) (s/M^2)^{2\alpha_O(t)-2} g_{OOP}(t) g_{PPP}(0) (M^2)^{\delta_P}$$

- assumption: $g_{OOP}(t)$ is t-independent and the t-dependent part of the odderon amplitude of the SD process has the form:**

$$A_{SD}^{SP}(s, M^2, \alpha) \sim e^{-\frac{i\pi\alpha}{2}} G(\alpha_O) (s/M^2)^{\alpha_O}$$

$$G'(\alpha_O) = a e^{b[\alpha_O-1]}$$

$$G(\alpha) = \int G'(\alpha) d\alpha$$

- $G(\alpha_O)$ incorporates the t-dependence coming from $g_{Opp}(t)$

- a dipole odderon contribution to the cross section is obtained as:

$$\frac{d^2\sigma_{SD}^0}{dt dM^2} = \frac{1}{M^2} \left(G'^2(\alpha) + 2L_{SD} G(\alpha) G'(\alpha) + G^2(\alpha) \left(L_{SD}^2 + \frac{\pi^2}{4} \right) \right) (s/M^2)^{2\alpha(t)-2} \sigma^{Pp}(M^2)$$

(the α parameter of $G(\alpha)$ accounts also in the difference between g_{OOP} and g_{PPP})

Odderon contribution in SD in form of a OOP vertex

- the pion exchange contribution to account for the high- ξ behaviour of the data:

$$\frac{d^2 \sigma}{d\xi dt} = f_{\pi/p}(\xi, t) \sigma^{\pi P}(s\xi)$$

- The full double SD differential cross section is written as:

$$\frac{d^2 \sigma_{SD}}{dt dM^2} = \frac{d^2 \sigma_{SD}^P}{dt dM^2} + \frac{d^2 \sigma_{SD}^O}{dt dM^2} + \frac{d^2 \sigma_{SD}^\pi}{dt dM^2}$$

In the ‘‘Reggeized’’ one-pion-exchange model [22], the pion flux is given by

$$f_{\pi/p}(\xi, t) = \frac{1}{4\pi} \frac{g_{\pi pp}^2}{4\pi} \frac{|t|}{(t - m_\pi^2)^2} G_1^2(t) \xi^{1 - 2\alpha_\pi(t)} \quad (3.17)$$

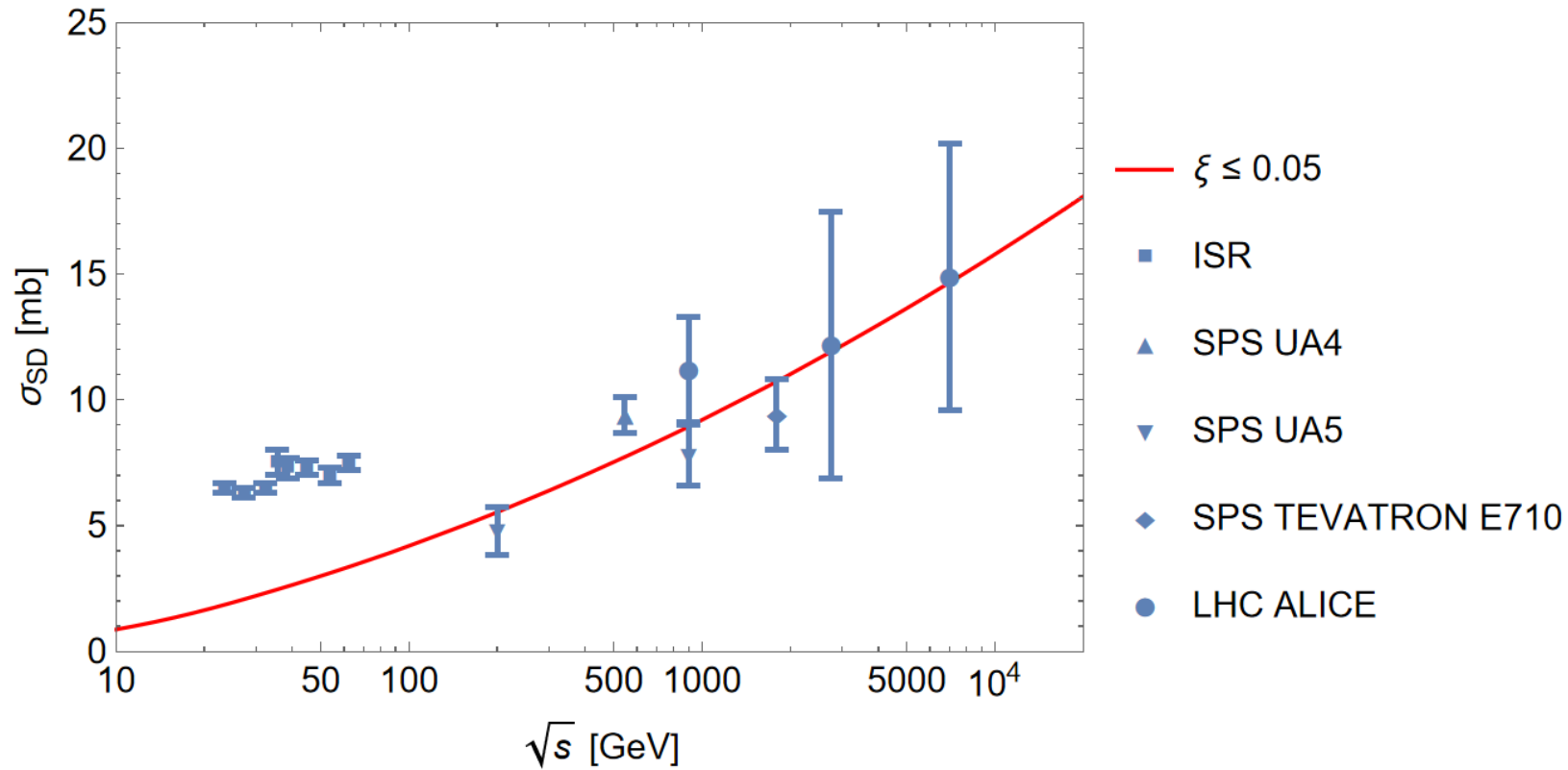
where $g_{\pi pp}^2/4\pi \approx 14.6$ [22] is the on mass-shell coupling, $\alpha_\pi(t) = 0.9t$ is the pion trajectory, and $G_1^2(t)$ is a form factor introduced to account for off mass-shell corrections. For $G_1(t)$ we use the expression (see [27] and references therein)

$$G_1(t) = \frac{2.3 - m_\pi^2}{2.3 - t}. \quad (3.18)$$

Since the exchanged pion is not far off-mass-shell, we use the on-shell πp total cross section [6],

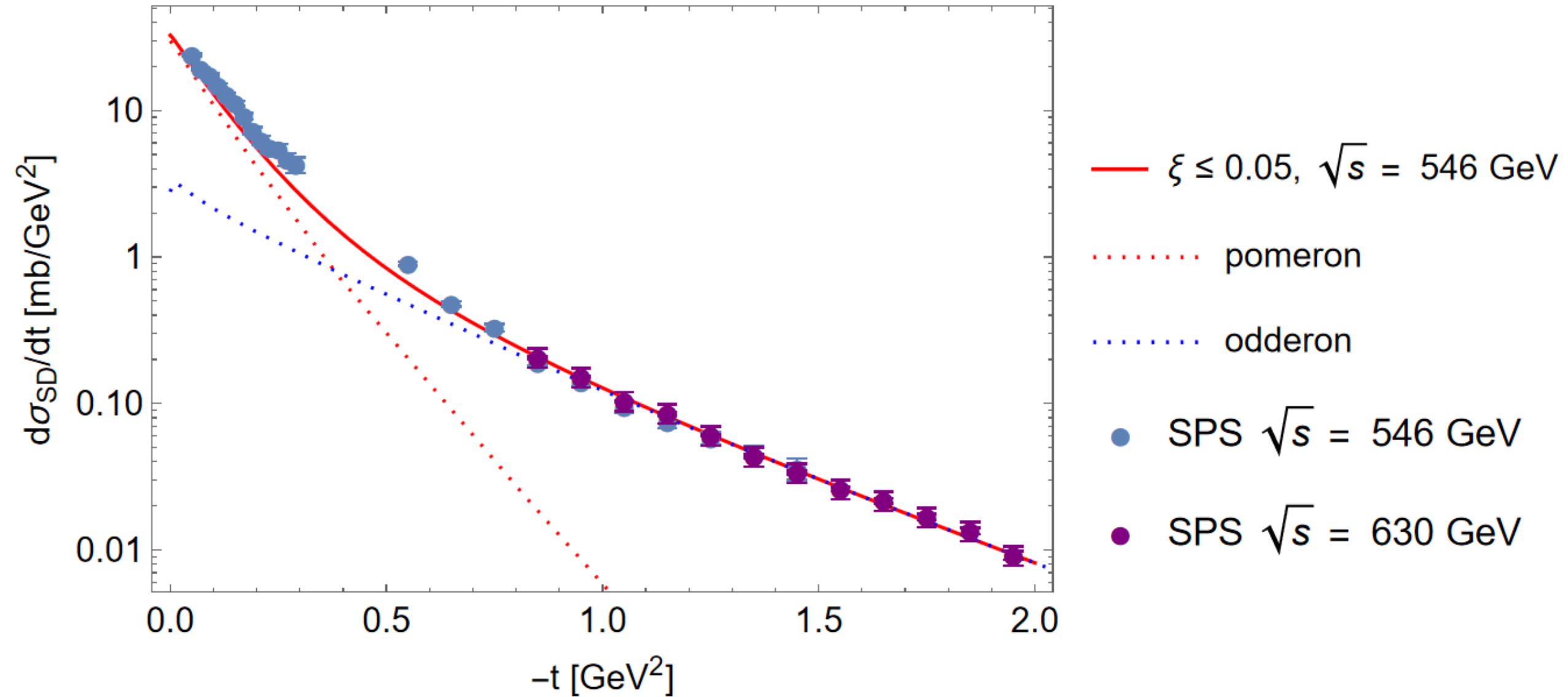
$$\begin{aligned} \sigma^{\pi P}(mb) &= \frac{1}{2} (\sigma^{\pi^+ P} + \sigma^{\pi^- P}) \\ &= 10.83 (s\xi)^{0.104} + 27.13 (s\xi)^{-0.32}. \end{aligned} \quad (3.19)$$

Total SD cross section

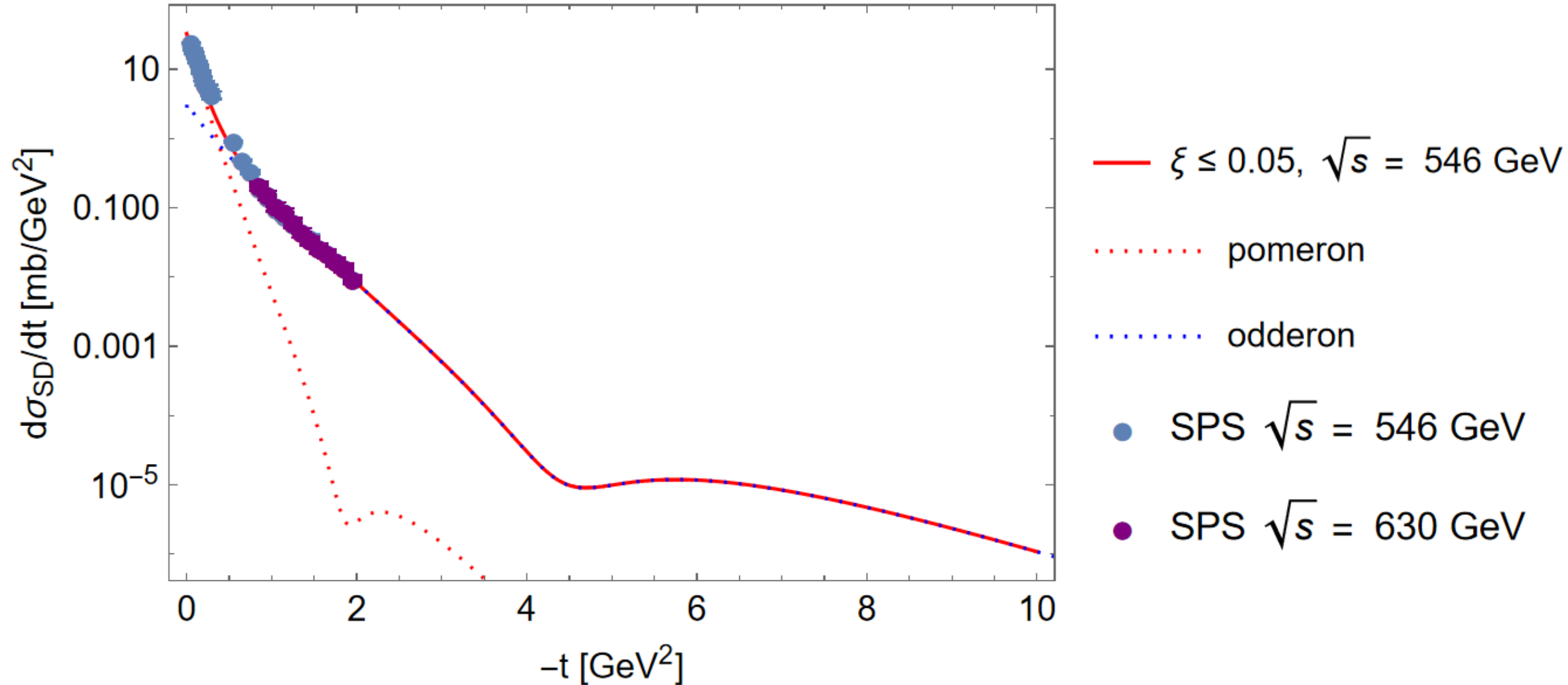


Pomeron	Odderon
$\delta_P = 0$	$\delta_O = 0$
$\alpha'_P = 0.43$	$\alpha'_O = 0.15$
$a_P = 0.32$	$a_O = 0.084$
$b_P = 2.86$	$b_O = 1.18$
$\gamma_P = 0.061$	$\gamma_O = 0.49$
$s_{0P} = 2.88$	$s_{0O} = 1$

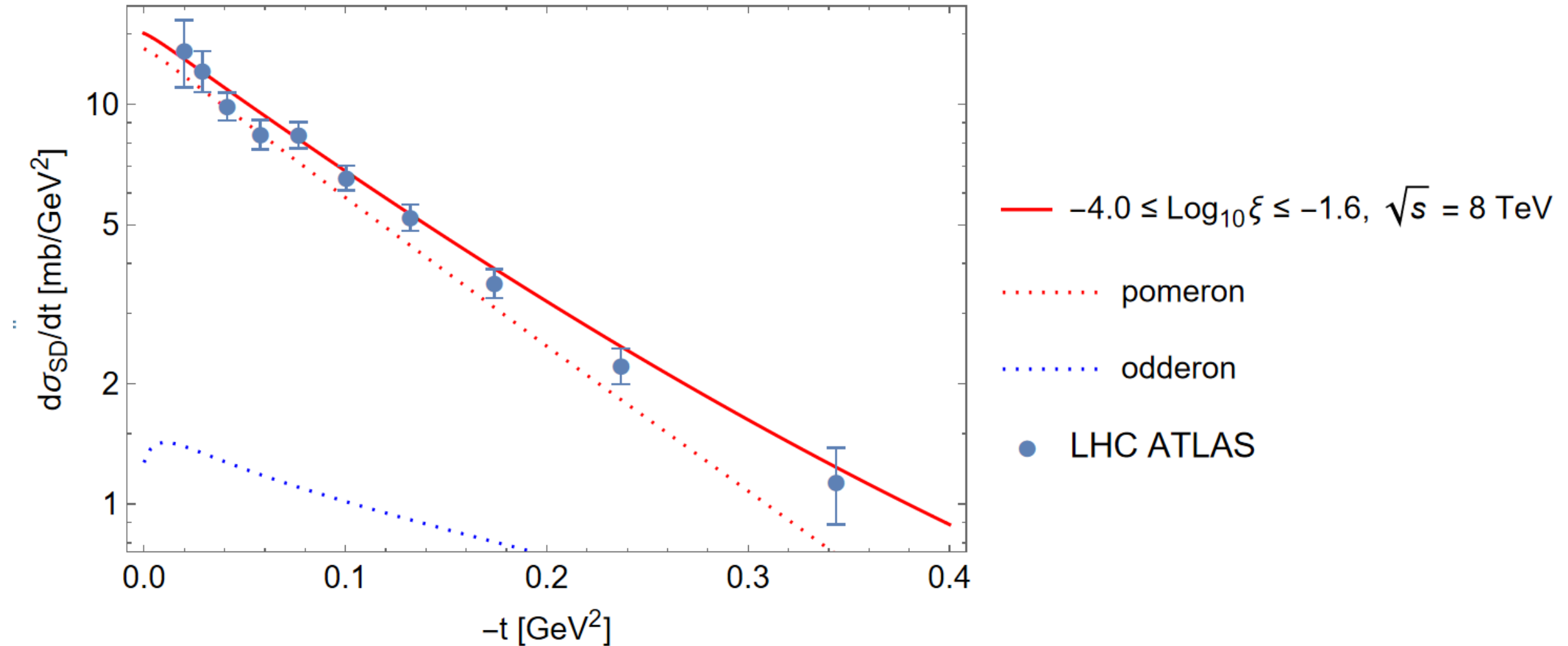
t dependence of the SD process at SPS energies



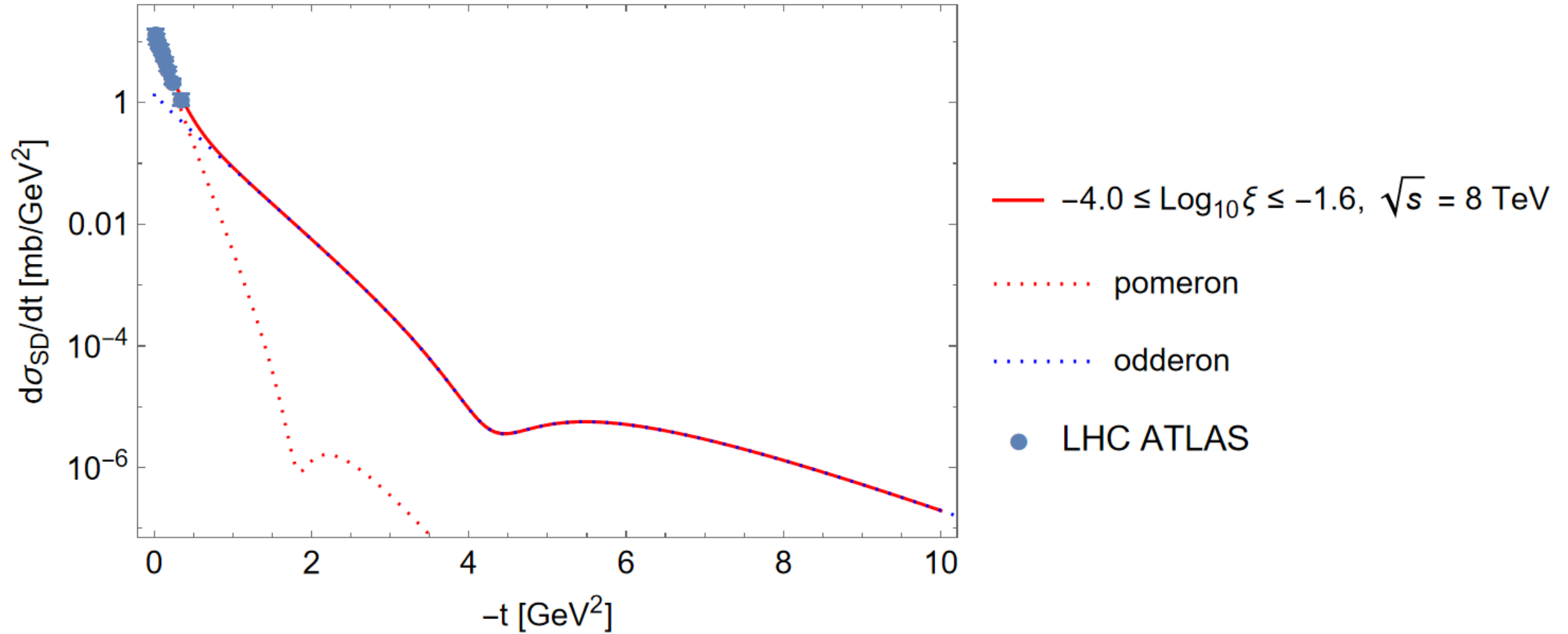
t dependence of the SD process at SPS energies



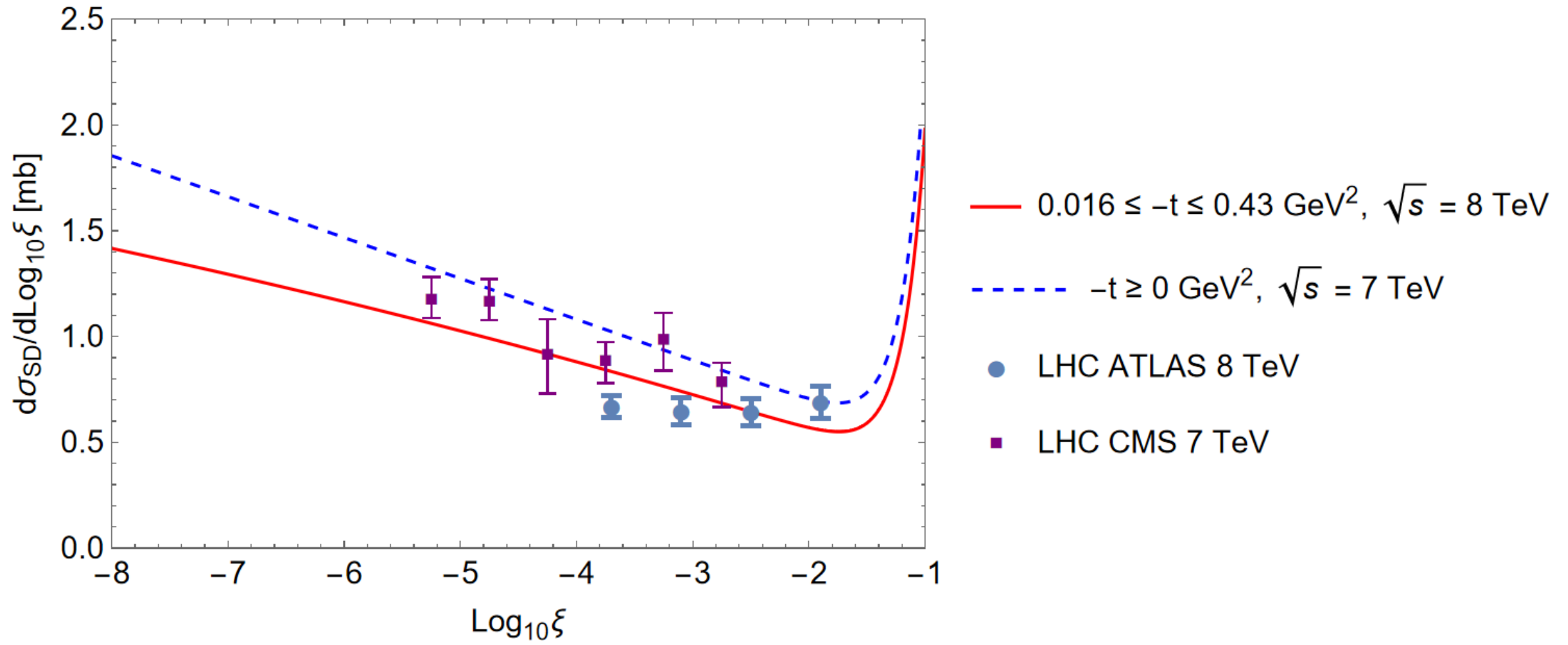
t dependence of the SD process at 8 TeV



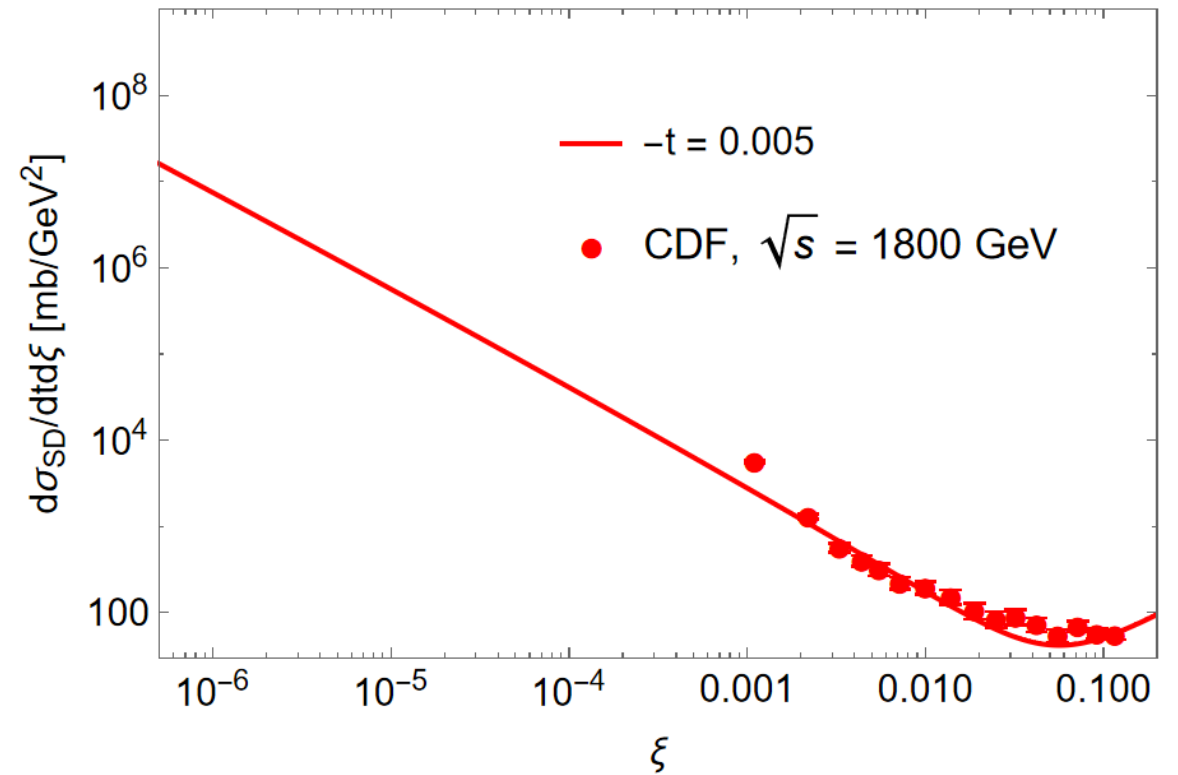
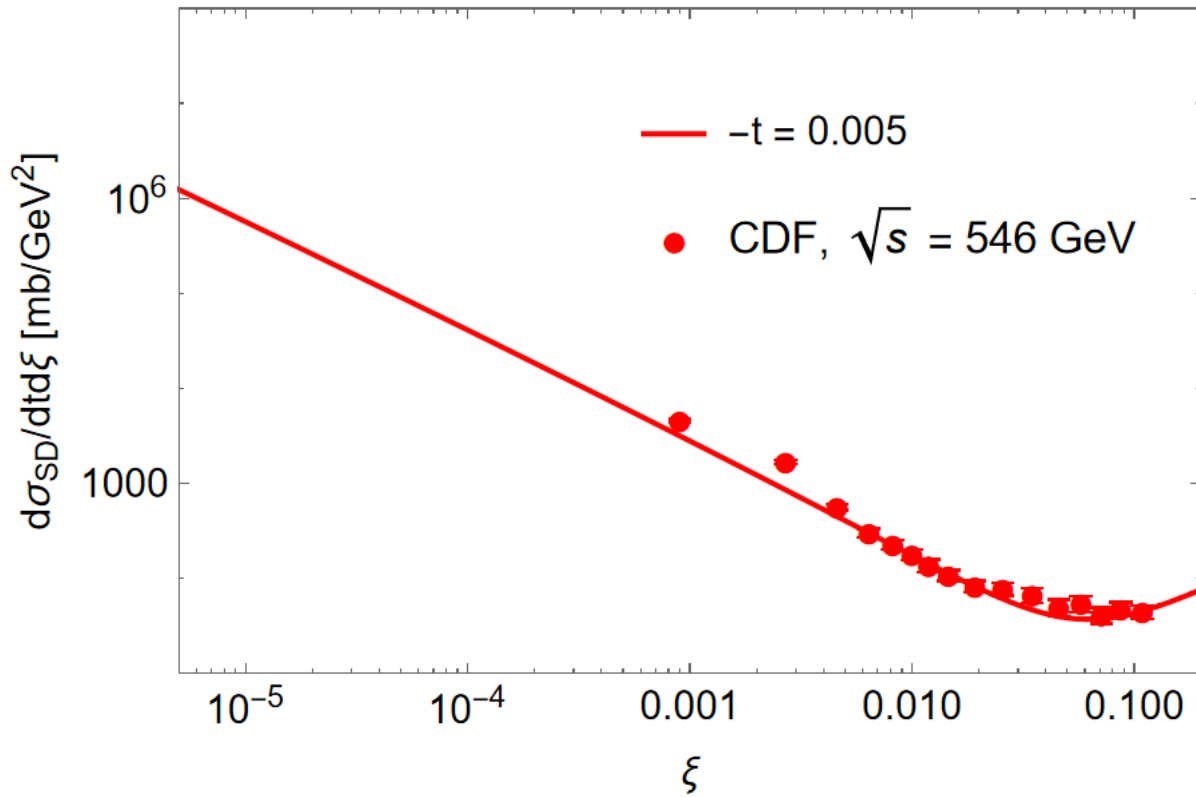
t dependence of the SD process at 8 TeV



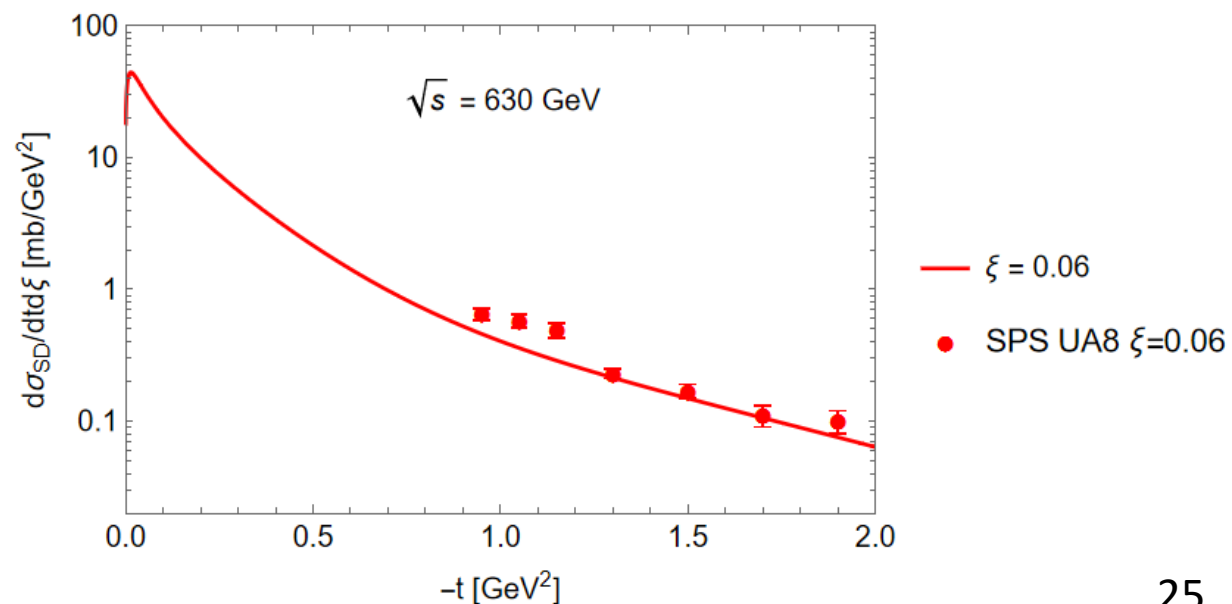
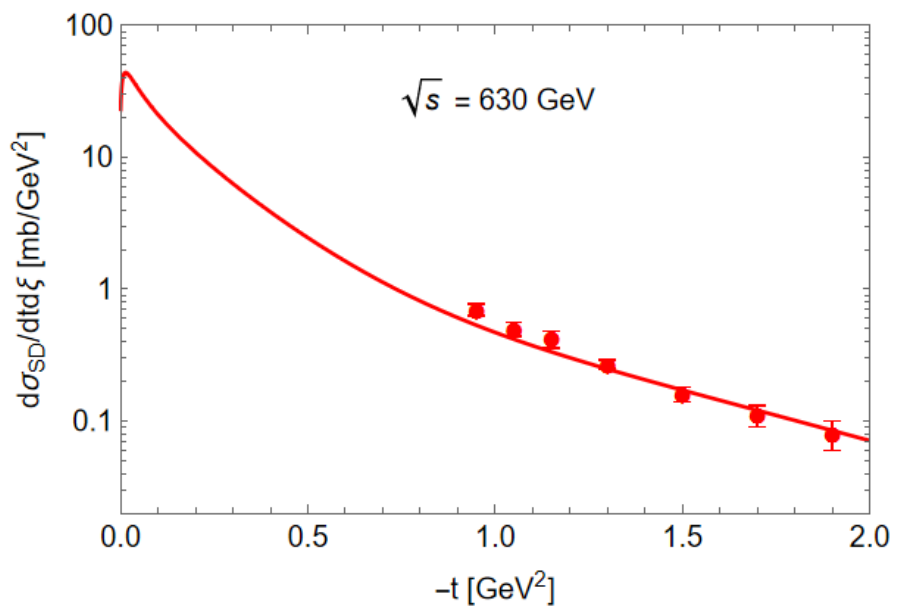
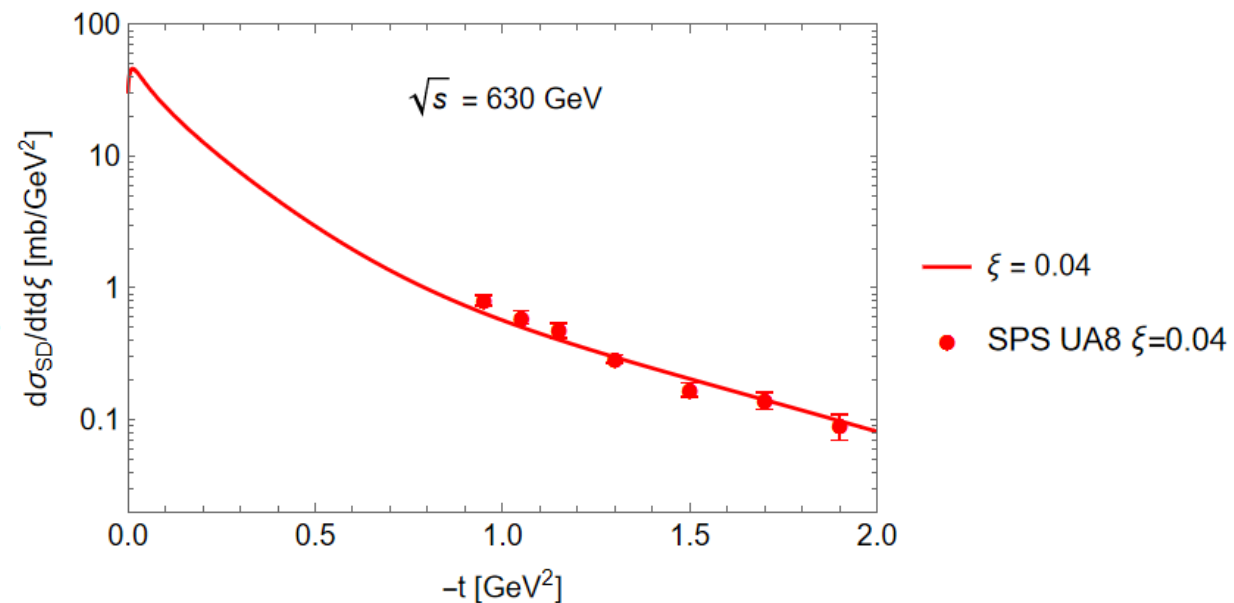
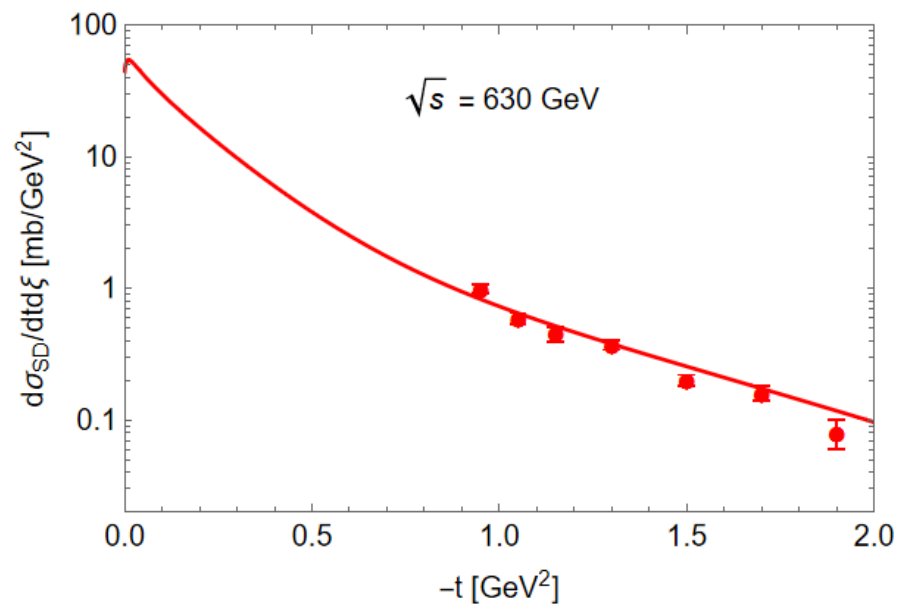
ξ dependence of the SD process at 8 TeV



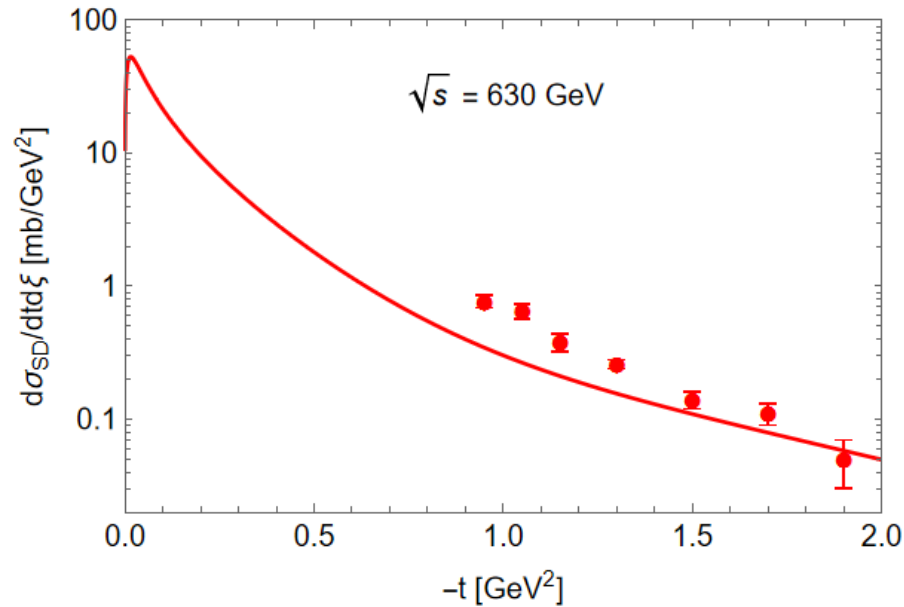
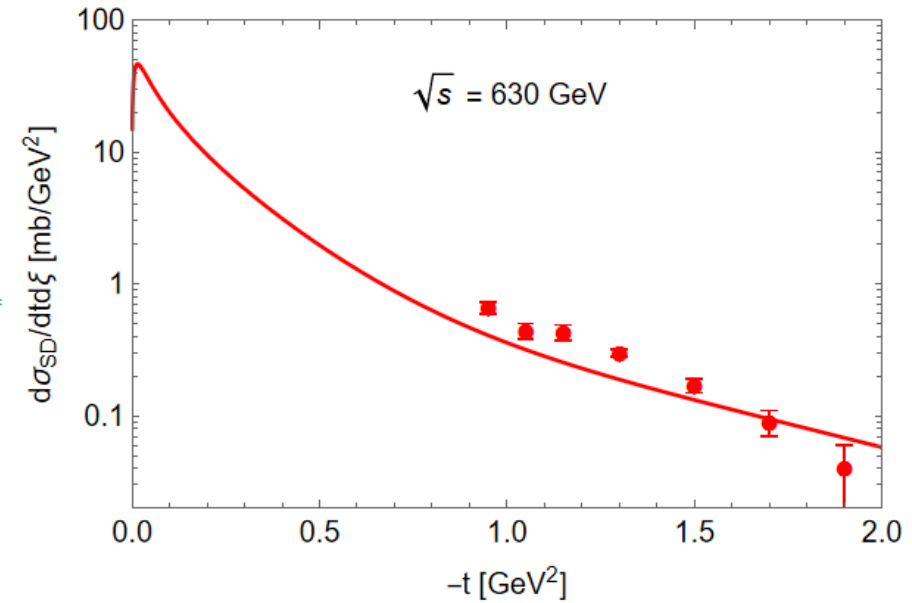
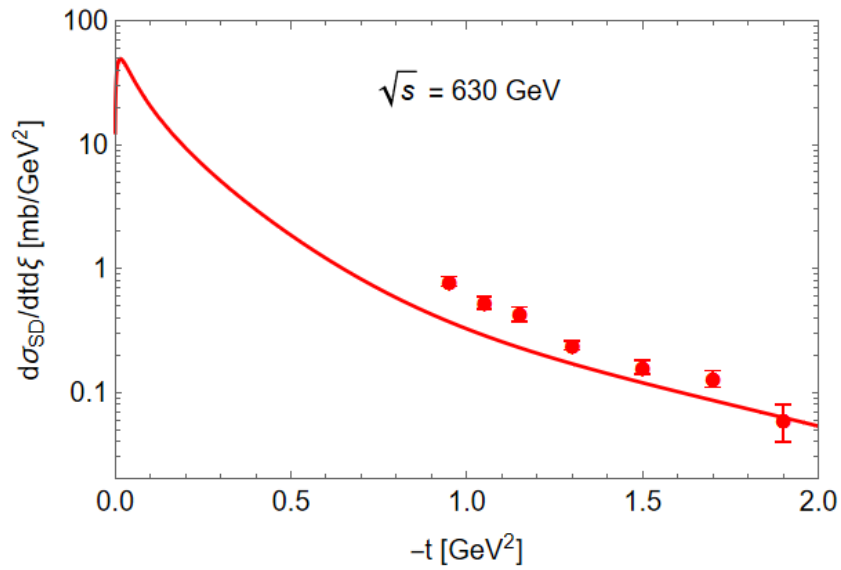
ξ dependence of the SD process at 546 GeV and 1.8 TeV



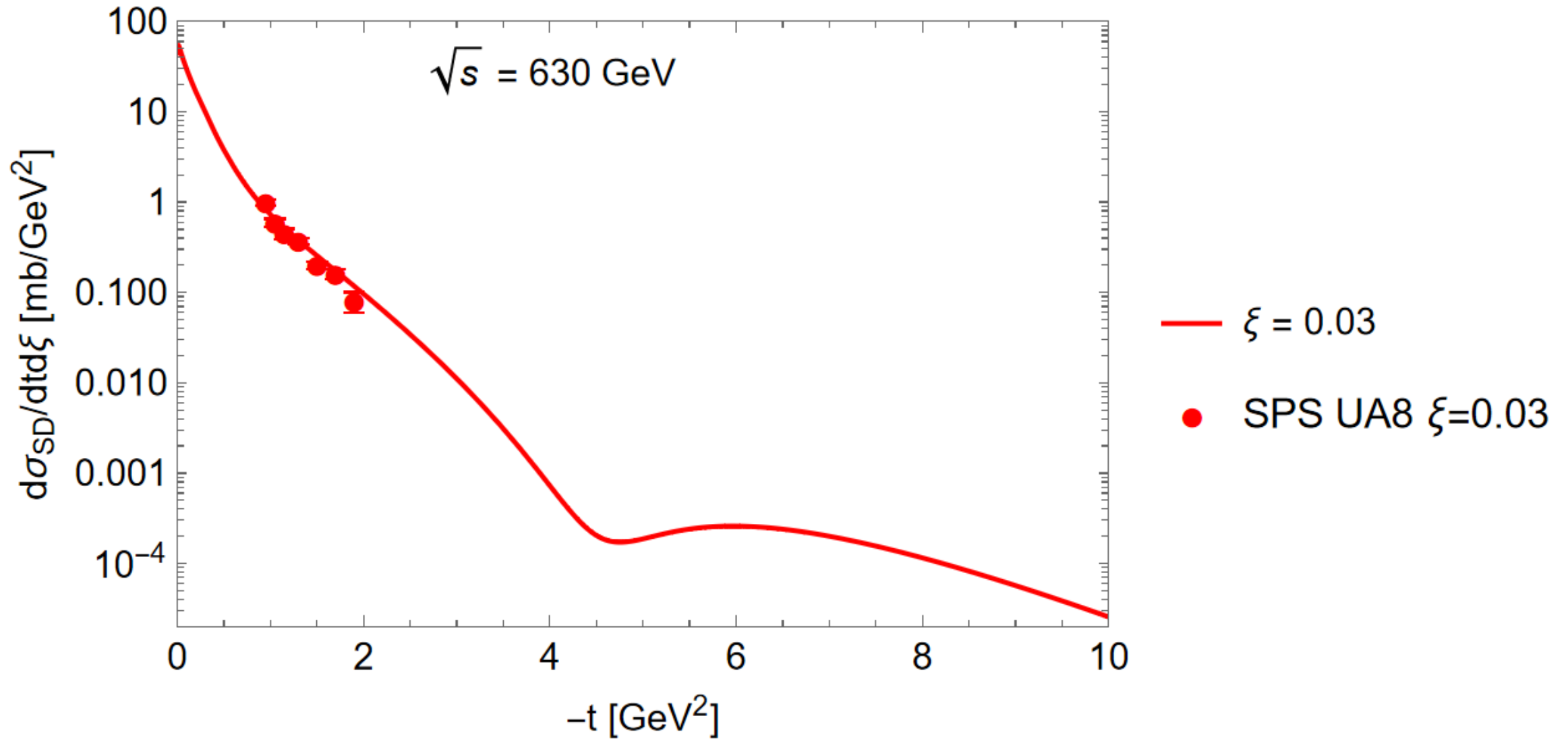
t dependence of the SD process at 630 GeV



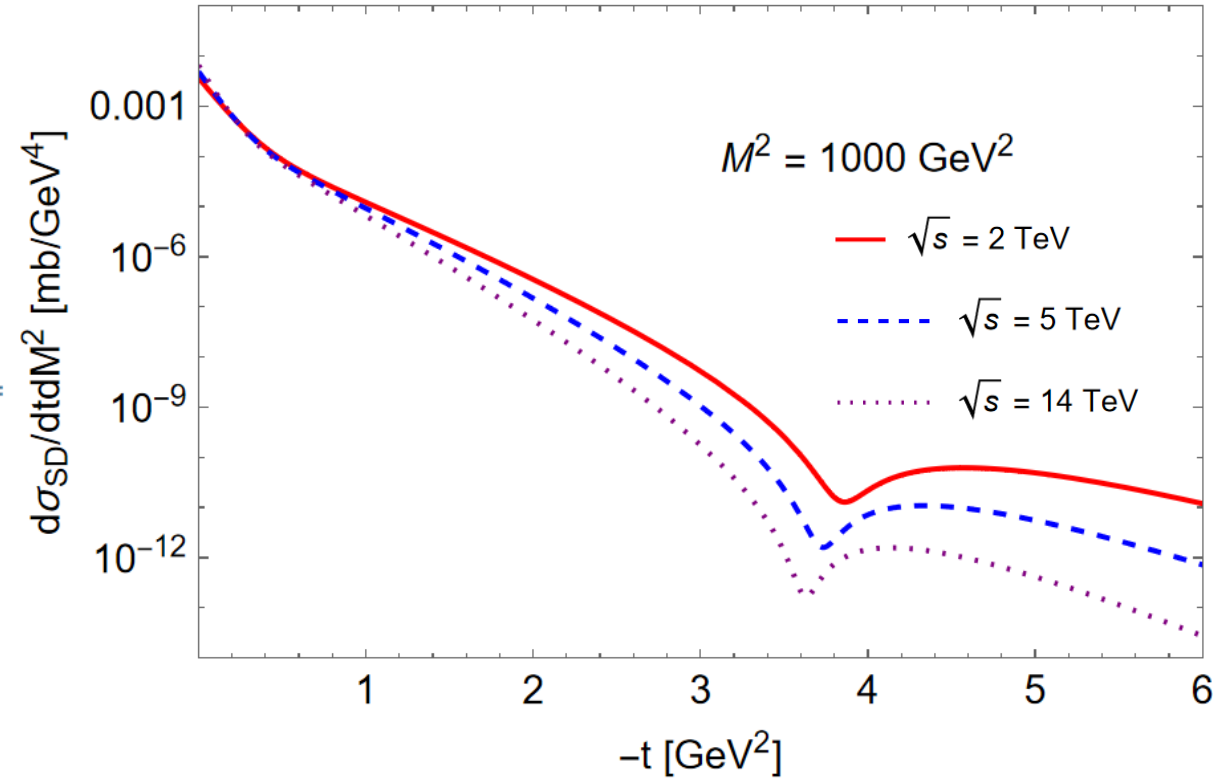
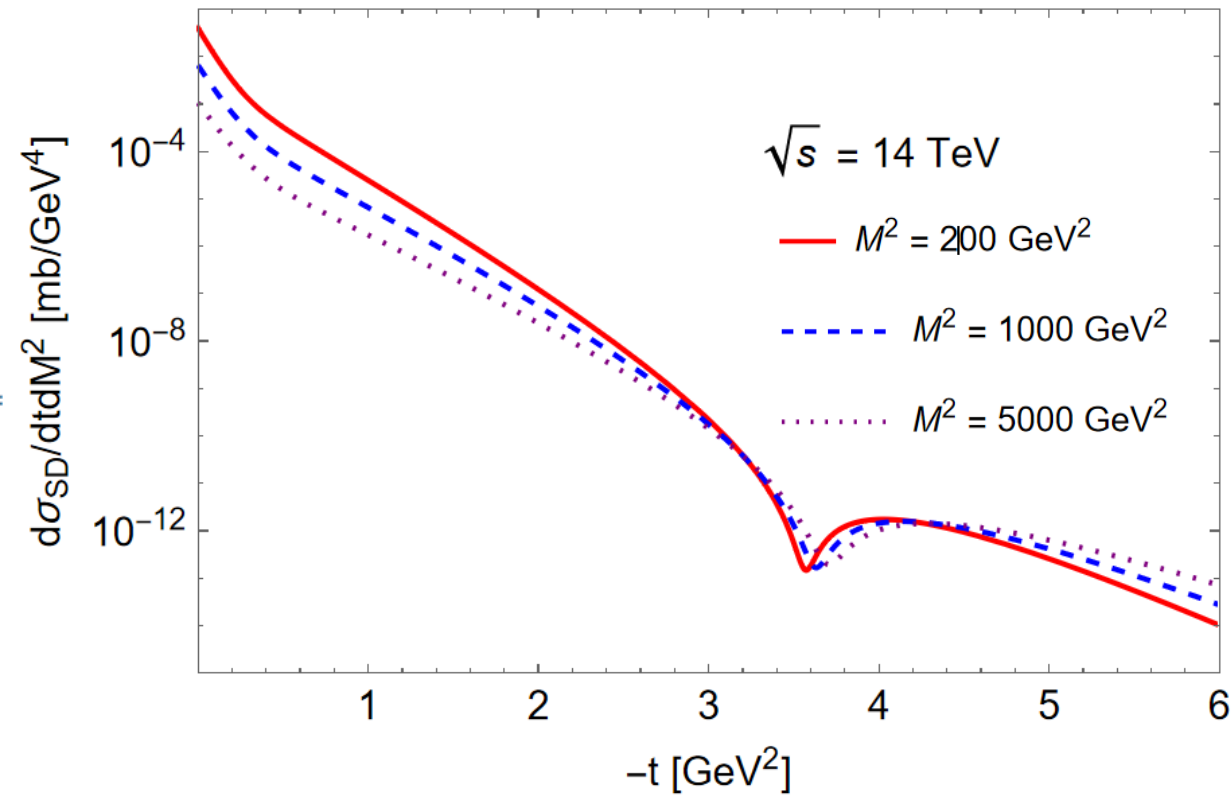
t dependence of the SD process at 630 GeV



t dependence of the SD process at 630 GeV



t , M^2 and s dependence of the SD process at LHC energies



Summary

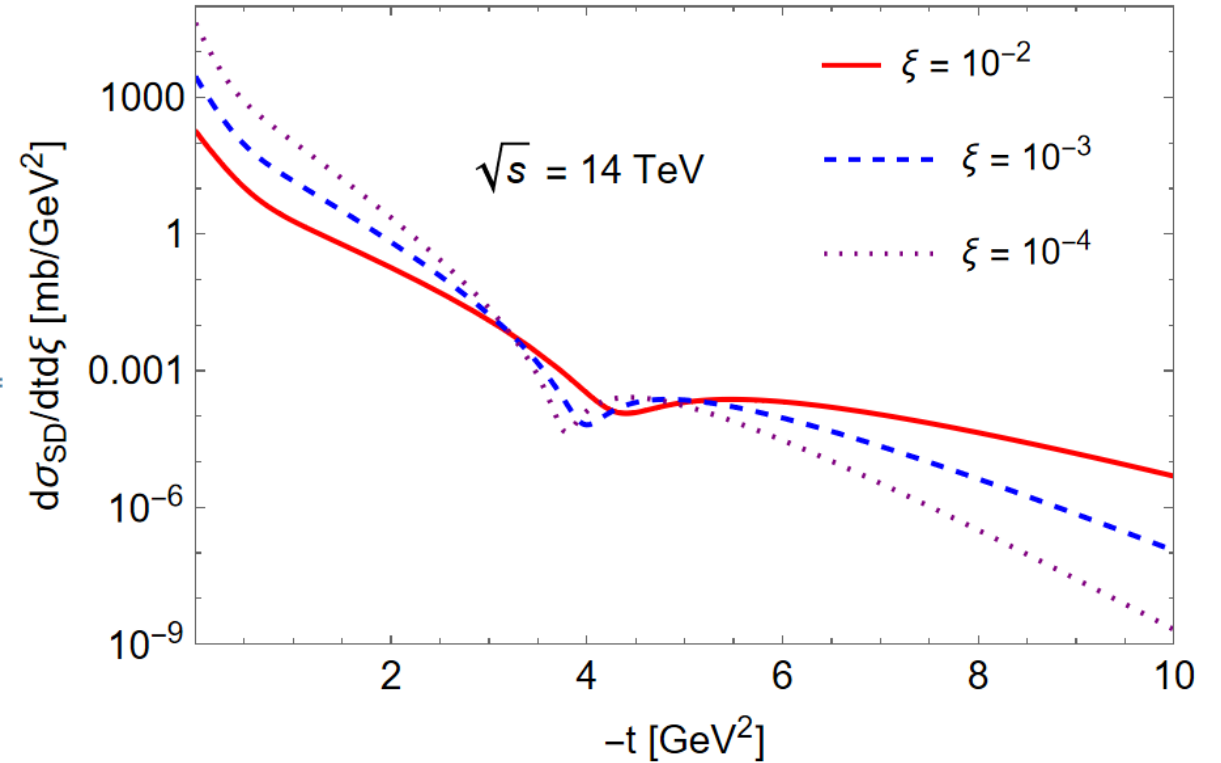
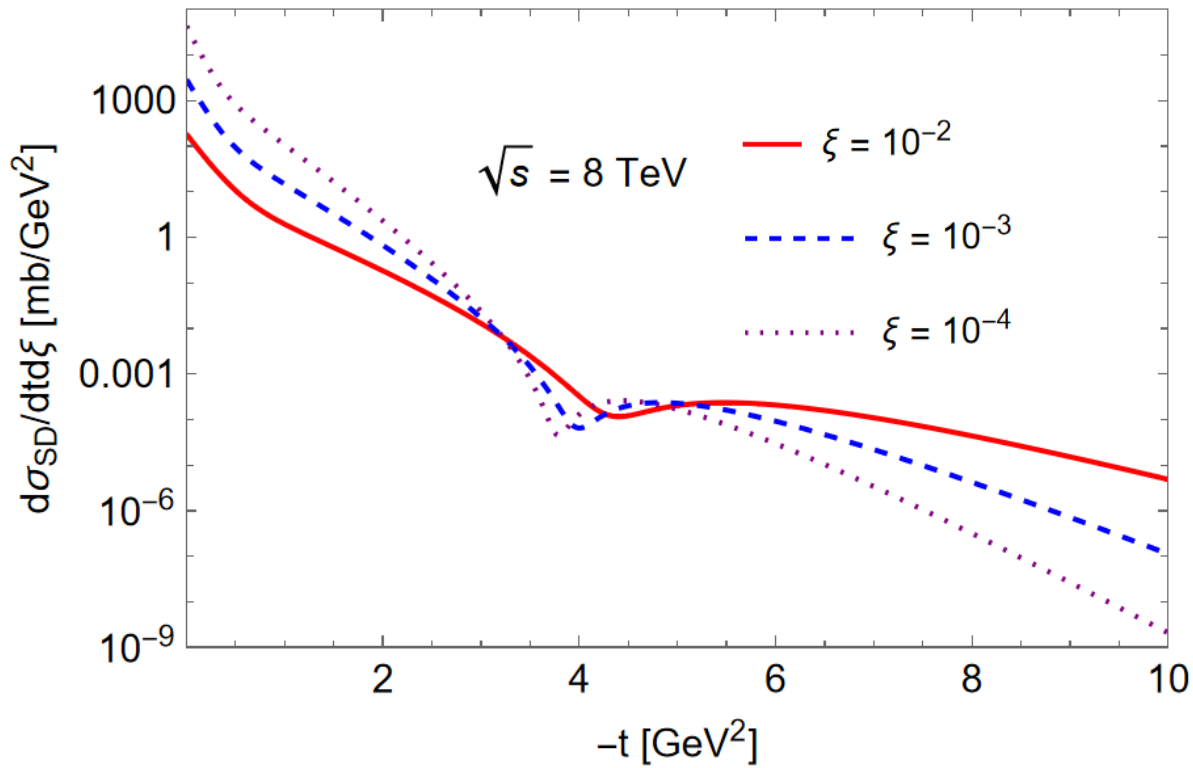
- dip-bump structure is predicted in SD process and it is resulted from a dipole odderon contribution
- as the M^2 rises the slope of the t distribution decreases and the position of the dip-bump structure goes to higher $-t$ values
- interesting to check experimentally if such a dip-bump structure is present in the SD process

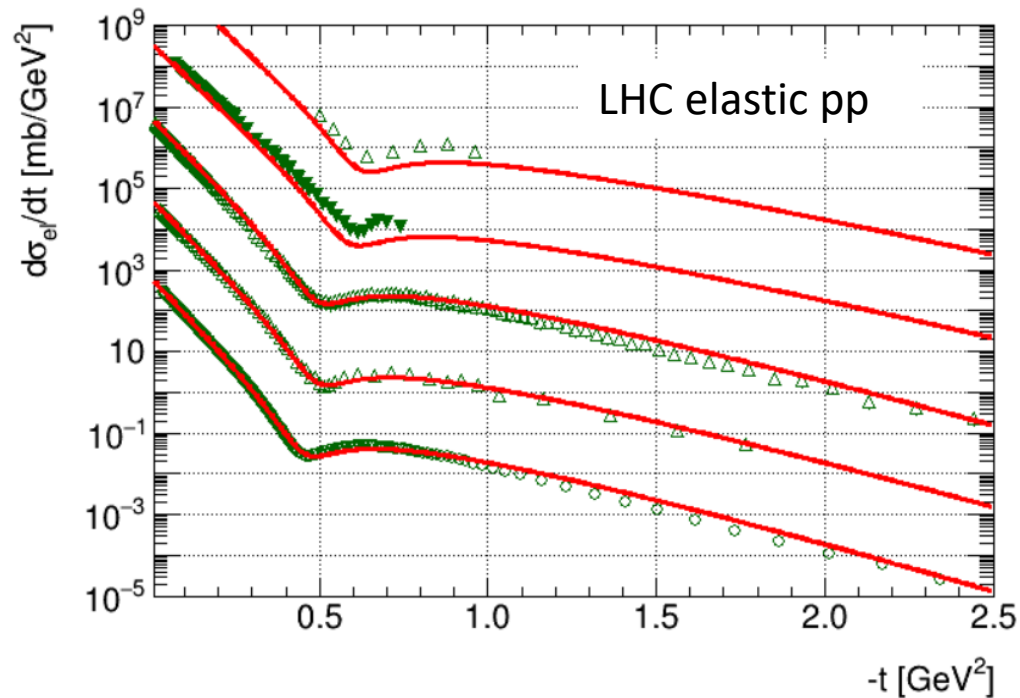
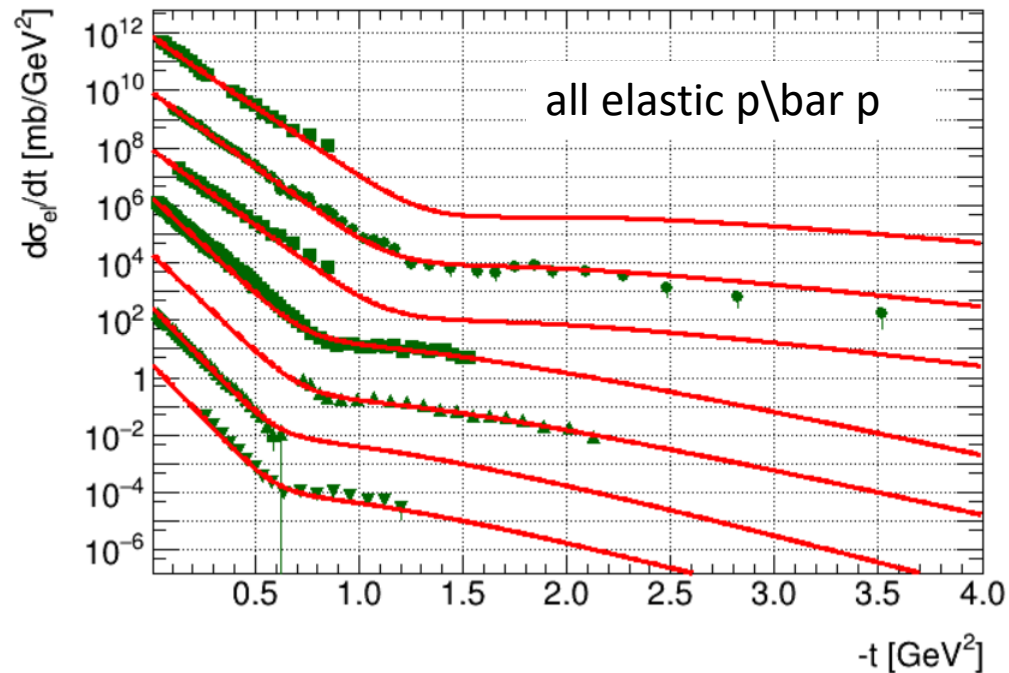
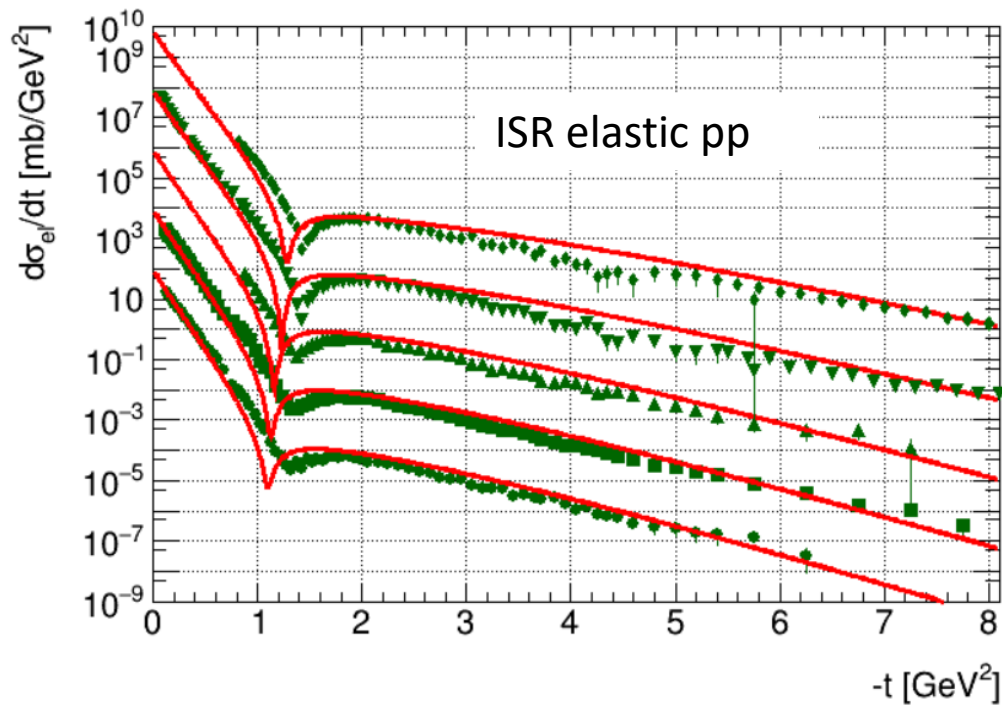
Thank you for your attention!



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t and ξ dependence of the SD process at LHC energies





Pomeron

$\delta_p = 0.04677 \pm 0.00004$
 $\alpha_{1p} = 0.4144 \pm 0.0002$
 $\alpha_{2p} = 0.0000$ (fixed)
 $a_p = 2.2488 \pm 0.0036$
 $b_p = 5.5835 \pm 0.0139$
 $\epsilon_p = 0.0604 \pm 0.0005$
 $s_{0p} = 1.0001 \pm 0.0003$

Odderon

$\delta_o = 0.28606 \pm 0.00013$
 $\alpha_{1o} = 0.1745 \pm 0.0001$
 $\alpha_{2o} = 0.0000$ (fixed)
 $a_o = 0.0202 \pm 0.0001$
 $b_o = 0.4015 \pm 0.0013$
 $\epsilon_o = 1.0036 \pm 0.0000$
 $s_{0o} = 2.7211 \pm 0.0038$

f-reggeon

$\alpha_{0f} = 0.6869$ (fixed)
 $\alpha_{1f} = 0.8400$ (fixed)
 $a_f = -15.4042$ (fixed)
 $b_f = 4.7842$ (fixed)
 $s_{0f} = 1.0000$ (fixed)

ω -reggeon

$\alpha_{0\omega} = 0.4380$ (fixed)
 $\alpha_{1\omega} = 0.9300$ (fixed)
 $a_\omega = 9.6945$ (fixed)
 $b_\omega = 3.5101$ (fixed)
 $s_{0\omega} = 1.0000$ (fixed)

