

# *Quantum observables for colliders*

## *Workshop summary*

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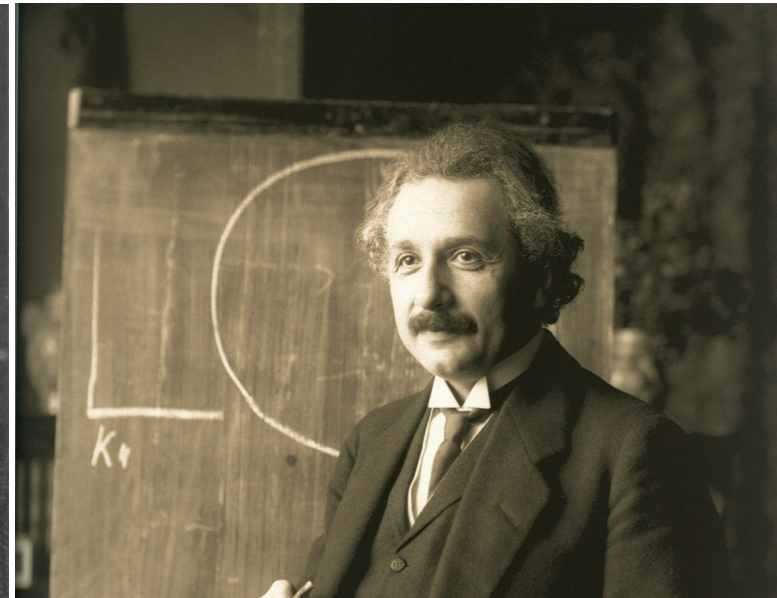
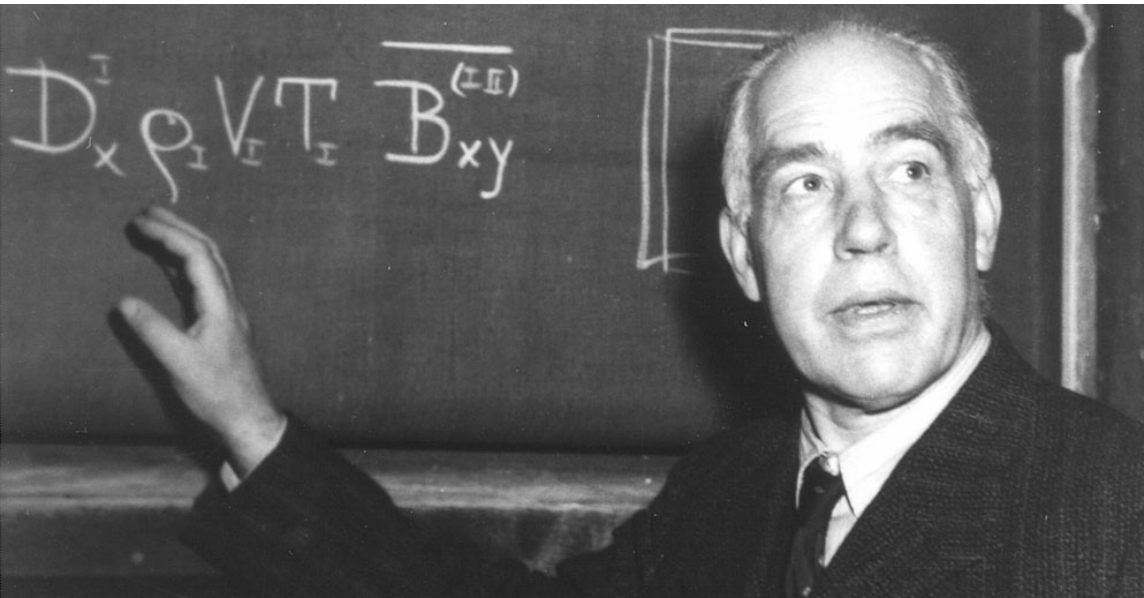
# GGI workshop quantum observables for HEP

49 participants, mixed theory-experiment, mixed QI-HEP, lots of lectures, some talks...

good attendance from ATLAS & CMS (>10), interest from Belle 2



# Foundations of quantum mechanics



Philosophical debate among founders of quantum mechanics (and hence modern physics)

**Einstein (and common sense):**  
Particles have properties

**Bohr (and quantum mechanics):**  
Quantum probabilities are all there is to know

1935: Einstein-Podolsky-Rosen thought experiment

## EINSTEIN ATTACKS QUANTUM THEORY

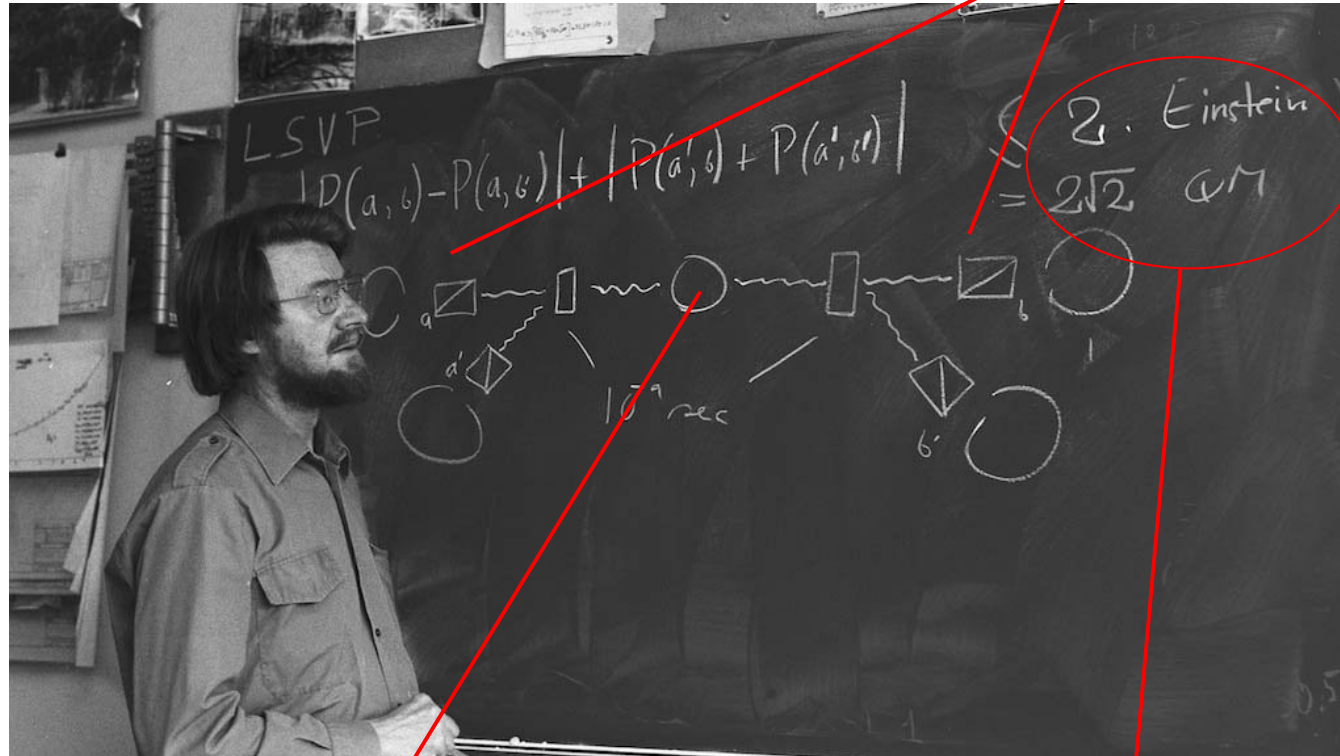
Scientist and Two Colleagues  
Find It Is Not 'Complete'  
Even Though 'Correct.'

SEE FULLER ONE POSSIBLE

Believe a Whole Description of  
'the Physical Reality' Can Be  
Provided Eventually.

# Bell-style experiments

Two well-separated & independent detectors



Source of quantum-correlated  
“entangled” photons

Outcome of the Bell tests decides between “Einstein”  
(local realistic theory with hidden variables) and  
“Bohr” (probabilistic interpretation of QM)

# Experimental quantum information

1970s-now: Aspect, Clauser, Zeilinger and many others designed and performed experiments that can test Bell inequalities

**The result: Bohr was right, Einstein and common sense were wrong**

A triumph of empirical science: settle a philosophical debate with an experiment

2022 Nobel prize “for experiments with entangled photons, establishing the violation of Bell inequalities and pioneering quantum information science”



© Nobel Prize Outreach. Photo: Stefan Bladh  
Alain Aspect  
Prize share: 1/3



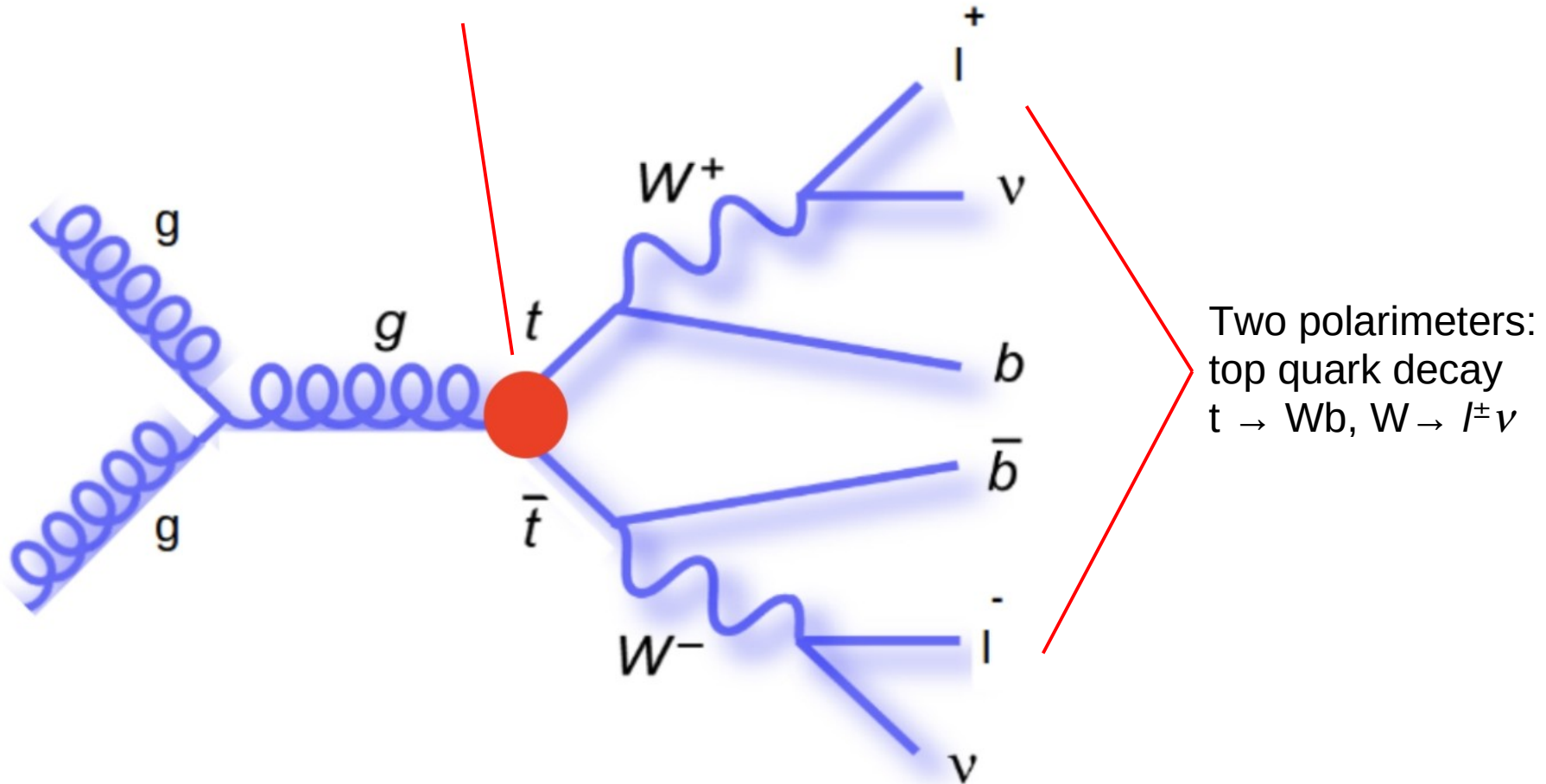
© Nobel Prize Outreach. Photo: Stefan Bladh  
John F. Clauser  
Prize share: 1/3



© Nobel Prize Outreach. Photo: Stefan Bladh  
Anton Zeilinger  
Prize share: 1/3

# High energy collisions

Source of entangled particles:  $pp \rightarrow t\bar{t}$



Entanglement: one calls a mixed state of two systems entangled if it cannot be written as a convex combination of product states...

Horodecki, Horodecki, Horodecki & Horodecki, RMP81 (2009), [arXiv](#)

# Quantum Information and High Energy Physics



2023: Several new results kick off new inter-disciplinary work:  
**“quantum information meets high energy physics”**

*Bell inequality, Go et al. (Belle), PRL99 (2007)*

*T-violation: Bernabeu et al., JHEP 08, Babar, PRL109 (2012)*

*Top quarks, arXiv:2311.07288, and soon CMS?*

*$B^0 \rightarrow J/\psi K^*$  @LHCb, Fabbrichesi et al., arXiv:2305.04982*

*Collider experiments can study quantum information in a unique high-energy environment with self-analyzing weak decays*

Lots of interest ([Oxford workshop](#), [GGI workshop](#))

## Alpinism analogy



In 1980, Reinhold Messner climbed Everest, solo, in alpine style, new route, without oxygen

This kicks off a new discipline in alpinism



## Alpinism analogy



In 1980, Reinhold Messner climbed Everest, solo, in alpine style, new route, without oxygen

And, of course, some people had to respond to the challenge!

Jerzy Kukuczka,  
same, but in winter

Andrzej Bargiel,  
same, but on skis

Harila, Nims,  
different, but fast

Pierre Carter,  
In parapente



# Alpinism analogy



In 1980, Reinhold Messner climbed everest, solo, in alpine style, new route, without oxygen

An anonymous dentist from Oklahoma...



Jerzy Kukuczka, same, but in winter

Andrzej Bargiel, same, but on skis

Harila, Nims, Jornet, different, but fast

Pierre Carter, In parapente



## **Where do we go next?**

What should we measure?

Which processes are promising?

What do we learn about the foundations of QM that's new?

Which techniques and ideas from QI can further the HEP programme?

# Lectures – everything quantum you need to know

**Lectures from J.I. Latorre, Michael Spannowsky, Pawel Horodecki, Stefano Carraza, Sofia Vallecorsa on several different aspects of “quantum meets HEP”**

- from proper blackboard lectures on foundations of QM to overview of activities in quantum computing of the CERN quantum initiative)

- also talks by Michal Eckstein, Juan de Nova, Ian Low, Alan Barr, etc. are highly recommended as didactic material.

- (nearly) everything is available

Youtube playlist:

<https://www.youtube.com/watch?v=gBhUpOd4TAQ&list=PL1CFLtxeIrQpAH1RGphax-xv7wSf-JM7o>

Videos linked on the GGI webpage:

<https://www.ggi.infn.it/showevent.pl?id=461>

INDICO:

<https://agenda.infn.it/event/34555/>

With a big thank you to Alessio Attardi

## Lectures – minimal or maximal entanglement

Discussion by both Ian Low and Jose Latorre whether nature picks maximum or minimum entanglement.

Entanglement suppression... <https://arxiv.org/pdf/1812.03138.pdf>

*“We conjecture that the suppression of entanglement is an important element of strong-interaction physics that is correlated with enhanced emergent symmetries”*

Maximal entanglement..., <https://arxiv.org/pdf/1703.02989.pdf>

*“QED couplings are found to be the solution to a MaxEnt principle [requiring maximum entanglement] once some global symmetries (C, P and T) are imposed”*

Numerology: Weinberg angle in SM is close to “optimal” choice of  $\theta_W = \pi/6$  (coincidence? or a deep hint from mother Nature?)

Paraphrasing Alan Barr:

*“In practice, entanglement is neither maximized nor minimized (exactly)”.*

# Lectures – physics beyond QM

Discussion by Michal Eckstein and Pawel Horodecki on physics beyond QM

Michal Eckstein: New Physics beyond QM, but assuming relativity. There might be a “Bell-like inequality” between QFT and QM.

Horodecki: freedom to perform any measurement is incompatible with universal laws of physics

<https://link.springer.com/article/10.1007/s10699-020-09711-y>

## The Experiment Paradox in Physics

Michał Eckstein<sup>1,2,3</sup>  · Paweł Horodecki<sup>4,5</sup>

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Horodecki points at “smart Bell inequalities” where QM touches “no signalling\*” bound.

*(\*) no-signaling principle: space-like separated parties cannot use the nonlocal correlations [of QM] to communicate superluminally.*

# Expert panel discussion

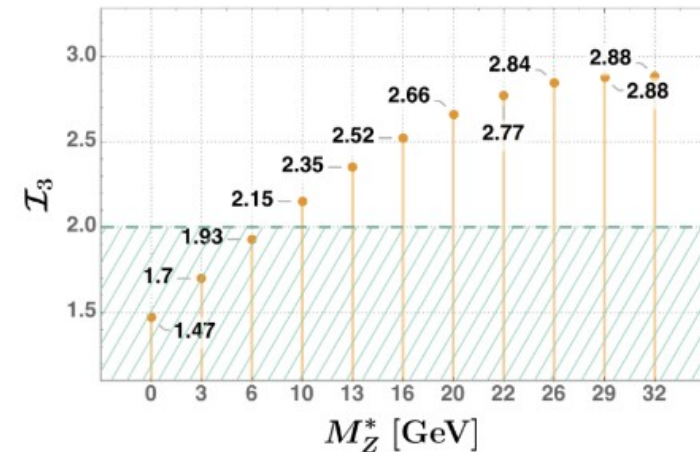
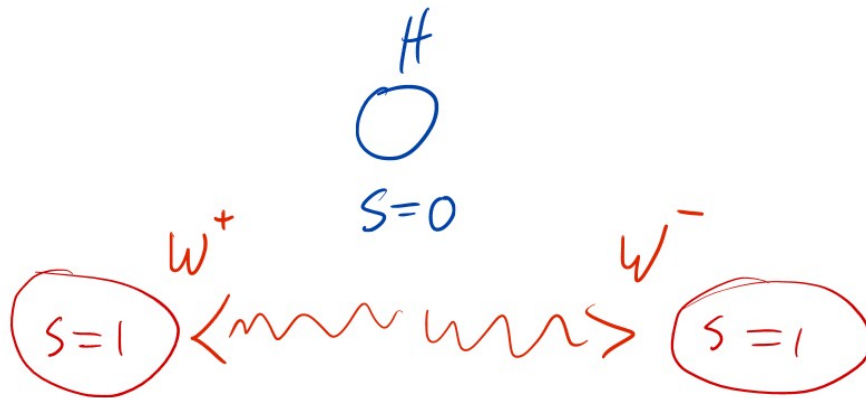
## Tests of Bell inequalities in systems with virtual particles ...

(raised by Alan Barr and picked up again in the theory panel discussion).

This is a nuisance ...

... or a unique possibility at colliders...

... in any case, it's inevitable in  $H \rightarrow ZZ, WW$ .



Optimised Bell Operator  
> 2?

Fabbrichesesi et al. 2302.00683

A virtual  $W$  or  $Z$  is still described by the same degrees of freedom and still a qutrit

## Pheno studies - non-tt

Slide from JA Aguilar

✓ Novel entanglement tests that were not possible before.

Also, tests with qutrits have only been performed with non-elementary objects. At LHC we have  $W$  and  $Z$  pairs in many processes:

▶ Higgs decays  $H \rightarrow WW$

Barr 2106.01377  
JAAS 2208.14033  
Fabbri, Howarth, Maurin 2307.13783

▶ Higgs decays  $H \rightarrow ZZ$

JAAS, Bernal, Casas, Moreno 2209.13441

▶ Electroweak production

Ashby-Pickering, Barr, Wierzychucka 2209.13990  
Fabbrichesi, Floreanini, Gabrielli, Marzola 2302.00683

▶ VBF

Morales 2306.17247

Also: Alexander Bernal & Luca Marzola,  $H \rightarrow ZZ$  with anomalous couplings, Erik Madge, new physics in di-boson production, arXiv:2307.09675

**Warning: pheno studies! Differing degrees of realism.**

2-3 sigma stat.-only in an idealized environment and for full HL-LHC is actually a NO!!!



# Loopholes

Marco Fabbrichesi and Dorival Gonçalves discussed loopholes at colliders

-- **detection loophole:** “if Alice and Bob measure only a small fraction of the emitted photons (or top quarks, or ...), correlations of the measurements may be unrepresentative. Problem avoided with detection efficiency  $> 60\text{-}80\%$ ”

Fabbrichesi: probably OK, as detection efficiency for energetic leptons is high  
experimentalists: we're not so sure, fraction of reconstructed tt events is small

-- **locality loophole:** “the choice of setting at a measurement site should not be able to influence the result of the other. Requires space-like separation between the two measurements.”

Fabbrichesi: OK for boosted tops and  $B \rightarrow \phi\phi$ , but not for tops at threshold

-- **free-will or setting independence loophole:** “the choice of setting at each measurement site must be freely chosen”

Most QI-experts: not OK, probably not possible to fix

**Conclusion: we're doing surprisingly well, maybe, but clearly collider experiments are not designed for Bell-type experiments...**

*Note from Juan de Nova: relevant for Bell tests, not for entanglement studies*

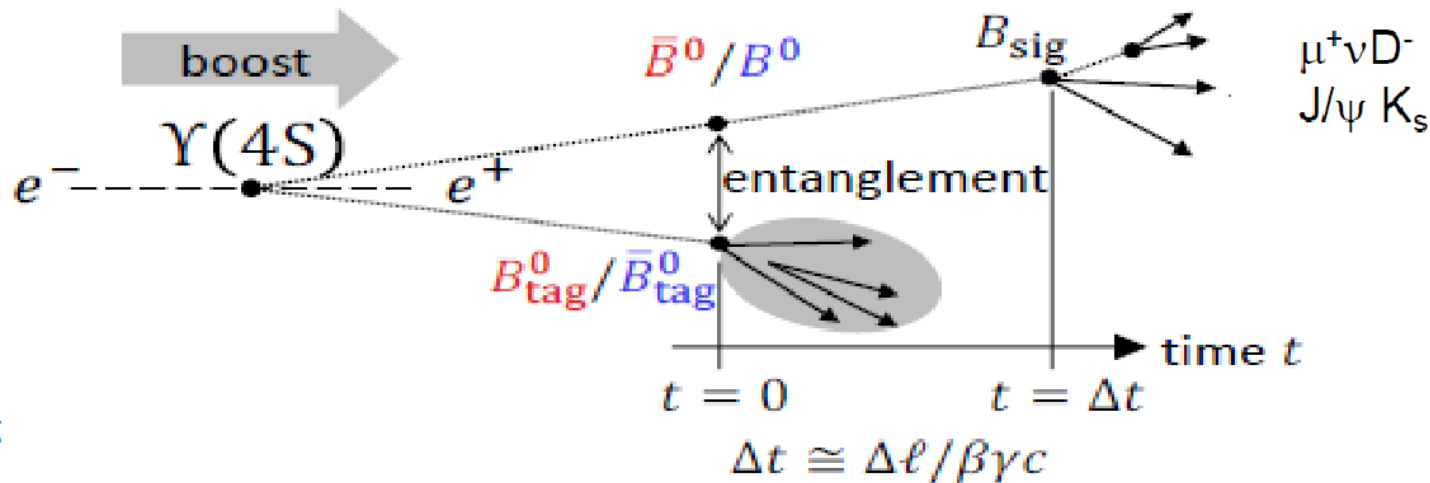
**Meanwhile, at the B-factories...**

## Meanwhile at the B-factories!!

Hans-Gunther Moser, Belle 2 decoherence studies,

Studies of CP violation assume entangled B-mesons from  $Y(4S)$ .

Decoherence (i.e. due to  $Y \rightarrow B^0\bar{B}^0\gamma$ , or... )  $\rightarrow$  systematic uncertainties.



-- First Bell test yielded  $S=2.8$  (cf.  $2\sqrt{2}$ )

A. Go & Chung Li, *quant-ph/0310192v1*.

However, short B life time leads to  $S=2.3$  even without quantum entanglement.

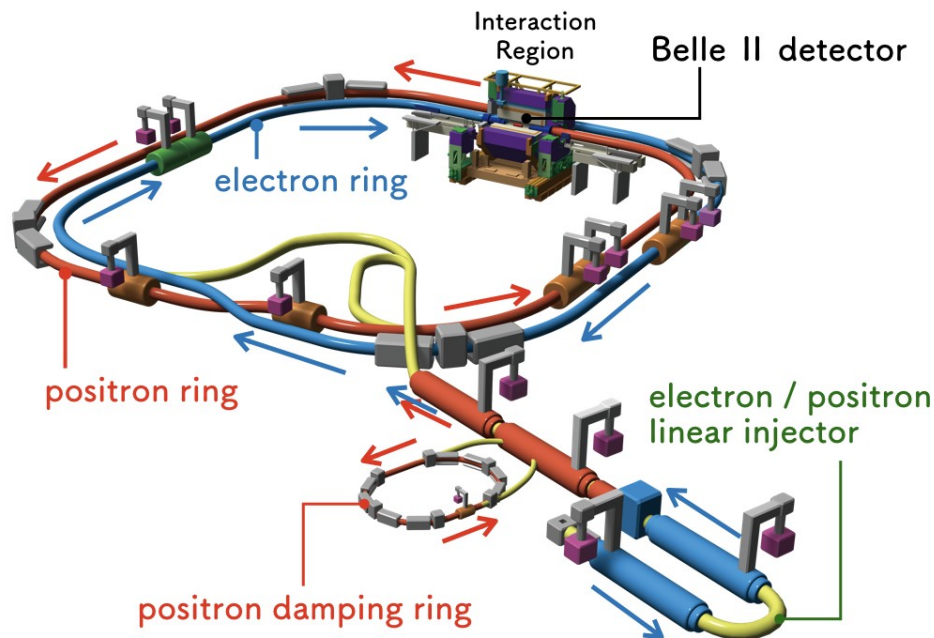
-- decoherence  $< 10\%$ , explicit local realistic Pompili & Selleri model discarded

A. Go & Belle, *PRL99 (2007) 131802*  $\rightarrow$

**Future:** Belle 2 needs to constrain decoherence better and can do Bell tests with Bs, constrain lifetime of first (tag)  $B^0$  better to avoid spurious correlations

# More from the B-factories (even if not from Belle 2 and LHCb)

*Christian Veelken projects potential of Belle 2 tau data,*  
400 M tau pairs without much background  
Tau polarization from hadronic channels  
Horodecki observable  $m_{12}$  = sum of 1st two eigenvalues



**Expected statistical significance  
of Bell inequality violation ~ 80  
standard deviations**

Full study needed, but missing  
experimental systematics expected  
to be small and a lot of margin!!

# More from the B-factories (even if not from Belle 2 and LHCb)

Emidio Gabrielli, Bell inequality violation in  $B^0 \rightarrow J/\psi K^*$ ,

Fabbrichesi et al., arXiv:2305.04982, based on  $B^0 \rightarrow J/\psi K^*$ ,  $J/\psi \rightarrow \mu\mu$ ,  $K^* \rightarrow K^+\pi^-$

Polarization amplitudes published by LHCb (arXiv:1307.2782)

$J/\psi K^*$  are spin 1  $\rightarrow$  qutrits  $\rightarrow$  CGLMP inequality:  $4 > I_3 > 2$  implies QM

## Observation of Bell inequality violation with collider data, in multiple decays

2305.04982 [hep-ph]

$0 < \text{von Neumann entropy} < \ln[3] \sim 1.1$

$$\mathcal{I}_3 = \text{Tr}[\rho \mathcal{B}]$$

	$\mathcal{E}$	$\mathcal{I}_3$	
• $B^0 \rightarrow J/\psi K^* (892)^0$ [5]	$0.756 \pm 0.009$	$2.548 \pm 0.015$	
• $B^0 \rightarrow \phi K^* (892)^0$ [20]	$0.707 \pm 0.133^*$	$2.417 \pm 0.368^*$	$\rightarrow 1.1\sigma$
• $B^0 \rightarrow \rho K^* (892)^0$ [21]	$0.450 \pm 0.067^*$	$2.208 \pm 0.129^*$	$\rightarrow 1.6\sigma$
• $B_s \rightarrow \phi\phi$ [22]	$0.734 \pm 0.050^*$	$2.525 \pm 0.084^*$	$\rightarrow 6.2\sigma$
• $B_s \rightarrow J/\psi\phi$ [23]	$0.731 \pm 0.032$	$2.462 \pm 0.080$	$\rightarrow 5.8\sigma$

## What about the Higgs factory?

# What about Higgs factories?

## Mohammad Altakach

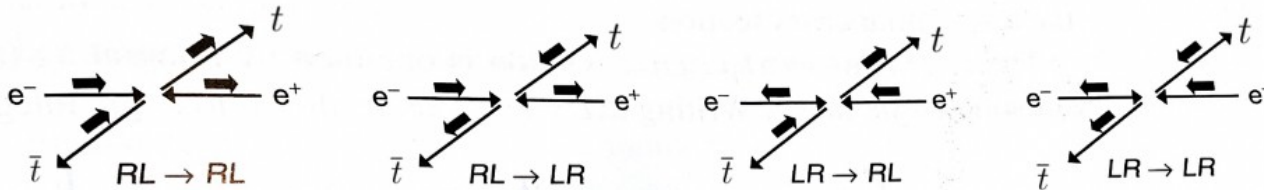
(with Lamba, Maltoni, Mawatari, Sakurai, *Phys.Rev.D* 107 (2023) 9, 093002)

- $H \rightarrow \tau\tau$  offers access to entanglement at ILC and FCCee
- Statistics is a problem: Bell inequalities marginal at FCCee, and worse at ILC (luminosity spectrum?)
- Fast simulation study, but ILD full-sim yields more promising CP results

## Alan Barr, private communication

(Alan Barr, Clelia Altamonte, *Quantum State-Channel Duality for the calculation of SM scattering amplitudes*)

- $e^+e^- \rightarrow t\bar{t}$  maps a two-qubits initial state onto a two-qubit final state



- beam polarization can be controlled at will  
(at linear colliders  $P(e^-)=80\%$ ,  $P(e^+)=30\%$  and LR, RL periods are foreseen, as well as short LL, RR)
- final-state top quark polarization can be measured
- Map out (at least parts of) Choi matrix

## Top quark pair production...



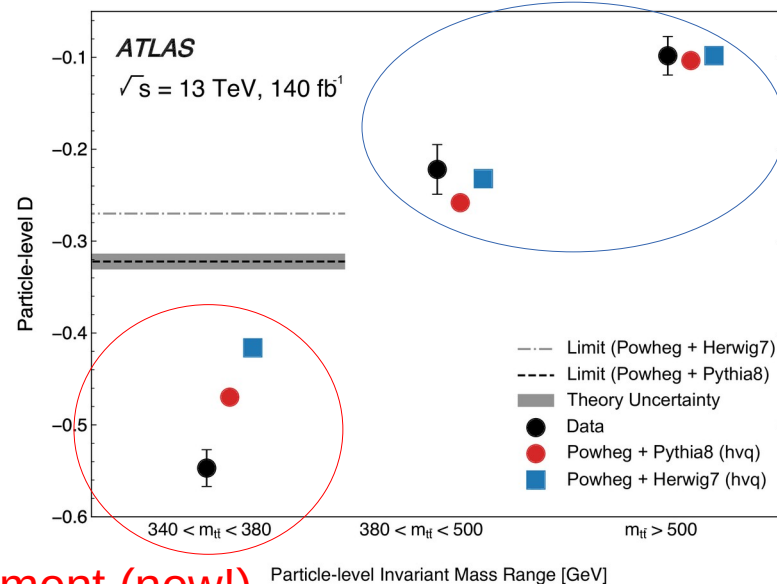
# Top quark pair production

ATLAS entanglement result  
(Jay Howarth@GGI, Ethan Lewis today)

ATLAS-CONF-2023-069  
→ now arXiv:2311.07288

CMS result was not ready in time for GGI  
(hopefully soon!)

Good old spin correlations (since 2013)

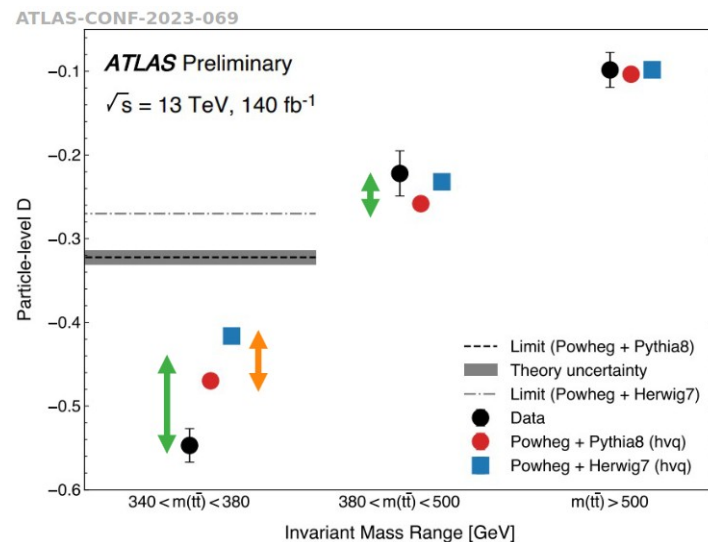


Entanglement (new!)

Claudio Severi: explanations for “ATLAS excess”.... (note: protest from ATLAS)

- Pseudo-bound-state with  $D=-1$   
-» must have pretty large strength
- EFT has difficulty to reproduce the pattern,  
-» A new scalar could work

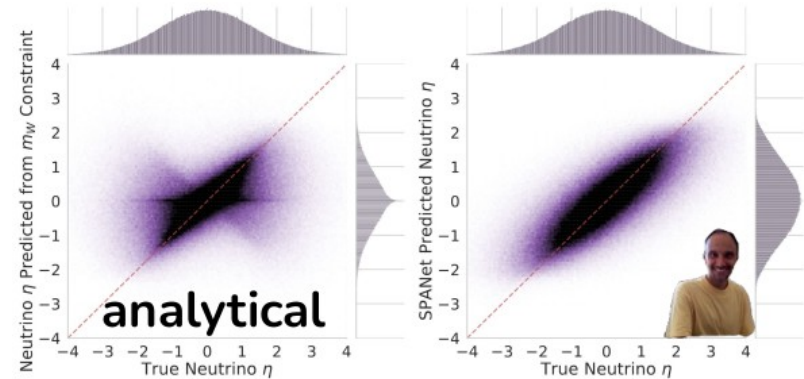
More on SM predictions and uncertainties later



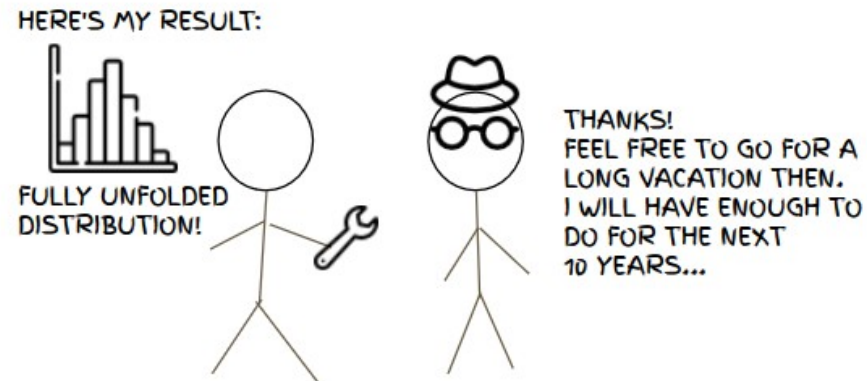
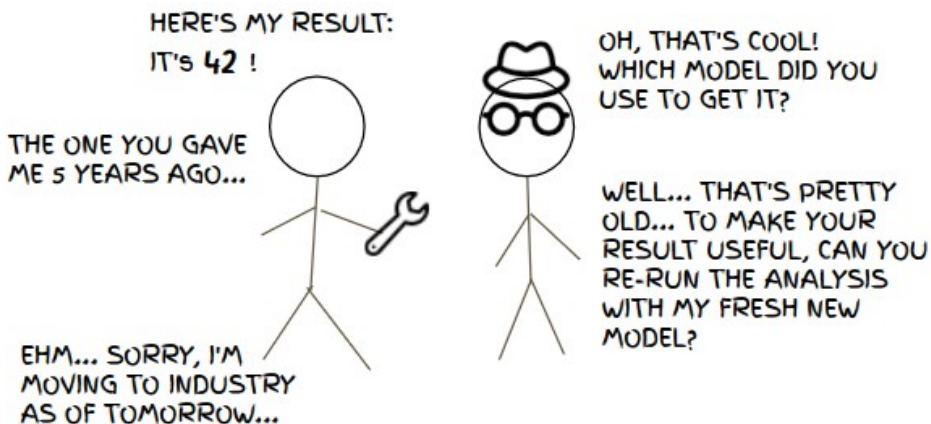
# Top-ics close to our heart

*Baptiste Ravine*: top reconstruction is key

Use ML for better tt reconstruction, or better selection of well-reconstructed events  
No need to develop ML; it's there already!



*Michele Pinamonti*: unfolding is key difference between Severi et al. (“Bell inequalities maybe at HL-LHC”) and Fabbrichesi et al. (“Bell inequalities already now”). Third opinion from Arthur Wu in the next talk.



# Monte Carlo modelling

*Eleni Vryonidou: MC and predictions for spin correlations*

*Top decay in Powheg-hvq and MadSpin performed with algorithm from Frixione et al., JHEP 0704, 081 (2007) [hep-ph/0702198]*

Label	$t\bar{t}$	$b\bar{b}4\ell$
Generator	hvq [20]	bb4l
Framework	POWHEG-BOX	POWHEG-BOX-RES
NLO matrix elements	$t\bar{t}$	$\ell^+ \nu_\ell l^- \bar{\nu}_l b \bar{b}$
Decay accuracy	LO+PS	NLO+PS
NLO radiation	Single	Multiple
Spin correlations	Approx.	Exact
Off-shell $t\bar{t}$ effects	BW smearing	Exact
$Wt$ and non-resonant effects	No	Exact
$b$ Quark massive	Yes	Yes

Jezo et al arXiv:1607.04538



NNLOxNNLO and EW corrections are small, virtual corrections somewhat larger:  
<https://arxiv.org/pdf/2008.11133.pdf> and <https://arxiv.org/pdf/2105.11478.pdf>

Lots of discussion on parton-level pseudo-top definition inside bb4l.

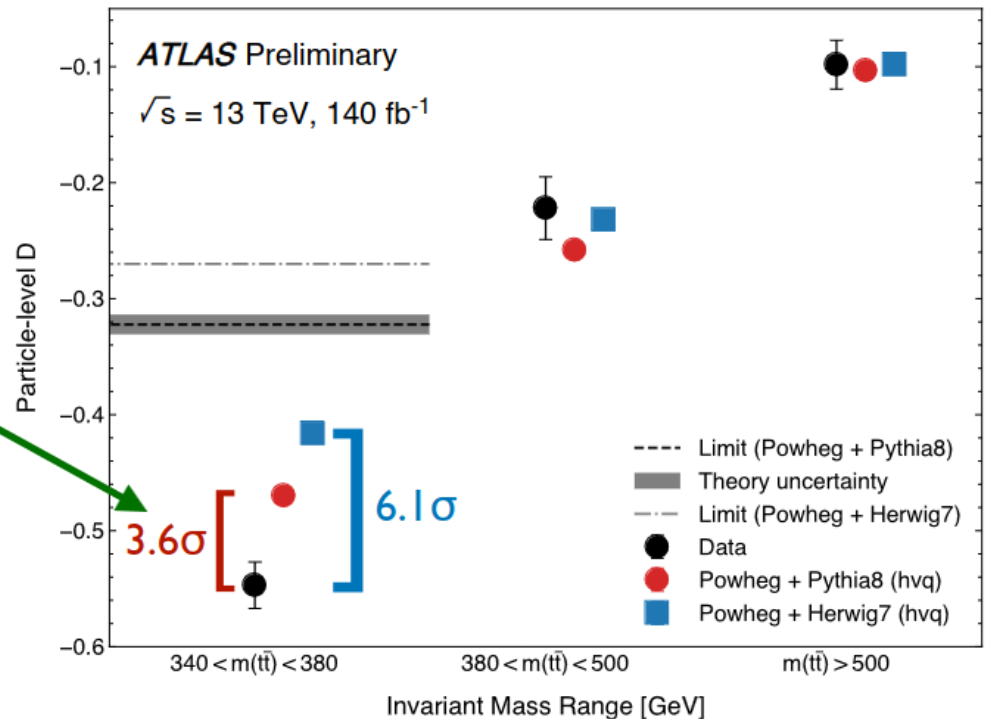
# Theory summary by J.A. Aguilar

☑ Last, but not least, entanglement measurements are quite demanding, and provide a **stress test** on our current understanding of

- theoretical modeling
- experimental systematic uncertainties

Example: ATLAS entanglement measurement

Even if ATLAS does not make such claim, everybody can see that predictions and measurement are quite off and digitise the plot



# Constructing the SM prediction

ATLAS provides Powheg-hvq+Pythia8 :  $D_{\text{particle}} = -0.47$  (with no uncertainty!!)

So, we can safely ignore SM uncertainties, now? NO!

ATLAS also gives Powheg-hvq + Herwig7 :  $D_{\text{particle}} \sim -0.41$  ( $\delta_{\text{PS}} \sim \pm 13\%$ )

And: Powheg-bb4l + Pythia8 differs by a similar amount: ( $\delta_{\text{ME}} \sim 10\%$ )

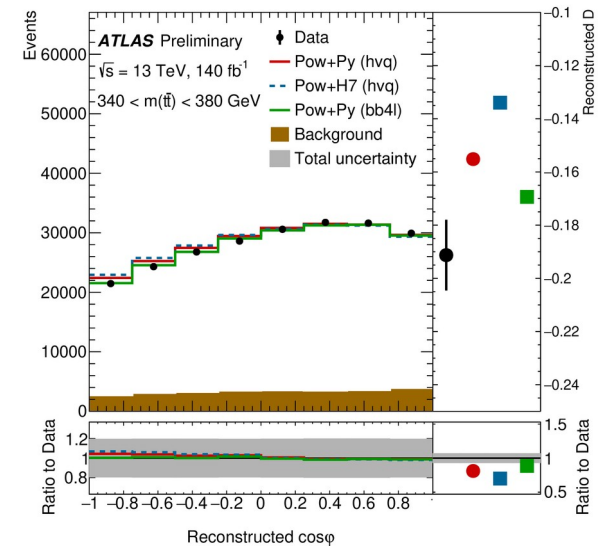
But, neither of these models includes pseudo-bound-state effects:

Assume 20% admixture with  $D = -1$  ( $\delta_{\text{BS}} \sim \pm 19\%$ )

My private best guess:

$D_{\text{particle}} = -0.47$  (but probably quite a bit lower)  
 $\pm 25\%$  (based on rough  $\delta_{\text{PS}} \oplus \delta_{\text{ME}} \oplus \delta_{\text{BS}}$ )

Taking into account SM uncertainty:  $D_{\text{ATLAS}} - D_{\text{SM}} < 1\sigma$



We need a better prediction before we can play the BSM game!

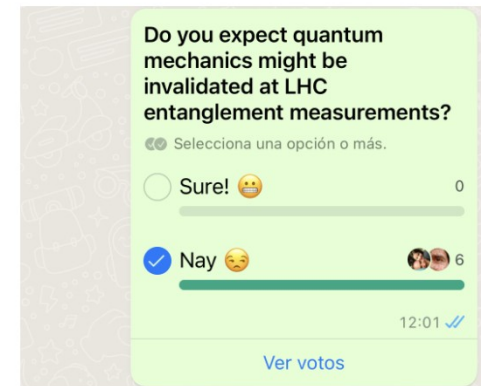
## Theory summary



The possibility of QM violation is interesting but does not give a **compelling argument** for a **sustained** theoretical / experimental effort

According to quick poll with a small sample, people are not very enthusiastic with the possibility of QM disproval at LHC...

A small and maybe not so representative sample of theorists expects ...



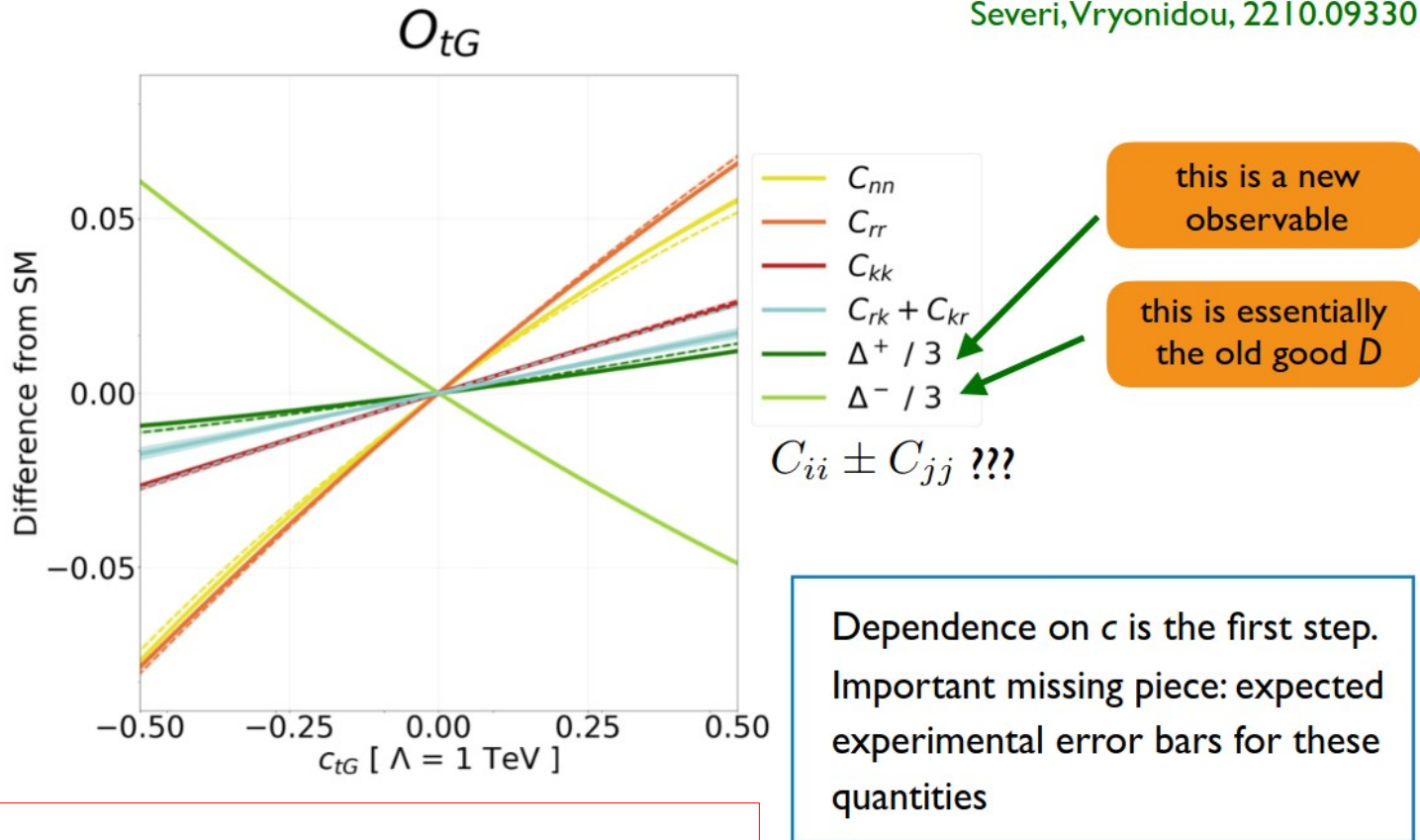
**Tests of Quantum Mechanics – the basis of everything we do – should of course be done, but I guess we’re warned NOT to expect any immediate surprises**

# Theory summary

BSM sensitivity of “quantum observables” is well-established (Maltoni, Severi, Vryonidiou & others)

$t$ -bar example: top chromomagnetic dipole operator

Severi, Vryonidiou, 2210.09330



JAAS

MV

Don't forget the theory uncertainty on the SM prediction; this may well be the bottle neck today.

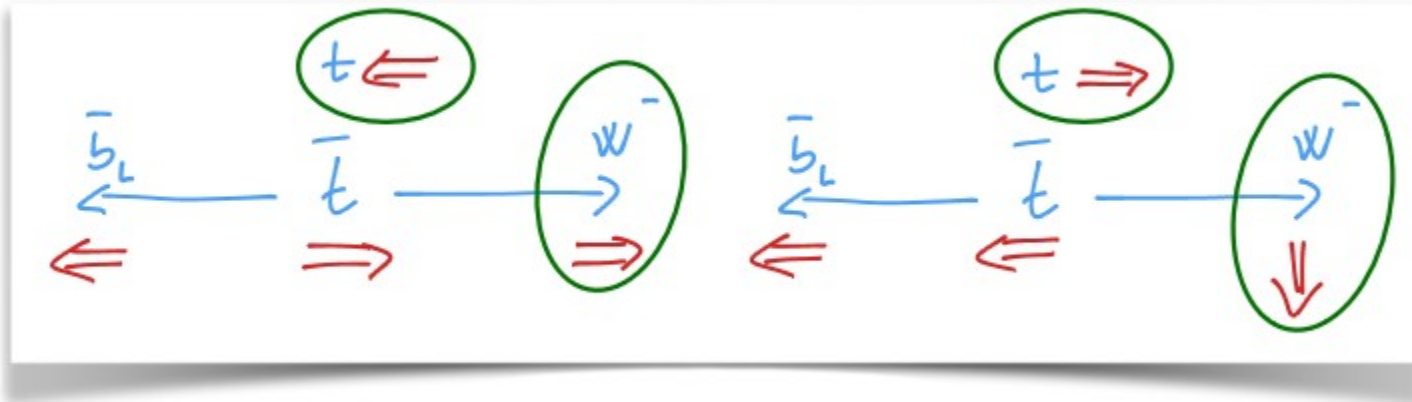
## What CAN we do that's NEW?

### What CAN we do in top quark pair production that's NEW?

-- entanglement and Bell inequality in boosted top quark pair production  
 (pheno to figure out optimal observable, channel, reconstruction...)

Gonçalves et al., arXiv:2305.07075 & Fabbri et al., 2307.13783 for l+jets)

-- measuring next decay  $tW$  entanglement (fermion bases; decay vs. measurement)



Enormous spin correlations. For example, at the LO [inclusively]

-- QI studies in  $ttW$ :

$$\begin{aligned} \rho_{ttW^+} = & \frac{1}{12} [1 - 0.83 \mathbb{1} \otimes \mathbb{1} \otimes T_0^2 + 0.88 t_0^1 \otimes t_0^1 \otimes \mathbb{1} \\ & + 0.2 (t_0^1 \otimes \mathbb{1} \otimes T_0^1 - t_1^1 \otimes \mathbb{1} \otimes T_{-1}^1 - t_{-1}^1 \otimes \mathbb{1} \otimes T_1^1) \\ & + 0.2 (\mathbb{1} \otimes t_0^1 \otimes T_0^1 - \mathbb{1} \otimes t_1^1 \otimes T_{-1}^1 - \mathbb{1} \otimes t_{-1}^1 \otimes T_1^1) \\ & - 0.2 (t_1^1 \otimes t_0^1 \otimes T_{-1}^2 + t_{-1}^1 \otimes t_0^1 \otimes T_1^2 + t_0^1 \otimes t_1^1 \otimes T_{-1}^2 + t_0^1 \otimes t_{-1}^1 \otimes T_1^2) \\ & - 0.88 t_0^1 \otimes t_0^1 \otimes T_0^2] \end{aligned}$$



three-particle measurements possible!



# Thanks

A big thanks, also on behalf of Fabio Maltoni, Andy Jung & Marco Fabbrichesi, to:

- **Stefania de Curtis and GGI staff**  
for hosting the workshop in beautiful Florence
- **Yoav Afik, Rafael Aoude, Federica Fabbri,**  
for organizing and running most of the sessions
- **all participants**  
for lively discussions, excellent talks, many new insights



BBC news 19 February 2015

# Conclusion



**There's a new game in town!**

**High-energy colliders as “quantum information laboratories”:**  
*experiments like ATLAS, CMS, LHCb and Belle 2 can study quantum information in a unique high-energy environment with self-analyzing weak decays*

***Join the fun! But try not to be the dentist!***