

# Study on measurement of cumulants of net-proton distributions for Au +Au collisions at $\sqrt{s_{NN}} = 7.7$ GeV in BES-II

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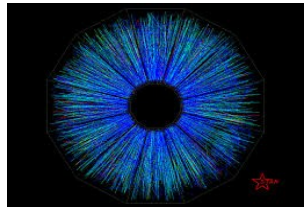
Supervisor: Prof. Bedangadas Mohanty

ALICE-STAR India collaboration meet  
24<sup>th</sup> Nov, 2023

National Institute of Science Education and Research, Bhubaneswar, India

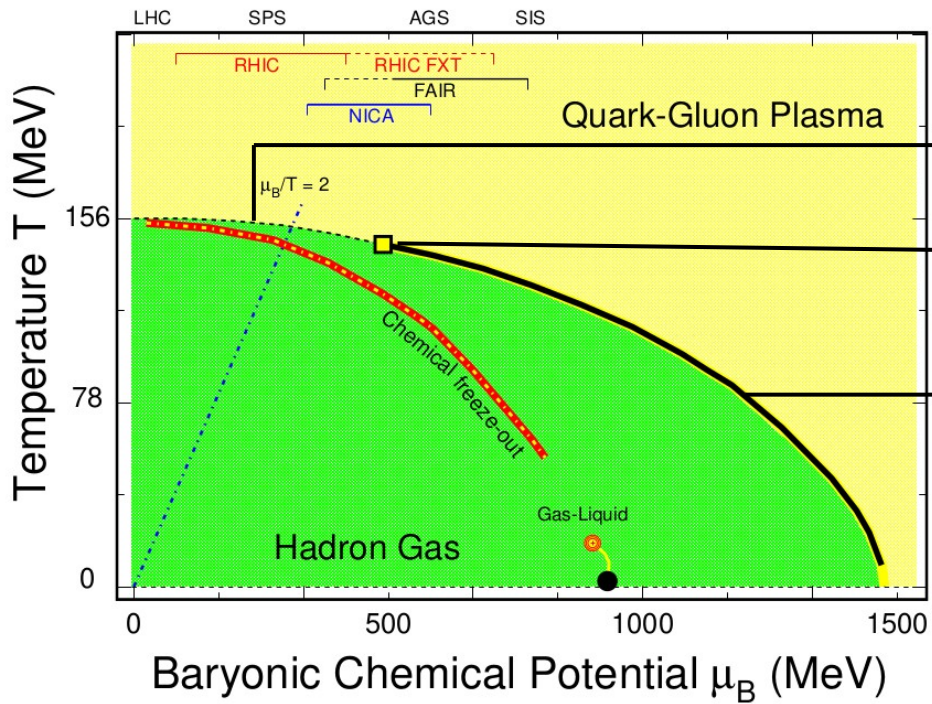
## Outline

- 1) Motivation
- 2) Observables
- 3) Previous results
- 4) Current Analysis status
- 5) Summary & Outlook



# Motivation

B. Mohanty, N. Xu, arXiv:2101.09210



✓ **Crossover transition (from Lattice QCD)**

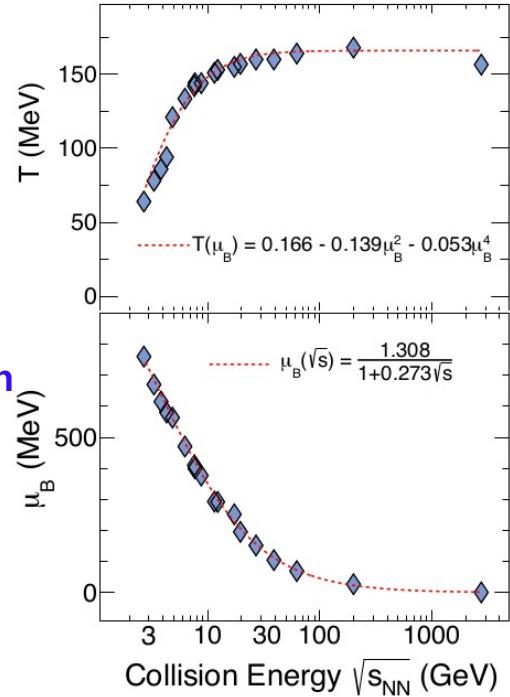
Y. Aoki et al, Nature 443 (2006) 675.

✓ **QCD critical point (CP)**

✓ **1st order phase transition (from models)**

S. Ejiri, Phys. Rev. D 78, 074507 (2008).

P. Braun-Munzinger, J. Stachel, Nature 448 (2007) 302



- **Goal:** To search for QCD critical point
- Varying collision energy varies Temperature (T) and Baryon Chemical Potential ( $\mu_B$ ).
- Fluctuation of conserved quantities are sensitive observable to study QCD critical point

# Observables

→ Higher order cumulants of net proton (proxy for net-baryon) distribution

$$C_1 = \langle N \rangle \quad \text{here, } \delta N = N - \langle N \rangle$$

$$C_2 = \langle (\delta N)^2 \rangle$$

$$C_3 = \langle (\delta N)^3 \rangle$$

$$C_4 = \langle (\delta N)^4 \rangle - 3 \langle (\delta N)^2 \rangle^2$$

$$C_5 = \langle (\delta N)^5 \rangle - 5 \langle (\delta N)^3 \rangle \langle (\delta N)^2 \rangle$$

$$C_6 = \langle (\delta N)^6 \rangle - 15 \langle (\delta N)^4 \rangle \langle (\delta N)^2 \rangle - 10 \langle (\delta N)^3 \rangle^2 + 30 \langle (\delta N)^2 \rangle^3$$

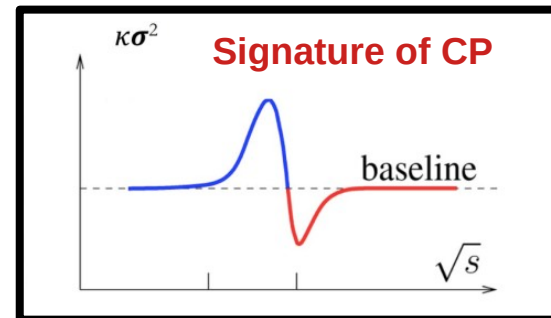
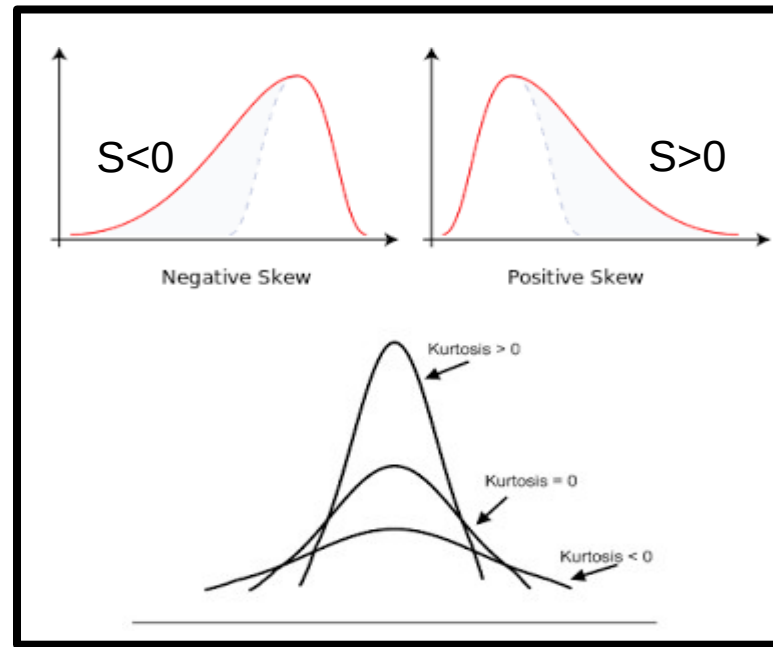
$$\frac{C_2}{C_1} = \frac{\sigma^2}{M} \quad \frac{C_3}{C_2} = S \sigma \quad \frac{C_4}{C_2} = \kappa \sigma^2 \quad M = \text{Mean}, \sigma^2 = \text{Variance}$$

$$S = \text{Skewness}, \kappa = \text{Kurtosis}$$

→ Higher order cumulants of net proton multiplicity distributions are sensitive observables for QCD critical point

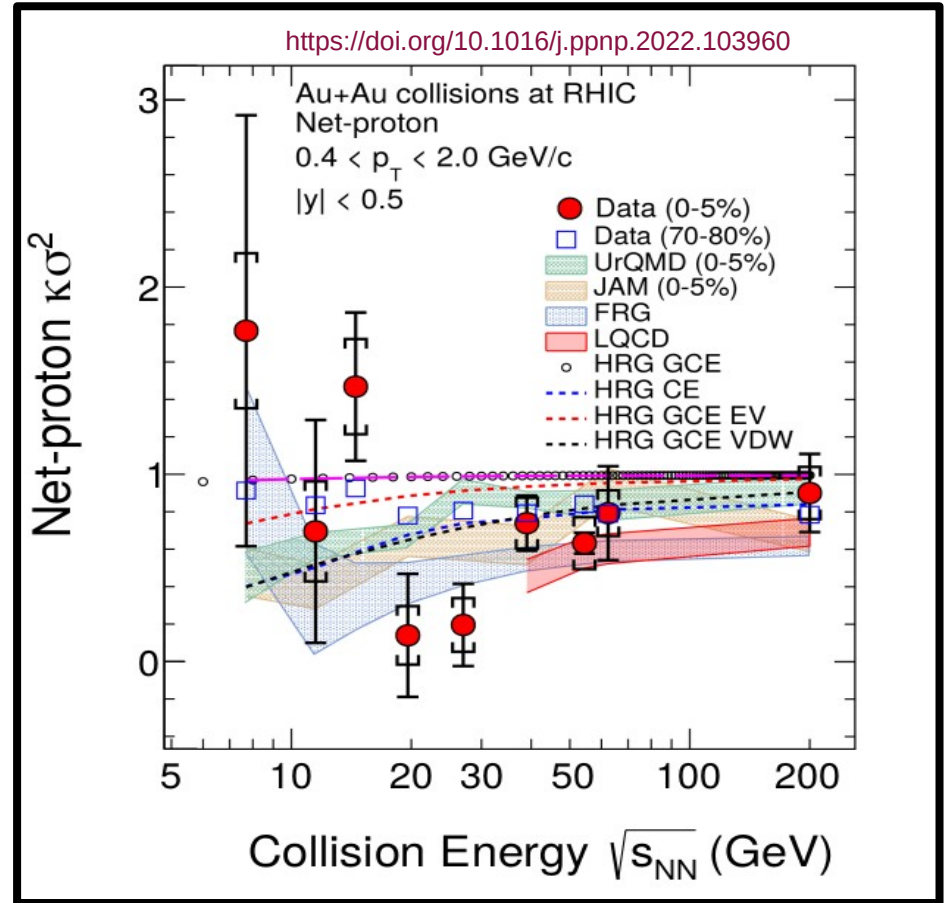
→ Related to correlation length  $C_2 \sim \xi^2$   $C_4 \sim \xi^7$

→ In presence of critical point: Non-monotonic collision energy dependence of  $C_4/C_2$

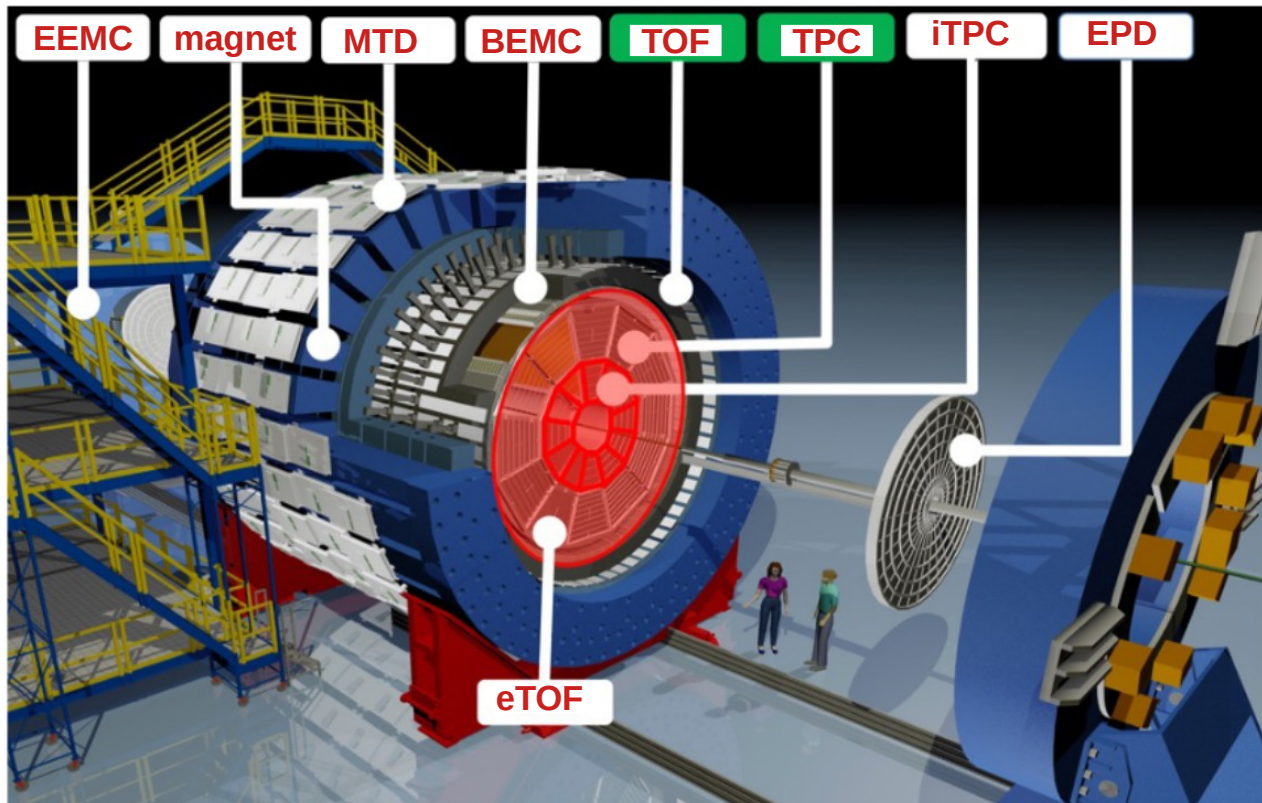


## Previous result from BES-I

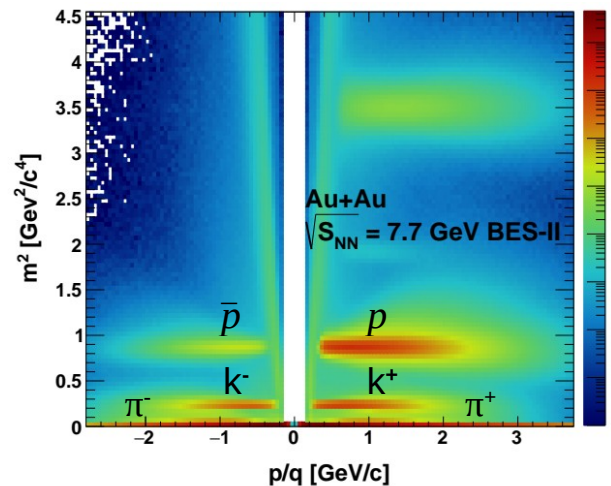
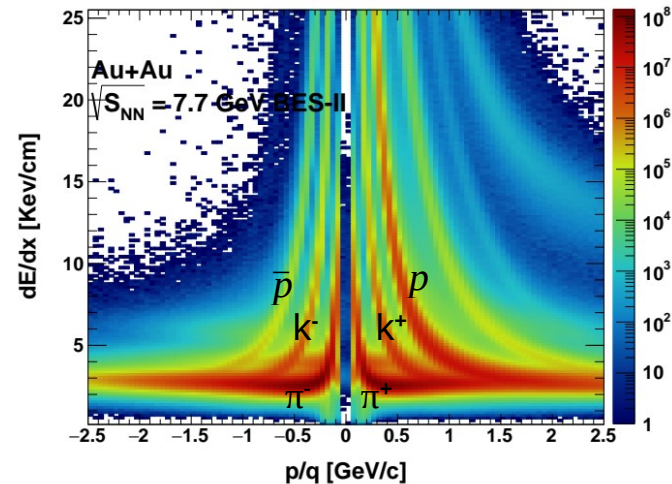
- Collision energy dependence of ratio of fourth to second-order cumulant of net-proton distribution (from BES-I) shown here
- Measurements are shown for 0-5% and 70-80% Au+Au collision centrality class as a function of various collision energies
- Non monotonic dependence over collision energy
- However at lower energy larger statistical uncertainty
- Analysis in BES-II needed for higher statistical precision
- Here we only focus on higher statistics data collected at 7.7 GeV collision energy in BES-II



# STAR Detector



- Two main detectors for current analysis: Time Projection Chamber & Time of Flight



## Analysis procedure

1/ Data set details

2/ Run-by-run Quality Assurance (QA)

3/ Event level QA

4/ Track level QA

5/ Bad event remove

6/ Centrality determination

7/ Analysis acceptance

8/ Cumulants result (efficiency uncorrected)

9/ Extended centrality \*

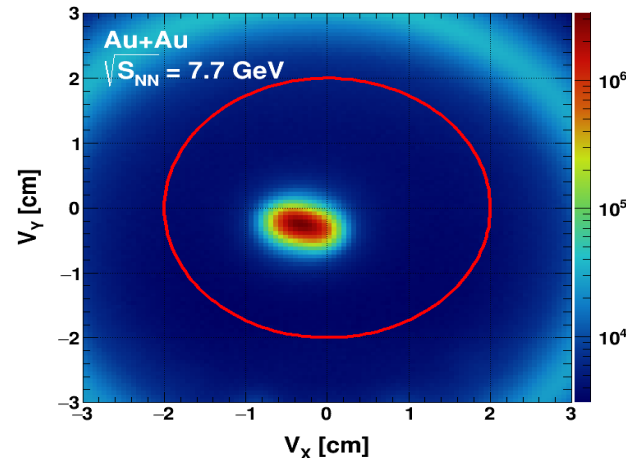
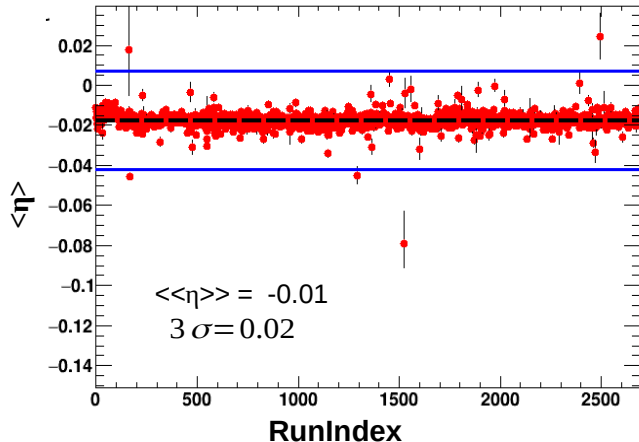
10/ Summary & Outlook

\* To improve on centrality resolution

# Data sets details

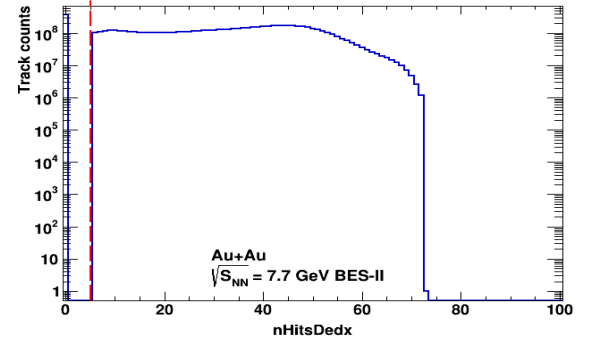
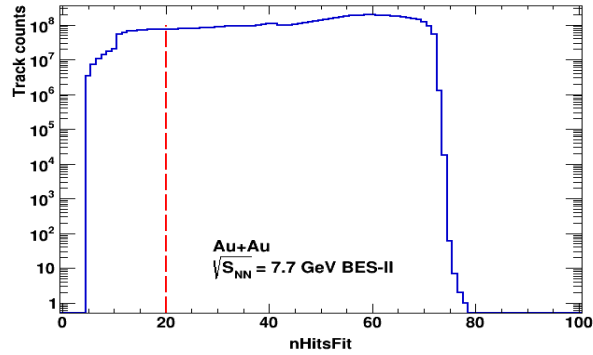
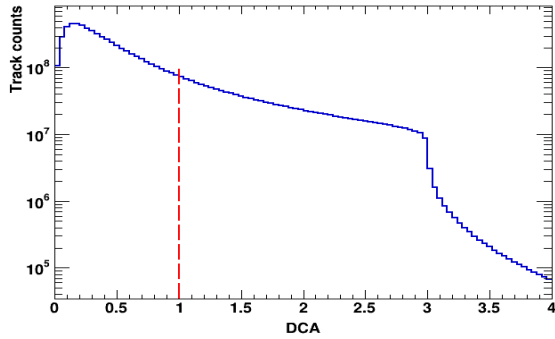
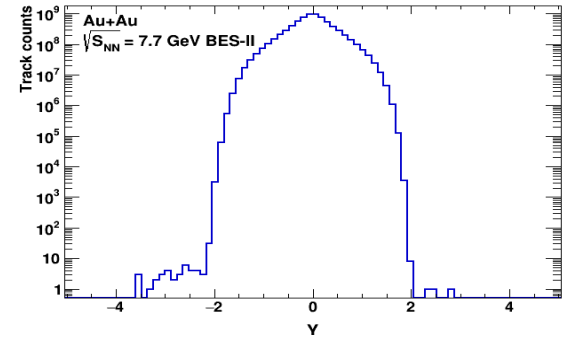
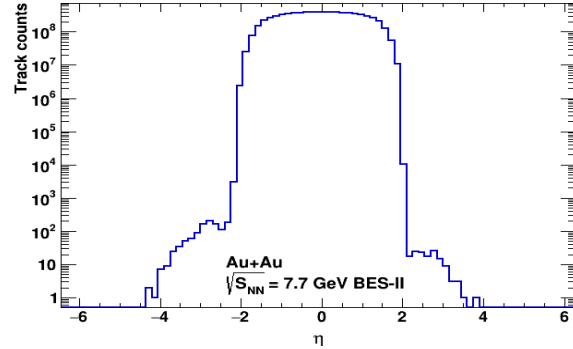
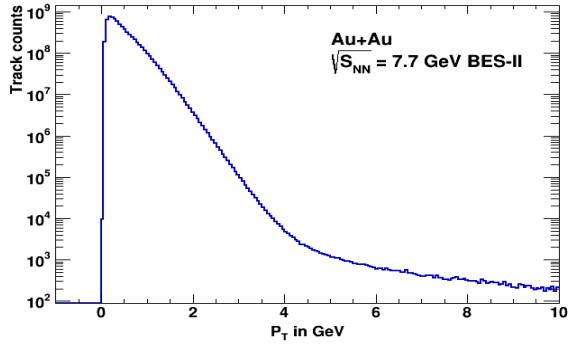
- Au + Au at  $\sqrt{s_{NN}} = 7.7$  GeV (BES-II)
- Run ID : 22031042 – 22121018 (total 2696 runs)
- Trigger ID : 810010,810020,810030 (minimum bias)
- Production tag : P22ia
- Total data size : 52 million events  
(with  $|V_z| < 50$  cm &  $V_r < 2$  cm)

## Run by run QA & event QA check



- $V_x$ ,  $V_y$ ,  $V_r$ , ZDC, tofmult, tofmatched,  $p_T$ , nhitsfit, nhitsdedx,  $n\sigma_p$  etc are also considered for QA check ==> 4.9 million events (379 bad run) excluded
- $|V_z| < 50$  cm &  $V_r < 2$  cm is used for event selection

# Track QA

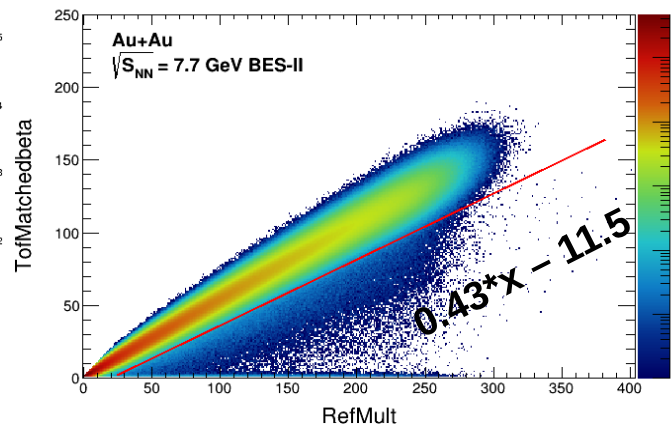
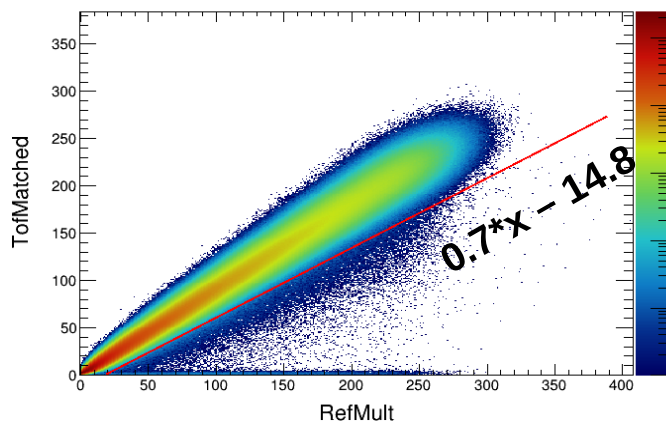


Track quality cut:

- $DCA < 1$
- $N_{hitsFit} > 20$
- $N_{hitsDedx} > 5$
- $n_{HitsFit}/(n_{HitsPoss}) > 0.52$



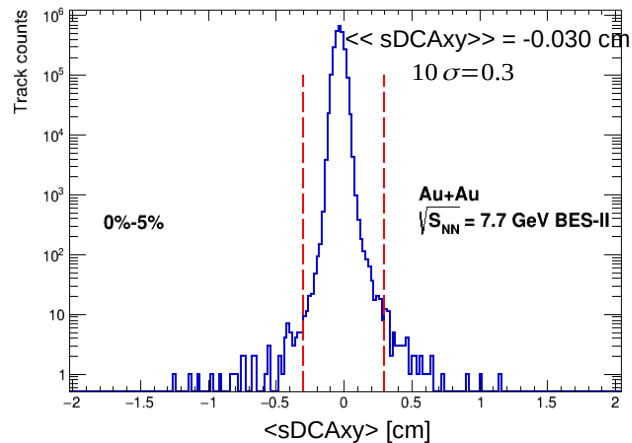
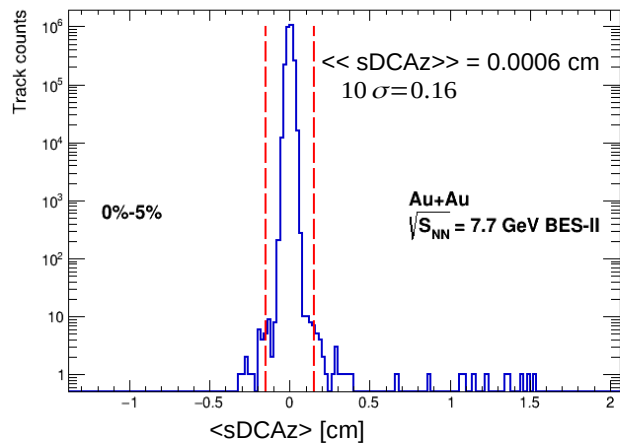
## Pileup event removal



- RefMult: Charge particle ( $|\eta| < 0.5$ )
- TofMatched : Number of tracks that matched TOF
- TofMatchedbeta: TofMatched with  $\beta > 0.1c$

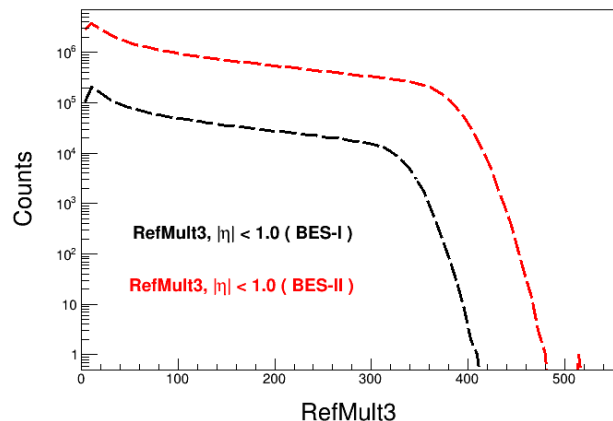
- Neglected those events below red line
- pileup events removed: 64,766 events

## Bad events from sDCAxy & sDCAz



- Obtain mean and sigma of  $\langle \text{sDCAz} \rangle$ ,  $\langle \text{sDCAxy} \rangle$  for 9 individual centrality
- Events 10 sigma ( $\sigma$ ) away from mean value are removed. **1524 events rejected**

## Centrality definition



- **Refmult3:** (Charge particle multiplicity with  $|\eta| < 1.0$  excluding protons and anti protons) distribution for centrality determination
- Compare with BES-I result

Centrality class (%)	0-5	5 - 10	10-20	20-30	30-40	40-50	50-60	60-70	70-80
RefMult3 cut (BES-I)	270	225	155	105	68	41	23	11	5
RefMult3 cut (BES-II)	307	254	173	116	74	45	26	13	6

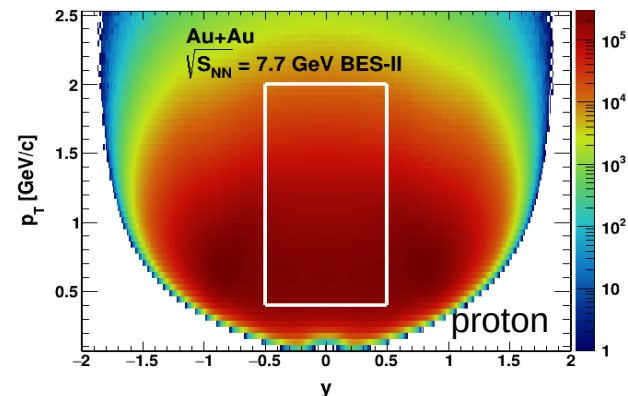
## Analysis cut

### Proton selection

- $|y| < 0.5$  &  $0.4 < p_T < 0.8$  GeV/c :  
TPC ( $|\ln\sigma_p| < 2$ )
- $|y| < 0.5$  &  $0.8 < p_T < 2$  GeV/c :  
TPC+TOF ( $|\ln\sigma_p| < 2$ ,  $0.6 < m^2 < 1.2$  GeV<sup>2</sup>/c<sup>4</sup>)

### Anti-proton selection

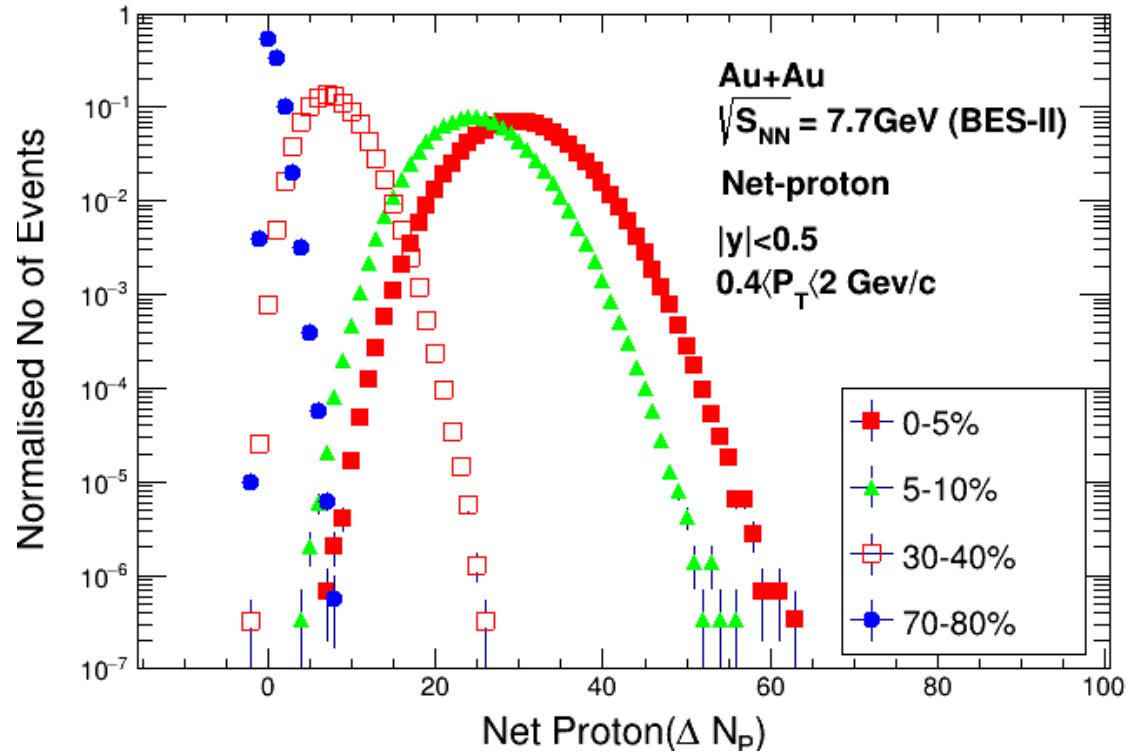
- $|y| < 0.4$  :  $0.4 < p_T < 0.7$  GeV/c use TPC  
( $-2 < n\sigma_p < 2$ )  
 $0.7 < p_T < 2.0$  GeV/c use TPC +TOF
- $0.4 < |y| < 0.5$  :  $0.4 < p_T < 0.7$  GeV/c use TPC  
( $-1 < n\sigma_p < 2$ )  
 $0.7 < p_T < 2.0$  use TPC + TOF



→ PID purity > 90%

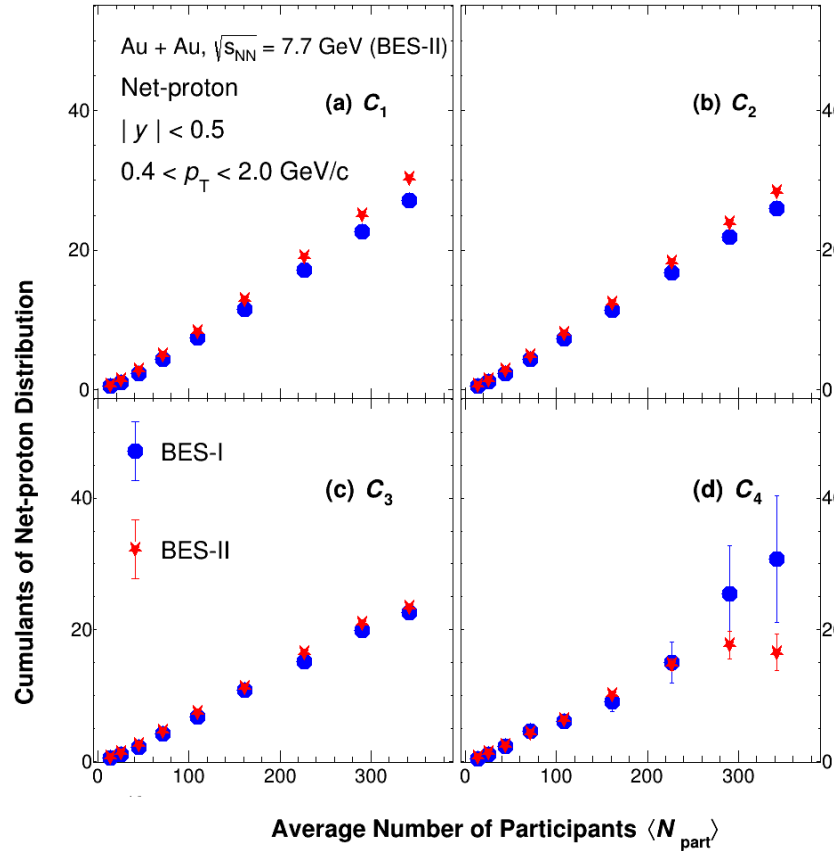
→ Good events: (45 million)

# Centrality dependence of net proton multiplicity distribution

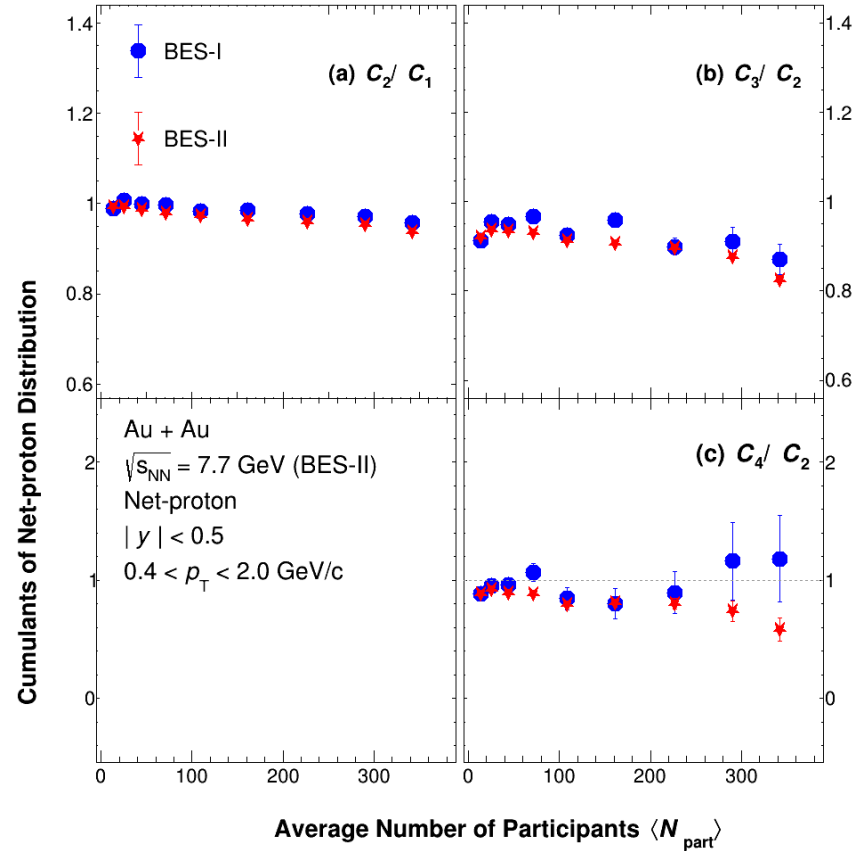


- Distributions are not corrected for proton and antiproton reconstruction efficiency in TPC and TOF.
- Mean & sigma of the distributions decreases from central to peripheral

# Centrality dependence of net proton cumulants (eff. uncorr.)

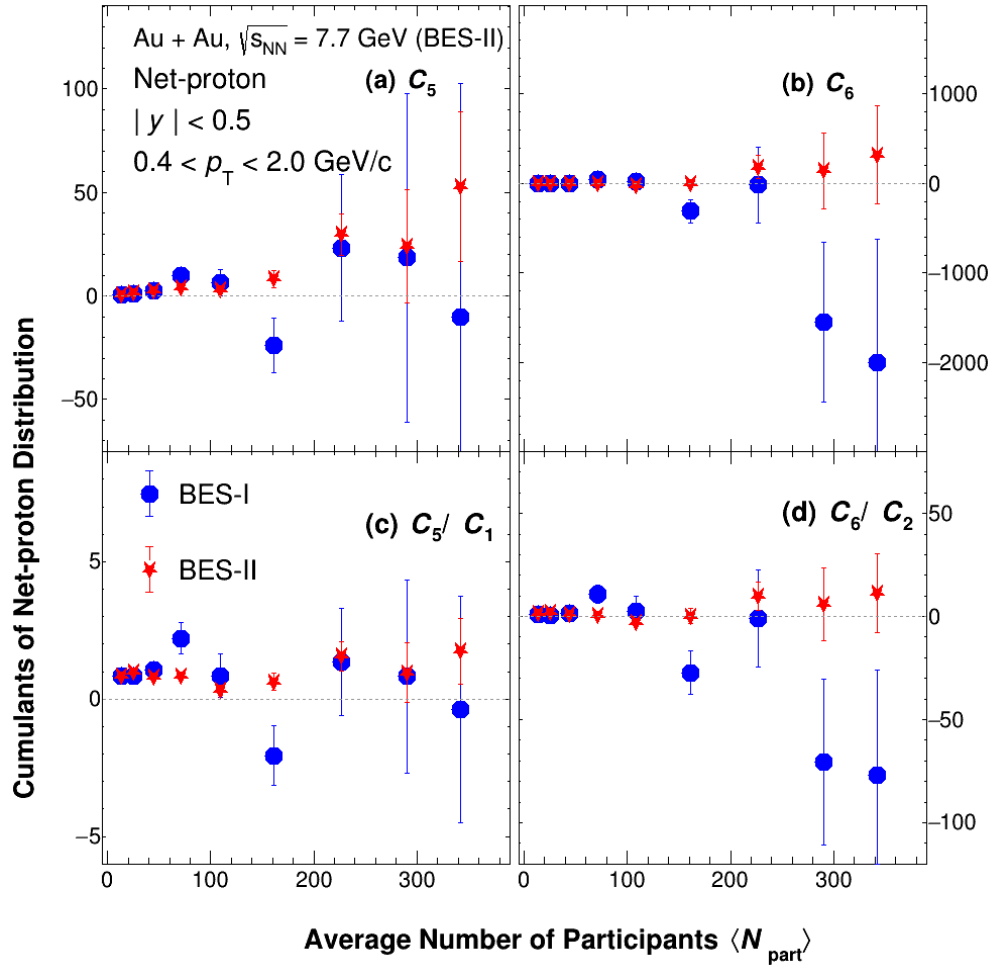


- Efficiency uncorr. cumulants
- Statistical error, obtained using bootstrap.
- Centrality bin width correction applied



- Increasing trend for cumulants as a function of centrality
- Cumulants ratios show weak dependence over centrality

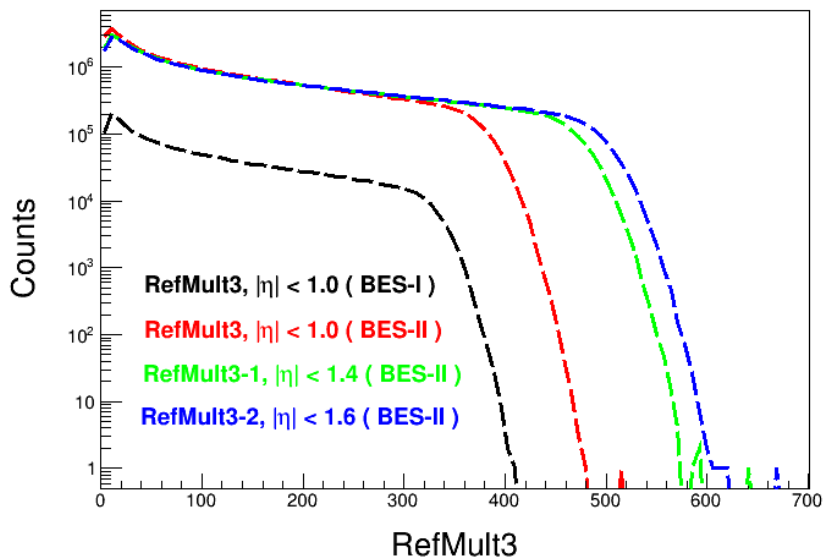
# Centrality dependence of net proton cumulants (eff. uncorr.)



- Efficiency uncorr. Cumulants
- Centrality bin width correction applied applied
- $C_5$  &  $C_5/C_1$  consistent within uncertainty
- $C_6$  &  $C_6/C_2$  (of BES-II) have values close to zero as compared to BES-I

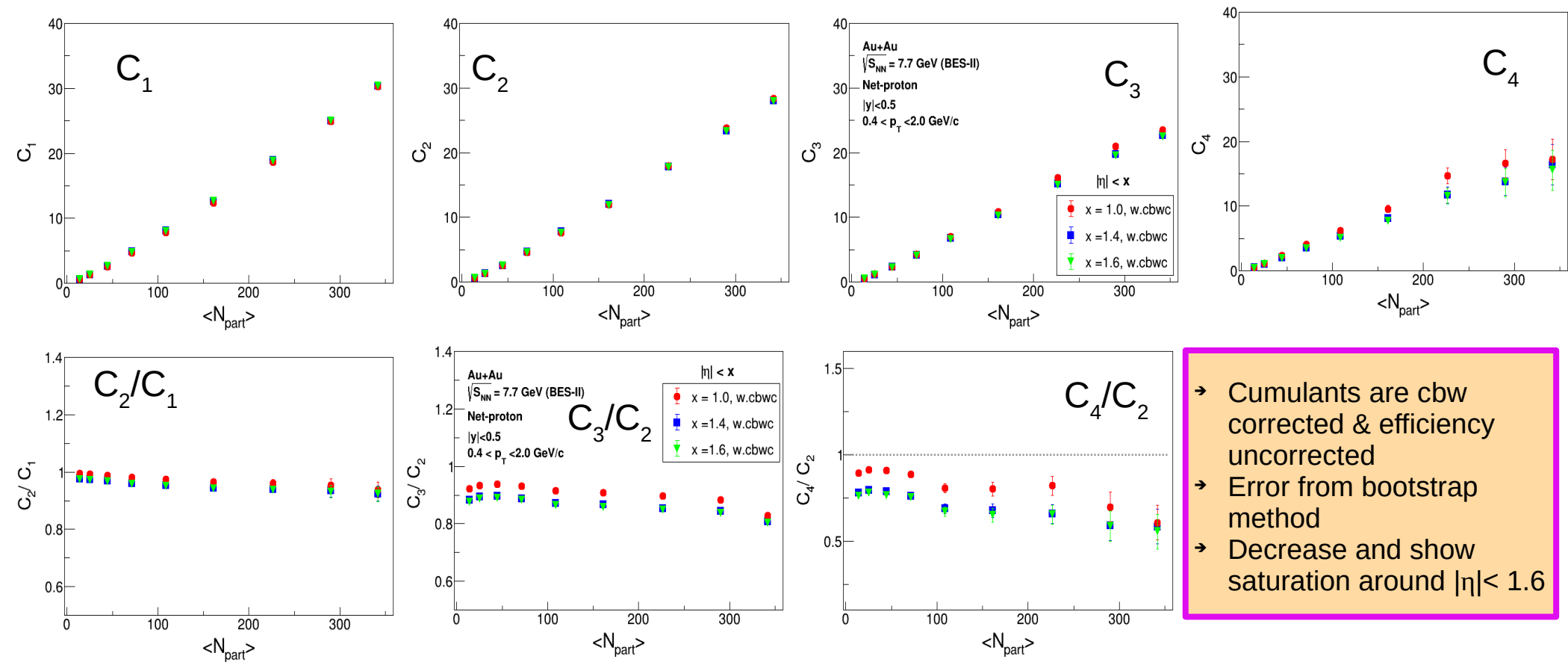
# Study the effect of different centrality definitions on net-proton cumulants

1. Three centrality definition :
  - RefMult3 (default) ( $|\eta| < 1.0$ )
  - RefMult3-1 ( $|\eta| < 1.4$ )
  - RefMult3-2 ( $|\eta| < 1.6$ )
2. Study centrality dependence of cumulants using these three centrality definitions.
3. Cumulants are efficiency uncorrected & CBW corrected



- RefMult3 distributions for three different definitions are plotted here
- Compare with BES-I result

# Centrality dependence of cumulants for different centrality definitions (efficiency uncorr.)



## Summary & outlook

1. Shown basic QA plots, centrality determination
2. Presented centrality dependence of efficiency uncorrected net proton cumulants upto sixth order
3. Good improvement in centrality resolution as we widen charge particle acceptance for centrality selection from  $|\eta| < 1.0$  to  $|\eta| < 1.6$ .
4. For centrality definition (7.7 GeV) we plan to take RefMult3-2 (with  $|\eta| < 1.6$ ) for better centrality resolution
5. Will focus on efficiency corrected net-proton cumulants
6. For my thesis I will work on 7.7 and 9.2 GeV data set in BES-II

## Acknowledgements

→ We thank the STAR focus group and STAR collaboration for opportunity and support.

**Thank You**



**Backup**

# CBWC

- $C_n = \sum_r w_r * C_{n,r}$        $C_n$  : is nth order cumulants
- $W_r = n_r / N$        $N_r$  : is number of events in rth refmutl3 bin
- **For error :**  $Err C_n = \sqrt{(\sum_r (W_r)^2 * (Err C_{n,r})^2)}$        $N$  : is total number of events

## Bootstrap method

- Bootstrap method is a re-sampling method to estimate statistical error
- Does not involve the complexities of the standard error propagation method
- It uses Monte-Carlo algorithm to estimate the statistical error

→ Construct B number of independent bootstrap samples  $X_1', X_2', X_3', \dots, X_B'$ , each consisting of n data points randomly drawn from the random sample X with replacement

→ Evaluate the estimator in each of these bootstrap samples:  $\hat{e}_b = \hat{e}(X_b')$        $b = 1, 2, 3, \dots, B.$

→ The sampling variance of the estimator:  $Var(\hat{e}) = \frac{1}{B-1} \sum_{b=1}^B (\bar{e} - \hat{e}_b)^2$       where,  $\bar{e} = \frac{1}{B} \sum_{b=1}^B (\hat{e}_b)$

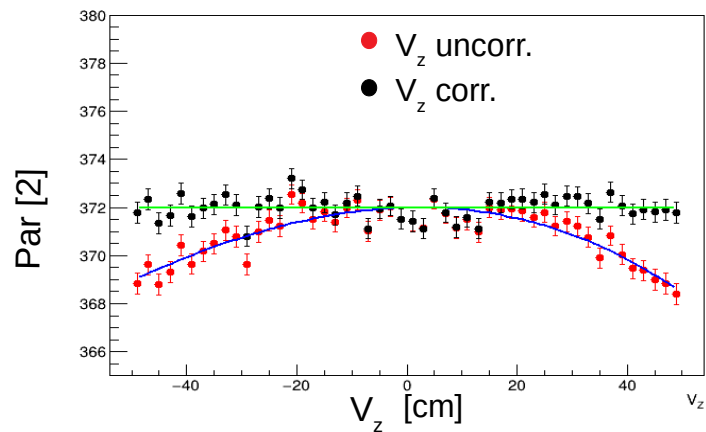
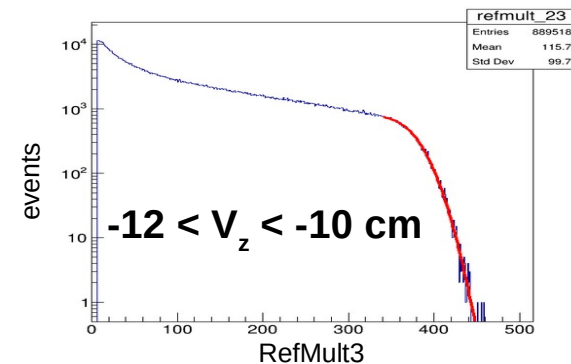
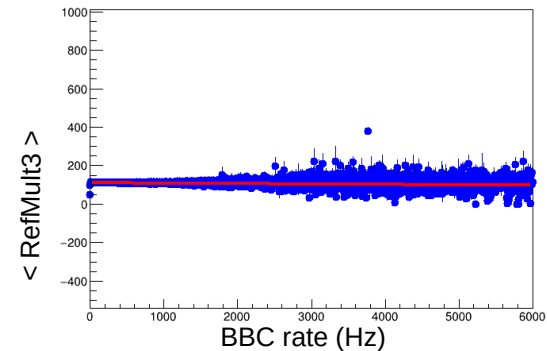
# Centrality Definition

→ **Refmult3:** (Charge particle multiplicity with  $|\eta| < 1.0$  excluding protons and anti protons) distribution for centrality determination

→ **Corr. to RefMult3:**

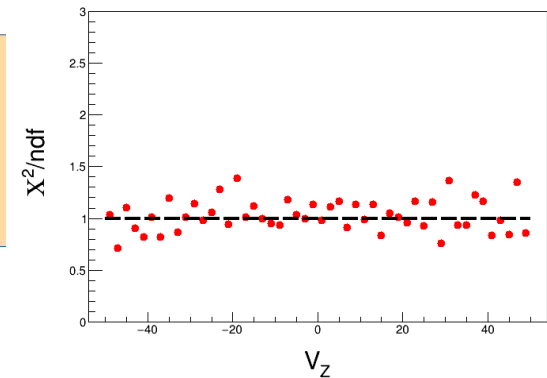
- has a negligible dependence on luminosity
- No luminosity corrections applied
- $V_z$  corrections applied

→ Refmult3 is obtained for each  $V_z$  window (2 cm for my analysis).  
 → Fit function:  $f(x) = [0] * \text{Tmath}::\text{Erf}(-[1]*(x-[2])) + [0]$   
 → After fitting par [2] is obtained for each  $V_z$  window

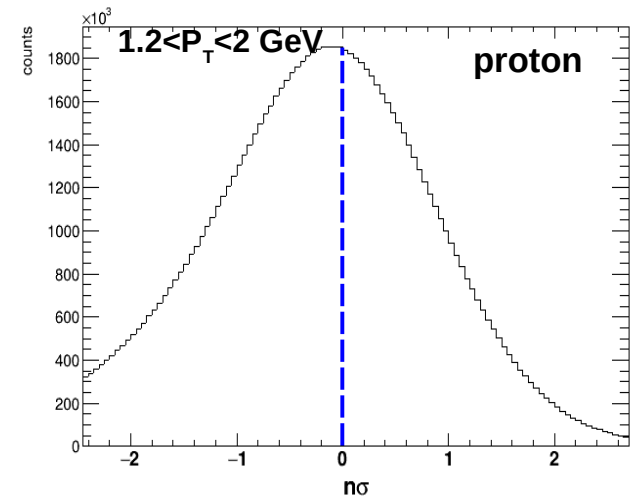
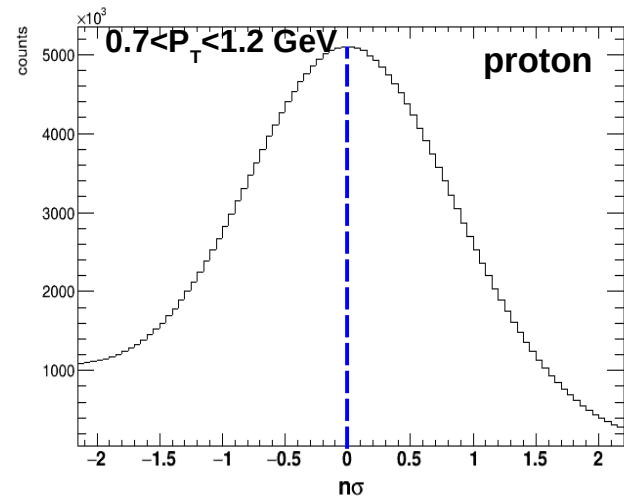
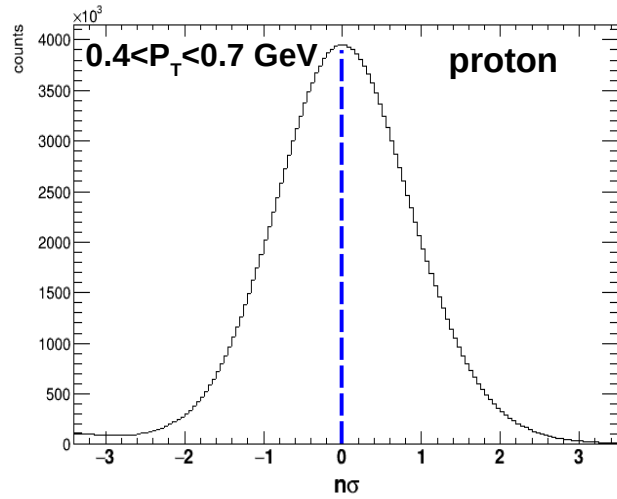


$V_z$  correction factor:

$$\frac{[0]}{[3] * x^3 + [2] * x^2 + [1] * x + [0]}$$



## n $\sigma$ shift



- Corrected n $\sigma$  (n $\sigma$ ) shift for the analysis
- n $\sigma$  distribution is shifted as a function of rapidity and p<sub>T</sub> bin