



# Precision Spectroscopy of Helium Atoms

Yu Sun  
孙羽

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International Conference on Precision Physics of Simple Atomic Systems  
ETH Zurich 2024/6/11

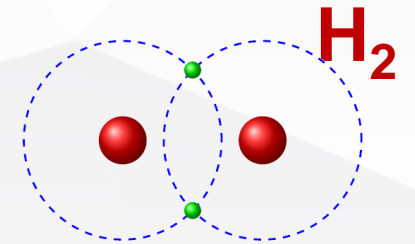
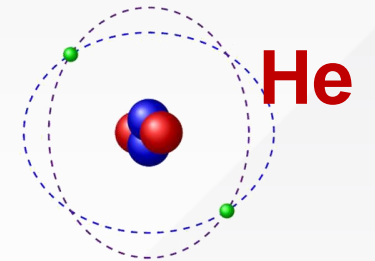
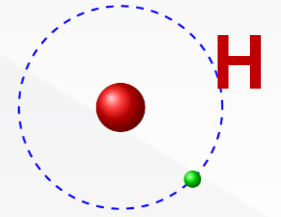
## Simple, Calculable, Systems

- Full quantum, ab initio, **no tunable parameters**
- ◆ Fine structure constant,  $\alpha \approx 1/137$
- ◆ Electron-Proton mass ratio,  $\mu = m_e/m_p \approx 1/1836$
- ◆ Rydberg constant,  $R_\infty$
- ◆ Nuclear charge radii,  $r_p, r_{\text{He}}$
- Test of bound-state QED
- Determination of  $R_\infty(r_p), \alpha, m_p/m_e$
- New Physics?

$$E_{nlj} = R_\infty \left[ -\frac{1}{n^2} + f_{nlj} \left( \alpha, \frac{m_e}{m_p}, \dots \right) + \delta_{\ell 0} \frac{C_{NS}}{n^3} r_p^2 \right]$$

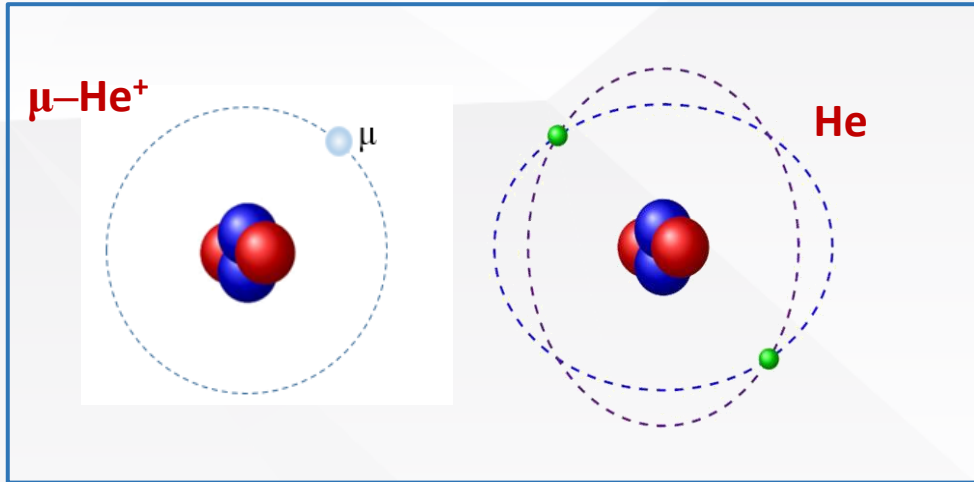
$$X_{20}\alpha^2 + X_{30}\alpha^3 + \dots$$

Beyer et al., Science 2017



H, He, H<sub>2</sub>, Li<sup>+</sup>, Be<sup>2+</sup>

## Nuclear Radius of $\mu\text{-He}^+$



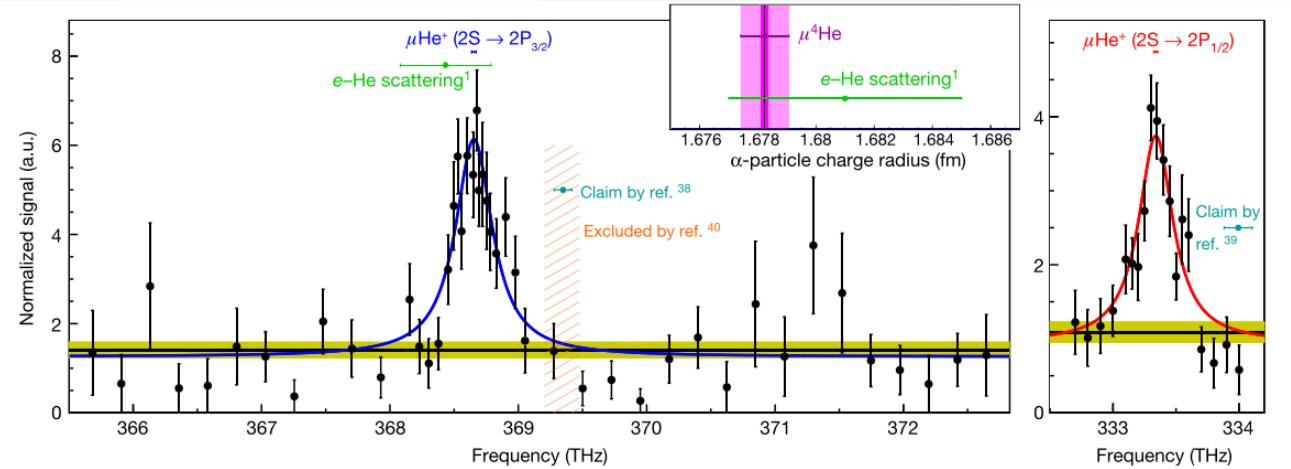
$\mu\text{-He}^+/\text{He}$

Testing fundamental interactions on the helium atom

Krzysztof Pachucki,<sup>1</sup> Vojtěch Patkóš,<sup>2</sup> and Vladimir A. Yerokhin<sup>3</sup>

- Physical Review A **95**,062510 (2017)

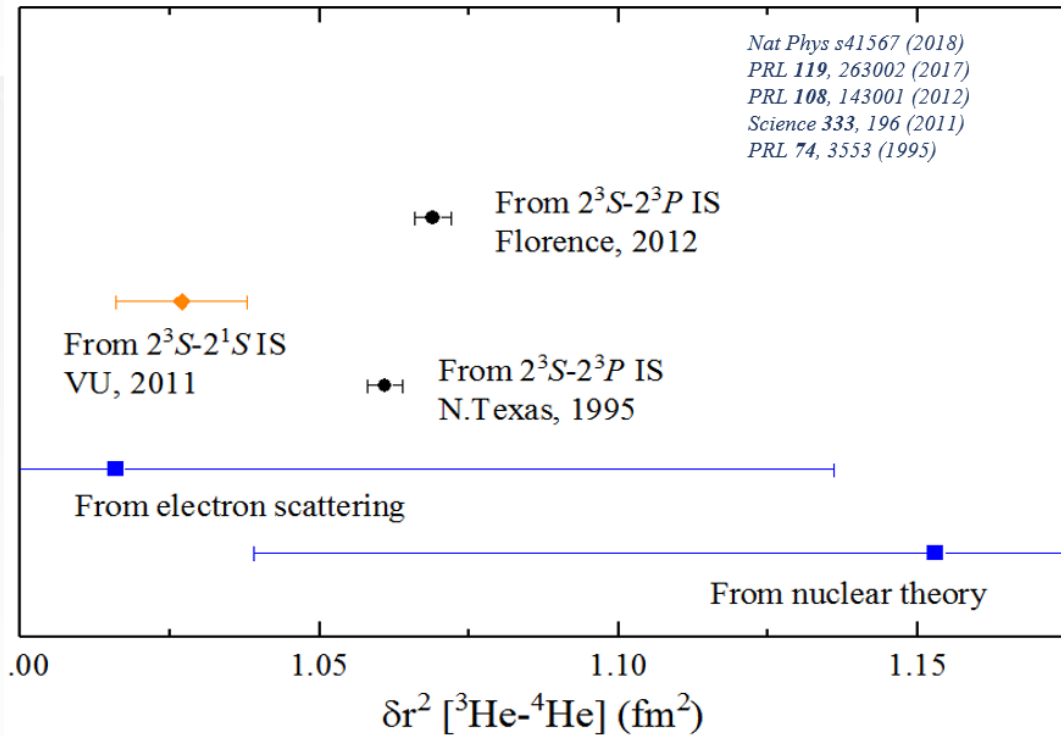
Nature (2021) **589** 527



Test of fundamental physics can be obtained not only from the hydrogenic systems but also from the few body atomic Systems, such as **He and He-like ions**.

## Find New Physics in He and He-like System

## ● Isotope Shift and Squared Nuclear Charge Radius Difference



➤  $\Delta r^2 = r_{\text{He-3}}^2 - r_{\text{He-4}}^2$

➤ Sufficient to Compare with  $\mu\text{-He}^+$

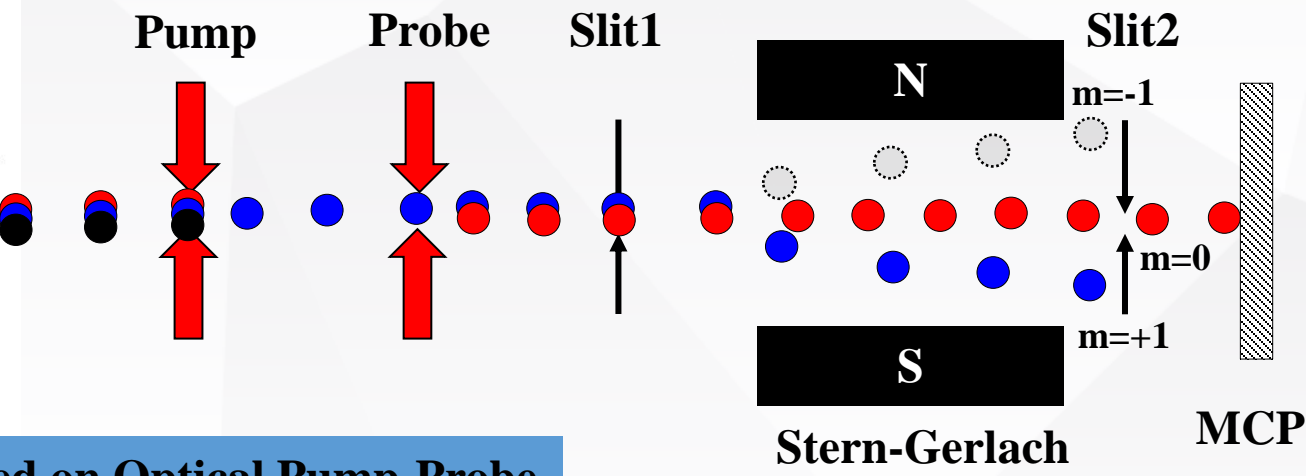
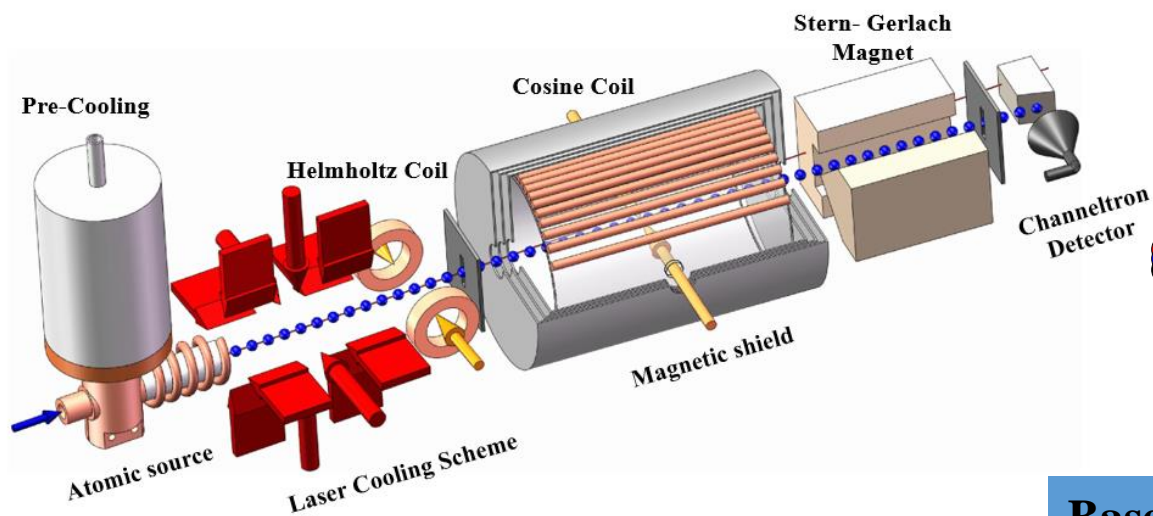
➤ Results from  $2S-2P$  different from  $2^1S-2^3S$

➤ Need more independent experiment to verify

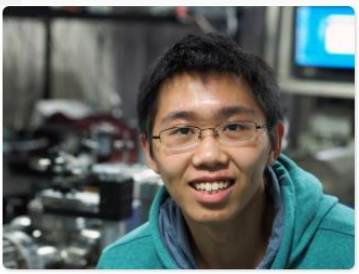
## Laser cooling based atomic beam system

Front. Phys. China, 4(2), 165 (2009)

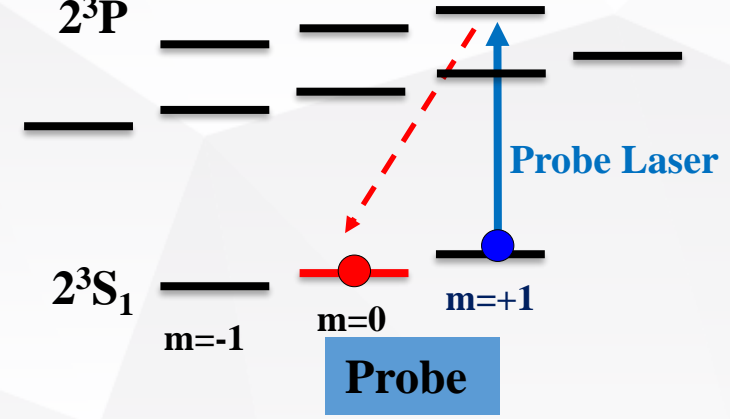
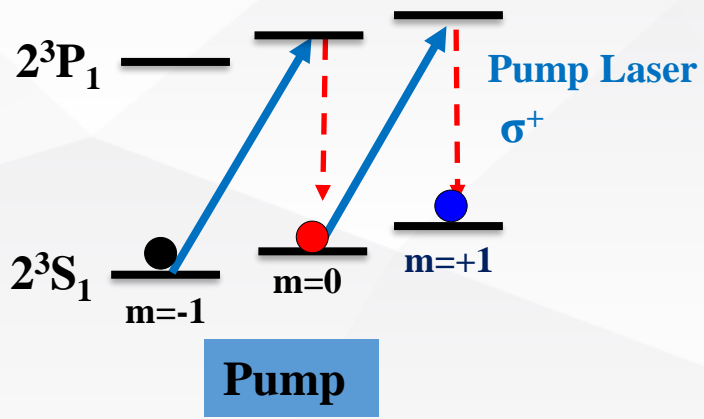
Physical Review A 91, 030502(R) (2015)



Based on Optical Pump-Probe



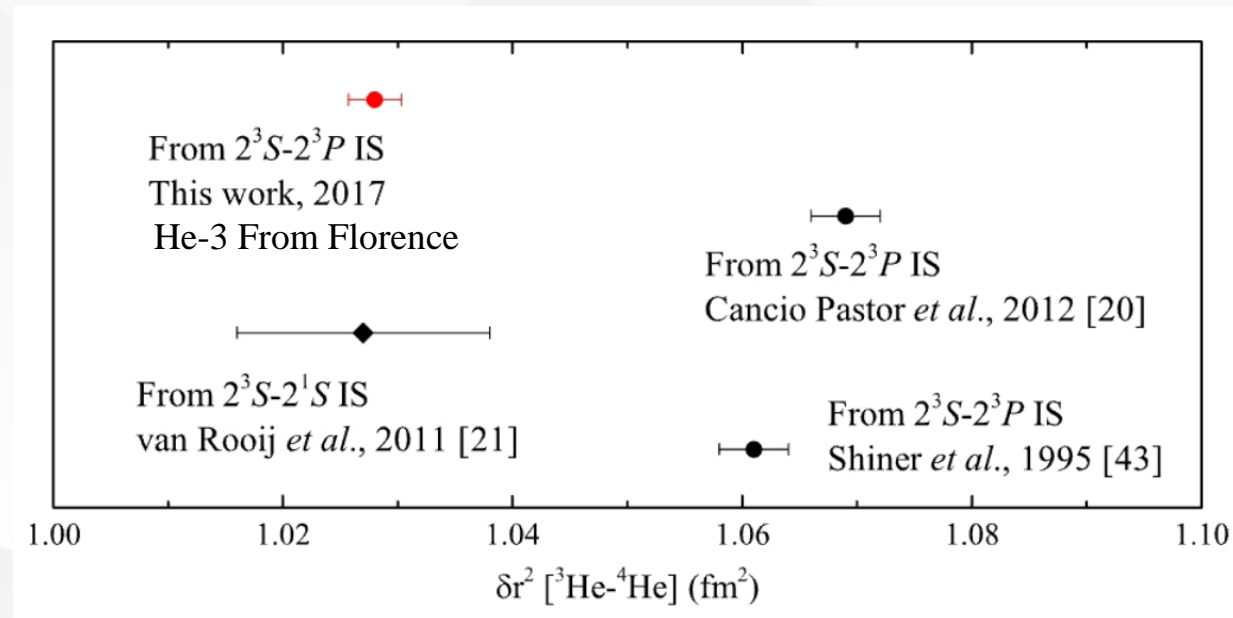
X. Zheng



## Uncertainty Budget of 2S-2P transition frequency Measurement

Uncertainty	Correction [kHz]	uncertainty [kHz]	Rel.uncertainty [ $10^{-12}$ ]
Statistics	-	0.50	1.8
Frequency calibration	-	0.55	2.0
First-Order Doppler	-	1.00	3.6
Line-Profile	-	0.40	1.2
Second-order Doppler	+0.70	0.15	0.5
Laser Power	-	0.10	0.3
Quantum Interference	+0.60	0.10	0.3
Scattering light	-	0.05	0.2
Zeeman effect	-	0.01	0.04
Light-force-induced shift	+0.5	0.8	3
Recoil shift	-42.20	-	-
Total	-40.90	1.6	5.0

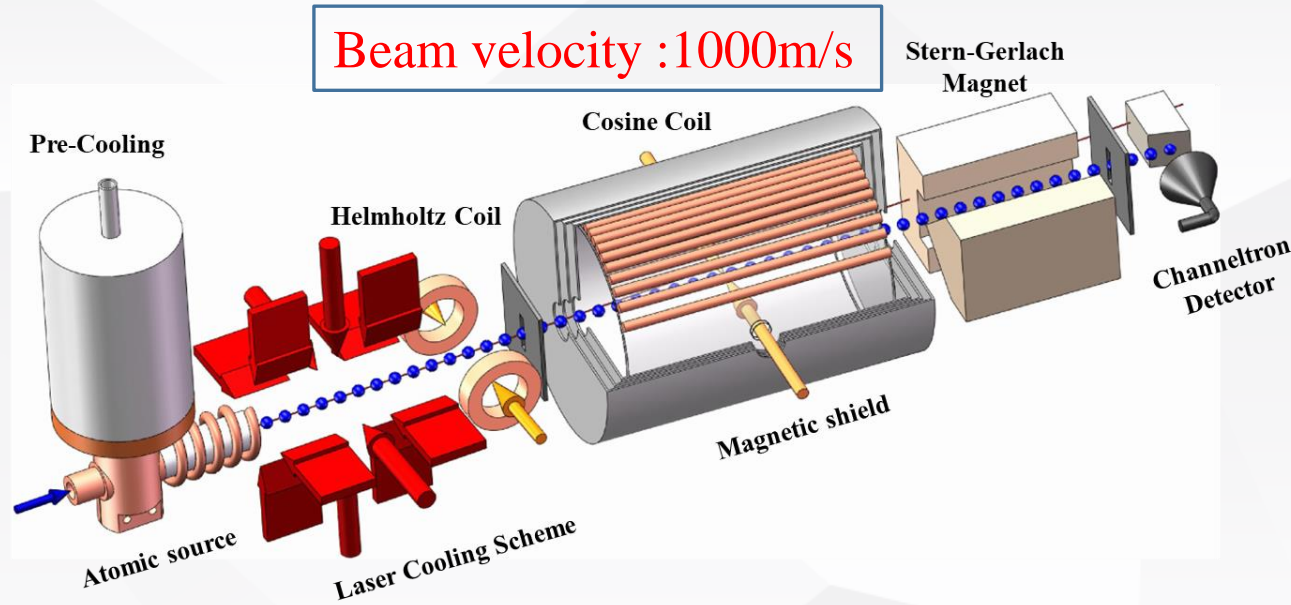
Physical Review Letters **119**, 263002 (2017)



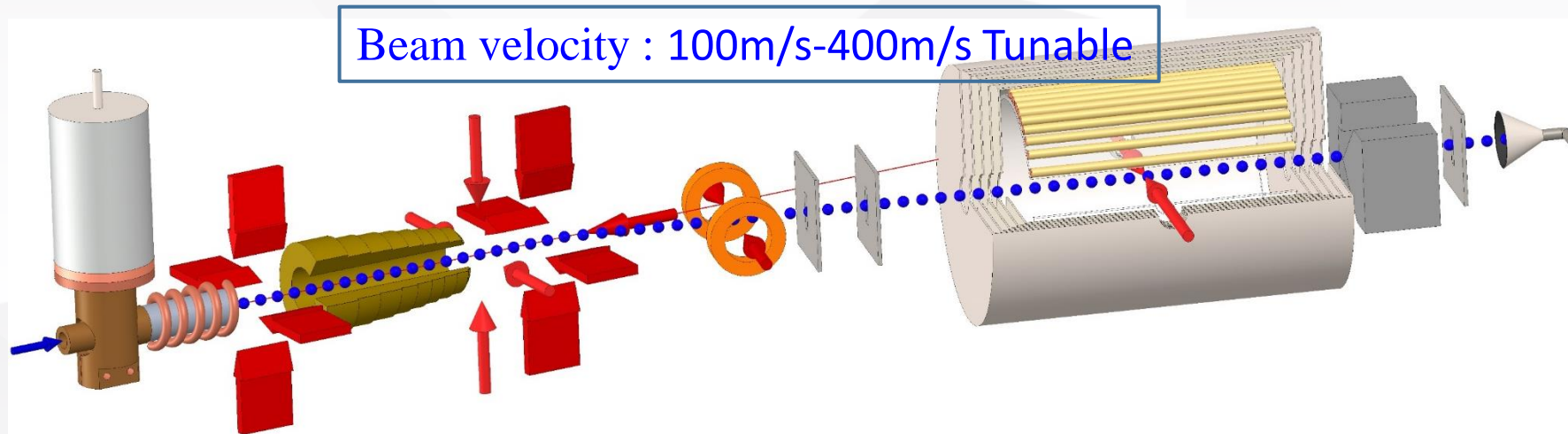
## Design New Experiment Method

Systematic effect:

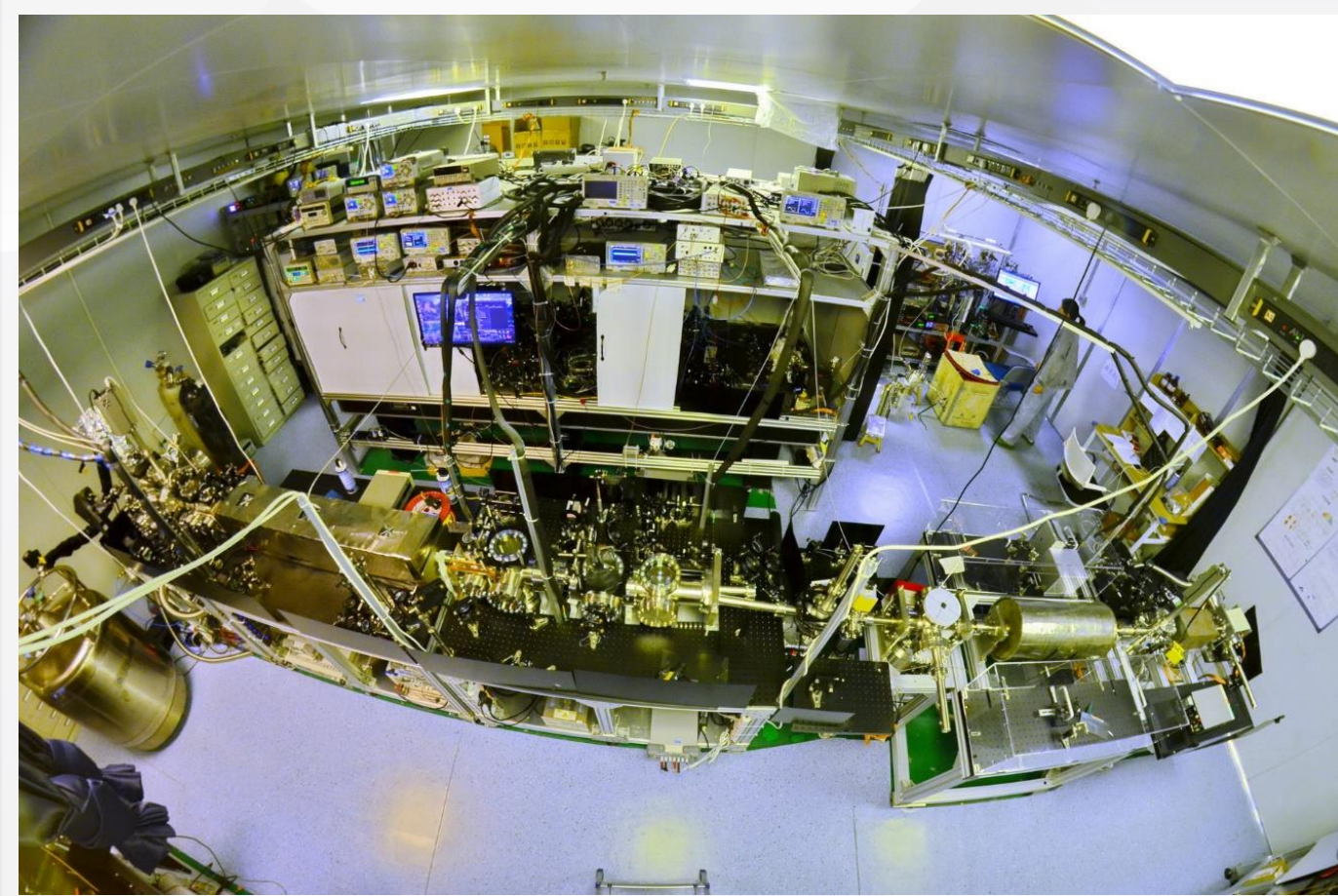
- First Order Doppler Effect
- Light Force shift



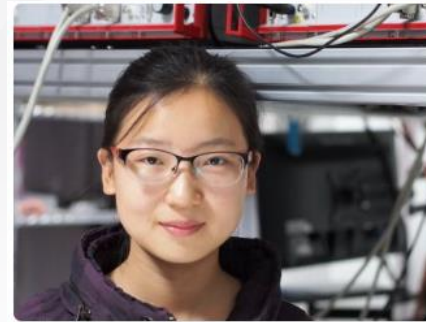
- Speed Fast
- Transvers velocity large
- Effect of SG Lower



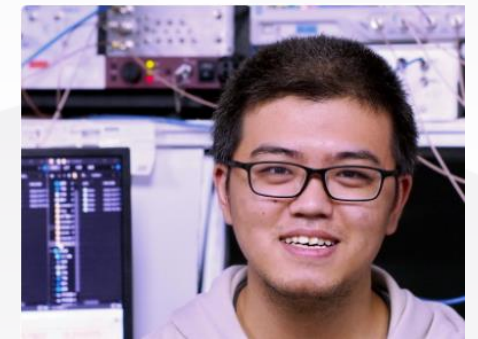
- Speed Slower
- Transvers velocity lower
- Effect of SG Higher



- Longitude velocity: 50m/s to 500m/s
- reduce one order of first order doppler
- Speed-adjustable atomic beam
- Better determine the uncertainty



**J.-J. Chen**



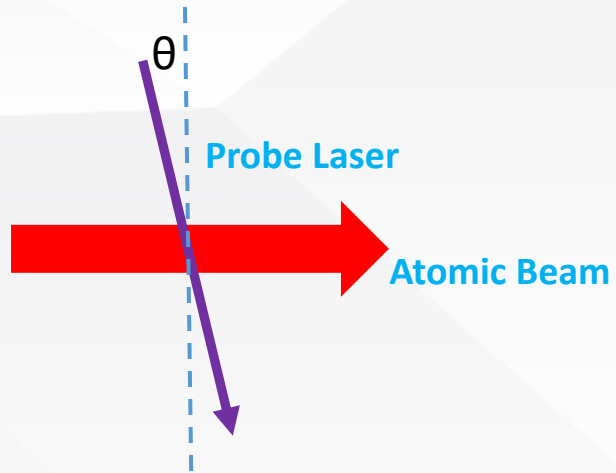
**J.-L. Wen**



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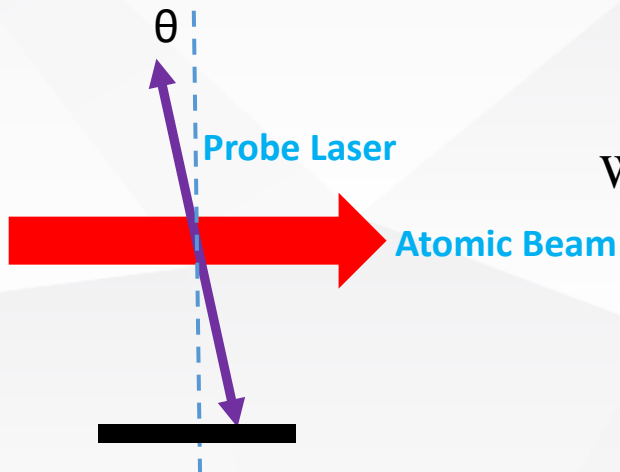
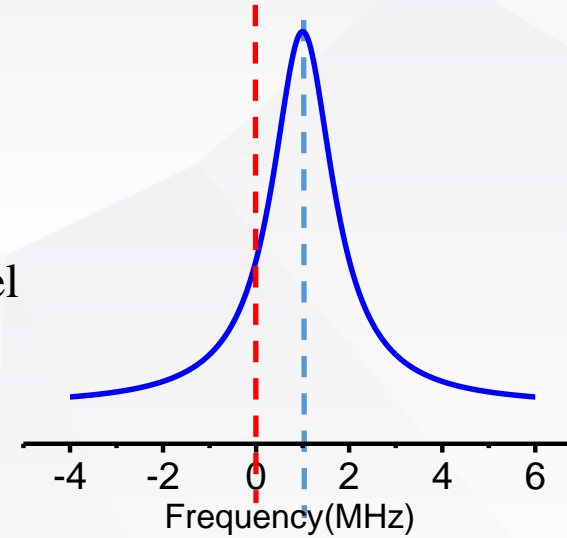
Uncertainty	Correction [kHz]	uncertainty [kHz]	Rel.uncertainty [10 <sup>-12</sup> ]
Statistics	-	<b>0.50</b>	<b>1.8</b>
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Recoil shift	<b>-42.20</b>	-	
<b>Total</b>	<b>-40.90</b>	<b>1.6</b>	<b>5.0</b>

## ● First Order Doppler

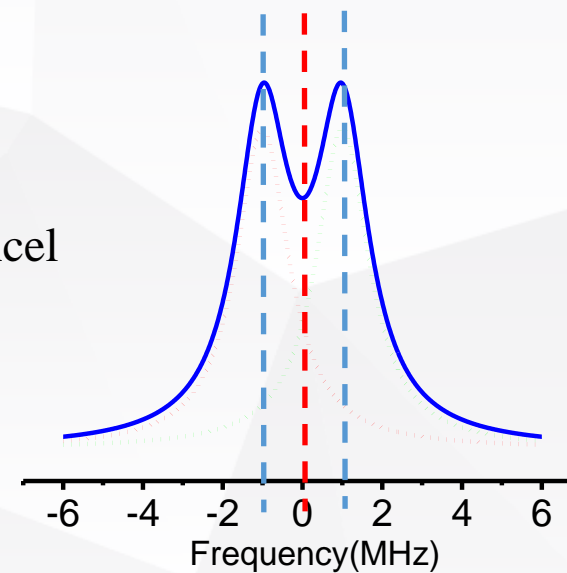


$$\Delta\nu_D = kv \cdot \theta$$

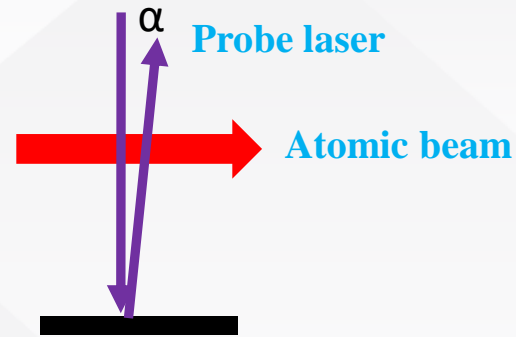
No Doppler cancel



With Doppler cancel



## ● First Order Doppler

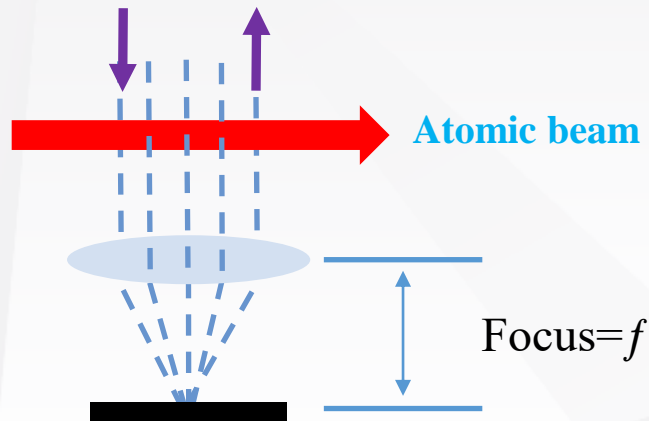


$$\Delta\nu_D \approx \frac{1}{2} kv \cdot \alpha$$

10urad correspond to about 3kHz derivation

### ➤ Cancel Mechanism

- ✓ Cat's eye optical method

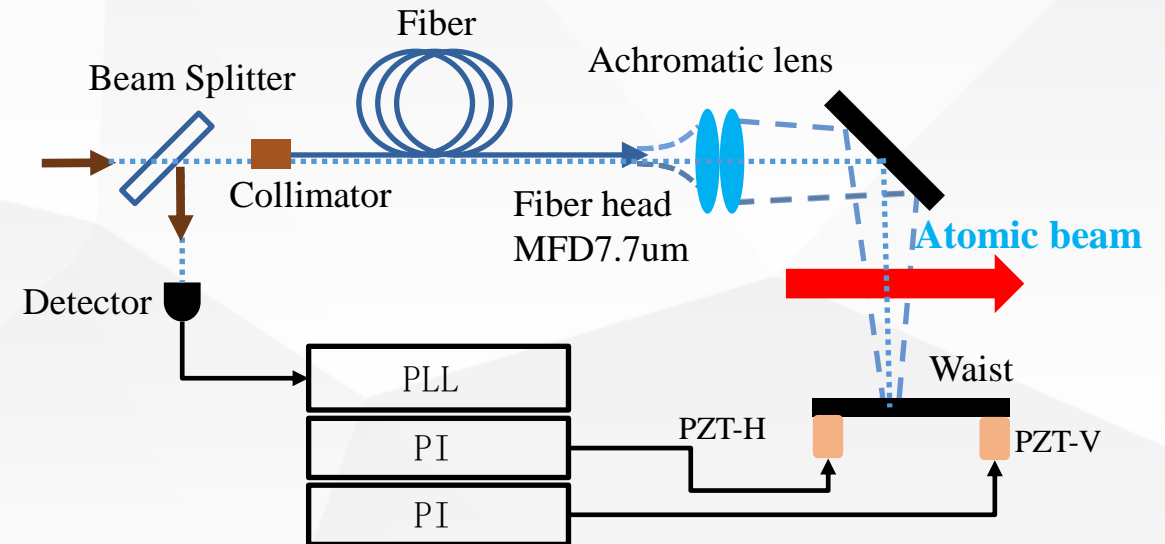


*Physical Review Letters* **92**,023001 (2004)

*Can. J. Phys.* **83**,301 (2005)

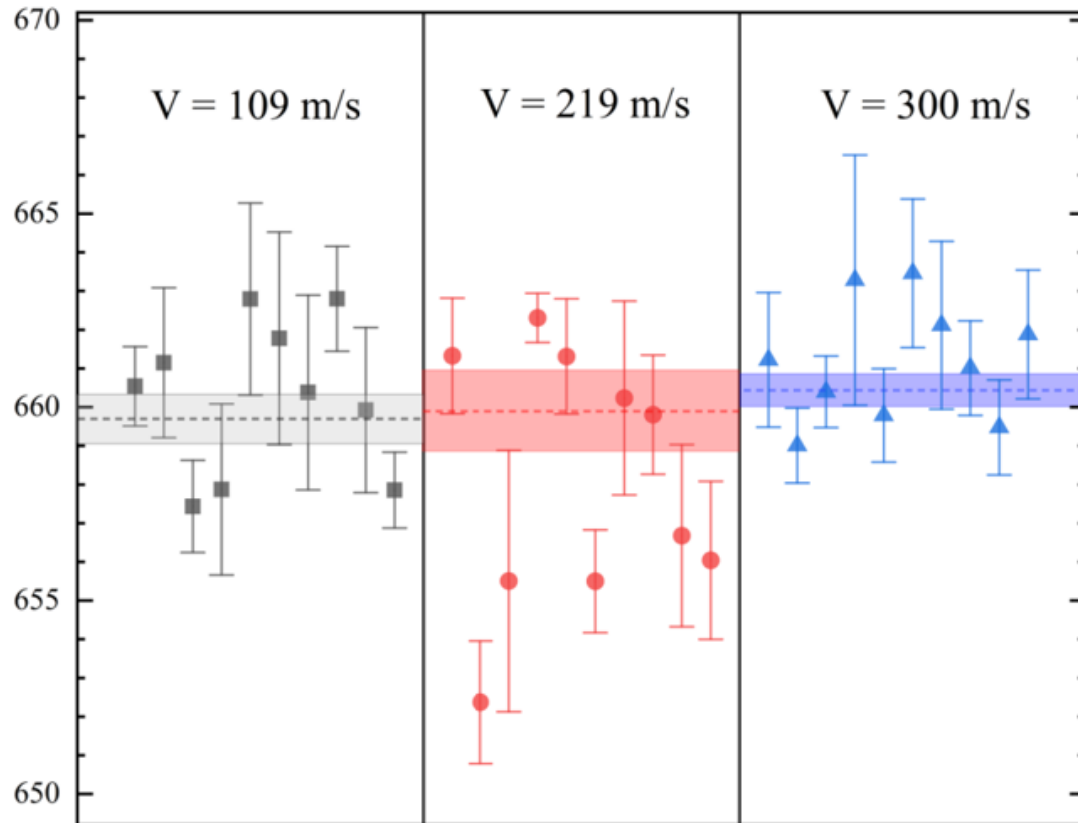
*Physical Review Letters* **105**,123001 (2010)

- ✓ Active Feedback method



*Optics Express* **24**,17470 (2016)

## Systematic effect : First Order Doppler Effect



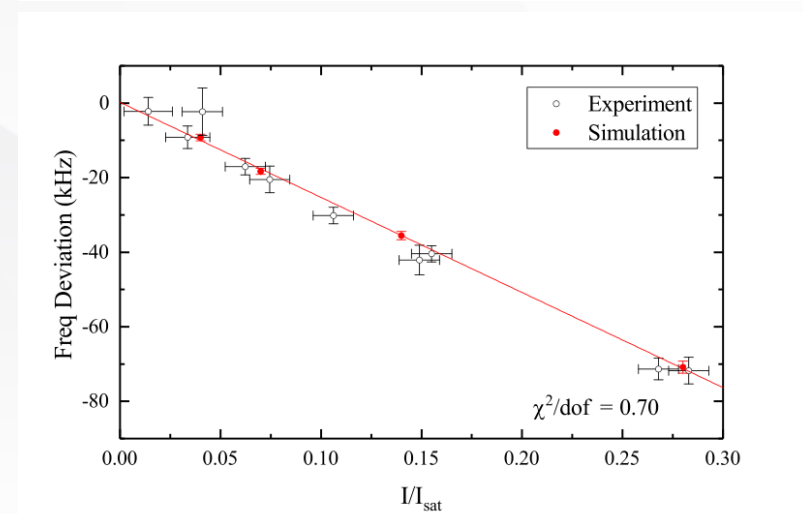
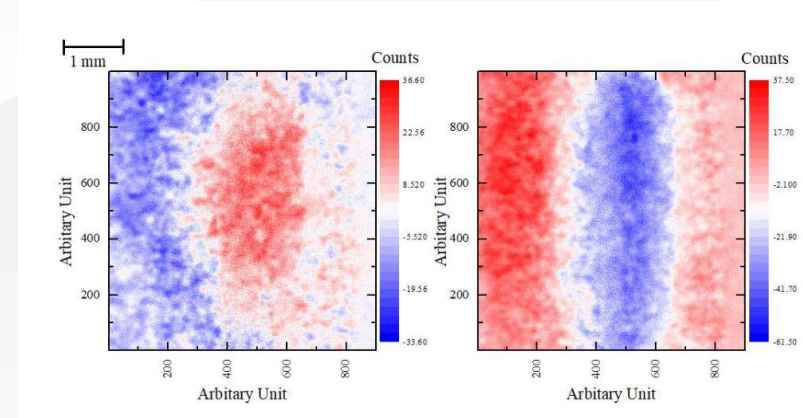
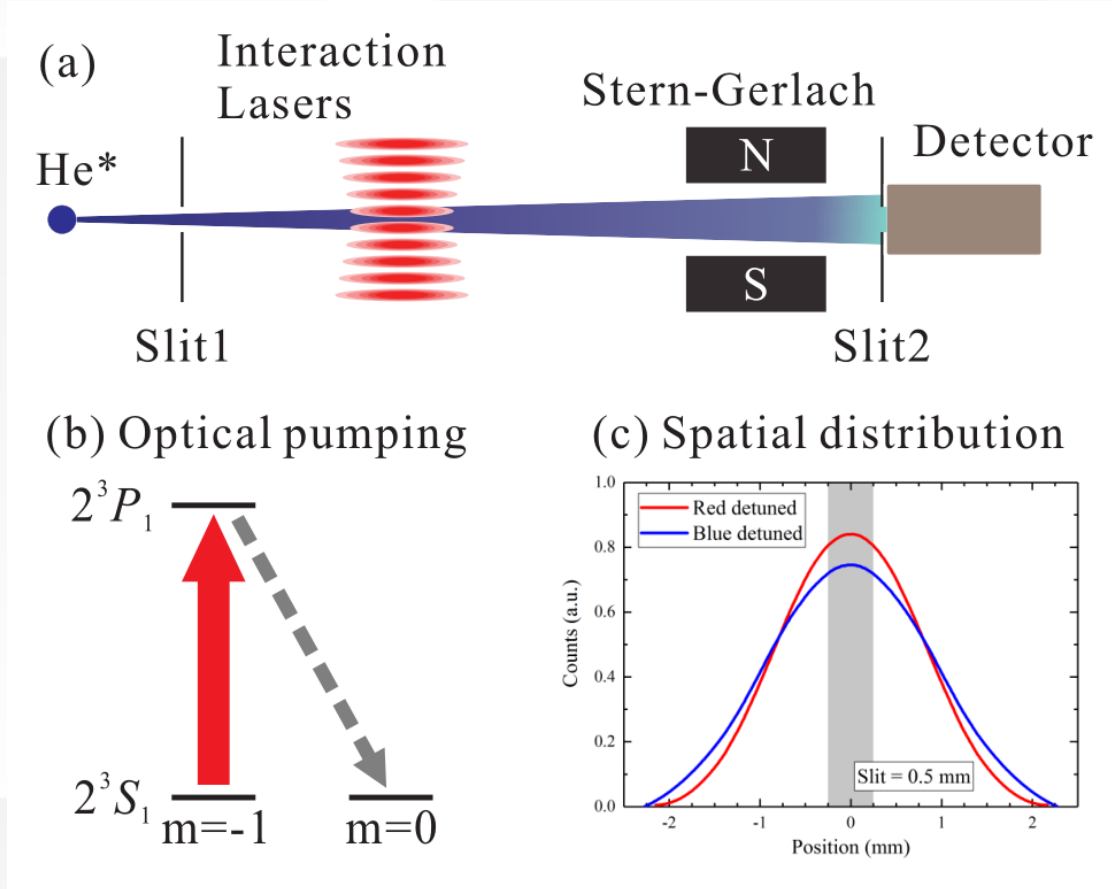
$$\Delta f = \vec{k} \cdot \vec{v}$$

- Tune to different velocity
- Better estimate the effect of doppler
- Consistent with each other
- The derivation is not from doppler effect

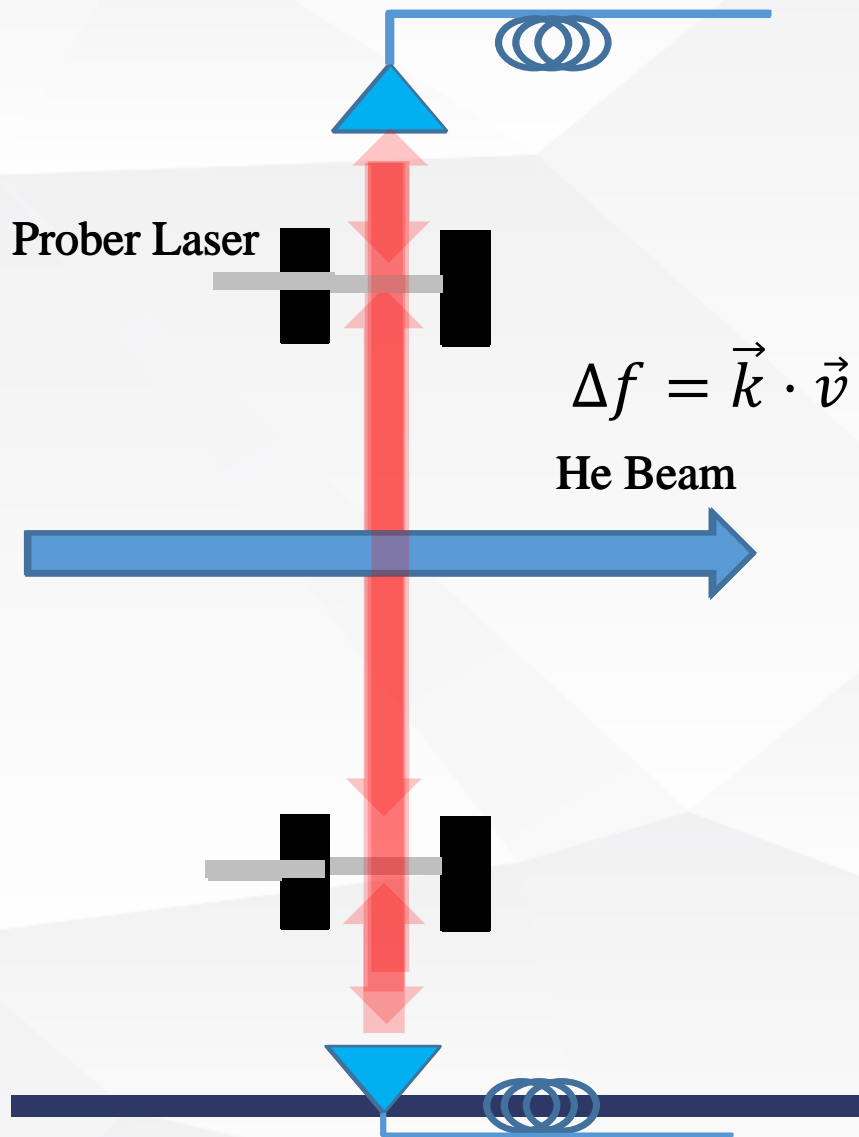
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Recoil shift	<b>-42.20</b>	-	
<b>Total</b>	<b>-40.90</b>	<b>1.6</b>	<b>5.0</b>

## ● Light Force Induce Shift



## Systematic effect : Light-Force-Shift

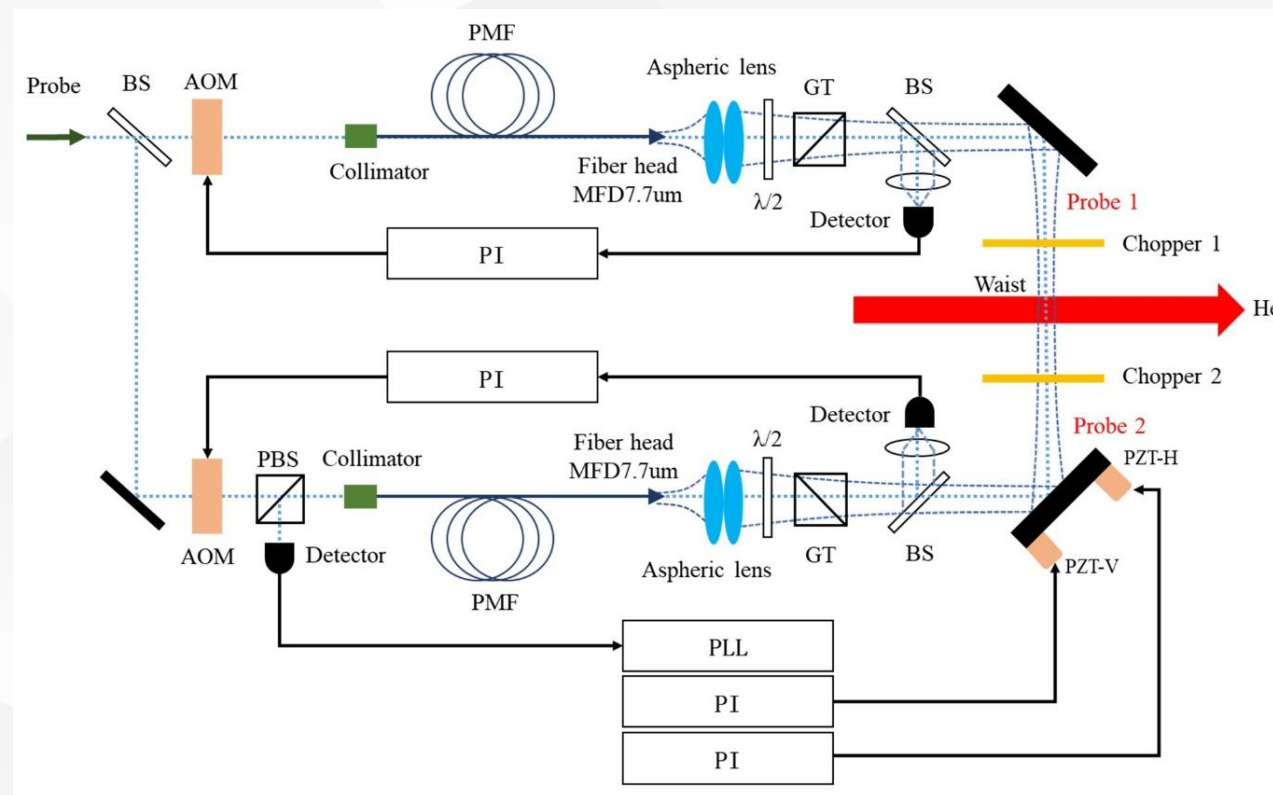


PHYSICAL REVIEW A **107**, 042811 (2023)

Editors' Suggestion

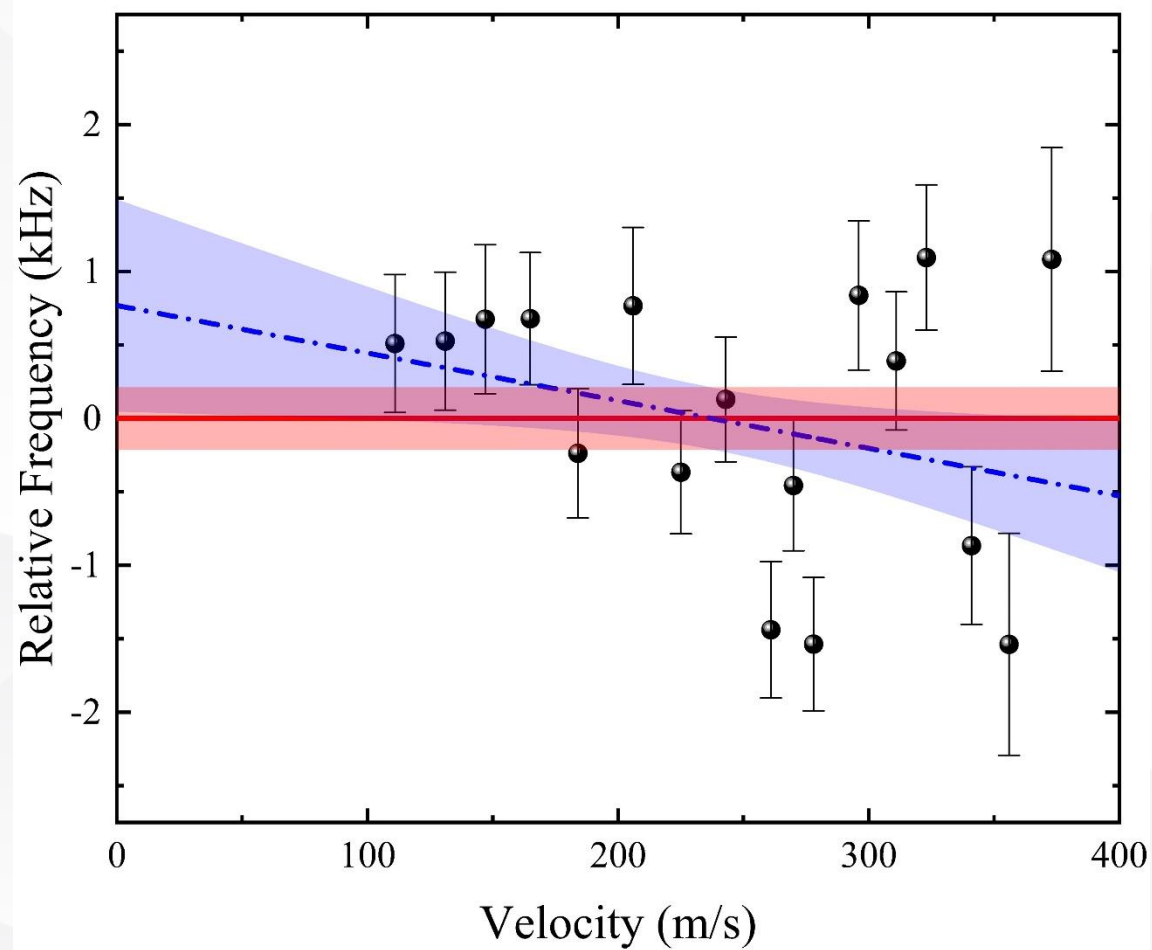
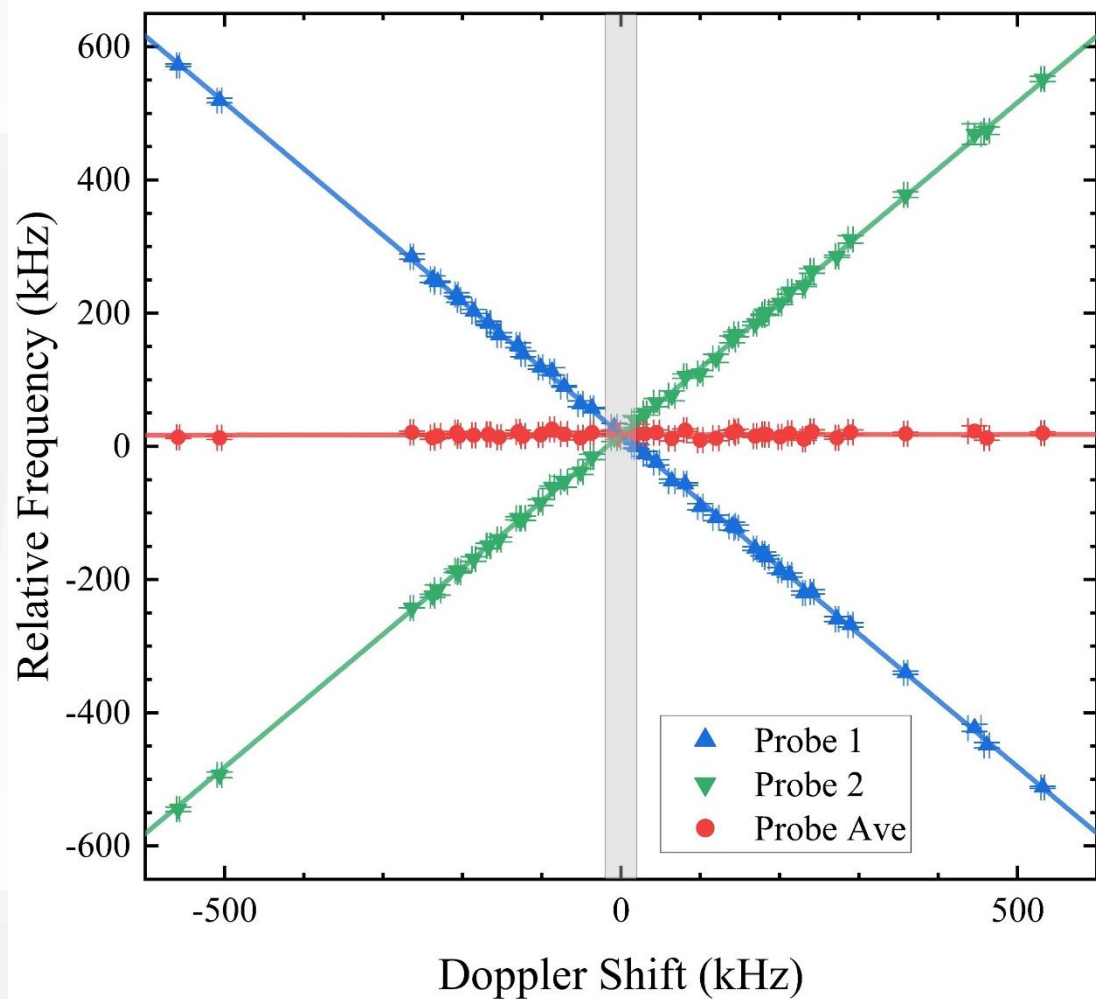
**Doppler-free spectroscopy of an atomic beam probed in traveling-wave fields**

Jin-Lu Wen (温金录)<sup>1</sup>, Jia-Dong Tang (唐家栋)<sup>2</sup>, Jun-Feng Dong (董俊峰)<sup>1</sup>, Xiao-Jiao Du (杜小娇)<sup>3</sup>,  
 Shui-Ming Hu (胡水明)<sup>1,2,\*</sup> and Y. R. Sun (孙羽)<sup>3,†</sup>



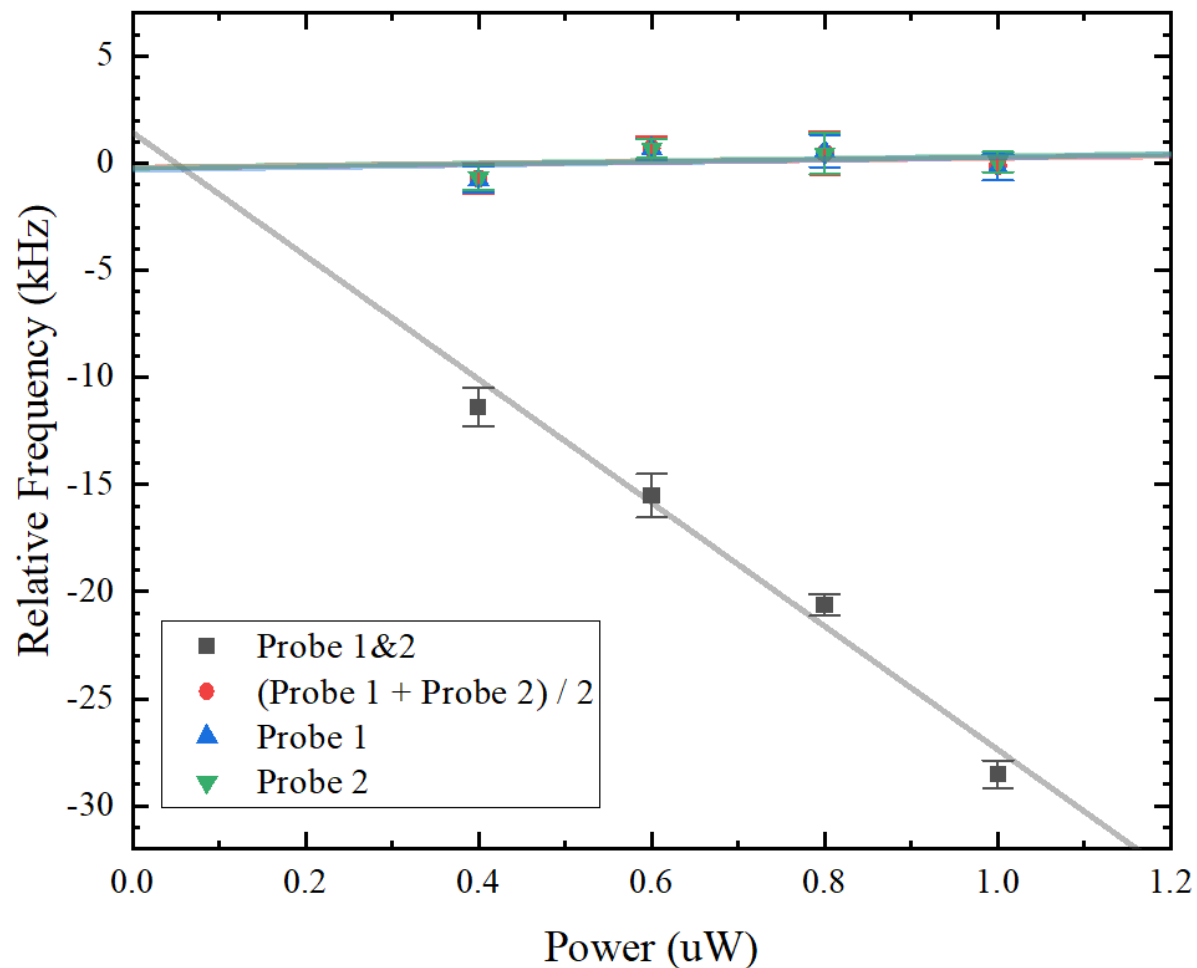
PRA **107**, 042811 (2023)

## Systematic effect :Light-Force-Shift





## Systematic effect :Light-Force-Shift

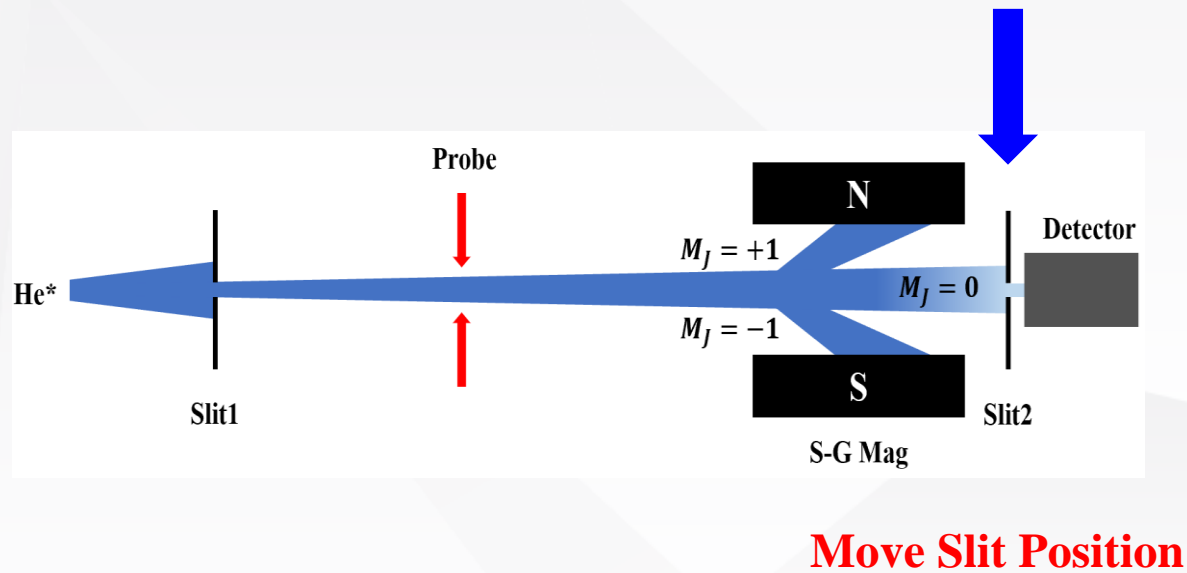


- Stand-Wave vs Traveling-Wave
- Estimate Light-Force-Shift
- The derivation is not from Light-Force-Shift

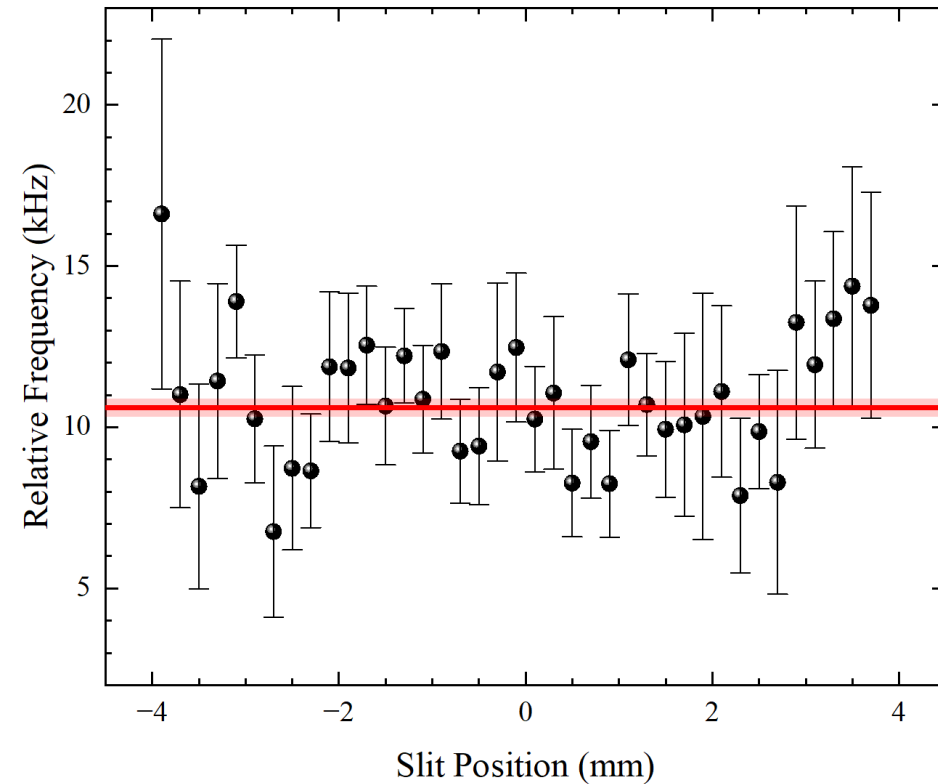
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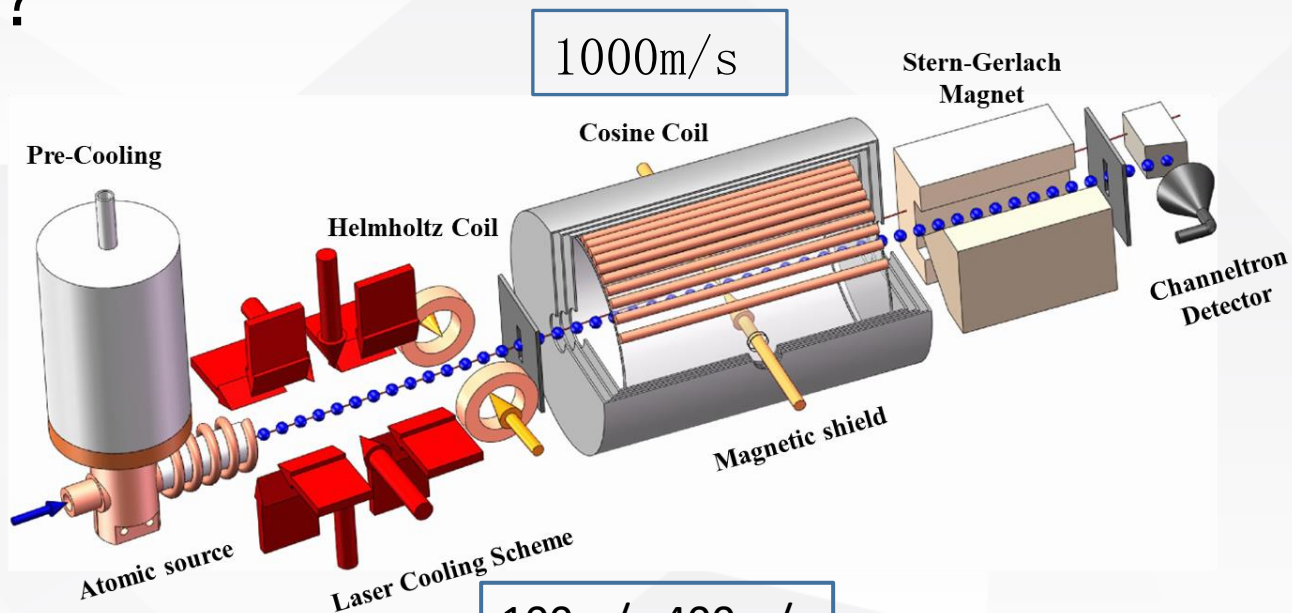
## Systematic effect : Geometry effect from the slit



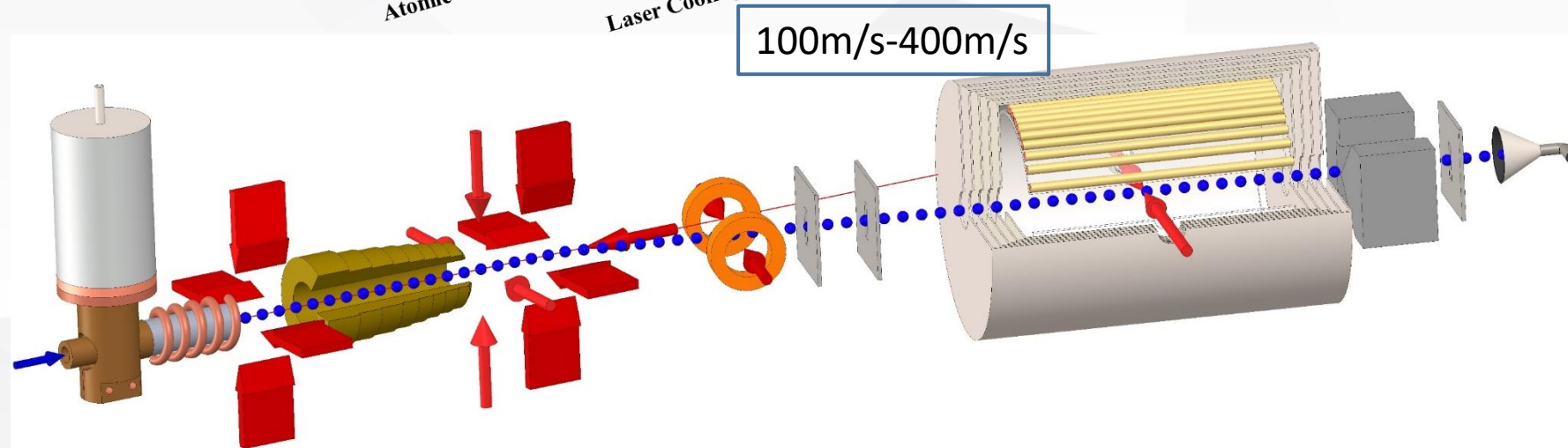
### ➤ Move Slit Position



## Remove Slit ?

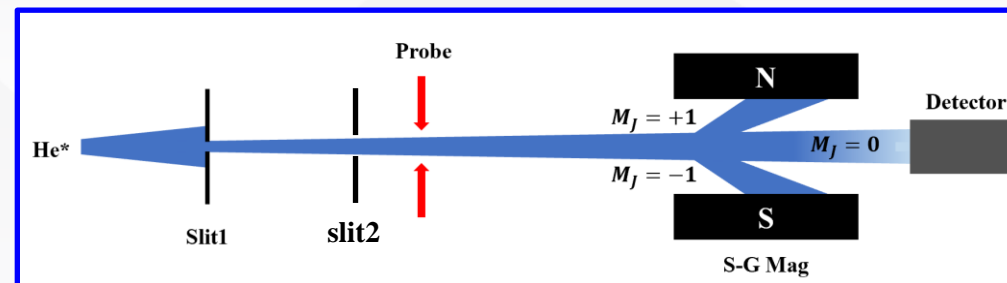
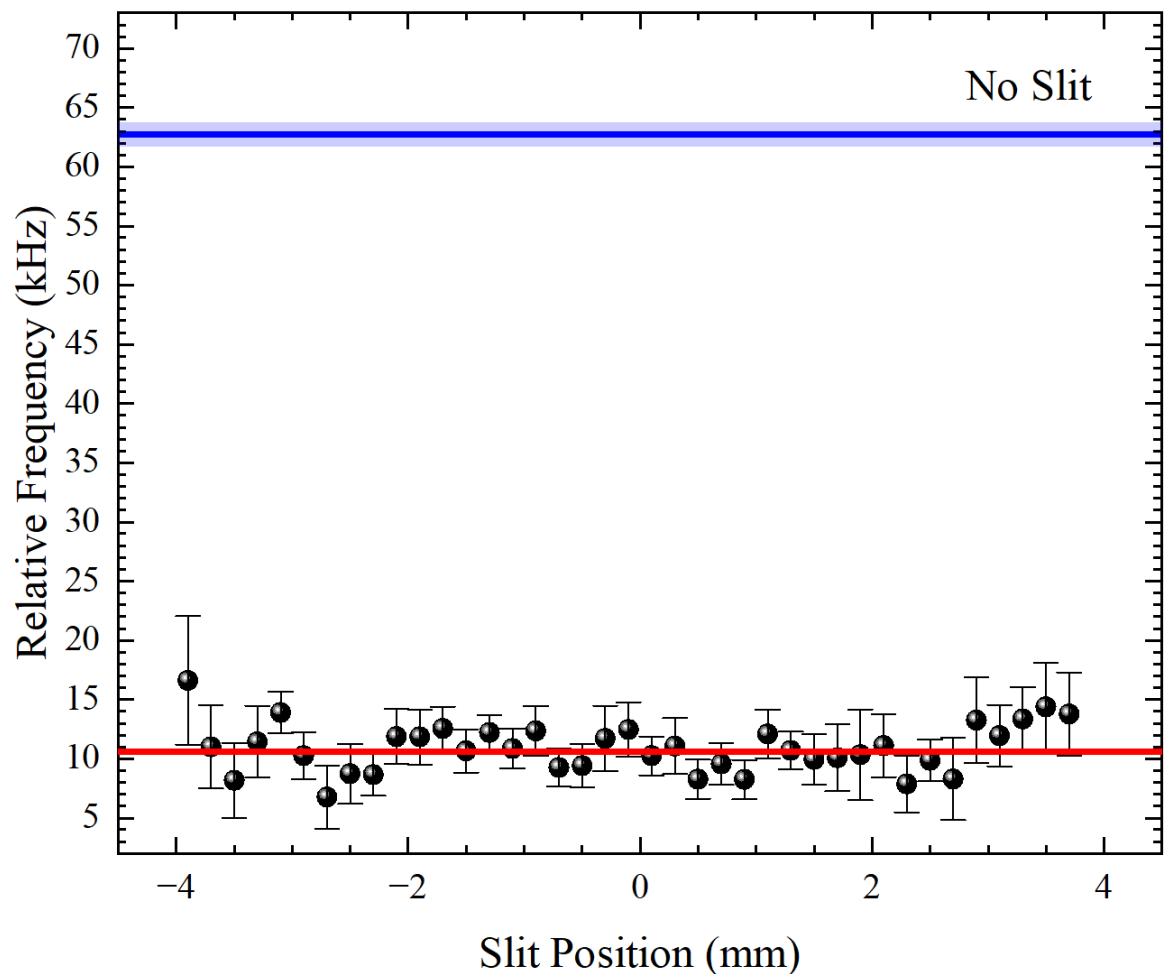


- Speed Fast
- Transvers velocity large
- Effect of SG Lower
- The Slit can not be removed



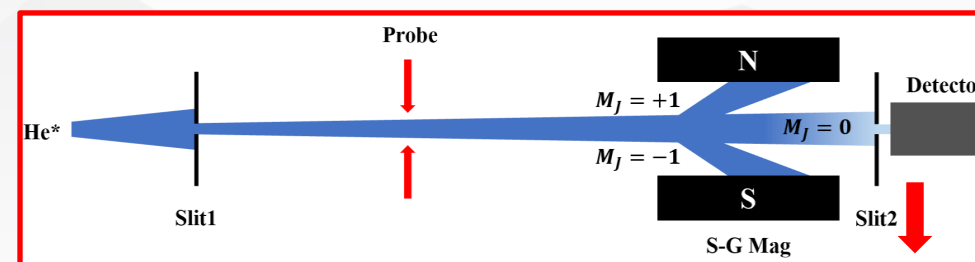
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## Systematic effect : Geometry effect from the slit

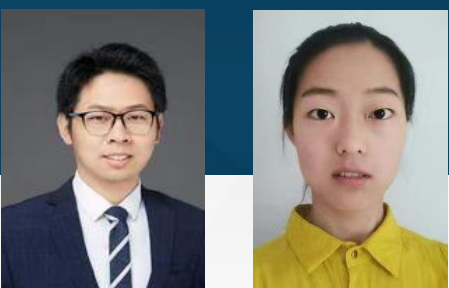


**Remove Slit**

- Move Slit—Different position give same result
- With and Without slit have big difference



**Move Slit Position**



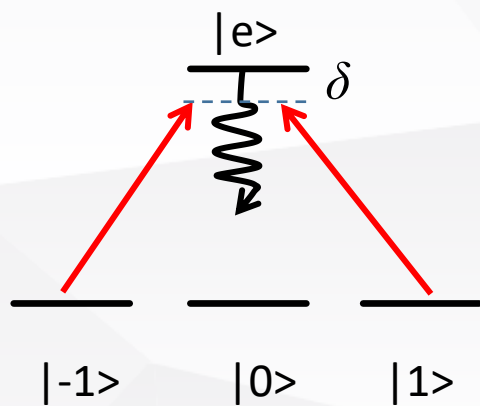
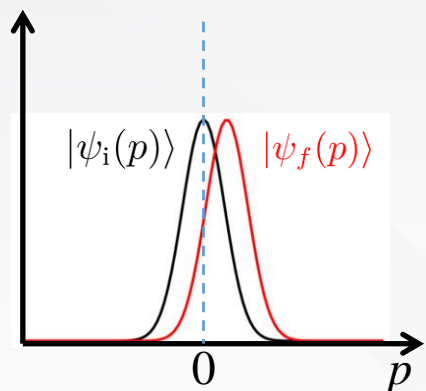
C.-L. Zou

Y.-N. Lv



### Initial State:

$$|\psi_i\rangle = |\pm 1\rangle \otimes |\psi_i(p)\rangle$$



### Coupling:

$$H = \delta \sigma_{ee} + (g_a e^{i\vec{k}\cdot\vec{r}} a^\dagger \otimes \sigma_{\pm 1, e}^- + h.c.) + \sum_k [\Delta_k b_k^\dagger b_k + (g_b e^{i\vec{k}_b\cdot\vec{r}} b_k^\dagger \otimes \sigma_{0e}^- + h.c.)]$$

At time  $t$ :  $|\psi_f\rangle$

$$|\psi_f\rangle = e^{-i \int_0^t H(\tau) d\tau} |\psi_i\rangle$$

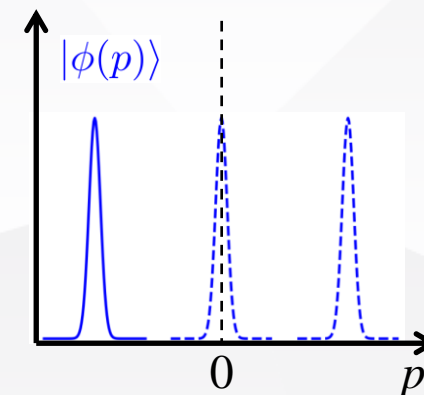
The number of atoms finally obtained by slit3  
 $N(\delta) \propto |\langle \phi(p) | U_{SE} |e\rangle \langle 0(\delta) | \pm 1 \rangle | \psi_i(p) \rangle|^2$

### Post-selection(WM):

$$\langle \phi | \psi_f \rangle = \langle \phi | e^{-i \int_0^t H(\tau) d\tau} | \psi_i \rangle$$

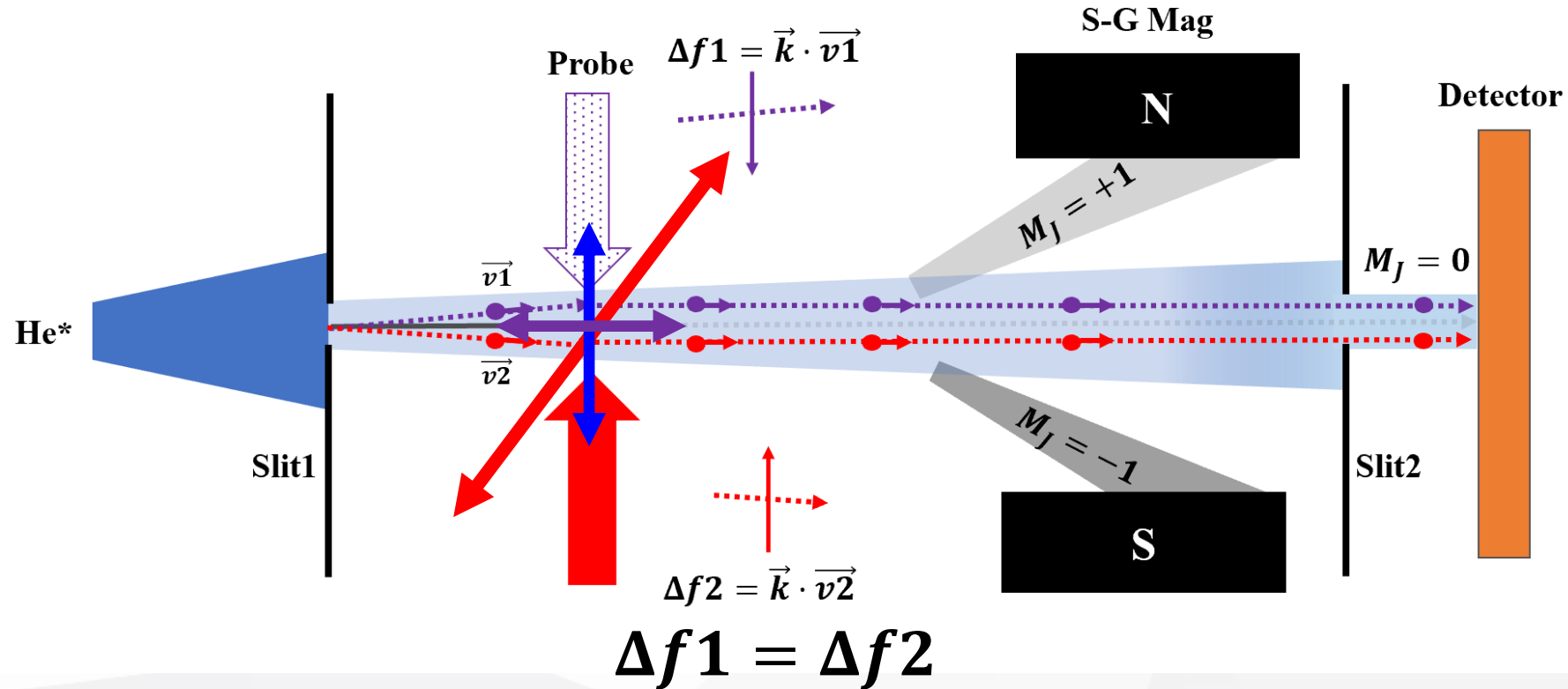
State of Post-selection

$$|\phi\rangle = |\phi(p)\rangle \otimes |0\rangle$$



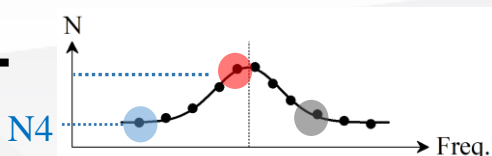
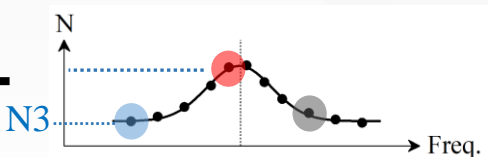
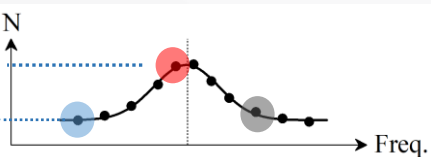
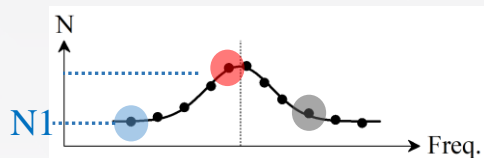
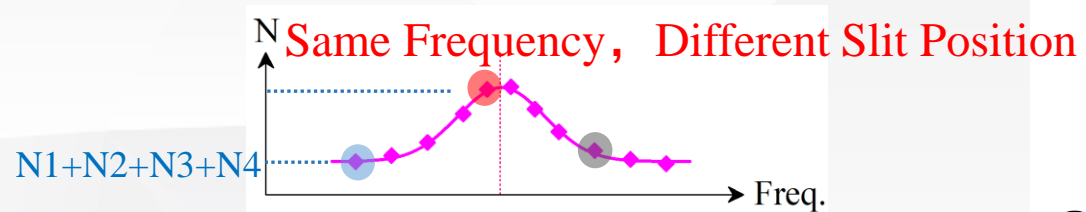
Different positions correspond to different distributions

## Systematic effect : Geometry effect from the slit => Post Selection

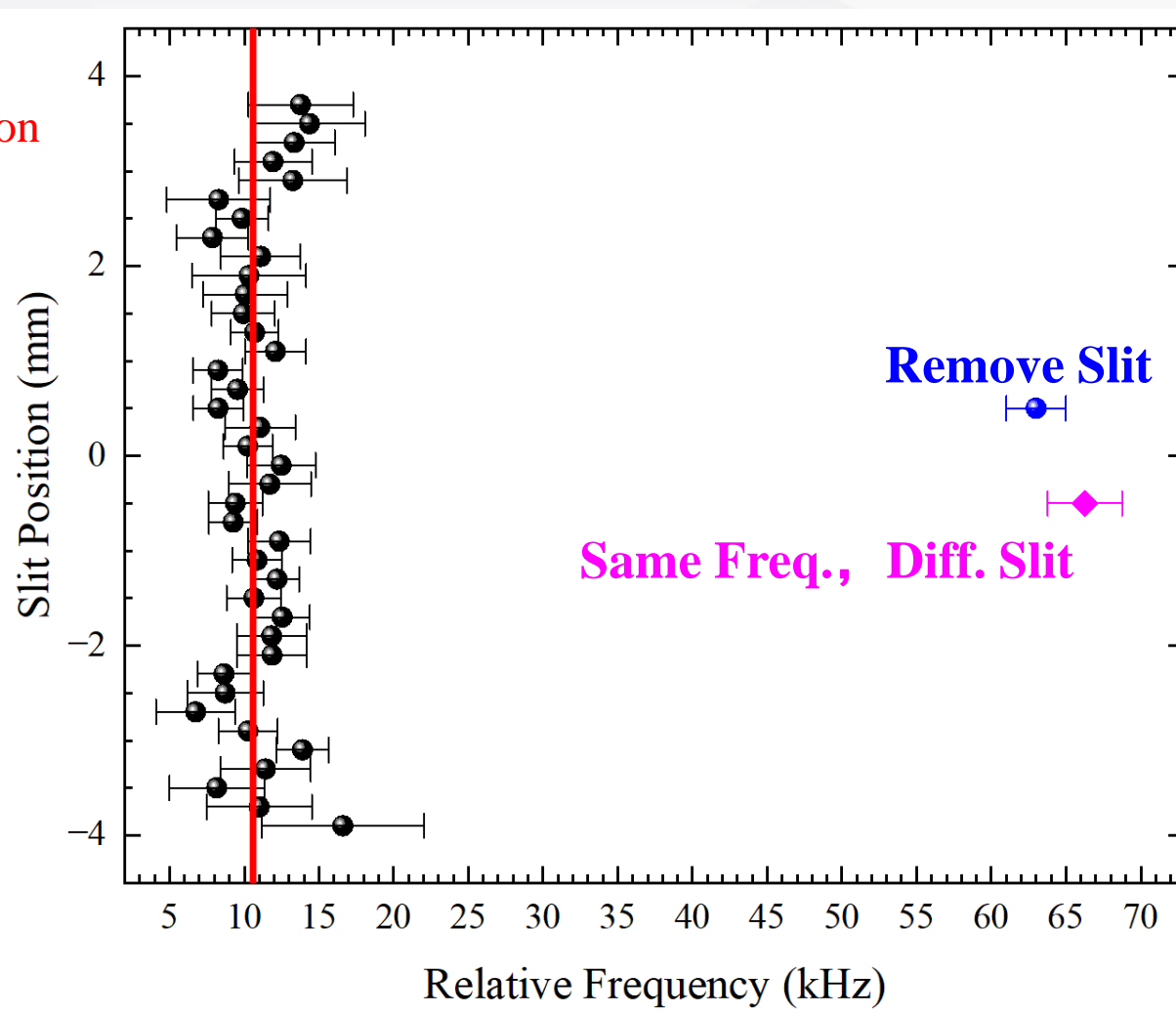


- ❑ The slit selects atoms with a certain Doppler shift
- ❑ The two retro-reflection lasers experience the same shift
- ❑ Standing Wave or Traveling Wave all the Same
- ❑ Move Position of the slit does not change

## Systematic effect : Post Selection



狭缝位置  
 $x$



### Test Post Selection Effect

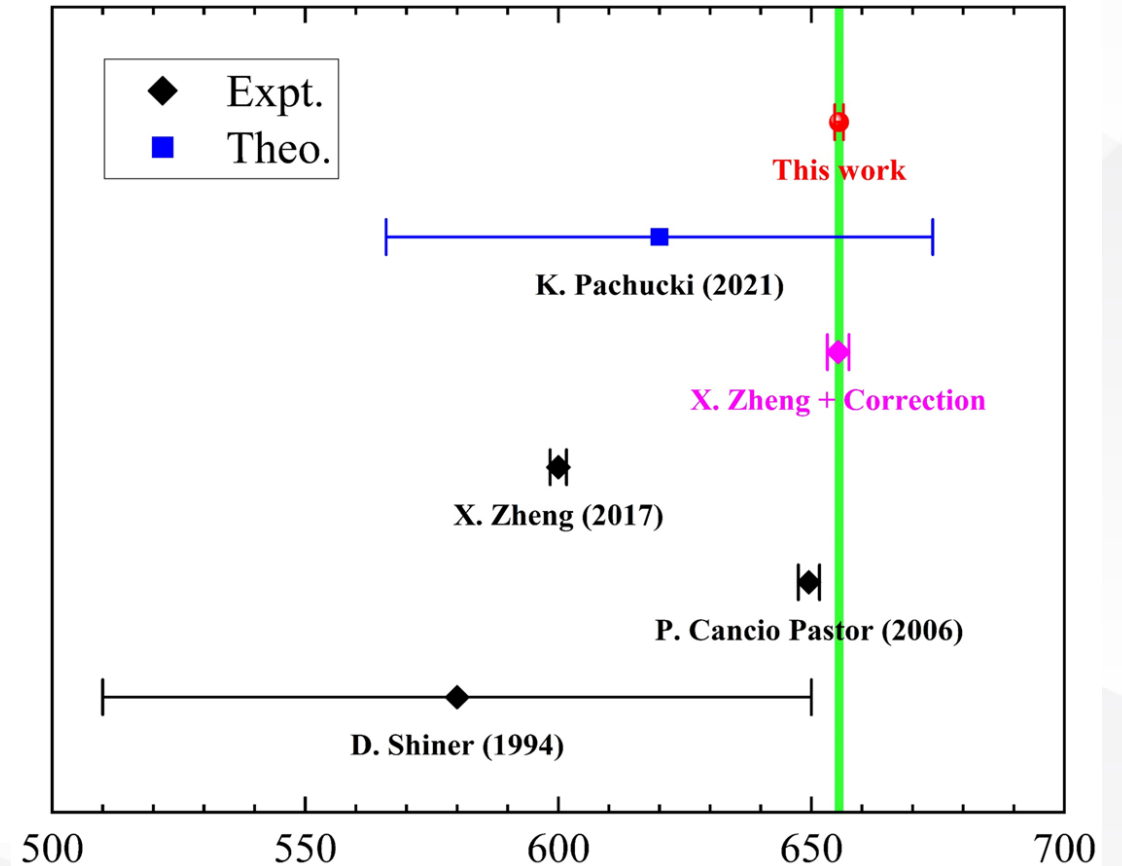


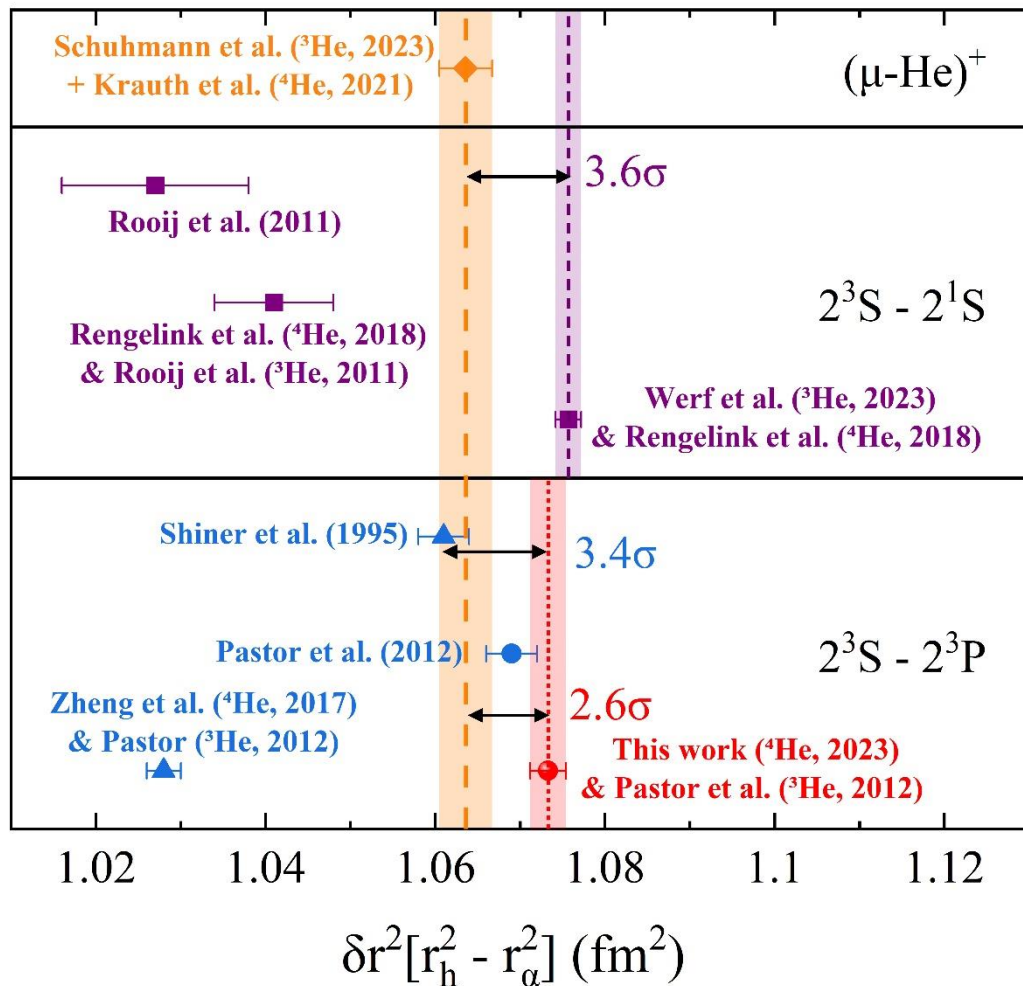
## Uncertainty Budget

This Work:  $f(2^3S_1 - 2^3P_0) = 276\,764\,094\,712.73 (86) \text{ kHz}$

	X. Zheng		This work	
	Correction	Error (1 $\sigma$ )	Correction	Error (1 $\sigma$ )
Statistics		0.45		0.22
1st Doppler		1.1		0.82
2nd Doppler	+ 0.70	0.15		0.01
Frequency calibration		0.55		0.06
Quantum interference	+ 0.08	0.03	+ 0.05	0.02
Zeeman effect		0.01		0.01
Laser power		0.1		0.20
Line profile		0.3		
Recoil shift	- 42.5		- 42.48	
Post-selection shift	+ 55.3	1.5		
Light-force shift	+ 0.5	0.8		
<b>Total</b>		<b>2.1</b>		<b>0.86</b>

2S-2P Centroid Frequency - 276, 736, 495 MHz (kHz)





Latest  $2^1\text{S}-2^3\text{S}$  result [arXiv:2306.02333v1]

Latest  $\mu\text{-He}^+$  result [arXiv:2305.11679v2]

--Deviation 3.6 times standard deviation

Ordinary Helium atomic spectrum:

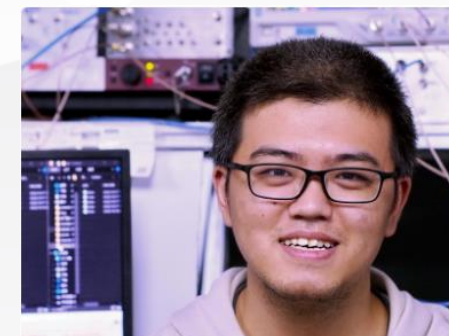
--Three independent experiments were consistent

--Shiner-95 3.4 times standard deviation

$\mu\text{-He}^+$  compare with He:

-- $\mu\text{-H}$  and H

--New Physics?



Jin-Lu Wen

## Institute of Advanced Science Facilities



Prof. Sun Yu

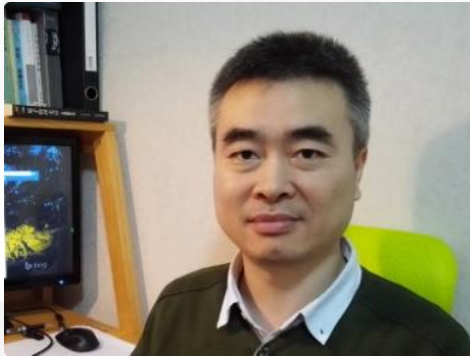


Du Xiao-Jiao

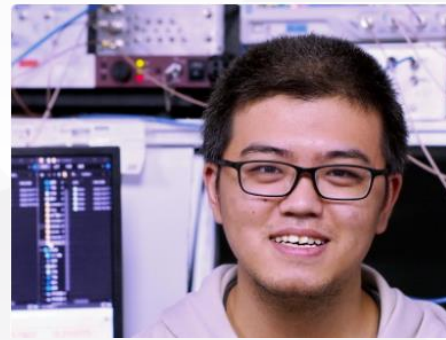


Wei Long

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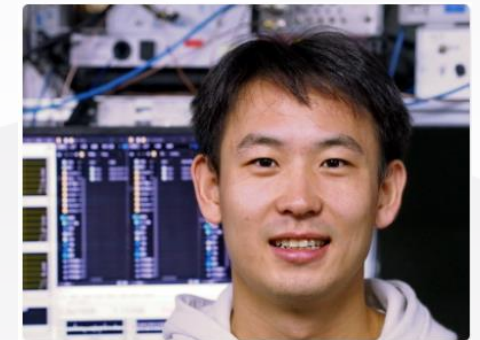
Prof. Hu Shui-Ming



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Tang Jia-Dong



Dong Jun-Feng

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