

# SCALE SEPARATION IN EXOTIC ATOMS

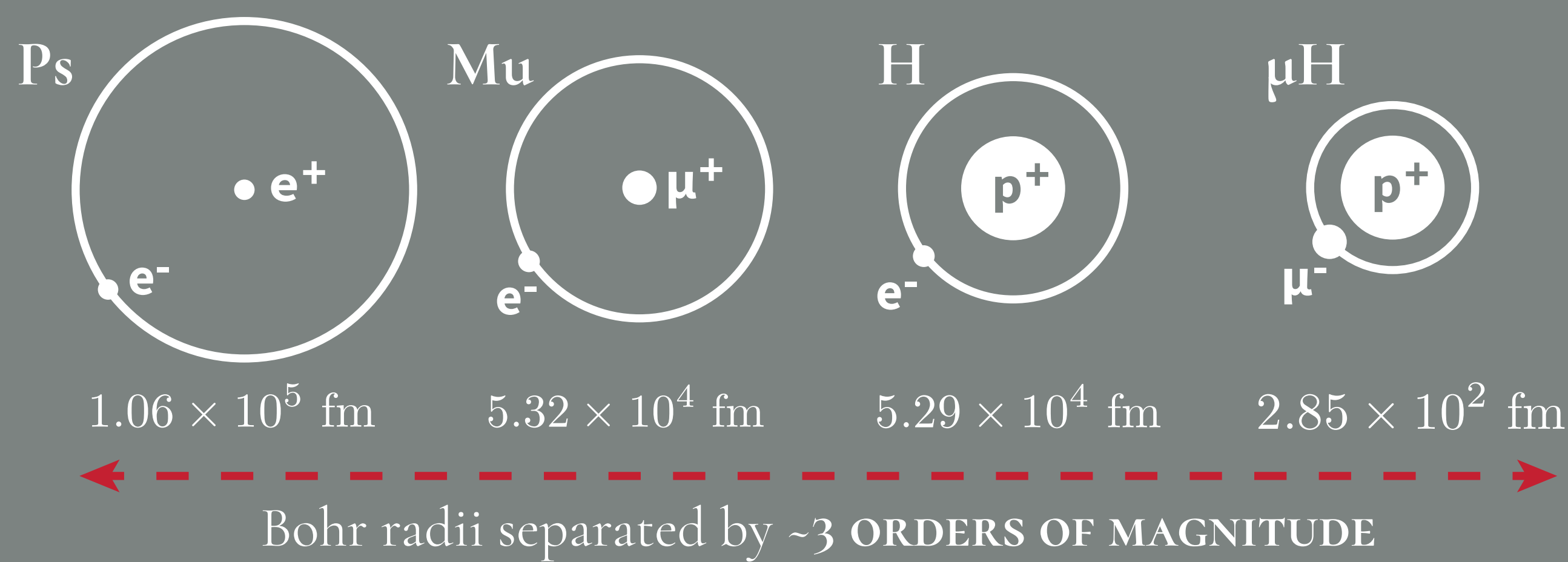
## PRECISION SPECTROSCOPY AS WINDOW TO NEW PHYSICS

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### SEPARATION OF SCALES ACROSS HYDROGEN-LIKE ATOMS

The Bohr radii of hydrogen-like atoms vary based on the reduced mass of the atom:



This leads to significant differences in their atomic spectra.

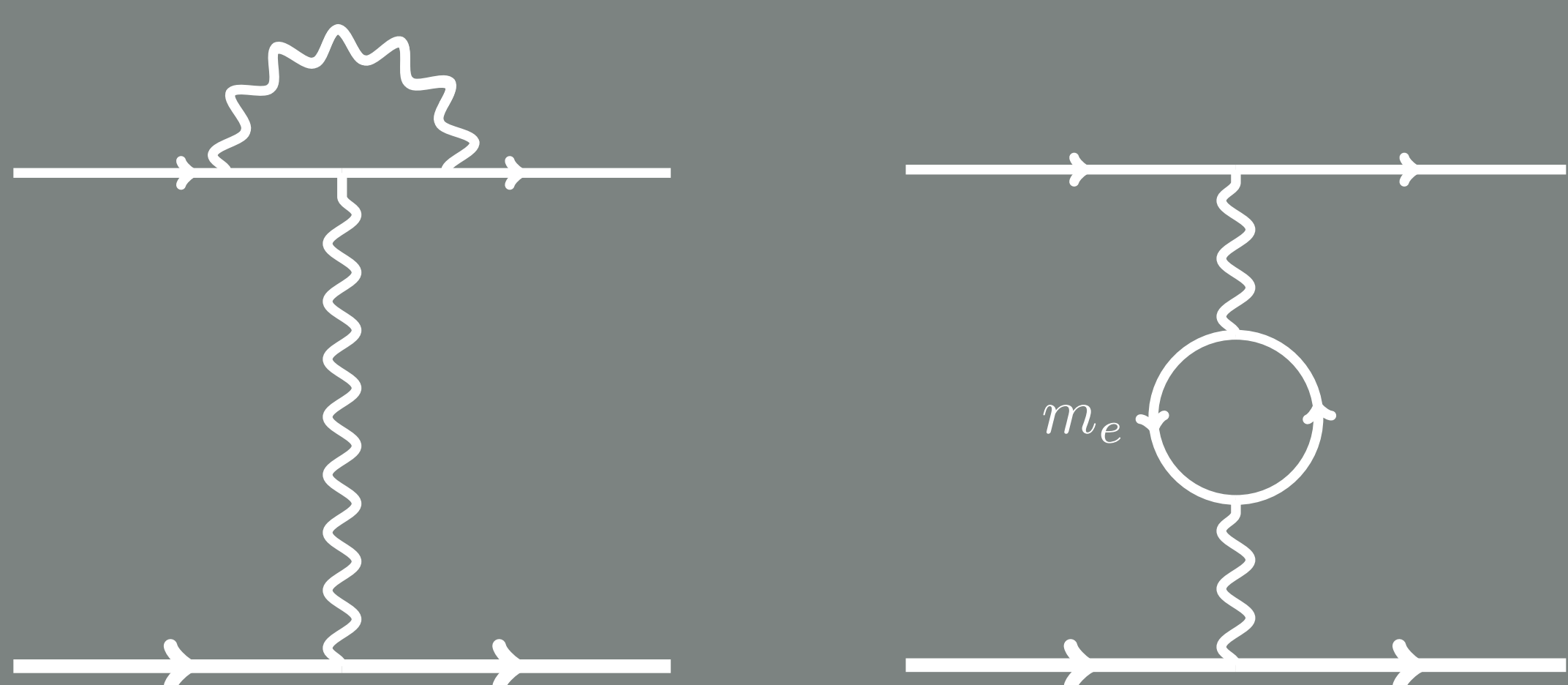


FIG 1: Leading contributions to the H (left) and  $\mu\text{H}$  (right) Lamb Shift.

### FINITE-SIZE CONTRIBUTION: TO EXPAND OR NOT?

- Finite-size contribution to the 2P-2S Lamb shift in hydrogen-like systems due to the proton electric Sachs form factor  $G_E(Q^2)$ :

$$E_{\text{LS}}^{\text{fin.}} = -\frac{(Z\alpha)^4 m_r^3}{2\pi} \int_{t_0}^{\infty} dt \frac{\text{Im} G_E(t)}{(\sqrt{t} + Z\alpha m_r)^4}$$

$m_r$  is the reduced mass of the proton-lepton system,  $Q^2 = -q^2$  is the squared momentum transfer, and  $t_0$  is the lowest particle-production threshold in the t channel.

- Finite-size expansion:

$$E_{\text{LS}}^{\text{fin.}} \simeq -\frac{(Z\alpha)^4 m_r^3}{12} [\langle r^2 \rangle_E - Z\alpha m_r \langle r^3 \rangle_E] + O(\alpha^6)$$

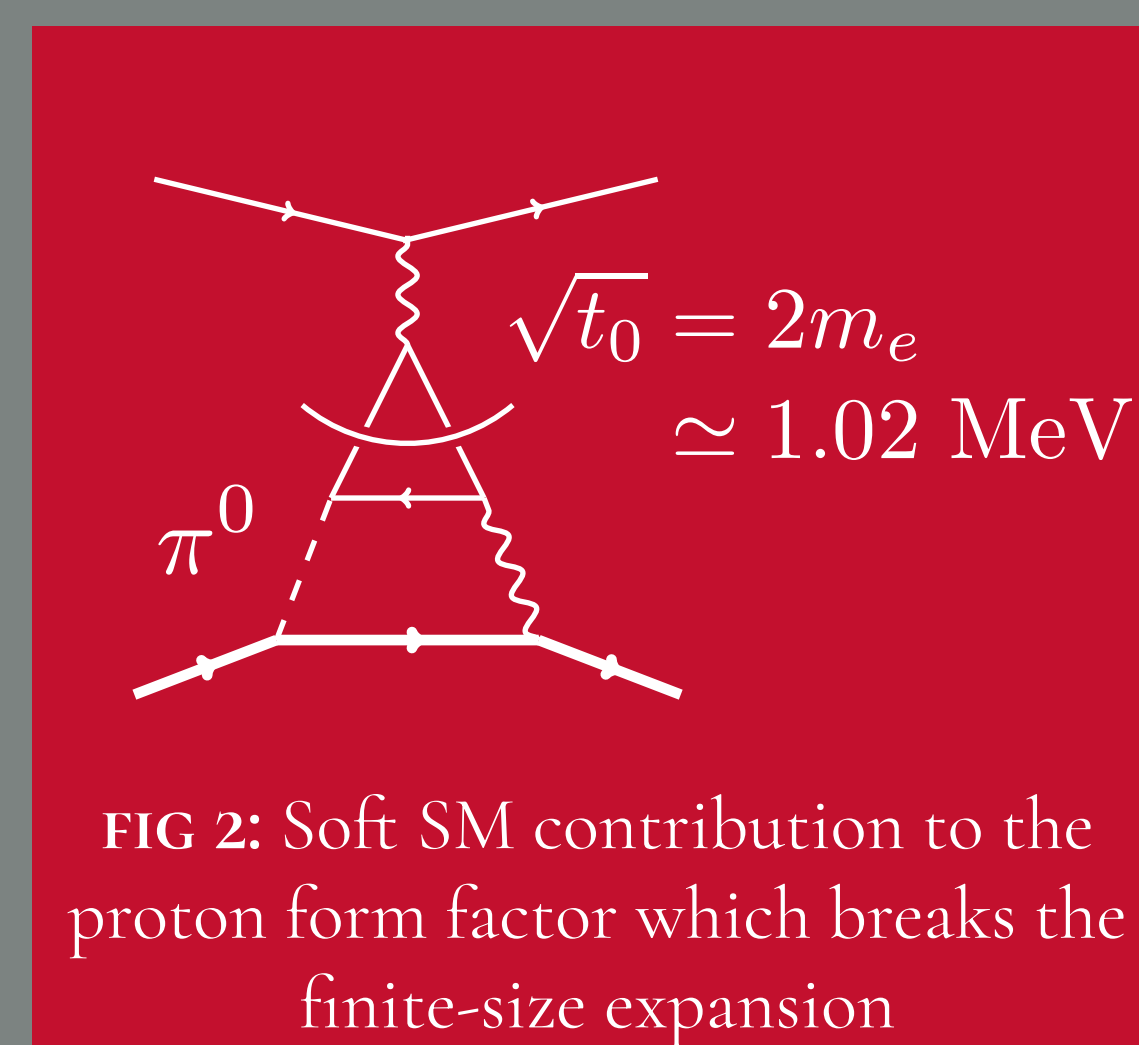
where  $\langle r^2 \rangle_E$  and  $\langle r^3 \rangle_E$  are the second and third moments of the proton charge distribution.

- Breaks down when  $\sqrt{t_0}$  becomes comparable to  $Z\alpha m_r$ , which is the inverse Bohr radius of the system.

TABLE I: Inverse Bohr radii of hydrogen-like atoms

SYSTEM	Ps	Mu	H	$\mu\text{H}$
$Z\alpha m_r [\text{MeV}]$	$1.86 \times 10^{-3}$	$3.71 \times 10^{-3}$	$3.73 \times 10^{-3}$	0.693

### ENHANCED SOFT CONTRIBUTIONS IN THE STANDARD MODEL



- Soft contributions can break the finite-size expansion: see f.i. the light particle cut across the upper loop of the diagram in FIG 2.
- Breaking occurs in systems with  $Z\alpha m_r \sim 2m_e$ , like  $\mu\text{H}$ .
- Not a problem with current experimental accuracy, but...

In hydrogen-like atoms, contributions may be enhanced depending on their lightest t-channel cut compared to the scale of the Bohr radius!

TABLE II: Breaking of the expansion in moments of charge distribution for the 2-loop diagram in FIG 2. Contribution to LS

SYSTEM	EXACT CALCULATION	EXPANSION	CURRENT EXPERIMENTAL ACCURACY
H [kHz]	$4 \times 10^{-11}$	$3 \times 10^{-11}$	3.2
$\mu\text{H} [\mu\text{eV}]$	$-8 \times 10^{-10}$	$3 \times 10^{-8}$	2.3

Each observable should be studied separately. For instance, the expansion of the HFS contribution is breaking for both H and  $\mu\text{H}$ .

TABLE III: Breaking of the expansion in moments of charge distribution for the 2-loop diagram in FIG 2. Contribution to 1S HFS

SYSTEM	EXACT CALCULATION	EXPANSION	CURRENT EXPERIMENTAL ACCURACY
H [ $10^{-6}$ kHz]	-0.009	-0.4	2
$\mu\text{H} [\mu\text{eV}]$	$-10^{-7}$	$-10^{-5}$	3 (1 ppm, projected)

### NEW PHYSICS SEARCHES: PICKING THE RIGHT TOOL FOR THE JOB

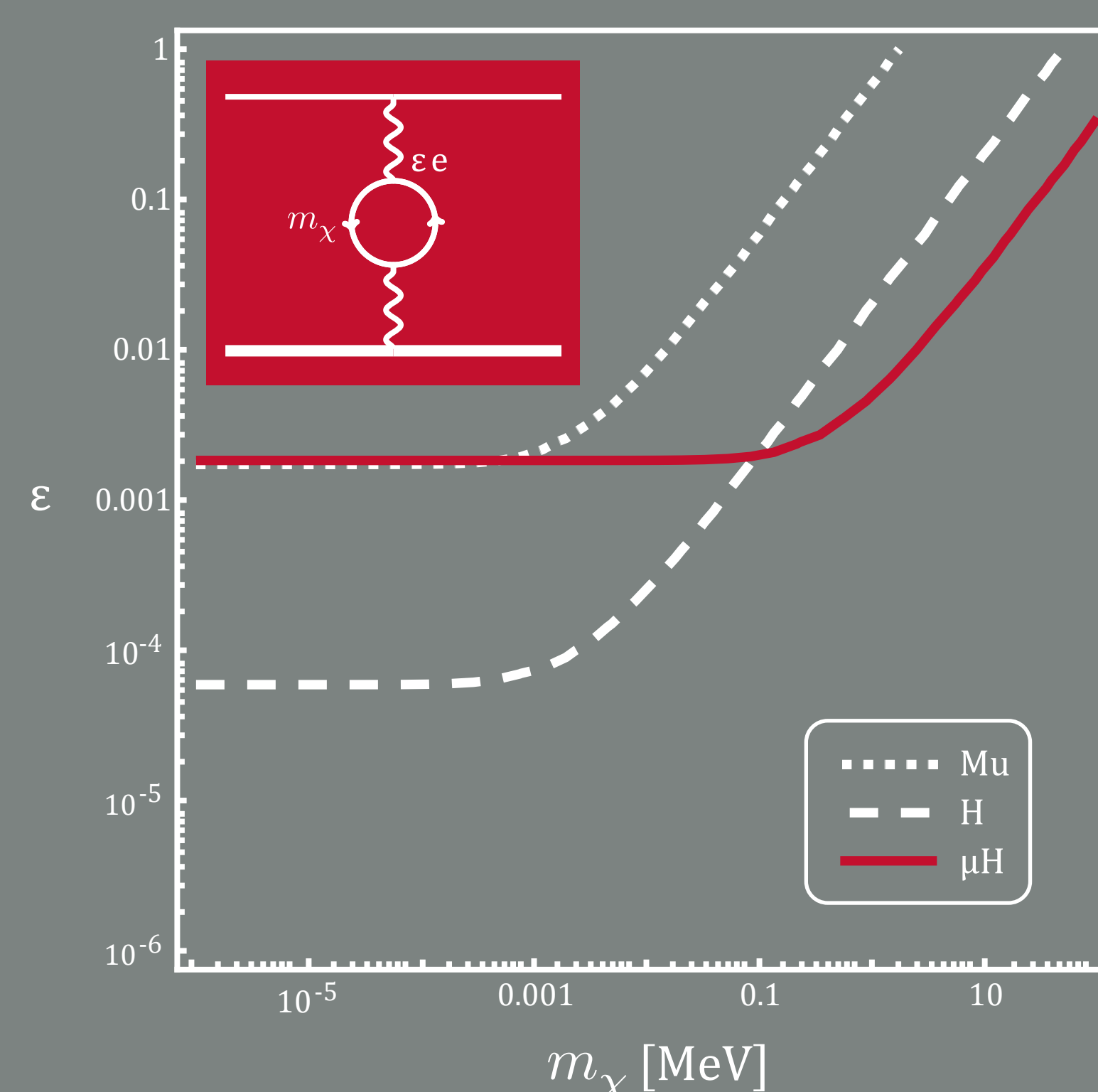


FIG 3: Sensitivity plot for a potential dark matter fermion contribution, indicating when the size of the contribution reaches the present experimental accuracy for the individual atoms

- Different atoms are sensitive to different ranges of New Physics parameters.

A dark matter example:

- State of the art results for the Lamb shift (in  $\mu\text{eV}$ ):  
Mu: 4.3309(105)  
H: 4.37483(1)  
 $\mu\text{H}$ : 202 370.6(2.3)
- $\mu\text{H}$  is less accurately measured than Mu, but it is equally or more sensitive.
- H is measured most accurately, but  $\mu\text{H}$  is still more sensitive at higher  $m_\chi$ !

When using hydrogen-like atoms as labs for New Physics searches, we can use the range of their Bohr radii to our advantage!

How does this affect our calculations?

**LIGHT NEW PHYSICS?**

**DISCUSS!**