

Lepton Flavor and Neutrino Oscillation

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1. Introduction \sim Lepton Flavor in SM

The Standard Model

Lepton

1st generation	$\nu_{eR}^?$	$\nu_{\mu R}^?$	$\nu_{\tau R}^?$
	ν_{eL}	$\nu_{\mu L}$	$\nu_{\tau L}$
	e_R	μ_R	τ_R
	e_L	μ_L	τ_L
	$u_R^{r,g,b}$	$c_R^{r,g,b}$	$t_R^{r,g,b}$
	$u_L^{r,g,b}$	$c_L^{r,g,b}$	$t_L^{r,g,b}$
	$d_R^{r,g,b}$	$s_R^{r,g,b}$	$b_R^{r,g,b}$
	$d_L^{r,g,b}$	$s_L^{r,g,b}$	$b_L^{r,g,b}$

Quark

+ Higgs boson H

Chiral Theory

- No RH neutrino
- L \leftrightarrow R nonsymmetric



Lepton Flavor (e-like, μ -like, τ -like)

is exact symmetry and conserved

Lepton Flavor in SM

Conserved “Charge” resulting from massless neutrinos

Electron, muon, tau number

L_e L_μ L_τ

e^- ν_e μ^- ν_μ τ^- ν_τ

L_e

1

1

L_μ

1

1

L_τ

1

1

Opposite(-1) for
anti particles

Example of conservation

$\pi^- \rightarrow \mu^- \bar{\nu}_\mu$

L_μ

0

=

1

+

(

-

1)

Derivation of lepton flavor charge

Lepton Part Only

$$L_i = \begin{pmatrix} \nu_{Li} \\ e_{Li} \end{pmatrix}, \quad e_{Ri}, \quad (i = 1, 2, 3)$$

Kinetic Part

$$\mathcal{L}_k = \bar{L}_i i \not{D}_L L_i + \bar{e}_{Ri} i \not{D}_R e_{Ri}$$

$$D_{L\mu} = \begin{pmatrix} \partial_\mu + \frac{i}{2} g_1 B_\mu - g_2 \frac{i}{2} W_\mu^0, & g_2 \frac{i}{\sqrt{2}} W_\mu^+ \\ g_2 \frac{i}{\sqrt{2}} W_\mu^-, & \partial_\mu + \frac{i}{2} g_1 B_\mu + \frac{i}{2} g_2 W_\mu^0 \end{pmatrix}$$

$$D_{R\mu} = \partial_\mu + i g_1 B_\mu$$

$$\mathcal{L}_k = \mathcal{L}_{k,diag} + \mathcal{L}_{k,W}$$

$$\mathcal{L}_{k,diag} = \bar{\Phi}_j i \not{D}_j \Phi_j \quad \begin{matrix} D_{\mu j} = \partial_\mu - i e Q_j A_\mu - i g_Z (T_{j3} - Q_j \sin^2 \theta_w) Z_\mu \\ \Phi_j = \{ \nu_L, e_L, e_R \} \end{matrix} \quad \mathbf{3} \times \mathbf{3}$$

Sum of 3 species of Weyl spinors

Invariant under **3** independent unitary transformation

$$U_l, \quad l = \nu_L, e_L, e_R, \quad \mathbf{3} \times \mathbf{3} \text{ Unitary Matrix}$$

$$l \rightarrow U_l l \quad (e_{Li} \rightarrow (U_{e_L} e_L)_i) \quad U_l \text{ independent}$$

$$\mathcal{L}_{k,W} = ig_2 \frac{1}{\sqrt{2}} W_\mu^+ \bar{\nu}_{Li} \gamma_\mu e_{Li} + h.c.$$

To make it invariant $U_{\nu_L} = U_{e_L}$ Is necessary. Reduction of symmetry
Higgs Part

$$\mathcal{L}_H = Y_{ij} \bar{L}_i e_{Rj} + h.c.$$

Y_{ij} **3 × 3 complex** :: diagonalized by **2** unitary matrices

$$Y_{ij} \longrightarrow Y_{diag} = \text{diag}\{y_e, y_\mu, y_\tau\} = U_L Y_{ij} U_R^\dagger$$

$$L_\alpha \equiv U_{L\alpha i} L_i = \begin{pmatrix} U_{L\alpha i} \nu_{Li} \\ U_{L\alpha i} e_{Li} \end{pmatrix}, \quad e_{R\alpha} \equiv U_{Ri} e_{Ri}, \quad \alpha = e, \mu, \tau$$

$$\begin{aligned} \longrightarrow \mathcal{L}_H &= Y_\alpha \bar{L}_\alpha e_{R\alpha} + h.c. \\ &= h^+ (y_e \bar{\nu}_{eL} e_R + y_\mu \bar{\nu}_{\mu L} \mu_R + y_\tau \bar{\nu}_{\tau L} \tau_R) \\ &\quad + h^0 (y_e \bar{e}_L e_R + y_\mu \bar{\mu}_L \mu_R + y_\tau \bar{\tau}_L \tau_R) + h.c. \end{aligned}$$

Since $U_{\nu_L} = U_{e_L}$ kinetic term is invariant

$$\begin{aligned} \mathcal{L}_{k,diag} &= \bar{\Phi}_\alpha i \not{D} \Phi_\alpha \quad \Phi_\alpha = \{\nu_{\alpha L}, e_{\alpha L}, e_{\alpha R}\} \\ \mathcal{L}_{k,W} &= ig_2 \frac{1}{\sqrt{2}} W_\mu^+ \bar{\nu}_{\alpha L} \gamma_\mu e_{\alpha L} + h.c. \end{aligned}$$

Kinetic terms under flavor basis !!

Residual symmetry : : Lepton Flavor

$$\Phi_\alpha = \{\nu_{L\alpha}, e_{L\alpha}, e_{R\alpha}\} \quad \alpha = e, \mu, \tau$$

Paired with same flavor

→ Lagrangian is invariant under phase shift of each flavor

→ **Lepton flavor conservation**

e.g $\{e'_L, e'_R, \nu'_{eL}\} = \exp\{-i\theta_e\}\{e_L, e_R, \nu_{eL}\}$ Phase transformation of electron flavor

$$\begin{aligned} \mathcal{L}'_{k,W} &= ig_2 \frac{1}{\sqrt{2}} W_\mu^+ \bar{\nu}'_e \gamma_\mu e'_L + h.c. \\ &= ig_2 \frac{1}{\sqrt{2}} W_\mu^+ \bar{\nu}_e e^{i\theta} \gamma_\mu e^{-i\theta} e_L + h.c. = \mathcal{L}_{k,W} \end{aligned}$$

From Noether's theorem **Conserved current exists**

In each flavor the conserved current is given by

$$j_\alpha^\mu = \bar{\nu}_{L\alpha} \gamma^\mu \nu_{L\alpha} + \bar{e}_{L\alpha} \gamma^\mu e_{L\alpha} + \bar{e}_{R\alpha} \gamma^\mu e_{R\alpha}$$

“Charge” is expressed as follows and it conserve

$$Q_\alpha = \int d^3x j_\alpha^0$$

For example $\alpha = e$, that is, electron flavor charge is given in terms of creation and annihilation operators of electrons

$$Q_e = L_e = \int d^3p \sum_{l=\nu_{eL}, e_L, e_R} b_l^\dagger(\mathbf{p})b_l(\mathbf{p}) - d_l^\dagger(\mathbf{p})d_l(\mathbf{p})$$

$b^\dagger b$ number operator for particle

$d^\dagger d$ number operator for anti - particle

Electron and electron neutrino $L_e = +1$

Positron and anti-electron neutrino $L_e = -1$

Similarly muon and tau flavor charge L_μ, L_τ is defined.

Lepton Flavor is conserved under SM

Electron, muon, tau number

	L_e	L_μ	L_τ				
	e^-	ν_e	μ^-	ν_μ	τ^-	ν_τ	Opposite(-1) for anti particles
L_e	1	1					
L_μ			1	1			
L_τ					1	1	

If SM is correct,
in **all** process, these numbers are **conserved**



Contraposition

If **non-conserved** is found, SM is not correct

With additional particles and hence additional operator in Lagrangian,
in general, under the transformation

$$\{\alpha'_L, \alpha'_R, \nu'_{\alpha L}\} = \exp\{-i\theta_\alpha\} \{\alpha_L, \alpha_R, \nu_{\alpha L}\} \quad \alpha = e, \mu, \tau$$

+ appropriate transformation for extra particles

Lagrangian is not invariant

→ Lepton flavor **cannot be defined**

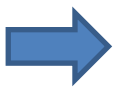
→ Lepton flavor “charge” defined under SM Lagrangian
cannot be conserved

Status of LFV with charged lepton

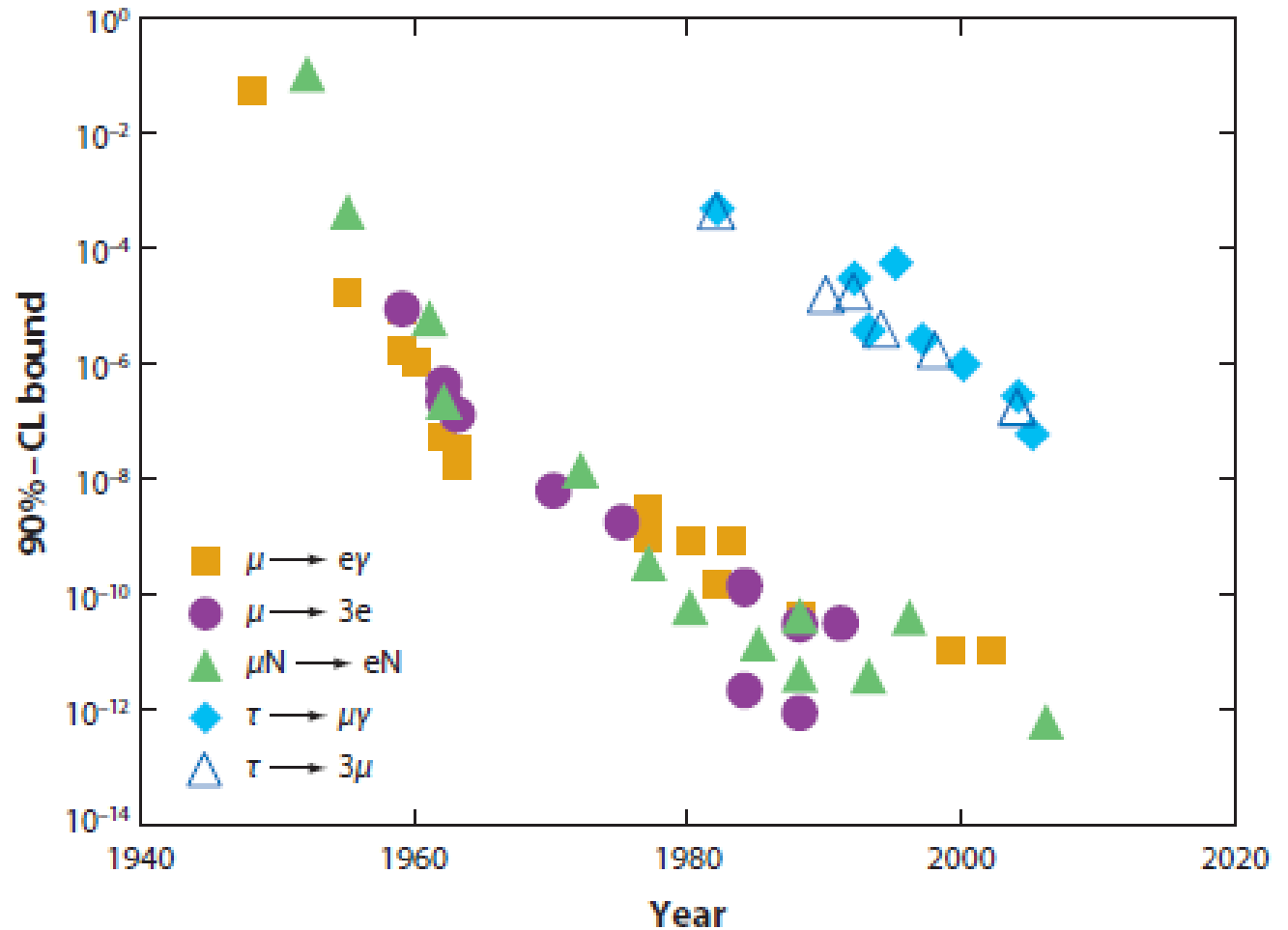
$$\mu^- \rightarrow e^- \gamma$$
$$L_\mu \quad 1 = 0 + 0$$
$$L_e \quad 0 = 1 + 0$$

Annu. Ref. Nucl. Part. Sci. 2008. 58:315-41
W. J. Marciano, T.Mori, and J. M. Roney

No
observation
of CLFV



No doubt
on SM
from CLFV



2. Lepton flavor violation

$$\{\alpha'_L, \alpha'_R, \nu'_{\alpha L}\} = \exp\{-i\theta_\alpha\} \{\alpha_L, \alpha_R, \nu_{\alpha L}\} \quad \alpha = e, \mu, \tau$$

For LF to be defined, Lagrangian must be invariant under this transformation with appropriate transformation on extra particles

If new Lagrangian is not invariant

→ Lepton flavor **cannot be defined**

→ Lepton flavor “charge” as defined under SM Lagrangian **cannot be conserved**

Simplest example

Neutrino mass term with **RH neutrinos** (SM singlets) ν_{Ra} :: Dirac mass term

$$\mathcal{L}_{H+} = \tilde{H} \tilde{Y}_{\alpha a} \bar{L}_\alpha \nu_{Ra} + h.c$$

Flavor basis α is fixed by **charge lepton mass**.

We **cannot rotate** lepton doublet.

If nature choose $Y_{\alpha i}$ to be diagonalized by rotating ν_{Ra} , $\nu_{R\alpha} \equiv U_{R\alpha a} \nu_{Ra}$

Then $\mathcal{L}_{H+} = \tilde{H} \tilde{Y}_\alpha \bar{L}_\alpha \nu_{R\alpha}$, and hence LF is defined as a

result of

$$\{\alpha'_L, \alpha'_R, \nu'_{L\alpha}, \nu'_{R\alpha}\} = \exp\{-i\theta_\alpha\} \{\alpha_L, \alpha_R, \nu_{L\alpha}, \nu_{R\alpha}\}$$



Appropriate transformation

In general, we need by unitary transformation to get mass basis for neutrino

$$\tilde{Y}_{\alpha a} \rightarrow \text{diag}\{\tilde{Y}_i\} = U_{MNS}^\dagger \tilde{Y}_{\alpha a} U_R^\dagger$$

→ Lepton flavor **cannot be defined**

→ Lepton flavor “charge” as defined under SM Lagrangian cannot be conserved

$$\tilde{H} \tilde{Y}_{\alpha a} \bar{L}_\alpha \nu_{Ra} = h^0 \tilde{Y}_i \bar{\nu}_{Li} \nu_{Ri} + h^- \tilde{Y}_{\alpha i} \bar{\alpha}_L \nu_{Ri}$$

Diagonalized mass

In another words flavor basis do not coincide with mass basis

$$\nu_{L\alpha} \neq \nu_{Li}$$

Interaction with W boson,

$$W_\mu^+ \bar{\nu}_{\alpha L} \gamma_\mu e_{\alpha L} = W_\mu^+ \bar{\nu}_{Li} U_{MNS}^\dagger \gamma_\mu e_{\alpha L}$$

Mass base mix with each other. -> Flavor changing processes appear
seed of neutrino oscillation

Incidentally, dirac mass terms, in general, conserve
lepton number


$$L_e + L_\mu + L_\tau = L$$

$$\mu^- \rightarrow e^- \gamma \quad \text{can happen}$$

$$L \quad 1 = 1 + 0$$

Lepton number = A part of particle number
 = (particle =1 & antiparticle=-1)

c.f. Majorana mass term leads lepton number (in general particle number) violation

 **neutrinoless double beta decay**
 $\mu^- \rightarrow e^+$

not necessary neutrino majorana mass term

3. Neutrino oscillation

In SM, neutrino flavor is defined with paired charged lepton

Beta decay, electron is emitted (Le=1) = anti-electron neutrino emitted (Le=-1)

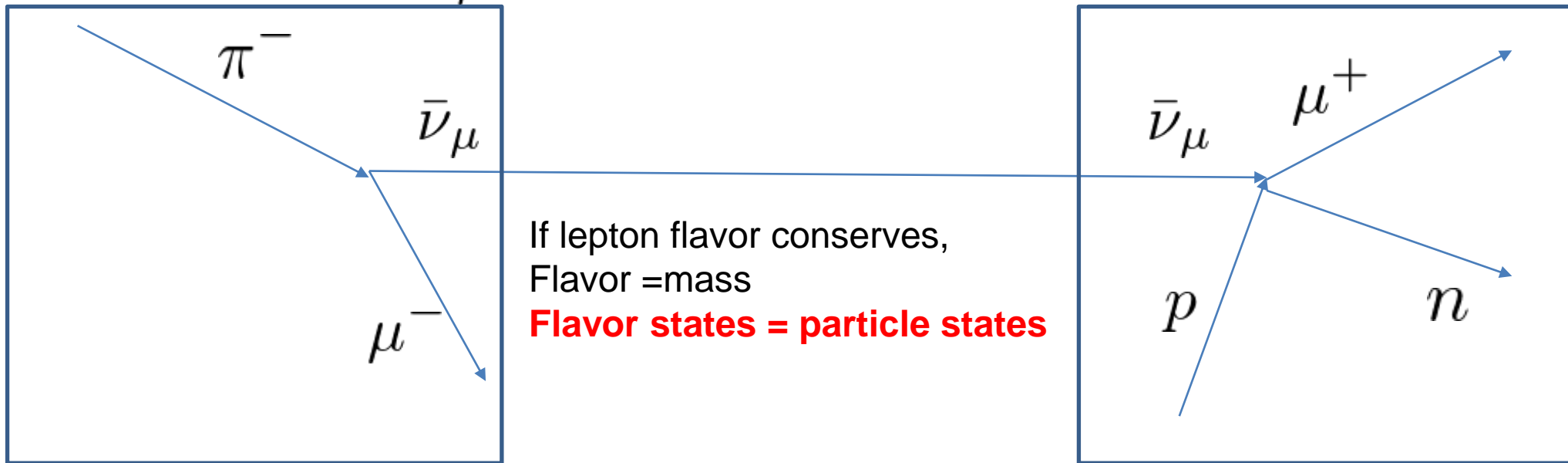
→ electron number $0=1+(-1)$

$$n \rightarrow p + e^- + \bar{\nu}_e$$

$$L_e \quad :: \quad 0 = 0 + 1 + (-1)$$

Neutrino oscillation

$$\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$$



creation

as a whole

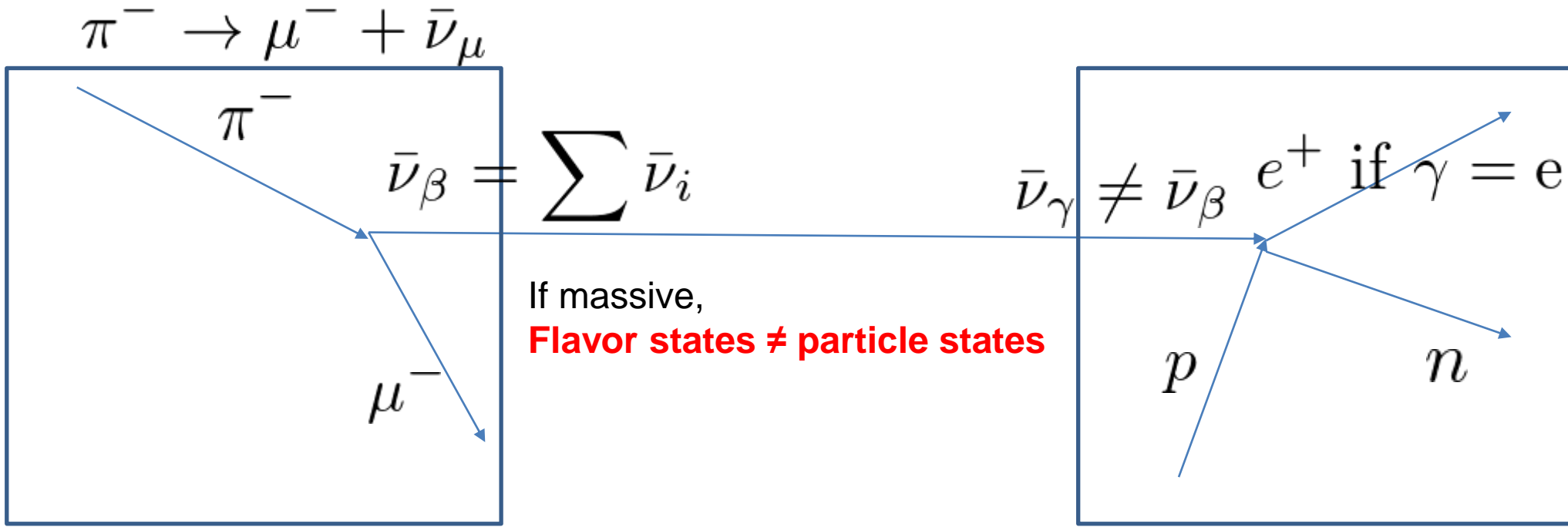
$$\pi^- + p^+ \rightarrow \mu^- + \mu^+ + n$$

detection

$$L_\mu \quad :: \quad 0 + 0 = 1 + (-1)$$

If neutrino is massive,

Neutrino oscillation



creation

as a whole

$$\pi^- + p^+ \rightarrow \mu^- + e^+ + n$$

$$L_e :: 0 + 0 = 0 + (-1)$$

$$L_\mu :: 0 + 0 = 1 + (0)$$

detection

LFV!! Logically SM is **incorrect** !!

To insist it is due to neutrino oscillation, more information has been accumulated
If neutrino is massive,

Maki, Nakagawa, Sakata

Flavor eigenstate \neq Mass eigenstate
Interaction state Particle state

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U_{\alpha i} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Propagation of neutrinos: As a particle = mass eigenstate

Creation of neutrinos : weak interaction accompanied
with partner charged lepton
Superposition of mass eigenstates



Multiple propagation of neutrinos

Quantum interference

= Neutrino Oscillation

Reactor Neutrino Example

Two flavor approximation

electron neutrino is emitted

$$\nu^f(0) = \nu_e = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad \text{incidentally} \quad \nu_\mu = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

At a distance $L = t$ survival probability of ν_e

$$P_{\nu_e \rightarrow \nu_e} = |\nu_e^\dagger \nu^f(L)|^2 = 1 - \sin^2 2\theta \sin^2 \frac{\delta m^2 L}{4E} \quad \text{Quantum interference (oscillation)}$$

$$\rightarrow 1 - \frac{1}{2} \sin^2 2\theta \quad \text{Large } \delta m^2 \text{ and/or Low } E$$

$$= \cos^4 \theta + \sin^4 \theta \quad \text{Quantum effect disappears}$$

Merely transition

$$\nu_e \xrightarrow{\cos \theta} \nu_1 \xrightarrow{\cos \theta} \nu_e \quad \text{Amplitude of this transition} \quad \cos^2 \theta$$

Similarly $\sin^2 2\theta$ for 2nd state

$$\text{incidentally } P_{\nu_e \rightarrow \nu_\mu} = |(0, 1) \nu^f(x)|^2 = \sin^2 2\theta \sin^2 \frac{\delta m^2 L}{4E}$$

As a result,

We have to explain neutrino masses and lepton mixings → Lepton Flavor Violation

Neutrinos

★ Neutral (Electromagnetic and color), real under SU(2)

★ Tiny mass (also mass pattern)

○ Neutral :: two types of mass term

Dirac : “partner” is necessary. It is neutral (= no charge) under **SM**

so-called Right-Handed(RH) neutrino $\bar{\nu}_R$. Higgs doublet can be reused

$$y H \bar{\nu}_R L \supset m \bar{\nu}_R \nu_L$$

Majorana : self mass term. Within **renormalizable**, we need to introduce SU(2) triplet ϕ

$$y \phi L^T C L \supset \nu_L^T C \nu_L$$

If **nonrenormalizable**, with cutoff without new particle

$$\frac{h_{ij}}{2\Lambda} (H L_i)(H L_j)$$

though Λ indicates new physics = new particle

For example, ν_R majorana mass can be new scale Λ . It is singlet **under SM**

$$M \nu_R^T C \nu_R \text{ Is allowed}$$

With Dirac mass term $m \bar{\nu}_R \nu_L$, we have mass term for **neutral particle under**

$$(\nu_L, \nu_R^C) \begin{pmatrix} 0 & m \\ m & M \end{pmatrix} \begin{pmatrix} \nu_L \\ \nu_R^C \end{pmatrix}$$

Eigenstate values are neutrino masses. Especially $m \ll M$

$$\frac{-m}{M}, M$$

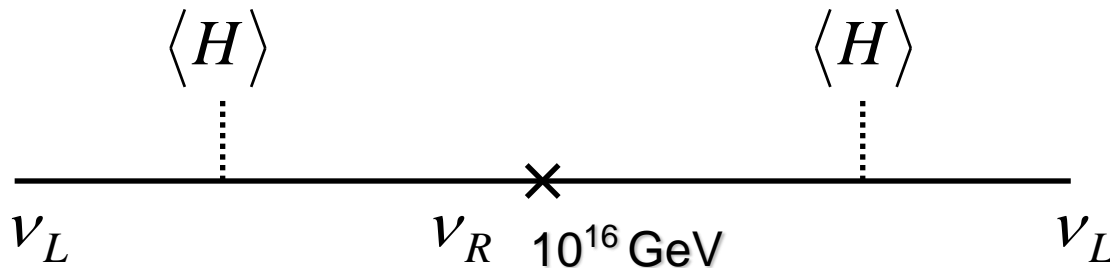
Seesaw

Particle states

$$\nu_L \quad \nu_R$$

Gell-mann *et al*, Yanagida

Λ Is RH neutrino Majorana masses. Graphically

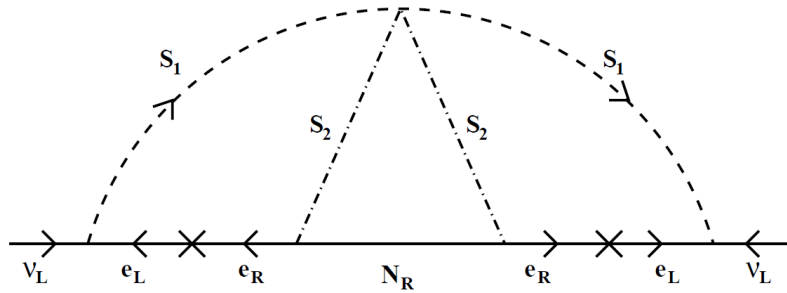


$$m_\nu = \frac{(100)^2}{10^{16}} \sim 10^{-12} \text{ GeV} \sim 10^{-3} \text{ eV}$$

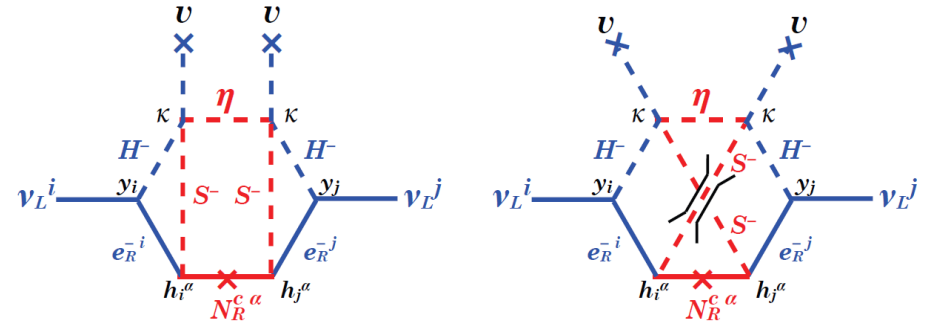
$m \ll M$ Is not necessary. Different type of models

Another example = loop correction Zee model · radiative seesaw

Krauss *etal*



Aoki *etal*



Majorana mass term for left-handed neutrinos

$$\frac{h_{ij}}{2\Lambda} (HL_i)(HL_j)$$

○ Majorana mass term

“violates”

Not only Lepton Flavor
But also Lepton Number

➔ Lepton **number** changing process

Example

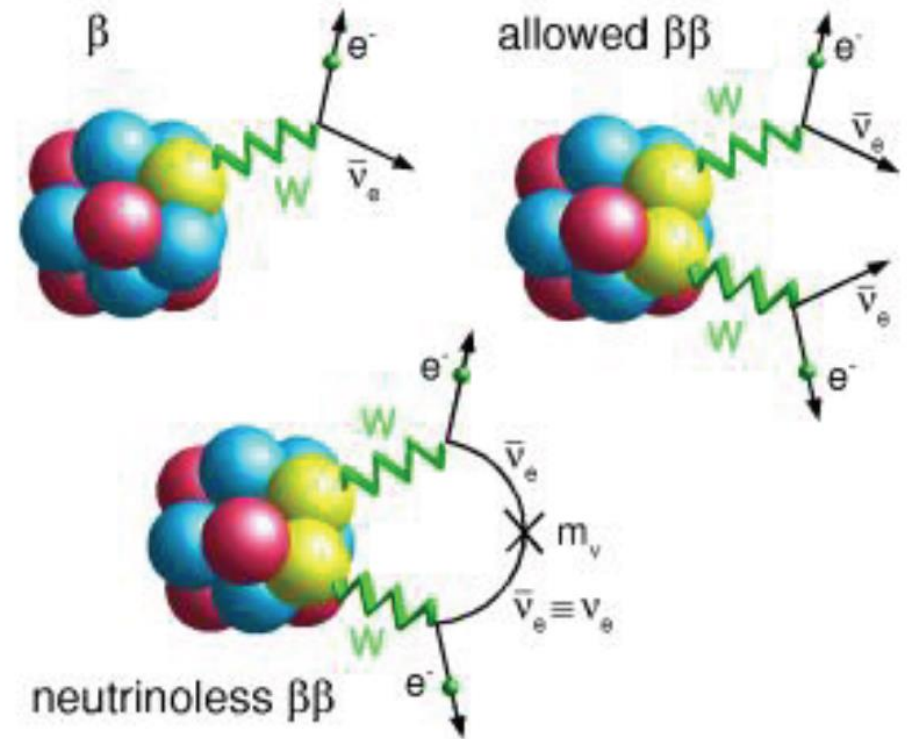
$$(A, Z) \rightarrow (A, Z + 2) + 2e^-$$

($0\nu 2\beta$) decay

$$m_{ee} = U_{eh}^2 m_h = c_{13}^2 (m_1 c_{12}^2 + m_2 s_{12}^2 e^{2i\alpha}) + m_3 s_{13}^2 e^{2i\beta'}$$

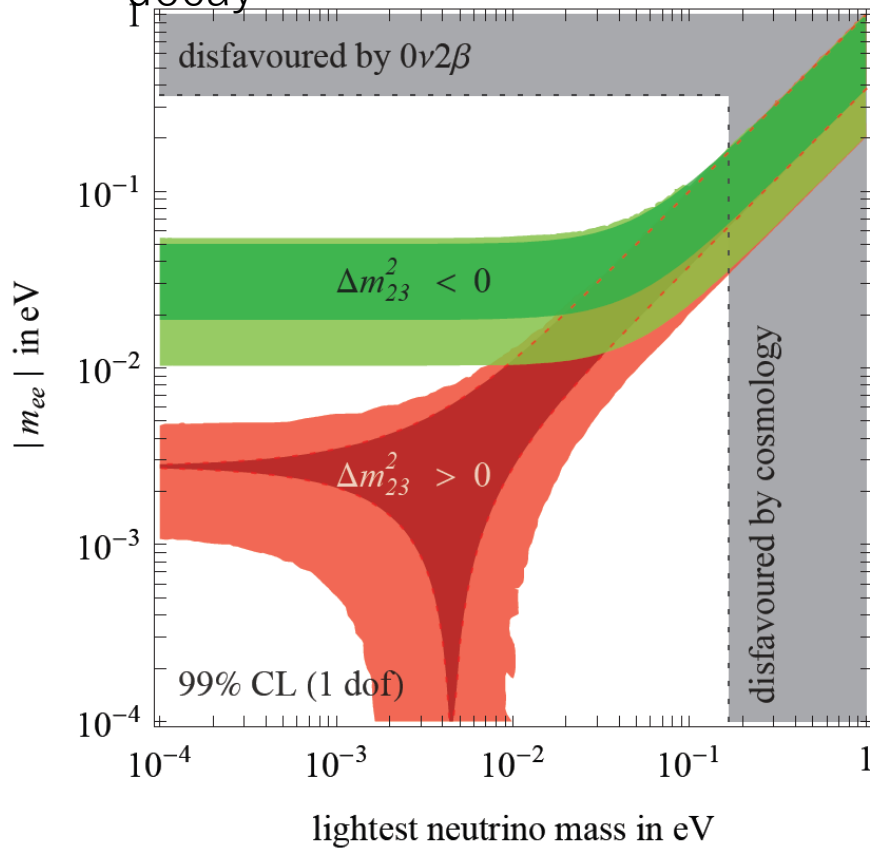
$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha} & 0 \\ 0 & 0 & e^{i\beta} \end{pmatrix}$$

Also $\mu^- \rightarrow e^+$ in muonic atom



Romanino

m_{ee} prediction from neutrino oscillation and constraint from Neutrinoless double beta decay

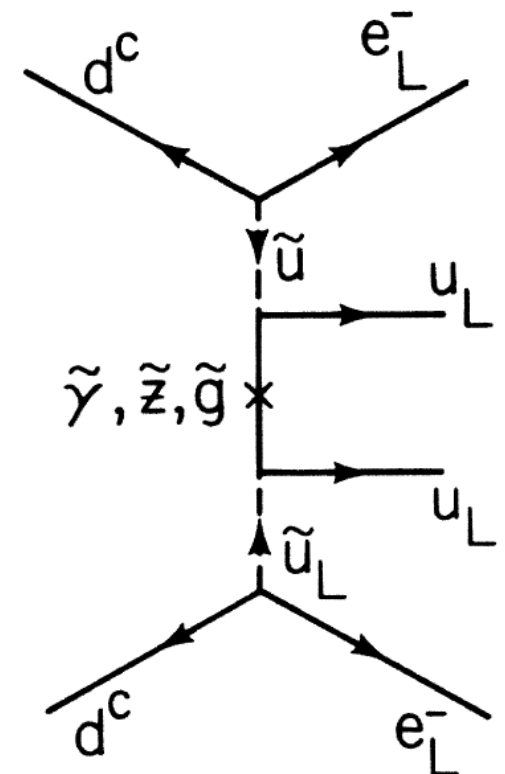


Two kinds of prediction from neutrino oscillation
 Normal hierarchy (NH) and inverted hierarchy (IH)
 Note

“ Majorana mass for left-handed neutrino
 → neutrinoless double beta decay “

Always holds
 but conversion
 is not true !!

Example from
 SUSY



$$\lambda'_{ijk} L_i Q_j D_k^c$$

Mohapatra 1986

Lepton flavor violation and particle number violation has
 different origin !!!

Majorana mass term \neq neutral
 Majorana mass term = real representation,
 can be charged

4. Charged Lepton Flavor violation

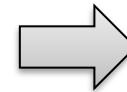
Lepton Flavor is exact symmetry in SM

as long as neutrinos are massless

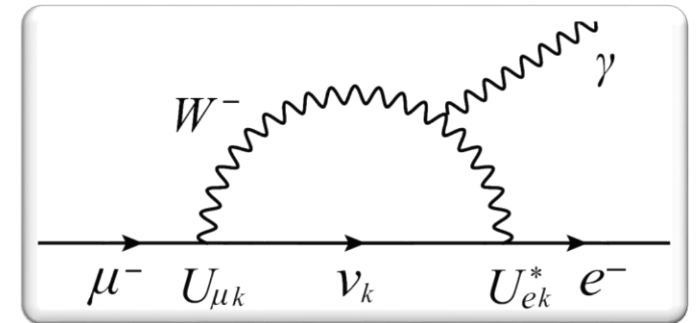
Charged Lepton Flavor Violation (cLFV) through Lepton Mixing in the neutrino oscillation

But ...

$$\text{BR}(\mu \rightarrow e\gamma) \sim \left(\frac{\delta m_\nu^2}{m_W^2} \right)^2 < 10^{-54}$$

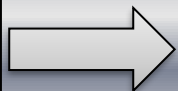


Invisible, eternally



Strong suppression of FCNC by GIM

Detection of the LFV signal



Clear evidence for beyond SM

Indeed, in physics beyond SM,

Large FCNC is expected

Particularly Combining with neutrino oscillation

Large FCNC in charged lepton is expected

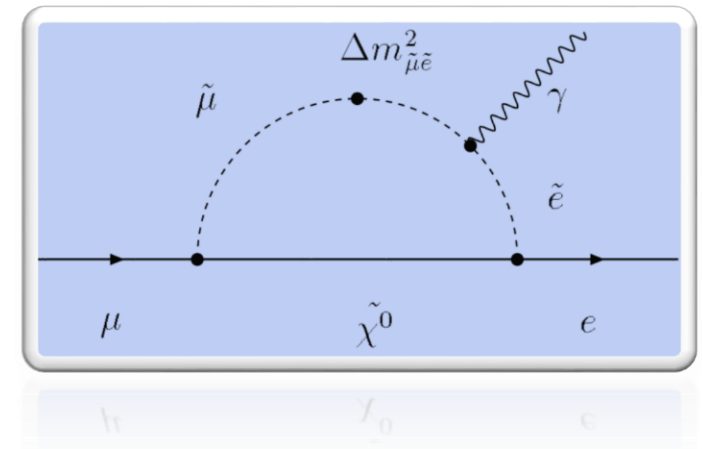
(must appear ??)

e.g. a supersymmetric model

Enhancement of LFV
through the slepton mixing

➔ Detectable at future experiments

➔ **Search for LFV with charged lepton
is inevitable**



cLFV from muon decay

Upper limit on Br

$$\mu^+ \rightarrow e^+ \gamma < 4.2 \times 10^{-13}$$

$$\mu^+ \rightarrow e^+ e^+ e^- < 1.0 \times 10^{-12}$$

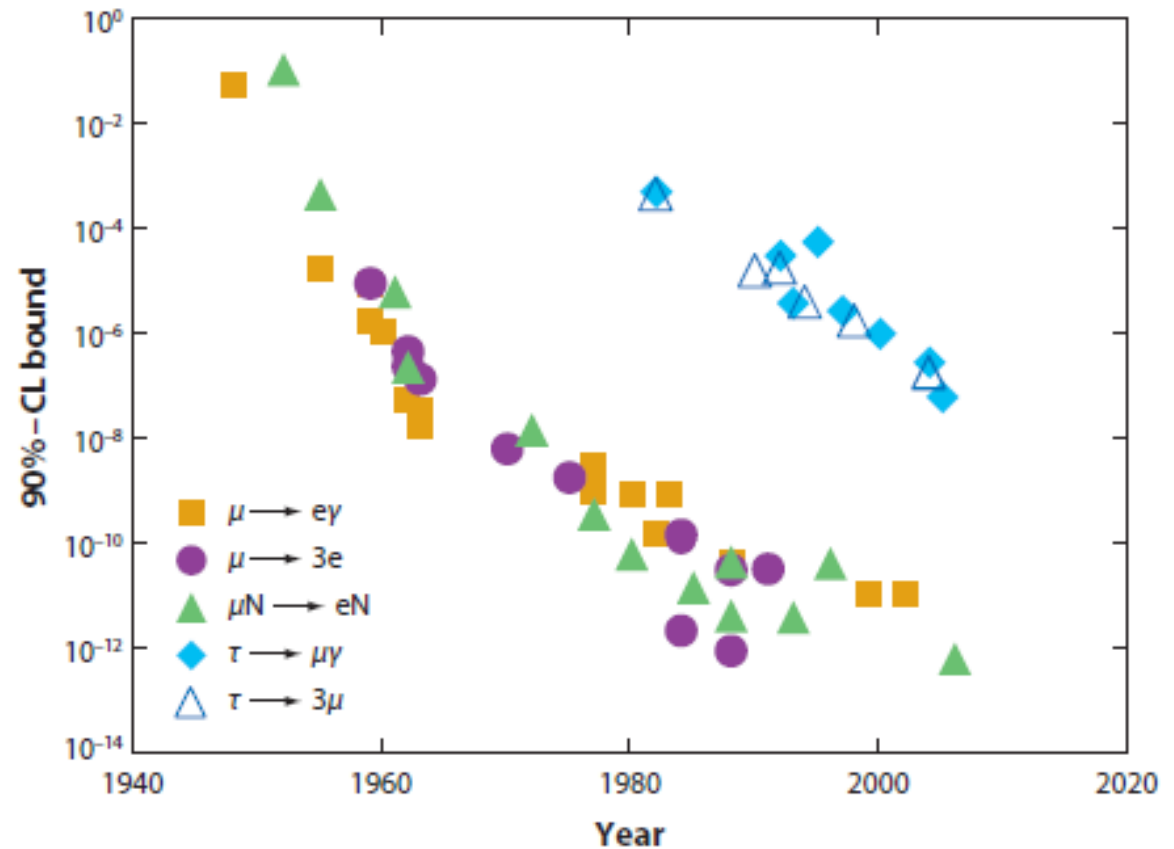
$$\mu^- \text{Ti} \rightarrow e^- \text{Ti} < 6.1 \times 10^{-13}$$

$$\mu^- \text{Au} \rightarrow e^- \text{Au} < 7 \times 10^{-13}$$

$$\mu^+ e^- \rightarrow \mu^- e^+ < 8.3 \times 10^{-11}$$

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W. J. Marciano, T. Mori, and J. M. Roney

Long history



Effective operators for CLFV

A) Loop vs Tree

$$\mu^+ \rightarrow e^+ \gamma \quad :: \text{Loop only, dipole}$$

Gauge Symmetry forbids tree contribution

$$\mu^+ \rightarrow e^+ e^- e^+ \quad :: \text{Loop and Tree}$$

$$\mu^- N \rightarrow e^- N$$

e.g. Loop = dipole + quark bilinear = $\mu^- N \rightarrow e^- N$

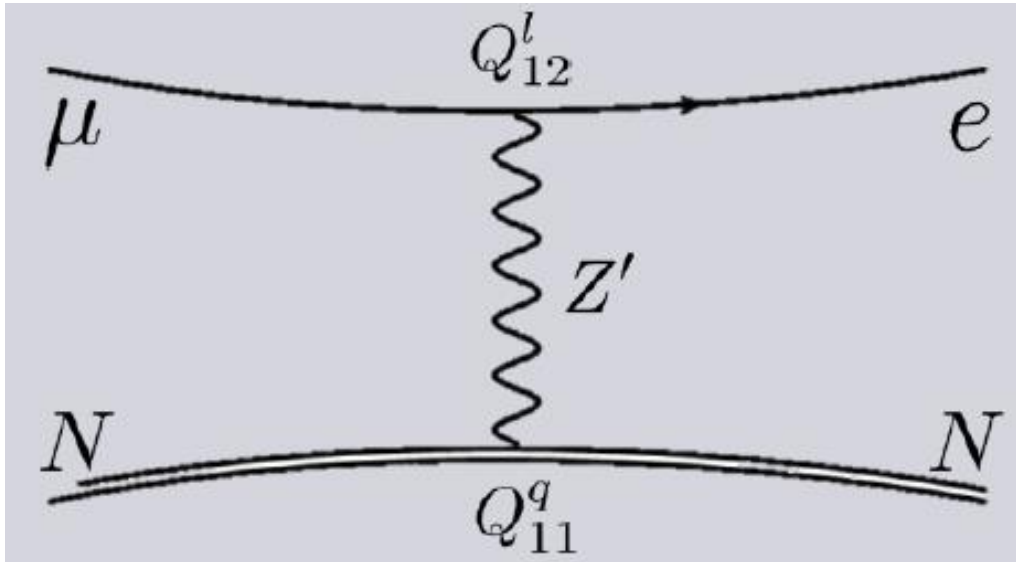
$\sim \alpha$ smaller than $\mu \rightarrow e \gamma$

Tree :: singlet particle is necessary for conversion!

Charge 2 is OK for $\mu \rightarrow 3e$

Leptoquark is OK for $\mu \rightarrow e$

Tree, e.g.



No direct relation with MEG
NO suppression

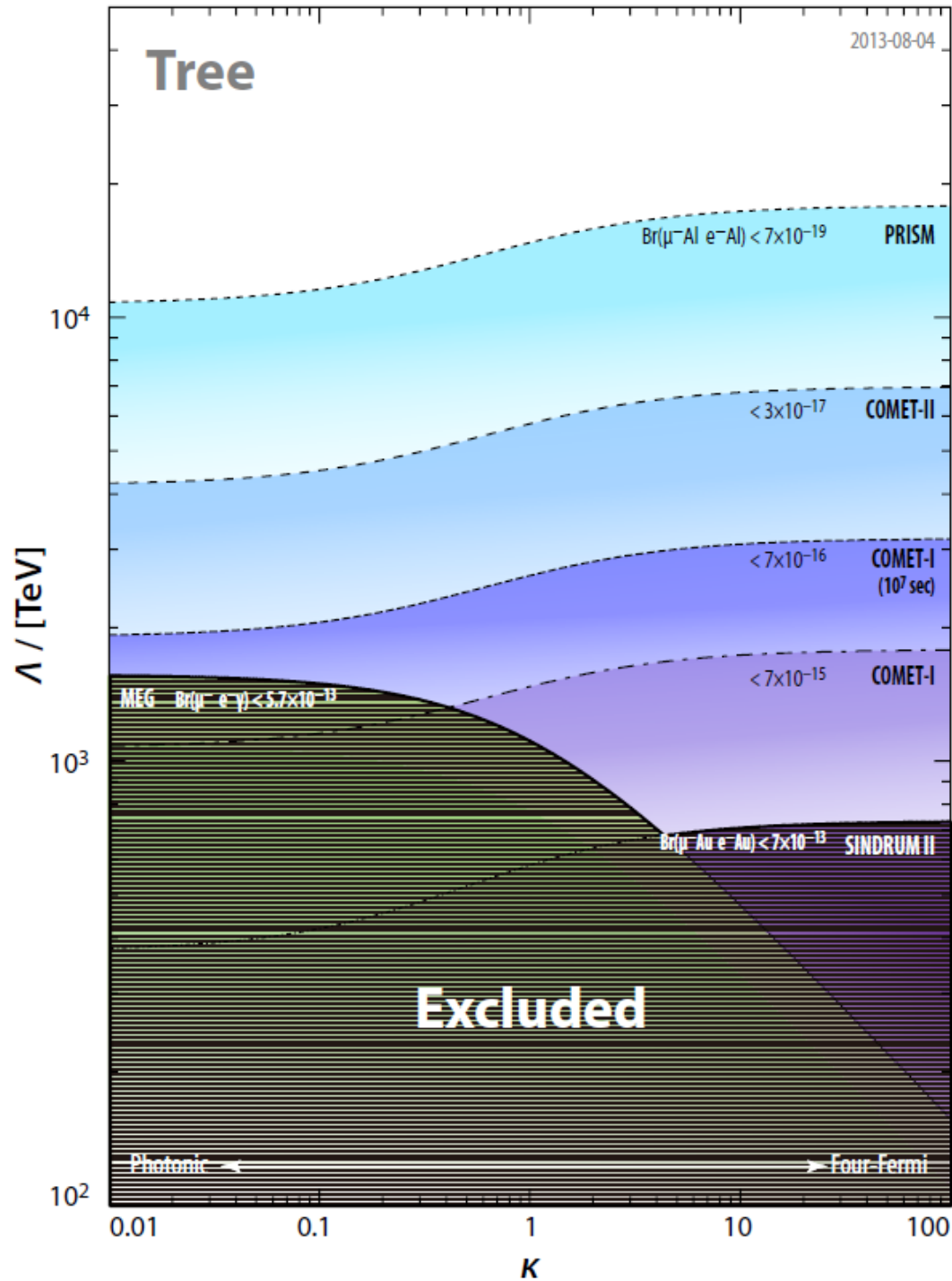
We can parameterize the relative strength

$$\mathcal{L} = \frac{1}{1 + \kappa} \frac{m_\mu}{\Lambda^2} \bar{\mu}_R \sigma^{\mu\nu} e_L F_{\mu\nu} + \frac{\kappa}{1 + \kappa} \frac{1}{\Lambda^2} (\bar{\mu}_L \gamma^\mu e_L) (\bar{q}_L \gamma_\mu q_L)$$

$\kappa \sim \alpha$:: dipole type, say SUSY with R parity

In general, Model Dependent

MEG



PRISM

COMET Phase-II

COMET Phase-I

B) Vector vs Scalar

cLFV is mediated by new particle(s)

Vector Boson ::

Boson with broken gauge

So-called Z' Model, Extra $U(1)$ from $SO(10)$ GUT

Kaluza-Klein mode of gauge

Higher dimensional models have massive modes of gauge bosons

Scalar Boson ::

From symmetry = SUSY

Extension of Higgs :: more 2plet, 3plet for nu mass

Explanation for new physics

Vector type interaction

If Vector boson has no charge

$$\mu^+ \rightarrow e^+ e^- e^+ \text{ and } \mu^- N \rightarrow e^- N$$

can occur at tree level

in a wide sense Z' model

$$\mu^+ \rightarrow e^+ \gamma \longleftrightarrow \mu^- N \rightarrow e^- N$$

irrelevant

cLFV Interaction

$$\frac{g_{Z'}}{\sin \theta_W} \bar{l}_i Q_{ij} \gamma^\mu l_j Z'_\mu$$

Different Q's !!

Experiment type	Charges probed
$\mu^- N \rightarrow e^- N$	Q_{12}
$\mu^+ \rightarrow e^+ \gamma$	$Q_{13} Q_{23}$ (and all others)
$\mu^+ \rightarrow e^+ e^- e^+$	$Q_{11} Q_{12}$
$e^+ e^- \rightarrow \mu^+ \tau^- (\mu^- \tau^+)$	$Q_{11} Q_{23}$ ($Q_{12} Q_{13}$)
$e^+ e^- \rightarrow \mu^+ \mu^-$	$Q_{11} Q_{22}$ (Q_{12})
muon $g - 2$	Q_{23} ($Q_{21} Q_{22}$)

Table 1: The CFLV experiments and the corresponding Z' charges probed at lowest order pro-

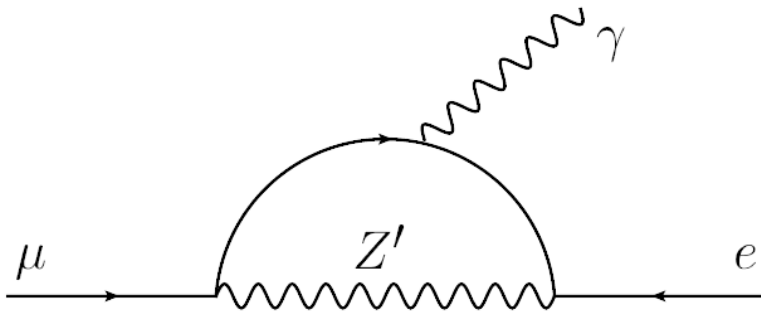


Figure 2: $\mu^+ \rightarrow e^+ \gamma$ in the Z' models.

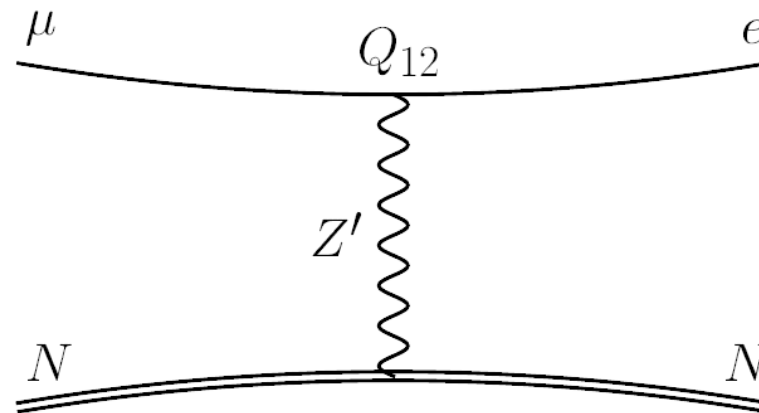
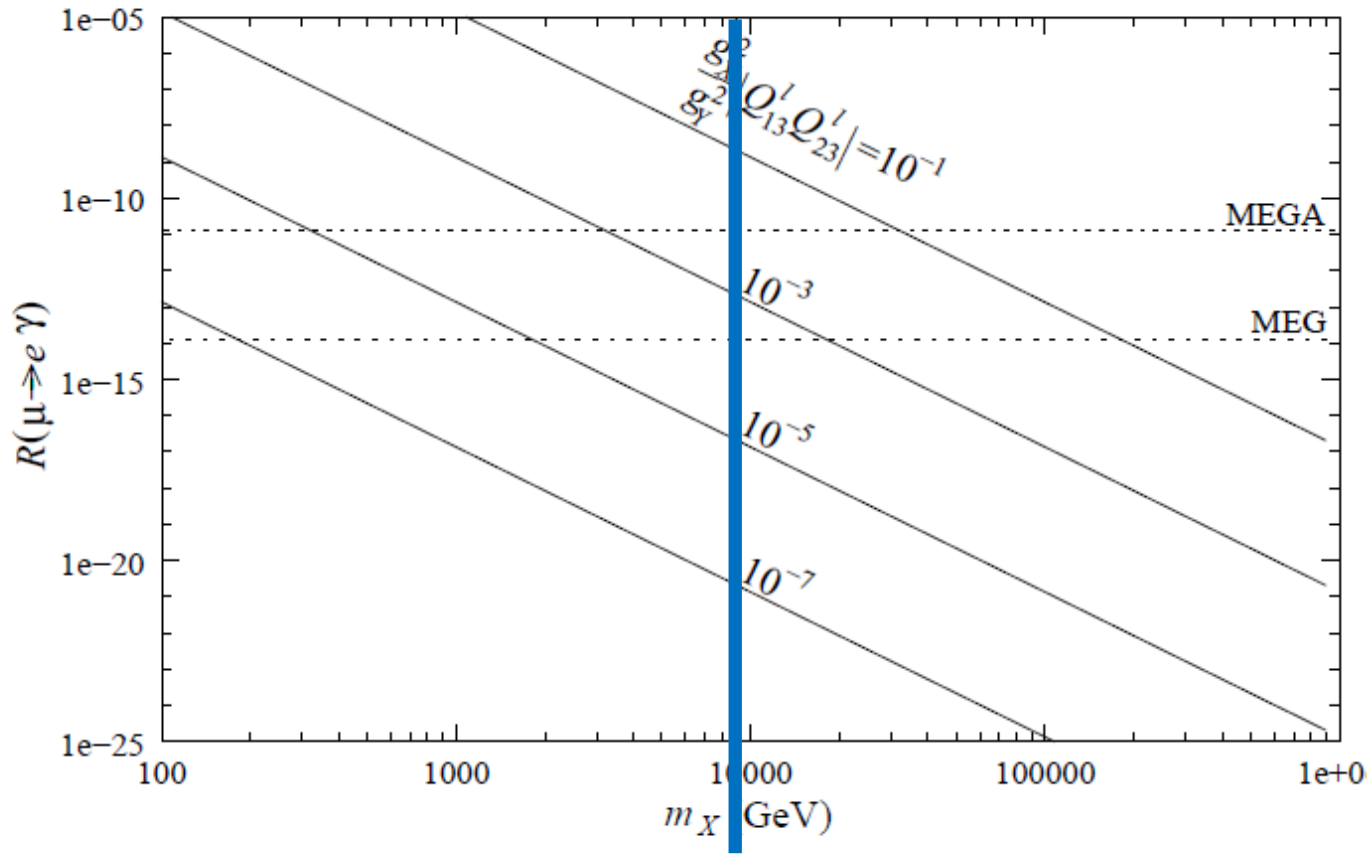


Figure 3: Non-photon diagram of $\mu^- \rightarrow e^-$ conversion in the Z' models.

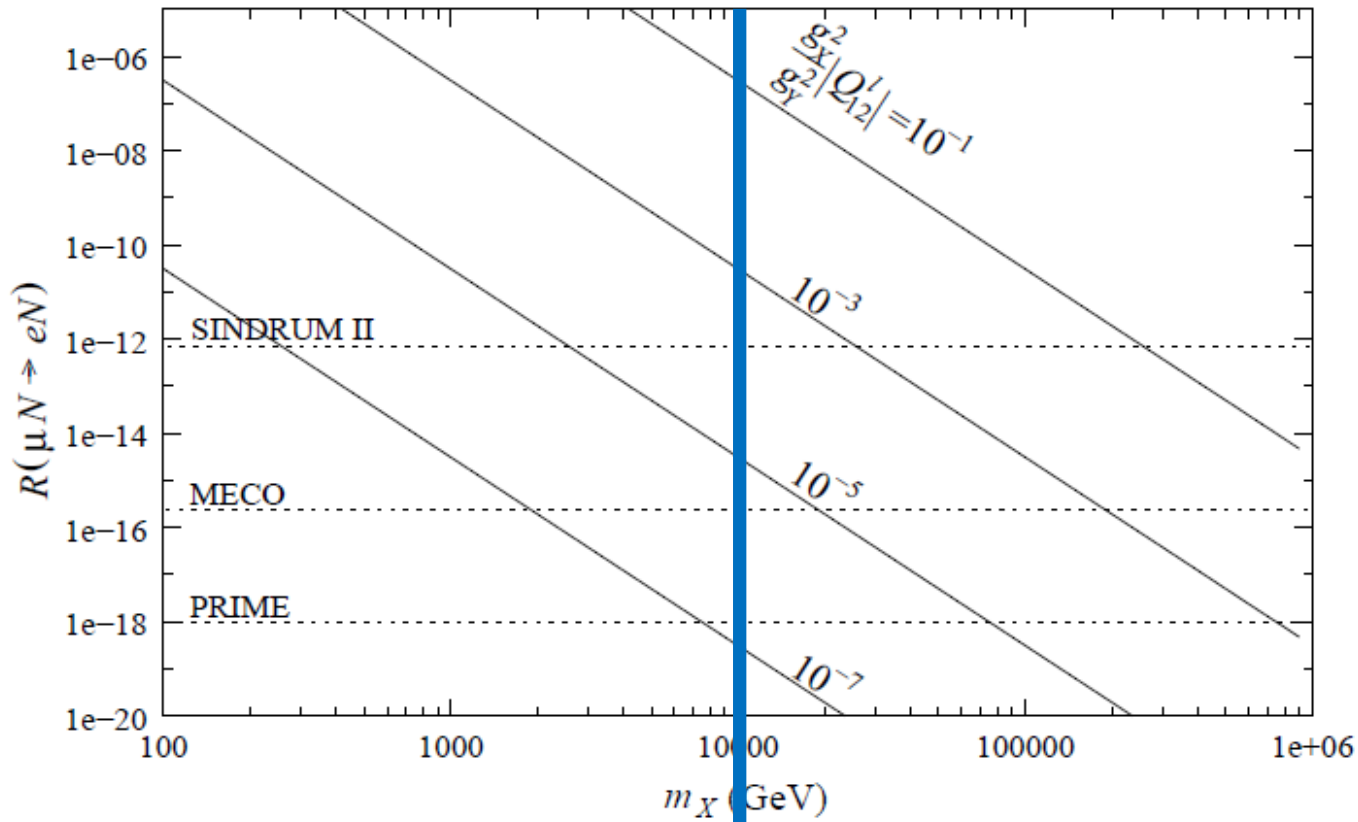


Brandon
Murakami

10TeV

Figure 4: Constraint of Z' by the current search for $\mu^+ \rightarrow e^+\gamma$.

$$B(\mu \rightarrow e\gamma) = 1.3 \times 10^{-13} \left(\frac{g_x}{g_Y} \right)^4 \left(\frac{Q_{13}Q_{23}}{10^{-5}} \right)^2 \left(\frac{1\text{TeV}}{m_{Z'}} \right)^4$$



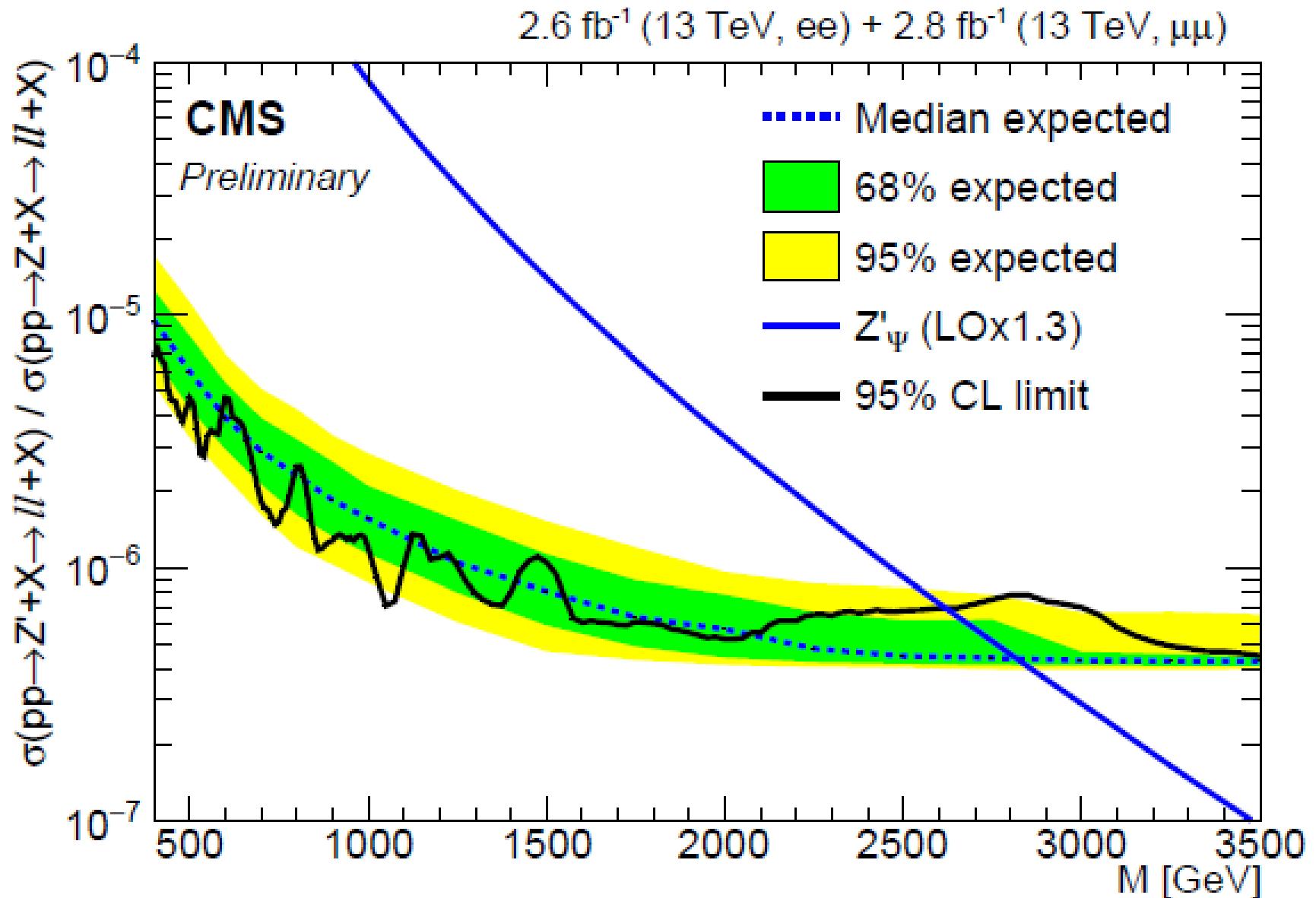
Brandon
Murakami

10TeV

Figure 5: Constraint of Z' by the current search for $\mu^- - e^-$ conversion.

$$B(\mu N \rightarrow e N) = 3.1 \times 10^{-11} \left(\frac{g_{Z'}}{g_Y} \right)^4 \left(\frac{Q_{12}}{10^{-5}} \right)^2 \left(\frac{1 \text{ TeV}}{m_{Z'}} \right)^4$$

Direct Search at LHC ,excluded < 3TeV



Scalar type

SUSY :: Still main target!?

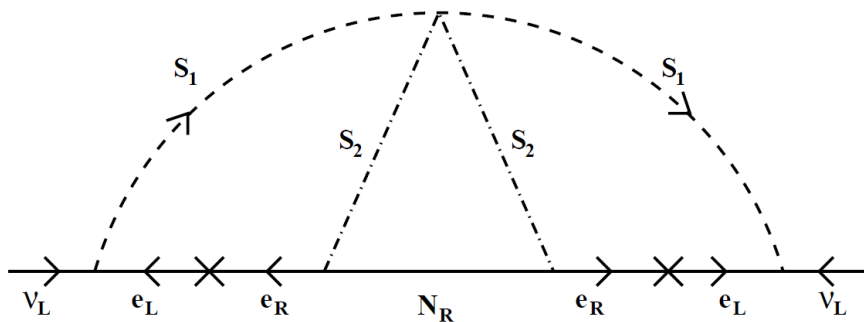
2< doublet higgs :: SUSY is restricted version

{ Higgs triplet :: doubly charged

{ Radiative generation of neutrino masses

Krauss et al

sometimes doubly charged



$$\mu^+ \rightarrow e^+ e^- e^+$$

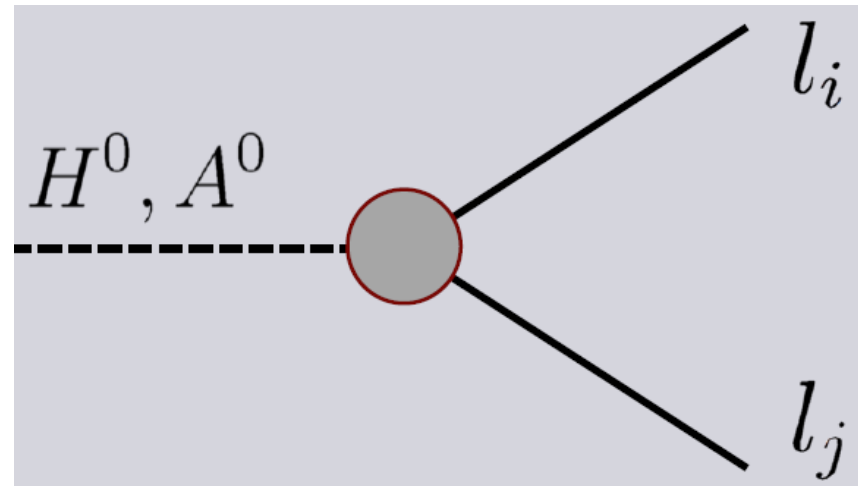
Is more relevant

SUSY

Neutral scalar : Heavy neutral higgs , sneutrino

With R-Parity

Scalar (Higgs) can contribute at tree level



Naïve $2 <$ doublets, this coupling can be large, though...

In SUSY , slepton mixing must be contributed , that is, the couplings has same or less magnitude as dipole

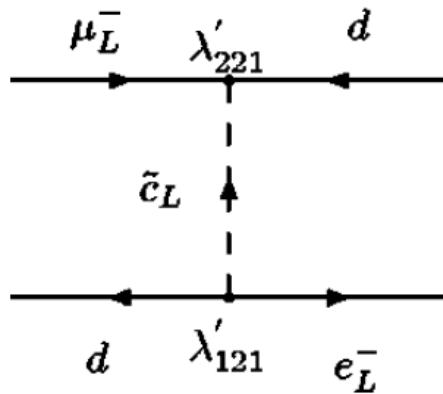
Furthermore, these higgses are probably very heavy

If R parity is broken,

$$W_{RPV} = \frac{\lambda_{ijk}}{2} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k + \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k + \mu'_i L_i H_u$$

Tree contribution may dominate for $\mu - e$ conversion

Leptoquark



While $\mu \rightarrow e + \gamma$
Induced by loop

→ distinction of models

André de Gouvea, Smaragda Lola, and Kazuhiro Tobe

	$\frac{\text{Br}(\mu \rightarrow e \gamma)}{\text{Br}(\mu \rightarrow 3e)}$	$\frac{\text{R}(\mu \rightarrow e \text{ in Ti})}{\text{Br}(\mu \rightarrow 3e)}$	A_P	A_{P_1}	A_{P_2}	A_{P_1}/A_{P_2}
$\lambda'_{121} \lambda'_{221}$	1.1	2×10^5	-100%	-26%	-5%	5.6
MSSM with ν_R	1.6×10^2	0.92	-100%	10%	17%	0.6

Orthodox scenario

Source of LFV
=
Slepton mixing

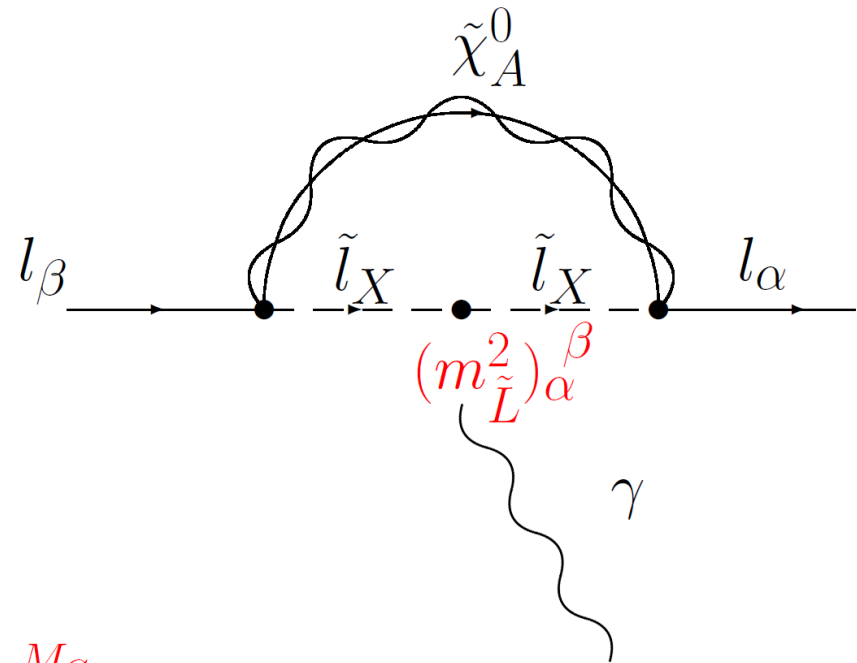
$$m_{\tilde{l}}^2 = \begin{pmatrix} m_{\tilde{e}\tilde{e}}^2 & \Delta m_{\tilde{e}\tilde{\mu}}^2 & \Delta m_{\tilde{e}\tilde{\tau}}^2 \\ \Delta m_{\tilde{\mu}\tilde{e}}^2 & m_{\tilde{\mu}\tilde{\mu}}^2 & \Delta m_{\tilde{\mu}\tilde{\tau}}^2 \\ \Delta m_{\tilde{\tau}\tilde{e}}^2 & \Delta m_{\tilde{\tau}\tilde{\mu}}^2 & m_{\tilde{\tau}\tilde{\tau}}^2 \end{pmatrix}$$

CMSSM + RH neutrino

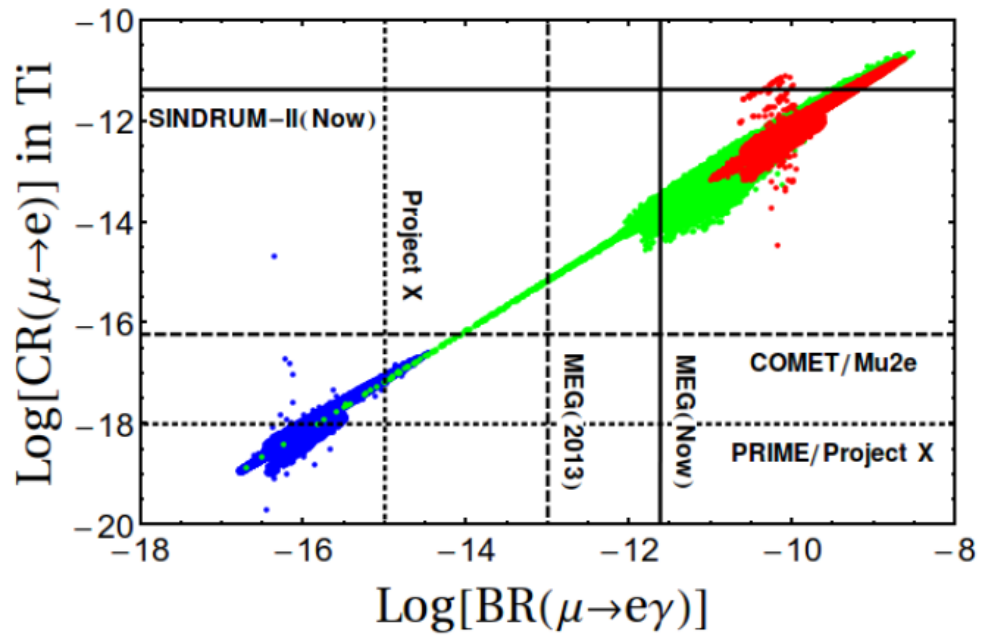
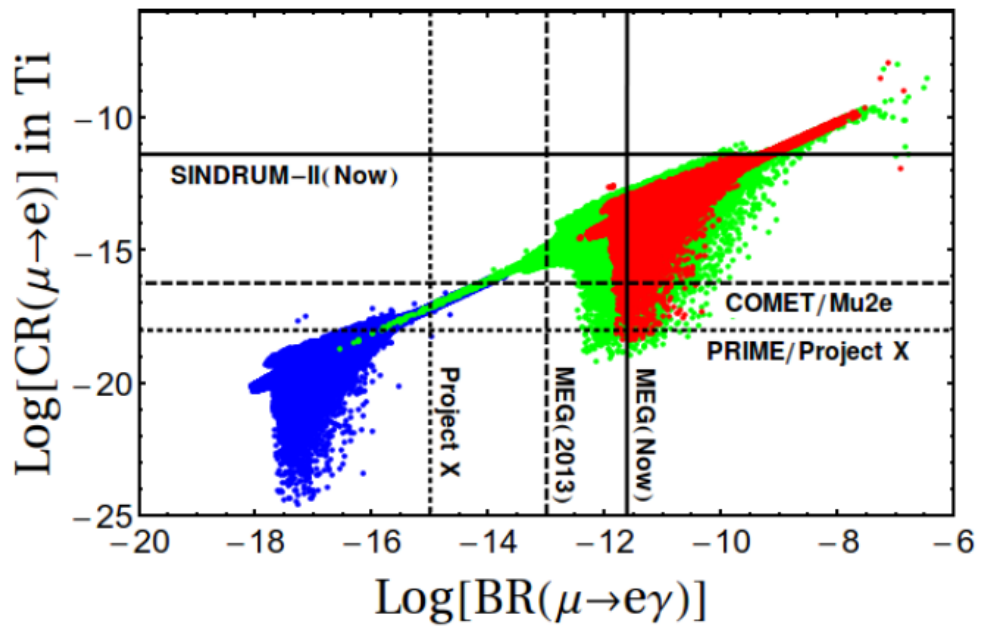
Most exhaustively studied

$$W = f_\nu^{i\beta} \bar{N}_i L_\beta H_u$$

$$\begin{aligned} (m_{\tilde{L}}^2)_\alpha^\beta &\simeq -\frac{(6 + a_0^2)m_0^2}{16\pi^2} (f_\nu^\dagger f_\nu)_\alpha^\beta \log \frac{M_G}{M_R} \\ &\simeq -\frac{(6 + a_0^2)m_0^2}{16\pi^2} U_{\alpha k}^{Dirac} (U^{Dirac*})^{\beta k} |f_{\nu k}|^2 \log \frac{M_G}{M_R} \end{aligned}$$



Dipole dominant



5. Summary

Lepton Flavor

Exact Symmetry in the Standard Model

If SM is correct then LF conserves

<-->

LFV then SM is not correct

Neutrino Oscillation

Manifestation of Lepton Flavor Violation

-->

SM must be extended so that neutrinos are massive

Neutrino masses

Dirac or Majorana? Tree or Induced?

If Majorana --> Lepton Number is also violated

neutrinoless double beta decay, $\mu^- \rightarrow e^+$ in muonic atom

Charged Lepton Flavor Violation

SU(2) connection indicates LFV in Charged lepton

Clean signal for Physics beyond the Standard Model

Not observed yet though many searches have been done

Muon decay , Tau decay, LFV in final state(decay product)

Classification of new physics

Tree vs Loop : $\mu^+ \rightarrow e^+ \gamma$: always loop effect

Scalar vs Vector

Model dependence

Most precise measurements with muon

$$\mu^+ \rightarrow e^+ \gamma \quad \text{and} \quad \mu^- \rightarrow e^-$$

Which one will be observed first?

Example of model dependent analysis with other signals

Connection among CLFVs an Example

J.S & M.Yamanaka

Phys. Rev. D91 055018-1-17, 2015

MEGII experiment updates/discovers(?)



COMET/DeeMe/Mu2E will discover(?)



In near future

Sensitivity is same.

If COMET find CLFV first then ...?

μ -e conversion and then ?

If μ -e conversion is found, while other cLFV processes will never be found

E.g.

R-parity violating SUSY gives such a situation

Tree contribution for CLFV
Scalar/Vector with LFV
Direct coupling with qq and μ -e

- ✓ No correlations among cLFVs
- ✓ How to confirm the scenario?

Aim of this work

To find out distinctive signals to discriminate the scenario and other new physics models

To show the feasibility to determine the parameters in the RPV scenario through observing the signals

How to confirm a model?

R-parity violating SUSY

☑ Candidate of new physics: R-parity violating SUSY

☑ Consistent with experimental/theoretical status

▣ New physics is required to cancel Higgs quadratic divergence

▣ TeV scale SUSY predicts grand unification of interactions

▣ So far no typical SUSY signals have been observed

Omit the term to avoid proton decay

☑ RPV terms in superpotential in SUSY

$$\mathcal{W}_{\mathcal{R}} = \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c + \lambda''_{ijk} U_i^c D_j^c D_k^c$$

Offers LFV Scalar

Framework of our scenario

Naturally realized by RG evolution
with universal masses@GUT scale

- ☑ Slepton contribution to RPV: only 3rd generation
- ☑ Different generation of left- and right-handed leptons
 λ_{ijk} ($i \neq k$ and $j \neq k$)

Assumption to realize
the interesting situation

- ☑ RPV terms in superpotential in SUSY

$$\mathcal{W}_{\mathcal{R}} = \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c + \lambda''_{ijk} U_i^c D_j^c D_k^c$$

Framework of our scenario

Naturally realized unless we introduce additional sources of flavor violation

- ☑ For quarks, flavor diagonal components are much larger than off-diagonal components

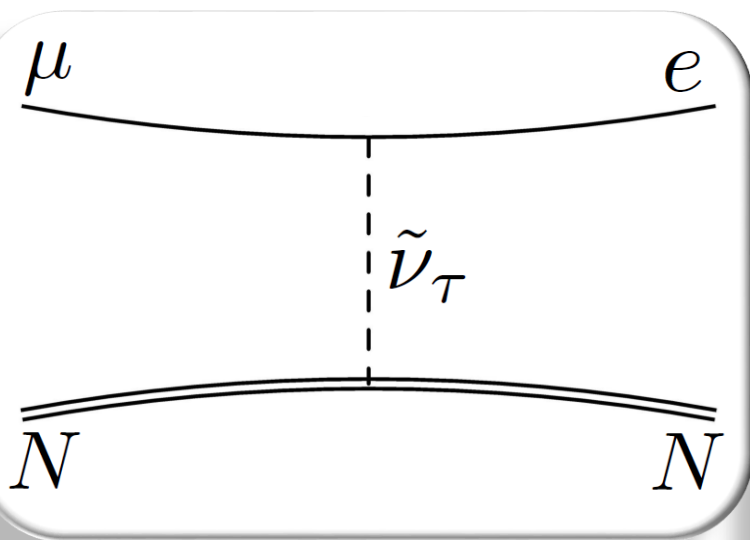
$$\lambda'_{ijj} \gg \lambda'_{ijk} \quad (j \neq k)$$

- ☑ RPV terms in superpotential in SUSY

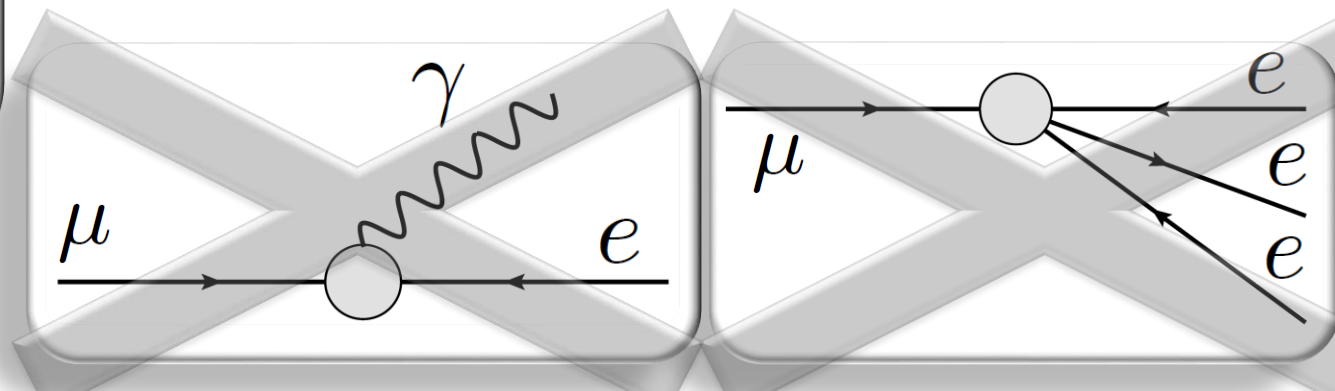
$$\mathcal{W}_{\mathcal{R}} = \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c - \lambda''_{ijk} U_i^c D_j^c D_k^c$$

Exotic processes in the scenario

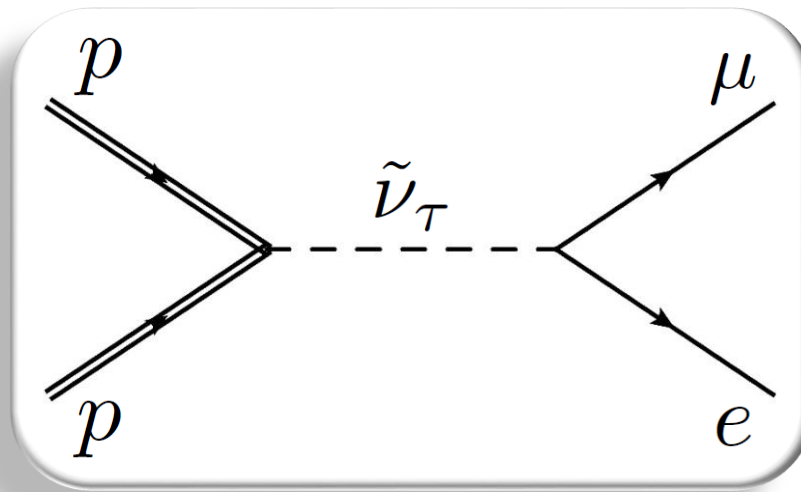
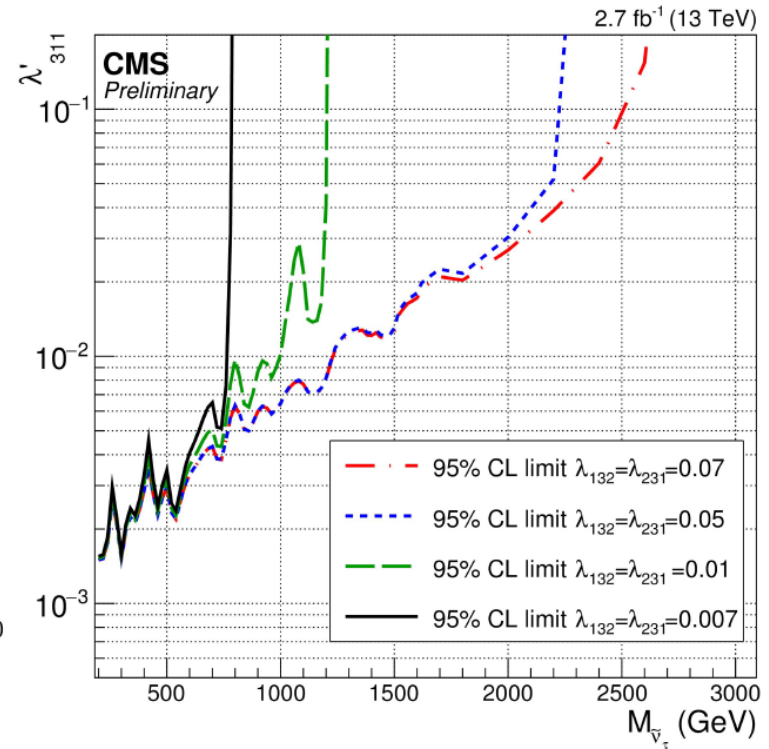
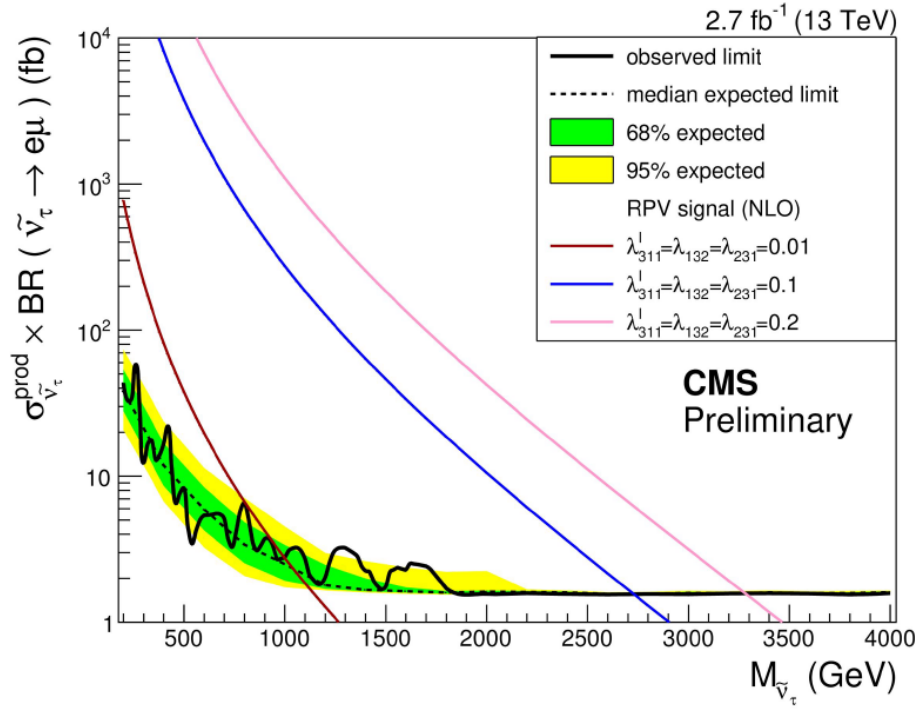
$$\mathcal{L}_{\text{RPV}} = 2 \left\{ \lambda_{312} \tilde{\nu}_\tau \bar{\mu}_R e_L + \lambda_{321} \tilde{\nu}_\tau \bar{e}_R \mu_L + \lambda_{132} \tilde{\tau}_L \bar{\mu}_R \nu_e + \lambda_{231} \tilde{\tau}_L \bar{e}_R \nu_\mu \right\} \\ + \left\{ \lambda'_{311} (\tilde{\nu}_\tau \bar{d}_R d_L - \tilde{\tau}_L \bar{d}_R u_L) + \lambda'_{322} (\tilde{\nu}_\tau \bar{s}_R s_L - \tilde{\tau}_L \bar{s}_R c_L) \right. \\ \left. + \lambda'_{333} (\tilde{\nu}_\tau \bar{b}_R b_L - \tilde{\tau}_L \bar{b}_R t_L) \right\} + \text{h.c.}$$



- ☑ μ -e conversion@tree level
- ☑ Negligible rates of other cLFV processes



Current bound for the scalar with LFV

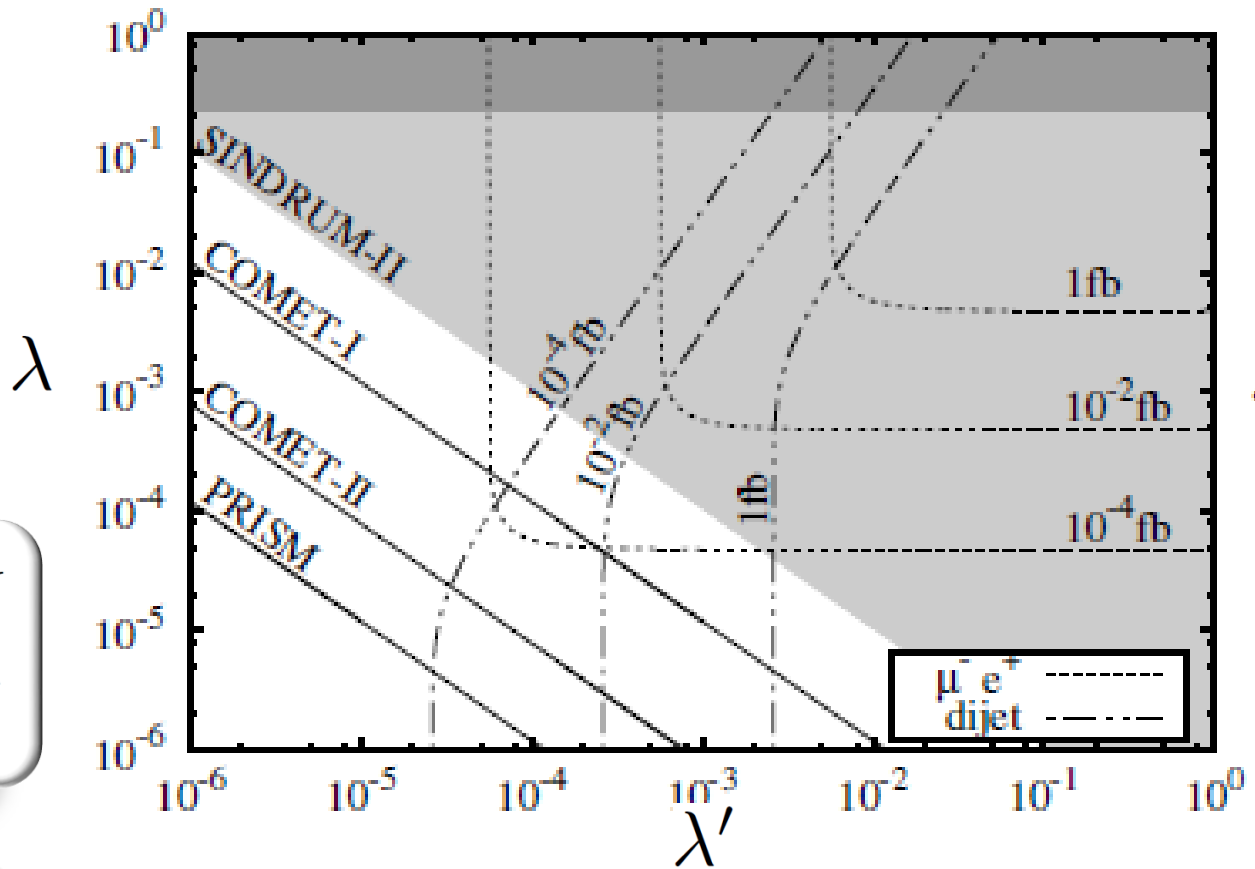


Correlations of distinctive signals

Contour plot of

- $\text{BR}(\mu^- + N \rightarrow e^- + N)$
- $\sigma(pp \rightarrow \mu\bar{e})$
- $\sigma(pp \rightarrow jj)$

- sneutrino mass $m_{\tilde{\nu}_\tau} = 1\text{TeV}$
- collision energy $\sqrt{s} = 14\text{TeV}$



- ☑ μ - e conversion search is a strong tool for exploring RPV
- ☑ PRISM explores all parameter space wherein LHC can survey

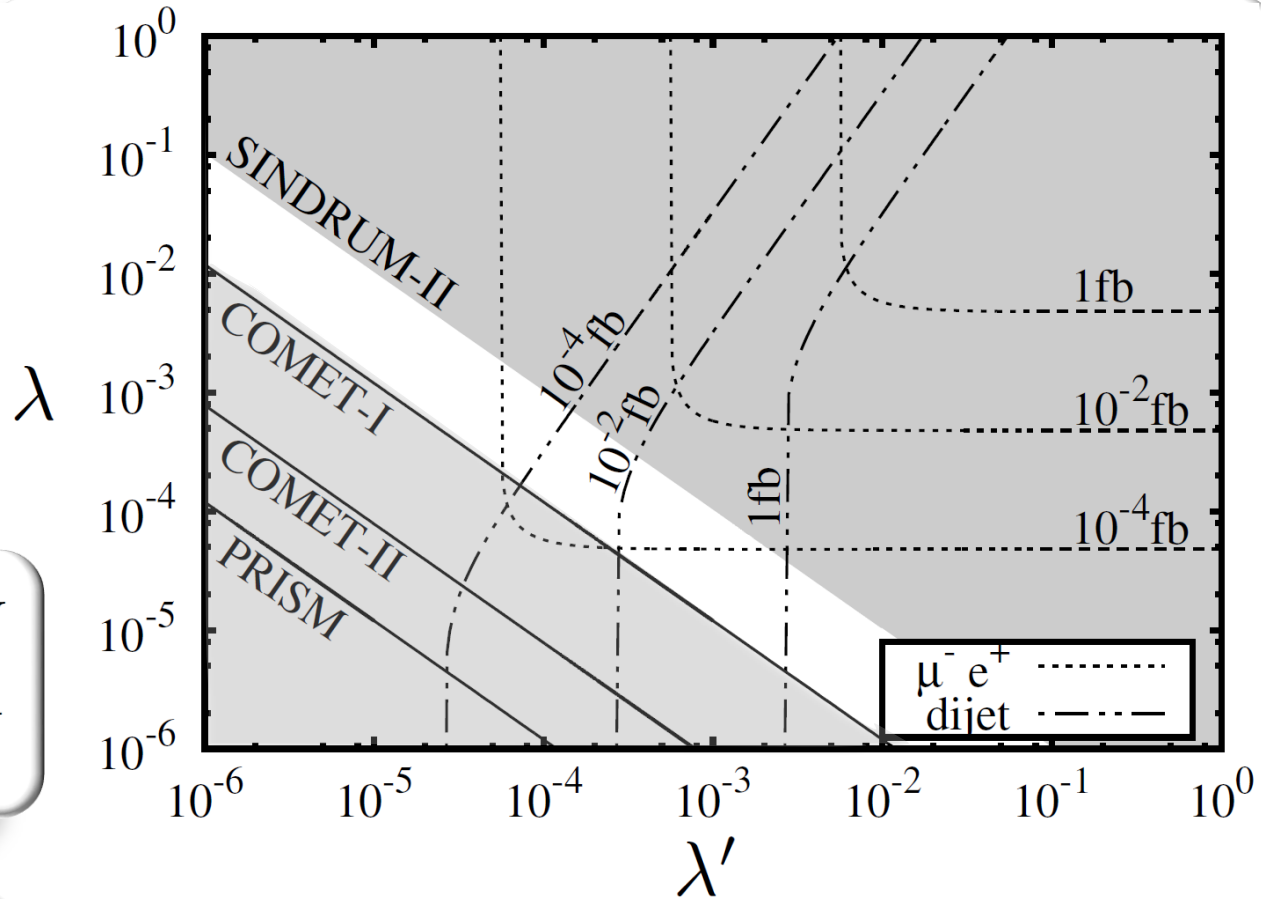
Correlations of distinctive signals

Contour plot of

- $\text{BR}(\mu^- + N \rightarrow e^- + N)$
- $\sigma(pp \rightarrow \mu e)$
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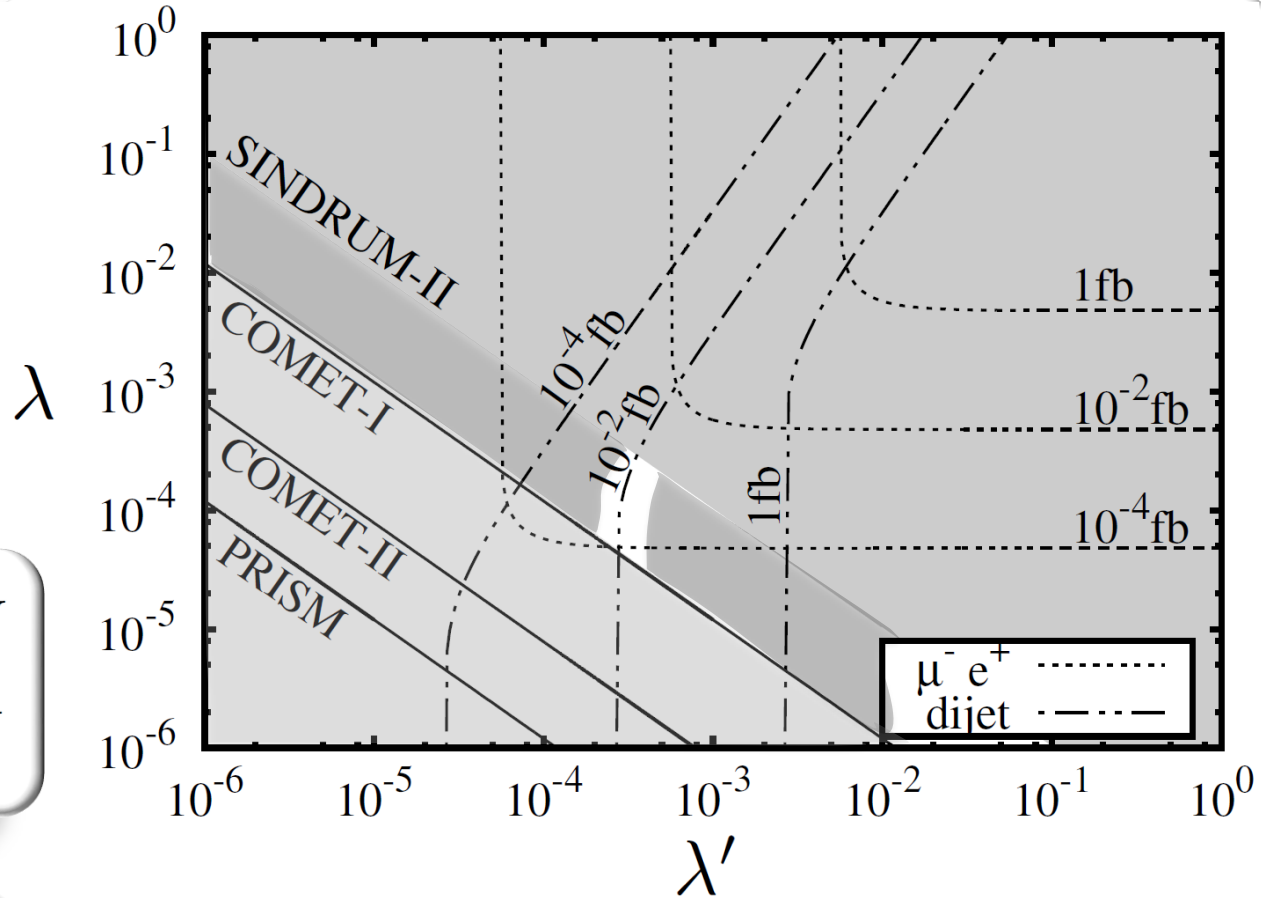
☑ COMET/DeeMe found $m \rightarrow e$ conversion \longrightarrow white band

Correlations of distinctive signals

Contour plot of

- $\text{BR}(\mu^- + N \rightarrow e^- + N)$
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- sneutrino mass $m_{\tilde{\nu}_\tau} = 1\text{TeV}$
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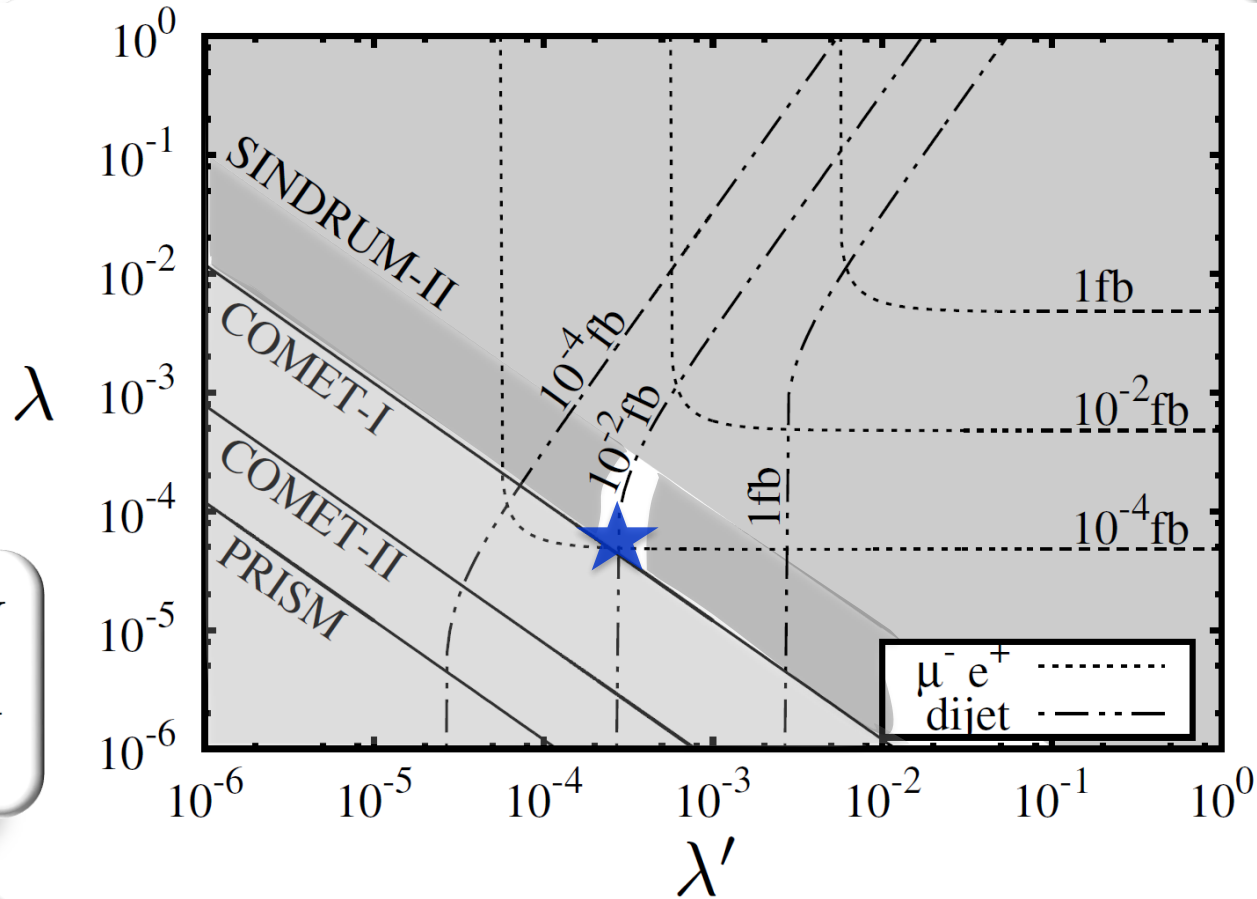
- ☑ COMET/DeeMe found $m-e$ conversion \longrightarrow white band
- ☑ Dijet resonance is found with 10 fb^{-2} \longrightarrow white small region

Correlations of distinctive signals

Contour plot of

- $\text{BR}(\mu^- + N \rightarrow e^- + N)$
- $\sigma(pp \rightarrow \mu\bar{e})$
- $\sigma(pp \rightarrow jj)$

- sneutrino mass $m_{\tilde{\nu}_\tau} = 1\text{TeV}$
- collision energy $\sqrt{s} = 14\text{TeV}$



- ☑ $\mu\bar{e}$ resonance is found with 10 fb^{-4} → blue star point
- ☑ J-PARC and LHC precisely determine the RPV parameters!

More on coupling discrimination

- Non Standard Interaction

Pion decay in scalar channel – chiral enhancement

Exotic decay



$$\epsilon_{\mu e}^S = \sqrt{2} \frac{m_\pi^2}{m_\mu m} \frac{\lambda_{312}^* \lambda'_{311}}{G_F m_\tau^2}$$

312 : LH electron only

- ILC with polarization

LHC signal is same for 312(LH e) and 321 (RH e)

Can you distinguish them ?