

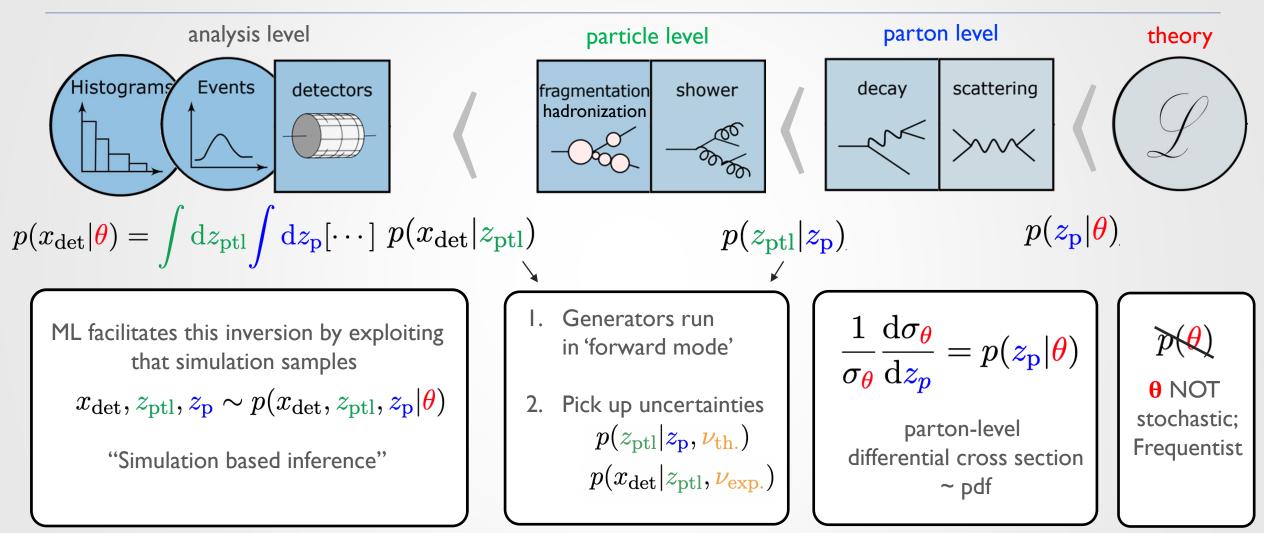
TREE BOOSTING (+NEURAL NETWORKS) FOR EFT ANALYSES

R. Schöfbeck (HEPHY Vienna), Oct. 24th, 2023, Area 3 meeting



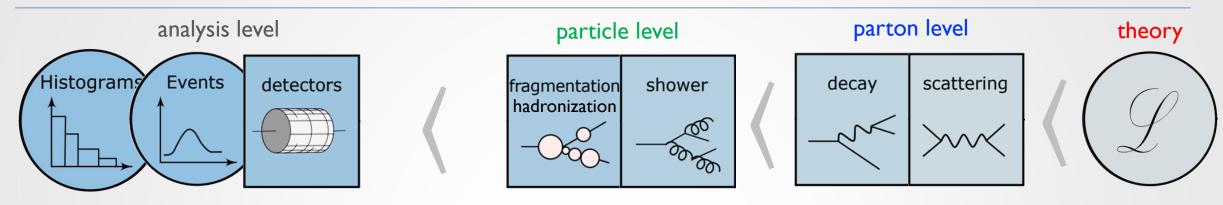
A CONDITIONAL SEQUENCE

adapted from <a>arXiv:2211.01421



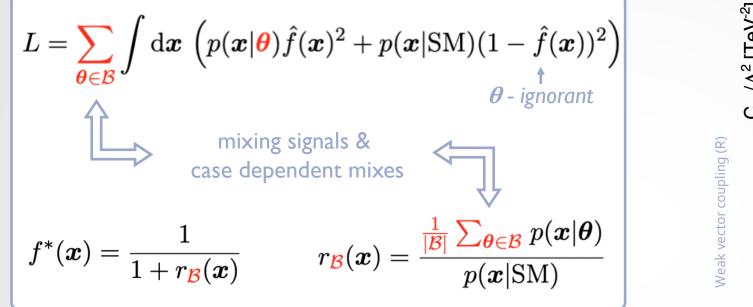
THE LIKELIHOOD RATIO TRICK

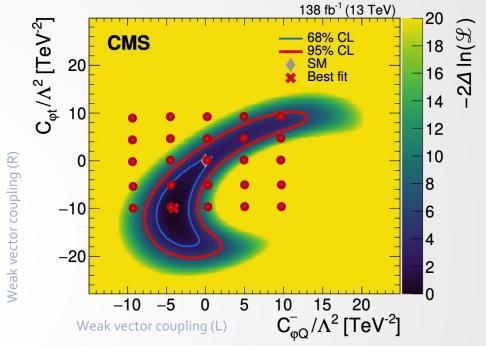
adapted from <a>arXiv:2211.01421



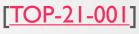
Event classification $\theta \to isSig \in \{0, I\}$ $L = \langle f(x)^2 \rangle_{isSig=1} + \langle (1 - f(x))^2 \rangle_{isSig=0} = \sum_{isSig} \int dx \cdots$ $f^*(x) = \frac{1}{1 + \frac{p(x|isSig=1)}{p(x|isSig=0)}}$ Learn LR by classification; "Likelihood ratio trick" achieve NP optimality (for x-sec)

CAN WE JUST LEARN EFT EFFECTS "ON AVERAGE"?





• We can try to learn EFT effects "on average"



- Sending 'mixed signals' to the loss function
 - Averages the training data set suboptimal when linear effects dominate
 - Classifier does not reflect knowledge on the $\boldsymbol{\theta}$ -dependence
- **1**. Back to the drawing board & inject θ polynomial SMEFT dependence in estimator.
- 2. Exploit the fact that SMEFT predictions can (optionally) be weighted: Only need one training data set

$$L = \sum_{\theta \in \mathcal{B}} \left(\langle \hat{f}(x; \theta)^2 \rangle_{\theta} + \langle (1 - \hat{f}(x; \theta))^2 \rangle_{\text{SM}} \right)$$

$$\stackrel{\bullet}{\xrightarrow{\theta - \text{ aware}}} EFT \text{ sample} \qquad \text{SM sample}$$

We start with SM and **BSM** samples

$$= \sum_{\theta \in \mathcal{B}} \int dx \, dz \, \left(p(x, z | \theta) \hat{f}(x; \theta)^2 + p(x, z | SM) (1 - \hat{f}(x; \theta))^2 \right)$$
 Let's write this under one integral z ... latent space

$$= \sum_{\theta \in \mathcal{B}} \int dx \, dz \, p(x, z | SM) \begin{pmatrix} r(x, z | \theta) \hat{f}(x; \theta)^2 + (1 - \hat{f}(x; \theta))^2 \end{pmatrix} \qquad \dots \text{ and use just one sample} \\ & \& \text{ joint likelihood ratio} \end{pmatrix}$$

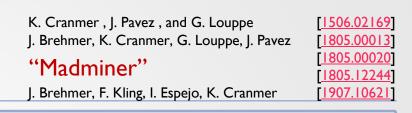
$$r = \frac{p(x_{\text{det}}, \cdots, z_{\text{ptl}}, \cdots, z_{\text{p}}|\boldsymbol{\theta})}{p(x_{\text{det}}, \cdots, z_{\text{ptl}}, \cdots, z_{\text{p}}|\mathbf{SM})} = \frac{p(x_{\text{det}}|z_{\text{ptl}}) \cdots p(z_{\text{ptl}}|z_{\text{p}}) \cdots p(z_{\text{p}}|\boldsymbol{\theta})}{p(x_{\text{det}}|z_{\text{ptl}}) \cdots p(z_{\text{ptl}}|z_{\text{p}}) \cdots p(z_{\text{p}}|\mathbf{SM})} = \frac{p(z_{\text{p}}|\boldsymbol{\theta})}{p(z_{\text{p}}|\mathbf{SM})} \sim \frac{|\mathcal{M}(z_{\text{p}}, \boldsymbol{\theta})|^{2}}{|\mathcal{M}(z_{\text{p}}, \mathbf{SM})|^{2}} = w_{i}(\boldsymbol{\theta})$$

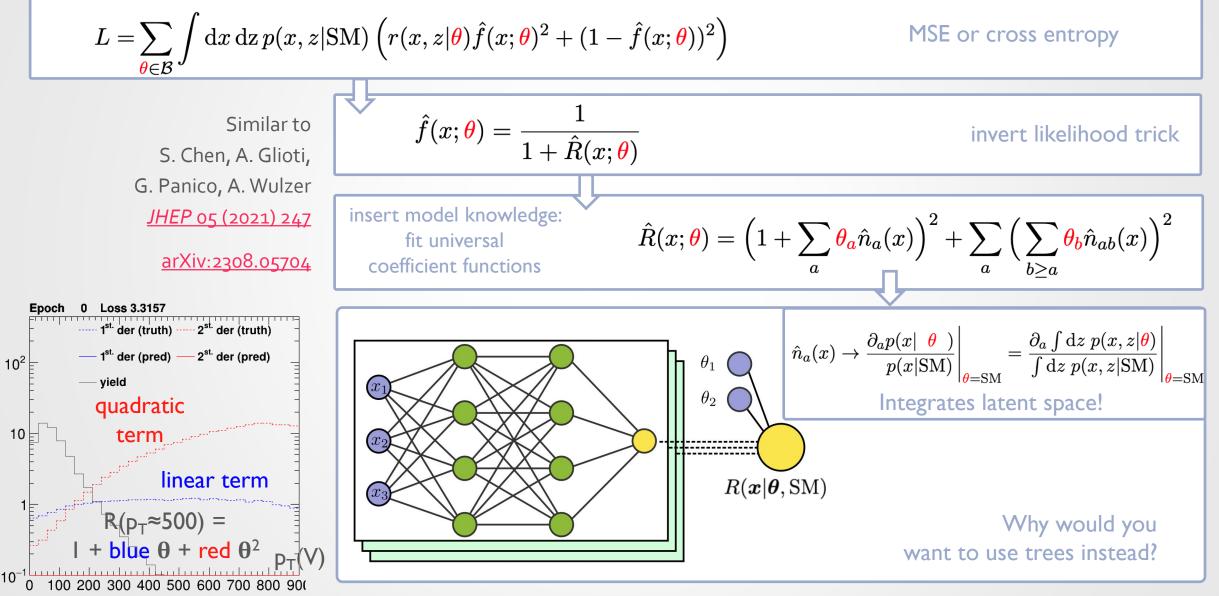
Change in likelihood of simulated observation x with latent "history" z going from "SM" to θ

staged simulation in forward mode: Intractable factors cancel re-calcuable theory prediction

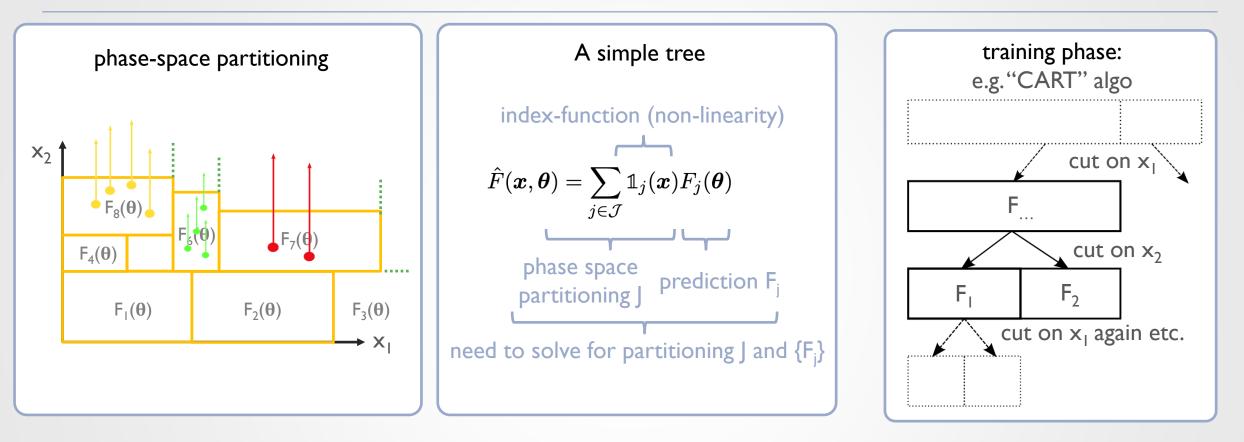
weighted simulation

PARAMETRIZED CLASSIFIERS



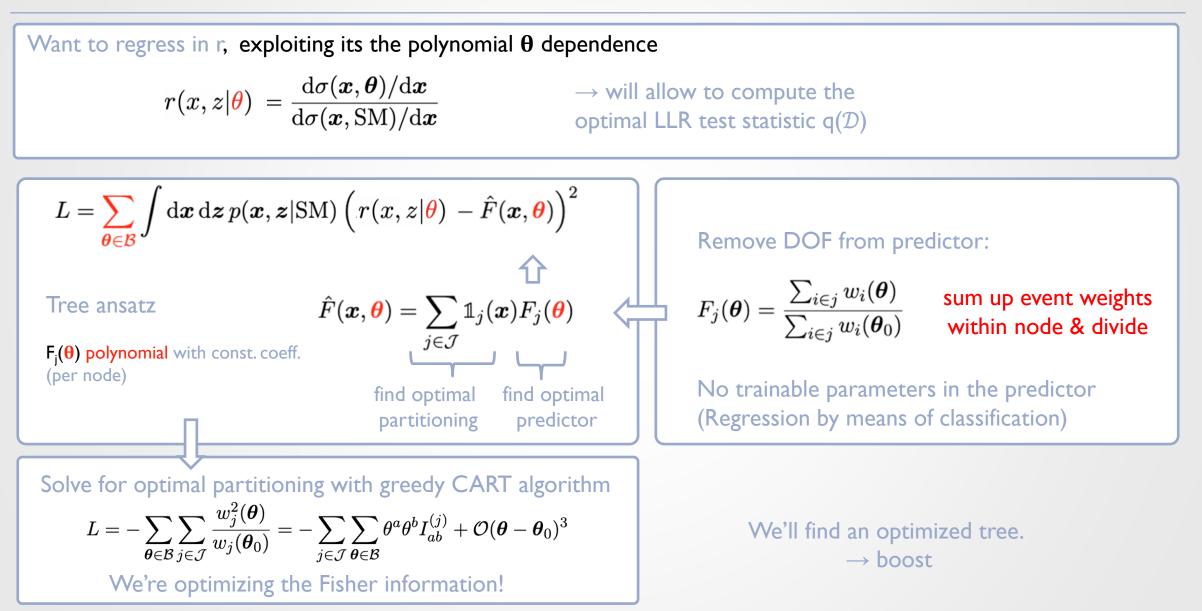


A SIMPLE TREE ALGORITHM



- A tree is a hierarchical phase-space partitioning (*J*)
 - the novelty in the Boosted Information Tree is that we associate each region j with a polynomial $F_i(\theta)$
 - Note: A tree algorithm can have an arbitrarily complicated predictive function; here it is a SMEFT polynomial
- Fitting tree: Optimize "node split positions" on some loss. Trained (e.g. greedily) on the *ensemble*.

PARAMETRIC TREES FOR SMEFT



CONCRETE SOLUTION: TREE BOOSTING

- Boosting: Fit model iteratively to pseudo-residuals of the preceding iteration with learning rate η

• Ansatz :
$$\hat{F}^{(b)}(\boldsymbol{x}, \boldsymbol{\theta}) = \hat{f}(\boldsymbol{x}, \boldsymbol{\theta}) + \eta \hat{F}^{(b-1)}(\boldsymbol{x}, \boldsymbol{\theta})$$

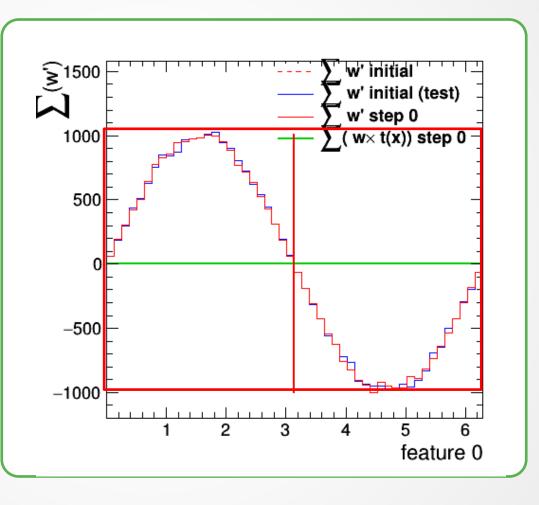
current previous iteration

• Insert into the loss function:

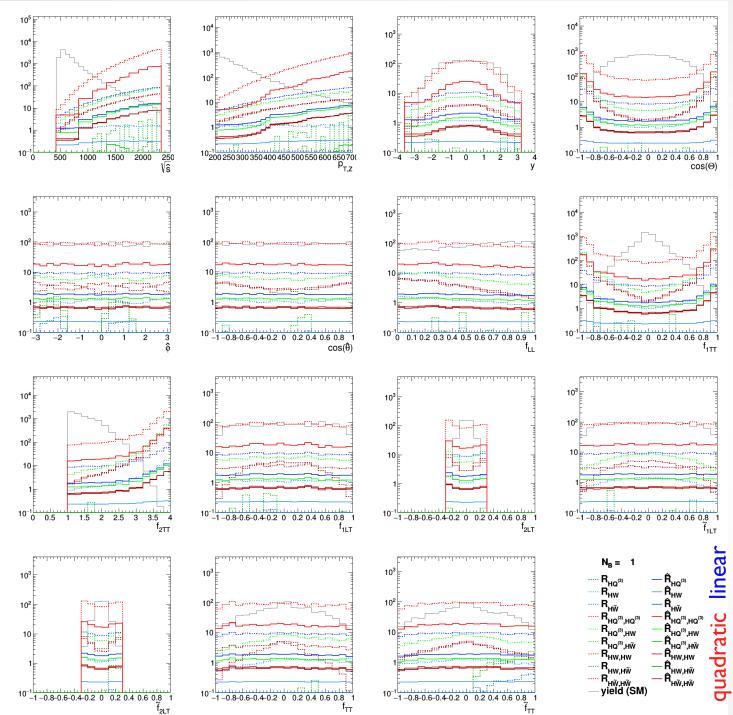
.... perform this iteratively "Boosted Information Tree"

1D TOY EXAMPLE

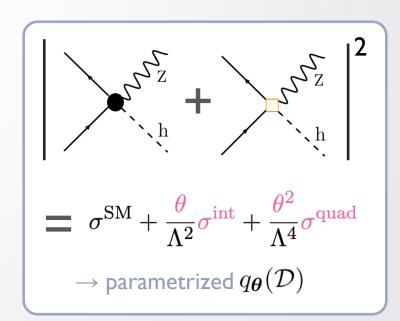
- $pdf(x|\theta) = 1/(2\pi) \theta Sin(x)$
- We predict the first derivative of the pdf wrt. to the parameter



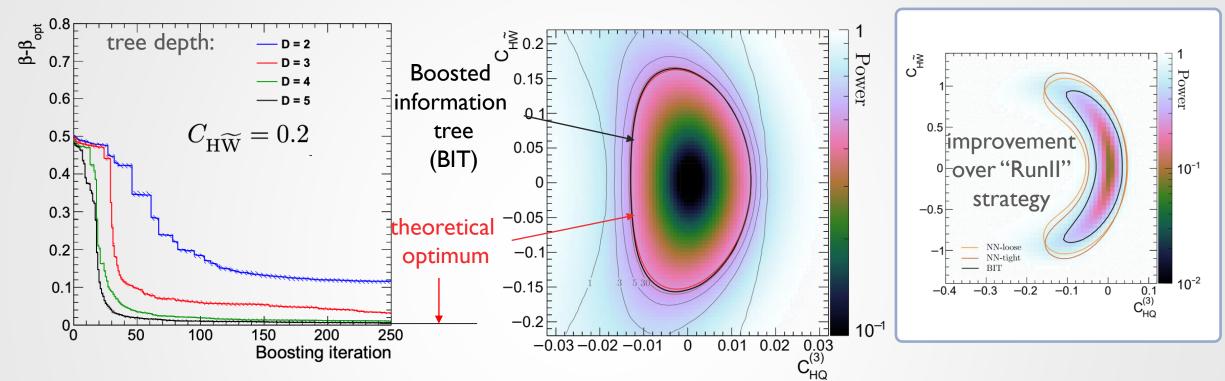
GIF animation not showing in pdf



- Realistic case: model of the ZH process
- "Boosted Information Tree (BIT)"
 - 3 WC, 9 DOF, 500k events, ZH
 - 200 trees, D=5, 9 minutes of training
 - also more realistic study, including backgrounds [2107.10859], [2205.12976]
- Learning coefficient functions to compute parametrized optimal oberables

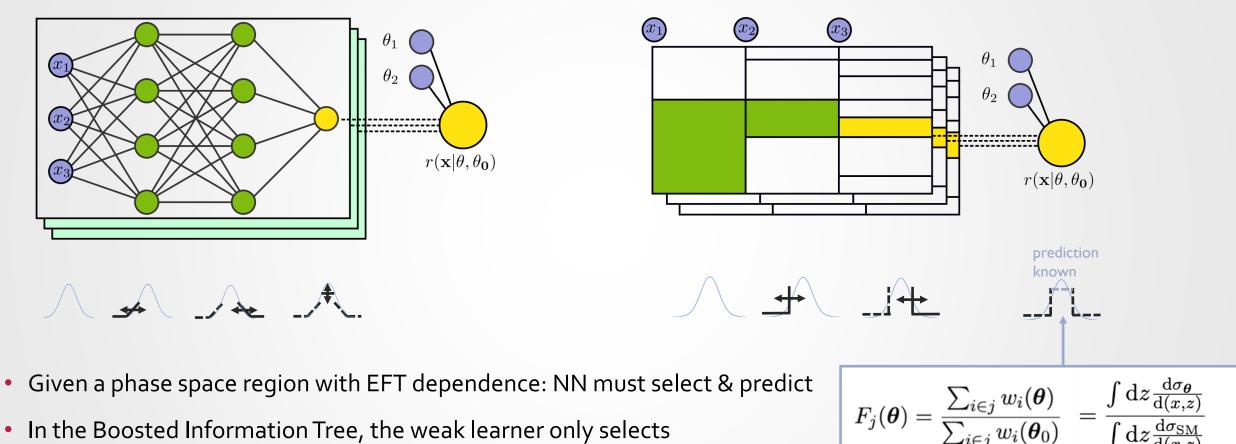


OPTIMALITY IN TEST CASES



- Obtain parametrized classifiers with 20-40% improvements in 2D toy cases (NOT marginalized!)
- No free lunch Analysis dependent choices are needed
 - Binned analysis: variable binning → background estimation is CPU intensive
 - Systematics treatment for unbinned analyses (beyond Higgs $M_{4\ell}$) less far developed
- Is it all worth it in higher dimensions? Yes! More examples: [ML4EFT]; full list of references in backup

NETWORKS VS. TREES – WHAT IS THE BIG DEAL?



- In the Boosted Information Tree, the weak learner only selects
 - The prediction (F_i) is computed from the boxed events \rightarrow integrates latent space
 - The regression problem is solved with computational complexity of classification
 - Speed advantage at high operator dimensions!

SUMMARY!

- Various algorithms predict SMEFT dependence, mostly capitalizing on weighted simulation
 - Provide NP-optimal observables for hypothesis tests
- Trees eliminate the latent space integration and suitable to weight-based SMEFT predictions
- Parametrized classifiers "ask" for unbinned analysis

SWAN project

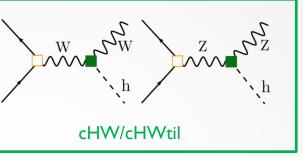
```
from MultiBoostedInformationTree import MultiBoostedInformationTree
                       bit = MultiBoostedInformationTree(
                               training_features
                                                     = training_features,
                                                     = training_weights,
                               training_weights
                                                     = base_points,
                               base_points
                                                     = model.feature_names,
                               feature_names
                               **model.multi_bit_cfg
 Get in touch with
us for an in-person
                       bit.boost()
                       test_predictions = bit.vectorized_predict(test_features)
      walkthrough
```

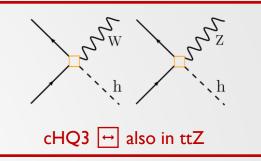
GOALS FOR MACHINE-LEARNING OF EFT



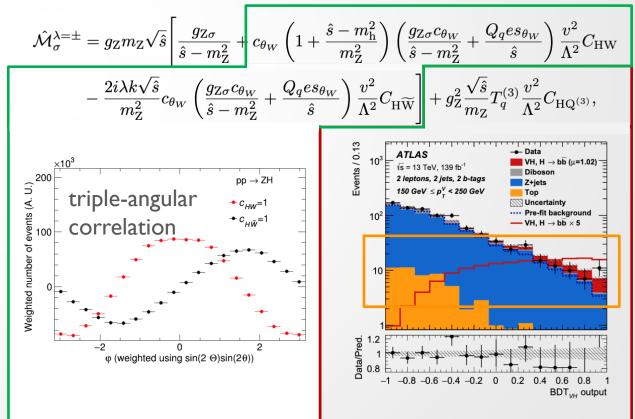
• SMEFT effects can be

- in the tails of the distributions because, e.g.
 4-point functions grow with energy
- in angular observables & correlations,
 sometimes encoding CP-violating effects
 - "interference resurrection" <u>PLB 2017 11 086</u>
 "method of moments" <u>JHEP 06 (2021) 031</u>
 - Enhance / single out the linear term
 - Up to triple-angular correlations, x5-10 boost in sensitivity
- 3. on top of "kinematically complex" backgrounds
 - Def: Usually amenable to classification MVAs
 - Unify the training target with classification





Tree-level SMEFT amplitude of ZH (transverse polarisation):



HOW TO PARAMETRIZE?

• Quantum field theory: Differential cross section predict polynomial SM-EFT dependence:

 $\mathrm{d}\sigma(oldsymbol{ heta}) \propto |\mathcal{M}_{\mathrm{SM}}(oldsymbol{z}) + oldsymbol{ heta}_a \mathcal{M}^a_{\mathrm{BSM}}(oldsymbol{z})|^2 \mathrm{d}oldsymbol{z}$

probability = wave function, squared

• additivity of the matrix element \rightarrow incur a simple (polynomial) dependence in θ for fixed configuration z

$$\frac{\mathrm{d}\sigma(\boldsymbol{x},\boldsymbol{\theta})}{\mathrm{d}\boldsymbol{x}} = \frac{\mathrm{d}\sigma_{\mathrm{SM}}(\boldsymbol{x})}{\mathrm{d}\boldsymbol{x}} + \sum_{a} \theta_{a} \frac{\mathrm{d}\sigma_{\mathrm{int.}}^{a}(\boldsymbol{x})}{\mathrm{d}\boldsymbol{x}} + \frac{1}{2} \sum_{a,b} \theta_{a} \theta_{b} \frac{\mathrm{d}\sigma_{\mathrm{BSM}}^{ab}(\boldsymbol{x})}{\mathrm{d}\boldsymbol{x}}$$

• Neyman-Pearson:
$$q(\mathcal{D}) = \frac{L(\mathcal{D}|\boldsymbol{\theta})}{L(\mathcal{D}|\mathrm{SM})}$$
 where $L(\mathcal{D}|\boldsymbol{\theta}) = P_{\mathcal{L}\sigma(\boldsymbol{\theta})}(N) \times \prod_{i=1}^{N} p(\boldsymbol{x}_i|\boldsymbol{\theta})$
 $q_{\boldsymbol{\theta}}(\mathcal{D}) = \mathcal{L}(\sigma_{\boldsymbol{\theta}} - \sigma_{\mathrm{SM}}) - \sum_{\boldsymbol{x}_i \in \mathcal{D}} \log R(\boldsymbol{x}_i|\boldsymbol{\theta}, \mathrm{SM})$ Optimality can be achieved with cross-section ratio R or its universal coefficient functions R_a, R_{ab}
 $\mathcal{R}(\boldsymbol{x}|\boldsymbol{\theta}, \mathrm{SM}) = \frac{\mathrm{d}\sigma(\boldsymbol{x}, \boldsymbol{\theta})/\mathrm{d}\boldsymbol{x}}{\mathrm{d}\sigma(\boldsymbol{x}, \mathrm{SM})/\mathrm{d}\boldsymbol{x}} = 1 + \sum_{a} \theta_a R_a(\boldsymbol{x}) + \frac{1}{2} \sum_{a,b} \theta_a \theta_b R_{ab}(\boldsymbol{x})$
NB #1 Curse of dimensionality is lifted!! NB #2: R is positive: Fit universal dependence using the most general quadratic polynomial $\hat{\boldsymbol{x}} = (1 + \sum_{a} \theta_a \hat{n}_a(\boldsymbol{x}))^2 + \sum_{a} (\sum_{b} \theta_b \hat{n}_{ab}(\boldsymbol{x}))^2$

TOP QUARK PAIR + Z BOSON

00000

W

 $\sim Z$

2000

 \mathcal{S}^{W}

tt

811 pb

t (t-channel)

217 pb

tW

72 pb

t (s-channel)

10 pb

ttΖ

d d

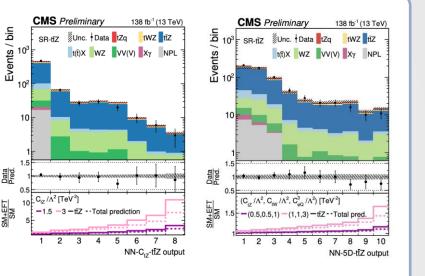
tZq

0.088 pb

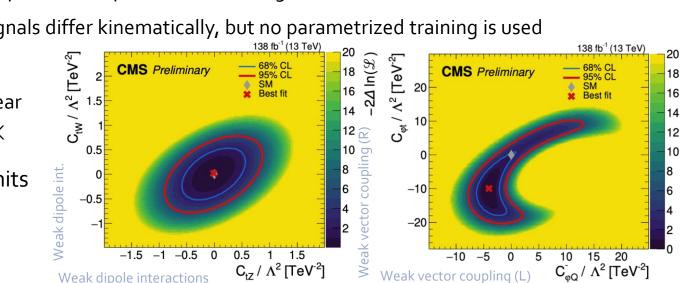
- Measure the top quark Z boson coupling
 - Train separate "SM vs. EFT" classifiers
 - Single operator O_{t7} , O_{tW} , $O_{3}_{\phi O}$
 - different trainings for different limits (!)
 - "likelihood trick" for SMEFT effects
- signal extraction with 1D, 2D, and 5D LL fit
 - Sampling of parameter space in the training
 - Targeted signals differ kinematically, but no parametrized training is used

Signal mix **CMS** Preliminary Best fit no large linear terms $\rightarrow OK$

Best current limits



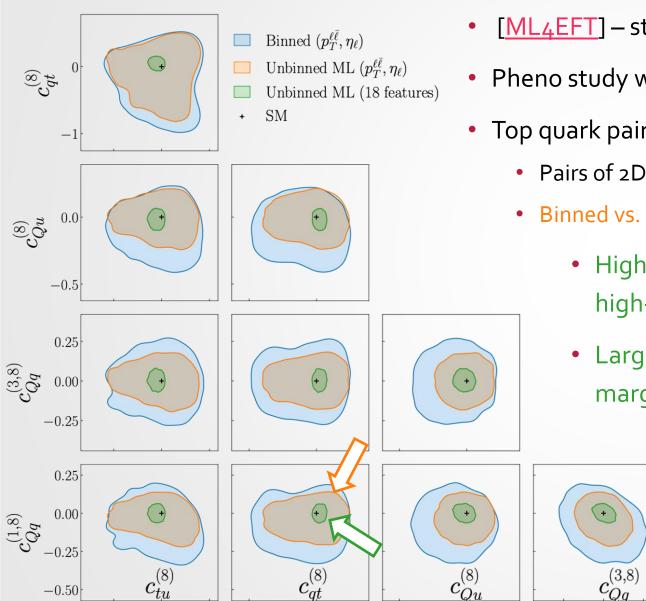




ML4EFT R. Ambrosio, J. Hoeve, M. Madigan, J. Rojo, V. Sanz [2211.02058]

IMPROVING HIGH DIMENSIONAL LIMITS

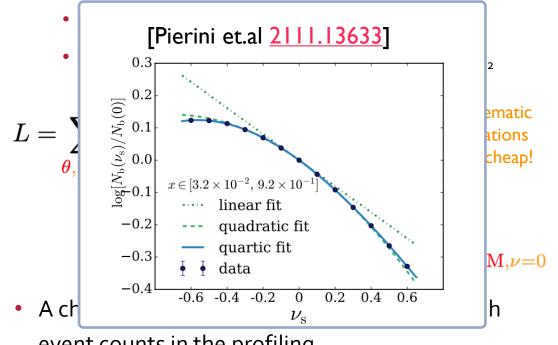




- [ML4EFT] study ZH and top quark pairs
- Pheno study with parametrized NN classifiers
- Top quark pairs in low ($N_f=2$) and high feature dimension $N_f=18$
 - Pairs of 2D limits with 6 more ops marginalized
 - Binned vs. unbinned: Some gain w/ unbinned when using 2 features
 - High dimensional observation (N_f=18) constraining a high-dimensional (N_{coef}=8) model using an SM candle
 - Large improvement for N_f=18– mostly in the marginalized limits
 - Take seriously constraining power from SM candle
 - Whether the sensitivity gain survives systematics in an unbinned detector-level analysis is an open question

TOWARDS UNBINNED ANALYSIS

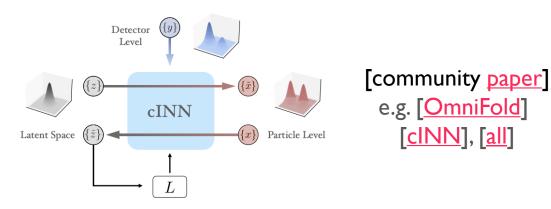
- Binned parametrized classifiers are impractical for high SMEFT parameter dimension
- What's missing to go all-in? Systematics.



event counts in the profiling

• Divide & conquer #1: Experiments begun machinelearning certain nuisances: h_{damp}, b-fragmentation

- Divide & conquer #2: Unbinned unfolding for high dimensions
- Consider on the conditional pdf $p(x_{
 m det}|z_{
 m ptl})$ which can be evaluated in the forward mode
- Unfolding algorithms use Bayes' theorem $p(x_{det}|z_{ptl})p(z_{ptl}) = p(z_{ptl}|x_{det})p(x_{det})$ to learn $p(z_{ptl}|x_{det})$; GAN & other generative versions
 - Mostly iterative, to remove simulated prior



• Report unbinned unfolded data; then SMEFT analysis

REFERENCES

- Madminer: Neural networks based likelihood-free inference & related techniques
 - K. Cranmer , J. Pavez , and G. Louppe [1506.02169]
 J. Brehmer, K. Cranmer, G. Louppe, J. Pavez [1805.00013] [1805.00020] [1805.12244]
 J. Brehmer, F. Kling, I. Espejo, K. Cranmer [1907.10621]
 - J. Brehmer, S. Dawson, S. Homiller, F. Kling, T. Plehn [<u>1908.06980</u>]
 - A. Butter, T. Plehn, N. Soybelman, J. Brehmer
 - established many of the *main ideas* & *statistical interpretation* in various *NN applications*

2109.10414

- Weight derivative regression (A.Valassi)
 [2003.12853]
- Parametrized classifiers for SM-EFT: NN with quadratic structure
- S. Chen, A. Glioti, G. Panico, A. Wulzer [JHEP 05 (2021) 247] [arXiv:2308.05704]
- **Boosted Information Trees**: Tree algorithms & boosting
 - S. Chatterjee, S. Rohshap, N. Frohner, <u>R.S.</u>, D. Schwarz [<u>2107.10859</u>], [<u>2205.12976</u>]
- ML4EFT R. Ambrosio, J. Hoeve, M. Madigan, J. Rojo, V. Sanz [2211.02058]
- All approaches are "SMEFT-specific ML" with differences mostly on the practical side

