Search for axion dark matter in the laboratory and in the cosmos

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PNU-IBS workshop on axion physics.

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Based on arXiv:2207.06884 and arXiv:2312.xxxxx (to appear) with Sang Hui Im (CTPU), K.S. Jeong, D.-h.Yeom (PNU): Stephen Lonsdale (PNU)

Introduction
- Motivation

Two stories of axion dark matter
- A proposal for new experiment for axion DM

The magnetic vortex
- Axion electrodynamics
- Axion magnetic vortex

Conclusion

Axion as a window to BSM

- There are many candidates for dark matter.
- Axion is still one of the prime candidates for dark matter.
- It is theoretically well motivated as a solution to the strong CP problem.
- Currently several experiments to detect axions are going on and new ones are being prposed.

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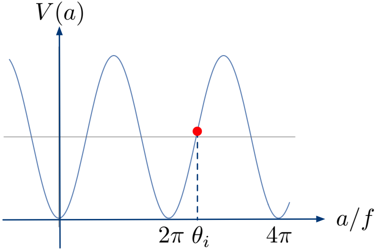
Axion as Dark matter

- The axion solves the strong CP problem dynamically.



- For $T \ll f$ and $H \ll m_a$, the axions are homogeneous and behave collectively as CDM (Preskill+Wise+Wilczek, Abbott+Sikivie, Dine+Fischler 1983):

$$a(t) = \frac{\sqrt{2\rho_a}}{m_a} \sin(m_a t)$$

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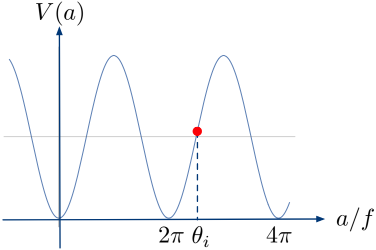

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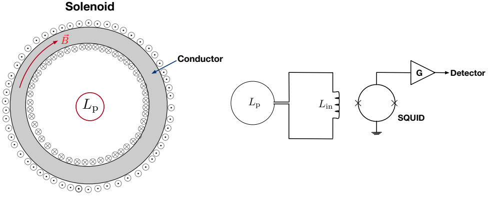
Axion as Dark matter

- For a large decay constant, axions are weakly coupled to SM particles and may constitue DM, $\rho_a \approx \rho_{\mathrm{DM}}$. (Turner 1986)

$$\Omega_a h^2 \approx 0.23 \times 10^{\pm 0.6} \left(\frac{f}{10^{12}\ \mathrm{GeV}} \right)^{1.175} \theta_i^2 F(\theta_i)\,,$$

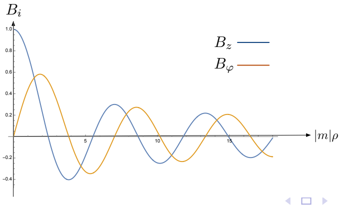
Two stories of axion DM (LACME and Axion Vortex)

- A proposal to detect axions (See talk by S.H. Im on Wed.) :



(a) (b)

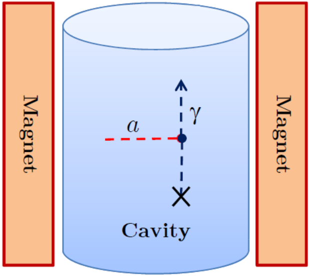
- Axion vortex ($m = g_{a\gamma}\dot{a}$) (See talk by S. Lonsdale on Thurs.)



Existing experiments and proposals

- From its coupling to photons: (Sikivie '83, ... CAPP)

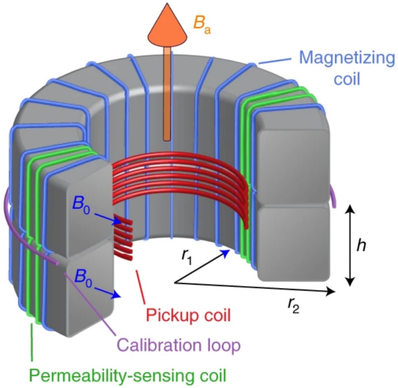
$$\mathcal{L}_{\rm int} \ni g_{a\gamma\gamma} \frac{a}{2f} \epsilon^{\mu\nu\rho\sigma} F_{\mu\nu} F_{\rho\sigma} .$$



Existing experiments and proposals

- Axions couple to photons, modifying Maxwell equations: ABRACADABRA '16, DMRadio, $\cdots$

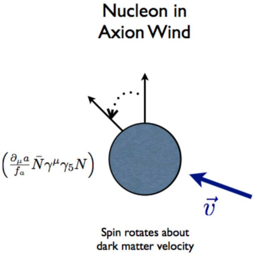
$$\nabla \times \vec{B} = g_{a\gamma\gamma} \dot{a} \vec{B} \,.$$

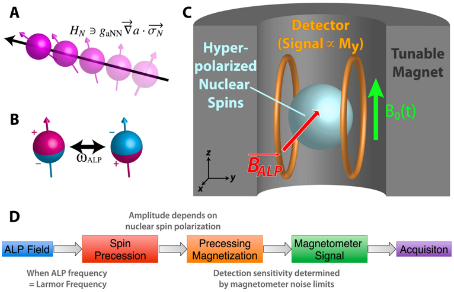


Existing experiments and proposals

- Axions couple to gluons and hadrons: CASPER, spin torsion, ...

$$\mathcal{L}_{\rm int} \ni \frac{c_N}{f}\partial_\mu a \bar{N}\gamma^\mu\gamma_5 N + i\frac{g_d}{2}a(t)\bar{N}\sigma_{\mu\nu}\gamma_5 N F^{\mu\nu}$$





Low temperature Axion Chiral Magnetic Effect

- Electrons couple to axion DM: LACME (our proposal)

$$\mathcal{L}_{\rm int} = C_e \frac{\partial_\mu a}{f} \bar{\psi}\gamma^\mu \gamma_5 \psi \approx \frac{C_e}{f}\sqrt{2\rho_{\rm DM}}\cos(m_a t)\psi^\dagger \gamma_5 \psi \,.$$

- Axion DM acts as an axial chemical potential for electrons.

$$\mu_5 = C_e \frac{\sqrt{2\rho_{\rm DM}}}{f}\cos(m_a t)$$

- The axial chemical potential induces a helicity imbalance if $B \neq 0$. $\Rightarrow$ Chiral Magnetic Effects (Fukushima+Kharzeev+Warringa 2008).

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Axionic Chiral Magnetic Effects

- The axial chemical potential adds a kick to electrons along their spin direction:

$$\mathcal{L} = \bar{\Psi}\left(i\partial\!\!\!/ - m + \mu\gamma^0 + \mu_5\gamma^0\gamma_5\right)\Psi$$

- We take a non-relativistic limit by subtracting out the rest mass and integrating out the negative states, χ:

$$\Psi \equiv \begin{pmatrix}\psi \\ \chi\end{pmatrix} e^{-imt} \qquad (\mu_{\rm NR} \equiv \mu - m)$$

$$\Rightarrow \mathcal{L}_{\rm NR} \;=\; \psi^\dagger\left[i\partial_0 - \frac{(i\vec{\sigma}\cdot\vec{\nabla} + \mu_5)^2}{2m}\right]\psi + \mu_{\rm NR}\psi^\dagger\psi + \cdots$$

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Normal medium

- Consider a cold medium of (free) electrons :

$$\mathcal{L} = \bar{\psi}\left(i\not{\partial} - m + \mu\gamma^0\right)\psi$$

$$\Downarrow$$

$$E = -\mu \pm \sqrt{m^2 + \vec{p}^2}\,,$$

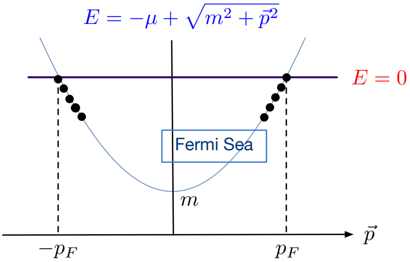

Figure: normal medium

chiral magnetic effects in chiral medium

- CME is a current flow due to the helicity imbalance in (polarized) medium by the axial chemical potential μ_5 and B:

$$\left\langle \vec{j} \right\rangle = v_F \frac{e^2}{2\pi^2} \mu_5 \vec{B}$$

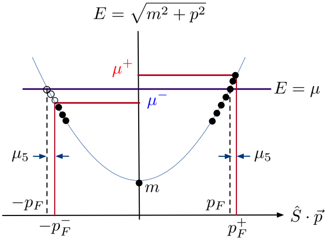

Figure: chiral medium

- We need polarized electrons to see this effect.
- Under an external magnetic field, electrons move parallel or antiparallel to $\vec{B}$ but the spins are always antiparallel for LLL.

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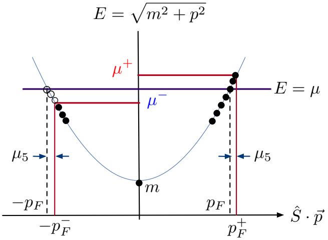

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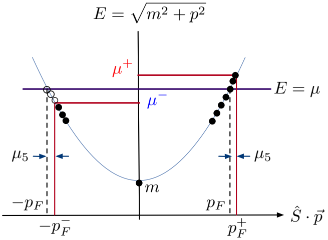

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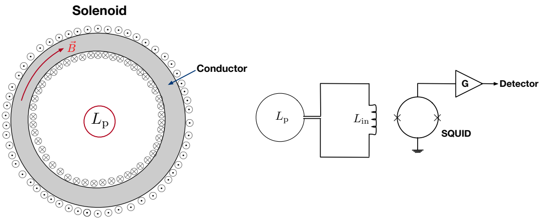
Axionic Chiral Magnetic Effects

- We propose a new experiment (LACME) to detect this non-dissipative currents in a conductor:

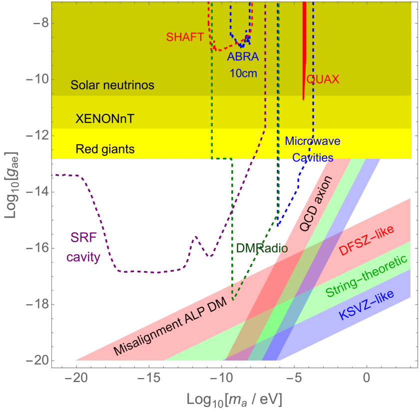
$$j^3 = 6.8 \times 10^{-15}\,\mathrm{Am}^{-2}\left(\frac{v_F}{0.01c}\right)\left(\frac{\rho_{\mathrm{DM}}}{0.4\,\mathrm{GeVcm}^{-3}}\right)^{1/2}\left(\frac{10^{12}\,\mathrm{GeV}}{f/C_e}\right)\left(\frac{B}{10\,\mathrm{Tesla}}\right)$$



(a) (b)

Axionic Chiral Magnetic Effects

- Projection of LACME from existing axion haloscopes, assuming $v_F = 0.01$ ($g_{ae} = 2C_e m_e/f$):



Axion-electron coupling

- The axion-electron coupling depends on the UV model.
- The strength of the axion-electron coupling varies as (See e.g. 2106.05816 by Choi+Im+Seong)

$$C_e \simeq \begin{cases} \mathcal{O}(1) & \text{DFSZ-like models} \\ \mathcal{O}(10^{-4} \sim 10^{-3}) & \text{KSVZ-like models} \\ \mathcal{O}(10^{-3} \sim 10^{-2}) & \text{String-theoretic axions}\,. \end{cases}$$

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Axion electrodynamics

- Axion electrodynamics for $\vec{\nabla} a = 0$:

$$\vec{\nabla} \cdot \vec{E} = 0 \,, \quad \vec{\nabla} \times \vec{B} - \frac{\partial}{\partial t} \vec{E} = -g_{a\gamma} \dot{a} \vec{B} \,,$$

- In axion electrodynamics, the magnetic field sources itself, producing a current $\vec{J} = -m\vec{B}$ with $m = g_{a\gamma}\dot{a}$ even in the absence of charged particles.
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Axion electrodynamics

- When $\dot{a}$ is almost constant, there should exist a topological soliton carrying a finite magnetic flux.
- We therefore ask how the magnetic fields along the vortex should be distributed to minimize its energy for a given magnetic flux, which is topologically conserved.
- Our ansatz :

$$\vec{E} = 0\,, \quad \vec{B} = (0, B_\varphi(\rho), B_z(\rho))\,,$$

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- The energy for the static magnetic field

$$\mathcal{E} = \int \mathrm{d}^3x \left\{ \frac{1}{2}\vec{B}^2 - \vec{A}\cdot\vec{J} \right\} = \int \mathrm{d}^3x \left\{ \frac{1}{2}\left(\vec{B} + m\vec{A}\right)^2 - \frac{1}{2}m^2\vec{A}^2 \right\}$$

- The minimum energy saturated by configurations that satisfy the Maxwell equation or $\vec{B} = -m\vec{A}$ in the Coulomb gauge:

$$B''_\varphi + \frac{1}{\rho}B'_\varphi - \left(\frac{1}{\rho^2} - m^2\right)B_\varphi = 0\,; \quad B''_z + \frac{1}{\rho}B'_z + m^2 B_z = 0\,.$$

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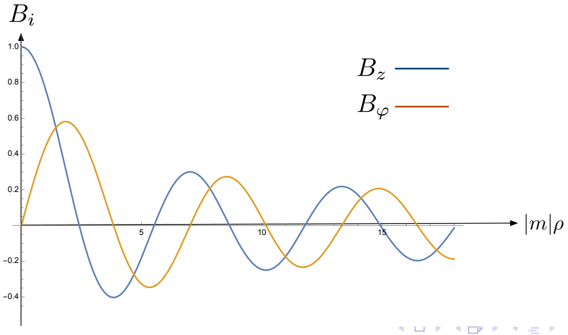
Axion magnetic vortex

- The minimum energy configuration for a given flux Φ is with the normalization, $\mathcal{N} = 2\pi \int_0^{x_c} x J_0(x) \mathrm{d}x$,

$$B_\varphi(\rho) = -m|m| \frac{\Phi}{\mathcal{N}} J_1(|m|\rho), \;\; B_z(\rho) = m^2 \frac{\Phi}{\mathcal{N}} J_0(|m|\rho).$$



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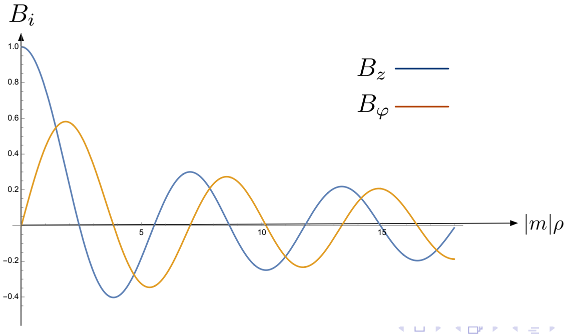
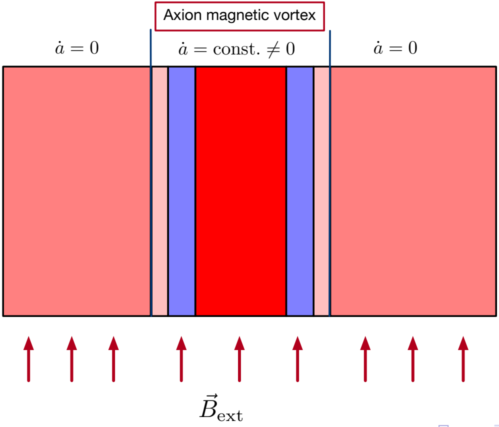


Axion magnetic vortex

- If we apply an external magnetic field, $\vec{B}_{\text{ext}}$, an axion magnetic vortex will form spontaneously:



Axion magnetic vortex

- For the normal modes inside axion magnetic vortex

$$\delta a = \theta(t) f(|m|\rho)$$

- The normal modes satisfy, after rescaling $|m|\rho$ to be ρ,

$$-\nabla^2 f(\rho) - \frac{\omega^2}{m^2} H(\rho) f(\rho) = -\lambda f(\rho)\,,$$

where $\omega^2 = -\ddot{\theta}/\theta$, $\lambda = m_a^2/m^2$, $H = 1 - g_{a\gamma}^2\, m|m| \left(\frac{\Phi}{\mathcal{N}} J_0(\rho)\right)^2$.

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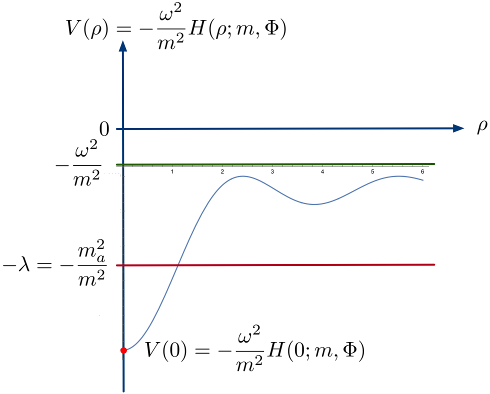
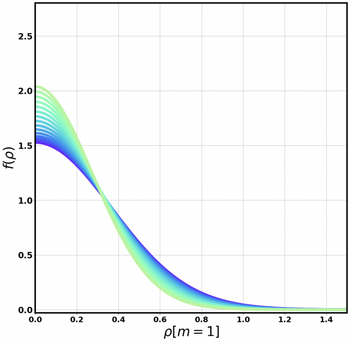
Axion magnetic vortex

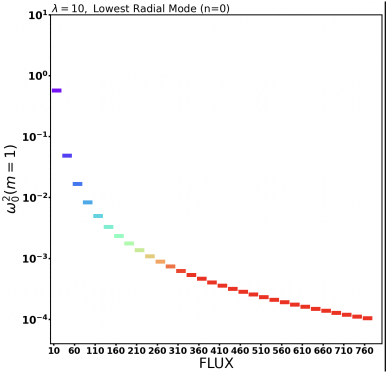
- Axion spectrum inside vortex is that of Schrödinger equation:



Axion magnetic vortex

- The lowest energy eigenstate :





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Conclusion

- We show that dark matter axions or axion-like particles (ALP) induce non-dissipative alternating electric currents in conductors along the external magnetic fields due to the axial anomaly, realizing the chiral magnetic effects.

$$\vec{j} = v_F \frac{e^2}{2\pi^2} \frac{C_e}{f} \dot{a} \vec{B} \,. \quad \text{(LACME)}\,.$$

- We propose a new experiment to measure this current in medium to detect the dark matter axions or ALP. (LACME)
- This non-dissipative currents are the electron medium effects, directly proportional to the axion or ALP coupling to electrons, which depends on their microscopic physics.

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- The axion magnetic vortex is stable for small fluctuations.
- Axions are bound to the vortex, having energy $\omega < m_a$.
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