

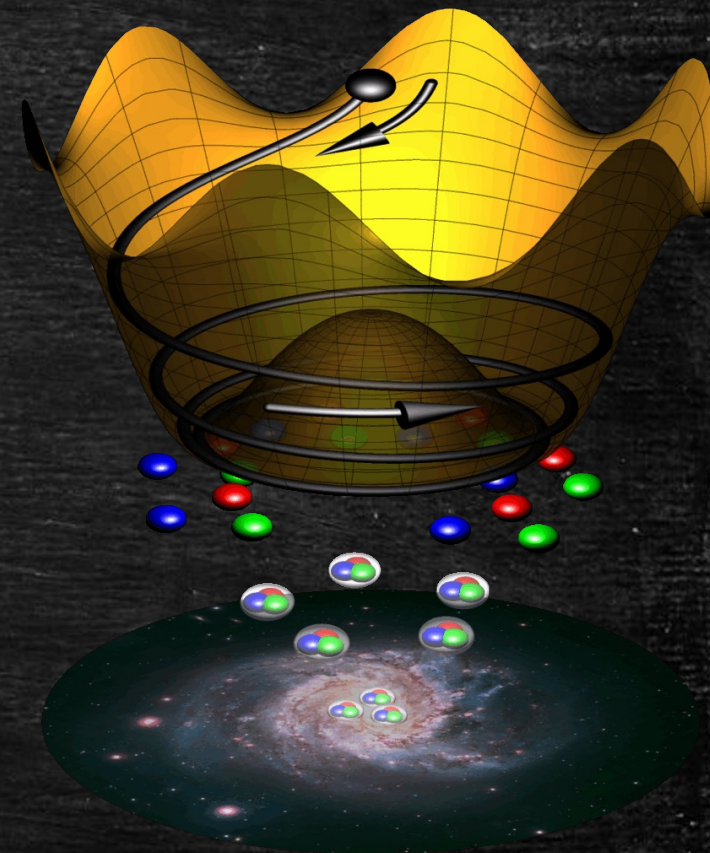
# Cosmological Implications of Axion Rotations

PNU-IBS workshop on Axion Physics : Search for axions  
Haeundae beach, Busan, South Korea

December 8<sup>th</sup>, 2023

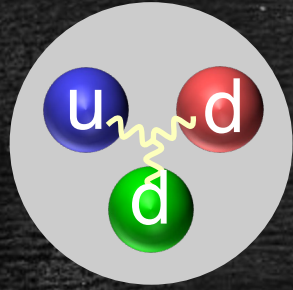
Raymond Co

Indiana University



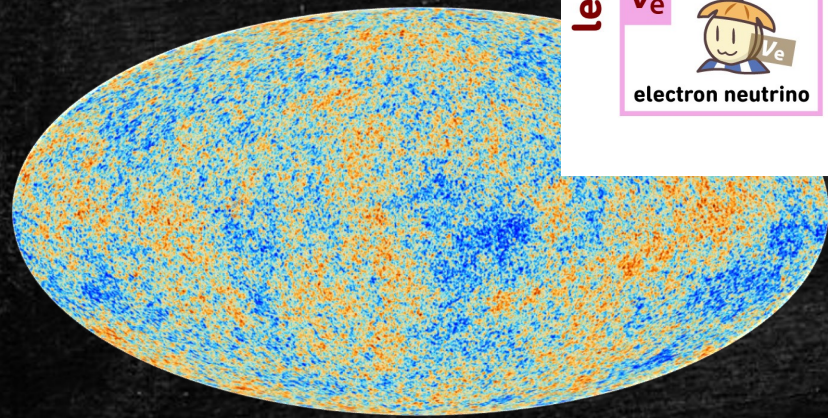
# Outline of the Talk

strong CP problem



neutron

	matter (fermions)			gauge bosons	
quarks	<b>u</b> up quark	<b>c</b> charm quark	<b>t</b> top quark	<b>γ</b> photon	electro-magnetic
	<b>d</b> down quark	<b>s</b> strange quark	<b>b</b> bottom quark	<b>g</b> gluon	strong
	<b>e</b> electron	<b>μ</b> muon	<b>τ</b> tau	<b>Z, W<sup>±</sup></b> weak bosons	weak
leptons	<b>ν<sub>e</sub></b> electron neutrino	<b>ν<sub>μ</sub></b> muon neutrino	<b>ν<sub>τ</sub></b> tau neutrino	<b>H</b> higgs boson	Higgs bosons



Source: Planck



matter-antimatter asymmetry

dark matter

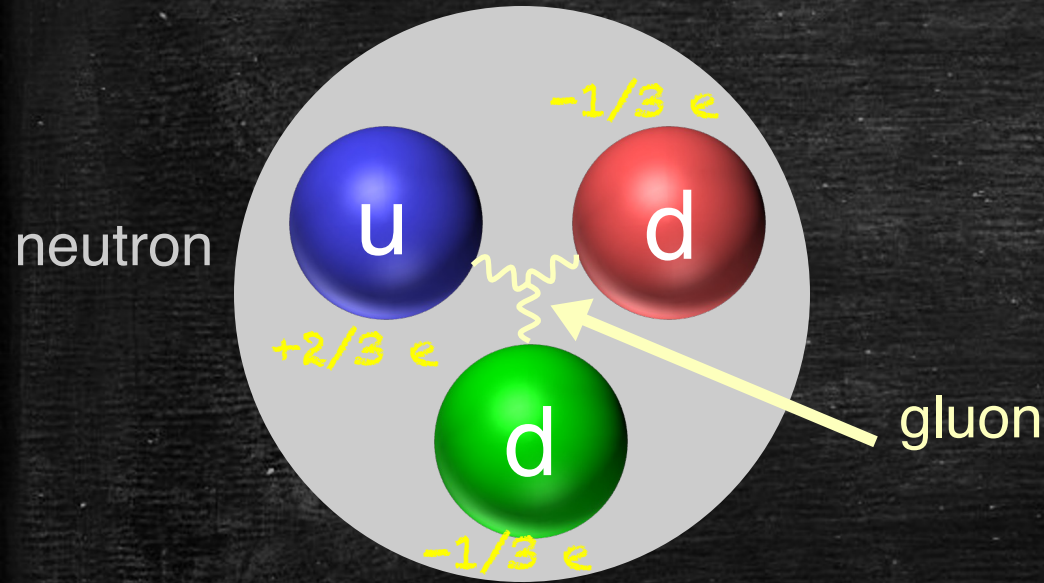


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# Review of the QCD Axion

# Strong CP Problem

“Charge-Parity” symmetry



Quantum field theory:

$$\mathcal{L} \supset \bar{\theta} \frac{\alpha_s}{8\pi} G_b^{\mu\nu} \tilde{G}_{b\mu\nu}$$

gluon

$$|d_n| \simeq 2.4 \times 10^{-16} \bar{\theta} e \cdot \text{cm}$$

Crewther, Di Vecchia, Veneziano, Witten 1979, Pospelov, Ritz 2000

Experiments:

$$|d_n| \lesssim 1.8 \times 10^{-26} e \cdot \text{cm}$$

PRL 97, 131801 2006, PRL 124, 081803 2020

Strong CP problem:

$$\bar{\theta} \lesssim 10^{-10}$$

Why exceedingly small?

# Strong CP Problem solution



Peccei

Quinn

2017  Quanta magazine

$$\mathcal{L} \supset \bar{\theta} \frac{\alpha_s}{8\pi} G_b^{\mu\nu} \tilde{G}_{b\mu\nu}$$

Peccei, Quinn 1977  
Weinberg 1978  
Wilczek 1978

QCD axion

Promoted to a dynamical field:

$$\mathcal{L} \supset \left( \bar{\theta} + \frac{a}{f_a} \right) \frac{\alpha_s}{8\pi} G_b^{\mu\nu} \tilde{G}_{b\mu\nu}$$

decay constant

QCD effects automatically generate an axion potential  $V(a) = m_a^2 f_a^2 \left[ 1 - \cos \left( \bar{\theta} + \frac{a}{f_a} \right) \right]$

This potential dynamically drives the axion to a field value that cancels  $\bar{\theta}$ . Problem solved!

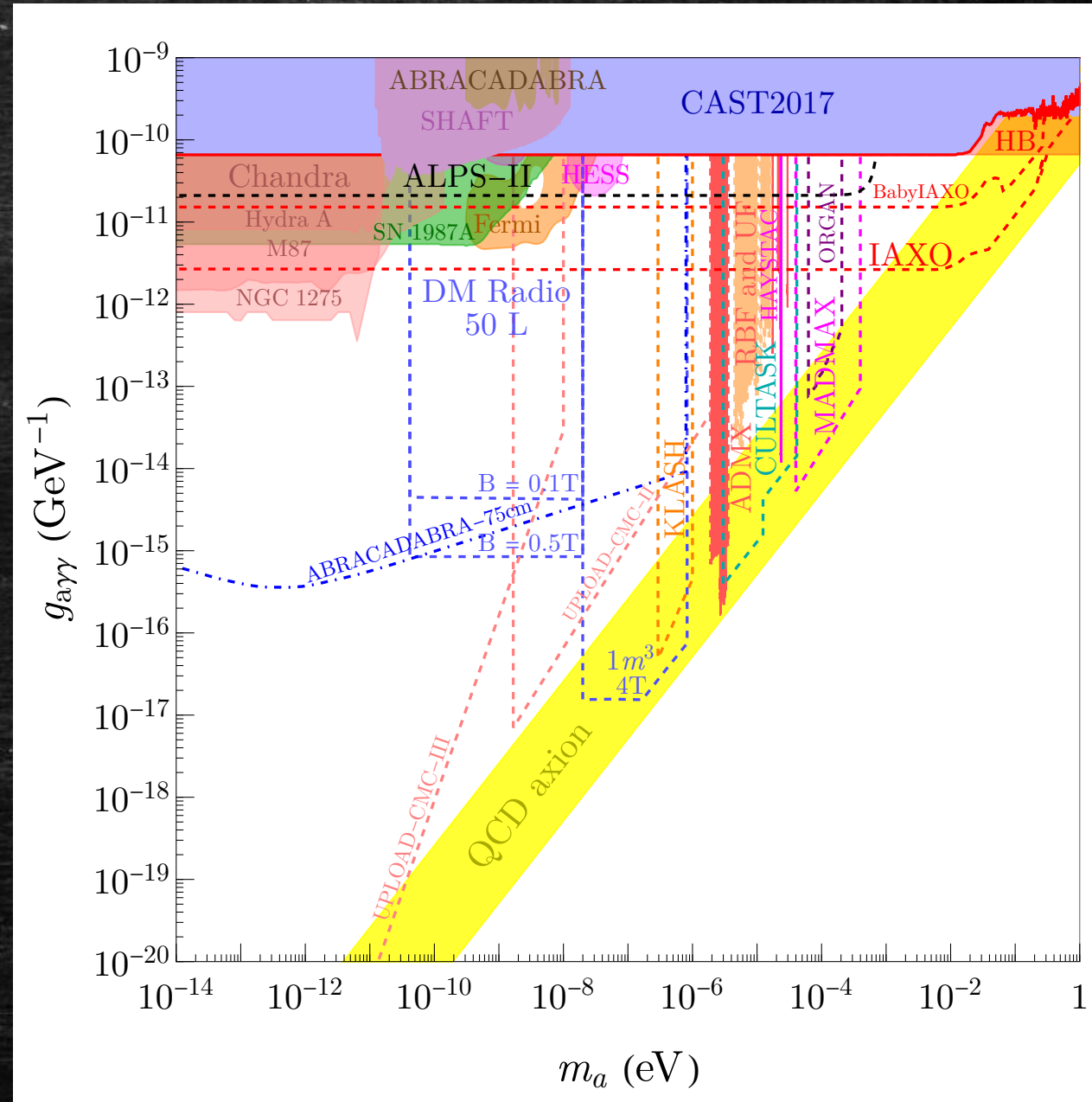
# Status of Axion Dark Matter

# Experimental Searches

## Experimental progress

shaded regions: excluded

broken lines: future sensitivities



# Axion Dark Matter Abundance

damped simple harmonic oscillator

Equation of motion: 
$$\left(\partial_t^2 + 3H\partial_t + m_a^2\right) a = 0$$

Hubble "friction"  
(from cosmic expansion)



# Axion Dark Matter Abundance

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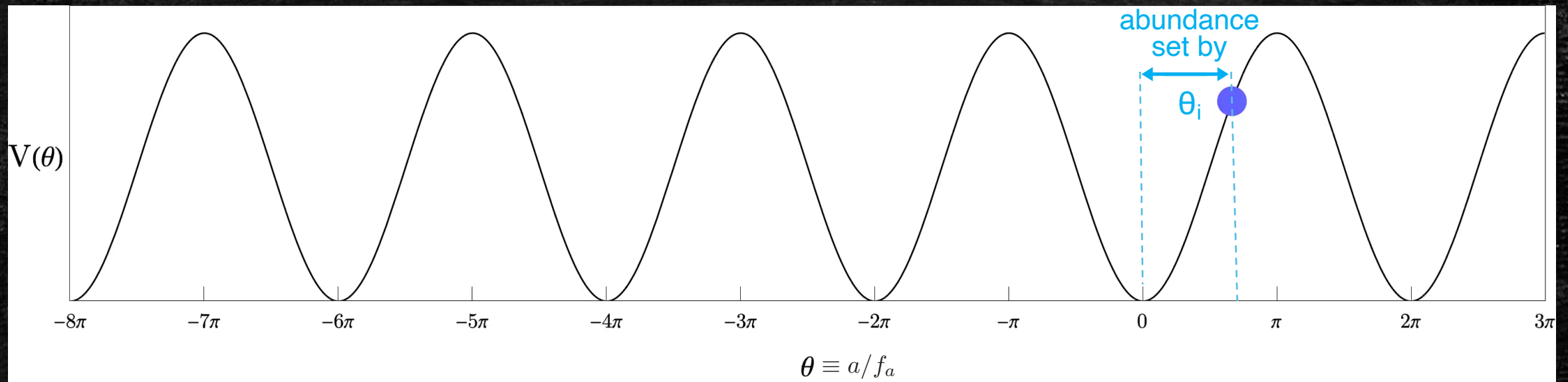
Hubble "friction"  
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## Misalignment Mechanism

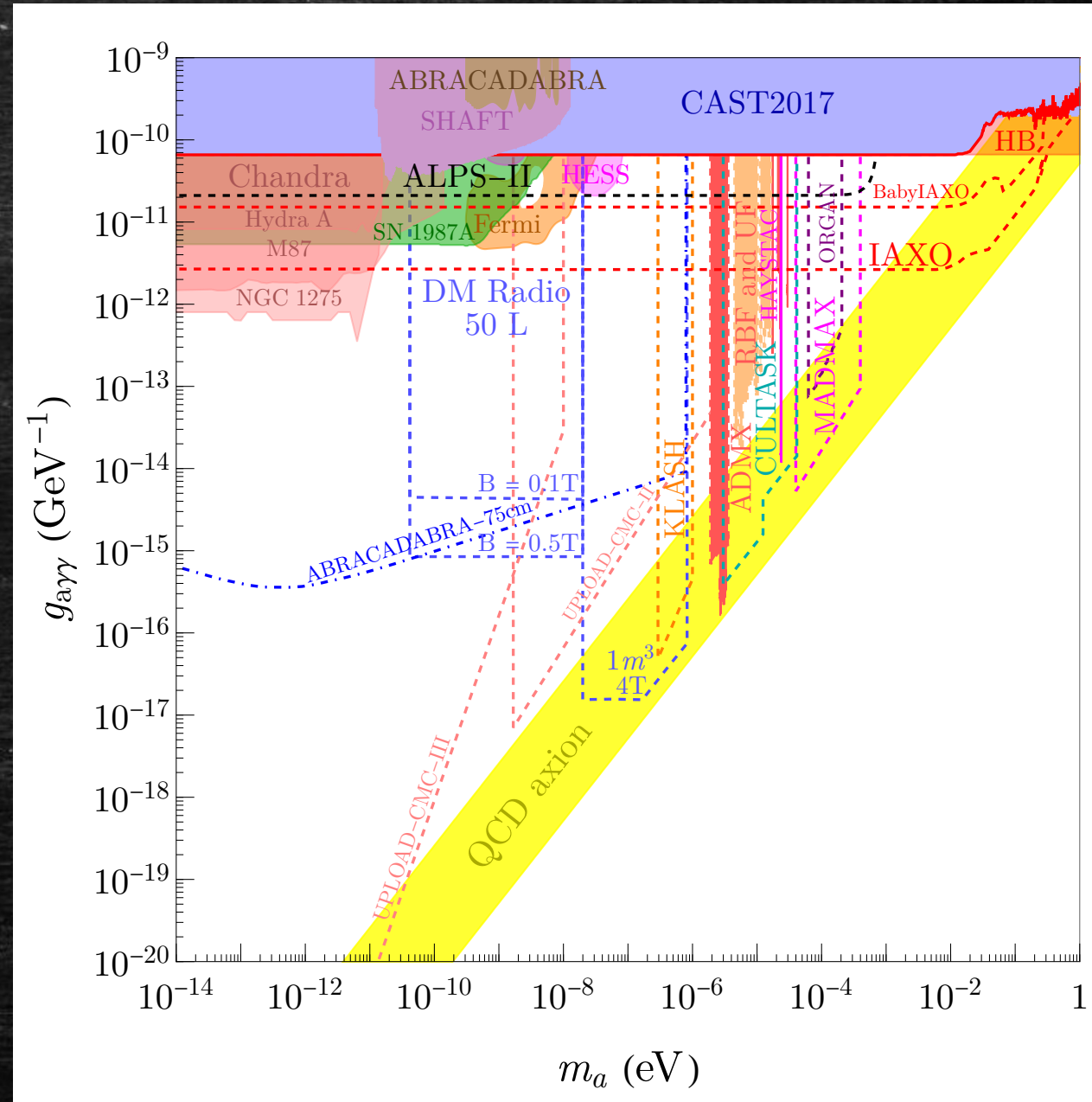
Preskill, Wise, Wilczek 1983  
Abbott, Sikivie 1983  
Dine, Fischler 1983

oscillations start when

$$H \lesssim m_a$$

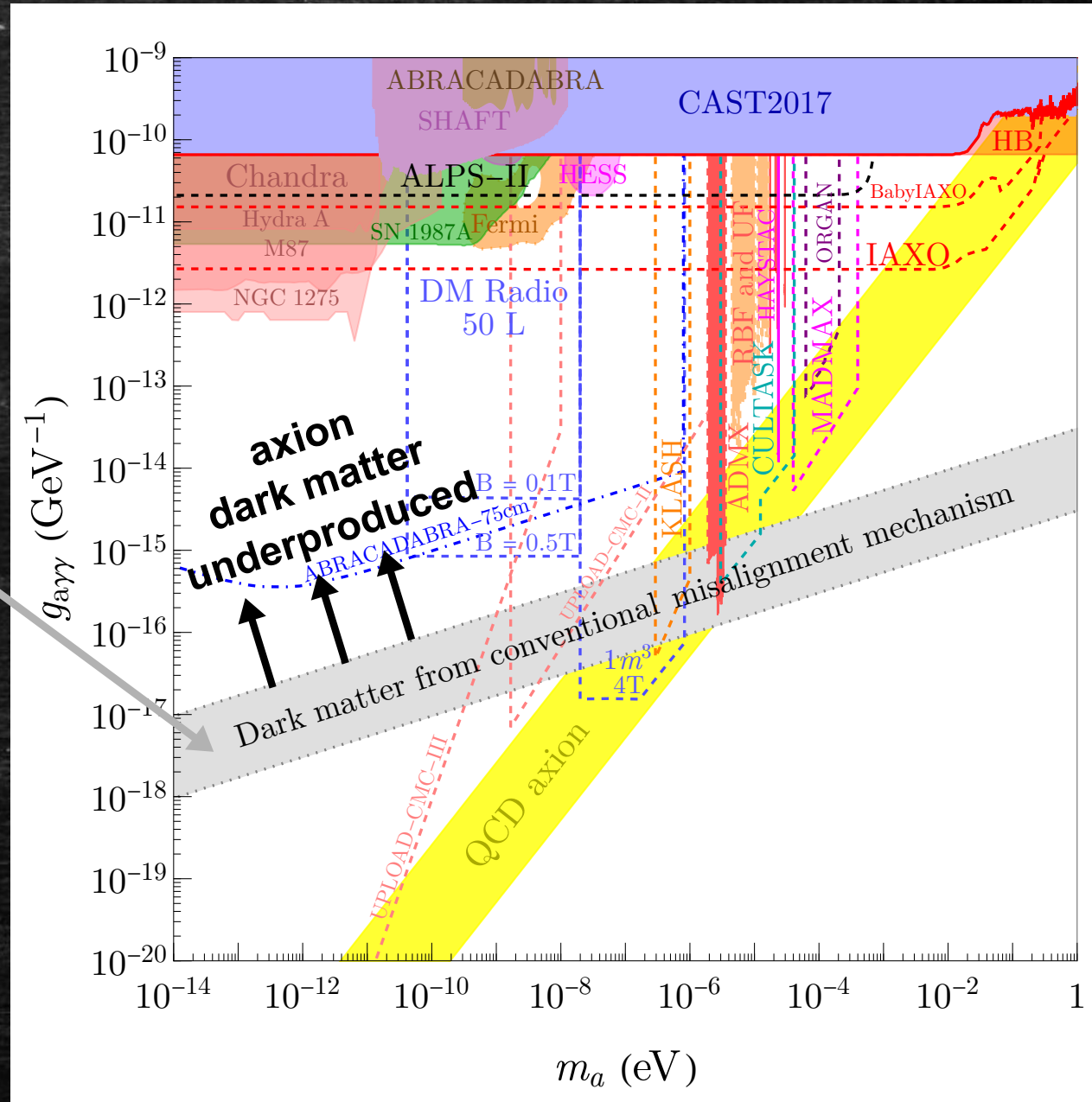


# Axion Dark Matter Abundance



# Axion Dark Matter Abundance

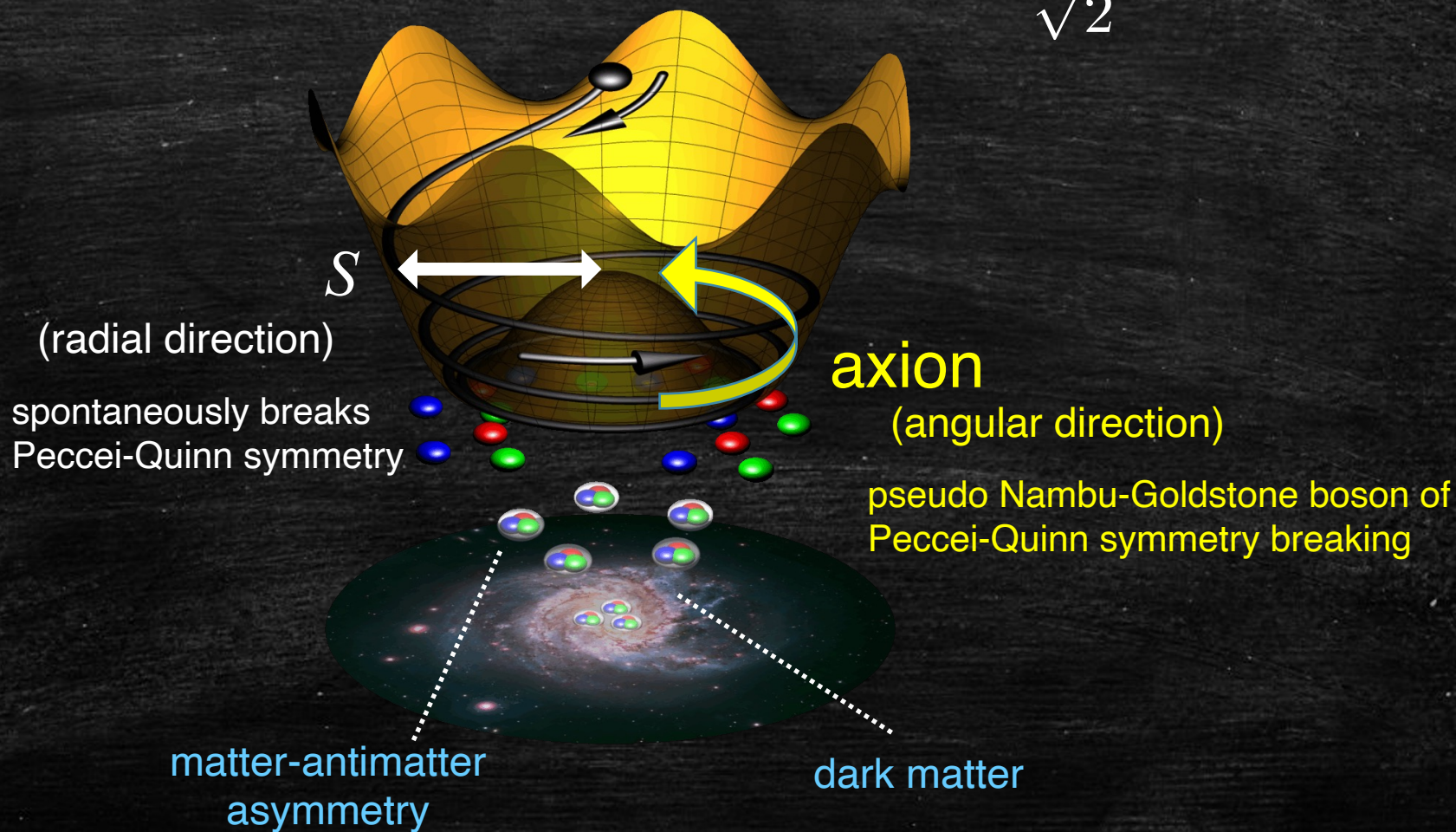
We assume  $\theta_i = \mathcal{O}(1)$  here.



# Axion Rotation

$$\mathcal{L} \supset \frac{\alpha_s}{8\pi} \frac{a}{f_a} G_b^{\mu\nu} \tilde{G}_{b\mu\nu}$$

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$



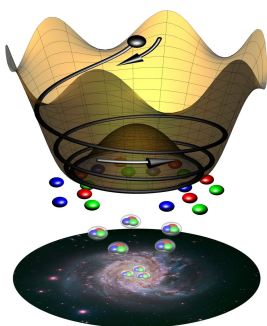
# PHYSICAL REVIEW LETTERS

Articles published week ending 20 MARCH 2020



## Paper sheds light on infant universe and origin of matter

10 March 2020



the School of Natural Sciences at the Institute for Advanced Study, and Raymond T. Co of the University of Michigan, have presented a compelling case in which the quantum chromodynamics (QCD) axion, first theorized in 1977, provides several important answers to these questions.

"We revealed that the rotation of the QCD axion can account for the excess of matter found in the universe," stated Harigaya. "We named this mechanism axiogenesis."

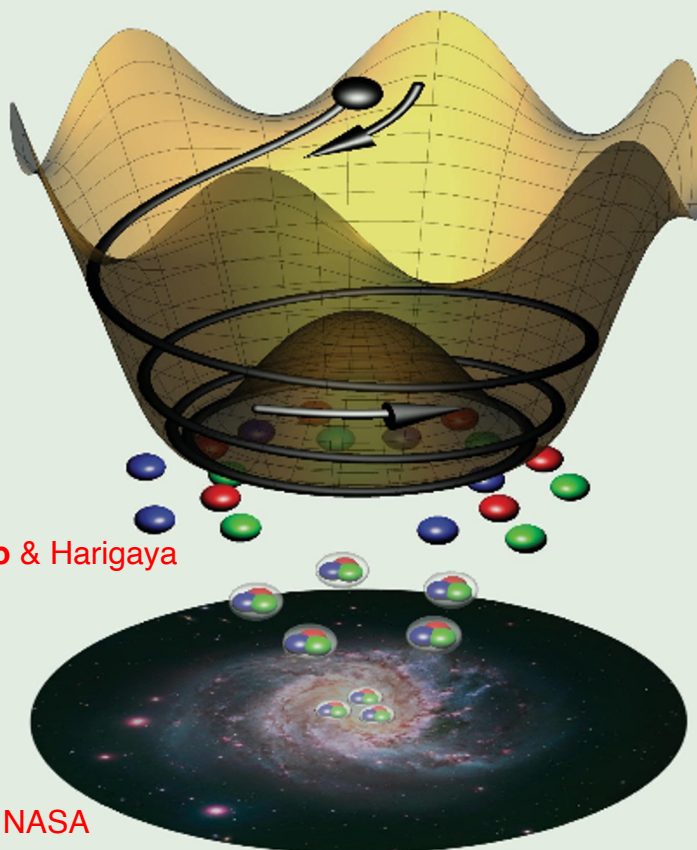
Infinitesimally light, the QCD axion—at least one billion times lighter than a proton—is nearly ghost-like. Millions of these particles pass through ordinary matter every second without notice. However, the subatomic level interaction of the QCD axion can still leave detectable signals in experiments with unprecedented sensitivities. While the QCD axion has never been directly detected, this study provides added fuel for experimentalists to hunt down the elusive particle.

"The versatility of the QCD axion in solving the mysteries of fundamental physics is truly amazing," stated Co. "We are thrilled about the unexplored theoretical possibilities that this new aspect of the QCD axion can bring. More importantly, experiments may soon tell us whether the mysteries of nature truly hint towards the QCD axion."

Harigaya and Co have reasoned that the QCD axion is capable of filling three missing pieces of the physics jigsaw puzzle simultaneously. First, the QCD axion was originally proposed to explain the so-called strong CP problem—why the strong force, which binds protons and neutrons together, unexpectedly preserves a symmetry called the Charge Parity (CP) symmetry. The CP symmetry is inferred from the observation that a neutron does not react with an electric field despite its charged constituents. Second, the QCD axion was found to

Graphic: Co & Harigaya

Photo: NASA



Quanta magazine

Physics Mathematics Bio

ABSTRACTS BLOG

## Axions Would Solve Another Major Problem in Physics

6 |

In a new paper, physicists argue that hypothetical particles called axions could explain why the universe isn't empty.

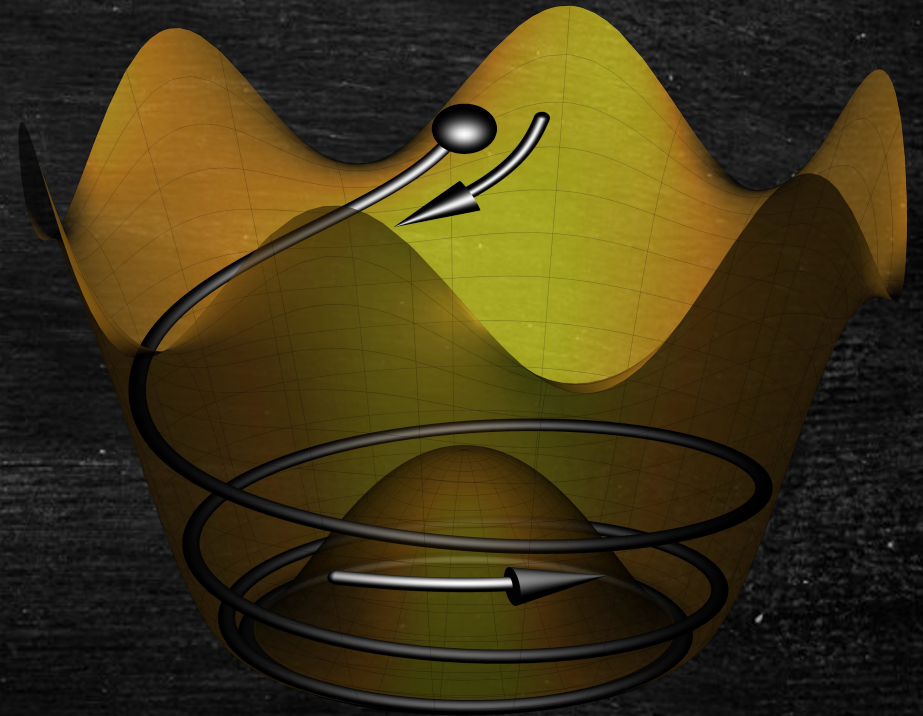
Published by  
American Physical Society



Volume 124, Number 11

# Why Rotation?

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$



Dynamics analogous to that in Affleck-Dine baryogenesis

I. Affleck and M. Dine 1991

PRL 92, 011301 (2004) T. Chiba, F. Takahashi, M. Yamaguchi  
PRL 124, 111602 (2020) RC and K. Harigaya

# Why Rotation?

Wiggles :

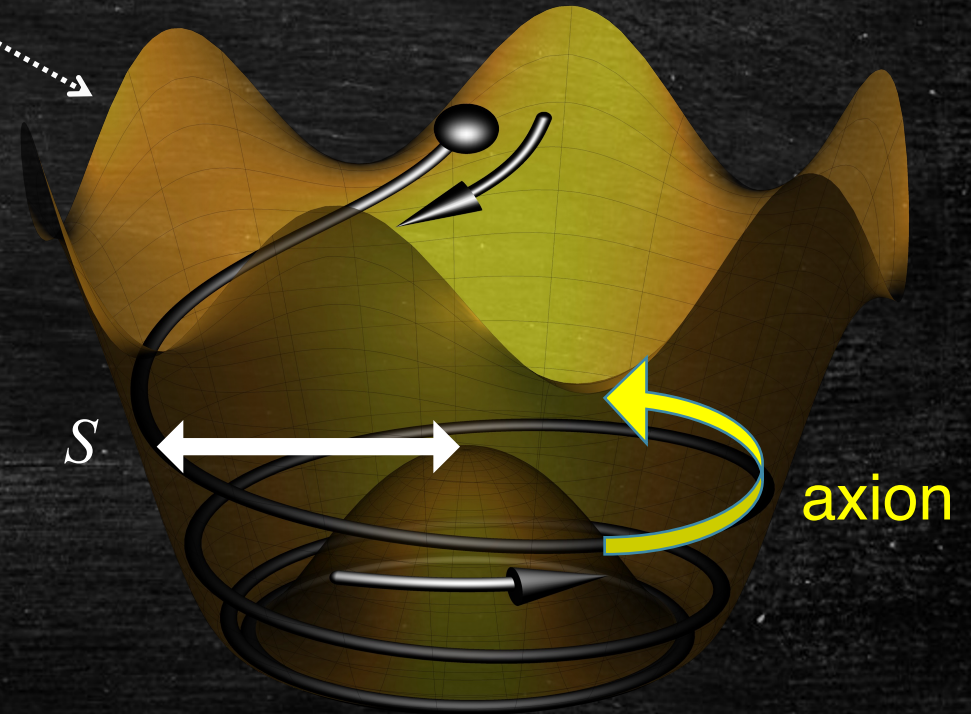
$$V(P) \sim \frac{P^n}{M^{n-4}} e^{i\varphi} + \text{h.c.} \sim \frac{|P|^n}{M^{n-4}} \cos\left(n \frac{a}{f_a} + \varphi\right)$$

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$

Explicit PQ breaking

expected from quantum gravity  
or PQ as an accidental symmetry

S. Giddings et al. 1988  
S. Coleman 1988  
G. Gilbert 1988



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S. Giddings et al. 1988  
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G. Gilbert 1988

Large field value :

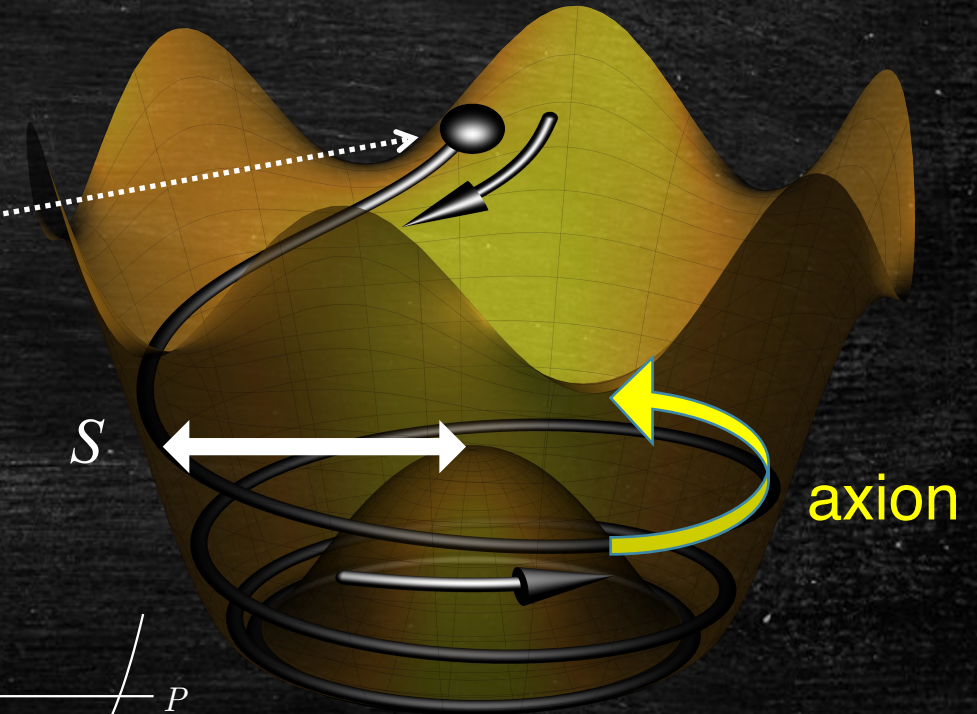
Flat potential

For example, as an initial condition or  
set dynamically by inflationary dynamics

$$V(|P|) \sim -H_I^2 |P|^2 + \frac{|P|^d}{M^{d-4}}$$

Hubble-induced mass

M. Dine, L. Randall, and S. D. Thomas 1991



Dynamics analogous to that in Affleck-Dine baryogenesis

I. Affleck and M. Dine 1991

PRL 92, 011301 (2004) T. Chiba, F. Takahashi, M. Yamaguchi

PRL 124, 111602 (2020) RC and K. Harigaya



# Asymmetry of PQ Charge

Noether charge associated with the shift symmetry

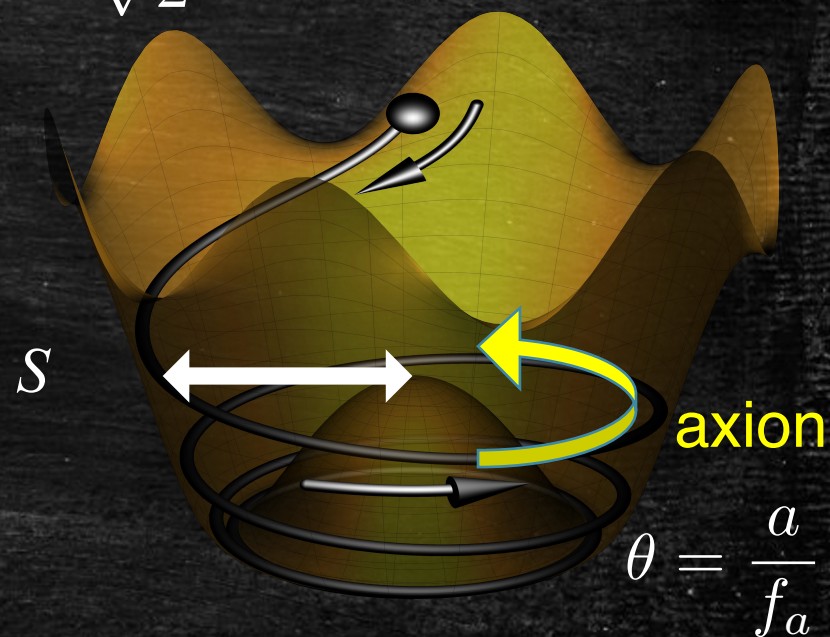
$$n_\theta = S^2 \dot{\theta}$$

this is nothing but  
"angular momentum"  $r^2 \omega$

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$

PQ asymmetry  
PQ charge density = Rotation of PQ field

This is conserved soon after the initial kick.



# Asymmetry of PQ Charge

Noether charge associated with the shift symmetry

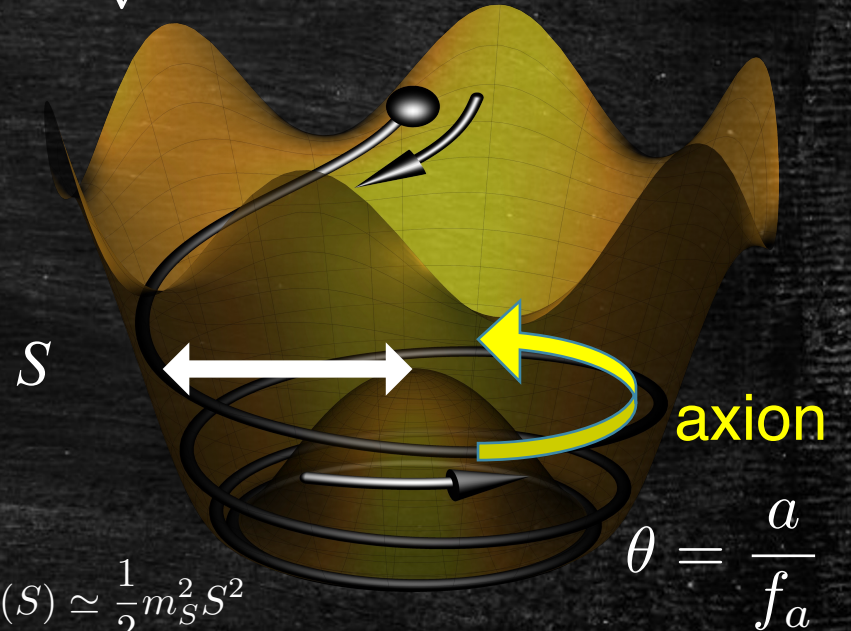
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PQ asymmetry  
PQ charge density = Rotation of PQ field

This is conserved soon after the initial kick.



What determines  $\dot{\theta}$ ? Centripetal force!

$$F_c = m a_c$$

$$V'(S) = S \dot{\theta}^2$$

$$m_S^2 S = S \dot{\theta}^2$$

$$V(S) \simeq \frac{1}{2} m_S^2 S^2$$

from supersymmetry

$$\theta = \frac{a}{f_a}$$

$\dot{\theta} = m_S$  which is in turn set by supersymmetry scale.

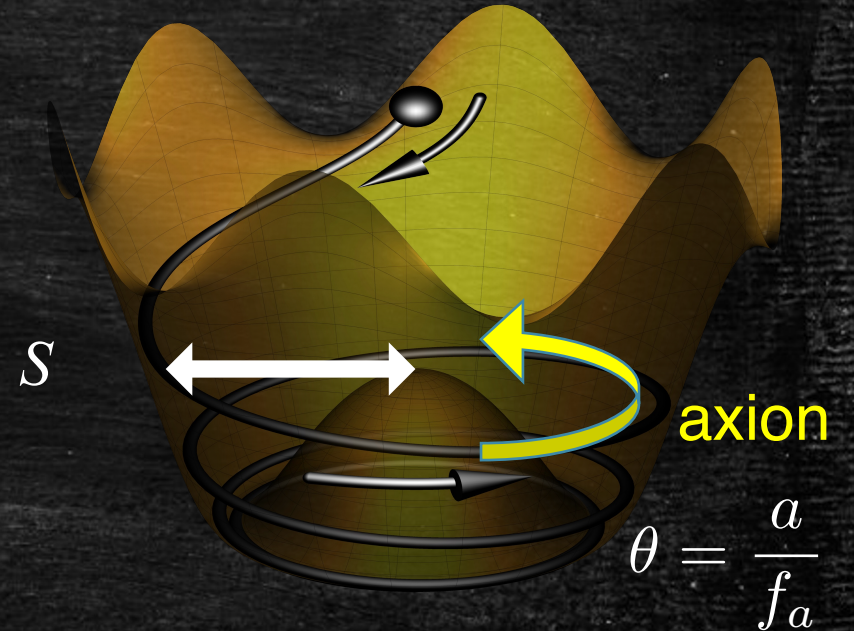
# PQ Charge Evolution

Charge conservation:

$$n_\theta = S^2 \dot{\theta} \propto \frac{R^{-3}}$$

scale factor of the universe

dilution due to cosmic expansion



# PQ Charge Evolution

Charge conservation:

$$n_\theta = S^2 \dot{\theta} \propto \frac{R^{-3}}{\text{scale factor of the universe}}$$

Large field ( $S \gg f_a$ ):

$$S^2 \propto R^{-3}$$

for quadratic potential  
 $V(S) \simeq \frac{1}{2} m_S^2 S^2$

$$\dot{\theta} = \text{constant}$$

$$\rho_\theta = \dot{\theta}^2 S^2 \propto R^{-3}$$

matter

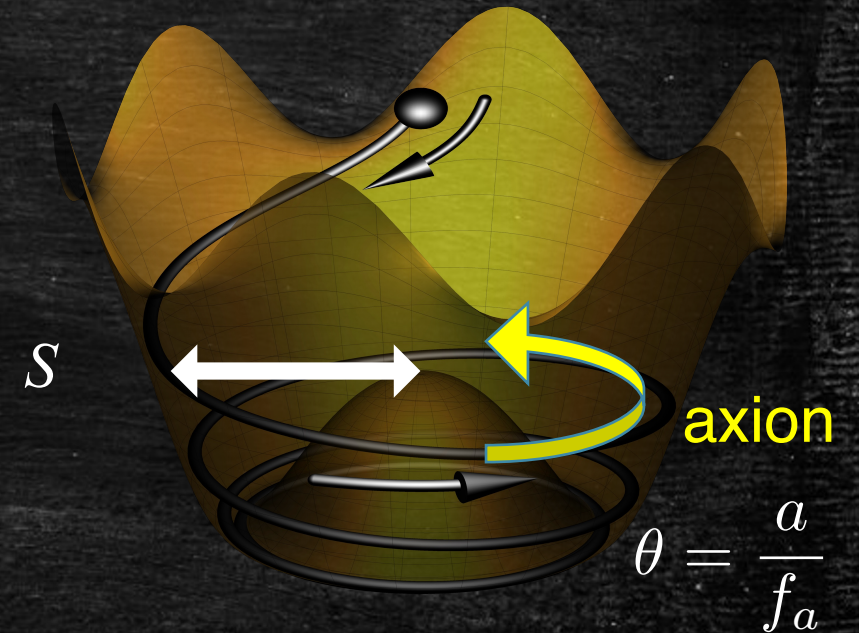
At the minimum:

$$S^2 = f_a^2$$

$$\dot{\theta} \propto R^{-3}$$

$$\rho_\theta = \dot{\theta}^2 f_a^2 \propto R^{-6}$$

kination



# Asymmetries in Thermal Equilibrium

The free energy is minimized at equilibrium.

fermion asymmetry

$$n_\psi \equiv n_{+\mu} - n_{-\mu} \sim \mu T^2$$

Change of the free energy

$$\Delta F_{\text{th}} \sim \Delta\rho - T\Delta s \sim \frac{n_\psi^2}{T^2}$$

$$\Delta F_{\text{rot}} \sim -\dot{\theta} n_\psi$$

$$\Delta F_{\text{tot}} \text{ is minimized when } n_\psi \sim \underline{\underline{\dot{\theta} T^2}} \ll \dot{\theta} S^2 = n_{\text{PQ}}$$

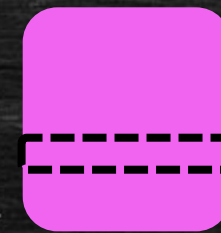
Most of the PQ charge remains in the rotation!

thermal bath

$$n_{\text{th}} \simeq T^3$$

rotation

$$n_{\text{PQ}} = \dot{\theta} S^2$$



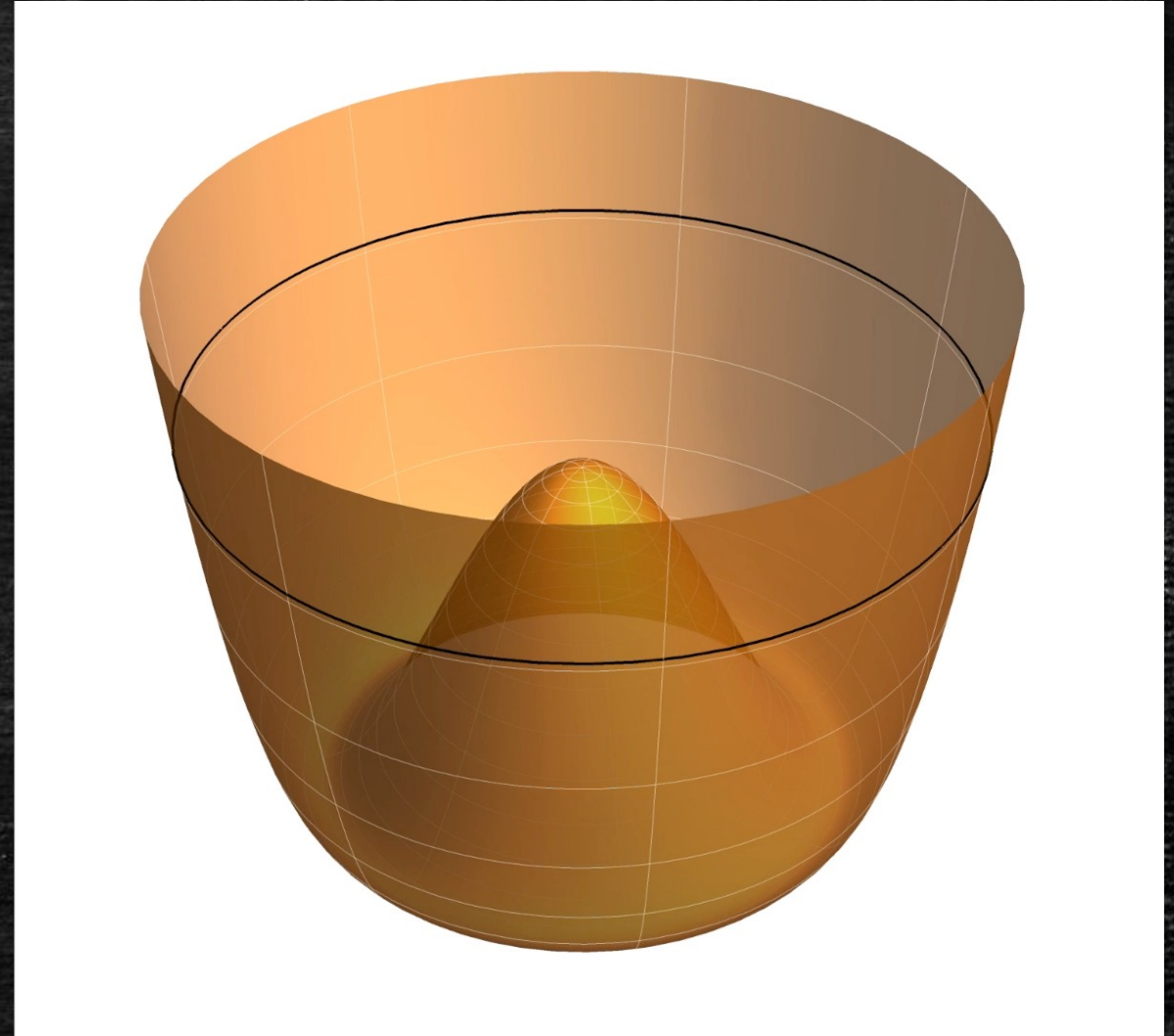
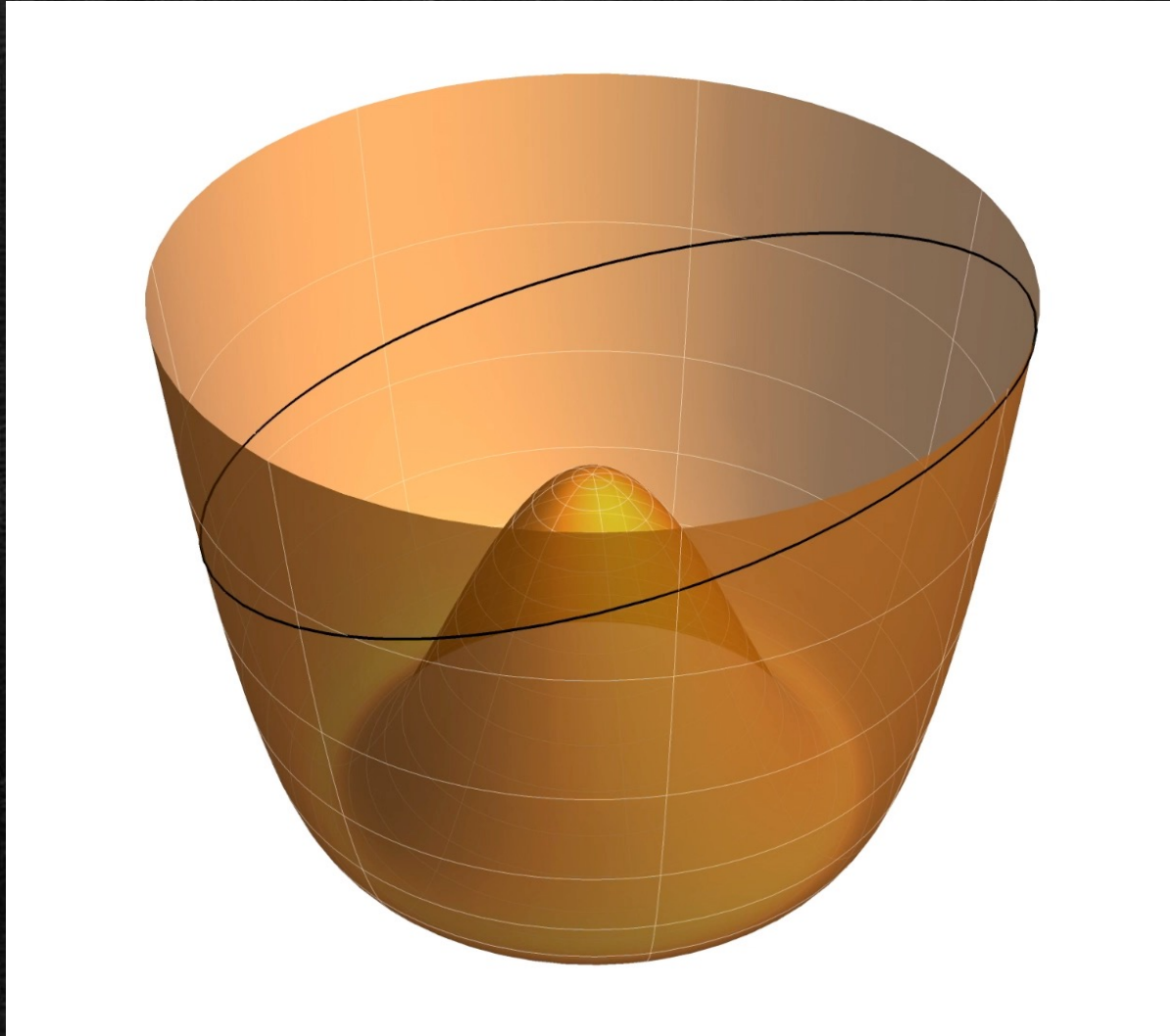
chiral asymmetry



$$n_\psi \simeq \dot{\theta} T^2$$

# Asymmetries in Thermal Equilibrium

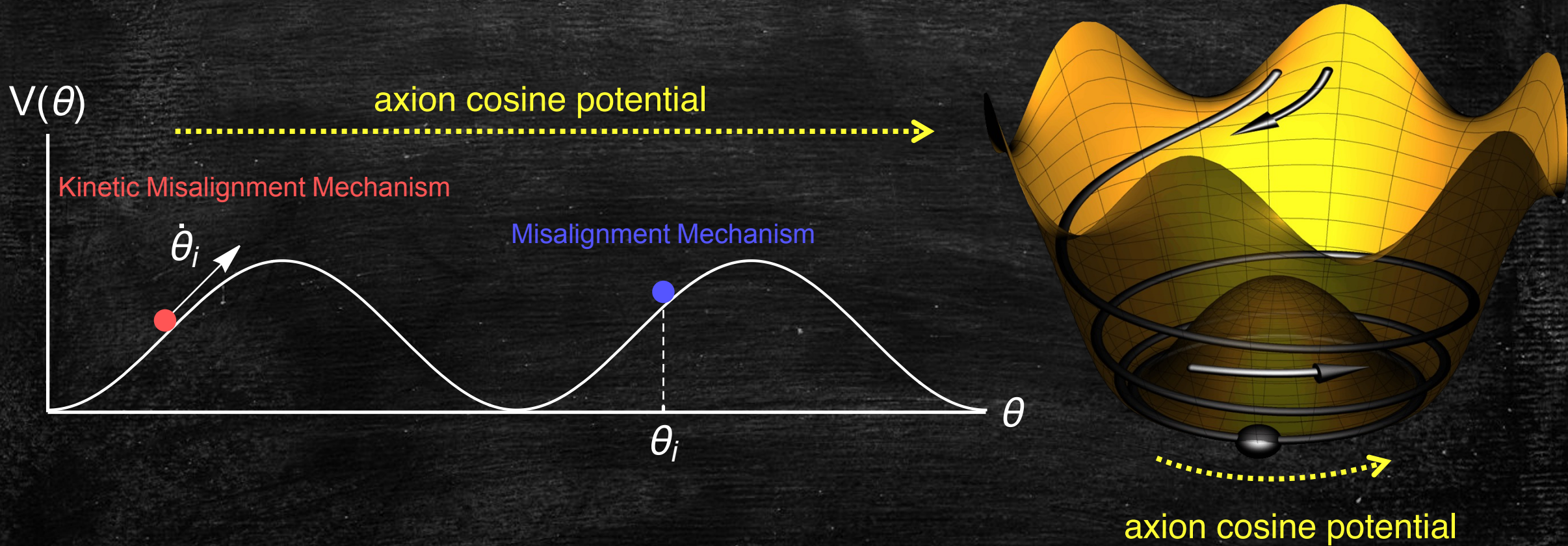
Thermalization  $n_{\text{PQ}} = S^2 \dot{\theta}$  Redshift



# Axion Dark Matter

# Kinetic Misalignment Mechanism

a novel scenario where the axion field has a nonzero initial velocity, e.g., from axion rotations.

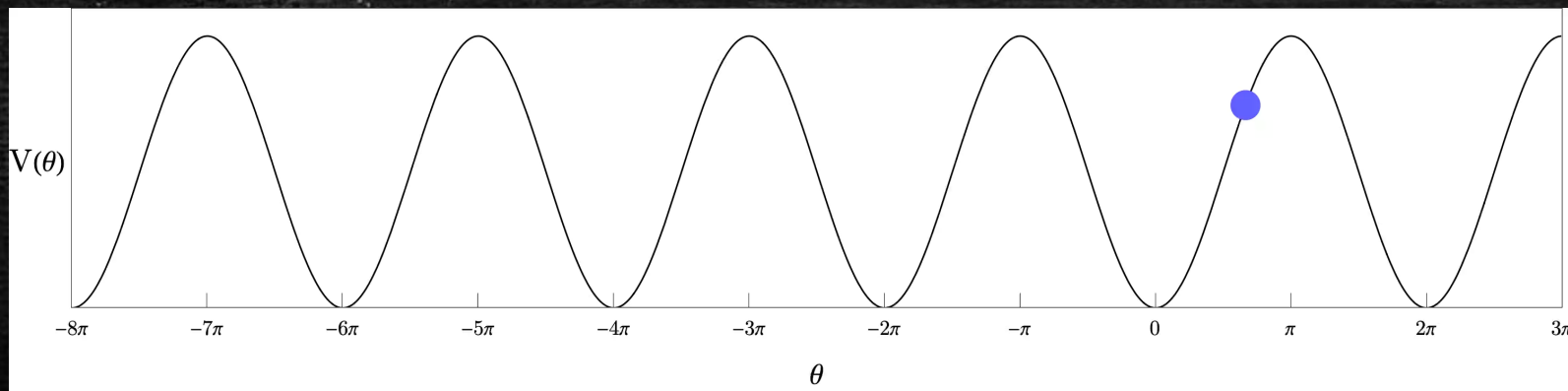




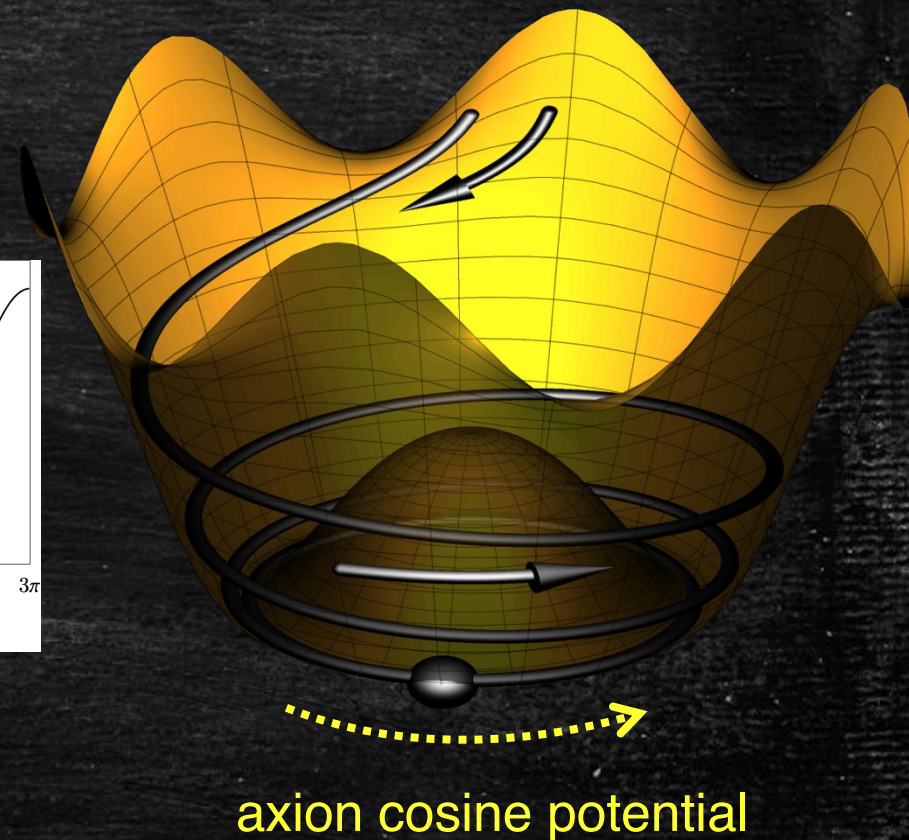
# Kinetic Misalignment Mechanism

a novel scenario where the axion field has a nonzero initial velocity, e.g., from axion rotations.

axion cosine potential

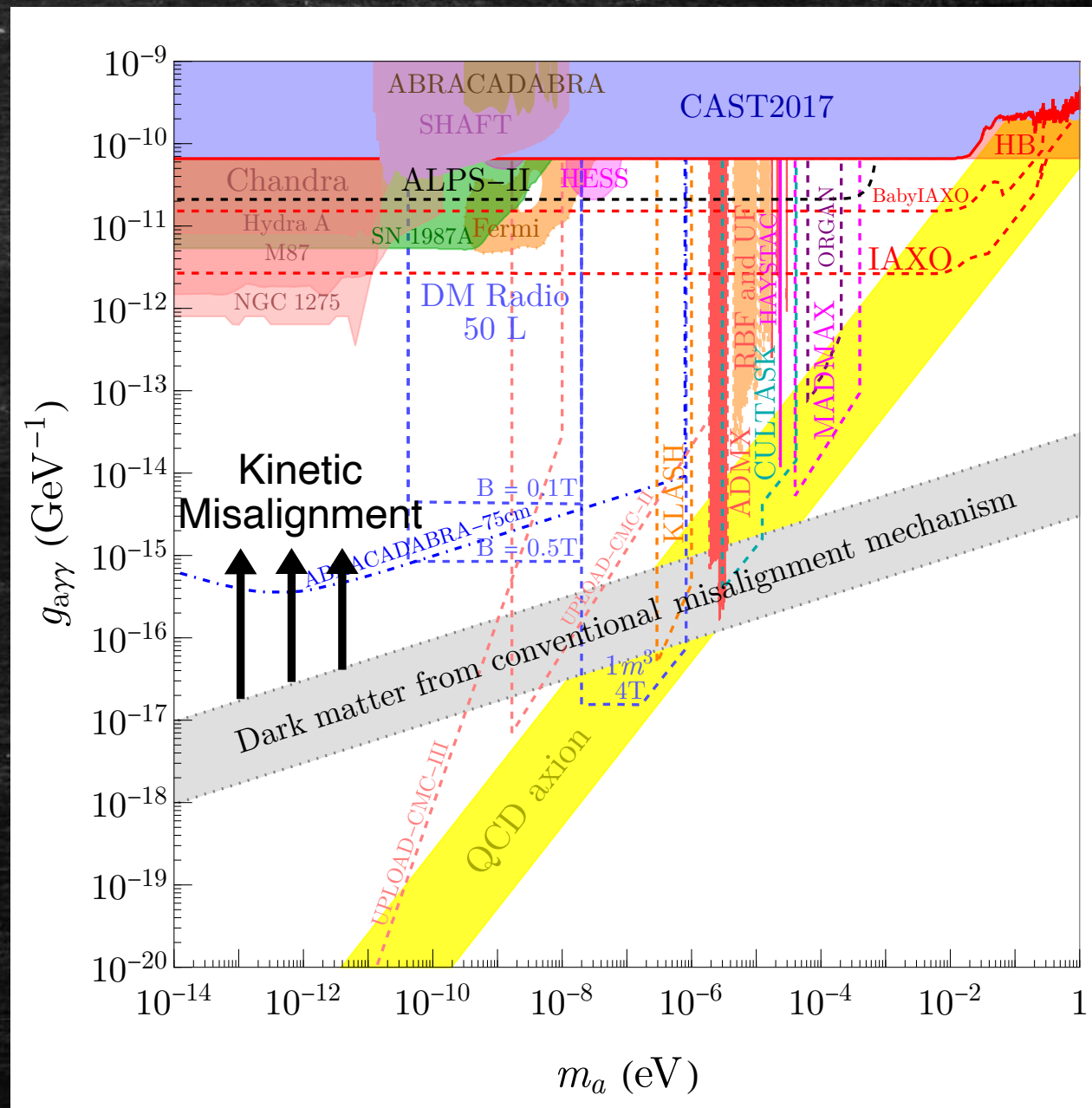


kinetic energy > potential energy  
enhancing axion abundance



# Kinetic Misalignment Mechanism

giving a strong motivation for axion dark matter experiment



# Kinetic Misalignment Mechanism

Kinetic Misalignment\*

charge yield

$$Y_\theta = \frac{n_\theta}{s}$$

$$\frac{\rho_a}{s} \simeq m_a Y_\theta$$

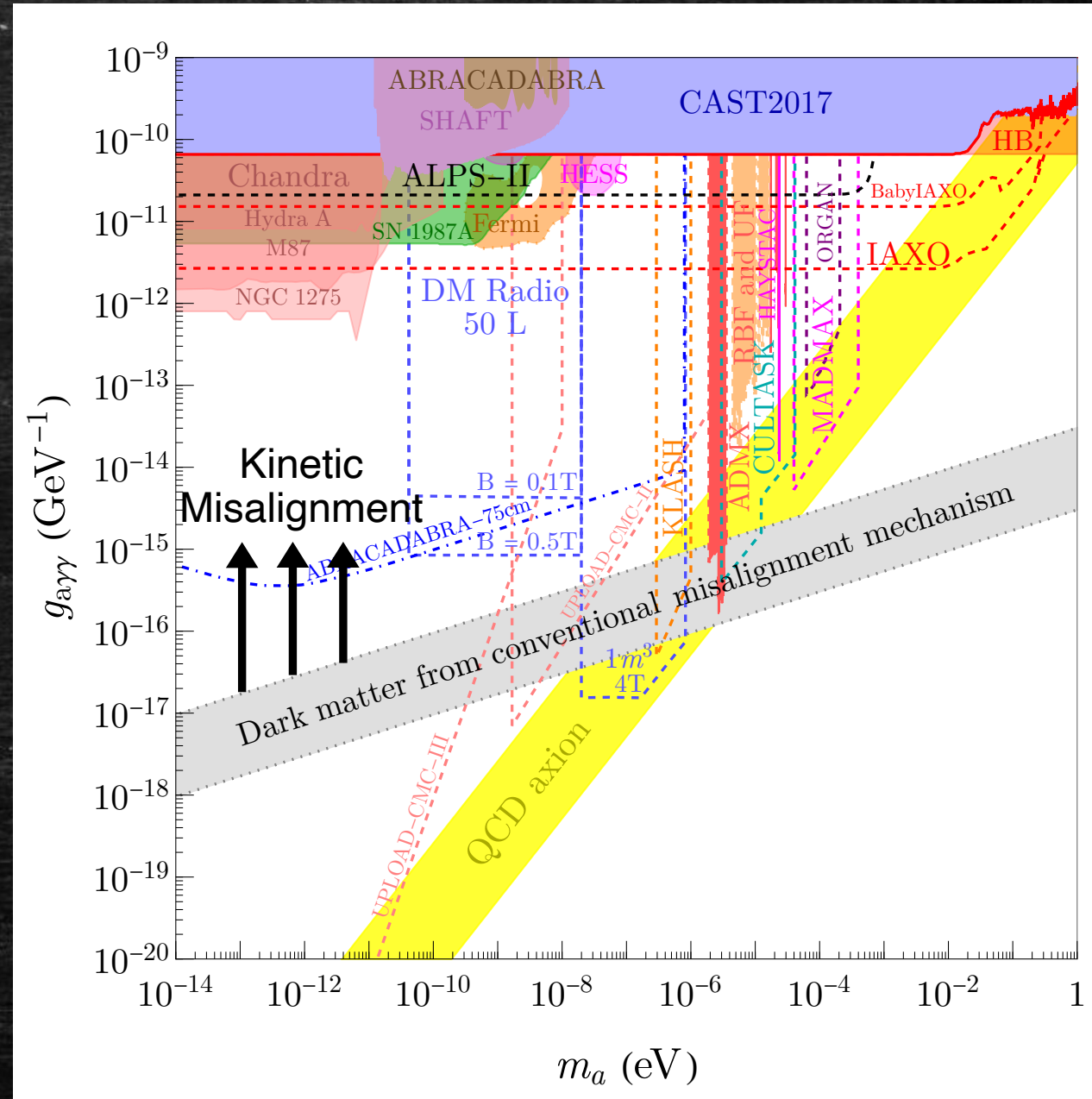
abundance

Observed dark matter abundance

$$\frac{\rho_{\text{DM}}}{s} \simeq 0.44 \text{ eV} \quad (\text{Planck 2018})$$

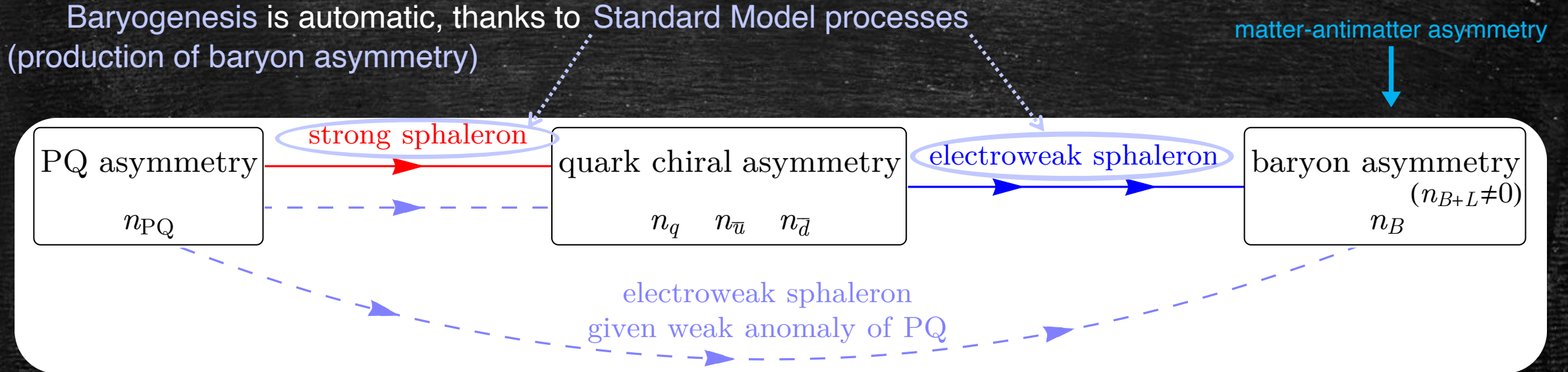
Thus, dark matter relates

$$m_a \overset{\text{DM}}{\longleftrightarrow} Y_\theta$$



# Baryon Asymmetry

# Axiogenesis



$$Y_B \equiv \frac{n_B}{s} = c_B Y_\theta \left( \frac{T_{\text{EW}}}{f_a} \right)^2$$

↑ produced by axion rotations

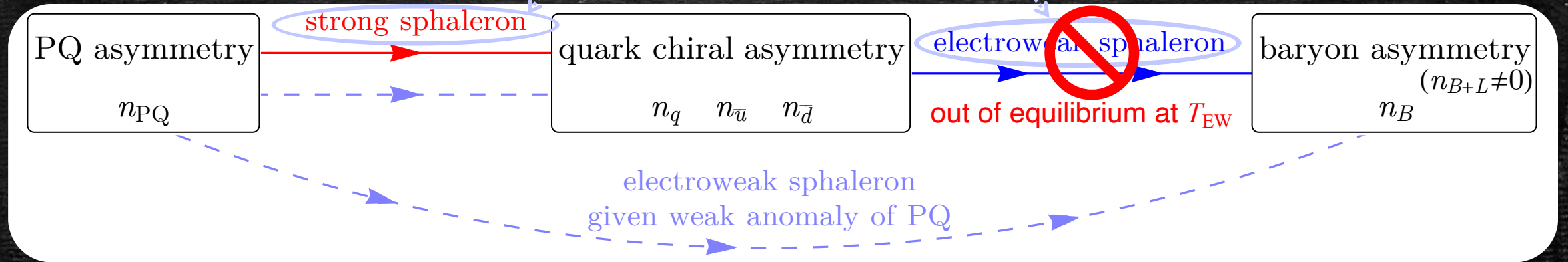
$$Y_B^{\text{obs}} \simeq 8.7 \times 10^{-11}$$

↑ experimentally measured value (Planck 2018)

# Axiogenesis

Baryogenesis is automatic, thanks to Standard Model processes  
(production of baryon asymmetry)

matter-antimatter asymmetry



$$Y_B \equiv \frac{n_B}{s} = c_B Y_\theta \left( \frac{T_{EW}}{f_a} \right)^2$$

$$Y_B^{\text{obs}} \simeq 8.7 \times 10^{-11}$$

experimentally measured value  
(Planck 2018)

Namely, the baryon asymmetry relates

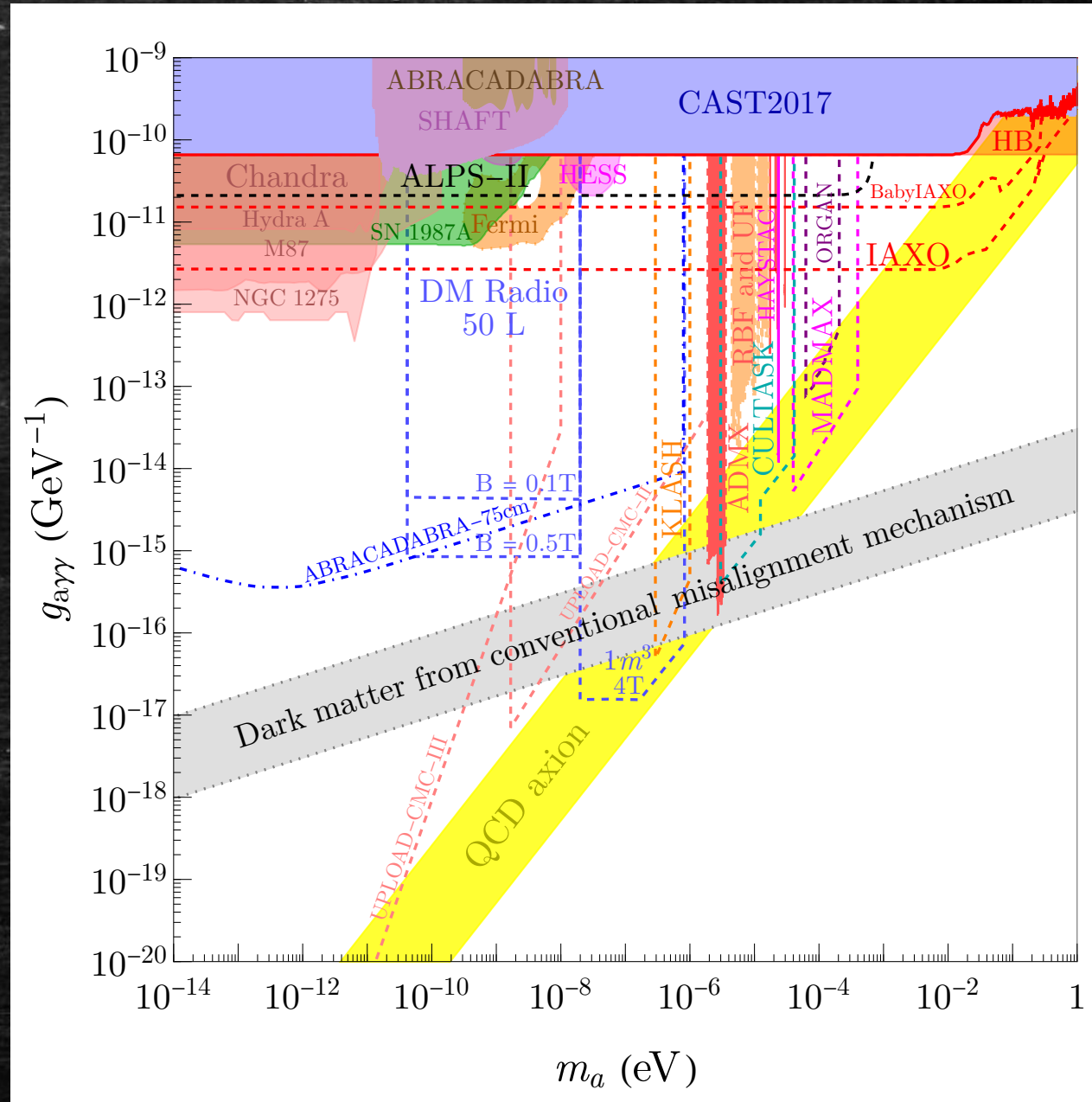
$$\left( \frac{T_{EW}}{f_a} \right)^2 \xleftrightarrow{Y_B} Y_\theta$$

# Axion/ALP Cogenesis

# Kinetic Misalignment + Axionogenesis

Prediction:

$$m_a \xleftrightarrow{\text{DM}} Y_\theta \xleftrightarrow{Y_B} \left( \frac{T_{\text{EW}}}{f_a} \right)^2$$





# Kinetic Misalignment + Axionogenesis

Prediction:

$$m_a \xleftrightarrow{\text{DM}} Y_\theta \xleftrightarrow{Y_B} \left( \frac{T_{\text{EW}}}{f_a} \right)^2$$

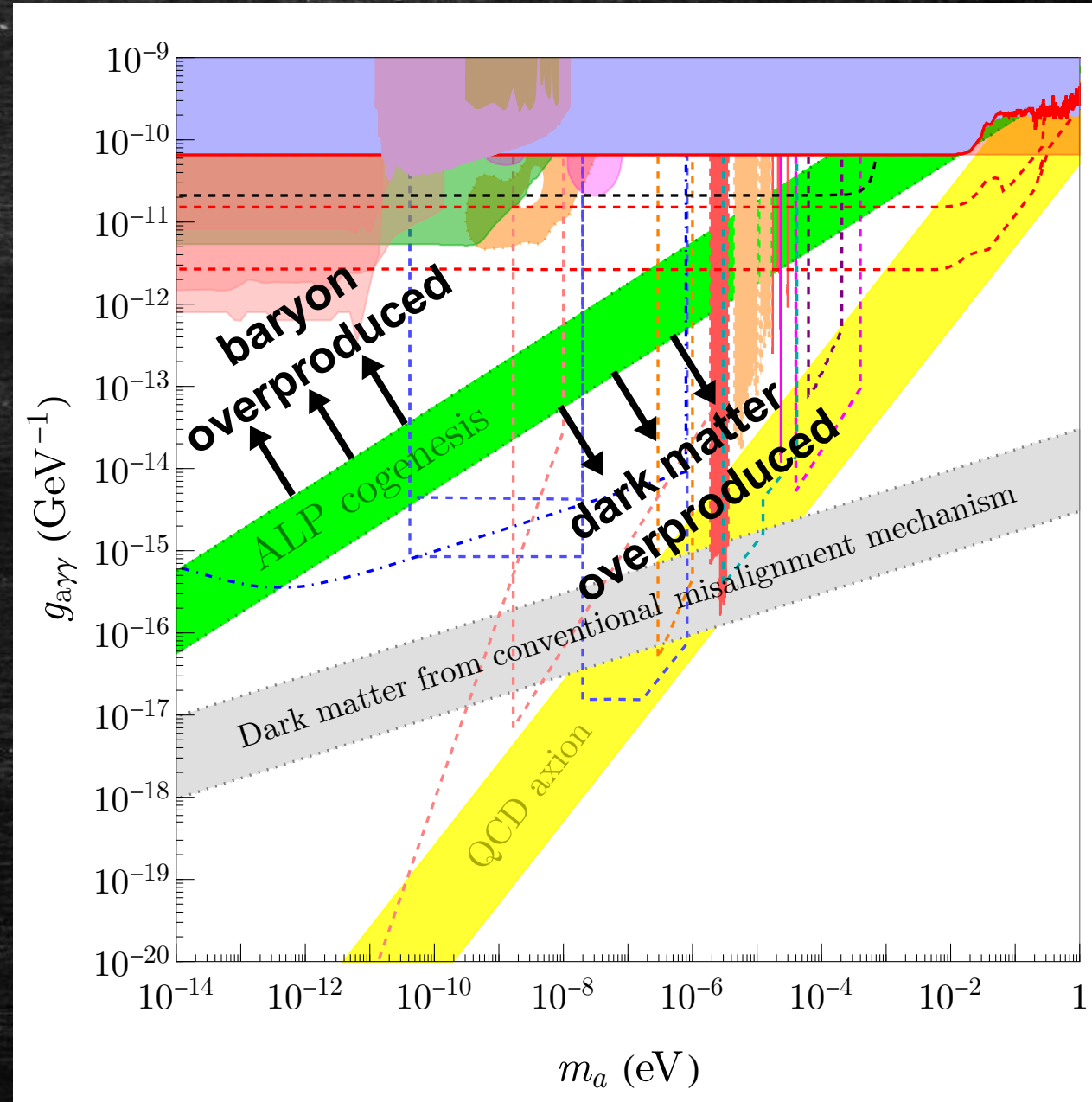
ALPogenesis :

ALP = axion-like particle  
(no gluon coupling)

cogenesis

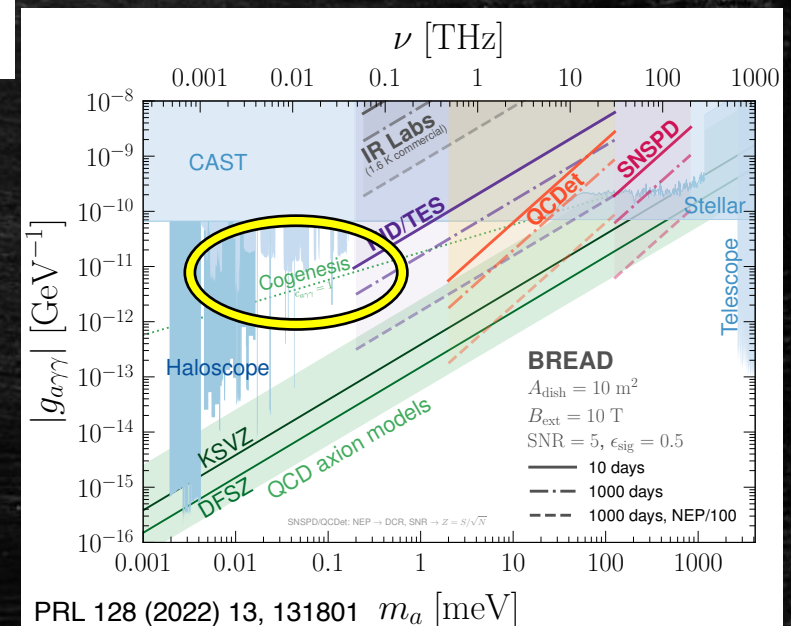
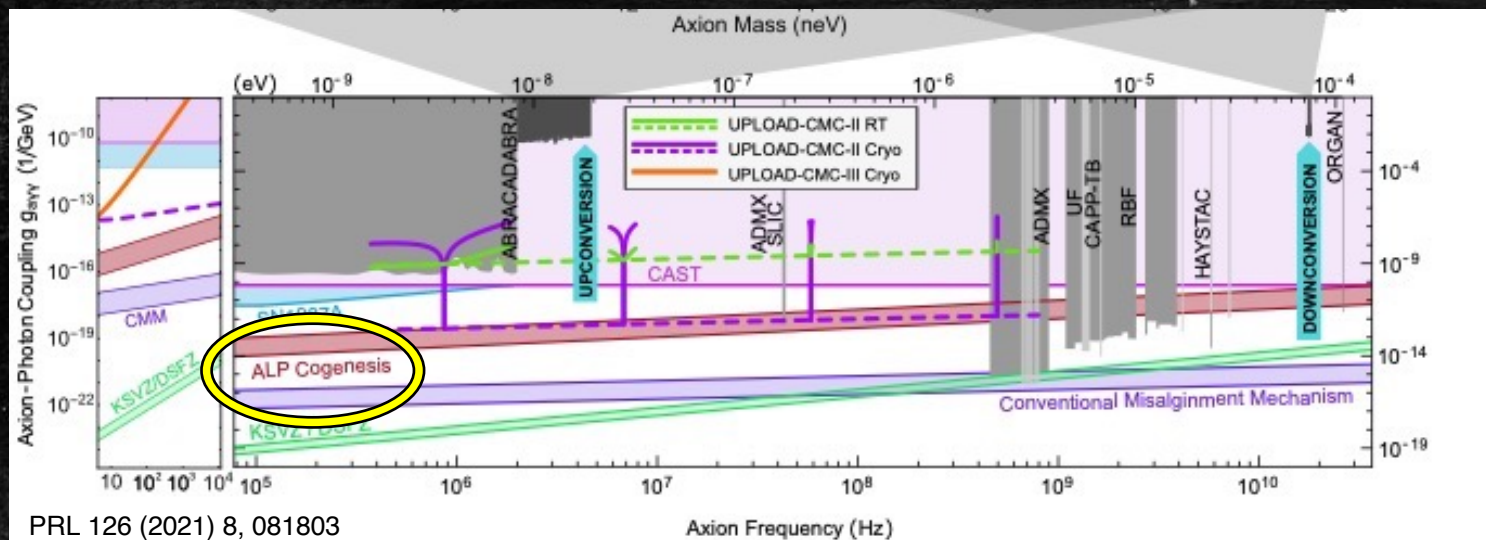
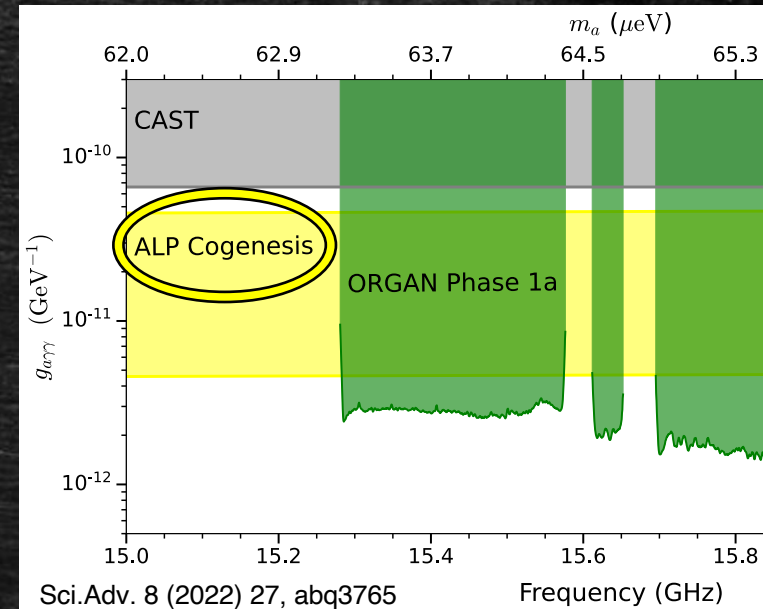
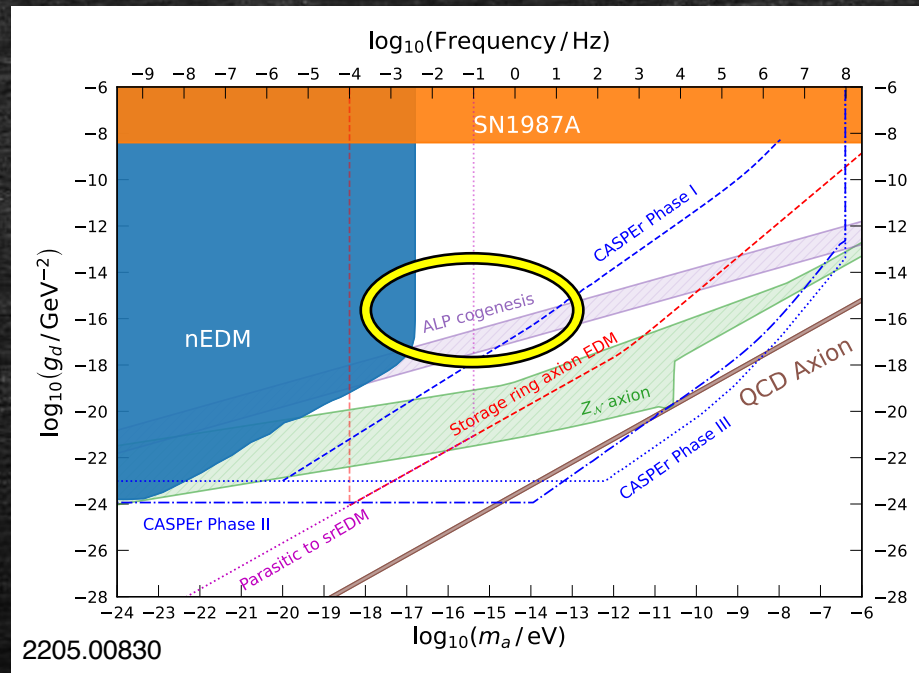
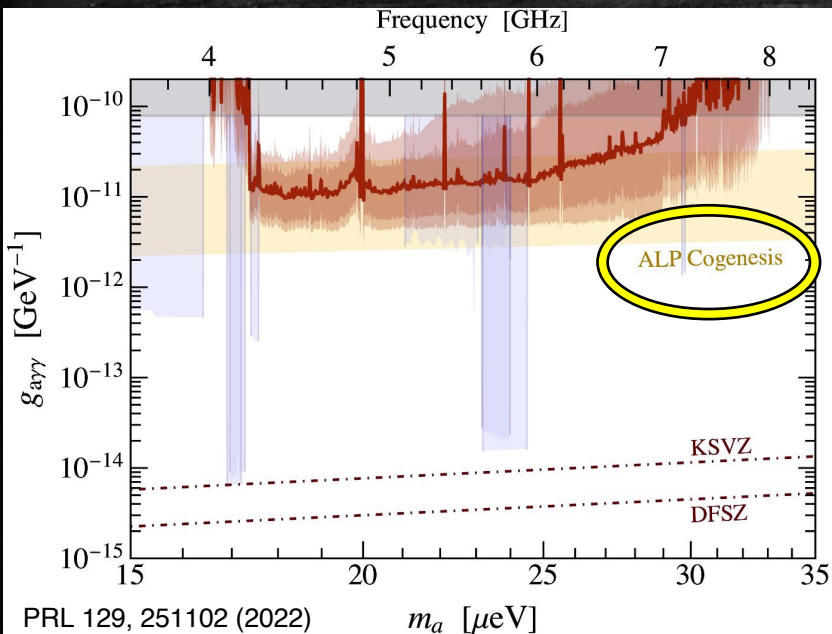
= production of both dark matter  
& matter-antimatter asymmetry

We assume  $T_{\text{EW}} = 130 \text{ GeV}$ .



# ALP Cogenesis

Experimental probes are happening!



# Kinetic Misalignment + Axionogenesis

Prediction:

$$m_a \xleftrightarrow{\text{DM}} Y_\theta \xleftrightarrow{Y_B} \left( \frac{T_{\text{EW}}}{f_a} \right)^2$$

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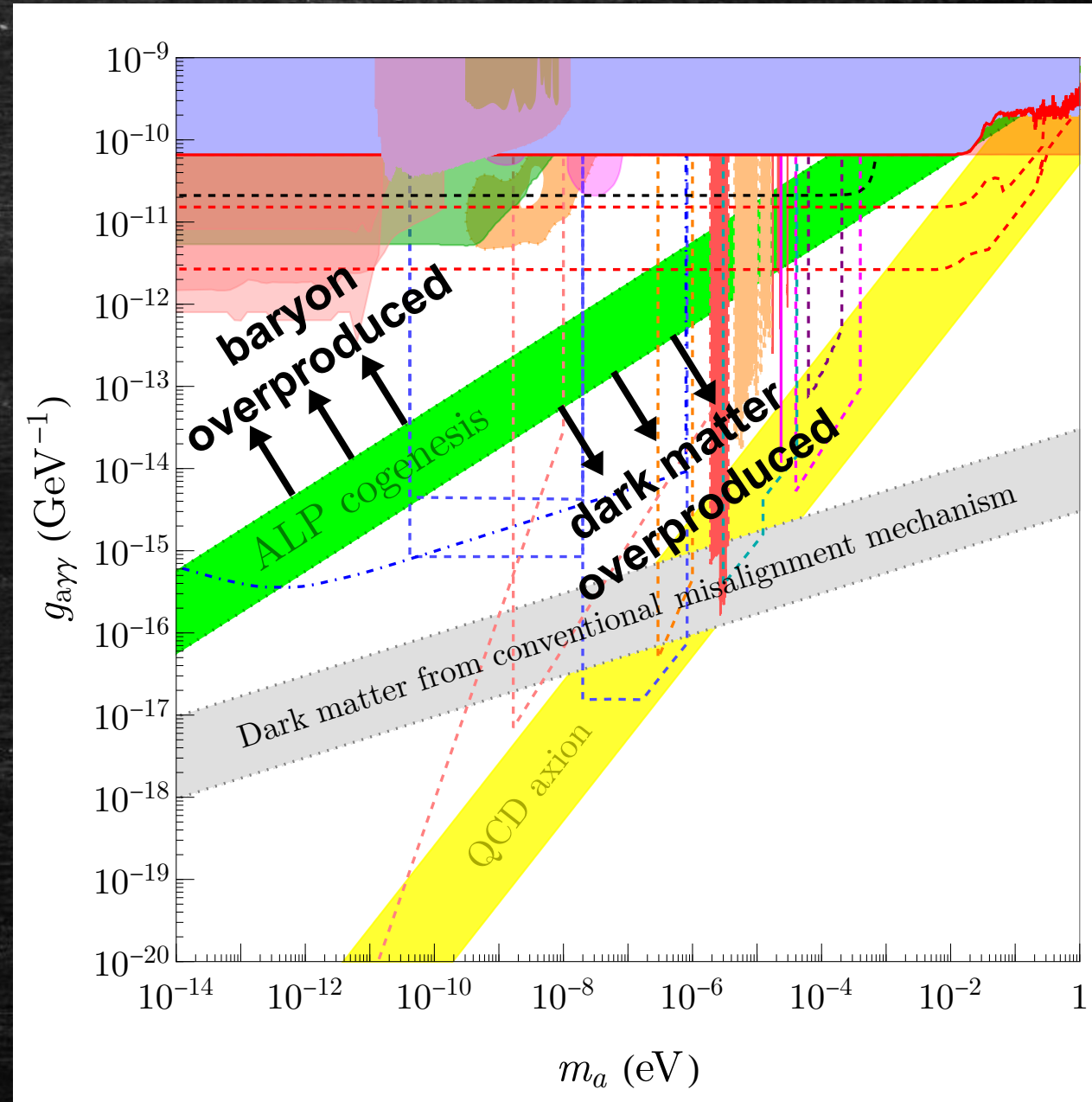
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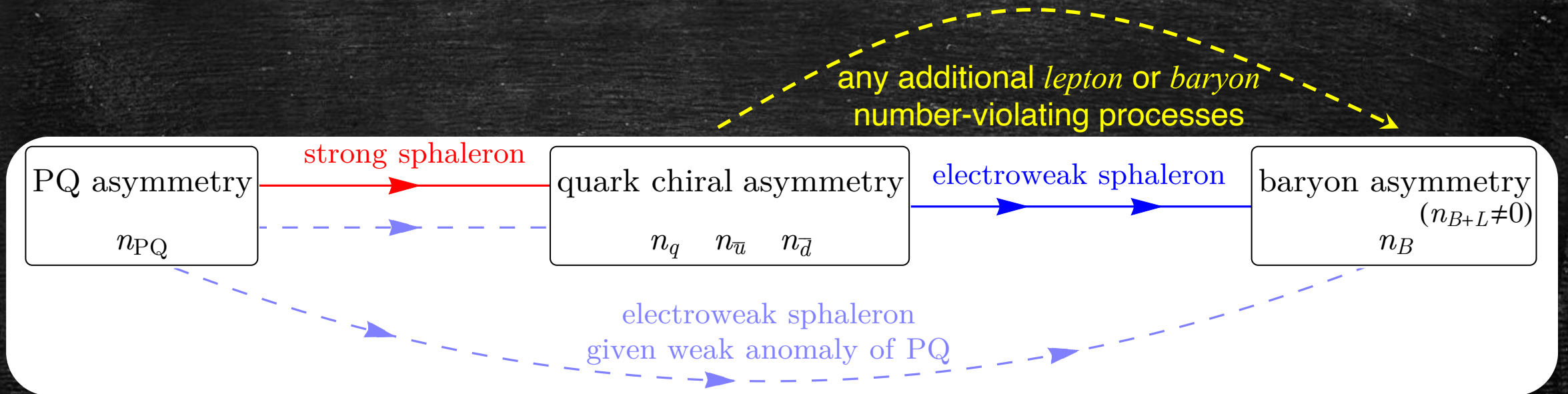
QCD axionogenesis?

Can the QCD axion be compatible  
with cogenesis from axion rotations?

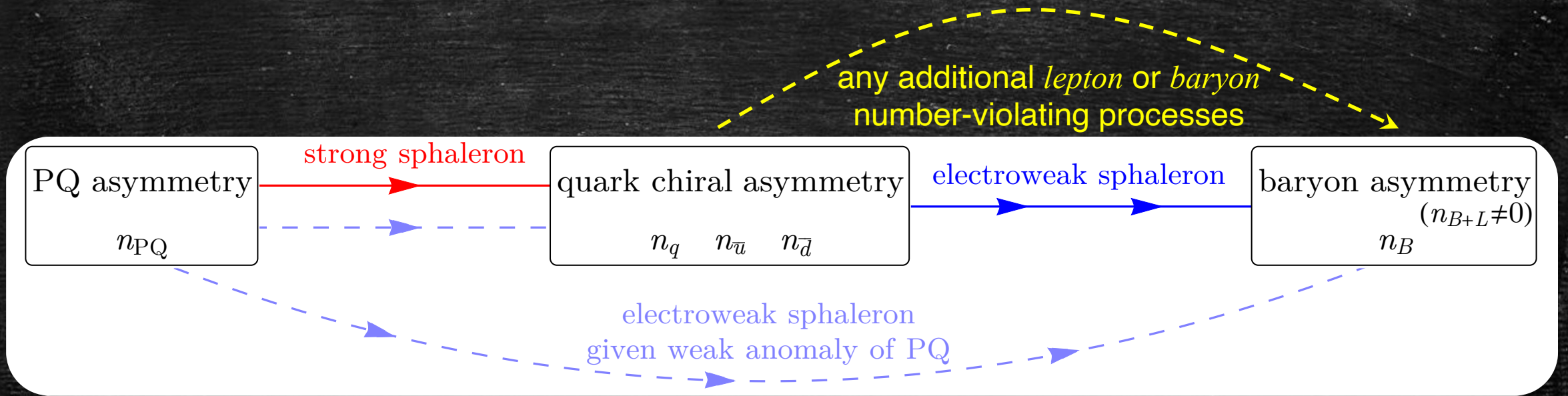
Yes. This is a great opportunity to bring  
other open questions into the picture!



# Extensions of Axiogenesis



# Extensions of Axiogenesis



## Lepto-Axiogenesis

$$\mathcal{L} \supset \frac{m_\nu}{2v_{EW}^2} \ell \ell H^\dagger H^\dagger$$

e.g., from the seesaw mechanism,  
or the Zee-Babu model

This Weinberg operator gives Majorana neutrino masses,  
breaks lepton number, and thus affects the charge transfer.

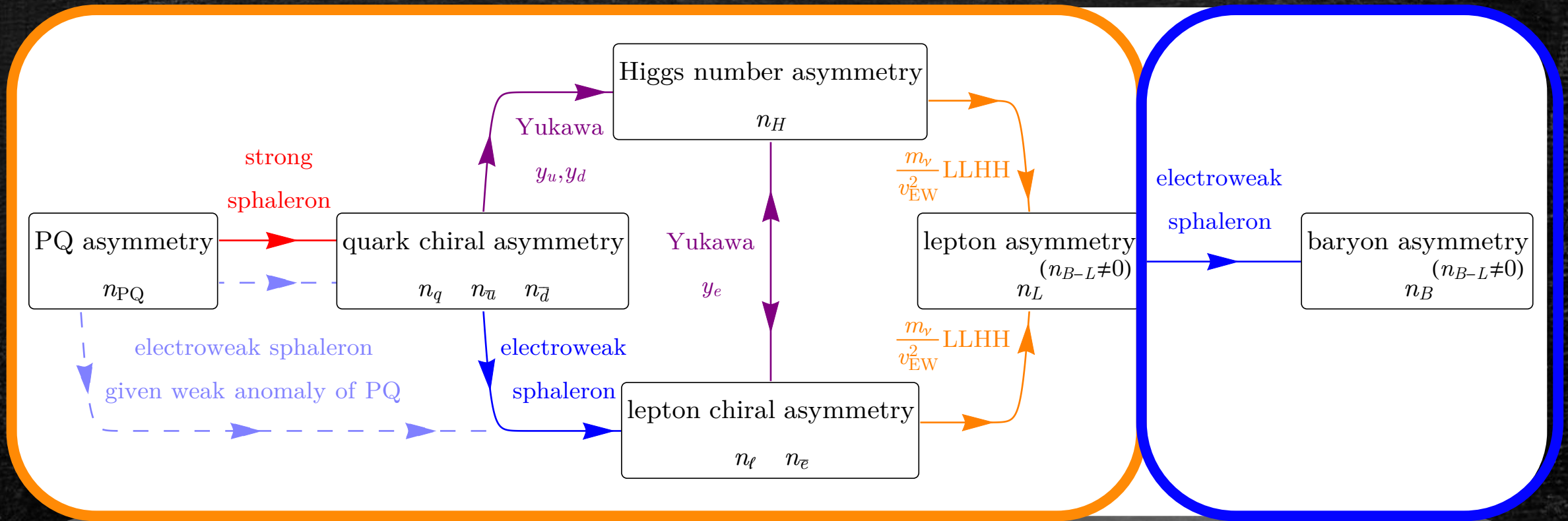
## other extensions

- ✓ RC *et al.* 1910.02080
- ✓ Harigaya *et al.* 2107.09679
- ✓ Chakraborty *et al.* 2108.04293
- ✓ Kawamura *et al.* 2109.08605
- ✓ RC *et al.* 2110.05487
- ✓ RC *et al.* 2206.00678
- ✓ Barnes, RC *et al.* 2208.07878
- ✓ RC *et al.* 2211.12517

# Lepto-Axiogenesis

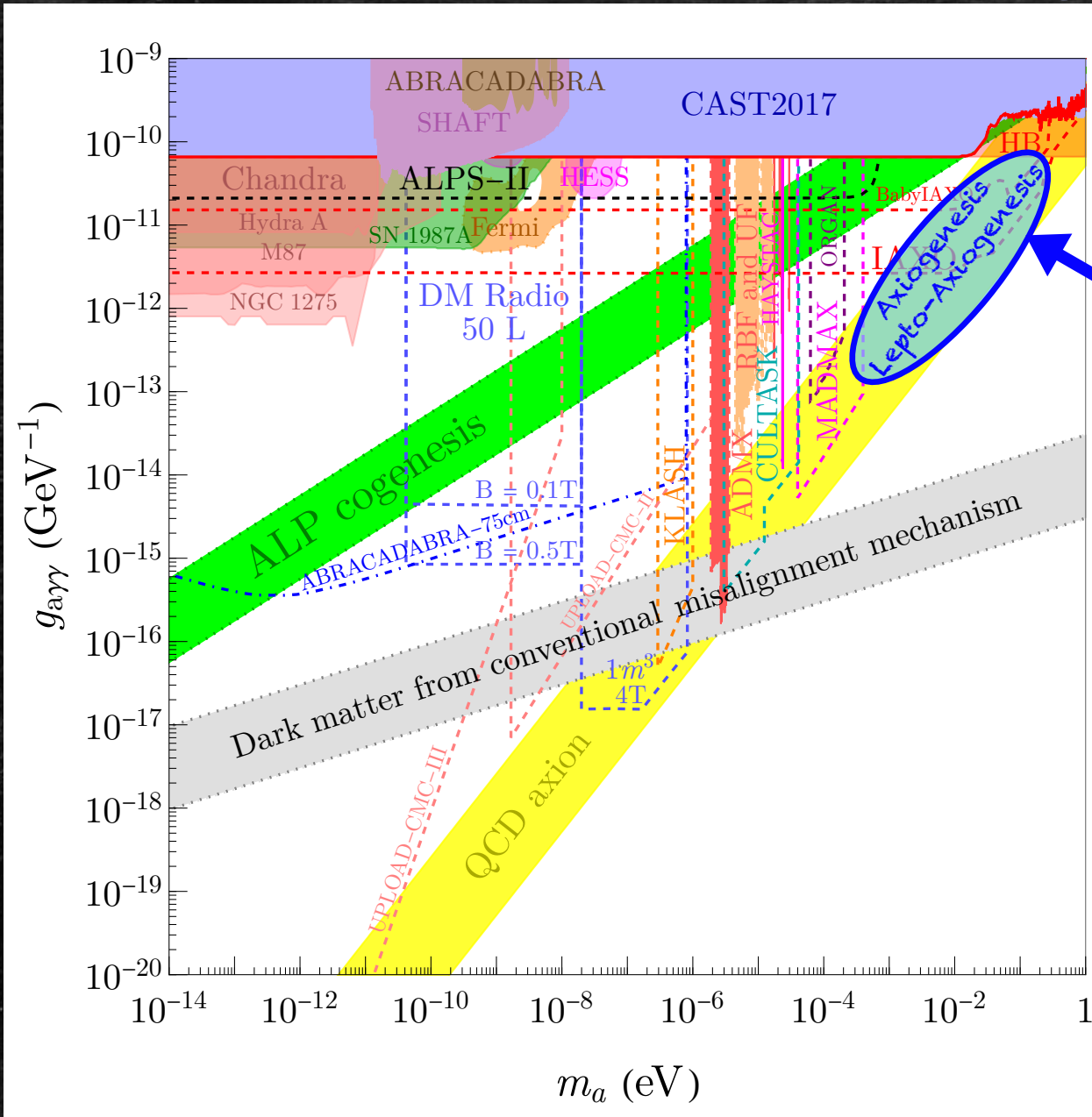
Producing  $L$  at high temperatures

Converting to  $B$  at  $T_{EW}$



$\int d^4x$

# Lepto-Axiogenesis



Lepto-Axiogenesis achievement:

- simultaneous production of
- dark matter
  - matter-antimatter asymmetry
- in the framework with
- QCD axion
  - Majorana neutrinos

# Baryogenesis from Decaying Magnetic Helicity in Axiogenesis

tachyonic instability

M. S. Turner and L. M. Widrow  
PRD 37 (1997) 2743

axion-photon coupling

chiral plasma instability

M. Joyce, M. E. Shaposhnikov  
PRL 79 (1997)

chiral magnetic field

$h$

decaying magnetic helicity

K. Kamada and A. J. Long  
PRD 94 no. 6, (2016)

PQ asymmetry

$n_{\text{PQ}}$

strong sphaleron

quark chiral asymmetry

$n_q$   $n_{\bar{u}}$   $n_{\bar{d}}$

electroweak sphaleron

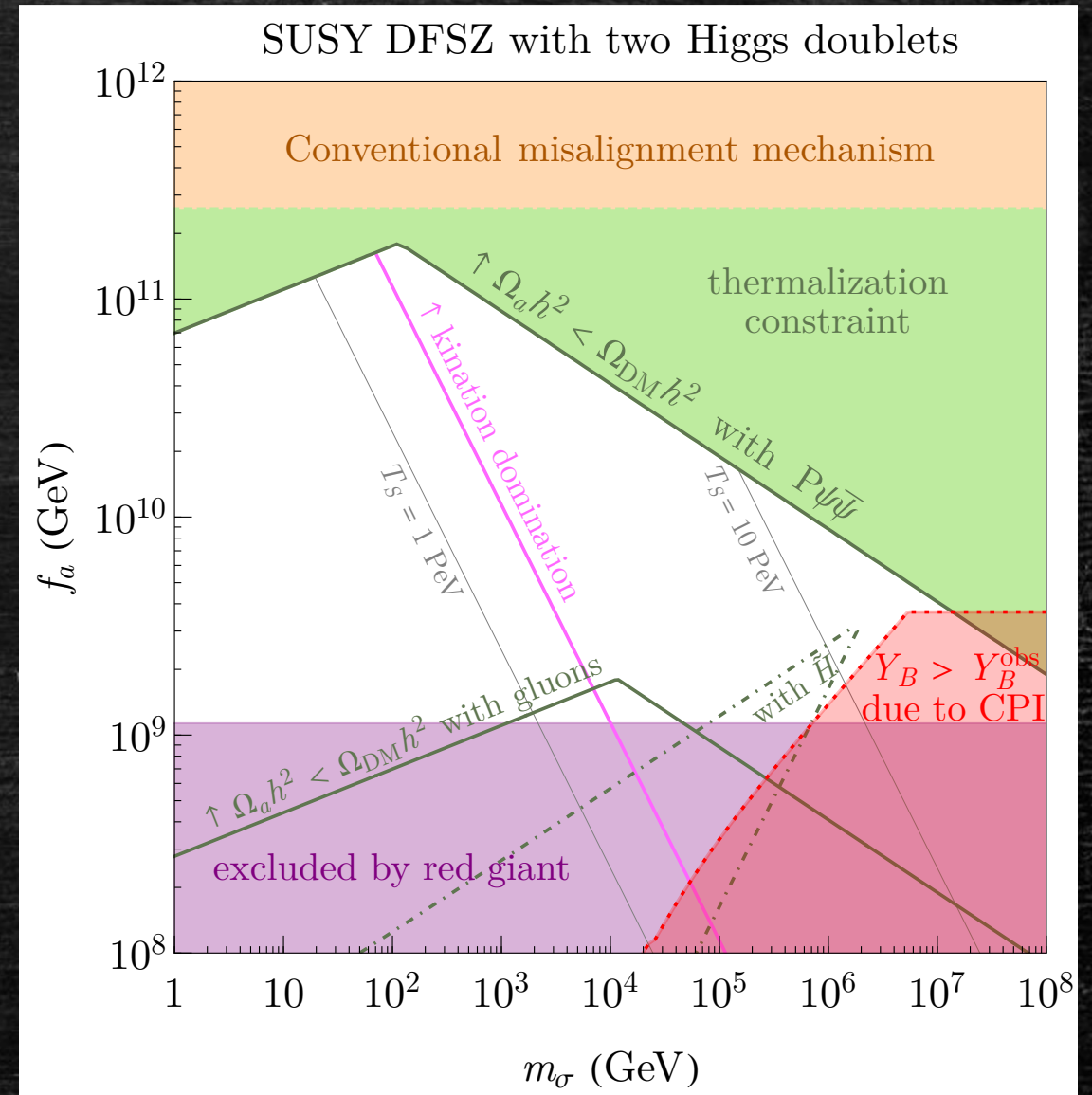
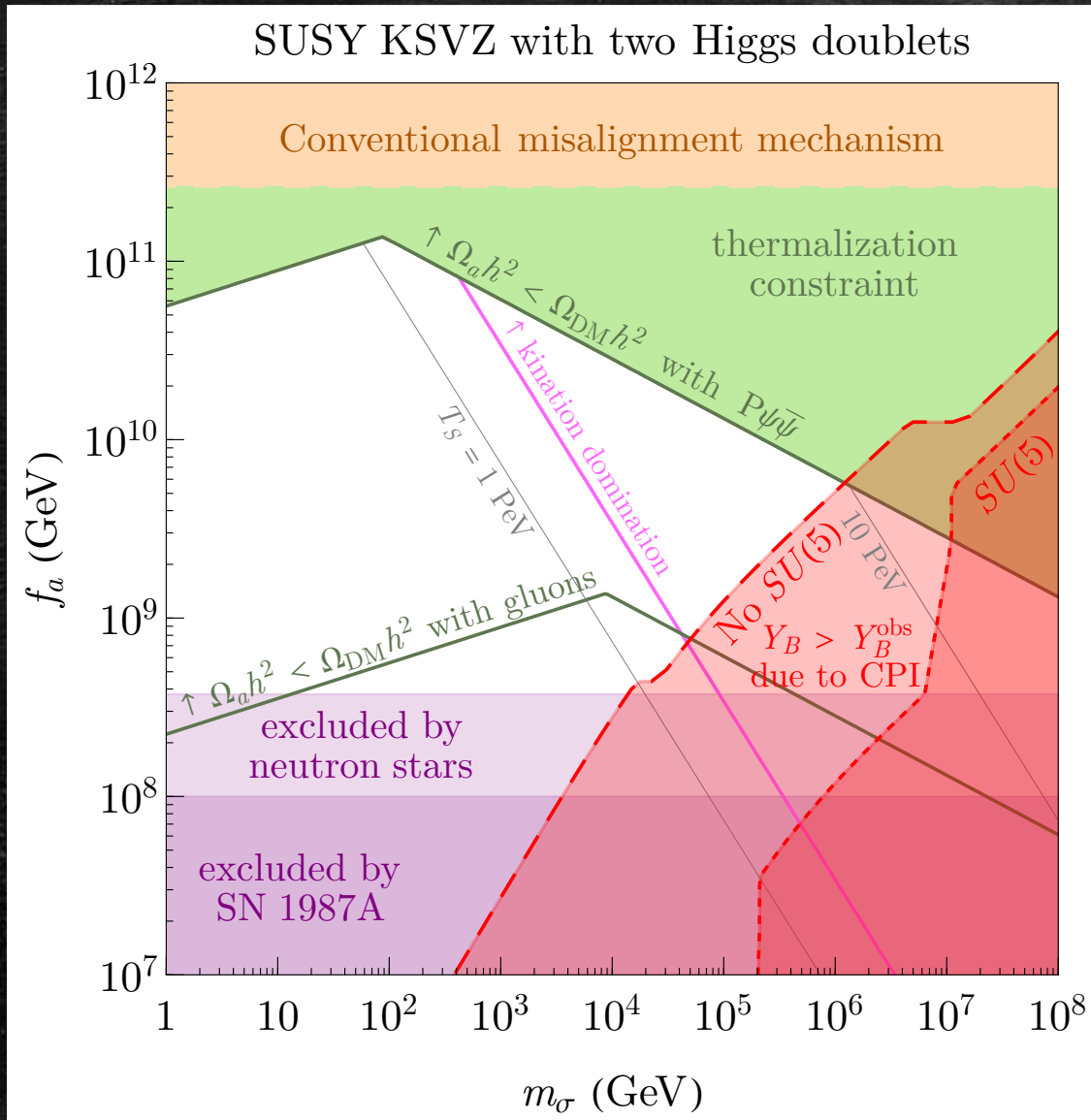
baryon asymmetry

$(n_{B+L} \neq 0)$   
 $n_B$

electroweak sphaleron  
given weak anomaly of PQ



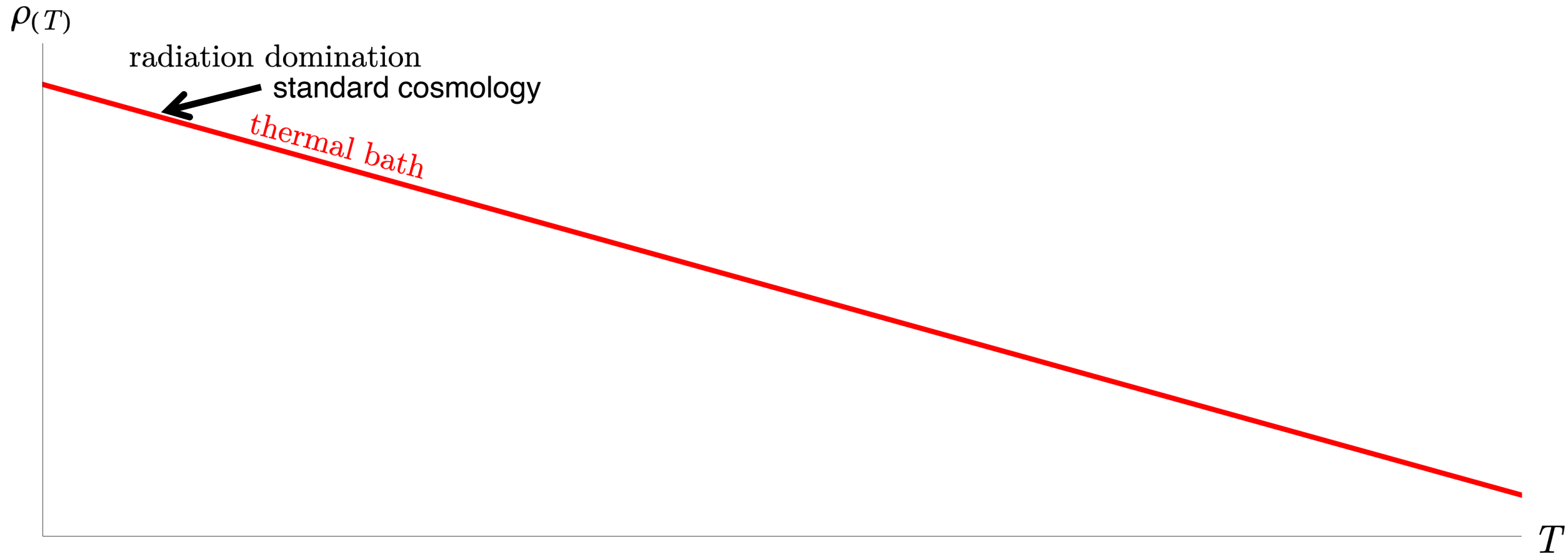
# Baryogenesis from Decaying Magnetic Helicity in Axionogenesis



# Gravitational Wave Signatures

# Evolution of Energy Densities

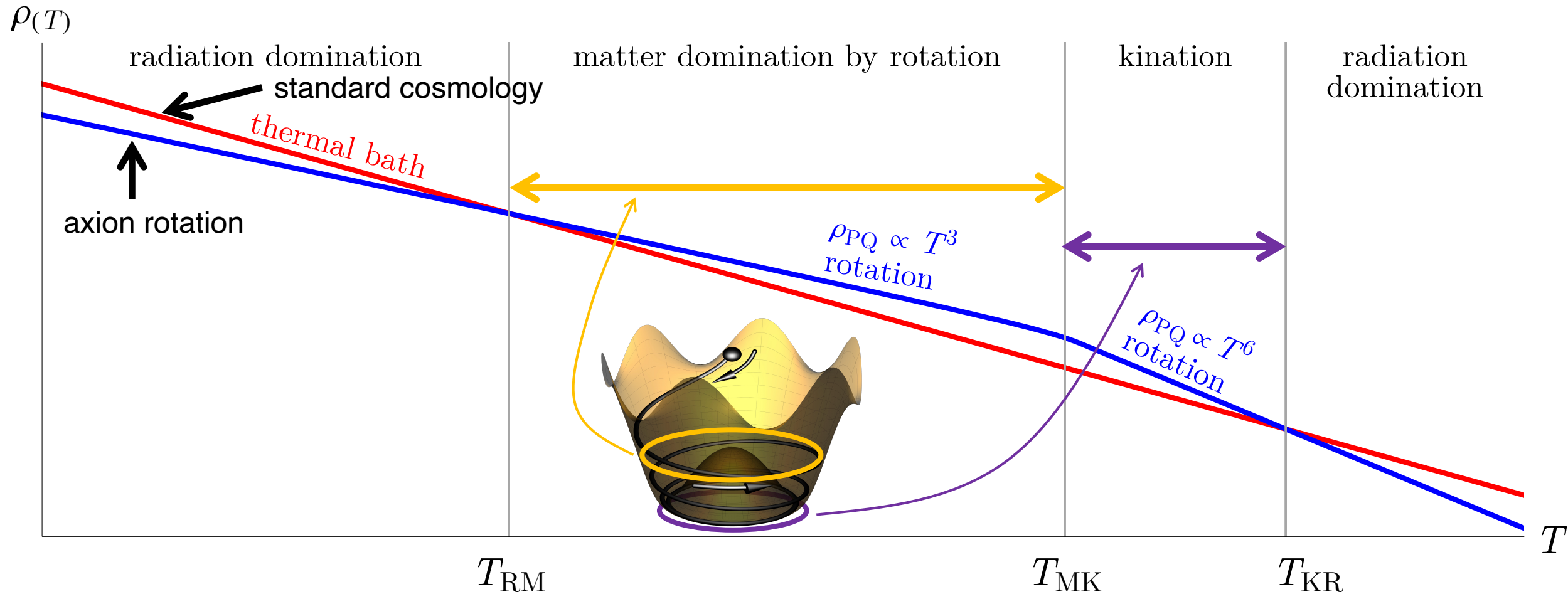
The **energy content** determines the universe's **expansion rate**.



Over time, the universe cools and temperature drops.

# Evolution of Energy Densities

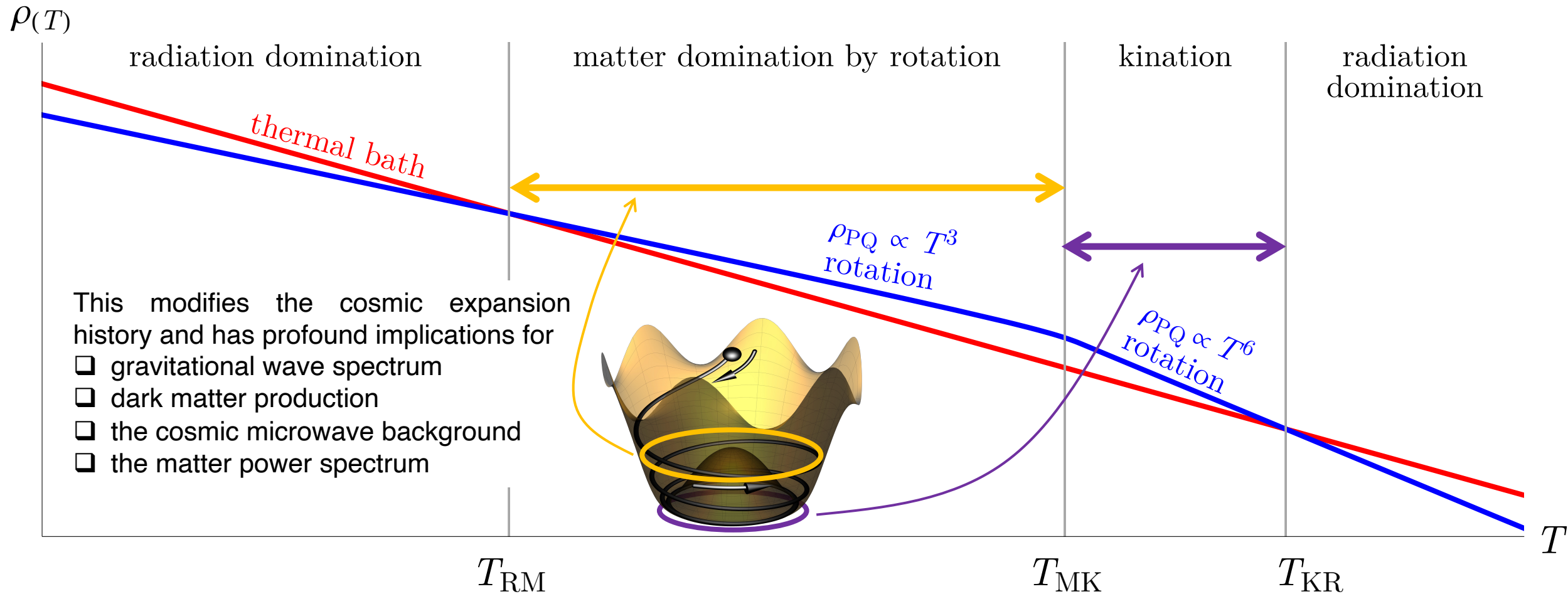
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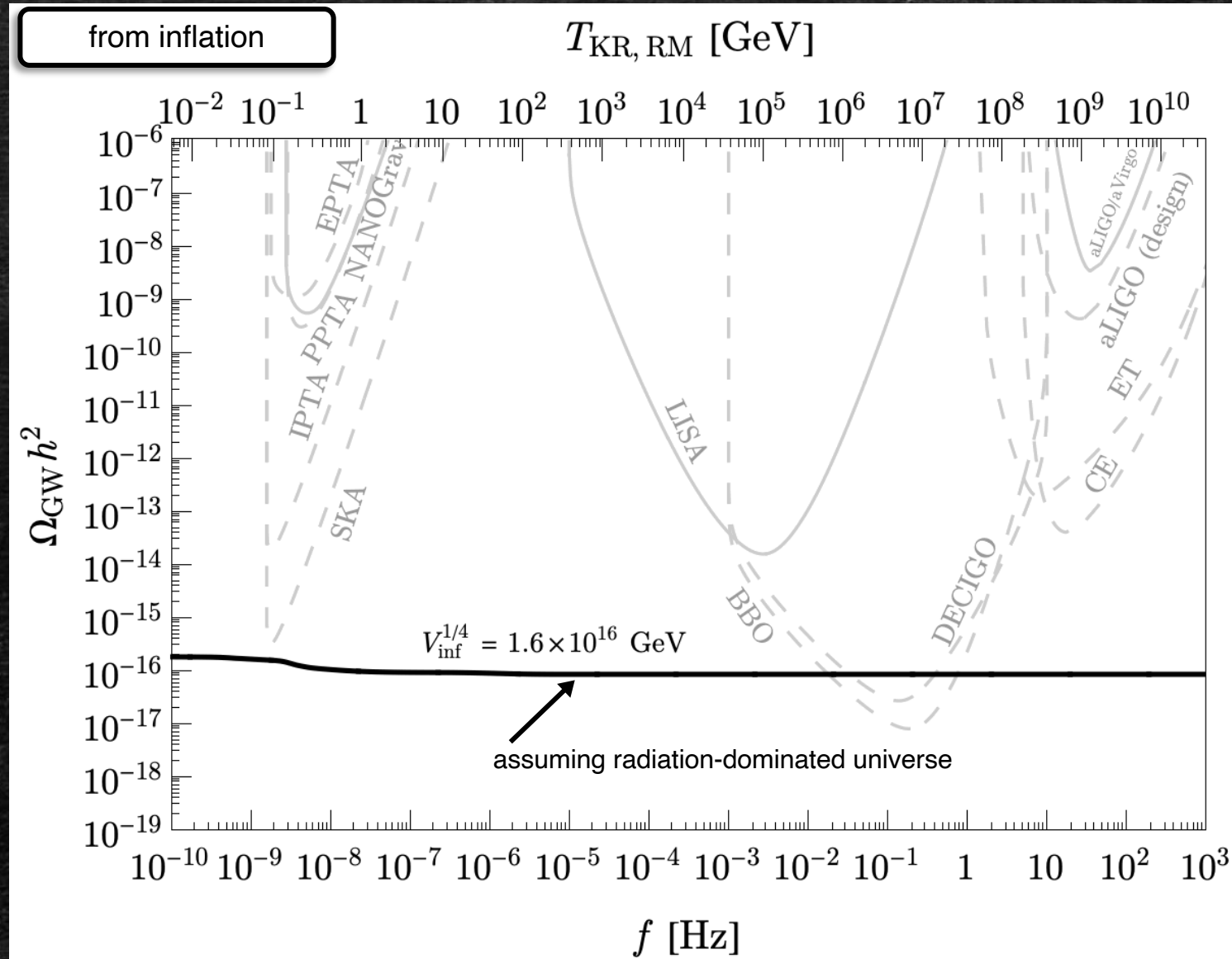
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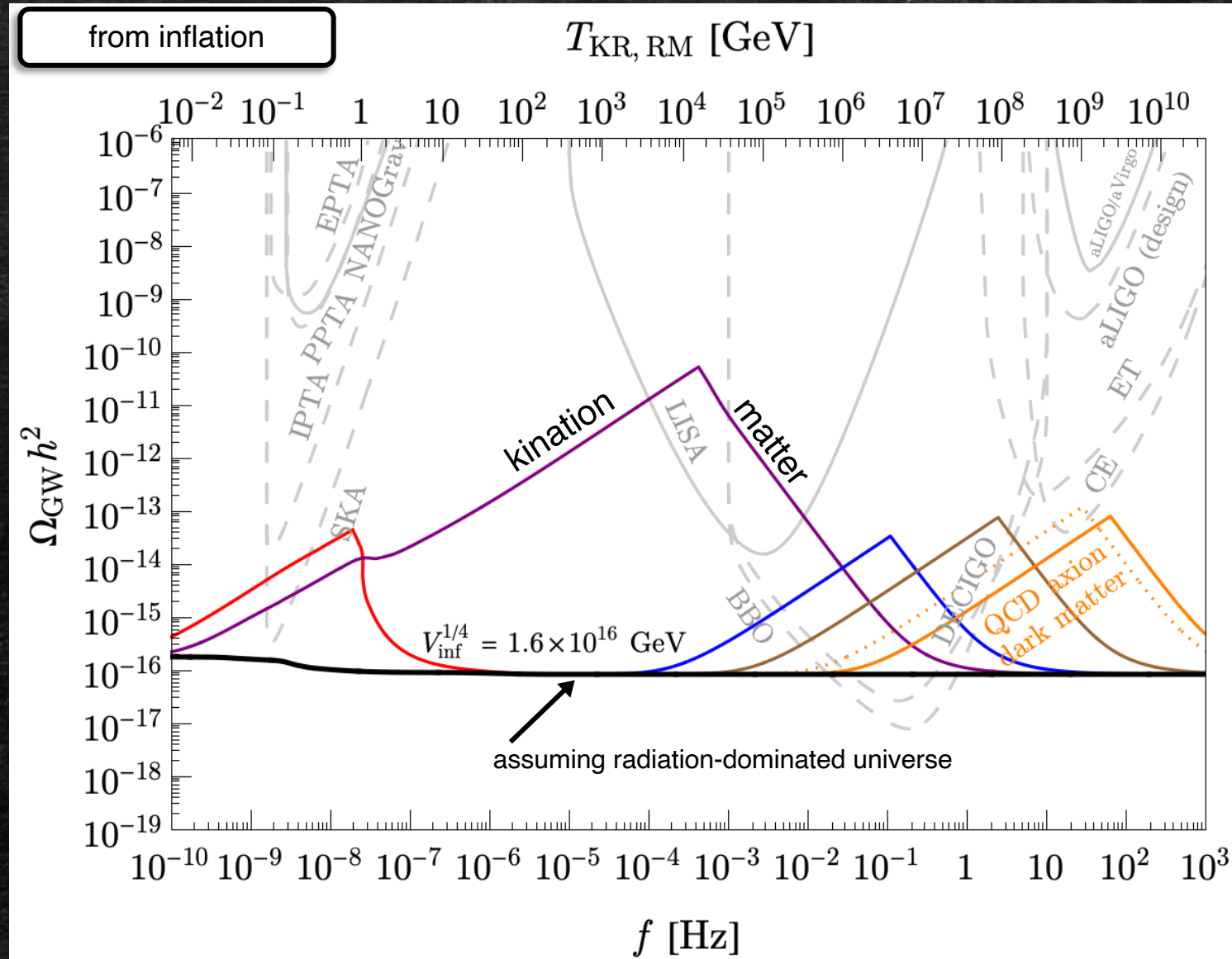
# Smoking Gun: Triangular Peak in Gravitational Wave Spectra



2108.09299 JHEP 09 (2022) 116 RC, D. Dunsky, N. Fernandez, A. Ghalsasi, L. Hall, K. Harigaya, J. Shelton

2108.10328, 2111.01150 Y. Gouttenoire, G. Servant, P. Simakachorn

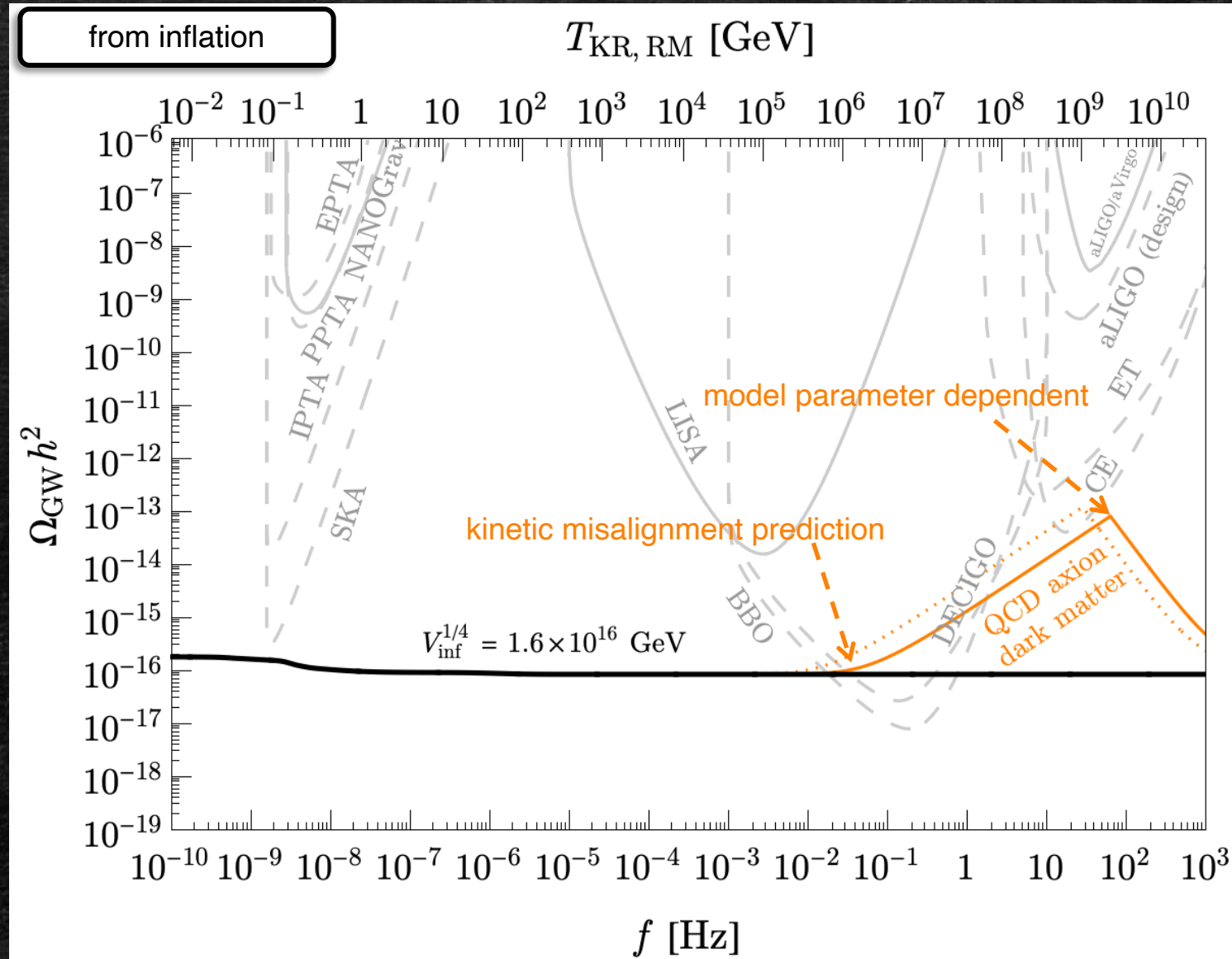
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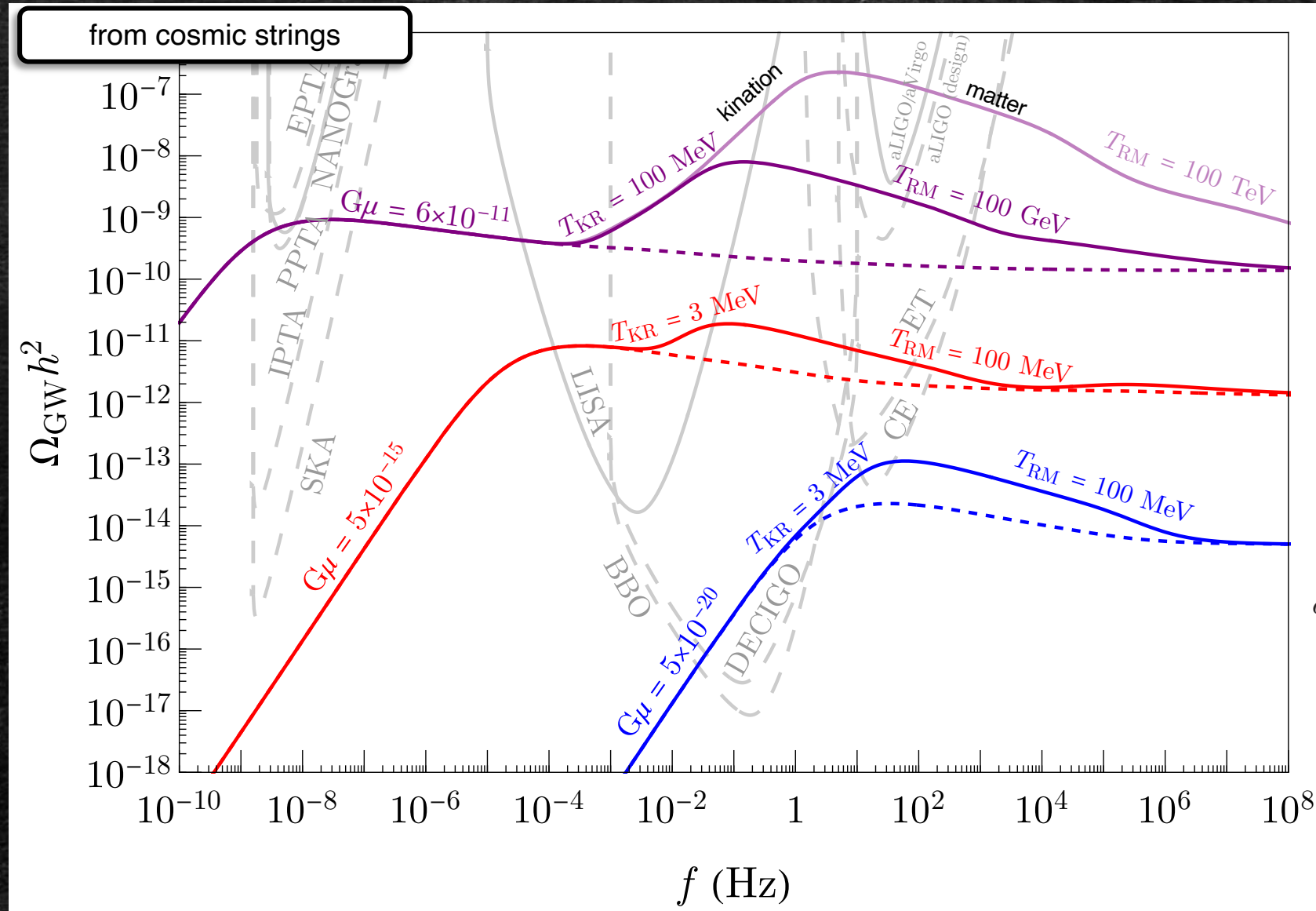


2108.09299 JHEP 09 (2022) 116 RC, D. Dunsky, N. Fernandez, A. Ghalsasi, L. Hall, K. Harigaya, J. Shelton

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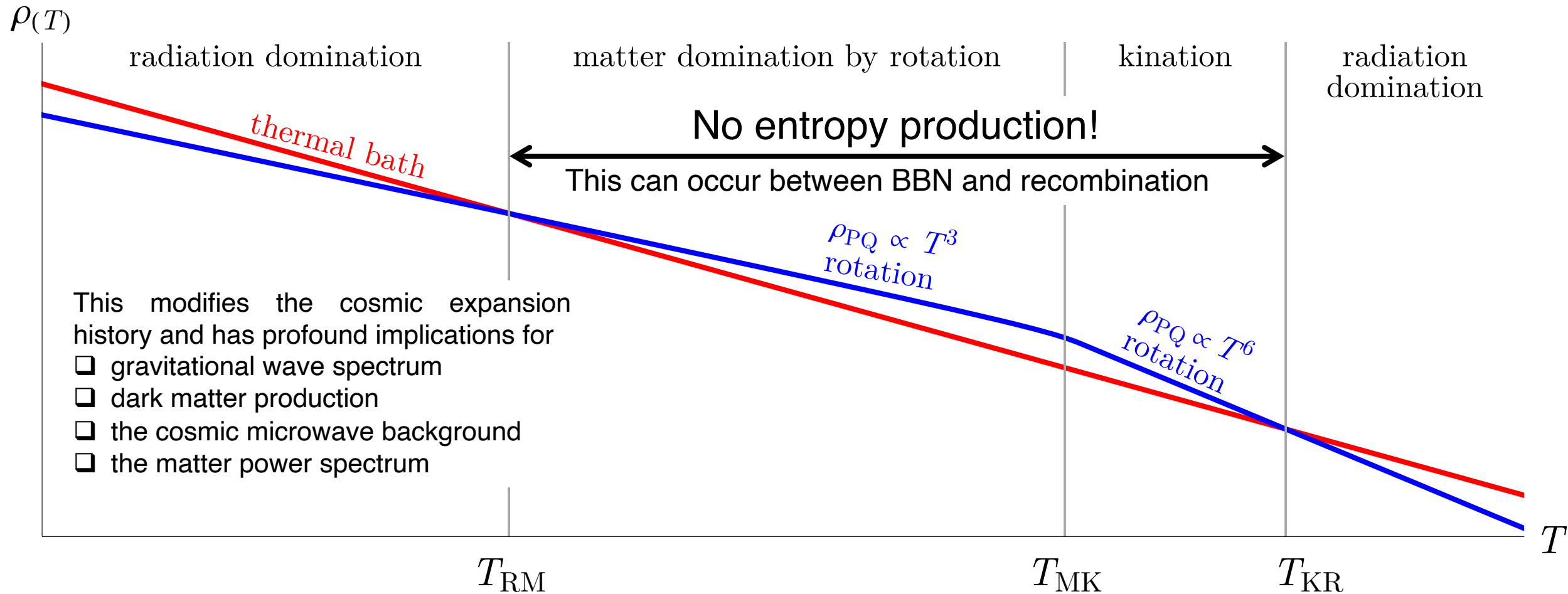


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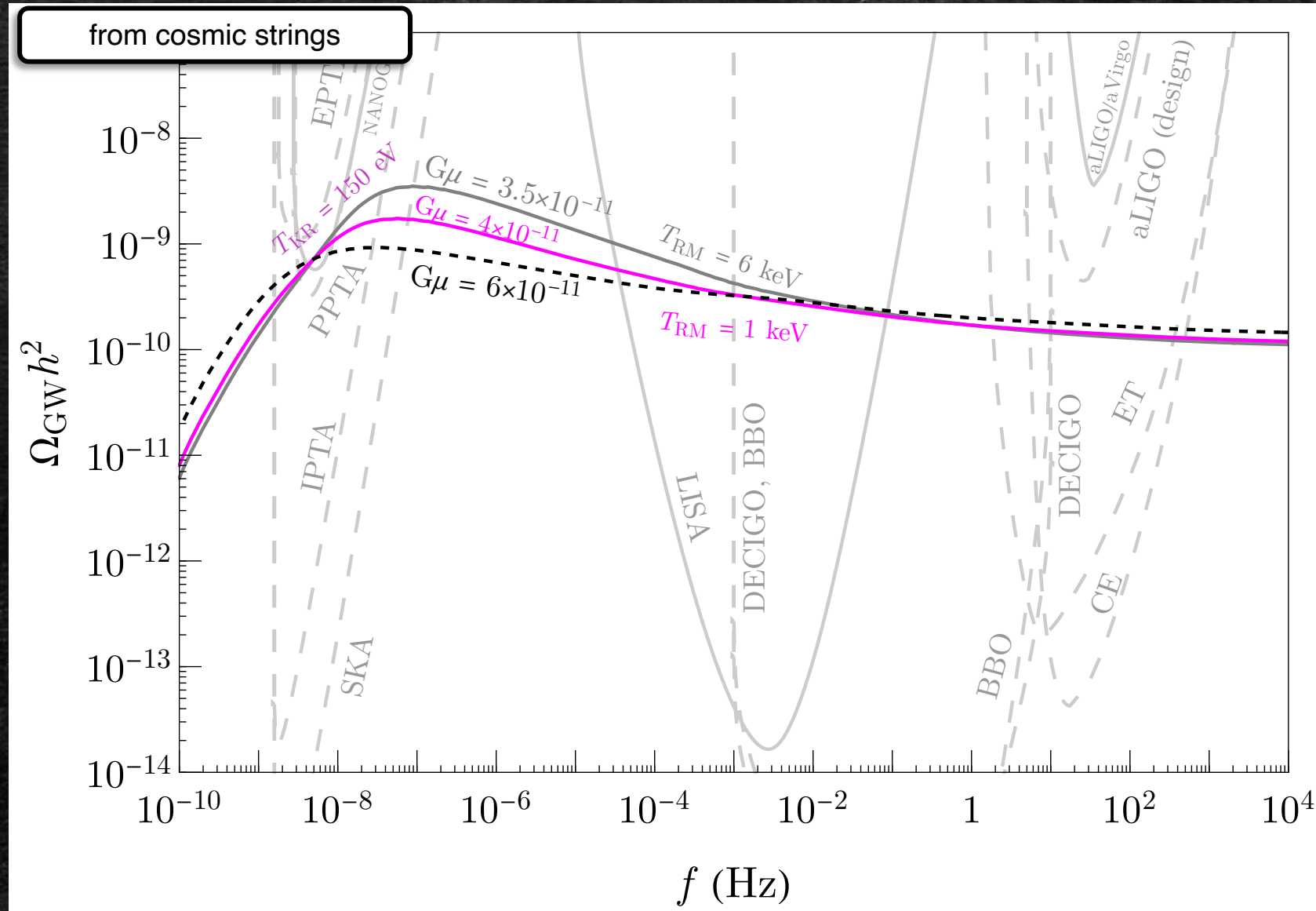
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# Probing PQ-breaking Potential

Piecewise approximation

$$\rho_\theta \propto \begin{cases} R^{-3} & \text{for } S \gg f_a \text{ i.e. } T \gg T_{\text{MK}} \\ R^{-6} & \text{for } S \simeq f_a \text{ i.e. } T \ll T_{\text{MK}} \end{cases}$$

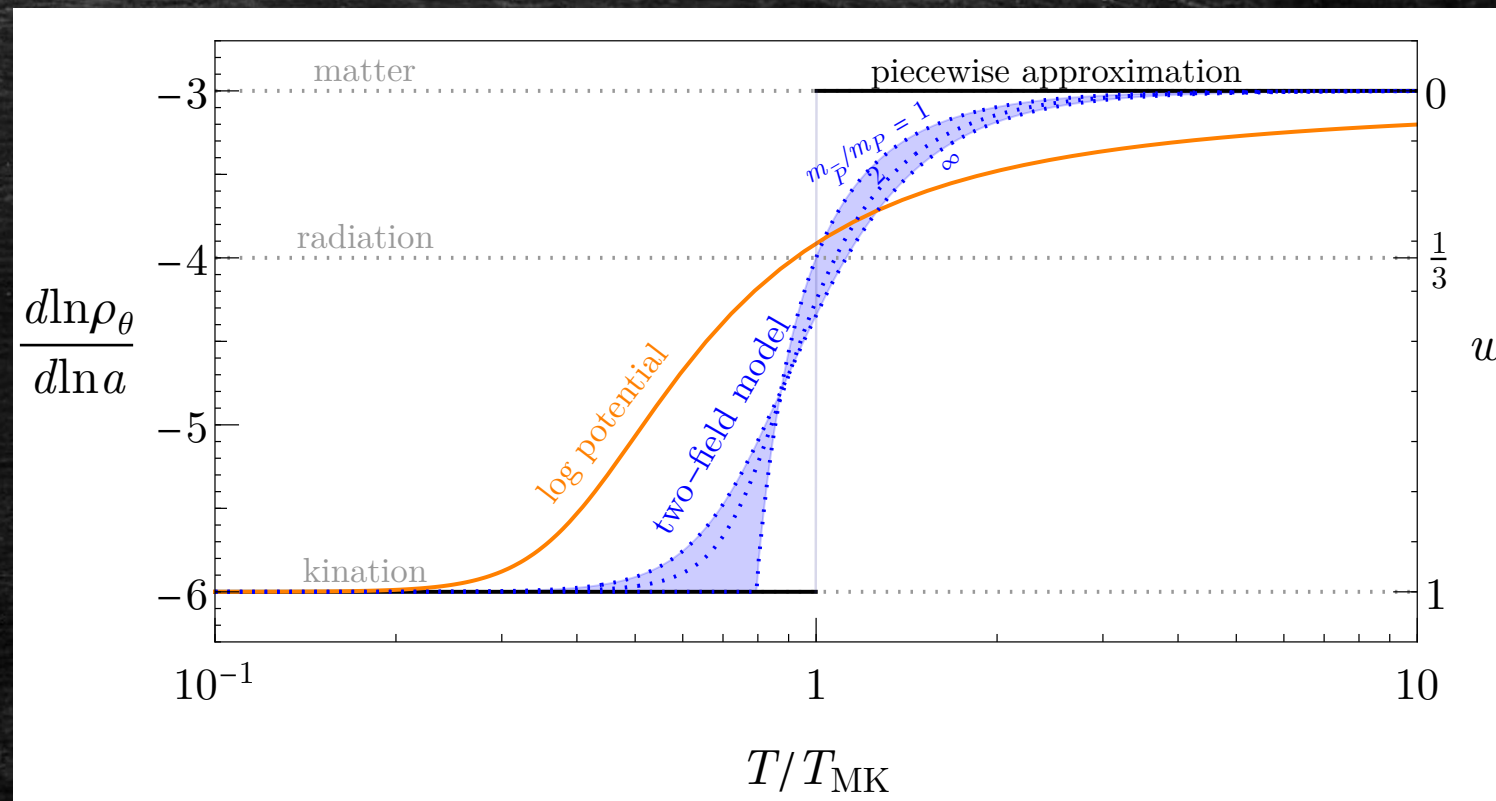
log potential

$$V(P) = m_S^2 |P|^2 \left( \ln \frac{2|P|^2}{f_a^2} - 1 \right)$$

Two-field model

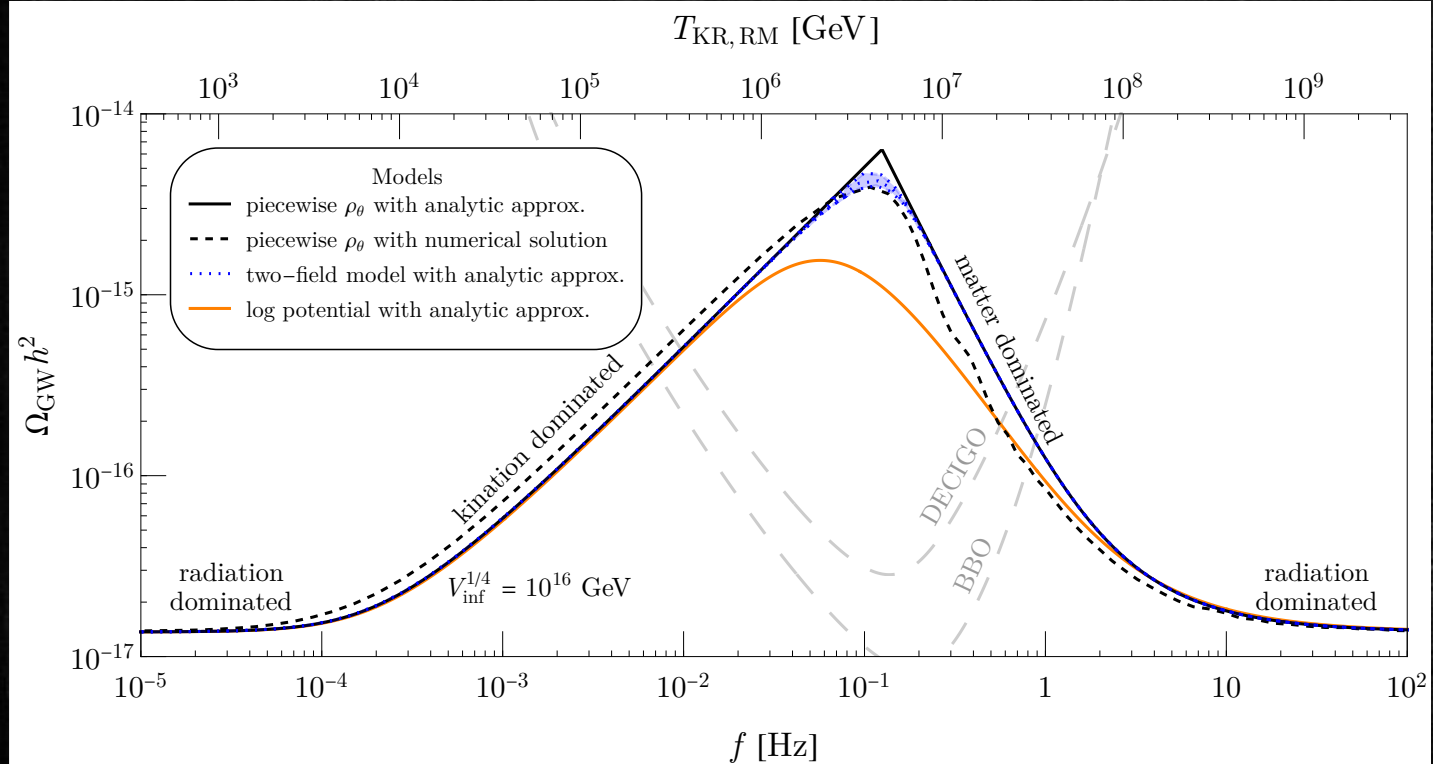
$$W = X(P\bar{P} - v_P^2)$$

$$V_{\text{soft}} = m_P^2 |P|^2 + m_{\bar{P}}^2 |\bar{P}|^2$$

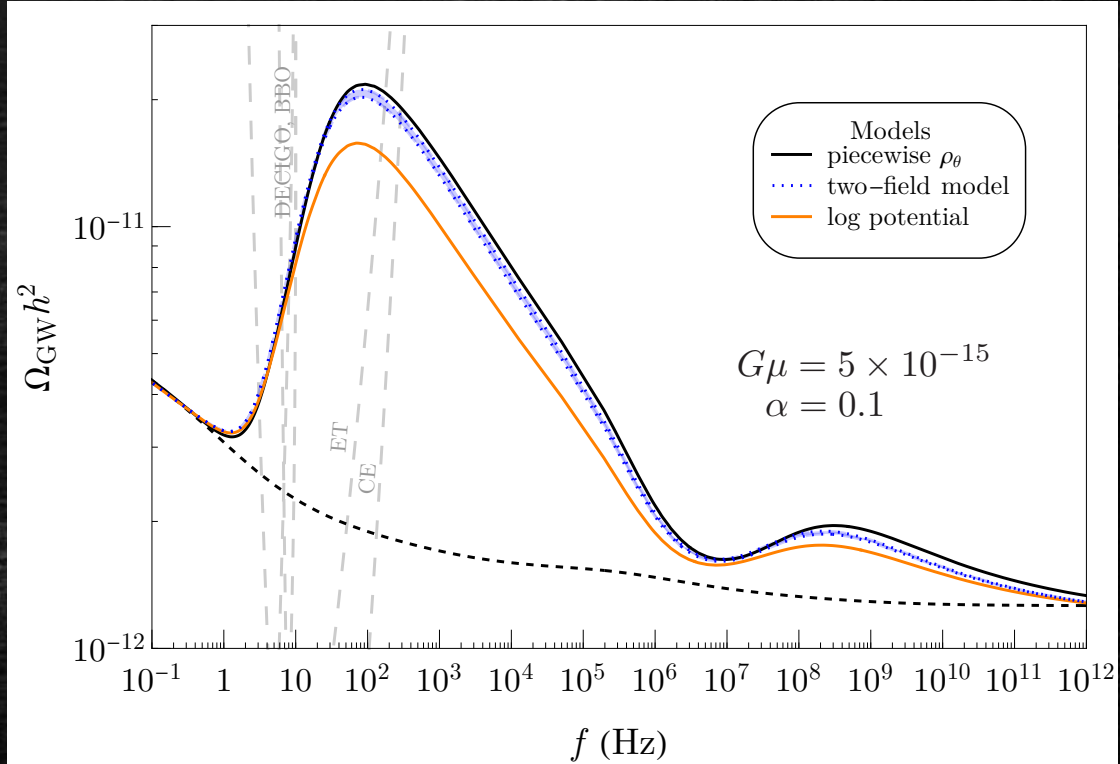


# Probing PQ-breaking Potential

from inflation



from cosmic strings



# Axion Rotations

## Axion Kination

- ✓ *RC et al.* 2108.09299
- ✓ *Gouttenoire et al.* 2108.10328
- ✓ *Gouttenoire et al.* 2111.01150

## Dark Matter

- ✓ *RC et al.* 1910.14152
- ✓ *Chang et al.* 1911.11885
- ✓ *RC et al.* 2004.00629
- ✓ *Di Luzio et al.* 2102.01082
- ✓ *Rusov et al.* 2109.01833
- ✓ *Barman et al.* 2111.03677
- ✓ *Eröncel et al.* 2206.14259
- ✓ *Eröncel et al.* 2207.10111
- ✓ *Oikonomou* 2208.05544
- ✓ *Kozów et al.* 2212.03518
- ✓ *Chatrchyan et al.* 2305.03756
- ✓ *Lee et al.* 2310.17710

## Baryogenesis

- ✓ *RC et al.* 1910.02080
- ✓ *RC et al.* 2006.04809
- ✓ *Domcke et al.* 2006.03148
- ✓ *RC et al.* 2006.05687
- ✓ *Harigaya et al.* 2107.09679
- ✓ *Chakraborty et al.* 2108.04293
- ✓ *Kawamura et al.* 2109.08605
- ✓ *RC et al.* 2110.05487
- ✓ *RC et al.* 2206.00678
- ✓ *Barnes, RC et al.* 2208.07878
- ✓ *RC et al.* 2211.12517
- ✓ *Berbig* 2307.14121
- ✓ *Chao et al.* 2311.06469
- ✓ *Chun et al.* 2311.09005

## Gravitational Waves

- ✓ *RC et al.* 2104.02077
- ✓ *Madge et al.* 2111.12730
- ✓ *Harigaya et al.* 2305.14242

## Cosmic Perturbations

- ✓ *RC et al.* 2202.01785

# Conclusions

- ✓ **New axion dynamics** allows the QCD axion to simultaneously explain
  - ✓ Strong CP problem
  - ✓ dark matter abundance
  - ✓ baryon asymmetry
- ✓ This paradigm predicts **exciting phenomenology**
  - ✓ specific axion mass-coupling relations
  - ✓ axion kination: unique gravitational wave spectra
- ✓ Other possible signatures include
  - ✓ gravitational lensing of axion mini-clusters
  - ✓ enhanced matter power spectrum
  - ✓ warm axion dark matter
  - ✓ Majorana neutrinos
- ✓ New model building opportunities
  - ✓ **other open questions** across disciplines

