

# Fitting the exotic hadron spectrum with an additional quark

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# The Hypothesis:

A seventh quark exists

charge:  $-1/3$

mass:  $\sim 2.8 \text{ GeV}$

The  $W$  boson connects this quark with the right-chiral component of the charm quark.

Right-chiral connection leads to  $Z$  being FCNC

arxiv:2203.03007

# Topics

- Mapping exotic hadrons to mesons and baryons
  - Reproducing observed production and decay of exotic hadrons
  - Predictions testable by LHCb (and other experiments)
- Addressing experiments that rule out an additional quark
- W & Z interactions of the additional quark
- Cancelling gauge anomalies
- Theory motivation: broken supersymmetry,  $3u+6d \rightarrow 3u+4d$

Additional slides...

- More predictions ... and possible additional evidence
- Alternative non-SM explanations for a few experiments



Mapping exotic hadrons to mesons and baryons

# Properties of the quark:

charge:  $-1/3$

mass:  $\sim 2.8 \text{ GeV}$

Given the symbol: "f"

Decays used in the mapping:

$$f \rightarrow c + W, \quad |V_{cf}| \sim 1, \quad \tau_f \sim 0.01 \tau_b$$

$$b \rightarrow f + Z, \quad |V_{bf}^Z| \sim 0.03, \quad |V_{bc}| \sim 0.04$$

$$Z \rightarrow d\bar{s} \quad Z \rightarrow d\bar{f} \quad Z \rightarrow s\bar{f}$$

and Hermitian conjugate decays

# Exotic hadrons mapped to mesons and baryons

Proposed  $f$ -quark Mesons and Baryons

Name	QM	Quarks
$X^{\pm,0}(3250)$	$1^1S_0$	$f\bar{u}, u\bar{f}, f\bar{d}, d\bar{f}$
$X(3350)$	$1^3S_1$	$f\bar{d}, d\bar{f}$
$\chi_{c0}(3860)$	$1^3P_0$	$f\bar{d}, d\bar{f}$
$\chi_{c1}(3872)$	$1^3P_1$	$f\bar{d}, d\bar{f}$
$T_{cc}^+(3875)$	$1^3P_1$	$u\bar{f}$
$Z_c^{\pm,0}(3900)$	$1^1P_1$	$f\bar{u}, u\bar{f}, f\bar{d}, d\bar{f}$
$Z_{cs}^{\pm,0}(3985)$	$2^1S_0$	$f\bar{u}, u\bar{f}, f\bar{d}, d\bar{f}$
$X^{\pm,0}(4020)$	$2^3S_1$	$f\bar{u}, u\bar{f}, f\bar{d}, d\bar{f}$
$X(4160)$	$1^1D_2$	$f\bar{d}, d\bar{f}$
$Y(4230)$	$1^3D_1$	$f\bar{d}, d\bar{f}$
$\chi_{c1}(4274)$	$2^3P_1$	$f\bar{d}, d\bar{f}$
$Z_c^{\pm}(4430)$	$2^1P_1$	$f\bar{u}, u\bar{f}$
$Y(4500)$	$3^3S_1$	$f\bar{d}, d\bar{f}$
$\psi(4660)$	$2^3D_1$	$f\bar{d}, d\bar{f}$
$\chi_{c1}(4685)$	$3^3P_1$	$f\bar{d}, d\bar{f}$
$\chi_{c0}(4700)$	$3^3P_0$	$f\bar{d}, d\bar{f}$

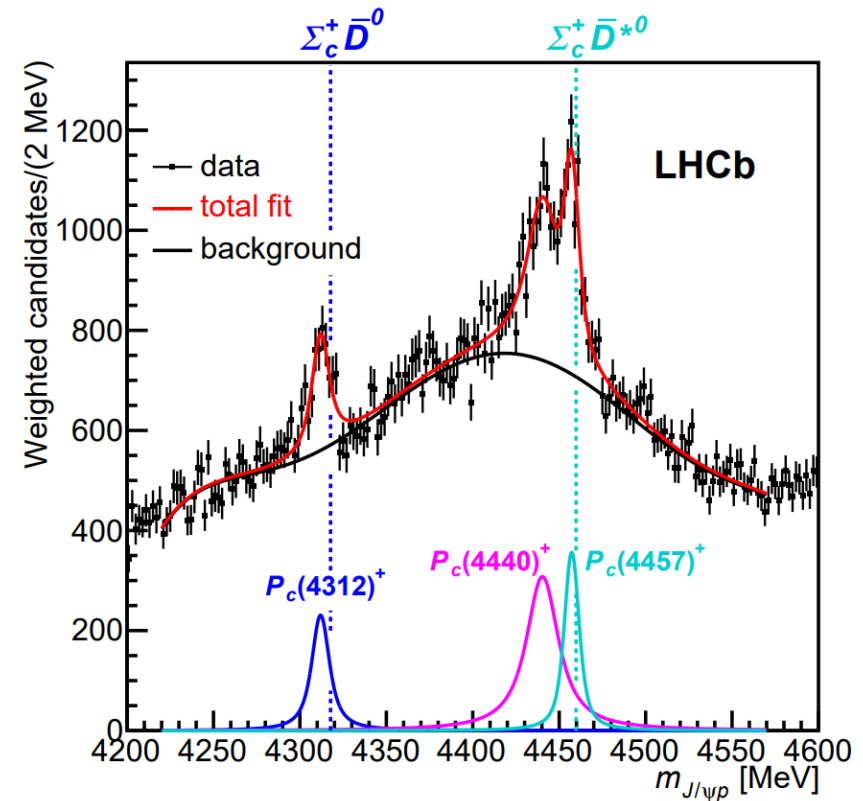
$$QM = n^{2S+1}L_J$$

$R(3760)$	$1^3S_1$	$f\bar{s}, s\bar{f}$
$X(3960)$	$1^3P_0$	$f\bar{s}, s\bar{f}$
$\chi_{c1}(4140)$	$1^3P_1$	$f\bar{s}, s\bar{f}$
$\psi(4360)$	$2^3S_1$	$f\bar{s}, s\bar{f}$
$R(4407)$	$1^3D_1$	$f\bar{s}, s\bar{f}$
$\chi_{c0}(4500)$	$2^3P_0$	$f\bar{s}, s\bar{f}$
$X(6600)$	$1^3S_1$	$f\bar{f}$
$X(6900)$	$1^3P_0$	$f\bar{f}$
$X(7200)$	$2^3S_1$	$f\bar{f}$
$P_c^+(4312)\dots$	$\Sigma_f^+$	$fuu$
$P_{\psi s}^{\Lambda 0}(4459)$	$\Sigma_f^0$	$fud$
$P_{\psi s}^{\Lambda 0}(4338)$	$\Lambda_f^0$	$fud$

# Pentaquarks

Name	Mass	$\Gamma$	$J^P$
$P_c^+(4312)$	4312	10	??
$P_c^+(4380)$	4380	200	??
$P_\psi^{N+}(4337)$	4337	29	??
$P_c^+(4440)$	4440	21	??
$P_c^+(4457)$	4457	6	??

Name	Mass	$\Gamma$	$J^P$
$P_{\psi_s}^{\Lambda^0}(4338)$	4338	7	$\frac{1}{2}^-$
$P_{\psi_s}^{\Lambda^0}(4459)$	4459	17	??



Motivates mass of f quark being a bit less than 2800 MeV

# Pentaquark Production and Decay

$$\Xi_b^- \rightarrow P_{\psi_s}^{\Lambda^0} K^- : bds \xrightarrow{\text{FCNC}} fds + Z \rightarrow fds + u\bar{u} \rightarrow fud + s\bar{u}$$

$$P_{\psi_s}^{\Lambda^0} \rightarrow \Lambda J/\psi : fud \rightarrow cud + W^- \rightarrow cud + s\bar{c} \rightarrow sud + c\bar{c}$$

$$B^- \rightarrow P_{\psi_s}^{\Lambda^0} \bar{p} : b\bar{u} \rightarrow f\bar{u} + Z + g \rightarrow f\bar{u} + u\bar{u} + d\bar{d} \rightarrow fud + \bar{u}\bar{u}\bar{d}$$

$$P_{\psi_s}^{\Lambda^0} \rightarrow \Lambda J/\psi : fud \rightarrow cud + W^- \rightarrow cud + s\bar{c} \rightarrow sud + c\bar{c}$$

$$B_s^0 \rightarrow P_{\psi}^{N^+} \bar{p} : s\bar{b} \xrightarrow{Z} f\bar{d} + 2g \rightarrow f\bar{d} + u\bar{u}u\bar{u} \rightarrow fuu + \bar{u}\bar{u}\bar{d}$$

$$P_{\psi}^{N^+} \rightarrow p J/\psi : fuu \rightarrow cuu + W^- \rightarrow cuu + d\bar{c} \rightarrow uud + c\bar{c}$$

$$\Lambda_b^0 \rightarrow P_{\psi}^{N^+} K^- : bdu \xrightarrow{Z} fsu + g \rightarrow fsu + u\bar{u} \rightarrow fuu + s\bar{u}$$

$$P_{\psi}^{N^+} \rightarrow p J/\psi : fuu \rightarrow cuu + W^- \rightarrow cuu + d\bar{c} \rightarrow uud + c\bar{c}$$



# Predicted Pentaquark decays to 1 c quark

**Isospin triplets:** positively charged

$$\Lambda_b^0 \rightarrow P_c^+ K^- : P_c^+ \rightarrow p D^{*0} \quad \left( \begin{array}{l} \text{(or replace } K^- \text{ with } K^{*-}, \pi^- \text{ or } \rho^- ) \\ \text{replace } D^{*0} \text{ with } D^0 \end{array} \right)$$

For neutral members, substitutions like  $K^- \Rightarrow K^0$  or  $\pi^- \Rightarrow \pi^0$  and  $p \Rightarrow \Lambda$

Also  $\Lambda_b^0 \rightarrow P_c^+ \pi^- : P_c^+ \rightarrow \Lambda_c^+ p \bar{p}$

Look for existing pentaquarks ... and the following predicted new fuu baryons:

$$\text{mass, } J^P : \sim 3870, \frac{1}{2}^+, \sim 4065, \frac{3}{2}^+, \sim 4260, \frac{3}{2}^-$$

**Isospin singlets:**

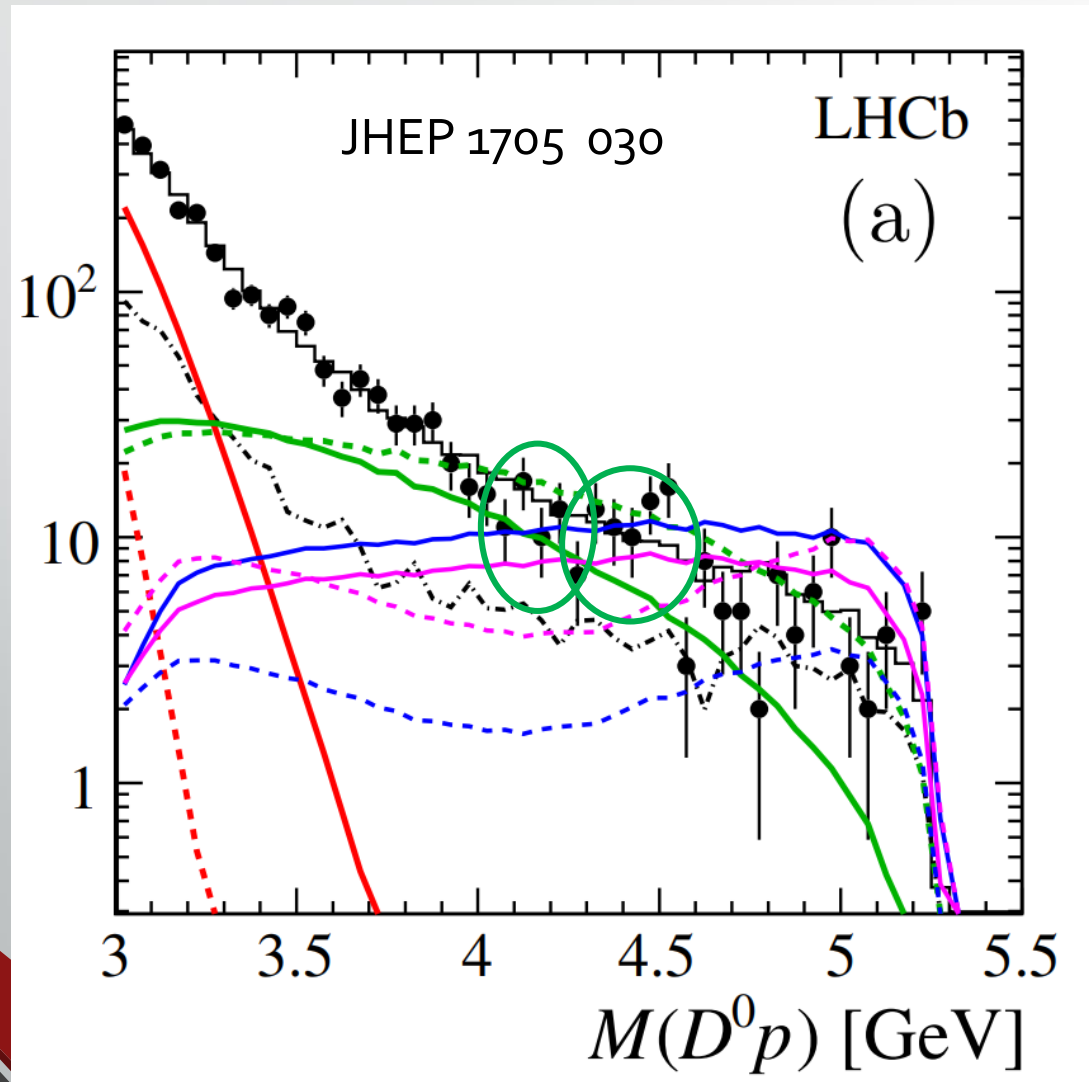
$$B^- \rightarrow P_{\psi s}^{\Lambda 0} \bar{p} : P_{\psi s}^{\Lambda 0} \rightarrow \Lambda D^{*0} : \text{ Belle: arxiv:1108.4271}$$

Look for  $P_{\psi s}^{\Lambda 0} (4338)$  and  $\sim 3795, \frac{1}{2}^+, \sim 4060, \frac{1}{2}^-, \sim 4085, \frac{1}{2}^-, \sim 4200, \frac{3}{2}^-$

LHCb has studied this in [arxiv:1804.09617](https://arxiv.org/abs/1804.09617)

# Has LHCb seen evidence of a predicted decay?

Predicted:  $\Lambda_b^0 \rightarrow P_c^+ \pi^- : P_c^+ \rightarrow pD^0$



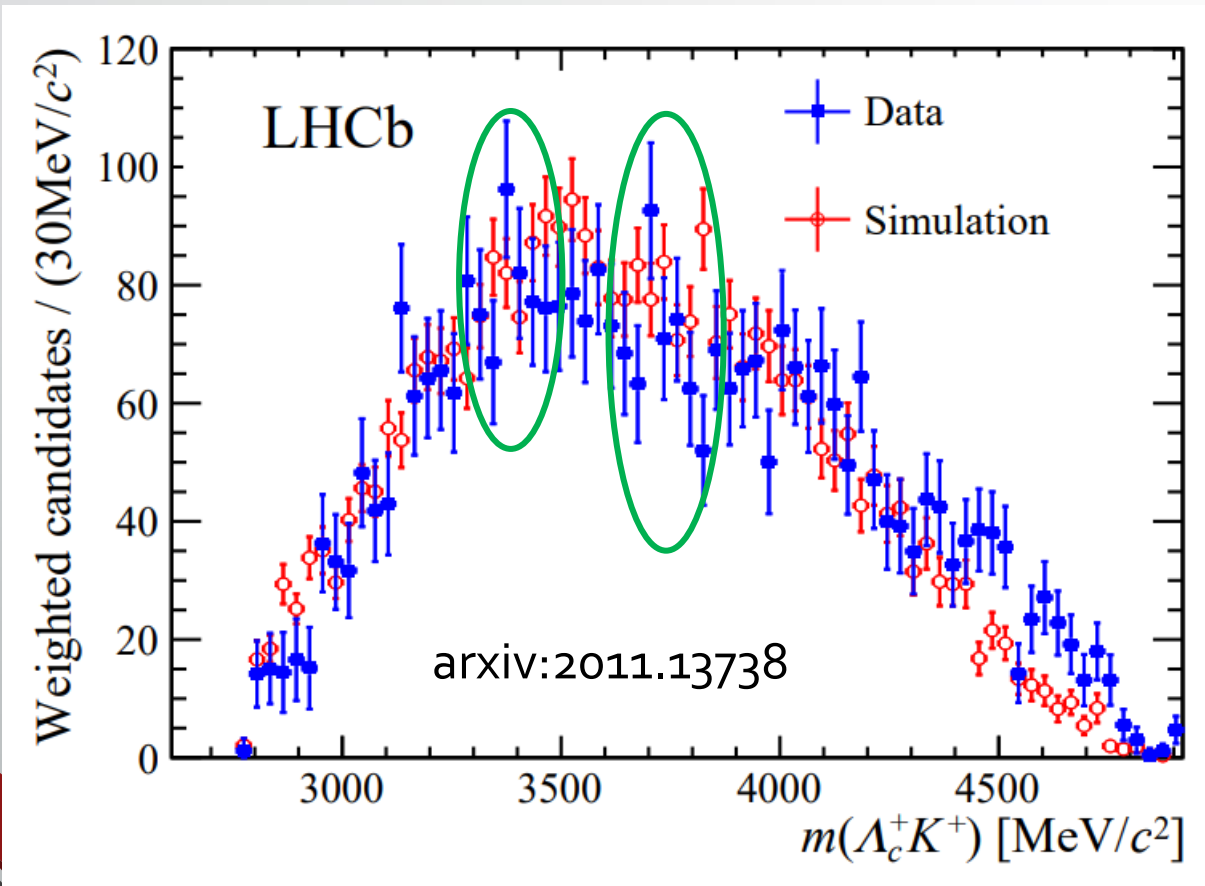
Could this be mapped to existing pentaquarks?

Other lower mass predictions?

# Hints of the predicted $P_c^+(3870)$ and $(4260)$ ?

$$\Lambda_b^0 \rightarrow P_c^+ \pi^- : bdu \rightarrow fdu + g \rightarrow fdu + u\bar{u} \rightarrow fuu + d\bar{u}$$

$$P_c^+ \rightarrow \Lambda_c^+ K^+ K^- : fuu \rightarrow cuu + W^- + g \rightarrow cuu + d\bar{u} + s\bar{s} \rightarrow cdu + s\bar{u} + u\bar{s}$$



When just looking at  
invariant mass of  $\Lambda_c^+ K^+$   
could there be hints of  
 $\Lambda_c^+ K^+ K^-$  resonances at

3870,  $1/2^{+}$ ?

4260,  $3/2^{-}$ ?

# Hadrons decaying to J psi pairs

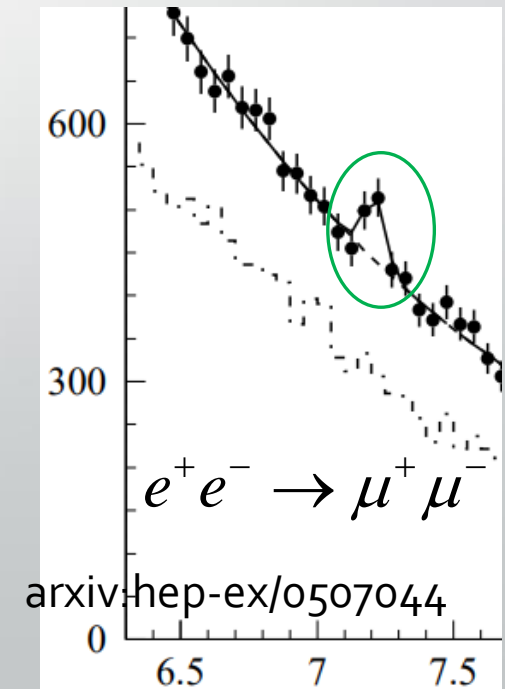
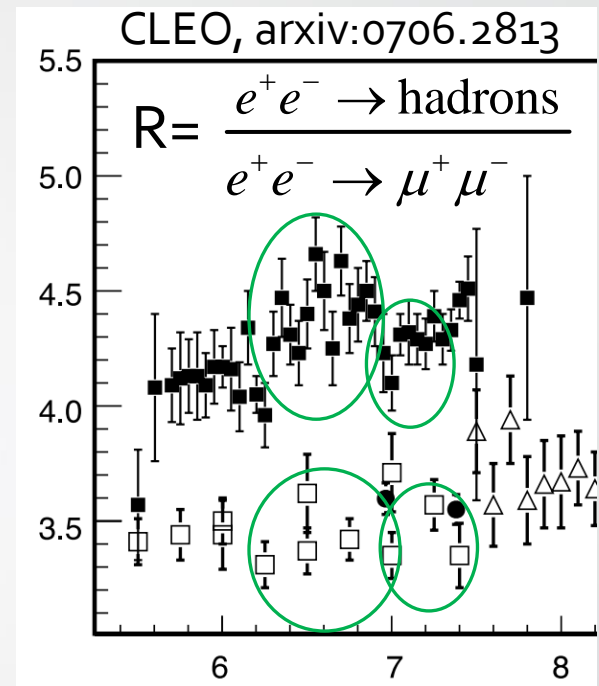
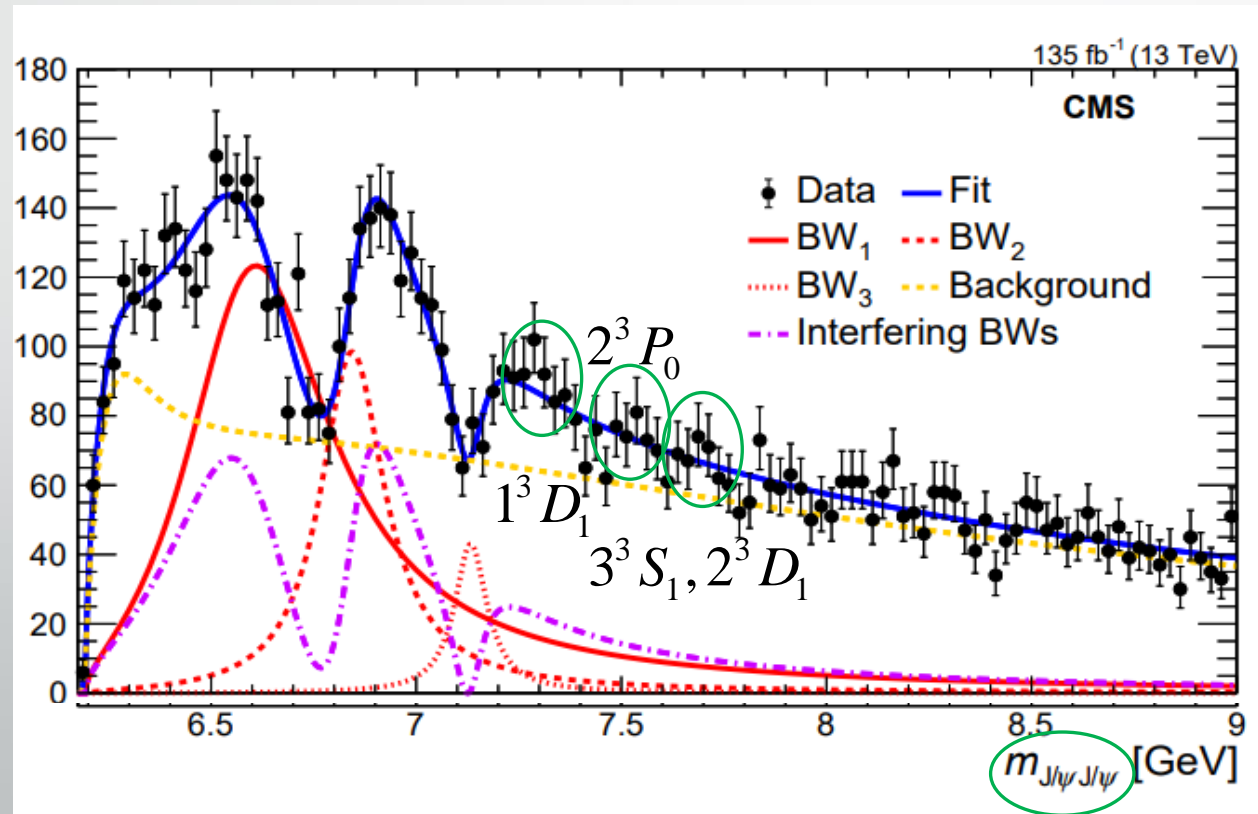
Wide resonances,  
must be strong decays

$$c\bar{c}c\bar{c} \rightarrow c\bar{c} + c\bar{c}$$

$$f\bar{f} \rightarrow f\bar{u} + u\bar{f}$$

Name	Mass	$\Gamma$	$J^{PC}$
X(6600)	6638	440	???
X(6900)	6847	191	0 <sup>++</sup>
X(7200)	7134	97	???

$$f\bar{f} \rightarrow c\bar{c} + c\bar{c}$$



# ffbar Production and Decay

$$g, \gamma \rightarrow X(6900) \dots : g, \gamma \rightarrow f\bar{f}$$

$$X(6900) \dots \rightarrow J/\psi J/\psi : f\bar{f} \xrightarrow{W} c\bar{c} + g \rightarrow c\bar{c} + c\bar{c}$$

This decay is analogous to  $\Upsilon \xrightarrow{W} J/\psi J/\psi$

But in the "CKM" matrix  $|V_{cf}|^4 \sim 40,000 |V_{cb}|^4$

# ffbar meson predictions

Look at pairs of  $\psi(2S)$

$$X \rightarrow \psi(2S)\psi(2S): \quad f\bar{f} \xrightarrow{W} c\bar{c} + g \rightarrow c\bar{c} + c\bar{c}$$

New invariant masses: **~7500 and ~7700 MeV**,  
corresponding to bumps seen in the  $J/\psi J/\psi$  chart

Also strong decays

$$X(6600)\dots \rightarrow X^+(3250)X^-(3250): \quad f\bar{f} \rightarrow f\bar{u} + u\bar{f}$$

$$X(6600)\dots \rightarrow X^0(3250)\bar{X}^0(3250): \quad f\bar{f} \rightarrow f\bar{d} + d\bar{f}$$

# $X(3250)$ (in PDG meson listings: Further States)

1993: PAN 56 1358 A.N. Aleev et al. (BIS-2 Collab.) Translated from YAF 56 100.

$$X^+(3250) \rightarrow \Lambda \bar{p} K^+ \pi^+ : \bar{u}f \rightarrow u\bar{u} + W^+ + 3g \rightarrow u\bar{u} + u\bar{d} + s\bar{s}u\bar{u}d\bar{d}$$

$$X^+(3250) \rightarrow \bar{\Lambda} p K^- \pi^+ : \bar{u}f \rightarrow u\bar{u} + W^+ + 3g \rightarrow u\bar{u} + u\bar{d} + s\bar{s}u\bar{u}d\bar{d}$$

$$X^+(3250) \rightarrow p \bar{p} K_s^0 K^+ : \bar{u}f \rightarrow u\bar{u} + W^+ + 3g \rightarrow u\bar{u} + u\bar{d} + s\bar{s}u\bar{u}d\bar{d}$$

$$X^0(3250) \rightarrow \Lambda \bar{p} K^+ : \bar{d}f \rightarrow d\bar{u} + W^+ + 2g \rightarrow d\bar{u} + u\bar{d} + s\bar{s}u\bar{u}$$

and Hermitian conjugate decays

Look for events with  $(\Lambda \bar{p} K^+ \pi^+)(\Lambda \bar{p} K^+ \pi^-)$  or h.c.

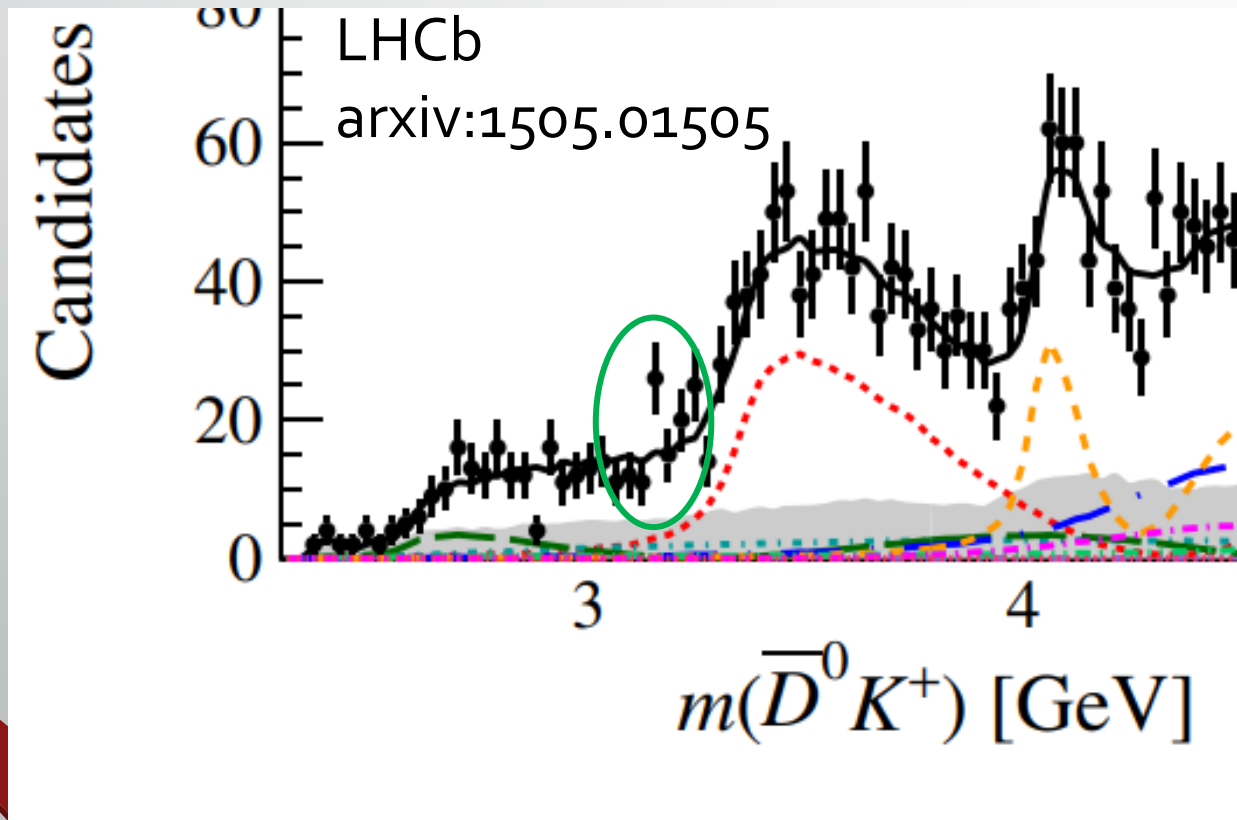
Look for invariant mass peaks at  $\sim 3250$  for hadrons in the parentheses (alternatively without the pions for neutral X pairs)

For those events with 3250 invariant masses, look for peaks in the invariant mass of a pair of 3250s. See if they are at 6600, 6900, 7200, etc.

# Has LHCb seen a hint of the charged 3250?

$$B^0 \rightarrow X^+(3250)\pi^- : d\bar{b} \rightarrow d\bar{f} + Z \rightarrow d\bar{f} + u\bar{u} \rightarrow u\bar{f} + d\bar{u}$$

$$X^+(3250) \rightarrow \bar{D}^0 K^+ : u\bar{f} \rightarrow u\bar{c} + W^+ \rightarrow u\bar{c} + u\bar{s}$$



Alternative search for strong decay of  $X(6600)$ ,  $X(6900)$  ...?

Look for

$$X(6600) \rightarrow X^+(3250) X^-(3250)$$

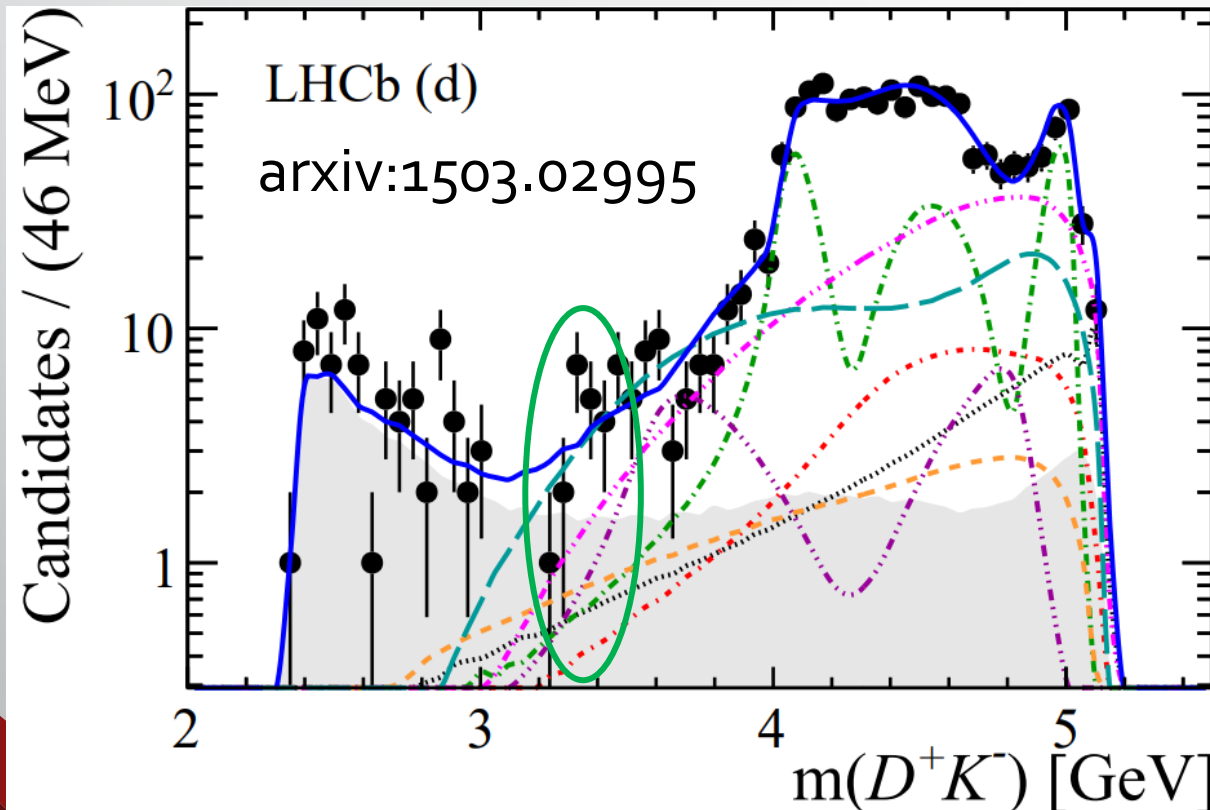
$$X^+(3250) \rightarrow \bar{D}^0 K^+$$



And maybe a hint of the neutral 3250?

$$B^- \rightarrow X^0(3250)\pi^- : b\bar{u} \rightarrow f\bar{u} + Z \rightarrow f\bar{u} + d\bar{d} \rightarrow f\bar{d} + d\bar{u}$$

$$X^0(3250) \rightarrow D^+K^- : f\bar{d} \rightarrow c\bar{d} + W^- \rightarrow c\bar{d} + s\bar{u}$$



Alternative search for strong decay of  $X(6600)$ ,  $X(6900)$  ...?

Look for

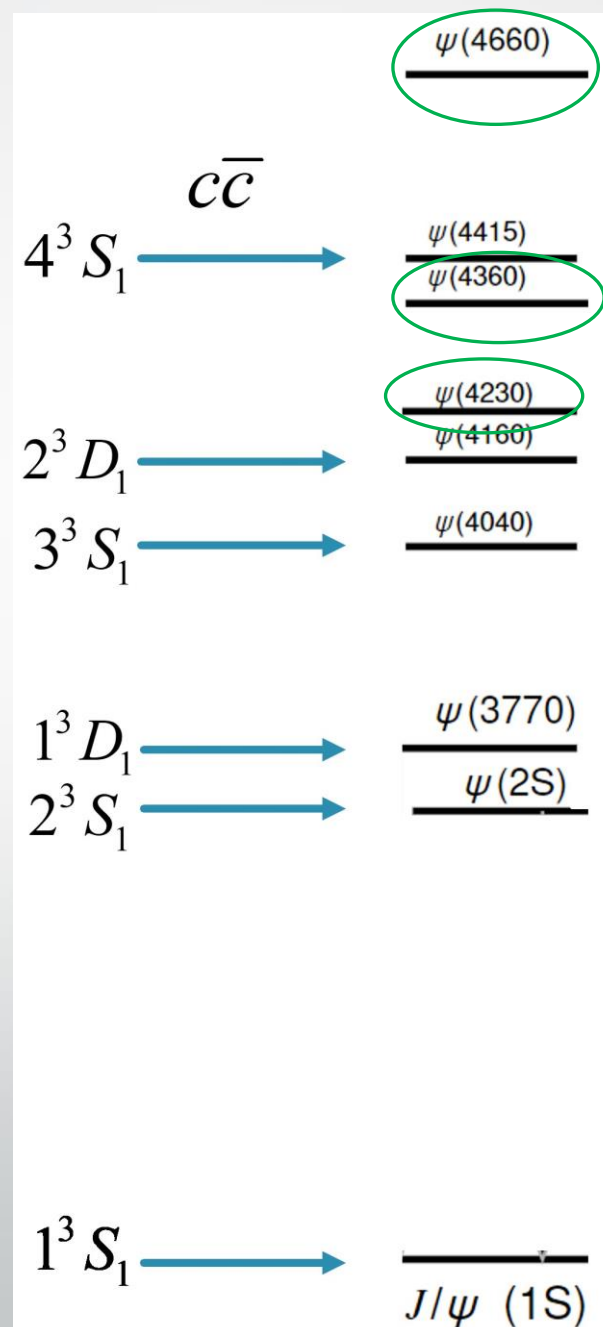
$$X(6600) \rightarrow X^0(3250)\bar{X}^0(3250)$$

$$X^0(3250) \rightarrow D^+K^-$$

# $J^{PC} = 1^{--}$ mesons

seen in  $e^+e^-$  collisions

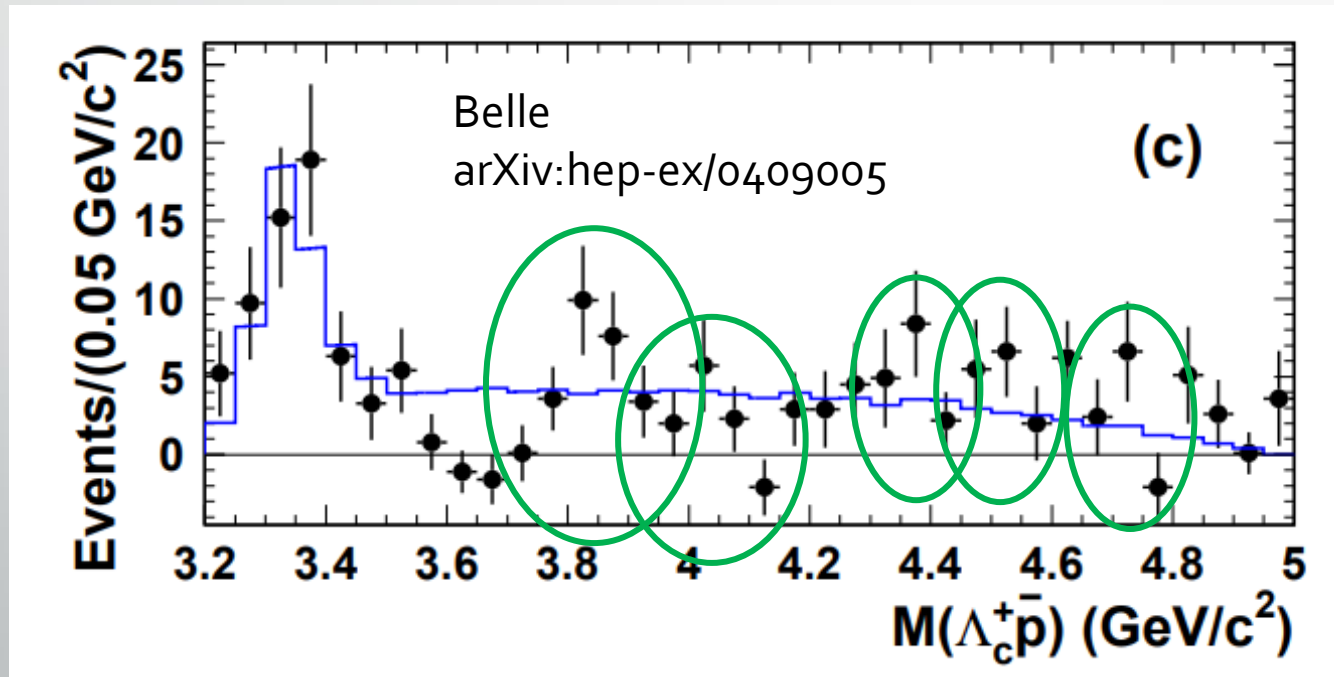
- Mesons in the diagram are in PDG listings for the charmonium system
- Model enables  $Z \rightarrow f\bar{d}$  and  $Z \rightarrow f\bar{s}$
- 4500, 4407, 3760 are in BESIII publications
- The  $J^{PC}$  of  $X(3350)$  and  $X^0(4020)$  are not determined
- Mass spacings for are somewhat similar to those for charmonium



# Observation of X(3350)

$$B^- \rightarrow X \pi^- : b\bar{u} \rightarrow f\bar{u} + Z \rightarrow f\bar{u} + d\bar{d} \rightarrow f\bar{d} + d\bar{u}$$

$$X \rightarrow \Lambda_c^+ \bar{p} : f\bar{d} \rightarrow c\bar{d} + W^- + g \rightarrow c\bar{d} + d\bar{u} + u\bar{u}$$



This was considered an observation of X(3350), mapped here as the  $1^{--} 1^3 S_1$  meson of  $f\bar{d}$

But it could also have been an observation of the  $0^{++} 1^3 P_0$  meson of  $f\bar{d}$  at  $\sim 3860$

And maybe also of the  $1^{--} 2^3 S_1$  meson of  $f\bar{d}$  :  $X^0(4020)$   
 $2^3 P_0 ? 3^3 S_1 ? 3^3 P_0 ?$

# Down, up, strange mesons

Proposed  $f\bar{d}$  and  $d\bar{f}$  Mesons

Name	Mass	$\Gamma$	$J^{PC}$	QM	$\Delta m_c$	$\Delta m_b$
$X(3250)$	3250	45	???	$1^1S_0$	1385	2030
$X(3350)$	3350	70	???	$1^3S_1$	1343	1975
$\chi_{c0}(3860)$	3862	201	$0^{++}$	$1^3P_0$	1519	1836
$\chi_{c1}(3872)$	3872	1.2	$1^{++}$	$1^3P_1$	1460	1854
$Z_c^0(3900)$	3887	28	$1^{+-}$	$1^1P_1$	1465	1839
$Z_{cs}^0(3985)$	3993	8	???	$2^1S_0$	1444	1978
$X^0(4020)$	4024	13	$?^{-}$	$2^3S_1$	1397	
$X(4160)$	4153	136	$2^{-+}$	$1^1D_2$		
$\psi(4230)$	4223	49	$1^{--}$	$1^3D_1$	1463	
$\chi_{c1}(4274)$	4286	51	$1^{++}$	$2^3P_1$		
$Y(4500)$	4485	111	$1^{--}$	$3^3S_1$		
$\psi(4660)$	4630	72	$1^{--}$	$2^3D_1$		
$\chi_{c1}(4685)$	4684	126	$1^{++}$	$3^3P_1$		
$\chi_{c0}(4700)$	4694	87	$0^{++}$	$3^3P_0$		

Proposed  $f\bar{u}$  and  $u\bar{f}$  Mesons

Name	Mass	$\Gamma$	$J^{PC}$	QM	$\Delta m_c$	$\Delta m_b$
$X(3250)$	3250	45	???	$1^1S_0$	1385	2030
$T_{cc}^+(3875)$	3875	0.4	$1^{+?}$	$1^3P_1$	1463	1851
$Z_c^\pm(3900)$	3887	28	$1^{+-}$	$1^1P_1$	1465	1839
$Z_{cs}^\pm(3985)$	3983	13	???	$2^1S_0$	1434	1988
$X^\pm(4020)$	4024	13	$?^{-}$	$2^3S_1$	1397	
$Z_c^\pm(4430)$	4478	181	$1^{+-}$	$2^1P_1$		

Proposed  $f\bar{s}$  and  $s\bar{f}$  Mesons

Name	Mass	$\Gamma$	$J^{PC}$	QM	$\Delta m_c$	$\Delta m_b$
$R(3760)$	3766	22	$1^{--}$	$1^3S_1$	1648	1655
$X(3960)$	3956	43	$0^{++}$	$1^3P_0$	1639	
$\chi_{c1}(4140)$	4147	19	$1^{++}$	$1^3P_1$	1687	
$\psi(4360)$	4372	115	$1^{--}$	$2^3S_1$	1658	
$R(4407)$	4407	128	$1^{--}$	$1^3D_1$		
$\chi_{c0}(4500)$	4474	77	$0^{++}$	$2^3P_0$		

# Three arguments against the proposed quark

1. The quark was not seen in precision  $e^+e^-$  to Z experiments at LEP/SLD.
2. The model doubles the coupling of the Z boson with the right-chiral charm quark, but LEP/SLD experiments established the charm-Z coupling to be the same as the Standard Model.
3. Inclusive hadronic cross sections fit the data with the known quarks

# Lifetime of the f quark

First calculate lifetime of f quark

Heavy quark effective theory zeroth order:

$$\frac{\tau_f}{\tau_b} \approx \frac{m_b^5 \left( |V_{cb}^+|^2 + 3|V_{cb}^-|^2 \right)}{m_f^5 \left( |V_{cf}^+|^2 + 3|V_{cf}^-|^2 \right)} \approx 1\%$$

Main reason: the new quark has stronger interactions with the W boson

$$|V_{cb}^+| \approx 0.04 \quad |V_{cf}^+| \approx |V_{cf}^-| \approx 1$$

**Lifetime: ~0.02 ps**

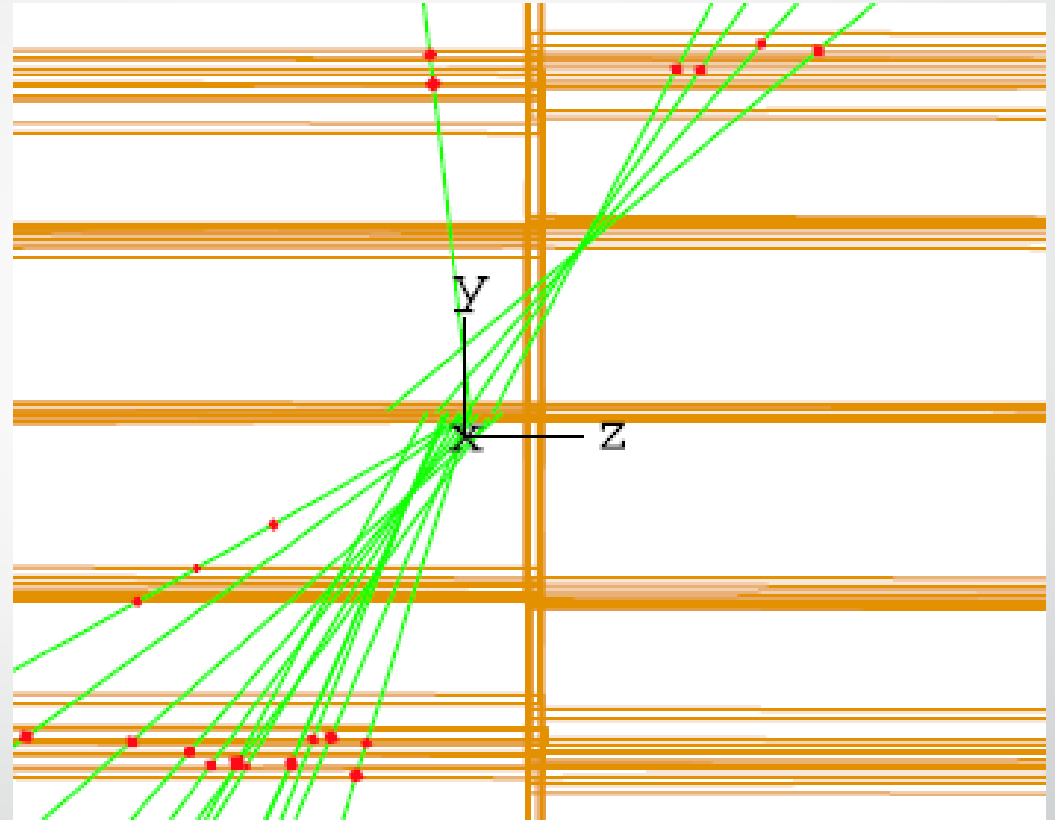
# Secondary vertex tagging at LEP & SLD

Experimental Resolution:  
~20-70 microns

Lifetime of b quark: ~1.6 ps  
Impact parameter: ~300 microns

Lifetime of c quark: ~.5 - 1 ps  
Impact pmtr: ~100-200 microns

Lifetime of f quark: ~0.016 ps  
Impact parameter: ~3 microns



b  $\rightarrow$  c and c  $\rightarrow$  s vertices were seen

An f  $\rightarrow$  c vertex would not have been seen

f quarks would have been lumped with c quarks

# Effective Z-charm coupling

Z-c coupling

	$V_{c\bar{c}}^V$	$V_{c\bar{c}}^A$
$7q$	$1 - \frac{4}{3}x$	$0$
<i>SM</i>	$\frac{1}{2} - \frac{4}{3}x$	$-\frac{1}{2}$

~no FCNC with c

$$V_{c\bar{c},eff}^V \square V_{c\bar{c}}^V + P_f V_{f\bar{f}}^V + 2 \sum_q P_q V_{q\bar{q}}^V$$

$$V_{c\bar{c},eff}^A \square V_{c\bar{c}}^A + P_f V_{f\bar{f}}^A + 2 \sum_q P_q V_{q\bar{q}}^A$$

$P_q$  is the probability that this survives tagging, cuts, etc.

Partial widths:  $\left(V_{c\bar{c},eff}^V\right)^2 + \left(V_{c\bar{c},eff}^A\right)^2$  Asymmetry:  $2V_{c\bar{c},eff}^V V_{c\bar{c},eff}^A / \left(\left(V_{c\bar{c},eff}^V\right)^2 + \left(V_{c\bar{c},eff}^A\right)^2\right)$

$P_f = P_b = 1, P_s = P_d = 0.5$  reproduces SM partial widths and the data

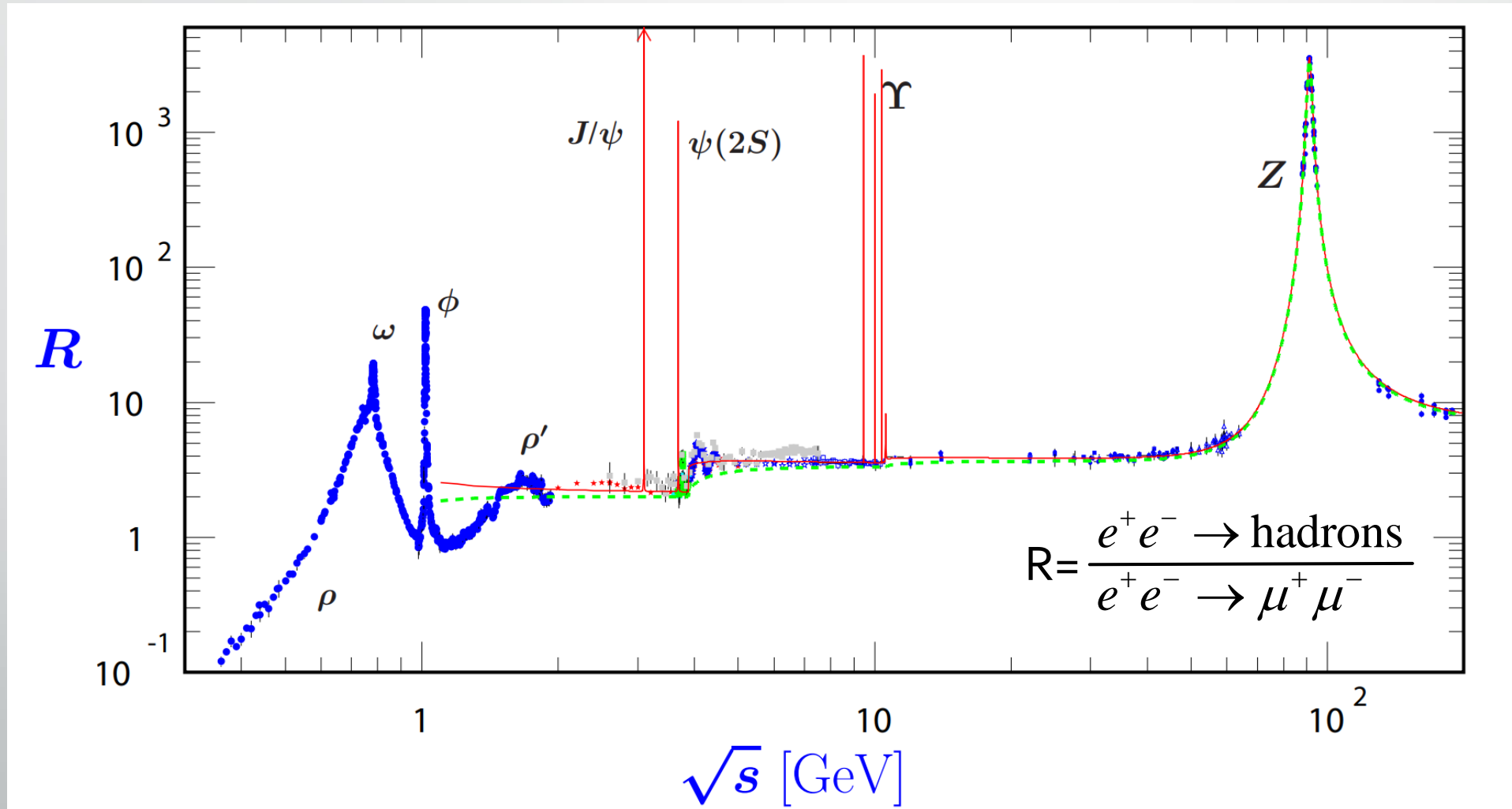
$P_f = P_b = 46\%, P_s = P_d = 23\%$  reproduces SM asymmetry and the data

This is consistent with:

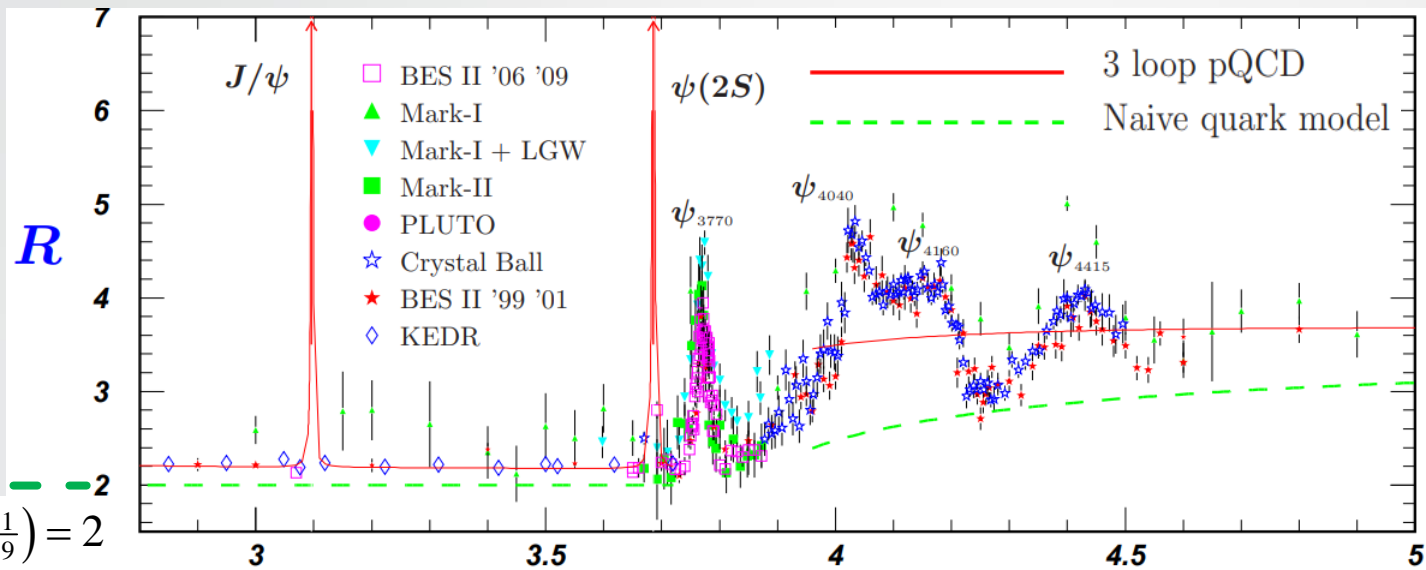
- the best tags for c events were ones that counted c quarks or D mesons
- asymmetry used tags like opposite hemisphere charge, lepton charge



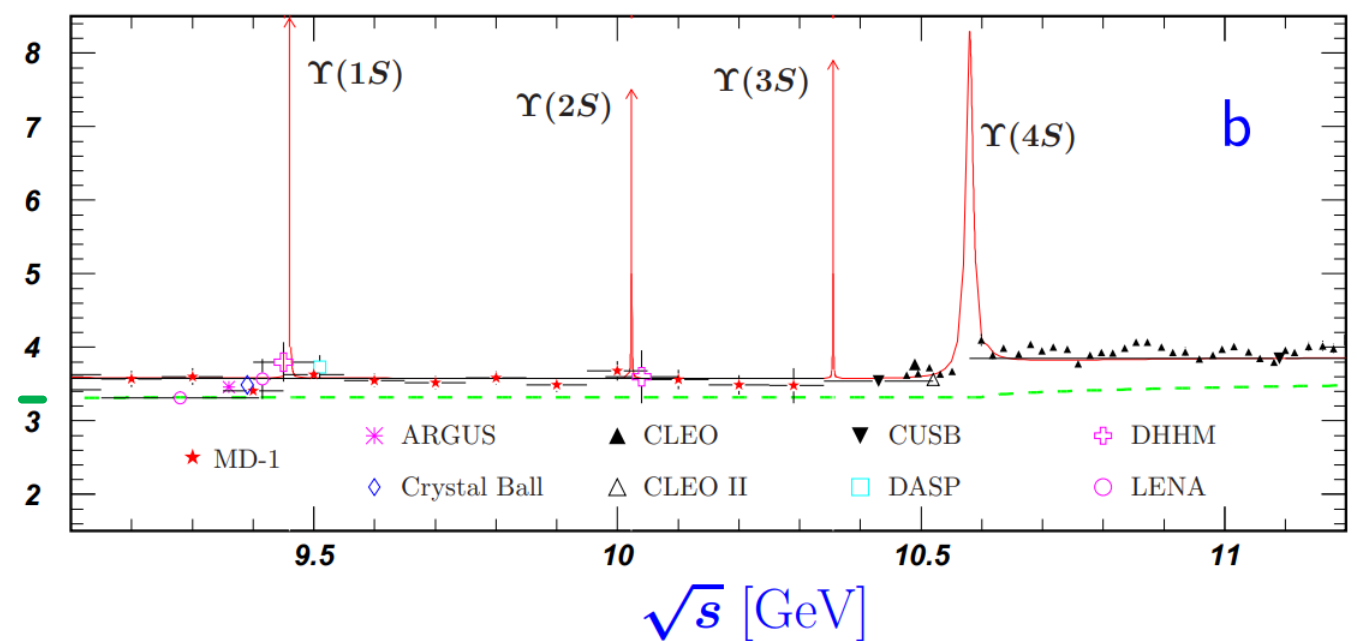
# Inclusive Hadronic Cross Section - PDG



# PDG R Graph showing quark levels



It will be hypothesized calculations may be missing an effect that would lower R by 1/3



Adding an f quark would add 1/3 to R

# Complete sets of states for inclusive cross sections

The calculation of the inclusive cross section adds exclusive cross sections over a complete set of orthogonal final states

It has been argued that:

- Any complete set of orthogonal states can be used; they will all generate the same answer
- The final states in the complete set do not need to be observable

The argument appears to be incorrect, at least for some cases.

# Two complete sets of final states

Set (a): photon & Z

$$\sum_{V=\gamma, Z} \left| \begin{array}{c} e^+ \\ e^- \end{array} \rightarrow \begin{array}{c} \text{wavy line} \\ V \end{array} \right|^2 \neq$$

Set (b): lepton and quark pairs

$$\sum_l \left| \sum_V \begin{array}{c} e^+ \\ e^- \end{array} \rightarrow \begin{array}{c} \text{wavy line} \\ V \end{array} \rightarrow \begin{array}{c} l \\ \bar{l} \end{array} \right|^2 + \sum_q \left| \sum_V \begin{array}{c} e^+ \\ e^- \end{array} \rightarrow \begin{array}{c} \text{wavy line} \\ V \end{array} \rightarrow \begin{array}{c} q \\ \bar{q} \end{array} \right|^2$$

- When using set (a), the photon and Z boson are treated as orthogonal final states, so there is no interference between them.
- When using set (b), interference between the photon and Z boson is included, since each can lead to the same final state
- Sets (a) and (b) generate different results
- Set (b) reproduces inclusive lepton data. Set (a) does not.

# Another complete set of final states

Set (b): lepton and quark pairs

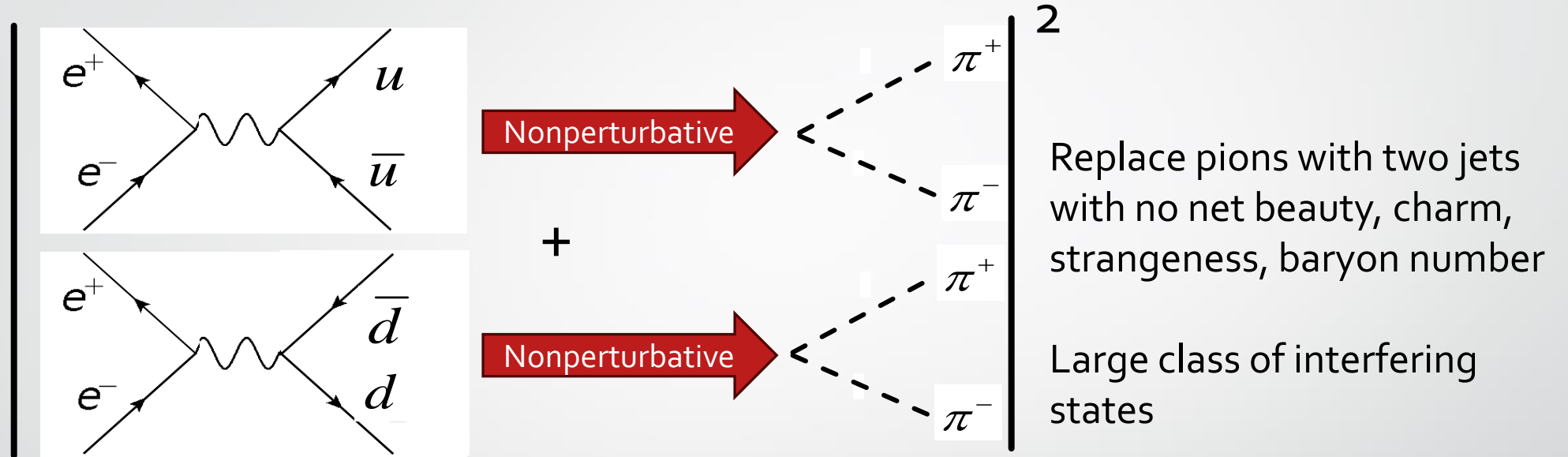
$$\sum_l \left| \sum_V \left[ \begin{array}{c} e^+ \nearrow \\ \searrow e^- \\ \text{---} V \text{---} \\ \nearrow l \\ \searrow \bar{l} \end{array} \right] + \sum_V \left[ \begin{array}{c} e^+ \nearrow \\ \searrow e^- \\ \text{---} V \text{---} \\ \nearrow q \\ \searrow \bar{q} \end{array} \right] \right|^2$$

Set (c): lepton pairs and hadrons

$$\sum_l \left| \sum_V \left[ \begin{array}{c} e^+ \nearrow \\ \searrow e^- \\ \text{---} V \text{---} \\ \nearrow l \\ \searrow \bar{l} \end{array} \right] + \sum_{X, V, q} \left[ \begin{array}{c} e^+ \nearrow \\ \searrow e^- \\ \text{---} V \text{---} \\ \nearrow q \\ \searrow \bar{q} \end{array} \right] \right|^2 \rightarrow \text{Hadron state X}$$

If there are hadronic states X in set (c) that could have been produced by different flavor quark pairs created by V, then interference between those quark-pair intermediate states must be considered in the set (c) calculation.

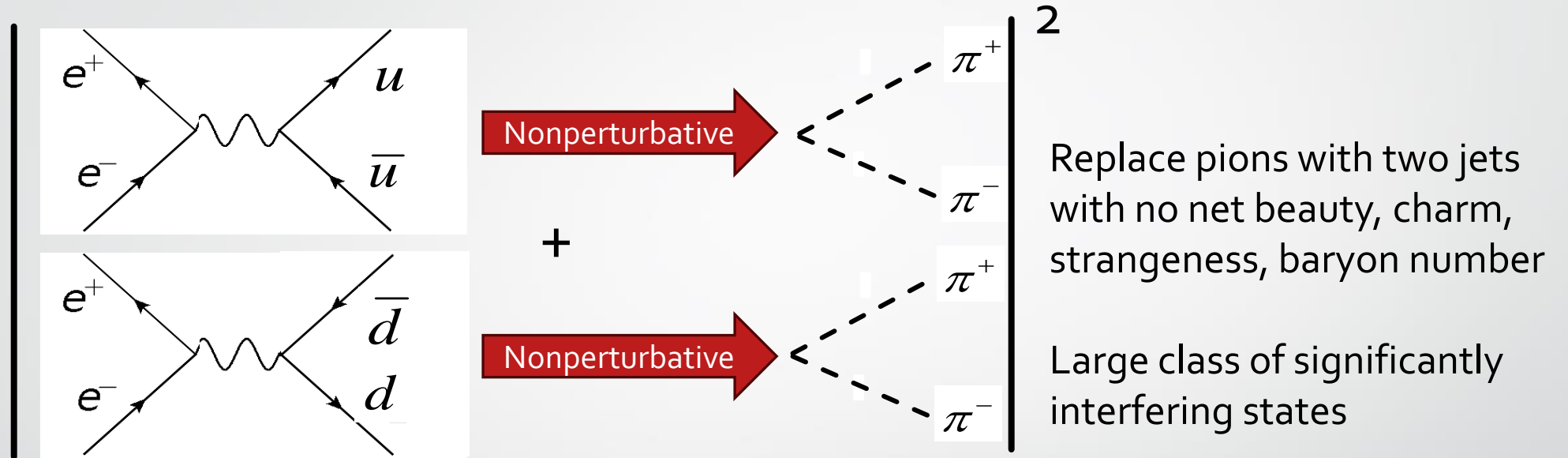
# Example "set (c)" final state: 2 pions



If complete set (c) is being used for calculation of the inclusive cross section (hadron states instead of  $q\bar{q}$  states), then interference between these two diagrams must be taken into account for this hadronic state X.

An inclusive cross section calculation using set (c) would be different than one using set (b).

# Is the interference significant?

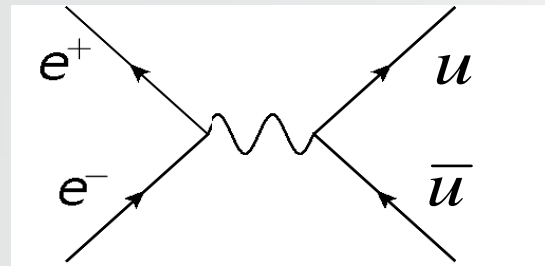


From isospin symmetry, the nonperturbative parts above should be the same (even if they can't be calculated analytically).

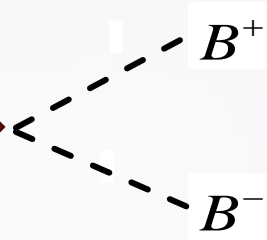
The difference between neglecting interference and including it is:

$$C\left(\left(\frac{2}{3}\right)^2 + \left(\frac{1}{3}\right)^2\right) \text{ vs. } C\left(\frac{2}{3} - \frac{1}{3}\right)^2$$

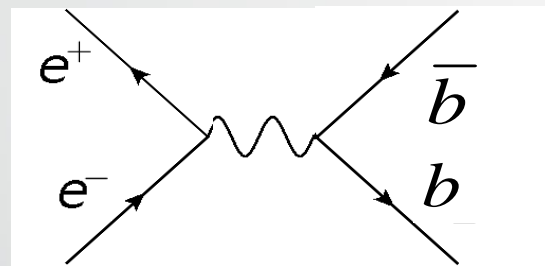
# Interference for heavy quarks?



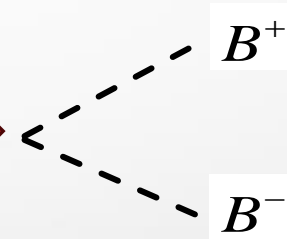
Nonperturbative



Negligible since  $2m_b \gg \Lambda_{QCD}$



Nonperturbative



Almost all the contribution  
 $2m_u \ll \Lambda_{QCD}$

Interference of this kind involving the heavy quarks is negligible.

So for heavy quarks, calculations using set (b) and set (c) should generate the same result, so might as well use set (b) for heavy quarks



# Comparing complete sets of final states

Set (b): lepton and quark pairs

$$\sum_l \left| \sum_V \left[ \begin{array}{c} e^+ \\ e^- \end{array} \right] \left[ \begin{array}{c} l \\ \bar{l} \end{array} \right] + \sum_V \left[ \begin{array}{c} e^+ \\ e^- \end{array} \right] \left[ \begin{array}{c} q \\ \bar{q} \end{array} \right] \right|^2$$

Set (c): lepton pairs and hadrons

$$\sum_l \left| \sum_V \left[ \begin{array}{c} e^+ \\ e^- \end{array} \right] \left[ \begin{array}{c} l \\ \bar{l} \end{array} \right] + \sum_{X, V, q} \left[ \begin{array}{c} e^+ \\ e^- \end{array} \right] \left[ \begin{array}{c} q \\ \bar{q} \end{array} \right] \right|^2$$

Hadron state X

There are hadronic states X in set (c) that could have been produced by either a u ubar or a d dbar intermediate state  
 Interference between those intermediate states must be considered

The set (c) calculation has not been performed

A set (c) calculation would generate different results than set (b)

- Due to up-down interference, inclusive cross section calculation results would be different using complete sets of states (b) vs. (c)
- Based on other examples, it is best to use a complete set of observable states: set (c)
- Therefore, the usual calculation of inclusive cross sections is incorrect: set (b)

## Hypothesis for a set c inclusive cross section calculation

- Given that the R generated by  $u \bar{u}$  is  $4/3$  and by  $d \bar{d}$  is  $1/3$ , it is plausible that if a set (c) calculation incorporating interference was performed, it could generate an R value for both of  $\sim 4/3$ , rather than  $\sim 5/3$ .
- If so, after including 3-loop pQCD corrections, this new cross section calculation would under-predict the measured R values by  $\sim 1/3$ .
- If there was an additional heavy quark with charge  $-1/3$ , that would contribute an additional  $\sim 1/3$  to the R value and reproduce the data.

It would be interesting to find some way to do the set (c) calculation.



W & Z interactions of the additional quark

# Modified W boson interactions

Add a fourth generation of down-type quark.

$$\begin{aligned} & (\bar{u}_{L1} \quad \bar{u}_{L2} \quad \bar{u}_{L3}) \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix} \gamma^\mu \begin{pmatrix} d_{L1} \\ d_{L2} \\ d_{L3} \\ d_{L4} \end{pmatrix} g W_\mu + h.c. \\ + & (\bar{u}_{R1} \quad \bar{u}_{R2} \quad \bar{u}_{R3}) \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix} \gamma^\mu \begin{pmatrix} d_{R1} \\ d_{R2} \\ d_{R3} \\ d_{R4} \end{pmatrix} g W_\mu + h.c. \end{aligned}$$

Both the 1<sup>st</sup> and 4<sup>th</sup> generation down-type quark have right-chiral W interactions

Two R and two L connections means gauge anomalies are cancelled for W

# Modified "CKM" Matrix

Vector (+) and Axial Vector (-) versions

$$V_{CKM}^{\pm} = V_R^U \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix} V_R^{D\dagger} = V_L^U \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} V_L^{D\dagger}$$

Unitary matrices that translate to quark mass eigenstates

$$M_D = \begin{pmatrix} -0.0338 & 0.0137 & 0.0246 & -0.0527 \\ -0.0252 & -0.0725 & -0.0636 & -0.0804 \\ 0.1054 & 1.4894 & -3.8554 & 0.1329 \\ 1.4717 & -0.0800 & 0.2408 & 2.3052 \end{pmatrix}$$

$$M_U = \begin{pmatrix} 0.00131 & -0.00191 & 0.0122 \\ 0.6493 & 1.1126 & -5.3477 \\ 1.7379 & -1.0843 & 171.94 \end{pmatrix},$$

$$|V_{CKM}^+| = \begin{pmatrix} 0.9745 & 0.2239 & 0.0043 & 0.0094 \\ 0.2323 & 0.9661 & 0.0388 & 0.9720 \\ 0.0088 & 0.0402 & 0.9973 & 0.0619 \end{pmatrix}$$

$$|V_{CKM}^-| = \begin{pmatrix} 0.9742 & 0.2252 & 0.0042 & 0.0093 \\ 0.2165 & 0.9805 & 0.0394 & 1.0278 \\ 0.0144 & 0.0349 & 0.9974 & 0.0621 \end{pmatrix}$$

This choice of mass matrices can reproduce all normal CKM data

It also helps with the vector vs. axial 3-sigma difference in  $V_{us}$

# Quark couplings to the Z boson by generation

$$Zq\bar{q}$$

Up-type quarks

Gen	$g_L$	$g_R$
1	$-\frac{2}{3}x$	$\frac{1}{2} - \frac{2}{3}x$
2	$\frac{1}{2} - \frac{2}{3}x$	$\frac{1}{2} - \frac{2}{3}x$
3	$\frac{1}{2} - \frac{2}{3}x$	$-\frac{2}{3}x$
SM	$\frac{1}{2} - \frac{2}{3}x$	$-\frac{2}{3}x$

$$x = \sin^2 \theta_W$$

Down-type quarks

Gen	$g_L$	$g_R$
1	$\frac{1}{3}x$	$-\frac{1}{2} + \frac{1}{3}x$
2	$-\frac{1}{2} + \frac{1}{3}x$	$\frac{1}{3}x$
3	$-\frac{1}{2} + \frac{1}{3}x$	$\frac{1}{3}x$
4	$\frac{1}{3}x$	$-\frac{1}{2} + \frac{1}{3}x$
SM	$-\frac{1}{2} + \frac{1}{3}x$	$\frac{1}{3}x$

Z boson coupling depends on the generation

Quark gauge anomalies cancel for Z boson:  
For every L interaction, there is an R interaction

# Example Z Mixing Matrix

$$V_{ZD}^L = V_L^D \begin{pmatrix} \frac{1}{3}x & 0 & 0 & 0 \\ 0 & -\frac{1}{2} + \frac{1}{3}x & 0 & 0 \\ 0 & 0 & -\frac{1}{2} + \frac{1}{3}x & 0 \\ 0 & 0 & 0 & \frac{1}{3}x \end{pmatrix} V_L^{D\dagger} = \begin{pmatrix} 0.0520 & -0.1093 & -0.0030 & 0.0032 \\ -0.1093 & -0.3972 & -0.0003 & 0.0147 \\ -0.0030 & -0.0003 & -0.4210 & -0.0304 \\ 0.0032 & 0.0147 & -0.0304 & 0.0749 \end{pmatrix}$$

- Since the diagonal elements are not the same, the Z boson mixes flavors
- There are 4 mixing matrices for U vs. D and L vs. R
- For the mass matrices that fit CKM data, most off-diagonal elements of the Z mixing matrices are very small, no appreciable FCNC
- $V_{f\bar{b}}^L, V_{f\bar{s}}^L, V_{f\bar{d}}^L, V_{d\bar{s}}^A$  are significant, non-negligible FCNC
- Non-negligible  $V_{f\bar{b}}^L$  facilitates  $b \rightarrow f \rightarrow c$  and could help with the 3 sigma difference between inclusive vs. exclusive measurements of CKM  $V_{cb}$

# Cancelling gauge anomalies

- In the Standard Model, quark gauge anomalies are cancelled by leptons
- In this model, quark gauge anomalies cancel among themselves
- A full theory should have additional right-handed leptons, so that gauge anomalies also cancel separately among leptons
- These right-handed leptons can include neutrinos needed for neutrino mixing (Twisted Superfields: [arxiv:2112.04469](https://arxiv.org/abs/2112.04469))



# “Twisted Superfields”

## A theory with broken supersymmetry

- Supersymmetry helps solve the hierarchy problem (Why doesn't the Higgs Boson have a much larger mass?)
- But supersymmetry predicts a lot of new particles that are not observed, since no existing particles can be N=1 superpartners with each other: **HLS**
- Breaking supersymmetry can allow existing particles to be superpartners with each other: quarks can be “superpartners” of the gauge bosons
- 3 key features of supersymmetry
  - ~~Invariance to global superspace translations~~
  - Invariance to local superspace gauge transformations
  - Holomorphic superpotential

Twisted superfields break supersymmetry to allow this

# Twisted Superfields for $U(3) \times U(3)$

Real twisted superfield  $V \square \begin{pmatrix} A_1^\mu & q_{VL}^\dagger, q_{VR} \\ q_{VL}, q_{VR}^\dagger & A_2^\mu \end{pmatrix}$   
 gluons are in  $A_1^\mu$ ,  $W^\mu$  is in  $A_2^\mu$

Each  $q$  is a  $3 \times 3$  matrix with 3 colors, and 3 flavors (1 up-type, 2 down-type)

Adjoint twisted superfield  $\Phi \square \begin{pmatrix} \phi_1 & q_{\Phi R} \\ q_{\Phi L} & \phi_2 \end{pmatrix}$   $\Psi_{1F} \square \begin{pmatrix} \varphi_{1F} \\ l_{LF} \end{pmatrix}$   $\Psi_{2F} \square \begin{pmatrix} q_{\varphi RF} \\ \varphi_{2F} \end{pmatrix}$

And 3 flavors of fundamental and conjugate representation fields (1 u 2 d)

No gauge anomaly – like Supersymmetric QCD

Adding up quarks:  $3u_L, 3u_R, 6d_L, 6d_R \rightarrow 3u_L, 3u_R, 4d_L, 4d_R$

Symmetry breaking to  $SU(3) \times SU(2) \times U(1)^2$  gives unification-scale masses to 2 quarks, leaving the 7 quarks and the CKM matrices discussed earlier

# Summary

- Hypothesis: A fourth down-type quark exists
  - It has a mass of  $\sim 2.8$  GeV
  - The W boson connects this quark with the right-chiral component of the charm quark
  - The right-left combo generates FCNC with the Z boson
- The quark explains the mass, spin, parity, production and decay processes of most exotic hadrons
- Inclusive cross sections and precision electroweak measurements do not definitively rule it out
- Predictions have been made for where to find more mesons and baryons
- Many published papers have charts that could be evidence of the predictions
- In the theory, gauge anomalies cancel separately among quarks

# Look for resonances in existing LHCb data?

In each decay below, look at invariant masses in parentheses:


- arxiv:1804.09617  $\Lambda_b^0 \rightarrow (\Lambda_c^+ p \bar{p}) \pi^-$ ,  $\Lambda_b^0 \rightarrow (\Lambda_c^+ \bar{p} \pi^-) p$
- arxiv:2011.13738  $\Lambda_b^0 \rightarrow (\Lambda_c^+ K^+ K^-) \pi^-$ ,  $\Lambda_b^0 \rightarrow (\Lambda_c^+ K^- \pi^-) K^+$  (2<sup>nd</sup>: fsd baryon)
- arxiv:1109.6831  $\bar{B}^0 \rightarrow (D^+ \pi^- \pi^-) \pi^+$ ,  $\bar{B}_s^0 \rightarrow (D_s^+ \pi^- \pi^-) \pi^+$ ,  $B^- \rightarrow (D^0 \pi^+ \pi^-) \pi^-$   
 $\bar{B}^0 \rightarrow (D^+ \pi^-) \pi^- \pi^+$ ,  $\bar{B}_s^0 \rightarrow (D_s^+ \pi^-) \pi^- \pi^+$ ,  $B^- \rightarrow (D^0 \pi^-) \pi^+ \pi^-$   
 $\Lambda_b^0 \rightarrow (\Sigma_c^0 \pi^+) \pi^-$ ,  $\Lambda_b^0 \rightarrow (\Sigma_c^0 \pi^-) \pi^+$ ,  $\Lambda_b^0 \rightarrow (\Sigma_c^{++} \pi^-) \pi^-$
- Phys Rev Lett 108, 161801  $B^- \rightarrow (D^0 \pi^+ \pi^-) K^-$ ,  $B^- \rightarrow (D^0 K^- \pi^+) \pi^-$
- Phys Rev D87, 112009  $B^0 \rightarrow (\bar{D}^0 K^+) \pi^-$ ,  $B_s^0 \rightarrow (\bar{D}^0 \pi^+) K^-$
- arxiv:1704.07581  $B^+ \rightarrow (D^{*-} K^+) \pi^+$
- arxiv:1803.06444  $B^+ \rightarrow (D^{(*)-} l^+ \nu) \pi^+$ ,  $B^0 \rightarrow (\bar{D}^{(*)0} l^+ \nu) \pi^-$
- arxiv:1704.08497  $B^0$  or  $B_s^0 \rightarrow (p \bar{p} h^+) h^-$ ,  $h$  is  $K$  or  $\pi$   
 $B^0$  or  $B_s^0 \rightarrow (\bar{p} h^+ h^-) p$ ,  $h$  is  $K$  or  $\pi$

# Questions?

## Additional slides

- more experimentally testable predictions
- more possible evidence of these predictions in published papers
- non-SM explanations for some experiments (e.g. forward  $Z+c$ )

arxiv:2203.03007



More experimentally testable predictions  
... and possible sightings

# 3872 Production and Decay

$$B^+ \rightarrow \chi_{c1}(3872) K^+ : ub \rightarrow uf + Z \rightarrow uf + ds \rightarrow df + us$$

$$\chi_{c1}(3872) \rightarrow \bar{D}^0 D^0 \pi^0 : df \rightarrow dc + W^+ + g \rightarrow dc + cd + uu$$

Decay from valence quarks exchanging a W boson

$$\chi_{c1}(3872) \rightarrow J/\psi \omega \text{ or } \bar{D}^0 D^{*0} : df \xrightarrow{W} cc + g \rightarrow cc + uu$$

Assume  $\chi_{c1}(3872) \rightarrow J/\psi \pi^+ \pi^-$  is mostly from  $\chi_{c1}(3872) \rightarrow J/\psi (\omega \text{ or } \rho^0)$

Same decay mechanism as above W exchange.

If there is a  $\chi_{c1}^+(3872) = uf$ , it cannot decay by W boson exchange.

This explains no significant signal in  $\chi_{c1}^+(3872) \rightarrow J/\psi \pi^+ \pi^0$

# $\chi_{c1}^+ (3872)$ Expected Production and Decay

$$B^+ \rightarrow \chi_{c1}^+ (3872) \pi^0 : u\bar{b} \rightarrow u\bar{f} + Z \rightarrow u\bar{f} + u\bar{u}$$

$$B^0 \rightarrow \chi_{c1}^+ (3872) \pi^- : d\bar{b} \rightarrow d\bar{f} + Z \rightarrow d\bar{f} + u\bar{u} \rightarrow u\bar{f} + d\bar{u}$$

Expected decay

$$\chi_{c1}^+ (3872) \rightarrow \bar{D}^0 D^0 \pi^+ \text{ or } \bar{D}^0 D^+ \pi^0 : u\bar{f} \rightarrow u\bar{c} + W^+ + g$$

If the  $\bar{D}^0$  did a  $\bar{D}^0 \rightarrow D^0$  fluctuation and then decayed,

this would look just like decays seen for  $T_{cc}^+ (3875)$

Why not a much larger signal for  $T_{cc}^+ (3875) \rightarrow \bar{D}^0 D^0 \pi^+$  ?



# Predicted 3872+ decays to 1 c quark

$$B^+ \rightarrow \chi_{c1}^+(3872) \pi^0 \quad B^0 \rightarrow \chi_{c1}^+(3872) \pi^-$$

$$\chi_{c1}^+(3872) \rightarrow D_s^- K^+ \pi^+ : \quad u\bar{f} \rightarrow u\bar{c} + W^+ + g \rightarrow u\bar{c} + u\bar{d} + s\bar{s}$$

$$\chi_{c1}^+(3872) \rightarrow \bar{D}^0 \pi^0 \pi^+ : \quad u\bar{f} \rightarrow u\bar{c} + W^+ + g \rightarrow u\bar{c} + u\bar{d} + u\bar{u}$$

$$\chi_{c1}^+(3872) \rightarrow D^- \pi^+ \pi^+ : \quad u\bar{f} \rightarrow u\bar{c} + W^+ + g \rightarrow u\bar{c} + u\bar{d} + d\bar{d}$$

$$\bar{B}^0 \rightarrow \chi_{c1}^-(3872) \pi^+ \text{ with } \chi_{c1}^- \text{ having h.c. decays}$$

LHCb has measured  $\bar{B}^0 \rightarrow D^+ \pi^- \pi^- \pi^+$

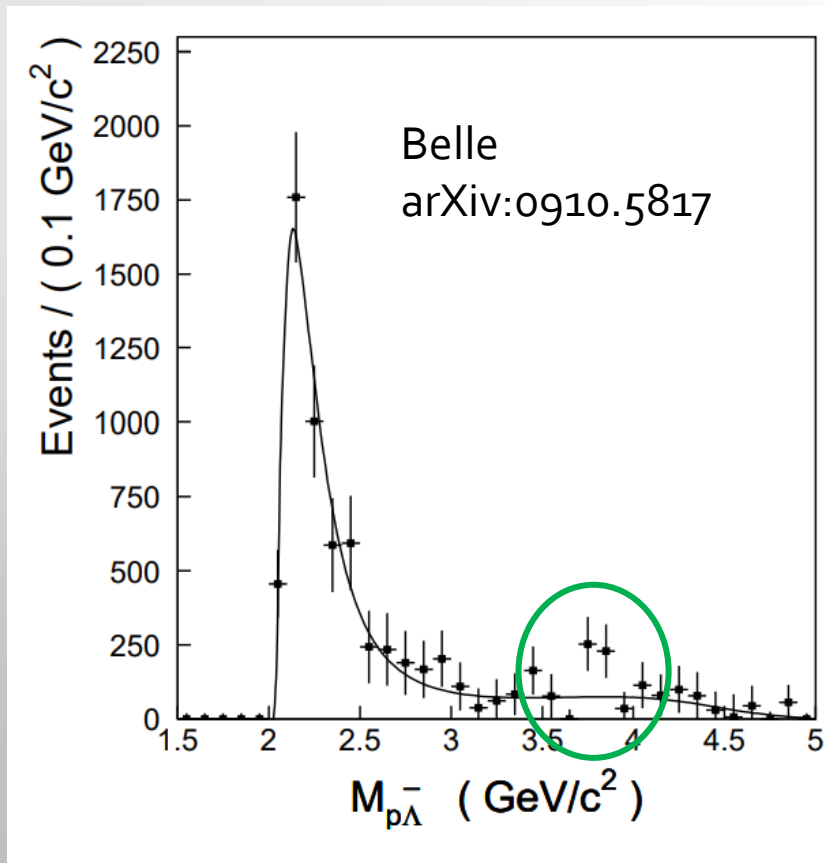
[1109.6831.pdf \(arxiv.org\)](https://arxiv.org/abs/1109.6831)

Check invariant mass of  $D^+ \pi^- \pi^-$  ?

# A predicted decay to $\chi_{c0}^+$

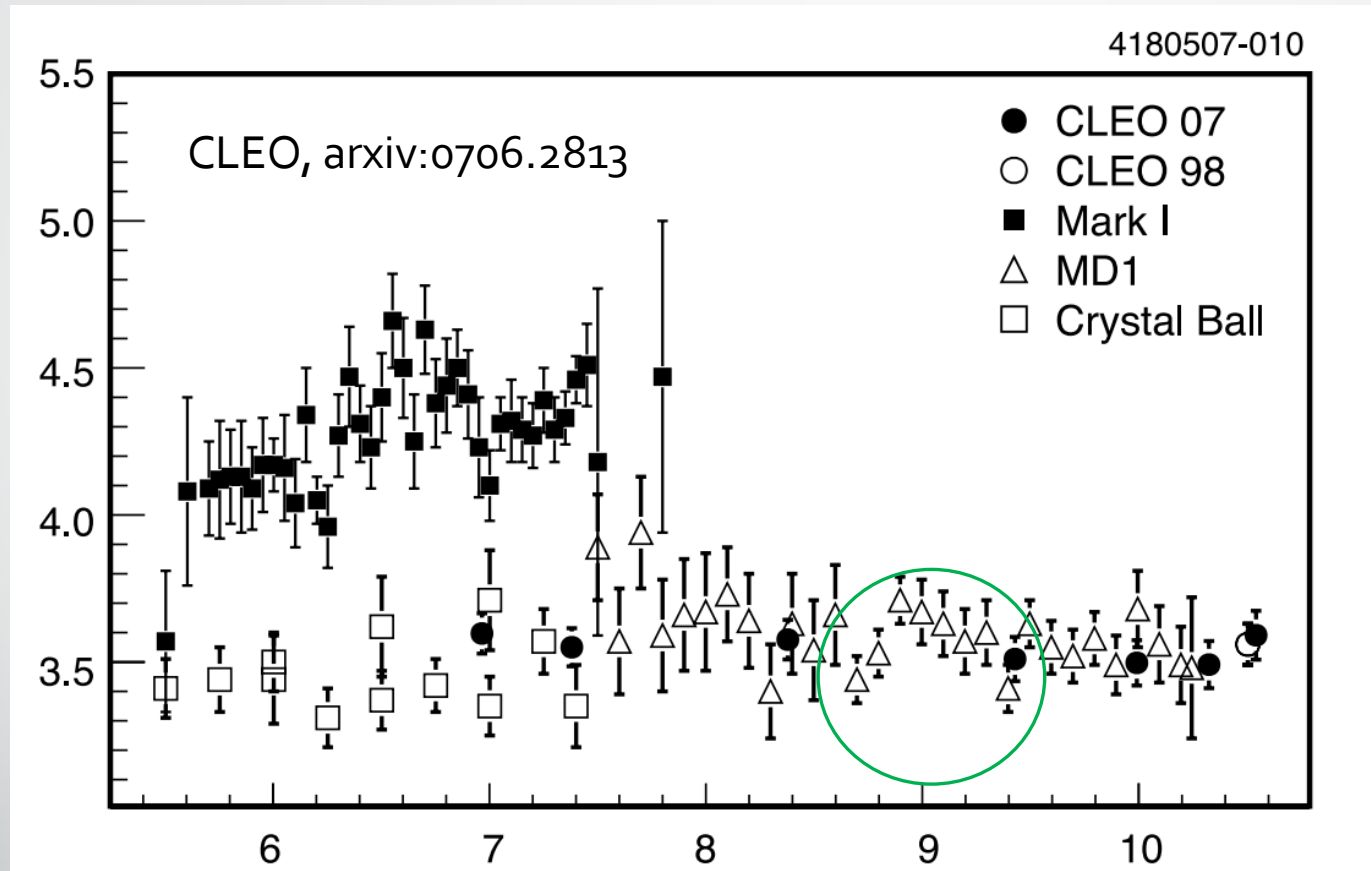
$$B^+ \rightarrow \chi_{c0}^+ (3860) \pi^+ \pi^- : u\bar{b} \rightarrow u\bar{f} + Z + g \rightarrow u\bar{f} + d\bar{d}u\bar{u}$$

$$\chi_{c0}^+ (3860) \rightarrow \bar{\Lambda} p : u\bar{f} \rightarrow u\bar{s} + Z + g \rightarrow u\bar{s} + d\bar{d}u\bar{u}$$




All mass combinations of  $\bar{\Lambda} p \pi^+ \pi^-$  were studied, and there was no mention of any structure in any other mass combination.

# Look for $f\bar{b}$ mesons in $e^+e^-$ ?

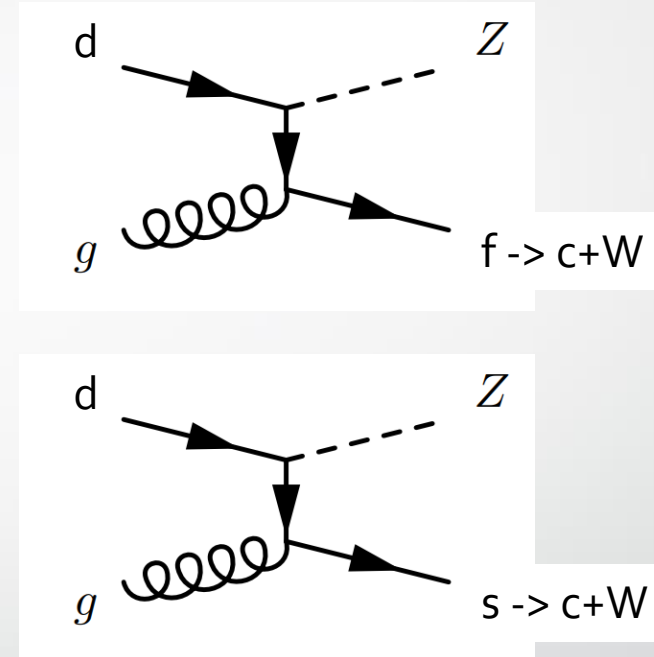
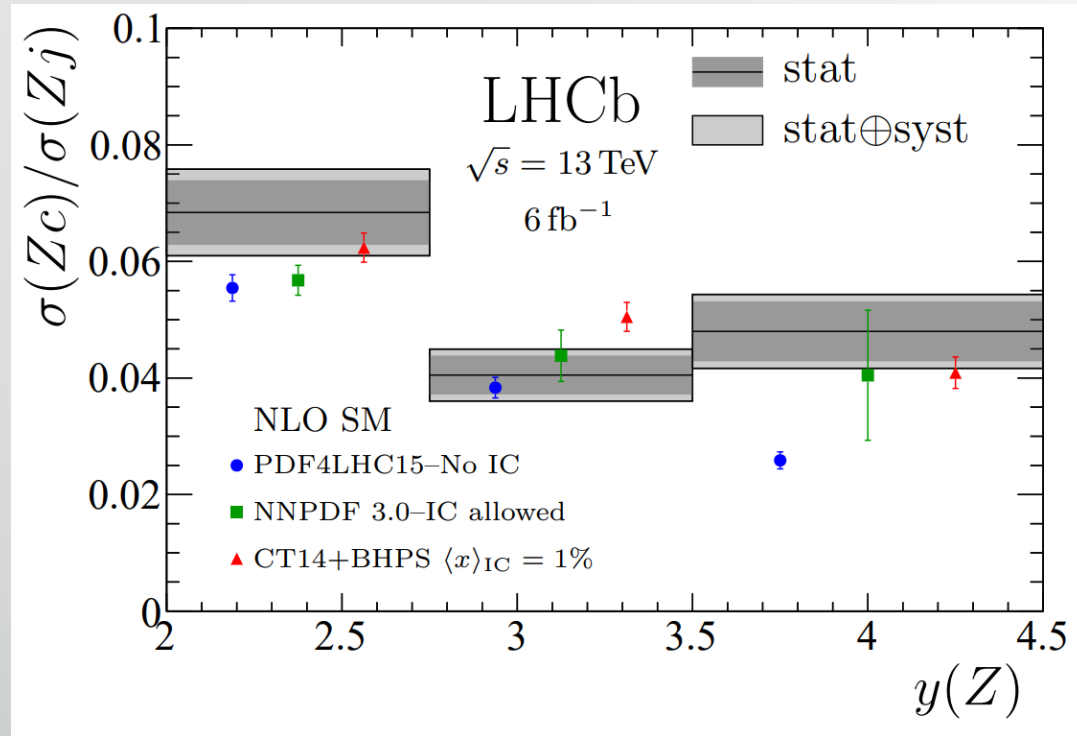


$$f\bar{b} (3^3 S_1 ?) \rightarrow X (3250) + B_1 (5721)$$



Alternative non-SM explanations  
for a few experiments

# Forward Z + c jet data



Data only reproduced by Standard Model with PDFs that have significant intrinsic charm

This model has two additional ways that valence d quarks can produce Z + c jet.  
 It is possible this model could reduce or eliminate the need for intrinsic charm.

Suggestion: Measure forward Z + c jet in heavy ion collisions where there are more neutrons. This model would predict much more than intrinsic charm models

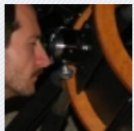
# Charm abundance is larger than most event generators



## W And Charm - Twice As Many As Predicted

By Tommaso Dorigo | August 15th 2010 08:14 AM | [Print](#) | [E-mail](#)

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Tommaso Dorigo

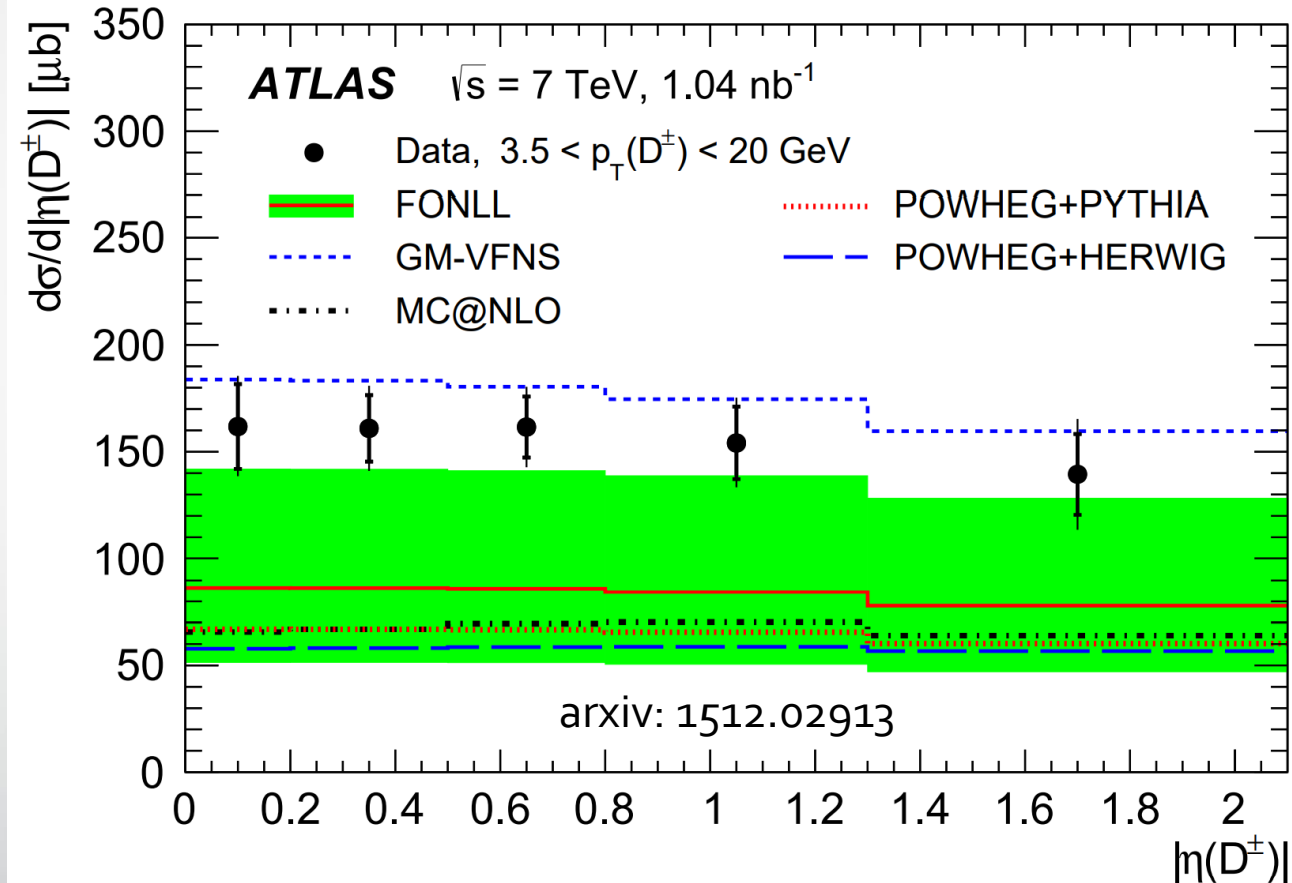
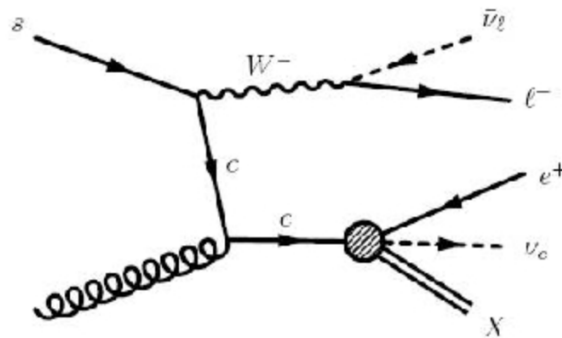
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W bosons have been thoroughly studied at the Tevatron collider. Discovered by the UA1 experiment at the CERN SppS proton-antiproton collider in 1984, these particles have since been produced also in electron-positron collisions at LEP II (in pairs), and recently at the Large Hadron Collider. But the CDF and DZERO experiments have some of the most precise measurements of the physics of these particles, thanks to their now very large datasets.

A question that has always caused

headaches in experimentalists and theorists concerning W production is how large a fraction of these particles is produced in association with heavy-flavour quarks -charm and bottom ones. These heavier brothers of up, down and strange quarks are not contained in the colliding protons and antiprotons in significant

amounts, and their observation together with a W boson in the final state of a collision is the result of a very distinct class of Feynman diagrams. For charm the typical process is the one shown on the right, where charm originates from a strange quark in the proton being transmuted by the weak interaction vertex which produces the W.



The model's FCNC mechanisms could help explain the excess of charm seen in high energy collisions with intrinsic charm or doubling the strange content of the proton

# Weak Radiative Hyperon Decay Puzzle

$$\Sigma^+ \rightarrow p\gamma$$

[2009.12552.pdf \(arxiv.org\)](#)

In hadronic field theory, the only allowed parity-violating interaction term is:

$$[\bar{\psi}_p i\sigma_{\mu\nu}\gamma_5\psi_{\Sigma^+} - \bar{\psi}_{\Sigma^+} i\sigma_{\mu\nu}\gamma_5\psi_p] q^\mu A^\nu$$

In the limit of flavor SU(3) being a good symmetry, this vanishes and these decays show little or no parity violation.

For baryon magnetic moments, flavor SU(3) has been shown to be a very good symmetry, but in  $\Sigma^+ \rightarrow p\gamma$  decays, parity is strongly violated

Data implies: Flavor SU(3) is a good symmetry for the EM interaction  
Flavor SU(3) is badly broken for the weak interaction.

In this model: the d and s quarks have the same electric charge  
d and s quarks have opposite chirality of weak interactions



# Papers on arXiv

[arxiv:2203.03007](https://arxiv.org/abs/2203.03007)

[arxiv:2112.04469](https://arxiv.org/abs/2112.04469)

[schapman@chapman.edu](mailto:schapman@chapman.edu)



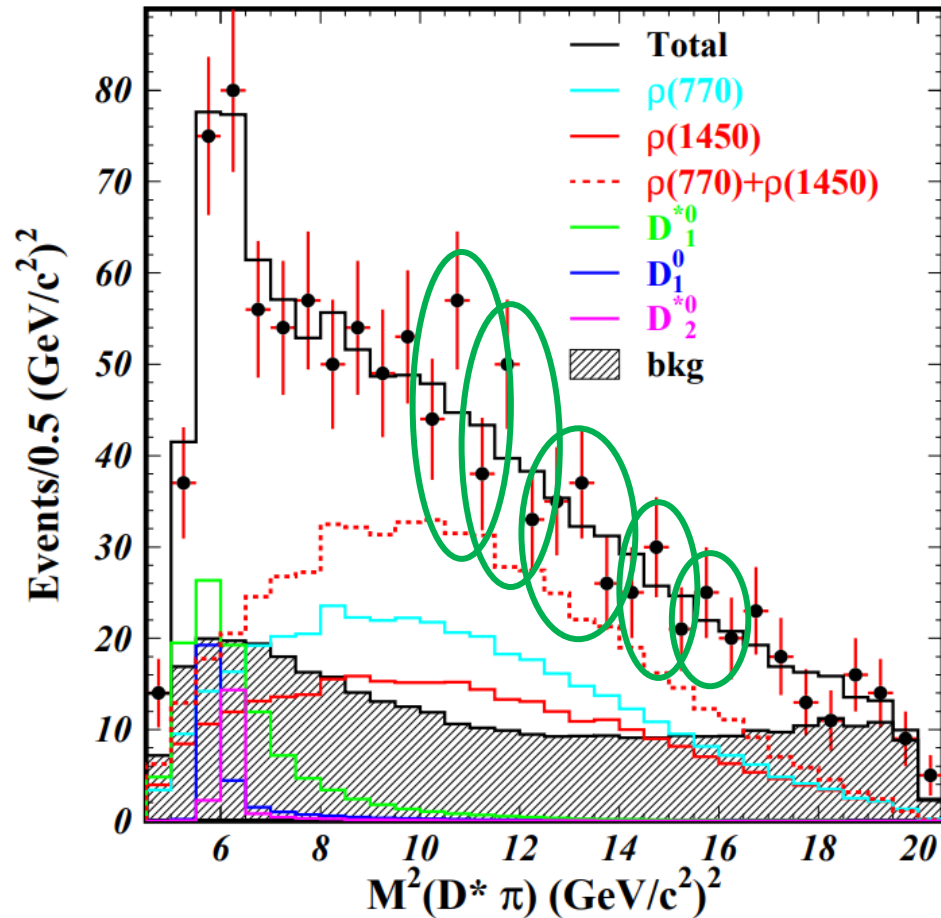


# Hints of Predicted $f$ quark decays

## Invariant mass data

# Hints of f meson resonances?

Belle, arxiv:1505.03362



$$\bar{B}^0 \rightarrow X^0 \omega: X^0 \rightarrow D^{*+} \pi^-$$

$f\bar{d}$

3250

3350

3860, the predicted  $1^3P_0$  meson

3985

$f\bar{s}$

3600  $1^1S_0$  meson?

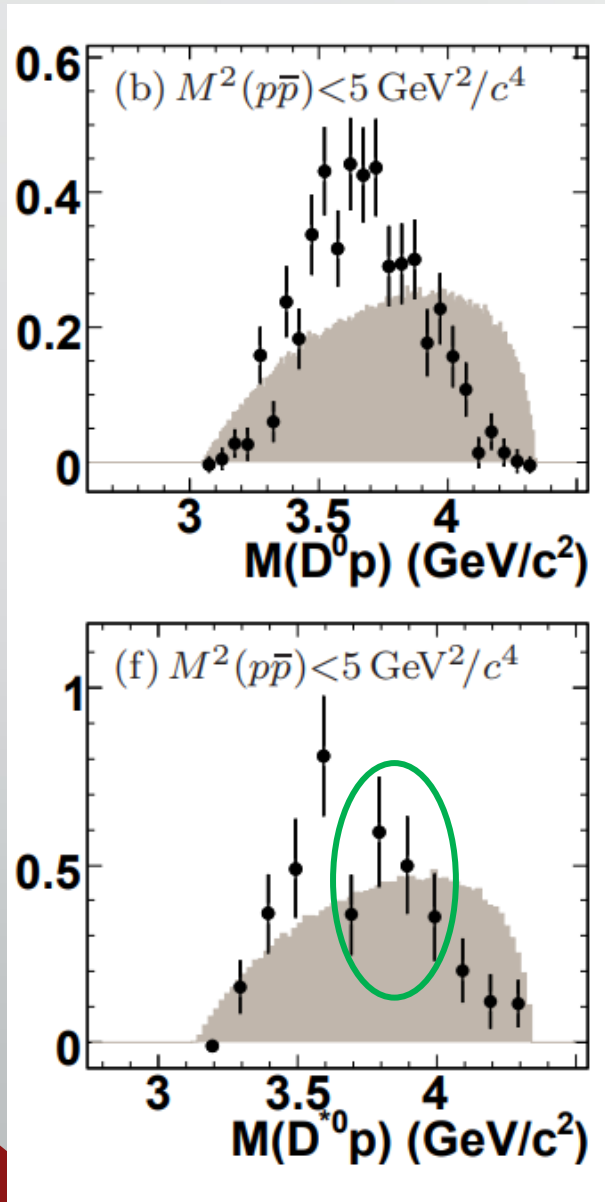
BaBar, arxiv:1111.4387

# Hint of predicted $P_c^+(3870)$ ?

$$\bar{B}^0 \rightarrow P_c^+ \bar{p} : P_c^+ \rightarrow D^{*0} p$$

A larger hint of 3870 resonance is seen in  $D^*$  events relative to  $D$  events

The decay  $\frac{1}{2}^+ \rightarrow 0^{-+} \frac{1}{2}^+$  is suppressed relative to  $\frac{1}{2}^+ \rightarrow 1^{--} \frac{1}{2}^+$

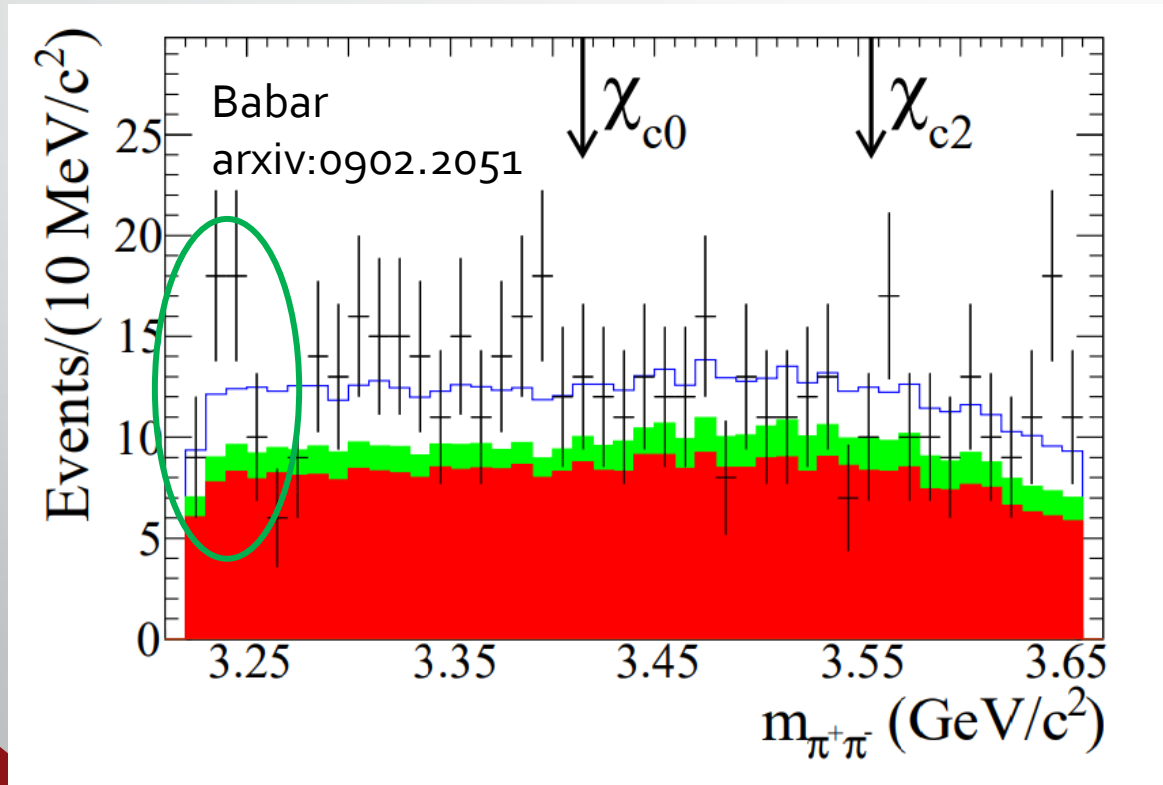


# Hint of 3250?

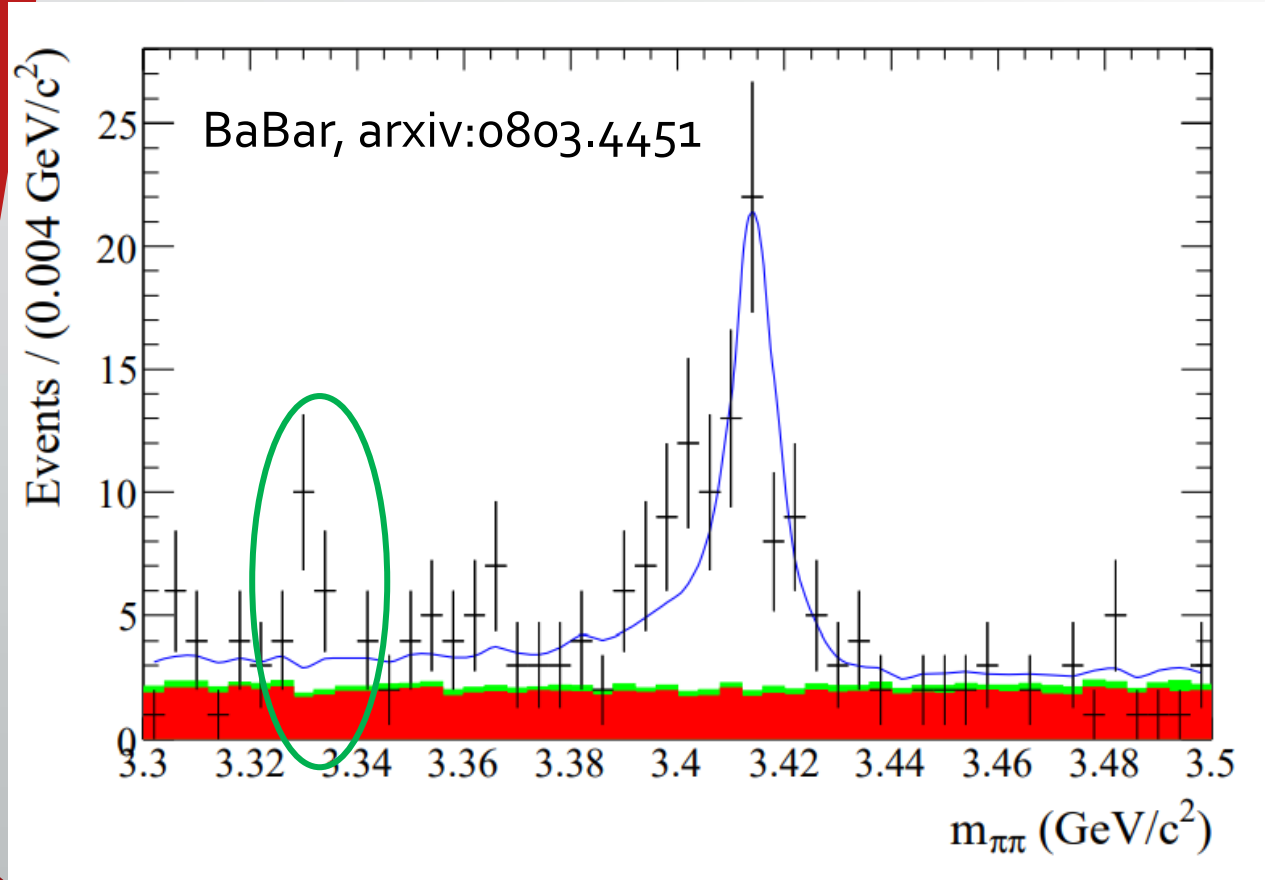
In this model  $X(3250)$  is mapped to the  $1^1S_0$   $J^{PC} = 0^{-+}$  meson of  $d\bar{f}$   
 $B^+ \rightarrow X(3250)\pi^+ : u\bar{b} \rightarrow u\bar{f} + Z \rightarrow u\bar{f} + d\bar{d} \rightarrow d\bar{f} + u\bar{d}$

$X(3250) \rightarrow \pi^+\pi^- : d\bar{f} \rightarrow d\bar{u} + W^+ \rightarrow d\bar{u} + u\bar{d}$

$$|V_{uf}| \sim 0.009$$



# Hint of 3350?



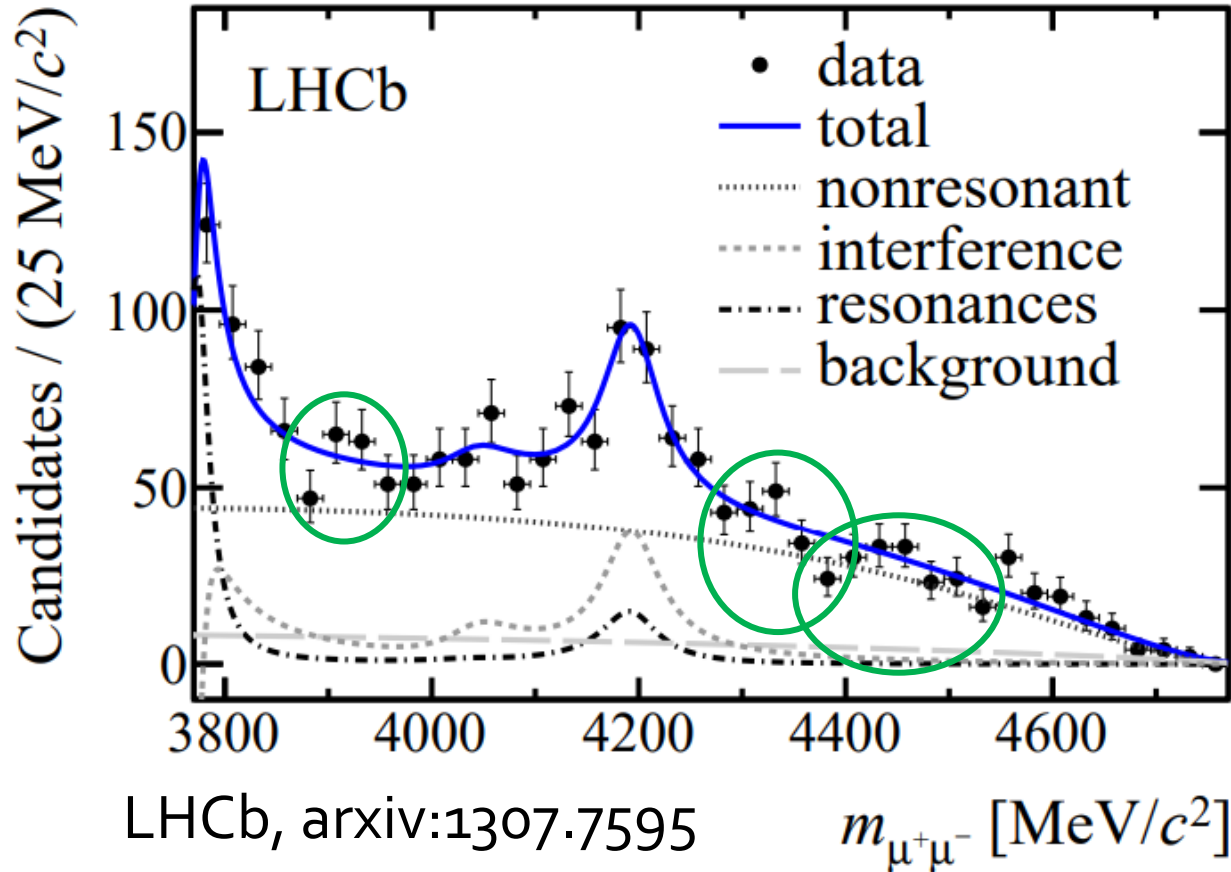
$$B^- \rightarrow XK^- : X \rightarrow \pi^+ \pi^-$$

Even larger invariant mass in K- pi+? Not shown in that range in the paper.

# Hints of $s\bar{f}$ mesons?

$$B^+ \rightarrow XK^+ : u\bar{b} \rightarrow u\bar{f} + Z \rightarrow u\bar{f} + s\bar{s} \rightarrow s\bar{f} + u\bar{s}$$

$$X \rightarrow \mu^+ \mu^- : s\bar{f} \rightarrow Z \rightarrow \mu^+ \mu^-$$



3960?

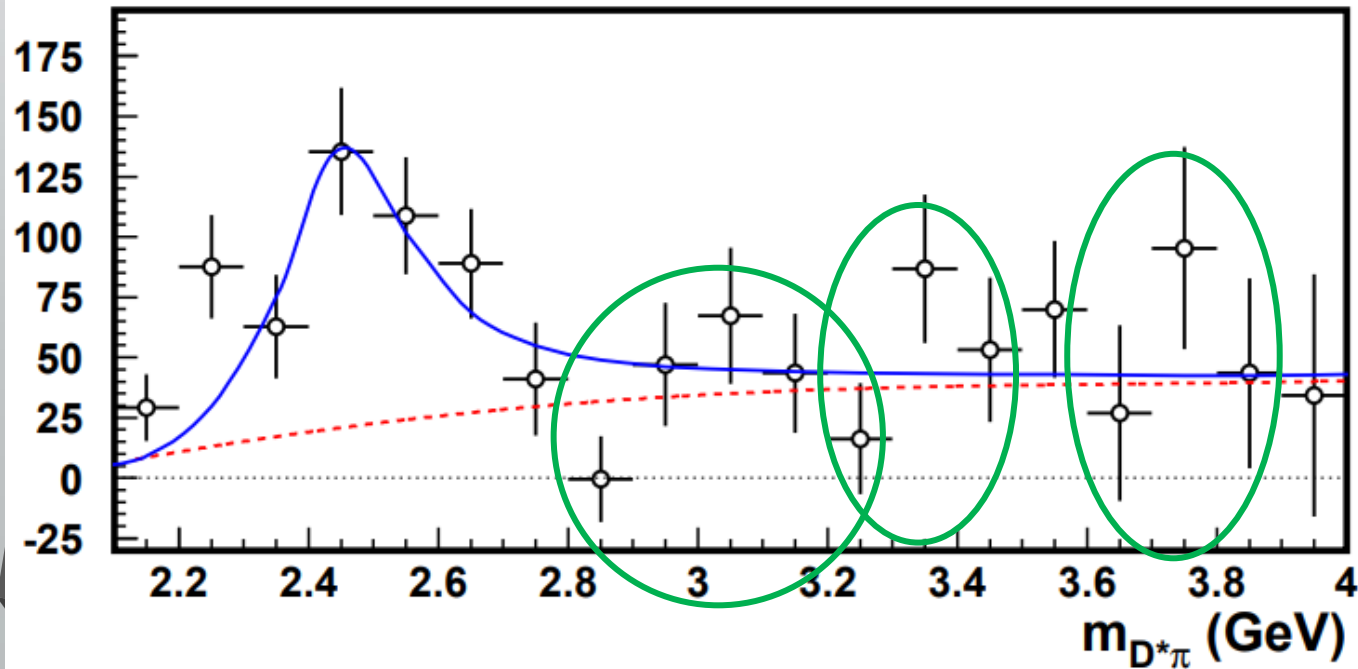
4360?

4407?

# Hints of 3250, 3350 and 3860?

BaBar, hep-ex/0604009

$$\bar{B}^0 \rightarrow D^{*+} \omega \pi^-$$

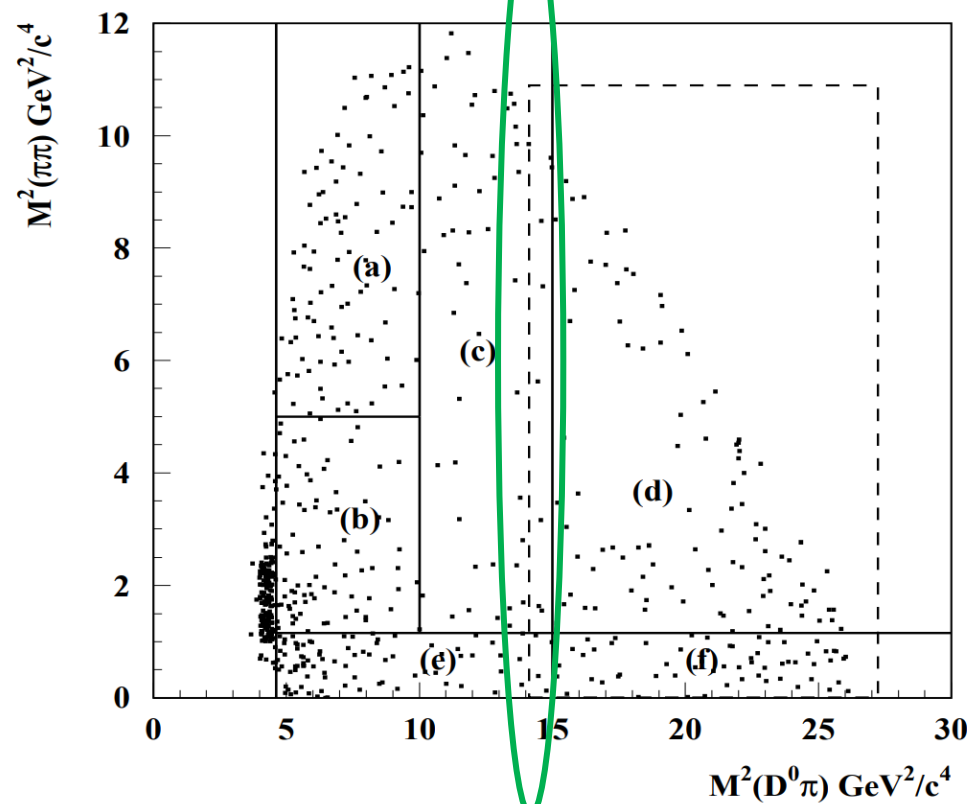


The peaks are consistent with

$$\bar{B}^0 \rightarrow X \omega : X \rightarrow D^{*+} \pi^- (\gamma)$$

for 3250, 3350, and 3860, but where 3250 and 3860 decays also include a soft photon

# Hint of charged $X(3860) 1^3 P_0$ meson?



Belle 2002, arxiv:hep-ex/0211022

looked at  $\bar{B}^0 \rightarrow D^0 \pi^+ \pi^-$  and also with  $D^{*0}$

A meson with an  $f$  quark cannot have positive charge, so cannot decay to  $D^0 \pi^+$

But  $f\bar{u} \rightarrow D^0 \pi^-$  is OK

Squinting, it looks like there might be more dots where needed for  $D^0 \pi^-$  to make a 3860 ... and maybe to make a 3350.

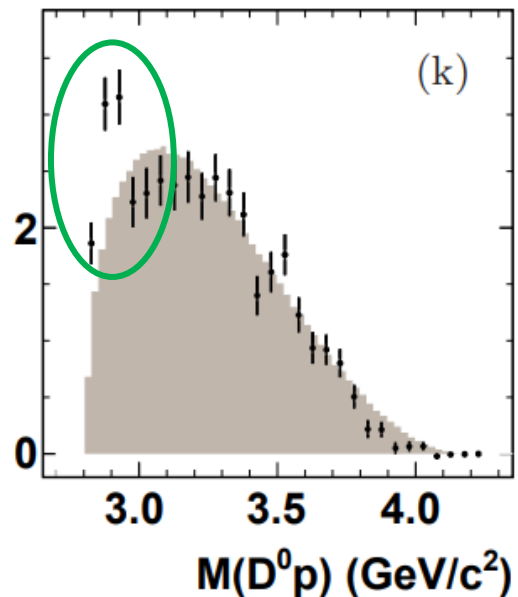
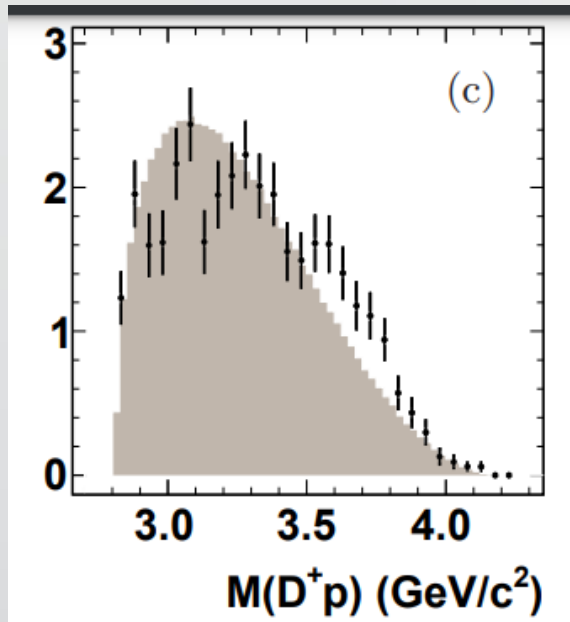




# Hints of Predicted $f$ quark decays

## Partial Invariant mass data

BaBar, arxiv:1111.4387



## Hint of $X(3860) 1^3 P_0$ state?

$$\bar{B}^0 \rightarrow D^+ p \bar{p} \pi^-$$

$$B^- \rightarrow X \pi^- : X \rightarrow D^0 p \bar{p}$$

A meson with an f cannot have positive charge, so cannot decay to  $D^+ p \bar{p}$

But  $f \bar{d} \rightarrow D^0 p \bar{p}$  is OK

A bump in the bottom but not in the top graph is consistent with the above  $X(3860)$  allowed decays

$D^0 p \bar{p}$  invariant mass would be interesting

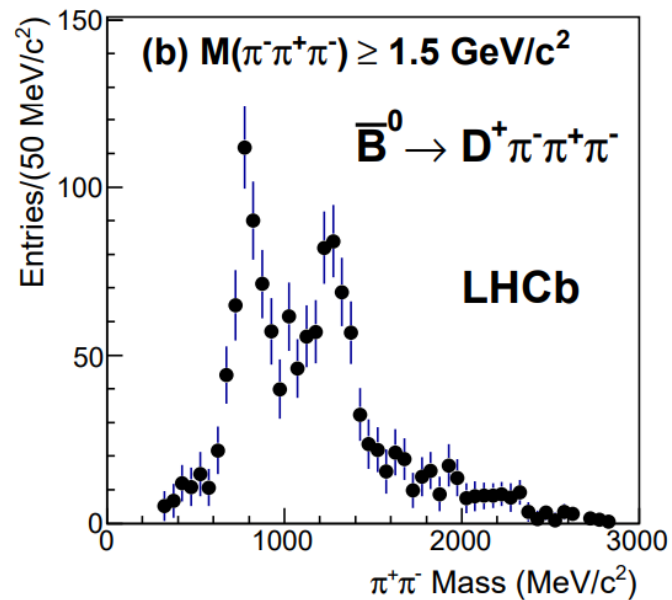
# Hint of $X(3860) 1^3 P_0$ state?

A meson with an f cannot have positive charge, so cannot decay to  $D^+ \pi^+ \pi^-$

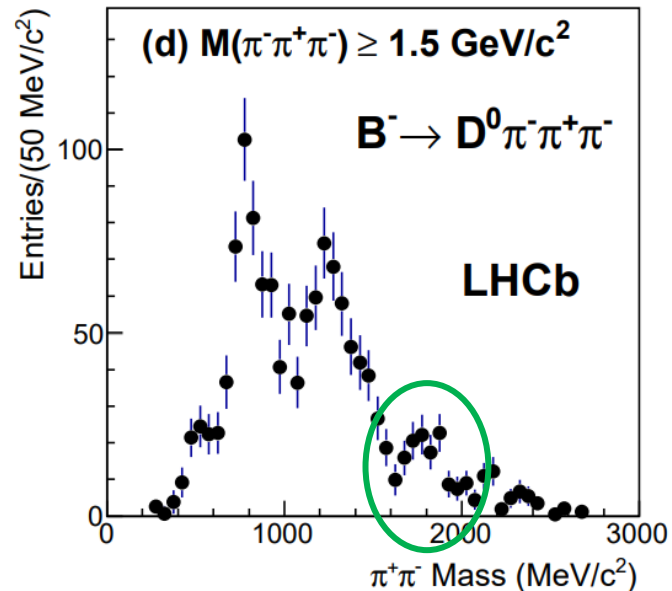
But  $f\bar{d} \rightarrow D^0 \pi^+ \pi^-$  is OK

A bump in the bottom but not in the top graph is consistent with the above  $X(3860)$  allowed decays

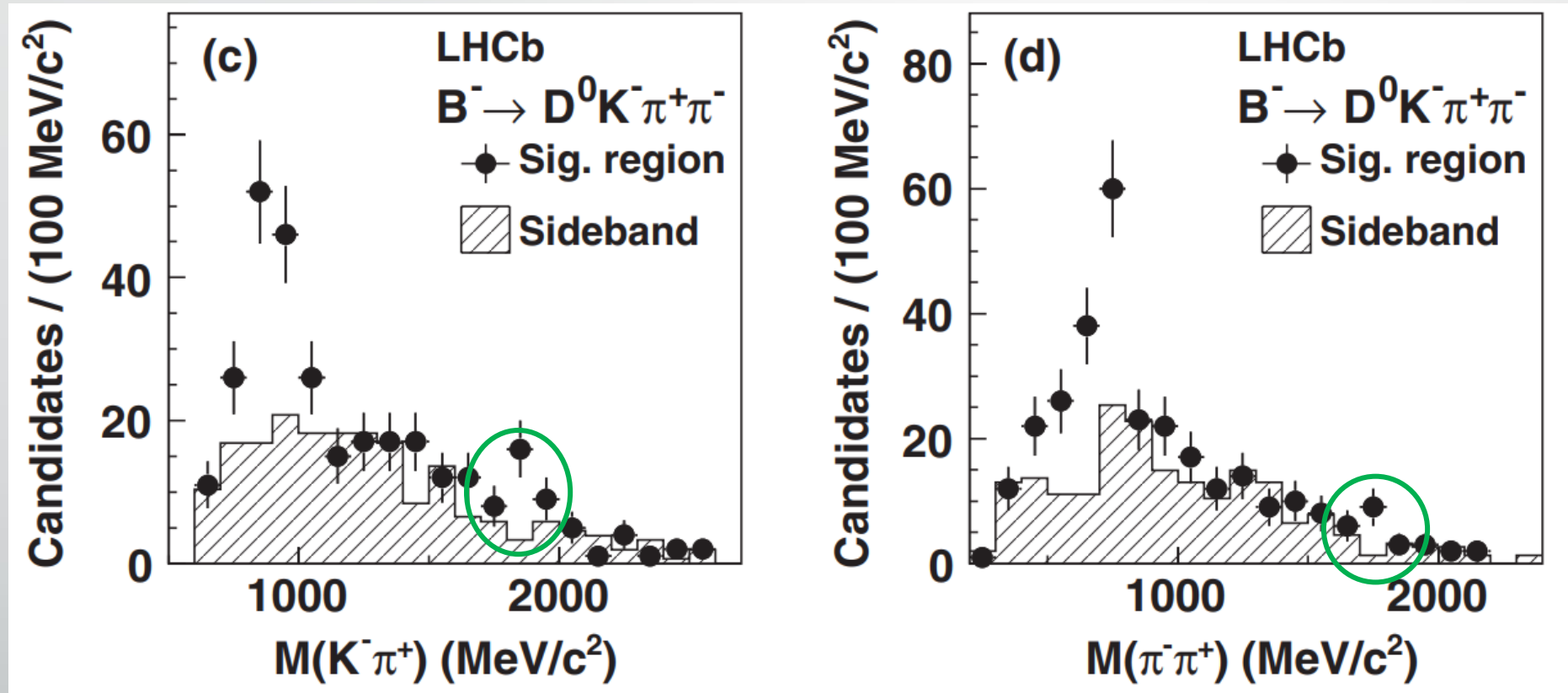
$D^0 \pi^+ \pi^-$  invariant mass would be interesting



LHCb, arxiv:1109.6831



# Hint of $X(3860) 1^3 P_0$ state?

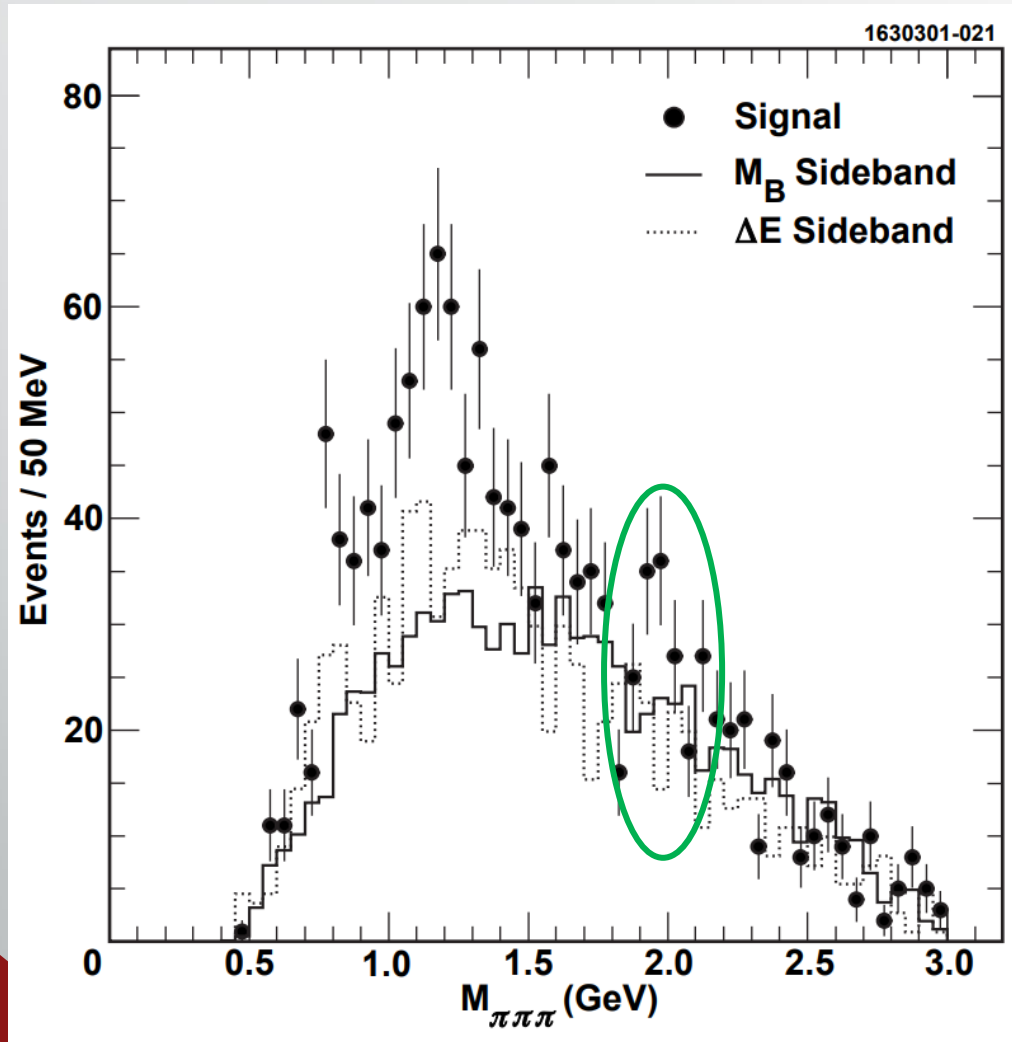


LHCb, 10.1103/PhysRevLett.108.161801

$D^0 K^- \pi^+$ ,  $D^0 \pi^- \pi^+$  invariant masses would be interesting

# Hint of 4020?

CLEO, hep-ex/0103021



$$B^- \rightarrow D^{*0} \omega \pi^-$$

The invariant mass is of the 3 pions that make the omega

The omega peak below 2 GeV could be consistent with

$$B^- \rightarrow X(4020) \pi^- : X(4020) \rightarrow D^{*0} \omega$$

$$D^{*0} \omega$$

invariant mass would be interesting