



# Triboson production in the SMEFT

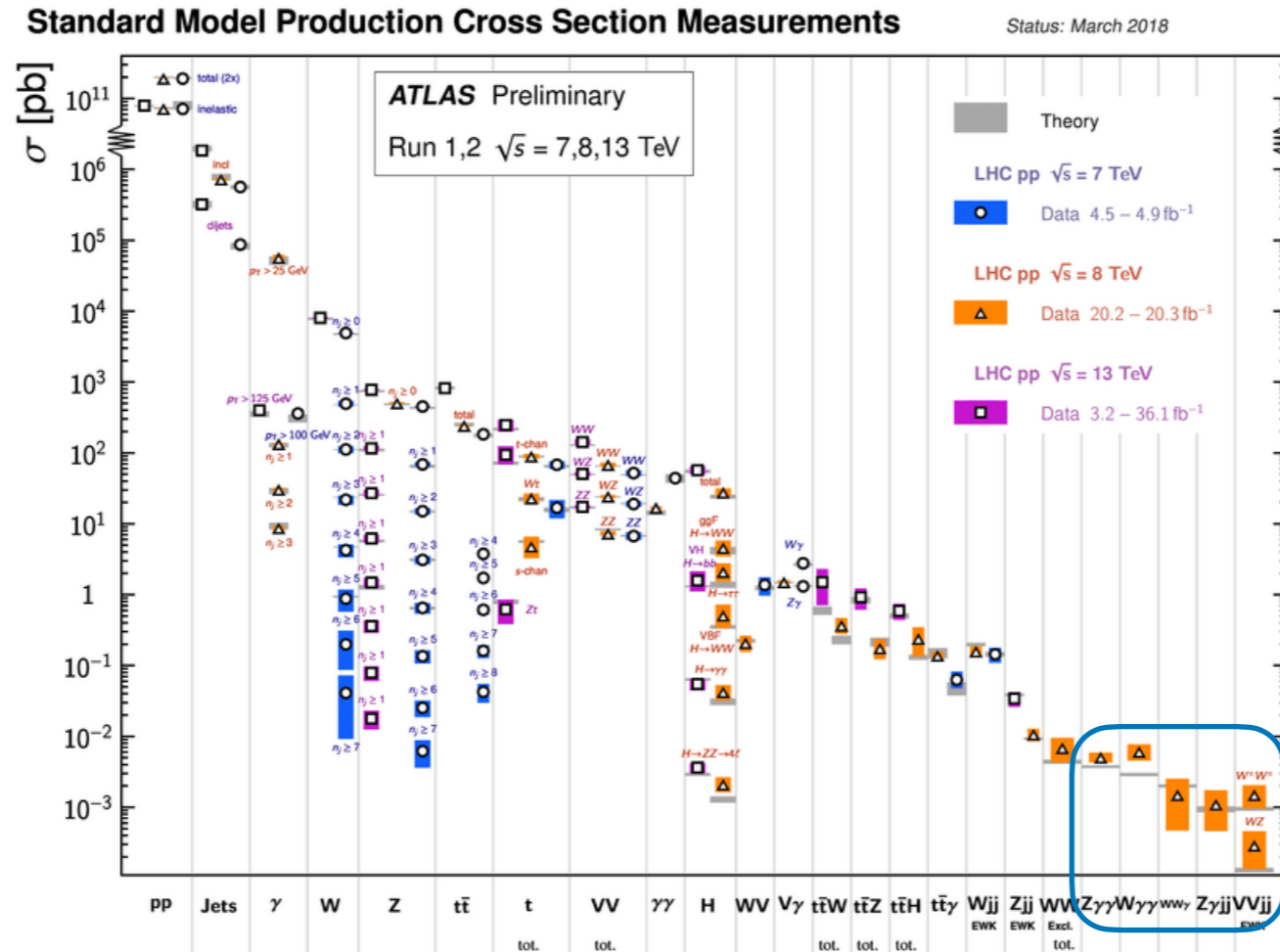
Based on a work with Gauthier Durieux, Ken Mimasu, Eleni Vryonidou

COMETA General meeting  
University of Bakırçay,  
29/02/24, Izmir, Turkey

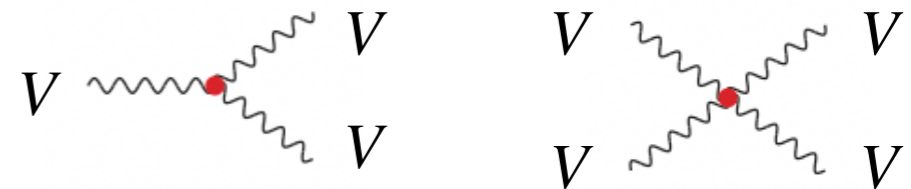
Eugenia Celada  
University of Manchester



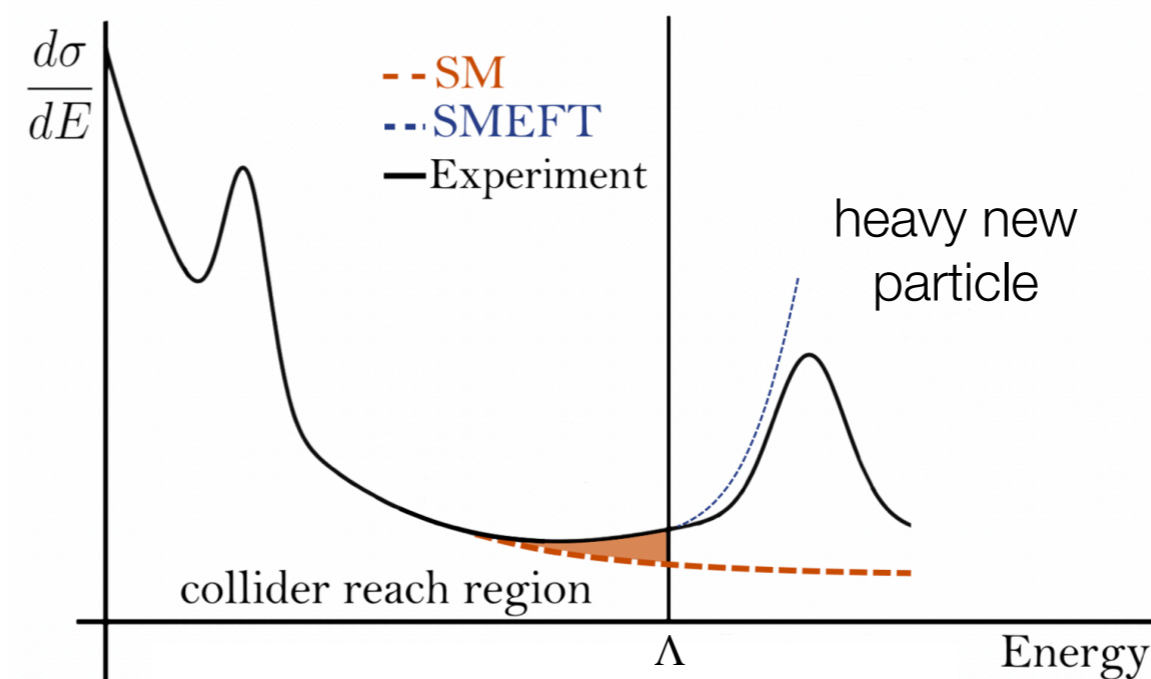
# Triboson production at the LHC



- Triboson have small cross sections, only accessible with LHC run 2
- Tree-level access to TGC and QGC



# The SMEFT



Original fig. by C. Severi, M. Thomas, E. Vryonidou

Dimension-6 operators Warsaw basis

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} O_i^{(6)} + \mathcal{O}(\Lambda^{-3})$$

$$\sigma \sim |\mathcal{M}_{\text{SM}}|^2 + \frac{1}{\Lambda^2} \left( \sum c^{(6)} 2\text{Re}[\mathcal{M}_{\text{SM}}^* \mathcal{M}_{\text{EFT}}^{(6)}] \right) + \frac{1}{\Lambda^4} \left( \sum c^{(6)} \mathcal{M}_{\text{EFT}}^{(6)} \right)^2$$

# EW operators in Warsaw basis

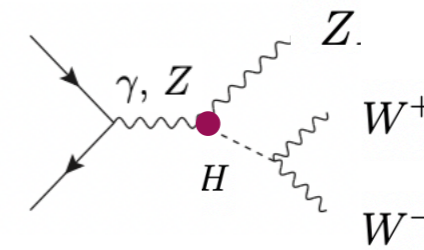
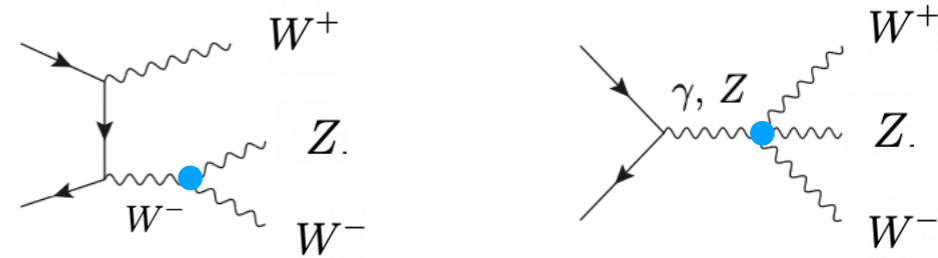
Operator	Definition
bosonic	
$\mathcal{O}_{\phi D}$	$(\phi^\dagger D^\mu \phi)^\dagger (\phi^\dagger D_\mu \phi)$
$\mathcal{O}_{\phi WB}$	$(\phi^\dagger \tau_I \phi) B^{\mu\nu} W_{\mu\nu}^I$
$\mathcal{O}_{WWW}$	$\epsilon_{IJK} W_{\mu\nu}^I W^{J,\nu\rho} W_{\rho}^{K,\mu}$
two-fermion	
$\mathcal{O}_{\phi q}^{(1)}$	$i(\phi^\dagger \overleftrightarrow{D}_\mu \phi)(\bar{q}\gamma^\mu q)$
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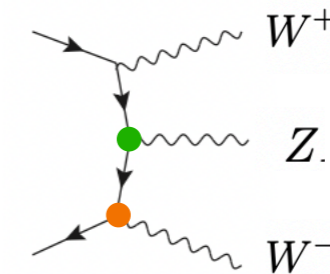
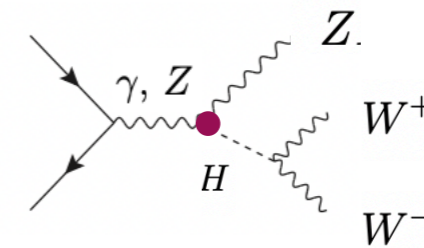
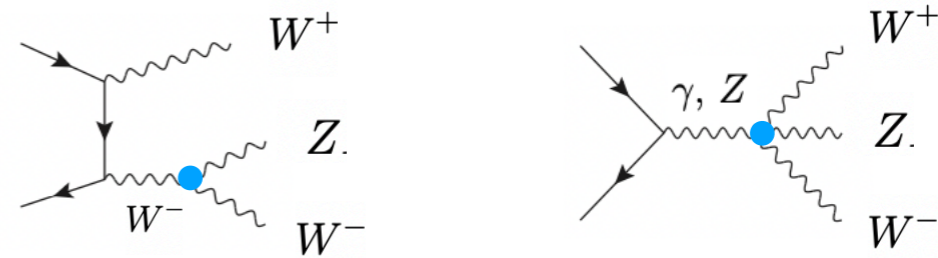
$$pp \rightarrow W^+ W^- Z$$



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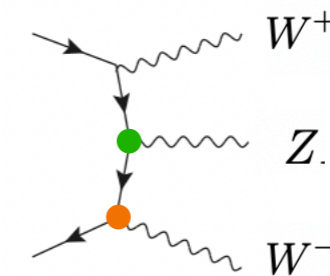
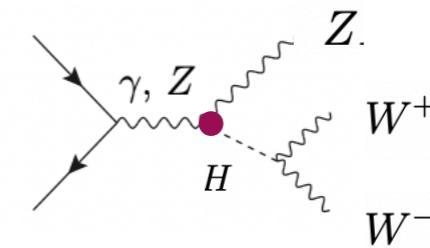
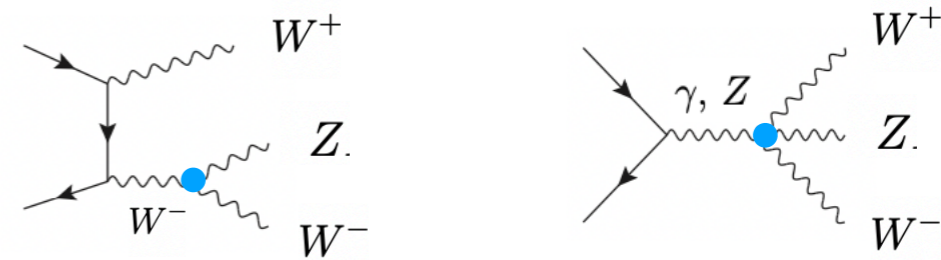
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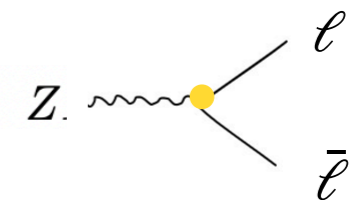
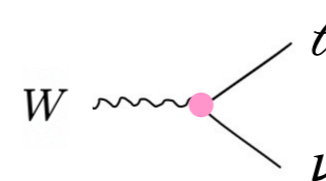
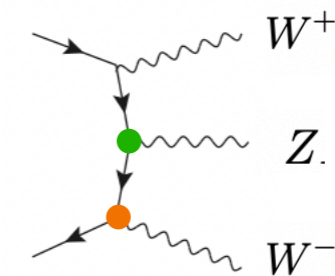
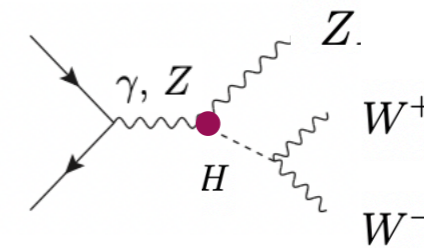
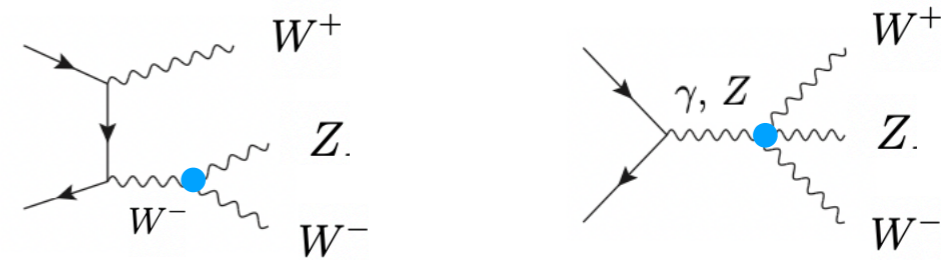
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$G_F$

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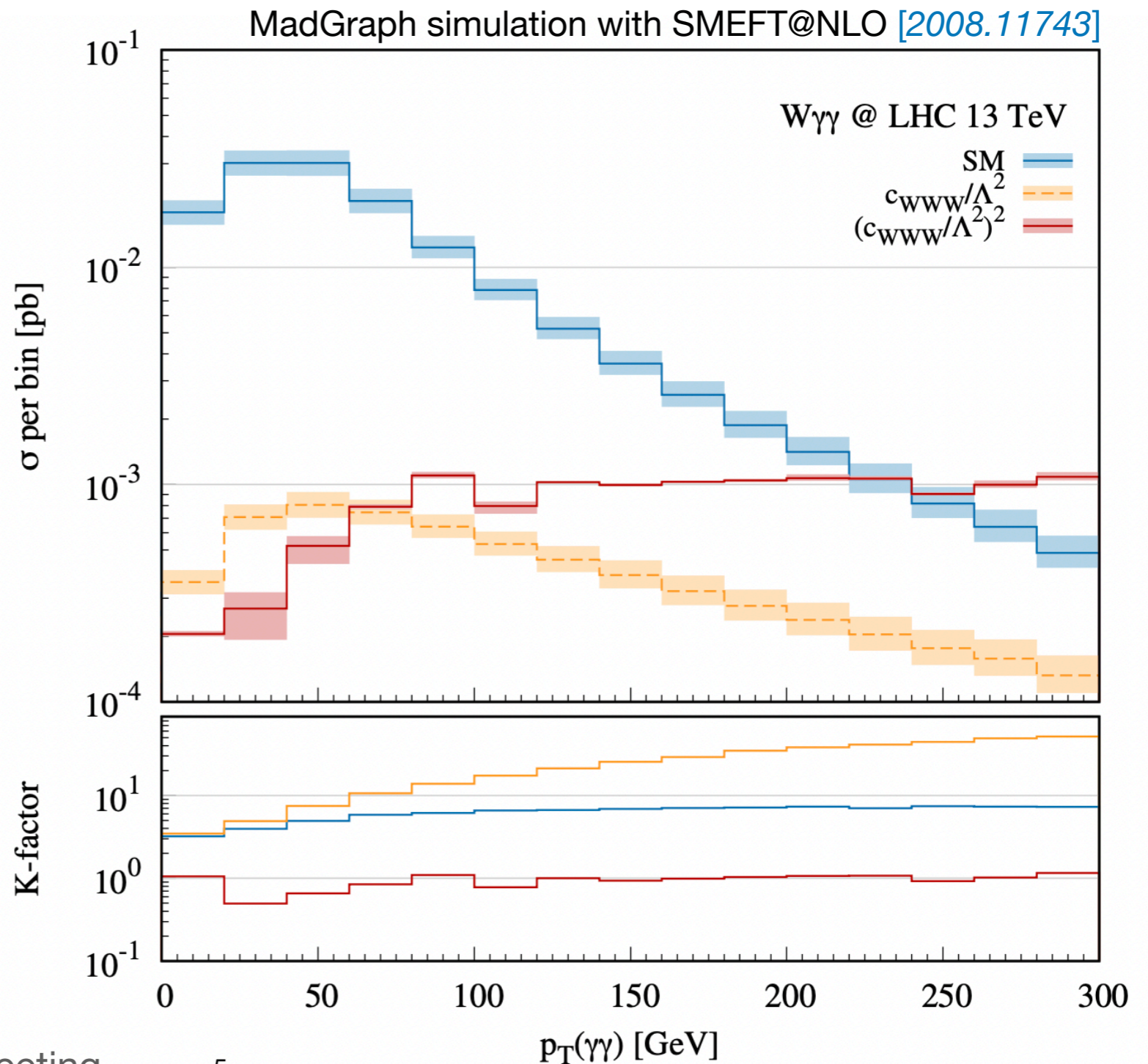


# Going NLO

NLO QCD corrections are large in triboson processes

$W\gamma\gamma$	
$\sigma(\text{fb})$	K-factor
$\sigma_{\text{SM}}$	4.84
$\sigma_{\phi D}$	4.86
$\sigma_{\phi D, \phi D}$	4.86
$\sigma_{\phi WB}$	4.70
$\sigma_{\phi WB, \phi WB}$	1.47
$\sigma_{WWW}$	12.24
$\sigma_{WWW, WWW}$	0.79
$\sigma_{\phi l^{(3)}}$	4.85
$\sigma_{\phi l^{(3)}, \phi l^{(3)}}$	4.85
$\sigma_{\phi q^{(3)}}$	4.80
$\sigma_{\phi q^{(3)}, \phi q^{(3)}}$	4.80
$\sigma_{ll}$	4.82
$\sigma_{ll, ll}$	4.82

$$K = \frac{\sigma_{\text{NLO}}}{\sigma_{\text{LO}}}$$



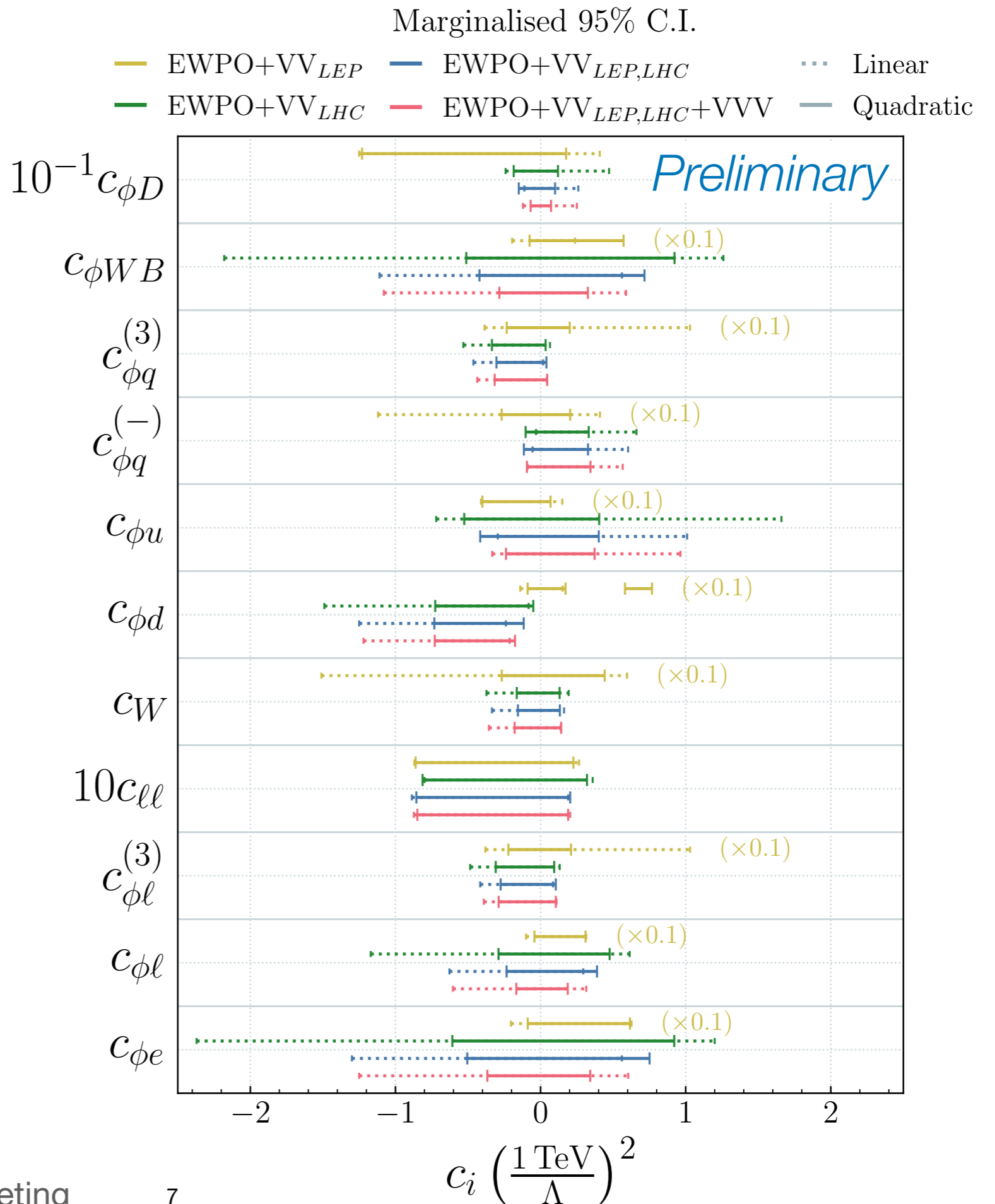
# Operators and observables

Operator	Definition	EWPOs	LEP $WW$	LHC $VV$	$VVV, VV\gamma, V\gamma\gamma$
bosonic					
$\mathcal{O}_{\phi D}$	$(\phi^\dagger D^\mu \phi)^\dagger (\phi^\dagger D_\mu \phi)$	✓	✓	✓	✓
$\mathcal{O}_{\phi WB}$	$(\phi^\dagger \tau_I \phi) B^{\mu\nu} W_{\mu\nu}^I$	✓	✓	✓	✓
$\mathcal{O}_{WWW}$	$\epsilon_{IJK} W_{\mu\nu}^I W^{J,\nu\rho} W_{\rho}^{K,\mu}$		✓	✓	✓
two-fermion					
$\mathcal{O}_{\phi q}^{(1)}$	$i(\phi^\dagger \overleftrightarrow{D}_\mu \phi)(\bar{q}\gamma^\mu q)$	✓		✓	✓
$\mathcal{O}_{\phi q}^{(3)}$	$i(\phi^\dagger \overleftrightarrow{D}_\mu \tau_I \phi)(\bar{q}\gamma^\mu \tau^I q)$	✓	✓	✓	✓
$\mathcal{O}_{\phi u}$	$i(\phi^\dagger \overleftrightarrow{D}_\mu \phi)(\bar{u}\gamma^\mu u)$	✓		✓	✓
$\mathcal{O}_{\phi d}$	$i(\phi^\dagger \overleftrightarrow{D}_\mu \phi)(\bar{d}\gamma^\mu d)$	✓		✓	✓
$\mathcal{O}_{\phi \ell}^{(1)}$	$i(\phi^\dagger \overleftrightarrow{D}_\mu \phi)(\bar{\ell}\gamma^\mu \ell)$	✓	✓	✓	✓
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$\mathcal{O}_{\phi e}$	$i(\phi^\dagger \overleftrightarrow{D}_\mu \phi)(\bar{e}\gamma^\mu e)$	✓	✓	✓	✓
four-fermion					
$\mathcal{O}_{\ell\ell}$	$(\bar{\ell}\gamma_\mu \ell)(\bar{\ell}\gamma^\mu \ell)$	✓	✓	✓	✓

# Fit results

- LHC W & VV appear to improve significantly the bounds from EWPOs & LEP W
- 50% improvement from VV on  $O_{\phi D}, O_{\phi WB}, O_{\phi \ell}, O_{\phi e}$
- Linear bounds are weaker than quadratic

Done with Fitmaker [\[2012.02779\]](#)





# Where do $WW$ & $VW$ help?

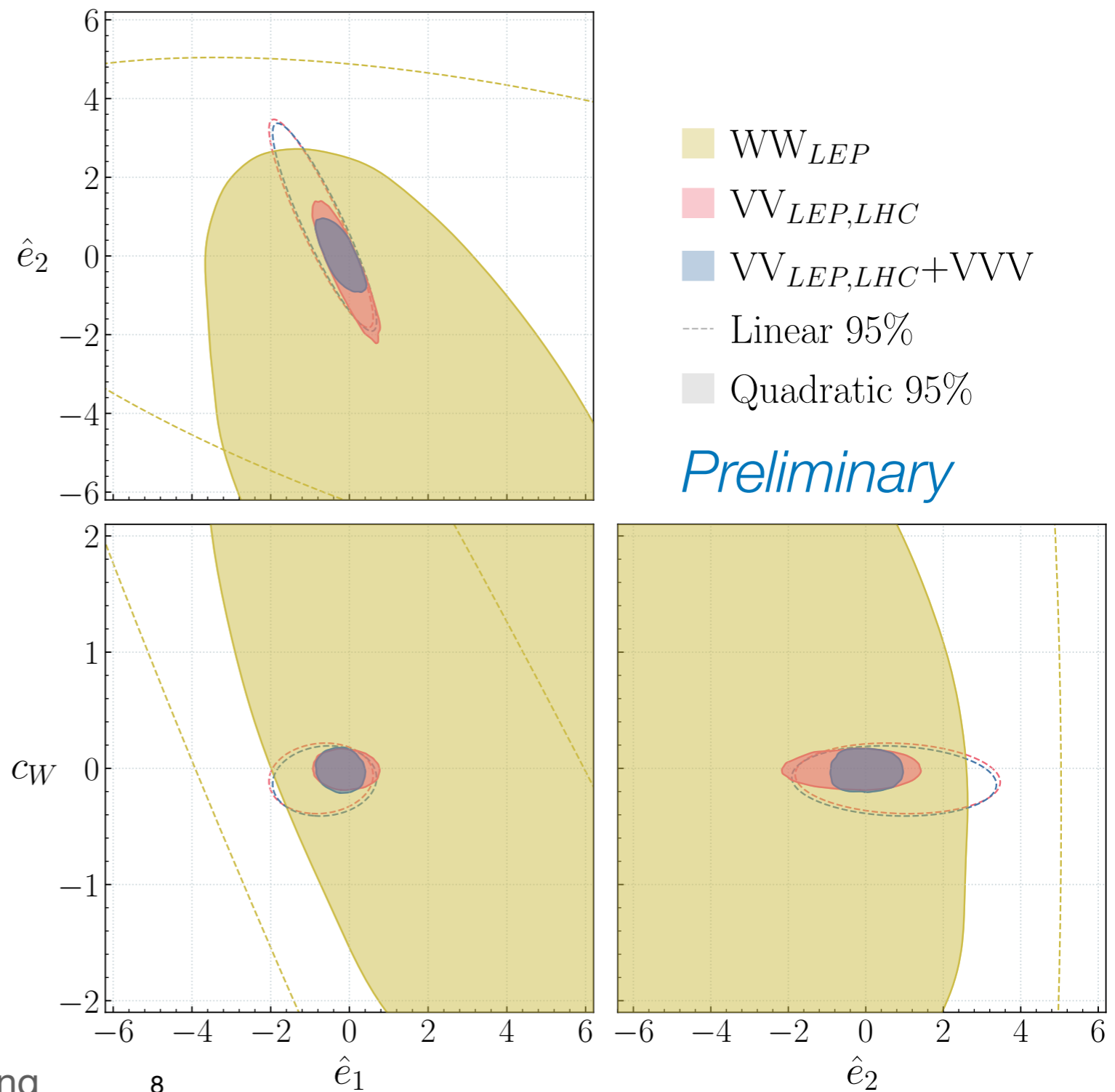
Three EWPOs unconstrained parameters:  $\hat{e}_1, \hat{e}_2, O_{WWW}$

[1701.06424]

- At order  $\mathcal{O}(\Lambda^{-2})$  triboson doesn't help
- $VW$  constrains the  $\hat{e}_1, \hat{e}_2$  space



- Quadratic corrections are important (also for LEP  $WW$ !)
- $VW$  improves in EWPOs flat directions

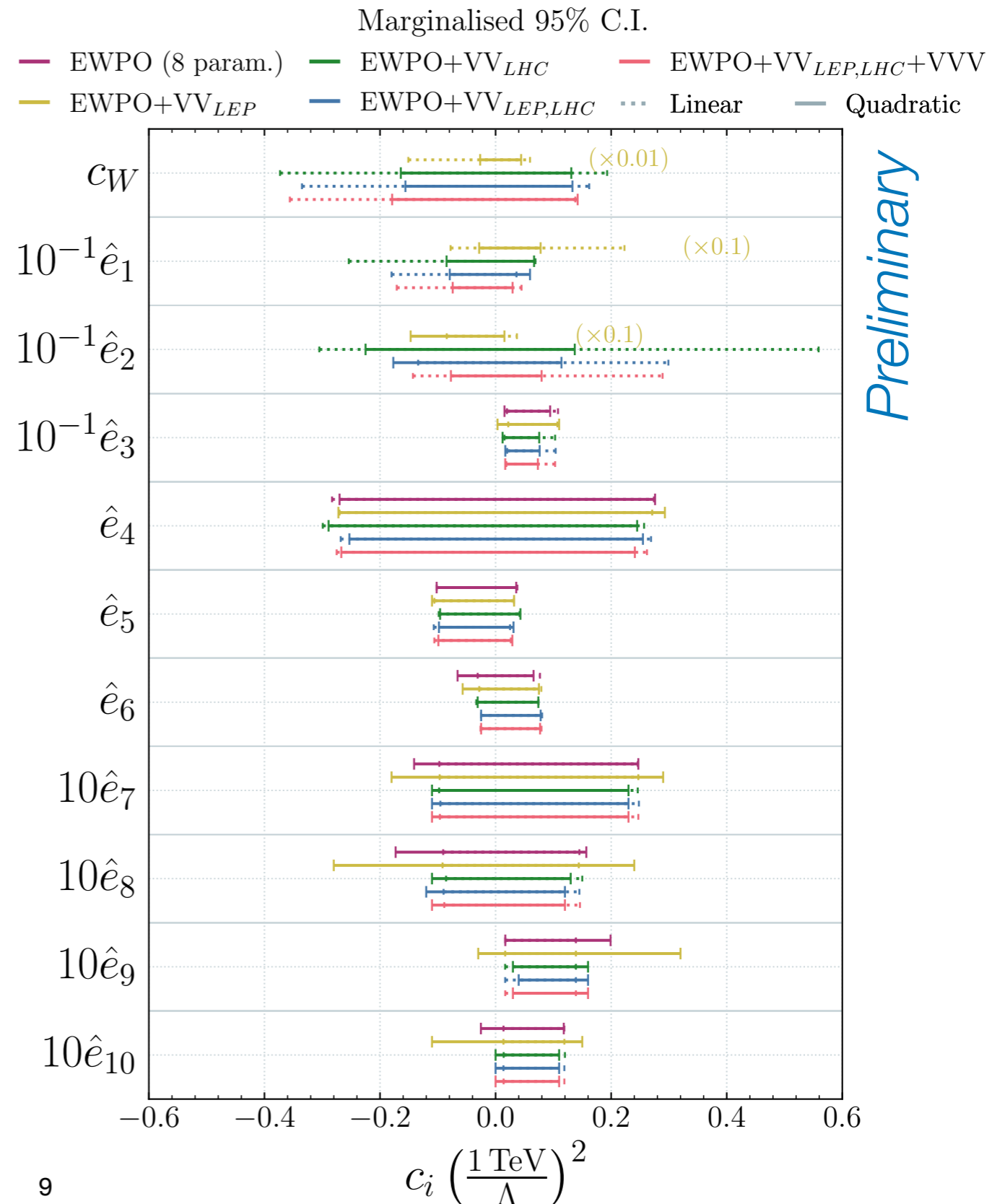




# What about the other directions?

Does multiboson help EWPOs in the directions orthogonal to  $\hat{e}_1, \hat{e}_2, O_{WWW}$ ?

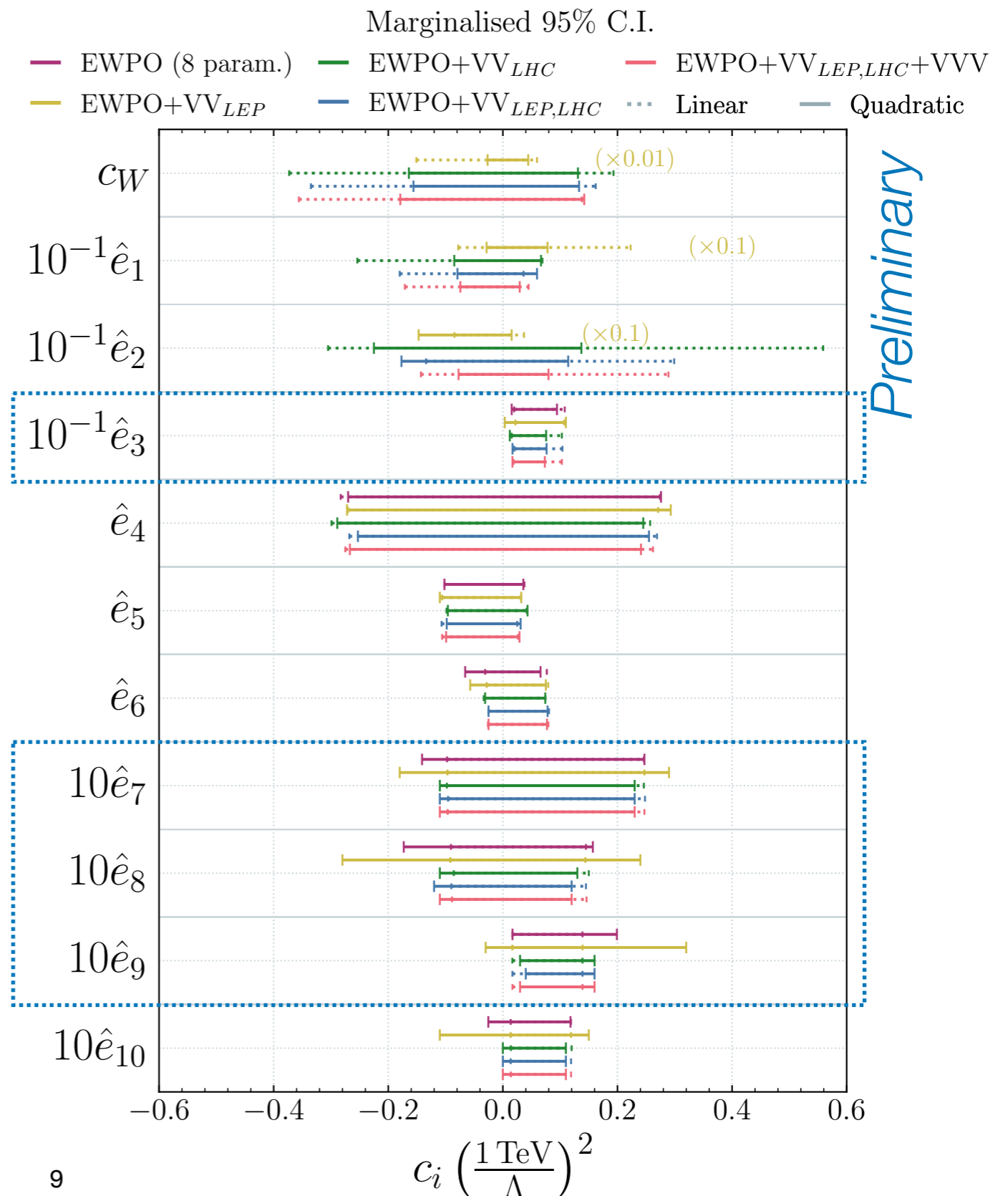
- in general, EWPOs constraints are dominant



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Does multiboson help EWPOs in the directions orthogonal to  $\hat{e}_1, \hat{e}_2, O_{WWW}$ ?

- in general, EWPOs constraints are dominant
- mild improvement from quadratics (even EWPOs) on some directions
- secondary minima in EWPOs+LEP lifted by LHC



# Conclusions

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- Triboson improves the bounds of up to a factor 2 compared to diboson in directions unconstrained by EWPOs
- Quadratic EFT contributions are sizeable for all the processes, from EWPO leading to secondary minima, to LEP diboson, and the LHC  $WW&VV$

# Backup

Constraints from multiboson in EWPOs flat directions space and in the orthogonal directions

